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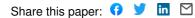
Emilien Azéma, Paul Sánchez, Daniel J. Scheeres

Institutions: University of Colorado Boulder

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## Scaling behavior of cohesive self-gravitating aggregates

Emilien Azéma,<sup>1,\*</sup> Paul Sánchez,<sup>2,†</sup> and Daniel J. Scheeres<sup>3,‡</sup>

<sup>1</sup>LMGC, Université Montpellier, CNRS, Montpellier, France

<sup>2</sup>Colorado Center for Astrodynamics Research, University of Colorado Boulder, 431 UCB, Boulder, Colorado 80309, USA
 <sup>3</sup>Aerospace Engineering Department, University of Colorado Boulder, 429 UCB, Boulder, Colorado 80309, USA

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By means of extensive three-dimensional contact dynamics simulations, we analyze the strength properties and microstructure of a granular asteroid, modeled as a self-gravitating cohesive granular aggregate composed of spherical particles, and subjected to diametrical compression tests. We show that, for a broad range of system parameters (shear rate, cohesive forces, asteroid diameter), the behavior can be described by a modified inertial number that incorporates interparticle cohesion and gravitational forces. At low inertial numbers, the behavior is ductile with a well-defined stress peak that scales with internal pressure with a prefactor  $\simeq 0.9$ . As the inertial number increases, both the prefactor and fluctuations around the mean increase, evidencing a dynamical crisis resulting from the destabilizing effect of particle inertia. From a micromechanical description of the contact and force networks, we propose a model that accounts for solid fraction, local stress, particle connectivity, and granular texture. In the limit of small inertial numbers, we find a very good agreement of the theoretical estimate of compressive strength, evidencing the major role of these structural parameters for the modeled aggregates.

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Understanding the physical and mechanical properties of small planetary bodies (comets, asteroids, small satellites) is essential not only for the study of the solar system and its origins, but also as a basis for future space exploration and mining missions [1]. Until very recently, it was assumed that the smallest of asteroids were monolithic rocks with a bare surface [2,3], but recent space missions and observations have established that not only their surfaces are covered by regolith, but that their internal structure is not monolithic either [4–6]. From these observations, the concept of a "granular asteroid" has progressively emerged [7,8].

Granular asteroids are naturally occurring gravitational aggregates (rubble piles) bound together by gravitational and possibly cohesive forces. They have large interior voids which allow them to support large plastic deformations [9]. Their macroscopic behavior and internal structure are still not well known and how to predict their mechanical strength, based on their microstructure and dynamics, is still an open question [1,10]. However, in view of their discrete nature, it is reasonable to use the theoretical concepts and numerical tools developed for granular media to study them.

After more than 15 years of research, the two following general features have been well established for granular materials (with some caveats for real geological systems [11]): (1) Their dynamical behavior, under various boundary conditions and confining geometries, is well captured through the so-called *inertial number I*, defined as the ratio of the particle relaxation time  $d\sqrt{\rho_0/p}$ , under a confining stress *p* and for a particle of density  $\rho_0$  and diameter *d*, to shear time  $t_s = \dot{\gamma}^{-1}$ 

imposed by the shear rate  $\dot{\gamma}$  [12–14], and (2) their strength properties result from the buildup of anisotropic structures at the particle scale which are induced by steric effects, force transmission, and friction mobilization [15–18].

In granular asteroids, long-range gravitational forces have to be taken into account along with cohesive forces and so, the generalization of these "granular concepts" is highly nontrivial. However, some recent simulations have started to include these effects; this has led researchers to propose new microscopic mechanisms [19,20] to explain the behavior of some of the small members of the near Earth object (NEO) population. For example, the fact that small asteroids (<150 m) can have a rotation rate higher than what a purely gravitational model would predict [21] can be attributed to local cohesion [22-24], where the smallest particles agglomerate in the form of a weak cohesive matrix that binds the larger particles [19,20]. Unfortunately, a general framework for the analysis of such bodies is still lacking. In this Rapid Communication we lay the foundation of a framework that unifies the I rheology with the overburden pressure given by self-gravity.

Considering that several forces come into play [19], it may be assumed that internal stresses result from two characteristic stresses acting on particles: (1) interparticle tensile strength  $\eta = f_0/d^2$ , where  $f_0$  is the cohesive force, and (2) interior stress given by  $\mathcal{P}(r) = 0.25\rho_0g_0D(1 - 4r^2/D^2)$ , with  $g_0 = GM_a/D^2$ , where G is the gravitational constant,  $M_a$  and D the total mass and diameter of the asteroid, and r the distance from the center, assuming a constant bulk density and spherical geometry. The pressure at the center is given by  $P_0 = \rho_0g_0D/4$  and can be used as a referential interior stress. Two different particle relaxation times can be built as  $t_\eta = d\sqrt{\rho_0/\eta}$ and  $t_{g_0} = d\sqrt{\rho_0/P_0}$ , leading, in combination with  $t_s$ , to the definition of two dimensionless numbers,  $I_\eta = \dot{\gamma} d\sqrt{\rho_0/\eta}$  and  $I_{g_0} = \dot{\gamma} d\sqrt{\rho_0/P_0}$ . From these two numbers, we can also find a

<sup>\*</sup>emilien.azema@umontpellier.fr

<sup>&</sup>lt;sup>†</sup>diego.sanchez-lana@colorado.edu

<sup>&</sup>lt;sup>‡</sup>daniel.scheeres@colorado.edu

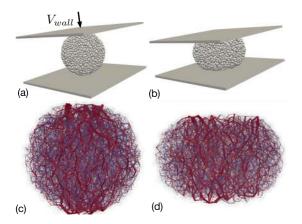


FIG. 1. Snapshots of a simulated granular asteroid under diametrical compression for (a)  $\varepsilon_h = 0$  and (b)  $\varepsilon_h = 0.1$ . Force chains are represented by lines joining the centers of two touching particles. Compressive forces in red, and tensile forces in blue.

modified version of the *Bond number*,  $\lambda = \eta/P_0 = (I_{g_0}/I_\eta)^2$ , which has been originally defined as the ratio of cohesive to gravitational forces [19,25]. We thus expect that the rheology of a granular asteroid will be governed by two of these three numbers.

By means of extensive three-dimensional (3D) contact dynamics simulations [26–29], we analyze the stress-strain behavior and microstructure of a granular asteroid, modeled as a cohesive granular agglomerate of spherical particles, subjected to vertical compression together with gravitational forces and for a broad range of parameters  $I_{\eta}$ ,  $I_{g_0}$ , and  $\eta$ . As we shall see, the peak strength, as well as the microstructure, scale with a modified inertial number that, in fact, combines two of these three numbers, so extending the *granular paradigm* to these ideal self-gravitating systems.

First, we build a large sample of 10 000 spherical particles under isotropic compression inside a box. The particles have a diameter  $d \in [0.6d_{\text{max}}, d_{\text{max}}]$ , with a uniform distribution per volume fraction. Friction, cohesion, and gravitational forces are not yet activated. Density  $\rho_0$  of the particles is fixed to 3200 kg/m<sup>3</sup>. We extract spherical agglomerates of diameter D from this sample comprising nearly  $N_p = 5000$  particles. In order to analyze the effect of aggregate size, four aggregates were built, with  $d_{\text{max}} \in [3, 6, 12, 18]$  m, so D is approximately [50, 100, 190, 375] m. Then, the friction coefficient is fixed to 0.4, cohesive forces, modeled as a constant reversible attractive force  $-f_0$  with a short-range action of the order of 0.01d, are activated. Gravitational forces are represented by the force  $F_{g_0} = \pi d^3 \rho_0 g_0 r / (6D)$  acting on the center of each particle at a distance r of the center of the aggregate and pointing towards it. The aggregates are then subjected to diametrical compression between two platens, with a prescribed velocity  $V_{\text{wall}} = \dot{\gamma} D$  [see Fig. 1(a)].  $I_n$  and  $\eta$  were varied between  $[5 \times 10^{-4}, 0.1]$  and  $[0.1 \text{ Pa}, \dots, 100 \text{ MPa}]$ , respectively. We performed 192 simulations for a broad range of combinations of these two parameters for both nongravitational and gravitational aggregates. When gravitational forces are considered,  $P_0$  increases with D, from ~0.48, to ~30 Pa.

During diametrical compression, the vertical stress  $\sigma_{zz}$  acting on an aggregate is given by  $4F/\pi D^2$ , where F is

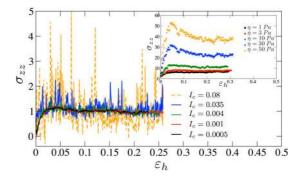


FIG. 2. Typical curve showing the vertical strength as a function of the cumulative vertical deformation for  $\eta = 1$  Pa, D = 50 m, and various values of  $I_{\eta}$  (gravitational forces are not activated). The inset show the same curve for  $I_c = 5 \times 10^{-5}$ ,  $\eta = \{1, 3, 10, 30, 50\}$  Pa for D = 190 m considering gravitational forces.

measured on the platen. It can be also calculated from the micromechanical expression of the stress tensor  $\sigma_{ij} = n_c \langle f_i^c \ell_j^c \rangle_c$ [27], where  $n_c = N_c / V$  with  $N_c$  the total number of contacts in the volume  $V = \pi D^3/6$ ; the average  $\langle \cdots \rangle_c$  is taken over the contacts *c* with contact force component  $f_i^c$  and branch vector component  $\ell_j^c$  (i.e., the vector joining the centroids of two contacting particles).

Figure 2 shows  $\sigma_{zz}$  as a function of the axial deformation  $\varepsilon_h$  for  $\eta = 1$  Pa, D = 50 m, and different values of  $I_{\eta}$ , and for  $I_{\eta} = 5 \times 10^{-4}$  with different values of  $\eta$  (inset).  $\varepsilon_h$  is the classical cumulative vertical deformation defined as  $\Delta D/D$ , where  $\Delta D = D - D_t$  and  $D_t$  the height of the wall at the time t. As a general observation, at small  $I_{\eta}$  values, the stress-strain curve is well defined and has very small deviations around the mean. The stress increases to a peak value at small strain  $(\approx 2\%)$  before relaxing to a constant plateau (plastic behavior) at larger strain. Deformations are localized in the vertical plane of the aggregate, where compressive force chains are mainly vertical and tensile force chains lie horizontally [see Fig. 1(b)]. This ductile behavior results from particle rearrangements, dissipation due to friction, and the short-range action of cohesive forces. As  $I_{\eta}$  increases, fluctuations in the stress-strain responses increase both in number and magnitude, revealing a dynamical crisis. Thus, in the following we consider only results for  $I_{\eta} < 0.035$  for nongravitational aggregates and  $I_{\eta} < 0.1$  for gravitational ones; the peak stress  $\sigma_{zz}^*$  is defined as an average stress around a deformation of 2%.

In the absence of gravitational forces, we naturally expect  $\sigma_{zz}^*$  to scale with  $\eta$  since cohesion is homogeneously distributed in all contacts. This is well observed in Fig. 3(a) for a wide range of values of  $I_{\eta}$ ,  $\eta$ , and D. In contrast, when gravitational forces are active, the scaling with  $\eta$  is not verified [see Fig. 3(b)]. This is because the effect of gravity is to increase the local stresses acting on the particles, so that interparticle tensile strength and interior stresses become additive. We can thus postulate that the mean pressure is  $p = \eta + \alpha P_0$ , where  $\alpha$  is a weight parameter that represents the stress gradient produced by the radial variation of the gravitational field inside an aggregate. A similar approach has been used for the scaling of shear stresses in dense suspensions [30,31] and in cohesive granular flow [32], where the fluid or cohesive forces

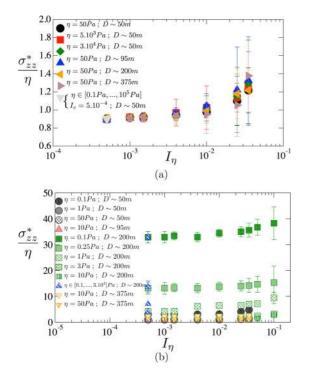


FIG. 3. Peak stress  $\sigma_{zz}^*$  normalized by the cohesive stress  $\eta$  as a function of  $I_{\eta}$  (a) without gravitational forces (i.e.,  $I_{g_0} = 0$ ), and (b) with gravitational forces (i.e.,  $I_{g_0} \neq 0$ ), in which only one or two parameters were varied.

and grain stresses are responsible for the effective friction angle. Accordingly, the inertial number can be rewritten as

$$I' = \dot{\gamma} d \sqrt{\frac{\rho_0}{\eta + \alpha P_0}} = \frac{I_{\eta}}{\sqrt{1 + \alpha \lambda^{-1}}} = \frac{I_{\eta} \cdot I_{g_0}}{\sqrt{I_{g_0}^2 + \alpha I_{\eta}^2}}.$$
 (1)

Figure 4 shows  $\sigma_{zz}^*$  normalized by  $(\eta + \alpha P_0)$  as a function of I', for  $\alpha = 0.48$ . We observe the collapse of all our simulation data with a prefactor  $\simeq 0.9$  for small I' values. This prefactor (and fluctuations around the mean) increases with I' to 1.3 in the range of values tested here, evidencing the dynamical crisis resulting from the destabilizing effect of particle inertia. It is thus crucial to explore the extent at

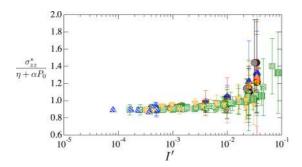


FIG. 4. Peak stress  $\sigma_{zz}^*$  normalized by additive stress  $p = \eta + \alpha P_0$  as a function of the modified inertial number *I'* for the raw data (color coding as in Fig. 3). Error bars represent the standard deviation around the peak state.

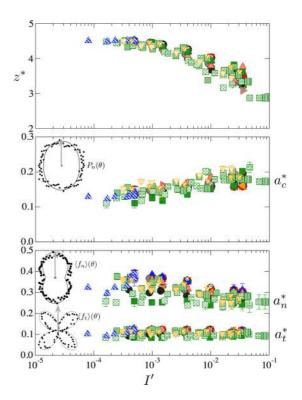


FIG. 5. Coordination number  $Z^*$  and anisotropy descriptors  $(a_c^*, a_n^*, a_l^*)$ , as a function of I' (the same color coding as in Fig. 3). The inset shows the polar diagrams of the angular distributions (black dot) together with harmonic approximations Eq. (2) (solid lines) for the smallest I'.

which the texture related to the contact and force network is controlled by I'.

At the lowest order, the contact network is characterized by the coordination number  $Z = 2N_c/N_p$  (average number of contacts per particle). Much more accurately, the anisotropy of the contact network, evidenced in Fig. 1(b) through a typical representation of forces, is characterized by the probability density functions  $P(\mathbf{n})$ ,  $\langle f_n \rangle(\mathbf{n})$ , and  $\langle f_t \rangle(\mathbf{n})$  of contact normal, mean normal force, and mean tangential force, respectively. In 3D, **n** is defined by the angles  $(\theta, \phi)$ , but given the spherical geometry of our aggregates, it may be argued that all these distributions are independent of the azimuthal angle  $\phi$ , so in the following, we will consider only the probability densities  $P_{\theta}(\theta)$ ,  $\langle f_n \rangle(\theta)$ , and  $\langle f_t \rangle(\theta)$  of the radial angles  $\theta$  (see the insets in Fig. 5). These distributions are  $\pi$  periodic and, at the peak state, an approximation based on spherical harmonics at leading terms (only those compatible with the symmetries) can capture their anisotropic behavior [17,33],

$$P_{n}(\theta) \simeq 1/(4\pi)\{1 + a_{c}^{*}[3\cos^{2}(\theta - \theta_{c}^{*}) - 1]\},$$
  

$$\langle f_{n}\rangle(\theta) \simeq \langle f_{n}\rangle\{1 + a_{n}^{*}[3\cos^{2}(\theta - \theta_{n}^{*}) - 1]\},$$
  

$$\langle f_{t}\rangle(\theta) \simeq -\langle f_{n}\rangle a_{t}^{*}\sin 2(\theta - \theta_{t}^{*}),$$
  
(2)

where  $\langle f_n \rangle$  is the mean normal force,  $a_c^*$ ,  $a_n^*$ , and  $a_t^*$  are anisotropy parameters, and  $\theta_c^* \simeq \theta_n^* \simeq \theta_t^*$  are the corresponding privileged directions which coincide with the major principal stress direction  $\theta_{\sigma} = \pi/2$  in the peak state.

The above microscopic descriptors, calculated in the peak state, are displayed in Fig. 5 as a function of I'. We obtain a very clear collapse of the data points (except maybe for  $a_n^*$ ), which provides factual evidence for a unified scaling of gravitational and nongravitational aggregates with the I' formalism. As is often observed,  $a_c^*$  and  $Z^*$  vary oppositely, so the reduction of  $Z^*$  with I' represents the loss of contact in the extension direction [34]. The fact that force chains are increasingly destabilized as I' increases is captured by the decrease of  $a_n^*$  together with the fact that  $a_t$ , which reflects friction mobilization ( $\langle |f_t| \rangle / \langle f_n \rangle \propto a_t$  [17]), remains constant.

Now, let us remark that the stress tensor can be rewritten as an integral as follows [17,33],

$$\sigma_{ij} = n_c \int \int \int f_{\alpha} \ell_{\beta} P_{\ell f n} df d\ell dn, \qquad (3)$$

where  $P_{\ell fn}$  is the joint probability density of forces and branch vectors  $\ell = \ell n$ . Neglecting the force-contact correlations (which is numerically always verified), *P* can be split as  $P_{\ell fn} = P_{\ell}(\ell)P_f(f)P_n(n)$ . Integrating over *f* and  $\ell$  and considering the normal and tangential components of the forces, we get the following relation [15,17],

$$\sigma_{ij} = n_c \ell_0 \int_{\Omega} [\langle f_n \rangle(\boldsymbol{n}) n_i + \langle f_t \rangle(\boldsymbol{n}) t_i] P(\boldsymbol{n}) n_j d\boldsymbol{n}, \quad (4)$$

where  $\Omega$  is the angular domain of integration, and  $\langle \ell \rangle = \ell_0 \simeq d$  (because of the weak size span [35,36]). Moreover, it is easy to show that  $n_c$  is related to both Z and the solid fraction  $v = N_p \pi d^3/(6V)$  by  $n_c = 3Zv/(\pi d^3)$  [37]. We assume also that an extreme value of the normal force  $f_n^*$  is  $(\eta + \alpha P_0)d^2$ , on the basis that at the peak state all contacts in a given direction are mobilized in extension and have reached their limit value. In the absence of gravitational forces this means that  $f_n^* = f_0$ . A similar hypothesis, which provided a correct estimate of the strength in direct shearing, was used by Richefeu *et al.* [37] for wet granular media.

Thus, introducing the expressions of  $n_c$  and  $f_n^*$  in Eq. (3) together with Eq. (2), we may introduce a theoretical peak strength for a gravitational aggregate as

$$\frac{\sigma_{zz}^{\text{theoric}}}{\eta + \alpha P_0} = \frac{Z^* \nu^*}{\pi} \left( 1 + \frac{4}{5} a_c^* a_n^* \right), \tag{5}$$

where  $v^*$  is the solid fraction at the peak state. Note that this equation can be reduced to the well-known "first-order" Rumpf's formula for  $P_0 = 0$  [38,39]. For all our simulated data we have  $v^* \simeq 0.60$ . The theoretical values of  $\sigma_{zz}^{\text{theoric}}$ are shown in Fig. 6 as a function of I', together with those obtained directly from the stress tensor. We observe that Eq. (5) approximates very well the peak stress at low I' values, which explains the microscopic origin of the value of  $\simeq 0.90$ , but underestimates it at larger values, where impulsive forces prevail, defying the hypothesis done on normal forces at the peak state. In the limit of small inertial numbers (i.e., for quasistatic deformation) the important parameters are related to the compactness (solid fraction and number of contacts) and, to a lesser extent, to the way in which the contacts and forces are distributed inside the aggregate. Equation (5)provides a clear evidence for the role of these structural parameters for a granular asteroid.

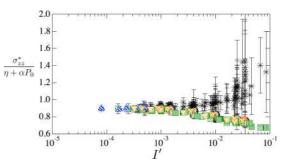


FIG. 6. Peak stress  $\sigma_{zz}^*$  normalized by additive stress  $p = \eta + \alpha P_0$  as a function of I' for the raw data (stars) (same as Fig. 4), together with the prediction given by Eq. (5) (color coding as in Fig. 3).

As explained above, understanding the physical and mechanical properties of small planetary bodies is an essential step to understand their formation and to plan present and future space missions. One of the outstanding questions in planetary sciences was the observation that, though most near Earth asteroids (NEAs) had a maximum spin period of  $\approx 2.2$  h [21], some of the small members of the population (<150 m) could reach spin periods of just a few minutes. This of course implied that these bodies had an amount of cohesive strength [23,24] that held them together beyond the gravitational limit; however, no explanation was given to the source of this strength. Prompted by this, Refs. [19,40] proposed that cohesive van der Waals forces among the small regolith and dust of an asteroid acted as a weak matrix that could hold the larger boulders in place and provide the cohesive strength necessary for the elevated spin rates that had been observed. The specifics of this were explored in Ref. [20], arriving at the conclusion that the strength of this matrix was inversely proportional to the average particle radius. This finding, or its principle, has been later used by others [41-43] in their own research. In spite of this, the study of the dynamics of cohesive granular asteroids has been limited to either specific asteroids or to bodies with specific sizes and cohesive strength [44].

To this moment, and even after obtaining a sample from asteroid Itokawa, little is known about the structural strength of small planetary bodies, and this was evidenced by the events of the Hayabusa mission to asteroid Itokawa and the Rosseta mission to comet 67P/Churyumov-Gerasimenko. The spacecraft of the Hayabusa mission seems to have touched the surface without piercing it [45], which would imply a cohesive strength of at least some tens of Pa. These values are in complete agreement with what would be expected if the findings of Ref. [20] were applied to a soil formed by mainly micron-size dust and small pebbles, whereas the lander of the Rosseta mission sank in the regolith of 67/P to then bounce off an underlying more rigid layer, which would imply an almost cohesionless upper layer [46].

At this moment, the Hayabusa 2 [47] and OSIRIS-REx [48] missions to asteroids Ryugu and Bennu, respectively, are scheduled to obtain a sample from their target asteroids. The strength of their surfaces and interiors has been the topic of large research efforts, but they have been focused on the macroscopic strength of the soil disjoint from the global mechanics of the asteroid. The upcoming DART [49] mission is also running into the same question about the strength of asteroid Didymos. Other efforts related to planetary defense and asteroid mining can also be added to the interested parties, but a theoretical explanation to establish how cohesive and gravitational forces interact to support the structural integrity of granular asteroids or how they scale is lacking. This is what we have tried to do with this Rapid Communication.

The numerical experiments we have carried out do not reflect events that asteroids could undergo; rotational fission, collisions, and gravitational tides are not represented by them. However, they allowed us to directly measure characteristics of a self-gravitating aggregate that are independent of the measuring technique. We used an idealized, simpler system that served as a proxy for an asteroid, and this is the strength of this work. Given that now we have a theoretical framework, we can explore ways to make our simulations more realistic and applicable to other scenarios. This will be the focus of future research.

To summarize, in this Rapid Communication we have defined a consistent framework for the analysis of the behavior of self-gravitating aggregates, which we used as a proxy for granular asteroids, by extending the *I*-rheology paradigm.

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Our extensive numerical simulations provide clear evidence that both macro- and microstructures are well captured through a modified inertial number incorporating interparticle cohesive and gravitational forces. A theoretical model, relating the peak stress to granular texture at sufficiently small I'values, is introduced and shown to be in good agreement with the measured data. The present study sheds some light on a vast and substantial scientific domain given the multitude of open questions related to granular asteroids. The above framework may now be used and extended to analyze much more "complex" self-gravitating systems by incorporating a wide range of particle and asteroid sizes and shapes, and various sources of cohesion (which are generally coupled with particle size [19]) so that they can better represent real asteroids. This will also allow us to explore various dynamical scenarios, such as the rotational evolution of granular asteroids and comets, their reshaping due to planetary tides, or even their exploration, exploitation, redirection, or destruction for planetary defense.

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