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J. Grygier et al. (The Belle Collaboration)

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## Search for $B \rightarrow h \nu \bar{\nu}$ decays with semileptonic tagging at Belle

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We present the results of a search for the rare decays $B \rightarrow h \nu \bar{\nu}$, where $h$ stands for $K^{+}, K_{\mathrm{S}}^{0}, K^{*+}, K^{* 0}, \pi^{+}, \pi^{0}, \rho^{+}$and $\rho^{0}$. The results are obtained with $772 \times 10^{6} B \bar{B}$ pairs collected with the Belle detector at the KEKB $e^{+} e^{-}$collider. We reconstruct one $B$ meson in a semileptonic decay and require a single $h$ meson but nothing else on the signal side. We observe no significant signal and set upper limits on the branching fractions. The limits set on the $B^{0} \rightarrow K_{\mathrm{S}}^{0} \nu \bar{\nu}$,
$B^{0} \rightarrow K^{* 0} \nu \bar{\nu}, B^{+} \rightarrow \pi^{+} \nu \bar{\nu}, B^{0} \rightarrow \pi^{0} \nu \bar{\nu}, B^{+} \rightarrow \rho^{+} \nu \bar{\nu}$, and $B^{0} \rightarrow \rho^{0} \nu \bar{\nu}$ channels are the world's most stringent.

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The decays $B \rightarrow h \nu \bar{\nu} \quad 1$ can proceed only via a penguin or a box diagram at leading order in the standard model (SM), as shown in Fig. 1, and are thus highly suppressed [2]. Theoretical calculations for the branching fractions cover the range from $1.2 \times 10^{-7}[3]\left(B^{0} \rightarrow \pi^{0} \nu \bar{\nu}\right)$ to $9.2 \times 10^{-6}$ [2] $\left(B^{+} \rightarrow K^{*+} \nu \bar{\nu}\right)$. Recent results by LHCb [4, 5] show evidence for a deviation of experimental data from expected values in the angular observable $P_{5}^{\prime}$ in $B^{0} \rightarrow K^{* 0} \mu^{+} \mu^{-}$decays, and in the ratio of the $B^{+} \rightarrow K^{+} \mu^{+} \mu^{-}$to $B^{+} \rightarrow K^{+} e^{+} e^{-}$branching fractions. A measurement of $P_{5}^{\prime}$ by Belle [6] is compatible with both, the SM prediction and the LHCb result. Different new physics models proposed to explain these observations can also influence $B \rightarrow K^{(*)} \nu \bar{\nu}$ decays. Therefore, $B \rightarrow h \nu \bar{\nu}$ channels provide an important test for any model proposed to solve these tensions. Additionally, $B \rightarrow h \nu \bar{\nu}$ channels are theoretically clean due to the mediation of the transition by a $Z$ boson alone, in contrast to $B \rightarrow K^{(*)} l^{+} l^{-}$decays [2] where the photon contributes.
$B \rightarrow h \nu \bar{\nu}$ decays have been studied previously by Belle with a hadronic tagging algorithm [7] and by BaBar utilizing both hadronic [8] and semileptonic tagging [9]. Recent results by Belle [10 have shown that the usage of semileptonic tagging enhances the sensitivity of some analyses significantly. The semileptonically tagged sample provides a statistically independent and more efficiently tagged data set of reconstructed $B \bar{B}$ events as compared to the hadronically tagged sample.

We search for $B \rightarrow h \nu \bar{\nu}$ decays with the full Belle data sample produced by the KEKB collider [11] at the $\Upsilon(4 \mathrm{~S})$ center-of-mass (CM) energy with an integrated luminosity of $711 \mathrm{fb}^{-1}$, corresponding to $(772 \pm 11) \times 10^{6}$ $B \bar{B}$ pairs. A data set of $89 \mathrm{fb}^{-1}$ taken at an energy $60 \mathrm{MeV} / \mathrm{c}^{2}$ below the resonance energy is used to study background from $e^{+} e^{-} \rightarrow q \bar{q}$ processes (continuum), where $q \in u, d, s, c$. We refer to this data set as the off-resonance sample. We model the decays with


FIG. 1: Lowest-order SM quark level diagrams for the $B^{+} \rightarrow K^{+} \nu \bar{\nu}$ channel; the diagrams for other channels are analogous.
the EVTGEN package 12 and simulate the detector response with the GEANT3 package [13]. We include a randomly-triggered sample to account for beam-related background. The signal process is modeled according to three-body phase space.

The Belle detector [14] is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrellike arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of $\mathrm{CsI}(\mathrm{Tl})$ crystals (ECL) located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect $K_{\mathrm{L}}^{0}$ mesons and to identify muons (KLM). The detector is described in detail elsewhere [14]. Two inner detector configurations were used. A 2.0 cm beampipe and a 3-layer silicon vertex detector were used for the first sample of $152 \times 10^{6} B \bar{B}$ pairs, while a 1.5 cm beampipe, a 4-layer silicon detector and a small-cell inner drift chamber were used to record the remaining $620 \times 10^{6} B \bar{B}$ pairs [15].

The three-body $B \rightarrow h \nu \bar{\nu}$ decay, with two invisible particles in the final state, does not convey sufficient kinematic information to isolate the signal. Thus, we first reconstruct the accompanying $B$ meson ( $B_{\mathrm{tag}}$ ) in the semileptonic decay channels $B \rightarrow D^{(*)} l \nu_{l}(l=$ $e, \mu)$, where neutral (charged) $D$ candidates are reconstructed in 10 (7) different decay channels. This amounts to 108 different decay channels. The tagging algorithm, described elsewhere [16, 17], uses multiple instances of neural network classifiers built using the NeuroBayes package [18] in a hierarchical approach to find $B_{\mathrm{tag}}$ candidates. The output of the neural network used to identify real $B_{\mathrm{tag}}$ candidates transformed into the interval $[0,1]$ is referred to as $\mathscr{N}_{\text {tag }}$ and can be interpreted as the probability of the $B_{\mathrm{tag}}$ meson to be a true $B$ in a generic sample. We combine $B_{\text {tag }}$ candidates with our signal selection to form signal event candidates. We separate charged pion and kaon candidates based on particle identification (PID) selection criteria utilizing CDC, ACC and TOF information. We combine the PID information in a likelihood ratio $\mathcal{P}_{K \pi}=\mathcal{L}_{K} /\left(\mathcal{L}_{K}+\mathcal{L}_{\pi}\right)$, where $\mathcal{P}_{K \pi}$ is a function of the polar angle and the momentum of the track in the laboratory system. We require $\mathcal{P}_{K \pi}>0.6(<0.4)$ for $K^{ \pm}\left(\pi^{ \pm}\right)$candidates. The kaon (pion) identification efficiency is $88 \%-93 \%$ $(86 \%-93 \%)$ with a $\pi(K)$ misidentification probability of $10 \%-12 \% ~(8 \%-11 \%)$.

We reduce the number of poor quality tracks by requiring that $d z(d r)<4(2) \mathrm{cm}$, where $d z(d r)$ is the distances of closest approach of a track to the interaction point along (transverse to) the $z$ axis, which is
antiparallel to the positron beam. Signal $B$ daughter candidates are reconstructed through the decays $K^{* 0} \rightarrow K^{+} \pi^{-}, K^{*+} \rightarrow K^{+} \pi^{0}$ and $K_{\mathrm{S}}^{0} \pi^{+}, \rho^{+} \rightarrow$ $\pi^{+} \pi^{0}, \rho^{0} \rightarrow \pi^{+} \pi^{-}, K_{\mathrm{S}}^{0} \rightarrow \pi^{+} \pi^{-}$, and $\pi^{0} \rightarrow \gamma \gamma$. $K_{\mathrm{S}}^{0}$ candidates are selected following Ref. [19]. Photons used for $\pi^{0}$ reconstruction are required to have a minimal energy of $50 \mathrm{MeV} / \mathrm{c}^{2}, 100 \mathrm{MeV} / \mathrm{c}^{2}, 150 \mathrm{MeV} / \mathrm{c}^{2}$ for the barrel $\left(\theta \in\left[32^{\circ}, 129^{\circ}\right]\right)$, forward $\left(\left[17^{\circ}, 32^{\circ}\right]\right)$, and backward $\left(\left[129^{\circ}, 150^{\circ}\right]\right)$ region of the ECL, respectively, where $\theta$ is taken with respect to the $z$ axis. The invariant mass of the two $\gamma$ candidates is required to fulfill $M_{\gamma \gamma} \in[118,150] \mathrm{MeV} / \mathrm{c}^{2}$, while the invariant mass of the $K^{*}(\rho)$ candidates is required to be within $150 \mathrm{MeV} / \mathrm{c}^{2}\left(250 \mathrm{MeV} / \mathrm{c}^{2}\right)$ of the nominal mass from Ref. [20]. The mass requirements are subsequently optimized using Monte Carlo (MC) simulations by maximizing the figure of merit $N_{R} / \sqrt{N_{R}+N_{F}}$, where $N_{R}$ is the number of correctly reconstructed mesons and $N_{F}$ the number of fake candidates, both passing the requirement. We combine a $B_{\text {tag }}$ candidate with the reconstructed signal- $B$ decay product ( $h_{\text {sig }}$ ) to form an $\Upsilon(4 \mathrm{~S})$ candidate.

Events with additional charged tracks or $\pi^{0}$ candidates that satisfy our selection criteria are rejected. Furthermore, we remove events with two or more tracks not fulfilling our requirement on $d r$ or $d z$ "raw tracks." We veto events with reconstructed $K_{\mathrm{L}}^{0}$ candidates and weight our background simulations to account for known dataMC differences, as described in Ref. 21]. An important variable to identify correctly-reconstructed signal events is the extra energy, $E_{\text {ECL }}$. We sum all ECL clusters not used in the reconstruction of the $\Upsilon(4 \mathrm{~S})$ candidate, not associated with a track, and fulfilling the same energy requirements as the clusters used to form $\pi^{0}$ candidates. We require $E_{\mathrm{ECL}}<1.2 \mathrm{GeV} / \mathrm{c}^{2}$. We also require the momentum of the $h_{\text {sig }}$ candidate in the CM system to fulfill $p_{\text {cms }} \in[0.5,2.96] \mathrm{GeV} / \mathrm{c}^{2}$, the missing energy in the CM system $E_{\text {miss }}>2.5 \mathrm{GeV} / \mathrm{c}^{2}$, the momentum of the $B_{\text {tag }}$ lepton candidate in the CM system $p_{l_{\text {tag }}}<2.5 \mathrm{GeV} / \mathrm{c}^{2}$, and a minimal tag quality of $\mathscr{N}_{\text {tag }}>0.005$. These requirements are motivated by kinematic boundaries, data-MC differences in case of low-momentum $h_{\text {sig }}$, and badly reconstructed tag candidates. To suppress pions from $D$ decays misreconstructed as muons, we veto events where the invariant mass of the $K\left(K^{* 0}\right)$ candidate and the tag-side lepton fulfill $M_{K l} \in[1.85,1.87] \mathrm{GeV} / \mathrm{c}^{2}$. The channel-dependent fraction of events with more than one $\Upsilon(4 \mathrm{~S})$ candidate can be as large as $20 \%$, dominated by candidate exchange between signal- and tag-side. In such cases, we select the candidate with the highest $\mathscr{N}_{\text {tag }}$ value, i.e, the candidate with the highest probability of being correctly reconstructed. In MC studies, we find that the efficiency of this selection is between $65 \%\left(B^{+} \rightarrow \rho^{+} \nu \bar{\nu}\right)$ and $92 \%$ $\left(B^{0} \rightarrow K_{\mathrm{S}}^{0} \nu \bar{\nu}\right)$.

We reconstruct tagged $B^{+} \rightarrow \overline{D^{0}}\left(K^{+} \pi^{-}\right) \pi^{+}$and $B^{0} \rightarrow D^{-}\left(K^{+} \pi^{-} \pi^{-}\right) \pi^{+}$decays to correct for experimental data-MC efficiency differences. Both channels
can be reconstructed with negligible background and are well described in MC. We bin $\mathscr{N}_{\text {tag }}$ equally in 4 (3) bins for charged (neutral) $B$ mesons and calculate the number of reconstructed events in data and MC. We assign the ratio as a weight in each bin of $\mathscr{N}_{\text {tag. }}$. This calibration includes a correction of the tagging efficiency $\times$ the number of $B \bar{B}$ pairs produced $\left(N_{B} \bar{B}\right) \times$ the branching fraction of $\Upsilon(4 \mathrm{~S})$ to charged and neutral $B$ meson pairs, as we have a separate calibration for $B^{+}$and $B^{0}$. We train one neural network per channel to suppress continuum events. We use 16 modified Fox-Wolfram moments [22], nine CLEO cones [23], the cosine of the angle of the thrust axis relative to the $z$ axis, and the angle of the momentum of the $B_{\mathrm{tag}}$ candidate with respect to the $z$ axis. We refer to the output of this neural network as $\mathscr{N}_{\text {CS }}$.

To optimally separate signal from background, another neural network is trained for each reconstructed channel. We optimize the requirement on the network output ( $\left.\mathscr{N}_{\text {sel }}\right)$ by maximizing a figure-of-merit $\varepsilon /\left(\frac{n_{\sigma}}{2}+\sqrt{N_{B}}\right)$, which is independent of the signal-to-background ratio and optimized for searches [24]. Here, $\varepsilon$ is the signal efficiency while $N_{B}$ denotes the number of background events passing the requirement on $\mathscr{N}_{\text {sel }}$. Both values are determined from MC. We choose a desired significance $n_{\sigma}=3$. The most powerful variables to identify the signal are $p_{\text {cms }}, \mathscr{N}_{\text {CS }}$, the cosine between the momentum of the $D^{(*)} l$ system and the momentum of the $B_{\text {tag }}$ in the CM system [25], the cosine of the angle of the missing momentum relative to the $z$ axis, the cosine of the angle of the thrust axis, $p_{l_{\mathrm{tag}}}$, and, for the $\rho$ and $K^{*}$ channels, the reconstructed invariant mass. The number of input variables varies for each channel, spanning a range from 17 to 31 .

We evaluate the description of the data by our MC by looking into an $E_{\mathrm{ECL}}$ sideband ( $E_{\mathrm{ECL}}>0.3 \mathrm{GeV} / \mathrm{c}^{2}$ ), by reconstructing tagged $B \rightarrow D^{*} l \nu_{l}$ decays, and by utilizing the off-resonance sample. We find good agreement between data and MC in the $E_{\mathrm{ECL}}$ sidebands for six of the eight channels. However, we find an underestimation of continuum background in MC in the $B^{+} \rightarrow K^{+} \nu \bar{\nu}$ and the $B^{+} \rightarrow \pi^{+} \nu \bar{\nu}$ channels, which we correct by scaling the continuum component in the background model by the observed data-MC ratio in the off-resonance sample.

To extract the signal yield in each channel, we perform an extended binned maximum likelihood (ML) fit to the $E_{\mathrm{ECL}}$ distribution. We use histogram templates to model signal as well as backgrounds from charm $B$-decay $(b \rightarrow c)$, charmless $B$-decay $(b \rightarrow s, u, d)$, and continuum. We fix the relative fractions of the background components to MC expectations and leave only the signal and the overall background yields as freely floating parameters. We perform extensive toy MC studies to estimate the sensitivity of our procedure. For this purpose, we simulate 1000 background-only samples for each channel and calculate an expected limit on the signal yield by integrating the profile likelihood up to the point where
it includes $90 \%$ of the positive region. We also simulate samples with various numbers of signal events to test for a possible bias. We find a non-negligible but modest bias in almost all investigated channels. We fit this bias with a linear function, whose slope is consistent with 1.0 and whose intercept lies between 0 and -2 events. We correct for this bias in our fit to data.


FIG. 2: $E_{\mathrm{ECL}}$ distributions for all eight $B \rightarrow h \nu \bar{\nu}$ channels.

The fit results are listed in Table Ia; Fig. 2 shows the distributions of the data together with the fitted signal and background models. The fit yields no significant signal in any channel. The largest signal contribution is observed in the $B^{+} \rightarrow K^{*+} \nu \bar{\nu}$ channel with a significance of $2.3 \sigma$. The significance is defined by evaluating the likelihood of the complete model $\mathcal{L}_{\text {max }}$ and the background-only likelihood $\mathcal{L}_{0}: S=\sqrt{2 \log \left(\mathcal{L}_{\max } / \mathcal{L}_{0}\right)}$. Both are evaluated at their respective best fitting point. We calculate the branching fraction of the $i$-th mode by
$\mathscr{B}^{i}=N_{\text {sig }}^{i} /\left(\varepsilon_{\text {rec }}^{i} \times N_{B \bar{B}}\right)$, where the reconstruction efficiency $\varepsilon_{\text {rec }}^{i}$ includes all daughter branching fractions. These efficiencies, along with the expected and measured $90 \%$ confidence level (C.L.) upper limit [26] for each channel, are displayed in Table Ib,

TABLE I: Results
(a) Observed signal yield (corrected for fitting bias) in each channel. The first error is statistical and the second is systematic.

| Channel | Observed signal yield | Significance |
| :--- | ---: | ---: |
| $K^{+} \nu \bar{\nu}$ | $17.7 \pm 9.1 \pm 3.4$ | $1.9 \sigma$ |
| $K_{\mathrm{S}}^{0} \nu \bar{\nu}$ | $0.6 \pm 4.2 \pm 1.4$ | $0.0 \sigma$ |
| $K^{*+} \nu \bar{\nu}$ | $16.2 \pm 7.4 \pm 1.8$ | $2.3 \sigma$ |
| $K^{* 0} \nu \bar{\nu}$ | $-2.0 \pm 3.6 \pm 1.8$ | $0.0 \sigma$ |
| $\pi^{+} \nu \bar{\nu}$ | $5.6 \pm 15.1 \pm 5.9$ | $0.0 \sigma$ |
| $\pi^{0} \nu \bar{\nu}$ | $0.2 \pm 5.6 \pm 1.6$ | $0.0 \sigma$ |
| $\rho^{+} \nu \bar{\nu}$ | $6.2 \pm 12.3 \pm 2.4$ | $0.3 \sigma$ |
| $\rho^{0} \nu \bar{\nu}$ | $11.9 \pm 9.0 \pm 3.6$ | $1.2 \sigma$ |

(b) Expected (median) and observed upper limits on the branching fraction at $90 \%$ C.L. The observed limits include the systematic uncertainties.

| Channel | Efficiency | Expected limit | Observed limit |
| :--- | :---: | ---: | ---: |
| $K^{+} \nu \bar{\nu}$ | $2.16 \times 10^{-3}$ | $0.8 \times 10^{-5}$ | $1.9 \times 10^{-5}$ |
| $K_{\mathrm{S}}^{0} \nu \bar{\nu}$ | $0.91 \times 10^{-3}$ | $1.2 \times 10^{-5}$ | $1.3 \times 10^{-5}$ |
| $K^{*+} \nu \bar{\nu}$ | $0.57 \times 10^{-3}$ | $2.4 \times 10^{-5}$ | $6.1 \times 10^{-5}$ |
| $K^{* 0} \nu \bar{\nu}$ | $0.51 \times 10^{-3}$ | $2.4 \times 10^{-5}$ | $1.8 \times 10^{-5}$ |
| $\pi^{+} \nu \bar{\nu}$ | $2.92 \times 10^{-3}$ | $1.3 \times 10^{-5}$ | $1.4 \times 10^{-5}$ |
| $\pi^{0} \nu \bar{\nu}$ | $1.42 \times 10^{-3}$ | $1.0 \times 10^{-5}$ | $0.9 \times 10^{-5}$ |
| $\rho^{+} \nu \bar{\nu}$ | $1.11 \times 10^{-3}$ | $2.5 \times 10^{-5}$ | $3.0 \times 10^{-5}$ |
| $\rho^{0} \nu \bar{\nu}$ | $0.82 \times 10^{-3}$ | $2.2 \times 10^{-5}$ | $4.0 \times 10^{-5}$ |

We estimate the uncertainty on the fixed fractions, the $K_{\mathrm{L}}^{0}$ veto efficiency, the continuum scaling, the tagging efficiency, and the fit bias correction by refitting the data with each of these quantities varied by $\pm 1 \sigma$. We estimate the shape uncertainty by simulating 1000 toy templates obtained by drawing a random number from a Gaussian distribution with the mean and error of the respective bin of our fit model as the central value and deviation. The $\pm 1 \sigma$ quantiles of the resulting distribution are used as estimators of the uncertainty. We estimate the uncertainty on the $\pi^{0}$ and charged track vetoes by comparing the respective efficiency differences between data and MC for the $B \rightarrow D \pi$ sample with and without the veto applied. We obtain a value of $4 \%$ in both cases for charged and neutral channels alike. We evaluate the influence of the requirement on the number of raw tracks via the same sample by setting it to two and zero, respectively. We subsequently average the contributions and obtain a value of $1 \%$. The uncertainty on the calibration ( $9.6 \%$ ) includes the uncertainty on the correction of $N_{B \bar{B}}(1.4 \%)$ and the uncertainty on $\mathcal{B}(B \rightarrow D \pi)$. Based on studies
using dedicated control samples, we assign $2.0 \%, 4.0 \%$, and $2.2 \%$ for the uncertainties on PID efficiency, $\pi^{0}$ efficiency and $K_{\mathrm{S}}^{0}$ efficiency, respectively. The systematic uncertainty is included by convolving the likelihood function with a Gaussian with zero mean and a width equal to the square root of the quadratic sum of the additive and multiplicative error. The additive uncertainty is defined as the uncertainty on the signal yield, and contributions are summarized in Table II A comparison of our results with previous ones is presented in Fig. 3 .


FIG. 3: Observed limits for all channels in comparison to previous results for the BaBar measurement with semileptonic [9] and hadronic tag [8, as well as the
Belle measurement utilizing hadronic tagging [7]. The theoretical predictions are taken from Ref. [2].

The systematic uncertainties are evaluated using independent samples of MC and data control samples for charged and neutral modes. They can therefore be considered uncorrelated. Thus, we combine charged and neutral modes by adding the negative log likelihoods. We scale the branching fraction of the neutral modes by a factor of $\tau_{B^{+}} / \tau_{B^{0}}$ since the lifetime difference is the only factor distinguishing charged from neutral $B \rightarrow h \nu \bar{\nu}$ decays in the SM. We subsequently repeat the calculation of the limit and obtain the following values at $90 \%$ C.L.:

$$
\begin{aligned}
& \mathscr{B}(B \rightarrow K \nu \bar{\nu})<1.6 \times 10^{-5} \\
& \mathscr{B}\left(B \rightarrow K^{*} \nu \bar{\nu}\right)<2.7 \times 10^{-5} \\
& \mathscr{B}(B \rightarrow \pi \nu \bar{\nu})<0.8 \times 10^{-5} \\
& \mathscr{B}(B \rightarrow \rho \nu \bar{\nu})<2.8 \times 10^{-5}
\end{aligned}
$$

Based on the values and theoretical uncertainties from Ref. [2], we also give a limit on the ratios between the measured branching fractions of $B \rightarrow K \nu \bar{\nu}$ and of $B \rightarrow$ $K^{*} \nu \bar{\nu}$ and the respective SM prediction $\mathcal{R}_{K^{*}}$. We obtain
values of $\mathcal{R}_{K}<3.9$ and $\mathcal{R}_{K^{*}}<2.7$, respectively, where we included the theoretical uncertainty. Both values are quoted at $90 \%$ C.L.

In summary, we report the results of a search for eight different $B$ decay channels with a pair of neutrinos in the final state, where the second $B$ is reconstructed in one of 108 semileptonic decay channels. No significant signal is observed and limits are set on the respective branching fractions at a confidence level of $90 \%$. The limits on the branching fraction for the $B^{0} \rightarrow K_{\mathrm{S}}^{0} \nu \bar{\nu}$, $B^{0} \rightarrow K^{* 0} \nu \bar{\nu}, B^{+} \rightarrow \pi^{+} \nu \bar{\nu}, B^{0} \rightarrow \pi^{0} \nu \bar{\nu}, B^{+} \rightarrow \rho^{+} \nu \bar{\nu}$, and $B^{0} \rightarrow \rho^{0} \nu \bar{\nu}$ channels are the most stringent to date. Although our analysis yields important improvements, none of these limits excludes SM predictions and all of them leave room for contributions from new physics.

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TABLE II: Additive systematic uncertainties. All values are event yields.

|  | $K^{+} \nu \bar{\nu}$ | $K_{\mathrm{S}}^{0} \nu \bar{\nu}$ | $K^{*+} \nu \bar{\nu}$ | $K^{* 0} \nu \bar{\nu}$ | $\pi^{+} \nu \bar{\nu}$ | $\pi^{0} \nu \bar{\nu}$ | $\rho^{+} \nu \bar{\nu}$ | $\rho^{0} \nu \bar{\nu}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $K_{\mathrm{L}}^{0}$ veto | 0.2 | 0.2 | 0.1 | 0.2 | 0.6 | 0.4 | 0.6 | 0.0 |
| Fixed fractions | 0.4 | 0.3 | 0.1 | 0.2 | 1.3 | 0.1 | 0.1 | 1.0 |
| Continuum scaling | 2.0 | 0.0 | 0.0 | 0.0 | 3.1 | 0.0 | 0.0 | 0.0 |
| Tag efficiency correction | 0.5 | 0.2 | 0.1 | 0.1 | 1.9 | 0.1 | 0.2 | 0.5 |
| Shape uncertainty | 2.6 | 1.3 | 1.8 | 1.7 | 4.5 | 1.5 | 2.3 | 3.4 |
| Fit bias | 0.2 | 0.1 | 0.2 | 0.1 | 0.2 | 0.1 | 0.2 | 0.2 |
| Total | 3.4 | 1.4 | 1.8 | 1.8 | 5.9 | 1.6 | 2.4 | 3.6 |

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Education and the Ministry of Science and Technology of Taiwan; and the U.S. Department of Energy and the National Science Foundation.
[1] Throughout this letter, $h$ refers to one of the following charmless states: $K^{+}, K_{\mathrm{S}}^{0}, K^{*+}, K^{* 0}, \pi^{+}, \pi^{0}, \rho^{+}, \rho^{0}$. Charge-conjugate channels are implied throughout this paper unless explicitly stated otherwise.
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[25] The cosine of the angle between the $B$ and the $D^{(*)} l$ system is defined as $\cos \theta_{B, D^{(*)} l}=$ $\left(2 E_{B} E_{D^{(*)} l}-M_{B}^{2} c^{4}-M_{D^{(*)}, \iota}^{2} c^{4}\right) /\left(2\left|\mathbf{p}_{B}\right|\left|\mathbf{p}_{D^{(*)} \iota}\right| c^{2}\right)$ where $M, E$, and $\mathbf{p}$ are the invariant mass, energy, and momentum of the $B\left(D^{(*)} l\right)$ system.
[26] As we use a Bayesian method, this is formally a "credibility level." However, we use "confidence level" here following common convention.

