## Search for $\boldsymbol{b} \rightarrow \boldsymbol{u}$ transitions in $\boldsymbol{B}^{-} \rightarrow \boldsymbol{D K} K^{-}$and $\boldsymbol{D}^{*} \boldsymbol{K}^{-}$decays

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We report results from an updated study of the suppressed decays $B^{-} \rightarrow D K^{-}$and $B^{-} \rightarrow D^{*} K^{-}$ followed by $D \rightarrow K^{+} \pi^{-}$, where $D^{(*)}$ indicates a $D^{(*) 0}$ or a $\bar{D}^{(*) 0}$ meson, and $D^{*} \rightarrow D \pi^{0}$ or $D^{*} \rightarrow D \gamma$. These decays are sensitive to the Cabibbo-Kobayashi-Maskawa unitarity triangle angle $\gamma$ due to interference between the $b \rightarrow c$ transition $B^{-} \rightarrow D^{(*) 0} K^{-}$followed by the doubly Cabibbo-suppressed

[^0]decay $D^{0} \rightarrow K^{+} \pi^{-}$, and the $b \rightarrow u$ transition $B^{-} \rightarrow \bar{D}^{(*) 0} K^{-}$followed by the Cabibbo-favored decay $\bar{D}^{0} \rightarrow K^{+} \pi^{-}$. We also report an analysis of the decay $B^{-} \rightarrow D^{(*)} \pi^{-}$with the $D$ decaying into the doubly Cabibbo-suppressed mode $D \rightarrow K^{+} \pi^{-}$. Our results are based on $467 \times$ $10^{6} \Upsilon(4 S) \rightarrow B \bar{B}$ decays collected with the BABAR detector at SLAC. We measure the ratios $\mathcal{R}^{(*)}$ of the suppressed ( $\left[K^{+} \pi^{-}\right]_{D} K^{-} / \pi^{-}$) to favored ( $\left[K^{-} \pi^{+}\right]_{D} K^{-} / \pi^{-}$) branching fractions as well as the $C P$ asymmetries $\mathcal{A}^{(*)}$ of those modes. We see indications of signals for the $B^{-} \rightarrow D K^{-}$ and $B^{-} \rightarrow D_{D \pi^{0}}^{*} K^{-}$suppressed modes, with statistical significances of 2.1 and $2.2 \sigma$, respectively, and we measure: $\mathcal{R}_{D K}=(1.1 \pm 0.6 \pm 0.2) \times 10^{-2}, \quad \mathcal{A}_{D K}=-0.86 \pm 0.47_{-0.16}^{+0.12}, \mathcal{R}_{\left(D \pi^{0}\right) K}^{*}=(1.8 \pm 0.9 \pm$ $0.4) \times 10^{-2}, \quad \mathcal{A}_{\left(D \pi^{0}\right) K}^{*}=+0.77 \pm 0.35 \pm 0.12, \quad \mathcal{R}_{(D \gamma) K}^{*}=(1.3 \pm 1.4 \pm 0.8) \times 10^{-2}, \mathcal{A}_{(D \gamma) K}^{*}=+0.36$ $\pm 0.94_{-0.41}^{+0.25}$, where the first uncertainty is statistical and the second is systematic. We use a frequentist approach to obtain the magnitude of the ratio $r_{B} \equiv\left|A\left(B^{-} \rightarrow \bar{D}^{0} K^{-}\right) / A\left(B^{-} \rightarrow D^{0} K^{-}\right)\right|=\left(9.5_{-4.1}^{+5.1}\right) \%$, with $r_{B}<16.7 \%$ at $90 \%$ confidence level. In the case of $B^{-} \rightarrow D^{*} K^{-}$we find $r_{B}^{*} \equiv \mid A\left(B^{-} \rightarrow\right.$ $\left.\bar{D}^{* 0} K^{-}\right) / A\left(B^{-} \rightarrow D^{* 0} K^{-}\right) \mid=\left(9.6_{-5.1}^{+3.5}\right) \%$, with $r_{B}^{*}<15.0 \%$ at $90 \%$ confidence level.

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## I. INTRODUCTION

The standard model accommodates $C P$ violation through a single phase in the Cabibbo-KobayashiMaskawa (CKM) quark mixing matrix $V$ [1]. In the Wolfenstein parameterization [2], the angle $\gamma=$ $\arg \left(-V_{u d} V_{u b}^{*} / V_{c d} V_{c b}^{*}\right)$ of the unitarity triangle is related to the complex phase of the CKM matrix element $V_{u b}$ through $V_{u b}=\left|V_{u b}\right| e^{-i \gamma}$. A theoretically clean source of information on the angle $\gamma$ is provided by $B^{-} \rightarrow D^{(*)}$ $K^{-}$decays, where $D^{(*)}$ represents an admixture of $D^{(*) 0}$ and $\bar{D}^{(*) 0}$ states. These decays exploit the interference between $B^{-} \rightarrow D^{(*) 0} K^{-}$and $B^{-} \rightarrow \bar{D}^{(*) 0} K^{-}$(Fig. 1) that occurs when the $D^{(*) 0}$ and the $\bar{D}^{(*) 0}$ decay to common final states.

In the Atwood-Dunietz-Soni (ADS) method [3], the $D^{0}$ from the favored $b \rightarrow c$ amplitude is reconstructed in the doubly Cabibbo-suppressed decay $K^{+} \pi^{-}$, while the $\bar{D}^{0}$ from the $b \rightarrow u$ suppressed amplitude is reconstructed in the favored decay $K^{+} \pi^{-}$. The product branching fractions for these final states, which we denote as $\left[K^{+} \pi^{-}\right]_{D} K^{-}$ $\left(B^{-} \rightarrow D K^{-}\right)$and $\left[K^{+} \pi^{-}\right]_{D^{*}} K^{-}\left(B^{-} \rightarrow D^{*} K^{-}\right)$, are small $\left(\sim 10^{-7}\right)$, but the two interfering amplitudes are of the same order of magnitude, and large $C P$ asymmetries are therefore possible. The favored decay mode $B^{-} \rightarrow$ $\left[K^{-} \pi^{+}\right]_{D^{(*)}} K^{-}$is used to normalize the measurement and cancel many systematic uncertainties. Thus, ignoring possible small effects due to $D$ mixing and assuming no $C P$ violation in the normalization modes, we define the


FIG. 1. Feynman diagrams for $B^{-} \rightarrow D^{(*) 0} K^{(*)-}$ and $\bar{D}^{(*) 0} K^{(*)-}$. The latter is CKM and color-suppressed with respect to the former.

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charge-specific ratios for $B^{+}$and $B^{-}$decay rates to the ADS final states as

$$
\begin{align*}
\mathcal{R} \stackrel{ \pm}{D} K & \equiv \frac{\Gamma\left(\left[K^{\mp} \pi^{ \pm}\right]_{D} K^{ \pm}\right)}{\Gamma\left(\left[K^{ \pm} \pi^{\mp}\right]_{D} K^{ \pm}\right)} \\
& =r_{B}^{2}+r_{D}^{2}+2 r_{B} r_{D} \cos ( \pm \gamma+\delta) \tag{1}
\end{align*}
$$

where $\quad r_{B}=\left|A\left(B^{-} \rightarrow \bar{D}^{0} K^{-}\right) / A\left(B^{-} \rightarrow D^{0} K^{-}\right)\right| \approx 10 \%$ [4-7] and $r_{D}=\left|A\left(D^{0} \rightarrow K^{+} \pi^{-}\right) / A\left(D^{0} \rightarrow K^{-} \pi^{+}\right)\right|=$ $(5.78 \pm 0.08) \%$ [8] are the suppressed to favored $B$ and $D$ amplitude ratios. The rates in Eq. (1) depend on the relative weak phase $\gamma$ and the relative strong phase $\delta \equiv$ $\delta_{B}+\delta_{D}$ between the interfering amplitudes, where $\delta_{B}$ and $\delta_{D}$ are the strong phase differences between the two $B$ and $D$ decay amplitudes, respectively. The value of $\delta_{D}$ has been measured to be $\delta_{D}=\left(201.9_{-12.4}^{+11.3}\right)^{\circ}$ [8], where we have accounted for a phase shift of $180^{\circ}$ in the definition of $\delta_{D}$ between Ref. [8] and this analysis.

The main experimental observables are the chargeaveraged decay rate and the direct $C P$ asymmetry, which can be written as

$$
\begin{gather*}
\mathcal{R}_{D K} \equiv \frac{1}{2}\left(\mathcal{R}_{D K}^{+}+\mathcal{R}_{D K}^{-}\right)=r_{B}^{2}+r_{D}^{2}+2 r_{B} r_{D} \cos \gamma \cos \delta,  \tag{2}\\
\mathcal{A}_{D K} \equiv \frac{\mathcal{R}_{D K}^{-}-\mathcal{R}_{D K}^{+}}{\mathcal{R}_{D K}^{-}+\mathcal{R}_{D K}^{+}}=2 r_{B} r_{D} \sin \gamma \sin \delta / \mathcal{R}_{D K} . \tag{3}
\end{gather*}
$$

The treatment for the $D^{*} K$ mode is identical to the $D K$ one, but the parameters $r_{B}^{*}$ and $\delta_{B}^{*}$ are not expected to be numerically the same as those of the $D K$ mode. Taking into account the effective strong phase difference of $\pi$ between the $D^{*}$ decays to $D \gamma$ and $D \pi^{0}$ [9], we define the charge-specific ratios for $D^{*}$ as

$$
\begin{align*}
\mathcal{R}_{\left(D \pi^{0}\right) K}^{* \pm} & \equiv \frac{\Gamma\left(\left[K^{\mp} \pi^{ \pm}\right]_{D^{*} \rightarrow D \pi^{0}} K^{ \pm}\right)}{\Gamma\left(\left[K^{ \pm} \pi^{\mp}\right]_{D^{*} \rightarrow D \pi^{0}} K^{ \pm}\right)} \\
& =r_{B}^{* 2}+r_{D}^{2}+2 r_{B}^{*} r_{D} \cos \left( \pm \gamma+\delta^{*}\right) \tag{4}
\end{align*}
$$

$$
\begin{align*}
\mathcal{R}_{(D \gamma) K}^{* \pm} & \equiv \frac{\Gamma\left(\left[K^{\mp} \pi^{ \pm}\right]_{D^{*} \rightarrow D \gamma} K^{ \pm}\right)}{\Gamma\left(\left[K^{ \pm} \pi^{\mp}\right]_{D^{*} \rightarrow D \gamma} K^{ \pm}\right)} \\
& =r_{B}^{* 2}+r_{D}^{2}-2 r_{B}^{*} r_{D} \cos \left( \pm \gamma+\delta^{*}\right) \tag{5}
\end{align*}
$$

with $r_{B}^{*}=\left|A\left(B^{-} \rightarrow \bar{D}^{* 0} K^{-}\right) / A\left(B^{-} \rightarrow D^{* 0} K^{-}\right)\right|$and $\delta^{*} \equiv$ $\delta_{B}^{*}+\delta_{D}$, where $\delta_{B}^{*}$ is the strong phase difference between the two $B$ decay amplitudes. The charge-averaged ratios for $D^{*} \rightarrow D \pi^{0}$ and $D^{*} \rightarrow D \gamma$ are then:

$$
\begin{align*}
\mathcal{R}_{\left(D \pi^{0}\right) K}^{*} & \equiv \frac{1}{2}\left(\mathcal{R}_{\left(D \pi^{0}\right) K}^{*+}+\mathcal{R}_{\left(D \pi^{0}\right) K}^{*-}\right) \\
& =r_{B}^{* 2}+r_{D}^{2}+2 r_{B}^{*} r_{D} \cos \gamma \cos \delta^{*}  \tag{6}\\
\mathcal{R}_{(D \gamma) K}^{*} & \equiv \frac{1}{2}\left(\mathcal{R}_{(D \gamma) K}^{*+}+\mathcal{R}_{(D \gamma) K}^{*-}\right) \\
& =r_{B}^{* 2}+r_{D}^{2}-2 r_{B}^{*} r_{D} \cos \gamma \cos \delta^{*} \tag{7}
\end{align*}
$$

Definitions of the direct $C P$ asymmetries $\mathcal{A}_{\left(D \pi^{0}\right) K}^{*}$ and $\mathcal{A}_{(D \gamma) K}^{*}$ follow Eq. (3).

This paper is an update of our previous ADS analysis in Ref. [4], which used $232 \times 10^{6} B \bar{B}$ pairs and set $90 \%$ C.L. upper limits $\mathcal{R}_{D K}<0.029, \mathcal{R}_{\left(D \pi^{0}\right) K}^{*}<0.023$ and $\mathcal{R}_{(D \gamma) K}^{*}<0.045$. In addition to an increased data sample, new features in the analysis include a multidimensional fit involving the neural network output used to discriminate the signal from the continuum background, rather than a simple cut on this variable as was done in the previous analysis. We also include measurements of the ratios of the doubly Cabibbo-suppressed to Cabibbofavored $D^{(*)} \pi$ decay rates,

$$
\begin{equation*}
\mathcal{R}_{D \pi}^{(*) \pm} \equiv \frac{\Gamma\left(B^{ \pm} \rightarrow\left[K^{\mp} \pi^{ \pm}\right]_{D^{(*)}} \pi^{ \pm}\right)}{\Gamma\left(B^{ \pm} \rightarrow\left[K^{ \pm} \pi^{\mp}\right]_{D^{(*)}} \pi^{ \pm}\right)} \tag{8}
\end{equation*}
$$

and of the corresponding asymmetries. These measurements are used as a check for the $B^{-} \rightarrow\left[K^{+} \pi^{-}\right]_{D^{(*)}} K^{-}$ ADS analysis. In the $D^{(*)} \pi$ case, we expect that the ratio $r_{B}^{(*)(D \pi)}$ of the $V_{u b}$ to $V_{c b}$ amplitudes is suppressed by a factor $\left|V_{c d} V_{u s} / V_{u d} V_{c s}\right|$ compared to the $D^{(*)} K$ case, if we assume the same color suppression factor for both decays. One expects therefore $r_{B}^{(*)(D \pi)} \approx r_{B}^{(*)} \times \tan ^{2} \theta_{c} \approx$ $5 \times 10^{-3} \ll r_{D}$, where $\theta_{c}$ is the Cabibbo angle and where we have assumed $r_{B}^{(*)}=10 \%$. Neglecting higher order terms, $\mathcal{R}_{D \pi}^{(*)} \simeq r_{D}^{2}$ and $\mathcal{A}_{D \pi}^{(*)} \simeq 2 r_{B}^{(*)} \tan ^{2} \theta_{c} \sin \gamma \sin \delta^{(*)} / r_{D}$. Hence, the maximum asymmetry possible for $D^{(*)} \pi$ ADS decays is $2 r_{B}^{(*)} \tan ^{2} \theta_{c} / r_{D} \approx 18 \%$.

## II. THE BABAR DETECTOR AND DATA SET

The results presented in this paper are based on $467 \times 10^{6} \mathrm{Y}(4 S) \rightarrow B \bar{B}$ decays, corresponding to an integrated luminosity of $426 \mathrm{fb}^{-1}$ (on-peak data). The data were collected between 1999 and 2007 with the BABAR detector [10] at the PEP-II $e^{+} e^{-}$collider at SLAC. In addition, a $44 \mathrm{fb}^{-1}$ data sample, with center-of-mass (CM) energy 40 MeV below the $\mathrm{Y}(4 S)$ resonance
(off-peak data), is used to study backgrounds from continuum events, $e^{+} e^{-} \rightarrow q \bar{q}(q=u, d, s$, or $c)$.

The $B A B A R$ detector response to various physics processes as well as to varying beam and environmental conditions is modeled with simulation software based on the GEANT4 [11] tool kit. We use EVTGEN [12] to model the kinematics of $B$ meson decays and JETSET [13] to model continuum processes $e^{+} e^{-} \rightarrow q \bar{q}$.

## III. ANALYSIS METHOD

## A. Basic requirements

We reconstruct $B^{-} \rightarrow D^{(*)} K^{-}$and $B^{-} \rightarrow D^{(*)} \pi^{-}$with the $D$ decaying to $K^{-} \pi^{+}$(right-sign [RS] decays) and $K^{+} \pi^{-}$(wrong-sign [WS] decays). Charge conjugate reactions are assumed throughout this paper. For decays involving a $D^{*}$, both $D^{*} \rightarrow D \pi^{0}$ and $D^{*} \rightarrow D \gamma$ modes are reconstructed. Charged kaon and pion candidates must satisfy identification criteria that are typically $85 \%$ efficient, depending on momentum and polar angle. The misidentification rates are at the few percent level. We select $D$ candidates with an invariant mass within $20 \mathrm{MeV} / c^{2}$ (about 3 standard deviations) of the known $D^{0}$ mass [14]. All $D$ candidates are mass and vertex constrained. For modes with $D^{*} \rightarrow D \pi^{0}$ or $D^{*} \rightarrow D \gamma$, the mass difference $\Delta m$ between the $D^{*}$ and the $D$ must be within $4 \mathrm{MeV} / c^{2}$ $(\simeq 4 \sigma)$ or $15 \mathrm{MeV} / c^{2}(\simeq 2 \sigma)$, respectively, of the nominal mass difference [14].

For the WS decays $B^{ \pm} \rightarrow\left[K^{\mp} \pi^{ \pm}\right]_{D} K^{ \pm}$, two important sources of background arise: the first from $B^{ \pm} \rightarrow$ $\left[\pi^{\mp} K^{ \pm}\right]_{D} K^{ \pm}$(in which the $K$ and $\pi$ in the $D$ decay are misidentified as $\pi$ and $K$ ) and the second from $B^{ \pm} \rightarrow$ $\left[K^{\mp} K^{ \pm}\right]_{D} \pi^{ \pm}$(when the $K^{\mp} \pi^{ \pm}$pair has an invariant mass within $20 \mathrm{MeV} / c^{2}$ of the nominal $D^{0}$ mass). To eliminate the first background, we recompute the invariant mass ( $M_{\text {switch }}$ ) of the $h^{+} h^{\prime-}$ pair in $D^{0} \rightarrow h^{+} h^{\prime-}$ switching the mass assumptions on the $h^{+}$and the $h^{\prime-}$. We veto candidates with $M_{\text {switch }}$ within $20 \mathrm{MeV} / c^{2}$ of the $D^{0}$ mass [14]. To eliminate the second background, we also veto any candidate where the $K K$ invariant mass is within $20 \mathrm{MeV} / c^{2}$ of the $D^{0}$ mass. To ensure the same selection efficiencies, these criteria are applied both to $B^{ \pm} \rightarrow$ $\left[K^{\mp} \pi^{ \pm}\right]_{D^{(*)}} K^{ \pm}$and to $B^{ \pm} \rightarrow\left[K^{ \pm} \pi^{\mp}\right]_{D^{(*)}} K^{ \pm}$candidates. These veto cuts are $88 \%$ efficient on signal decays, while removing approximately $90 \%$ of the $\left[\pi^{\mp} K^{ \pm}\right]_{D} K^{ \pm}$and $\left[K^{\mp} K^{ \pm}\right]_{D} \pi^{ \pm}$peaking background. Other possible background contributions faking the signal, like $B^{ \pm} \rightarrow$ $\left[K^{ \pm} \pi^{\mp} \pi^{0}\right]_{D} K^{ \pm}$, are found to be negligible, thanks to the $\Delta E$ and $D$ mass cuts.

We identify $B$ candidates using two nearly independent kinematic variables that are customarily used when reconstructing $B$-meson decays at the $\mathrm{Y}(4 S)$. These variables are the energy-substituted mass, $m_{\mathrm{ES}} \equiv$ $\sqrt{\left(\frac{s}{2}+\vec{p}_{0} \cdot \vec{p}_{B}\right)^{2} / E_{0}^{2}-p_{B}^{2}}$ and energy difference $\Delta E \equiv$ $E_{B}^{*}-\frac{1}{2} \sqrt{s}$, where $E$ and $p$ are energy and momentum,

TABLE I. Selection efficiencies, after correction for known data/MC differences, for $B^{\mp} \rightarrow\left[K^{ \pm} \pi^{\mp}\right]_{D^{(*)}} h^{\mp}\left(\epsilon_{\mathrm{WS}}\right)$ and $B^{\mp} \rightarrow$ $\left[K^{\mp} \pi^{ \pm}\right]_{D^{(\aleph)}} h^{\mp}\left(\epsilon_{\mathrm{RS}}\right)$, and efficiency ratio $\epsilon_{\mathrm{WS}} / \epsilon_{\mathrm{RS}}$.

| Channel | $\epsilon_{\mathrm{WS}}(\%)$ | $\epsilon_{\mathrm{RS}}(\%)$ | $\epsilon_{\mathrm{WS}} / \epsilon_{\mathrm{RS}}\left(10^{-2}\right)$ |
| :--- | :---: | :---: | :---: |
| $D K$ | $26.5 \pm 0.1$ | $26.6 \pm 0.1$ | $99.6 \pm 0.5$ |
| $D_{D}^{*} \pi^{0} K$ | $13.3 \pm 0.1$ | $13.2 \pm 0.1$ | $100.6 \pm 1.1$ |
| $D_{D \gamma}^{*} K$ | $17.4 \pm 0.1$ | $17.5 \pm 0.1$ | $99.8 \pm 0.8$ |
| $D \pi$ | $26.0 \pm 0.1$ | $26.5 \pm 0.1$ | $97.9 \pm 0.5$ |
| $D_{D \pi^{0}}^{*} \pi$ | $14.3 \pm 0.1$ | $14.8 \pm 0.1$ | $96.4 \pm 0.9$ |
| $D_{D \gamma}^{*} \pi$ | $18.8 \pm 0.1$ | $19.5 \pm 0.1$ | $96.3 \pm 0.7$ |

the asterisk denotes the CM frame, the subscripts 0 and $B$ refer to the $\Upsilon(4 S)$ and $B$ candidate, respectively, and $s$ is the square of the CM energy. For signal events $m_{\mathrm{ES}}=m_{B^{+}}$ [14] and $\Delta E=0$ within the resolutions of about $2.6 \mathrm{MeV} / c^{2}$ and 17 MeV , respectively. We require that all candidates have $|\Delta E|<40 \mathrm{MeV}$ and we use $m_{\mathrm{ES}}$ in the fit to extract the number of signal events.

The average number of $B \rightarrow D^{(*)} K$ candidates reconstructed per selected event is about 1.4 in $B \rightarrow D K$ signal Monte Carlo (MC) simulation events and about 2 for $B \rightarrow$ $D^{*} K$ signal MC events. This is mostly due to the cross-feed between the $D K$ and the $D^{*} K$ final states. For all events with multiple $B \rightarrow D^{(*)} K$ candidates, we retain only one candidate per event, based on the smallest value of $|\Delta E|$. This method does not bias the sample since $\Delta E$ is not used to extract the number of signal events. After this arbitration, less than $0.4 \%(0.5 \%)$ of the $B \rightarrow D K\left(B \rightarrow D^{*} K\right)$ signal MC events selected are reconstructed as $B \rightarrow D^{*} K$ $(B \rightarrow D K)$. About $10 \%$ of the $B \rightarrow D_{D \pi^{0}}^{*} K$ events selected are reconstructed as $B \rightarrow D_{D \gamma}^{*} K$ and about $2 \%$ of the $B \rightarrow$ $D_{D \gamma}^{*} K$ events selected are reconstructed as $B \rightarrow D_{D \pi^{0}}^{*} K$.

The $B \rightarrow D^{(*)} \pi$ analysis is performed independently of the $B \rightarrow D^{(*)} K$ analysis, but uses the same multiple candidate selection algorithm. A summary of the selection efficiencies for the WS modes $\left[K^{ \pm} \pi^{\mp}\right]_{D^{(*)}} h^{\mp}(h=K, \pi)$ and the RS modes $\left[\pi^{ \pm} K^{\mp}\right]_{D^{* *}} h^{\mp}$ is given in Table I.

## B. Neural network

After these initial requirements, backgrounds dominantly arise from continuum events, especially $e^{+} e^{-} \rightarrow$ $c \bar{c}$, with $\bar{c} \rightarrow \bar{D}^{0} X, \bar{D}^{0} \rightarrow K^{+} \pi^{-}$and $c \rightarrow D^{0} X, D^{0} \rightarrow$ $K^{-}+$anything. The continuum background is reduced by using a multilayer perceptron artificial neural network with 2 hidden layers, available in the framework of the TMVA package [15]. To select the discriminating variables used in the neural network, we rely on a study performed for the previous version of this analysis [4], and we consider the seven quantities listed below:
(1) Two event shape moments $L_{0}=\sum_{i} p_{i}$, and $L_{2}=$ $\sum_{i} p_{i} \cos ^{2} \theta_{i}$, calculated in the CM frame. Here, $p_{i}$ is the momentum and $\theta_{i}$ is the angle with respect to the thrust axis of the $B$ candidate; the index $i$ runs over
all tracks and clusters not used to reconstruct the $B$ meson (rest of the event). These variables are sensitive to the shape of the event, separating jetlike continuum events from more spherical $B \bar{B}$ events.
(2) The absolute value of the cosine of the angle in the CM frame between the thrust axes of the $B$ candidate and the detected remainder of the event, $\left|\cos \theta_{T}\right|$. The distribution of $\left|\cos \theta_{T}\right|$ is approximately uniform for signal and strongly peaked at one for continuum background.
(3) The absolute value of the cosine of the CM angle between the $B$ candidate momentum and the beam axis, $\left|\cos \theta_{B}\right|$. In this variable, the signal follows a $1-\cos ^{2} \theta_{B}$ distribution, while the background is approximately uniform.
(4) The charge difference $\Delta Q$ between the sum of the charges of tracks in the $D^{(*)}$ hemisphere and the sum of the charges of the tracks in the opposite hemisphere, excluding the tracks used in the reconstructed $B$, and where the partitioning of the event into two hemispheres is done in the CM frame. This variable exploits the correlation occurring in $c \bar{c}$ events between the charge of the $c($ or $\bar{c}$ ) in a given hemisphere and the sum of the charges of all particles in that hemisphere. For signal events, the average charge difference is $\langle\Delta Q\rangle=0$, whereas for the $c \bar{c}$ background $\langle\Delta Q\rangle \approx \frac{7}{3} \times Q_{B}$, where $Q_{B}$ is the charge of the $B$ candidate.
(5) The product $Q_{B} \cdot Q_{K}$, where $Q_{K}$ is the sum of the charges of all kaons in the rest of the event. In many signal events, there is a charged kaon among the decay products of the other $B$ in the event. The charge of this kaon tends to be highly correlated with the charge of the $B$. Thus, signal events tend to have $Q_{B} \cdot Q_{K} \leq-1$. On the other hand, most continuum events have no kaons outside of the reconstructed $B$, and therefore $Q_{K}=0$.
(6) A quantity $\mathcal{M}_{K \ell}$, defined to be zero if there are no leptons ( $e$ or $\mu$ ) in the event, and, if a lepton is found, taken to be equal to the invariant mass of this lepton and the kaon from $B$ (bachelor $K$ ). This quantity differentiates between continuum background and signal because continuum events have fewer leptons than $B \bar{B}$ events. Furthermore, a large fraction of leptons in $c \bar{c}$ background events are from $D \rightarrow K \ell \nu$, where the kaon becomes the bachelor kaon candidate, so that the average $\mathcal{M}_{K \ell}$ in $c \bar{c}$ events is lower than in $B$ signal events.
(7) The absolute value of the measured proper time interval between the two $B$ decays, $|\Delta t|$. This is calculated from the measured separation, $\Delta z$, between the decay points of the reconstructed $B$ and the other $B$ along the beam direction, and the known Lorentz boost of the initial $e^{+} e^{-}$state. For continuum background, $|\Delta t|$ is peaked at 0 , with most


FIG. 2 (color online). Signal and background distributions of the neural network output, and results of the $N N$ verifications for $D K$ (a), $D^{(*)} K(\mathrm{~b}, \mathrm{c}), D \pi(\mathrm{~d})$ and $D^{(*)} \pi(\mathrm{e}, \mathrm{f})$ candidates. (a, d): $D h^{ \pm}$right-sign candidates, signal-enriched by a cut on the $\Delta E, m_{\text {ES }}$ signal region. Shaded plain histograms are MC expectations for $q \bar{q}$ background (dark gray/blue), $b \bar{b}$ background (middle gray/green) and $B^{ \pm} \rightarrow D h^{ \pm}$signal events (light gray/yellow). Points with error bars are on-peak data. (b, e): $D^{(*)} h^{ \pm}$wrong-sign background. (c, f): $D^{(*)} h^{ \pm}$right-sign background. Plots $\mathrm{b}, \mathrm{c}$, e, and f are normalized to unity. The dotted line histograms show the distribution of simulated continuum events. The off-peak data used to check the $N N$ are overlaid as data points. To increase the statistics, the $m_{\mathrm{ES}}$ and $\Delta E$ requirements on the off-peak and continuum MC events have been relaxed, and $D h^{ \pm}$and $D^{*} h^{ \pm}$contributions have been summed.
events having $|\Delta t|<2 \mathrm{ps}$, while it is less peaked and can extend beyond 5 ps for $B^{ \pm} \rightarrow D^{(*)} h^{ \pm}$signal events.
The neural network is trained with simulated continuum and signal $\left[K^{ \pm} \pi^{\mp}\right]_{D^{(*)}} K^{\mp}$ events. Only wrong-sign $D^{(*)} K$ candidates are used in the training, but the neural network is used in the analysis of all the $D^{(*)} h^{\mp}$ channels. The distributions of the neural network output ( $N N$ ) for signal-enriched right-sign control samples are compared with expectations from the MC simulation in Fig. 2(a) ( $D K$ ) and Fig. 2(d) $(D \pi)$. The agreement is satisfactory. In the same figure, the $N N$ spectra of background control samples (off-peak data) are compared with expectations from continuum $q \bar{q}$ MC. Since we do not expect these distributions to be exactly the same for the right-sign and wrong-sign background samples, they are shown separately for the $\left[K^{ \pm} \pi^{\mp}\right]_{D_{-}^{(*)}} K^{\mp}$ [Fig. 2(b)], $\left[K^{\mp} \pi^{ \pm}\right]_{D^{(*)}} K^{\mp}$ (Fig. 2(c)), $\left[K^{ \pm} \pi^{\mp}\right]_{D^{(*)}} \pi^{\mp}$ [Fig. 2(e)) and $\left[K^{\mp} \pi^{ \pm}\right]_{D^{(*)}} \pi^{\mp}$ (Fig. 2(f)) channels. To increase the statistics, the $m_{\text {ES }}$ and $\Delta E$ requirements on the off-resonance and continuum MC events have been relaxed, and the $D h^{ \pm}$and $D^{*} h^{ \pm}$contributions have been summed, after checking that they are in agreement with each other. Good agreement between data and the simulation is observed in all channels. Good agreement between the $D^{(*)} K$ and the $D^{(*)} \pi$ background $N N$ distributions is also visible in Fig. 2, while on the contrary
the background $N N$ distribution of wrong-sign decays is clearly different from the background $N N$ distribution of right-sign decays. We have examined the distributions of all variables used in the neural network, and found good agreement between the simulation and the data control samples. Finally, we examined the $N N$ distributions in the signal MC for the different $B$ signal channels, rightsign and wrong-sign separately $\left(D \pi, D^{*} \pi, D K, D^{*} K\right)$ and did not observe any significant difference between these channels.

## C. Fitting for event yields and $\mathcal{R}^{(*)}$

The ratios $\mathcal{R}^{(*)}$ are extracted by performing extended unbinned maximum likelihood fits to the set of variables $m_{\mathrm{ES}}, N N$, and $I_{\text {sign }}$, where $I_{\text {sign }}$ is a discrete variable equal to 0 for WS events and to 1 for RS events. We write the extended likelihood $\mathcal{L}$ as

$$
\mathcal{L}=\frac{e^{-N^{\prime}}}{N!} N^{I N} \prod_{j=1}^{N} f\left(\mathbf{x}_{j} \mid \theta\right)
$$

where the vector $\mathbf{x}$ indicates the variables ( $m_{\mathrm{ES}}, N N$, and $I_{\text {sign }}$ ) and $\theta$ indicates the set of parameters which are fitted from the data. $N$ is the total number of signal and background events, and $N^{\prime}=\sum_{i} N_{i}$ is the expectation value for the total number of events. The sum runs over the different
signal and background categories $i$ which will be detailed below. The probability density function (PDF) $f\left(\mathbf{x}_{j} \mid \theta\right)$ is written as the sum over the different signal and background categories

$$
f\left(\mathbf{x}_{j} \mid \theta, N^{\prime}\right)=\frac{\sum_{i} N_{i} f_{i}\left(\mathbf{x}_{j} \mid \theta\right)}{N^{\prime}}
$$

where $f_{i}(\mathbf{x} \mid \theta)$ is the product $F\left(m_{\mathrm{ES}}\right) \times G(N N) \times H\left(I_{\text {sign }}\right)$ of an $m_{\mathrm{ES}}$ component $F\left(m_{\mathrm{ES}}\right)$, a $N N$ component $G(N N)$ and a two-bin histogram $H\left(I_{\text {sign }}\right)$ set to $(1,0)$ for the WS category and $(0,1)$ for the RS category. The $N N$ distributions are all modeled by histograms with 102 bins between -1.02 and 1.02 .

The fits are performed separately to each of the $D \pi$, $D_{D \pi^{0}}^{*} \pi, D_{D \gamma}^{*} \pi, D K, D_{D \pi^{0}}^{*} K$ and $D_{D \gamma}^{*} K$ samples. They are configured in such a way that $\mathcal{R}^{(*)}$ is an explicit fit parameter: for the $B$ signal, we fit for the number of right-sign decays $N_{\mathrm{RS}}$ and the ratio $\mathcal{R}^{(*)}=N_{\mathrm{WS}} /\left(c \times N_{\mathrm{RS}}\right)$, where $N_{\text {WS }}$ is the number of wrong-sign signal events and $c$ is the ratio of the wrong-sign to right-sign selection efficiencies. For $B \rightarrow D^{(*)} K$, the factor $c$ is consistent with unity within the statistical precision of the simulation (Table I) and is set to this value in the fits. For $B \rightarrow D^{(*)} \pi, c$ differs slightly from unity due to different particle identification cuts applied at an early stage of the event selection and we use therefore the values of Table I in the fits.

The following signal and background categories are used to describe each sample in the fits:
(1) The right-sign signal $B^{-} \rightarrow\left[K^{-} \pi^{+}\right]_{D^{(*)}} K^{-} / \pi^{-}$: for $B^{-} \rightarrow D h^{-}$and $B^{-} \rightarrow D_{D \pi^{0}}^{*} h^{-}$events, the $m_{\mathrm{ES}}$ component is parametrized by a Gaussian function $\mathcal{G}_{\text {sig }}\left(m_{\mathrm{ES}}\right)$ whose mean and width are determined from the fit to data. For $B^{-} \rightarrow D_{D \gamma}^{*} h^{-}$events, we use the "Crystal Ball" lineshape [16], an empirical smooth function that better describes the nonGaussian tail on the left side of the distribution. The $N N$ PDF $\mathcal{N} \mathcal{N}_{\text {sig }}$ is constructed from the $N N$ spectrum of the $B^{-} \rightarrow D h^{-}$signal MC.
(2) The wrong-sign signal $B^{-} \rightarrow\left[K^{+} \pi^{-}\right]_{D^{(*)}} K^{-} / \pi^{-}$: its $m_{\mathrm{ES}}$ and $N N$ spectra have the same parametrizations as the right-sign signal.
(3) The right-sign combinatorial background from $q \bar{q}$ $(q=u, d, s, c)$ events into $\left[K^{-} \pi^{+}\right] K^{-}(D K)$ or $\left[K^{-} \pi^{+}\right] \pi^{-}(D \pi)$ : its $m_{\text {ES }}$ component is modeled with the ARGUS function [17] $\mathcal{A}_{q \bar{q}}\left(m_{\mathrm{ES}}\right)$ whose shape and end point parameters, $\zeta_{q \bar{q}}$ and $m_{0}$, are allowed to vary in the fit. The $N N \operatorname{PDF} \mathcal{N} \mathcal{N}_{q \bar{q}}^{(R S)}$ is constructed from the $N N$ spectrum of $\left[K^{-} \pi^{+}\right] K^{-}$ $(D K)$ or $\left[K^{-} \pi^{+}\right] \pi^{-}(D \pi)$ candidates in the $q \bar{q}$ continuum MC (Figs. 2(c) and 2(f)), where the $\Delta E$ requirement has been extended to $|\Delta E|<200 \mathrm{MeV}$ and the $D K$ and $D^{*} K$ (or $D \pi$ and $D^{*} \pi$ ) samples have been summed to increase the statistics.
(4) The wrong-sign combinatorial background from $q \bar{q}$ events into $\left[K^{+} \pi^{-}\right] K^{-}(D K)$ or $\left[K^{+} \pi^{-}\right] \pi^{-}(D \pi)$ : its $m_{\mathrm{ES}}$ component is parameterized by the same ARGUS function $\mathcal{A}_{q \bar{q}}\left(m_{\mathrm{ES}}\right)$ used for the right-sign component. The $N N$ PDF $\mathcal{N} \mathcal{N}_{q \bar{q}}^{(W S)}$ is constructed from the $N N$ spectrum of $\left[K^{+} \pi^{-}\right] K^{-}(D K)$ or $\left[K^{+} \pi^{-}\right] \pi^{-}(D \pi)$ candidates in the $q \bar{q}$ continuum MC (Figs. 2(b) and 2(e)).
(5) The right-sign combinatorial background from $B \bar{B}$ events into $\left[K^{-} \pi^{+}\right] K^{-}(D K)$ or $\left[K^{-} \pi^{+}\right] \pi^{-}(D \pi)$, excluding the peaking background which is considered in category 7: its $m_{\mathrm{ES}}$ component is described by an ARGUS function [17] $\mathcal{A}_{B}^{(\mathrm{RS})}\left(m_{\mathrm{ES}}\right)$ with shape parameter $\zeta_{B}^{(\mathrm{RS})}$ fixed to its value determined from $B \bar{B}$ MC, after removal of the $B \rightarrow D^{(*)} K / \pi$ signal events. The $N N$ PDF used to describe this background is the PDF $\mathcal{N} \mathcal{N}_{\text {sig }}$ describing the $N N$ spectrum of the $B^{-} \rightarrow D^{(*)} h^{-}$signal MC. The number of $B \bar{B}$ right-sign combinatorial background events is allowed to vary in the $D h^{-}$fits but is fixed to the MC prediction in the $D^{*} h^{-}$fits (see below).
(6) The wrong-sign combinatorial background from $B \bar{B}$ events into $\left[K^{+} \pi^{-}\right] K^{-}(D K)$ or $\left[K^{+} \pi^{-}\right] \pi^{-}(D \pi)$, excluding the peaking background which is considered in category 8 : its $m_{\text {ES }}$ component is described by an ARGUS function [17] $\mathcal{A}_{B}^{(\mathrm{WS})}\left(m_{\mathrm{ES}}\right)$ with shape parameter $\zeta_{B}^{(\mathrm{WS})}$ fixed to its value determined from the $B \bar{B}$ MC, after removal of the $B \rightarrow D^{(*)} K / \pi$ signal events. The $N N$ PDF used to describe this background is the PDF $\mathcal{N} \mathcal{N}_{\text {sig }}$ describing the $N N$ spectrum of the $B^{-} \rightarrow D^{(*)} h^{-}$signal MC. The number of $B \bar{B}$ wrong-sign combinatorial background events is allowed to vary in the $D h^{-}$fits but is fixed in the $D^{*} h^{-}$fits (see below).
(7) The background from $B \bar{B}$ events in the right-sign component peaking in $m_{\mathrm{ES}}$ inside the signal region (peaking background): this background is discussed in more detail in Section IV. For the $D K^{ \pm}, D \pi^{ \pm}$ and $D_{D \pi^{0}}^{*} K^{ \pm}$categories, the peaking part of the $B \bar{B}$ background $m_{\mathrm{ES}}$ spectrum is described by the same Gaussian function $\mathcal{G}_{\mathrm{sig}}\left(m_{\mathrm{ES}}\right)$ as the signal. This component is therefore indistinguishable from the signal and its rate has to be fixed to the MC predictions. For the $D_{D \pi^{0}}^{*} \pi^{ \pm}, D_{D \gamma}^{*} \pi^{ \pm}$and the $D_{D \gamma}^{*} K^{ \pm}$ categories, the $m_{\mathrm{ES}}$ component is described by an asymmetric Gaussian whose shape parameters and amplitude for each category are determined from a fit to the $m_{\mathrm{ES}}$ spectrum of $B \bar{B} \mathrm{MC}$ events, after vetoing the $B^{ \pm} \rightarrow D^{(*)} h^{ \pm}$signal component. For all categories, the $N N$ PDF used to describe this background is the PDF $\mathcal{N} \mathcal{N}_{\text {sig }}$ describing the $N N$ spectra of the $B \rightarrow D^{(*)} h^{ \pm}$signal MC.
(8) The peaking background from $B \bar{B}$ events in the wrong-sign component: the treatment is similar to the previous component but $\mathcal{G}_{\text {sig }}\left(m_{\mathrm{ES}}\right)$ is used to describe the $m_{\text {ES }}$ spectrum of the $D K^{ \pm}, D \pi^{ \pm}$, $D_{D \pi^{0}}^{*} K^{ \pm}$and $D_{D \gamma}^{*} K^{ \pm}$categories, while an asymmetric Gaussian is used to describe the $m_{\mathrm{ES}}$ spectrum of the $D_{D \pi^{0}}^{*} \pi^{ \pm}$and $D_{D \gamma}^{*} \pi^{ \pm}$categories.
To summarize, we fit for the number of right-sign signal events $N_{\mathrm{RS}}$, the ratio $\mathcal{R}=N_{\mathrm{WS}} /\left(c \times N_{\mathrm{RS}}\right)$ of wrong-sign to right-sign events, the number of wrong-sign and rightsign $q \bar{q}$ combinatorial background events, $N_{\mathrm{WS}}^{(q \bar{q})}$ and $N_{\mathrm{RS}}^{(q \bar{q})}$, and for $D h^{ \pm}$the number of wrong-sign and right-sign $B \bar{B}$ combinatorial background events, $N_{\mathrm{WS}}^{(B \bar{B})}$ and $N_{\mathrm{RS}}^{(B \bar{B})}$. We fix to their MC expectations the numbers of wrong-sign and right-sign $B \bar{B}$ peaking background, $N_{\text {WS }}^{(B \bar{B}, p k)}$ and $N_{\mathrm{RS}}^{(B \bar{B}, p k)}$, as well as the number of $B \bar{B}$ combinatorial background events for $D^{*} h^{ \pm}$. The other parameters fitted are the reconstructed $m_{\mathrm{ES}}$ peak and resolution, $m_{B}$ and $\sigma_{m_{B}}$, and the $q \bar{q}$ continuum background shape parameter and end point, $\zeta_{q \bar{q}}$ and $m_{0}$.

## IV. STUDY OF $\boldsymbol{B} \overline{\boldsymbol{B}}$ BACKGROUNDS

We study the $B \bar{B}$ background for each signal category ( $D \pi, D^{*} \pi D K, D^{*} K$ ) and charge combination (right-sign and wrong-sign) using a sample of $e^{+} e^{-} \rightarrow Y(4 S) \rightarrow B \bar{B}$ MC events corresponding to about 3 times the data luminosity. In addition, dedicated Monte Carlo signal samples are used to estimate the background from $B^{-} \rightarrow D h^{-}$ events and the background from the charmless decay $B^{-} \rightarrow K^{+} \pi^{-} K^{-}$. We identify three main classes of background events which can peak in $m_{\mathrm{ES}}$ inside the signal region and mimic the $D^{(*)} \pi$ and $D^{(*)} K$ signal:
(1) Charmless $B$ decays $B^{-} \rightarrow h^{+} h^{-} h^{-}(h=\pi, K)$ : we list in Table II the 3-body charmless decays affecting our analysis, their branching fractions [14] and the numbers of reconstructed events expected in the affected modes after the selection. Because of the particle identification criteria used in the analysis only decays with the same final state particles as our signal modes contribute significantly to the background. These events are indistinguishable from the $D h^{ \pm}$signal if the $K^{-} \pi^{+}$invariant mass is consistent with the $D$ mass. The two decays

TABLE II. Charmless background channels and branching fractions, $D h^{ \pm}$channels affected by this background and background yields expected in our data sample.

| Mode | Affected <br> channel | $\mathcal{B}\left(10^{-6}\right)$ | Estimated <br> Yield |
| :--- | :---: | :---: | :---: |
| $K^{-} \pi^{+} \pi^{-}$ | $D \pi$ RS | $55 \pm 7[14]$ | $67.1 \pm 9.7$ |
| $K^{+} \pi^{-} \pi^{-}$ | $D \pi$ WS | $<0.9[18]$ | $<1.1$ |
| $K^{-} \pi^{+} K^{-}$ | $D K \mathrm{RS}$ | $<0.2[18]$ | $<0.2$ |
| $K^{+} \pi^{-} K^{-}$ | $D K$ WS | $5.0 \pm 0.7[19]$ | $6.0 \pm 0.8$ |

affected by a significant charmless background are right-sign $B^{-} \rightarrow\left[K^{-} \pi^{+}\right]_{D} \pi^{-}$and wrong-sign $B^{-} \rightarrow\left[K^{+} \pi^{-}\right]_{D} K^{-}$. Using $B^{-} \rightarrow K^{-} \pi^{+} \pi^{-}$events selected in the $B \bar{B}$ Monte Carlo sample, we estimate the efficiency of $B^{-} \rightarrow K^{-} \pi^{+} \pi^{-}$events to be reconstructed as a $\left[K^{-} \pi^{+}\right]_{D} \pi^{-}$candidate as $(0.26 \pm$ $0.02) \%$. The corresponding background is estimated to be $67.1 \pm 9.7$ events, where the error is dominated by the statistical uncertainty on the $B^{-} \rightarrow$ $K^{-} \pi^{+} \pi^{-}$branching fraction. The efficiency of $B^{-} \rightarrow K^{+} \pi^{-} K^{-}$events to be reconstructed as $\left[K^{+} \pi^{-}\right]_{D} K^{-}$WS candidates is determined from a high statistics dedicated $B^{-} \rightarrow K^{+} \pi^{-} K^{-}$signal Monte Carlo sample, and is found to be ( $0.27 \pm$ $0.01) \%$. The corresponding peaking background from $B^{-} \rightarrow K^{+} \pi^{-} K^{-}$events mimicking $B^{-} \rightarrow$ $\left[K^{+} \pi-\right]_{D} K^{-} \quad$ WS decays is estimated to be $6.0 \pm 0.8$ events, where the error is dominated by the statistical uncertainty on the $B^{-} \rightarrow K^{+} \pi^{-} K^{-}$ branching fraction. From a fit to data selected in the $D$ mass sidebands, we cross-check this prediction and find $6.5 \pm 4.0$ peaking events, in good agreement with the MC prediction. We also check that, because of the tight $\Delta m$ cut applied to the $D^{*}$ decay products, the $B^{-} \rightarrow D^{*} h^{-}$channels are not affected by charmless peaking backgrounds.
(2) Events of the type $B^{-} \rightarrow D h^{-}$: this background is estimated by running the analysis on a sample of $B^{-} \rightarrow D h^{-}$signal MC events properly renormalized to the data sample, and fitting the $m_{\mathrm{ES}}$ spectra of the selected events to the sum of a Gaussian signal and a combinatorial background. We find that a peaking background of $2.6 \pm 0.4$ events is predicted in the $B^{-} \rightarrow\left[K^{+} \pi-\right]_{D} K^{-}$WS channel. This component is dominated (2 events out of 2.6) by decays $B^{-} \rightarrow\left[K^{-} K^{+}\right]_{D} \pi^{-}$failing the $D$ mass veto and by WS decays $B^{-} \rightarrow\left[K^{+} \pi^{-}\right]_{D} \pi^{-}$where the $\pi^{-}$is misidentified as a $K^{-}$. For the $D^{*} K$ channels, the $B^{-} \rightarrow\left[K^{-} K^{+}\right]_{D} \pi^{-}$contribution is suppressed by the $\Delta m$ cut on the $D^{*}-D$ mass difference, and the WS $D^{*} \pi$ contribution is $0.5 \pm 0.1$ events for $D^{*} \rightarrow D \pi^{0}$ and $0.6 \pm 0.2$ events for $D^{*} \rightarrow D \gamma$. Another background of the same type occurs in the right-sign $D K$ decays. It consists of events $B^{-} \rightarrow\left[K^{-} \pi^{+}\right]_{D^{(*)}} \pi^{-}$where the bachelor $\pi^{-}$ is misidentified as a $K^{-}$, which fake the RS signal $B^{-} \rightarrow\left[K^{-} \pi^{+}\right]_{D^{(*)}} K^{-}$. This contribution is predicted by the simulation and has been verified in the data by fitting the $\Delta E$ spectrum of $D^{(*)} K$ candidates in the $m_{\text {ES }}$ signal region, which shows a second peak due to $D^{(*)} \pi$ candidates, shifted by 50 MeV with respect to the signal.
(3) Other decays: this component is estimated by fitting the $m_{\mathrm{ES}}$ spectra of $B \bar{B}$ MC events, after removing the charmless and $B^{-} \rightarrow D h^{-}$components. For

TABLE III. Expected numbers of signal and $B \bar{B}$ background events, peaking background parametrization and dominant sources of peaking backgrounds for $B \rightarrow D^{(*)} \pi$ and $B \rightarrow D^{(*)} K . N_{B \bar{B}}^{(\text {comb) }}$ is the combinatorial part of the background, parametrized by an ARGUS function, and $N_{B \bar{B}}^{(\text {peak })}$ is the component peaking in $m_{\mathrm{ES}}$, parametrized by either a Gaussian function or a bifurcated Gaussian function. The average event yield expected for the WS signal is computed assuming $r_{B}^{(*)}=10 \%$ and no interference term $(\cos \gamma \times \cos \delta=0)$.

| Mode | Signal yield | $N_{B \bar{B}}^{(\text {comb })}$ | $N_{B \bar{B}}^{\text {(peak) }}$ | Peaking background parametrization | Peaking background sources |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $D \pi^{-}$WS | 86 | $94 \pm 6$ | $11 \pm 3$ | Gaussian | $D_{0}^{*-} e^{+} \nu_{e}$ |
| $D_{D \pi^{0}}^{*} \pi^{-}$WS | 31 | $25 \pm 8$ | $29 \pm 9$ | Bifurcated Gaussian | $D_{0}^{*-} e^{+} \nu_{e}, D_{1}^{\prime-} e^{+} \nu_{e}$ |
| $D_{D \gamma}^{* * \pi} \pi^{-}$WS | 25 | $111 \pm 9$ | $47 \pm 7$ | Bifurcated Gaussian | $D_{0}^{*-} e^{+} \nu_{e}, D_{1}^{\prime-} e^{+} \nu_{e}$, and $D^{(*) 0} \rho^{0}$ |
| $D \pi^{-} \mathrm{RS}$ | 24240 | $307 \pm 12$ | $222 \pm 10$ | Gaussian | $K^{-} \pi^{+} \pi^{-},(c \bar{c}) K^{-}$ |
| $D_{D \pi^{0}}^{*} \pi^{-} \mathrm{RS}$ | 8931 | $621 \pm 34$ | $507 \pm 33$ | Bifurcated Gaussian | $D^{*} \rho^{-}, D^{*+} \pi^{-}$ |
| $D_{D \gamma}^{* *} \pi^{-} \mathrm{RS}$ | 7242 | $1225 \pm 64$ | $2432 \pm 67$ | Bifurcated Gaussian | $D^{*} \rho^{-}, D^{*+} \pi^{-}$, and $D_{D \pi^{0}}^{*} \pi^{-}$ |
| DK ${ }^{-}$WS | 26 | $107 \pm 6$ | $13 \pm 3$ | Gaussian | $D h^{-}, K^{-} K^{+} \pi^{-}$ |
| $D_{D \pi^{0}}^{*} K^{-}$WS | 9 | $17 \pm 3$ | $3 \pm 2$ | Gaussian | - |
| $D_{D \gamma}^{*} K^{-} \mathrm{WS}$ | 7 | $68 \pm 5$ | $6 \pm 2$ | Gaussian | - |
| $D K^{-} \mathrm{RS}$ | 1944 | $51 \pm 5$ | $299 \pm 11$ | Gaussian | $D \pi^{-}$ |
| $D_{D \pi^{0}}^{*} K^{-} \mathrm{RS}$ | 618 | $56 \pm 7$ | $127 \pm 8$ | Gaussian | $D_{D \pi^{0}}^{*} \pi^{-}$ |
| $\underline{D}_{\text {D } \gamma}^{*} K^{-} \mathrm{RS}$ | 503 | $66 \pm 15$ | $327 \pm 17$ | Bifurcated Gaussian | $D_{D \gamma}^{*} \pi^{-}, D_{D \pi^{0}}^{*} K^{-}$ |

$B^{-} \rightarrow\left[K^{+} \pi^{-}\right]_{D} K^{-}$WS decays, the peaking component is estimated to be $4 \pm 3$ events, where the uncertainty is dominated by the statistical error on the simulated data. The main sources of peaking background which could be identified are listed in Table III. They include $\bar{B}^{0} \rightarrow D^{*+} h^{-}$reconstructed as $B^{-} \rightarrow D^{* 0} h^{-}$, semileptonic decays $B^{0} \rightarrow$ $D^{* *-} e^{+} \bar{\nu}_{e}\left(D^{* *-} \rightarrow \bar{D}^{(*) 0} \pi^{-}, \bar{D}^{0} \rightarrow K^{+} \pi^{-}\right)$where the $e^{+}$is missed, faking the WS signal $B^{-} \rightarrow$ $\left[K^{+} \pi^{-}\right]_{D^{(*)}} \boldsymbol{\pi}^{-}$, and decays $B^{-} \rightarrow D^{(*)} \rho^{-}$faking the RS signal $B^{-} \rightarrow\left[K^{-} \pi^{+}\right]_{D^{(*)}} \pi^{-}$. The $D^{* *-}$ states contributing in the $B^{0} \rightarrow D^{* *-} e^{+} \bar{\nu}_{e}$ peaking background to $B^{-} \rightarrow\left[K^{+} \pi^{-}\right]_{D^{(*)}} \pi^{-}$were found to be dominantly the wide P-wave states $D_{0}^{*-}$ and $D_{1}^{\prime-}$. A $50 \%$ relative error on the $B^{0} \rightarrow D^{* *-} e^{+} \bar{\nu}_{e}$ decay rates was assumed when computing the associated systematic uncertainty on $\mathcal{R}_{D \pi}^{(*)}$.
A summary of the $B \bar{B}$ background studies is given in Table III, for $B \rightarrow D^{(*)} \pi$ and $B \rightarrow D^{(*)} K$. For each channel, the $m_{\text {ES }}$ spectra of events selected in the $B \bar{B}$ MC simulation (after removing the corresponding signal) were fitted by the sum of a combinatorial background component and a peaking component, using the same parametrization described in Sec. IIIC. The average number of $B \bar{B}$ combinatorial and peaking background events predicted by the simulation are given in Table III, together with the main sources of peaking events and the functional shapes chosen to describe the peaking background. The numbers of signal events expected are also given for comparison. For the $B \rightarrow D^{*} K$ WS channels, we could not identify a specific source of peaking background due to the lack of statistics in the simulation. For all channels, we use the values of the peaking components summarized in Table III in the maximum likelihood fit. Statistical uncertainties in the expected yields are incorporated in the corresponding systematic uncertainties.

## V. RESULTS

## A. Results for $\boldsymbol{B} \rightarrow \boldsymbol{D}^{(*)} \boldsymbol{\pi}$

The results for $B \rightarrow D^{(*)} \pi$ are displayed in Fig. 3 (rightsign modes) and Fig. 4 (wrong-sign modes). They are summarized in Table IV. Clear signals are observed in the $B \rightarrow D \pi$ and in the $B \rightarrow D_{D \pi^{0}}^{*} \pi$ WS modes, with statistical significances of $7 \sigma$ and $4.8 \sigma$, respectively. The significance is defined as $\sqrt{-2 \ln \left(\mathcal{L}_{0} / \mathcal{L}_{\text {max }}\right)}$, where $\mathcal{L}_{\text {max }}$ and $\mathcal{L}_{0}$ are the likelihood values with the nominal and with zero WS signal yield, respectively. For $B \rightarrow D_{D \gamma}^{*} \pi$ WS decays, the significance is only $2 \sigma$, due to the large peaking background. Below we discuss the sources of systematic uncertainties that contribute to our $\mathcal{R}_{D \pi}^{(*)}$ measurements:
(1) Signal $N N$ shape: in the nominal fit, we use the $N N$ PDF from the $B$ signal MC. To estimate the related systematics, we refit the data using a signal $N N$ PDF extracted from the high purity and high statistics $B \rightarrow D \pi$ RS data, after subtracting the residual continuum background contamination predicted by the simulation. We set the systematic uncertainty to the difference with the nominal fit result.
(2) $B$ background $N N$ shape: from a study of generic $B \bar{B} \mathrm{MC}$, it appears that the $N N$ spectra of $B$ background events in the $m_{\mathrm{ES}}-\Delta E$ signal box are similar to the signal (but suffer from very low statistics), while the $N N$ spectra of background events in an enlarged $m_{\mathrm{ES}}-\Delta E$ region differ significantly from the signal and show less peaking close to 1 . In the nominal fit we assumed that both the peaking and the nonpeaking $B \bar{B}$ background components could be described by the $B \rightarrow D \pi$ signal $N N$ PDF. To estimate the related systematic error, we used $B \bar{B}$ generic background events selected in a $\Delta E-m_{\mathrm{ES}}$ enlarged window $|\Delta E|<200 \mathrm{MeV}$ and


FIG. 3 (color online). Projections on $m_{\mathrm{ES}}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ and $N N(\mathrm{~d}, \mathrm{e}, \mathrm{f})$ of the fit results for $D \pi(\mathrm{a}, \mathrm{d}), D_{D \pi^{0}}^{*} \pi(\mathrm{~b}, \mathrm{e})$ and $D_{D \gamma}^{*} \pi(\mathrm{c}, \mathrm{f})$ RS decays, for samples enriched in signal with the requirements $N N>0.94$ ( $m_{\mathrm{ES}}$ projections) or $5.2725<m_{\mathrm{ES}}<5.2875 \mathrm{GeV} / c^{2}$ ( $N N$ projections). The points with error bars are data. The curves represent the fit projections for signal plus background (solid) and background (dashed).
$m_{\mathrm{ES}}>5.20 \mathrm{GeV} / c^{2}$ to build the $N N$ PDF of the nonpeaking part of the $B \bar{B}$ background (keeping the signal $N N$ PDF to describe the peaking part of this background) and repeated the fits, taking the
difference of the results as the associated systematic uncertainty.
(3) Continuum background $N N$ shape: to account for possible differences between the simulation and the


FIG. 4 (color online). Projections on $m_{\text {ES }}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ and $N N(\mathrm{~d}, \mathrm{e}, \mathrm{f})$ of the fit results for $D \pi(\mathrm{a}, \mathrm{d}), D_{D \pi^{0}}^{*} \pi(\mathrm{~b}, \mathrm{e})$ and $D_{D \gamma}^{*} \pi(\mathrm{c}, \mathrm{f})$ WS decays, for samples enriched in signal with the requirements $N N>0.94$ ( $m_{\mathrm{ES}}$ projections) or $5.2725<m_{\mathrm{ES}}<5.2875 \mathrm{GeV} / c^{2}$ ( $N N$ projections). The curves represent the fit projections for signal plus background (solid), the sum of all background components (dashed), and $q \bar{q}$ background only (dotted).

TABLE IV. Summary of fit results for $D^{(*)} \pi$.

| Mode | $D \pi$ | $D_{D \pi^{0}}^{*} \pi$ | $D_{D \gamma}^{*} \pi$ |
| :--- | :---: | :---: | :---: |
| Ratio of rates, $\mathcal{R}_{D \pi}^{(*)}\left(10^{-3}\right)$ | $3.3 \pm 0.6$ | $3.2 \pm 0.9$ | $2.7 \pm 1.4$ |
| Number of signal events $N_{\text {WS }}$ | $80 \pm 14$ | $28 \pm 8$ | $19 \pm 10$ |
| Number of normalization events $N_{\mathrm{RS}}$ | $24662 \pm 160$ | $9296 \pm 102$ | $7214 \pm 105$ |
| $B^{+}$ratio of rates, $\mathcal{R}_{D \pi}^{(*)+}\left(10^{-3}\right)$ | $3.2 \pm 0.8$ | $3.5 \pm 1.2$ | $4.6 \pm 2.2$ |
| $B^{-}$ratio of rates, $\mathcal{R}_{D \pi}^{(*)-}\left(10^{-3}\right)$ | $3.4 \pm 0.8$ | $2.9 \pm 1.2$ | $1.0 \pm 1.8$ |
| Asymmetry $\mathcal{A}_{D \pi}^{(*)}$ | $0.03 \pm 0.17$ | $-0.09 \pm 0.27$ | $-0.65 \pm 0.55$ |

data, we used the $N N$ spectrum from off-peak data instead of $q \bar{q} \mathrm{MC}(q=u, d, s, c)$ to model this component. We set the associated systematic uncertainty to the difference of the two results, but the error is dominated by the large statistical uncertainty on the off-peak data sample.
(4) The shape parameters $\zeta_{B}^{(\mathrm{WS})}$ and $\zeta_{B}^{(\mathrm{RS})}$ of the ARGUS functions describing the suppressed and favored $B \bar{B}$ combinatorial background: in the nominal fits, these parameters are fixed to their values as determined from $B \bar{B}$ simulated events. To account for possible disagreement between data and simulation, we repeated the fits varying these parameters in a conservative range.
(5) Peaking component in the $B$ background: we varied the yield of the peaking component by $\pm 1 \sigma$, where $\sigma$ is either the statistical error from a fit to generic $B \bar{B}$ MC or the uncertainty on the branching fraction for known sources of peaking background.
(6) Uncertainty on the number of $B \bar{B}$ combinatorial background events: in the $D^{*} \pi$ (and $D^{*} K$ ) fits where this component has been fixed, we vary it by $\pm 25 \%$ (the level of agreement between data and simulation observed in the $D \pi$ and $D K$ fits) and we take the difference with the nominal fit result as a systematic uncertainty.

Model uncertainties, like the fit model used to parametrize the $m_{\mathrm{ES}} \mathrm{PDF}$, or the number of bins in the neural network PDF histogram, are found to be much smaller and are neglected. The resulting systematic uncertainties are listed
in Table V. We add them in quadrature and quote the results:

$$
\begin{aligned}
\mathcal{R}_{D \pi} & =(3.3 \pm 0.6 \pm 0.4) \times 10^{-3} \\
\mathcal{R}_{\left(D \pi^{0}\right) \pi}^{*} & =(3.2 \pm 0.9 \pm 0.8) \times 10^{-3}, \\
\mathcal{R}_{(D \gamma) \pi}^{*} & =(2.7 \pm 1.4 \pm 2.2) \times 10^{-3}
\end{aligned}
$$

where the first uncertainty is statistical and the second is systematic. The values of $\mathcal{R}_{D \pi}^{(*)}$ are in good agreement with the world average $R_{D}=r_{D}^{2}=\mathcal{B}\left(D^{0} \rightarrow K^{+} \pi^{-}\right) / \mathcal{B}\left(D^{0} \rightarrow\right.$ $\left.K^{-} \pi^{+}\right), R_{D}=(3.36 \pm 0.08) \times 10^{-3}$ [8].

A separate fit to $B^{+}$and $B^{-}$candidates provides a measurement of the corresponding asymmetries. We obtain the following results:

$$
\begin{aligned}
\mathcal{A}_{D \pi} & =0.03 \pm 0.17 \pm 0.04 \\
\mathcal{A}_{\left(D \pi^{0}\right) \pi}^{*} & =-0.09 \pm 0.27 \pm 0.05 \\
\mathcal{A}_{(D \gamma) \pi}^{*} & =-0.65 \pm 0.55 \pm 0.22
\end{aligned}
$$

where the uncertainties are dominated by the statistical error. No significant asymmetry is observed for the $D^{(*)} \pi$ WS decays. The largest source of systematic uncertainty on the $D^{(*)} \pi$ asymmetries is from the uncertainty on the $B$ background peaking component.

## B. Results for $\boldsymbol{B} \rightarrow \boldsymbol{D}^{(*)} \boldsymbol{K}$

The results for $B \rightarrow D^{(*)} K$ are displayed in Fig. 5 (RS modes) and Fig. 6 (WS modes). They are summarized in Table VI. Indications of signals are observed in the

TABLE V. Summary of systematic uncertainties on $\mathcal{R}$ for $D^{(*)} \pi$, in units of $10^{-3}$.

|  | $\Delta \mathcal{R}\left(10^{-3}\right)$ | $\Delta \mathcal{R}\left(10^{-3}\right)$ | $\Delta \mathcal{R}\left(10^{-3}\right)$ |
| :--- | :---: | :---: | :---: |
| Source | $D \pi$ | $D_{D \pi^{0}}^{*} \pi$ | $D_{D \gamma}^{*} \pi$ |
| Signal $N N$ | $\pm 0.1$ | $\pm 0.1$ | $\pm 0.1$ |
| $B \bar{B}$ background $N N$ | $\pm 0.1$ | $\pm 0.1$ | $\pm 0.9$ |
| udsc background $N N$ | $\pm 0.1$ | $\pm 0.1$ | $\pm 0.3$ |
| $B \bar{B}$ combinatorial background shape $\left(m_{\mathrm{ES}}\right)$ | $\pm 0.2$ | $\pm 0.1$ | $\pm 0.2$ |
| Peaking background WS | $\pm 0.2$ | $\pm 0.8$ | $\pm 2.0$ |
| Peaking background RS | $\pm 0.0$ | $\pm 0.1$ | $\pm 0.1$ |
| $B \bar{B}$ combinatorial background | - | $\pm 0.0$ | $\pm 0.4$ |
| Combined | $\pm 0.4$ | $\pm 0.8$ | $\pm 2.2$ |



FIG. 5 (color online). Projections on $m_{\mathrm{ES}}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ and $N N(\mathrm{~d}, \mathrm{e}, \mathrm{f})$ of the fit results for $D K(\mathrm{a}, \mathrm{d}), D_{D \pi^{0}}^{*} K(\mathrm{~b}, \mathrm{e})$ and $D_{D \gamma}^{*} K(\mathrm{c}, \mathrm{f}) \mathrm{RS}$ decays, for samples enriched in signal with the requirements $N N>0.94$ ( $m_{\mathrm{ES}}$ projections) or $5.2725<m_{\mathrm{ES}}<5.2875 \mathrm{GeV} / c^{2}$ ( $N N$ projections). The points with error bars are data. The curves represent the fit projections for signal plus background (solid) and background (dashed).


FIG. 6 (color online). Projections on $m_{\mathrm{ES}}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ and $N N(\mathrm{~d}, \mathrm{e}, \mathrm{f})$ of the fit results for $D K(\mathrm{a}, \mathrm{d}), D_{D \pi^{0}}^{*} K(\mathrm{~d}, \mathrm{e})$ and $D_{D \gamma}^{*} K(\mathrm{c}, \mathrm{f})$ WS decays, for samples enriched in signal with the requirements $N N>0.94$ ( $m_{\mathrm{ES}}$ projections) or $5.2725<m_{\mathrm{ES}}<5.2875 \mathrm{GeV} / c^{2}$ ( $N N$ projections). The points with error bars are data. The curves represent the fit projections for signal plus background (solid), the sum of all background components (dashed), and $q \bar{q}$ background only (dotted).

TABLE VI. Summary of fit results for $D^{(*)} K$.

| Mode | $D K$ | $D_{D \pi^{0}}^{*} K$ | $D_{D \gamma}^{*} K$ |
| :--- | :---: | :---: | :---: |
| Ratio of rates, $\mathcal{R}_{D K}^{(*)}\left(10^{-2}\right)$ | $1.1 \pm 0.6$ | $1.8 \pm 0.9$ | $1.3 \pm 1.4$ |
| No. of signal events $N_{\mathrm{WS}}$ | $19 \pm 10$ | $10 \pm 5$ | $6 \pm 6$ |
| No. of normalization events $N_{\mathrm{RS}}$ | $1755 \pm 48$ | $587 \pm 28$ | $455 \pm 29$ |
| $B^{+}$Ratio of rates, $\mathcal{R}_{D K K}^{(*)+}\left(10^{-2}\right)$ | $2.2 \pm 0.9$ | $0.5 \pm 0.8$ | $0.9 \pm 1.6$ |
| $B^{-}$Ratio of rates, $\mathcal{R}_{D K}^{(*)-}\left(10^{-2}\right)$ | $0.2 \pm 0.6$ | $3.7 \pm 1.8$ | $1.9 \pm 2.3$ |
| Asymmetry $\mathcal{A}_{D K}^{(*)}$ | $-0.86 \pm 0.47$ | $0.77 \pm 0.35$ | $0.36 \pm 0.94$ |

$B \rightarrow D K$ and in the $B \rightarrow D_{D \pi^{0}}^{*} K$ WS modes, with statistical significances of $2.2 \sigma$ and $2.4 \sigma$, respectively, (Fig. 7). Accounting for the systematic uncertainties, the significances become $2.1 \sigma$ and $2.2 \sigma$, respectively. For $B \rightarrow D_{D \gamma}^{*} K$ WS, no significant signal is observed.

The systematic uncertainties have been estimated by testing different fit models and recomputing $\mathcal{R}_{D K}^{(*)}$, as explained in Section VA. A summary of the different systematic uncertainties is given in Table VII. The uncertainties on the $N N$ describing the $B \bar{B}$ combinatorial background and the uncertainties on the $B \bar{B}$ peaking background are the two main contributions. For $B^{ \pm} \rightarrow D K^{ \pm}$, we find for the ratio of the WS to RS decay rates

$$
\mathcal{R}_{D K}=(1.1 \pm 0.6 \pm 0.2) \times 10^{-2}
$$

Expressed in terms of event yields, the fit result is $19.4 \pm$ $9.6 \pm 3.5 \mathrm{WS}$ events. The results of fits to separate $B^{+} \rightarrow$ $D K^{+}$and $B^{-} \rightarrow D K^{-}$data samples are given in Table VI. Projections of the fits to $B^{+}$and $B^{-}$data are shown in Figs. 8 and 9, respectively. We fit $\mathcal{R}_{D K}^{+}=(2.2 \pm 0.9 \pm$ $0.3) \times 10^{-2}$ for the $B^{+}$sample, corresponding to $19.2 \pm$ $7.9 \pm 2.6$ events. On the contrary, no significant WS signal is observed for the $B^{-}$sample, and we fit $\mathcal{R}_{D K}^{-}=(0.2 \pm$ $0.6 \pm 0.2) \times 10^{-2}$. The statistical correlation between $\mathcal{R}_{D K}^{+}$and $\mathcal{R}_{D K}^{-}$(or $\mathcal{R}_{D K}$ and $\mathcal{A}_{D K}$ ) is insignificant.

The systematic errors on the asymmetries are estimated using the method discussed previously. The main systematic
error on $\mathcal{A}_{D K}$ is from the uncertainty on the number of peaking $B$ background events for the WS channel. This source contributes $+0.11-0.14$ to $\mathcal{A}_{D K}$, and $\pm 0.08 \times 10^{-2}$ to $\mathcal{R}_{D K}$, where the changes in the two quantities are $100 \%$ negatively correlated (increasing the peaking background increases $\mathcal{A}_{D K}$ but decreases $\mathcal{R}_{D K}$ ). The other sources of systematic uncertainty considered in Table VII are $100 \%$ correlated between $\mathcal{R}^{+}$and $\mathcal{R}^{-}$, and mostly cancel in the asymmetry calculation. By comparing the number of $B^{+}$and $B^{-}$events reconstructed in the $\left[K^{ \pm} \pi^{\mp}\right]_{D} \pi^{ \pm}$analysis, where no significant asymmetry is expected, the uncertainty due to the detector charge asymmetry is estimated to be below the $1 \%$ level. Finally, we also account for a possible asymmetry of the charmless $B^{ \pm} \rightarrow$ $K^{ \pm} K^{\mp} \pi^{ \pm}$peaking background. The asymmetry of this background has been measured to be $0 \pm 10 \%$ [19] and we estimate the corresponding systematic uncertainty by assuming a $\pm 10 \%$ asymmetry of this background. The final result for the asymmetry is

$$
\mathcal{A}_{D K}=-0.86 \pm 0.47_{-0.16}^{+0.12}
$$

For $B^{ \pm} \rightarrow D_{D \pi^{0}}^{*} K^{ \pm}$, we find for the ratio of the WS to RS decay rates

$$
\mathcal{R}_{\left(D \pi^{0}\right) K}^{*}=(1.8 \pm 0.9 \pm 0.4) \times 10^{-2}
$$

Expressed in terms of event yields, the fit result is $10.3 \pm$ $5.5 \pm$ 2.4 WS events. The results of fits to separate $B^{+} \rightarrow$


FIG. 7. Negative log-likelihood variation vs $\mathcal{R}_{D K}^{(*)}$ for $B^{ \pm} \rightarrow D K^{ \pm}$(left), $B^{ \pm} \rightarrow D_{D \pi^{0}}^{*} K^{ \pm}$(center) and $B^{ \pm} \rightarrow D_{D \gamma}^{*} K^{ \pm}$(right). Systematic uncertainties are not included.

TABLE VII. Summary of systematic uncertainties on $\mathcal{R}$ for $D^{(*)} K$, in units of $10^{-2}$.

| Error source | $\Delta \mathcal{R}\left(10^{-2}\right)$ | $\Delta \mathcal{R}\left(10^{-2}\right)$ | $\Delta \mathcal{R}\left(10^{-2}\right)$ |
| :--- | :---: | :---: | :---: |
|  | $D K$ | $D_{D \pi^{0}}^{*} K$ | $D_{D \gamma}^{*} K$ |
| Signal $N N$ | $\pm 0.1$ | $\pm 0.1$ | $\pm 0.3$ |
| $B \bar{B}$ background $N N$ | $\pm 0.1$ | $\pm 0.3$ | $\pm 0.4$ |
| $q \bar{q}$ background $N N$ | $\pm 0.1$ | $\pm 0.1$ | $\pm 0.1$ |
| $B \bar{B}$ combinatorial background shape $\left(m_{\mathrm{ES}}\right)$ | $\pm 0.1$ | $\pm 0.1$ | $\pm 0.1$ |
| Peaking background WS | $\pm 0.2$ | $\pm 0.3$ | $\pm 0.6$ |
| Peaking background RS | $\pm 0.0$ | $\pm 0.1$ | $\pm 0.1$ |
| Floating $B \bar{B}$ combinatorial background | - | $\pm 0.1$ | $\pm 0.2$ |
| Combined | $\pm 0.2$ | $\pm 0.4$ | $\pm 0.8$ |

$D^{*} K^{+}$and $B^{-} \rightarrow D^{*} K^{-}$data samples are given in Table VI. Projections of the fits to $B^{+}$and $B^{-}$data are shown in Figs. 8 and 9, respectively. We find $\mathcal{R}_{\left(D \pi^{0}\right) K}^{*-}=(3.7 \pm 1.8 \pm 0.9) \times$ $10^{-2}$ for the $B^{-}$sample, corresponding to $10.2 \pm 4.8 \pm 2.4$ events. On the contrary, no significant WS signal is observed for the $B^{+}$sample, and we find $\mathcal{R}_{\left(D \pi^{0}\right) K}^{*+}=(0.5 \pm 0.8 \pm$ $0.3) \times 10^{-2}$. The systematic errors are estimated using the same method as for $B^{ \pm} \rightarrow D K^{ \pm}$, separately for $B^{+}$and $B^{-}$ events. The main systematic error on the asymmetry $\mathcal{A}_{\left(D \pi^{0}\right) K}^{*}$ is from the uncertainty on the number of peaking $B$ background events for the WS channel. This source contributes $\pm 0.09$ to $\mathcal{A}_{\left(D \pi^{0}\right) K}^{*}$, and $\mp 0.3 \times 10^{-2}$ to $\mathcal{R}_{\left(D \pi^{0}\right) K}^{*}$, where the two quantities are anticorrelated. The other sources of systematic uncertainties mostly cancel in the asymmetry calculation, because they induce relative changes on $\mathcal{R}^{*+}$
and $\mathcal{R}^{*-}$ which are $100 \%$ correlated. The final result for the asymmetry is

$$
\mathcal{A}_{\left(D \pi^{0}\right) K}^{*}=+0.77 \pm 0.35 \pm 0.12
$$

The asymmetry for $D_{D \pi^{0}}^{*} K$ has the opposite sign to the asymmetry for $D K$, in agreement with the shift of approximately $180^{\circ}$ between $\delta_{B}$ and $\delta_{B}^{*}$ suggested by the measurements of Refs. [5,7].

For $B \rightarrow D_{D \gamma}^{*} K$, we have no significant signal and fit

$$
\mathcal{R}_{(D \gamma) K}^{*}=(1.3 \pm 1.4 \pm 0.8) \times 10^{-2}
$$

Expressed in terms of event yields, this result corresponds to $5.9 \pm 6.4 \pm 3.2$ events $D_{D \gamma}^{*} K$ WS. We fit $211 \pm 19 \mathrm{RS}$ $B^{-}$events and $244 \pm 20 \mathrm{RS} B^{+}$events, and find for the WS to RS ratios $\mathcal{R}_{(D \gamma) K}^{*-}=(1.9 \pm 2.3 \pm 1.2) \times 10^{-2}$ and


FIG. 8 (color online). Projections on $m_{\mathrm{ES}}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ and $N N(\mathrm{~d}, \mathrm{e}, \mathrm{f})$ of the fit results for $D K^{+}(\mathrm{a}, \mathrm{d}), D_{D \pi^{0}}^{*} K^{+}(\mathrm{b}, \mathrm{e})$ and $D_{D \gamma}^{*} K^{+}(\mathrm{c}, \mathrm{f})$ WS decays, for samples enriched in signal with the requirements $N N>0.94$ ( $m_{\mathrm{ES}}$ projections) or $5.2725<m_{\mathrm{ES}}<5.2875 \mathrm{GeV} / c^{2}$ ( $N N$ projections). The points with error bars are data. The curves represent the fit projections for signal plus background (solid), the sum of all background components (dashed), and $q \bar{q}$ background only (dotted).


FIG. 9 (color online). Projections on $m_{\text {ES }}(\mathrm{a}, \mathrm{b}, \mathrm{c})$ and $N N(\mathrm{~d}, \mathrm{e}, \mathrm{f})$ of the fit results for $D K^{-}(\mathrm{a}, \mathrm{d}), D_{D \pi^{0}}^{*} K^{-}(\mathrm{b}, \mathrm{e})$ and $D_{D \gamma}^{*} K^{-}(\mathrm{c}, \mathrm{f})$ WS decays, for samples enriched in signal with the requirements $N N>0.94$ ( $m_{\mathrm{ES}}$ projections) or $5.2725<m_{\mathrm{ES}}<5.2875 \mathrm{GeV} / c^{2}$ ( $N N$ projections). The points with error bars are data. The curves represent the fit projections for signal plus background (solid), the sum of all background components (dashed), and $q \bar{q}$ background only (dotted).
$\mathcal{R}_{(D \gamma) K}^{*+}=(0.9 \pm 1.6 \pm 0.7) \times 10^{-2}$. The corresponding asymmetry is

$$
\mathcal{A}_{(D \gamma) K}^{*}=+0.36 \pm 0.94_{-0.41}^{+0.25}
$$

## VI. DISCUSSION

We use the $B^{-} \rightarrow D^{(*)} K^{-}$analysis results and a frequentist statistical approach [20] to extract information on $r_{B}$ and $r_{B}^{(*)}$. In this technique a $\chi^{2}$ is calculated using the differences between the measured and theoretical values (including systematic errors) of the various ADS quantities from Eqs. (1), (4), and (5). We assume Gaussian measurement uncertainties. This assumption was checked to be valid and conservative at low $r_{B}$ values with a full frequentist approach [5]. For $B^{-} \rightarrow D K^{-}$, we have for instance

$$
\begin{align*}
\chi^{2}= & \left(\mathcal{R}_{D K}^{+}-\mathcal{R}_{D K}^{+(\mathrm{th})}\left(r_{B}, \gamma, \delta_{B}, r_{D}, \delta_{D}\right)\right)^{2} / \sigma_{\mathcal{R}^{+}}^{2} \\
& +\left(\mathcal{R}_{D K}^{-}-\mathcal{R}_{D K}^{-(\mathrm{th)}}\left(r_{B}, \gamma, \delta_{B}, r_{D}, \delta_{D}\right)\right)^{2} / \sigma_{\mathcal{R}^{-}}^{2} \\
& +\left(r_{D}^{(m)}-r_{D}\right)^{2} / \sigma_{r}^{2}+\left(\delta_{D}^{(m)}-\delta_{D}\right)^{2} / \sigma_{\delta}^{2} \tag{9}
\end{align*}
$$

where $\mathcal{R}_{D K}^{ \pm \text {(th) }}\left(r_{B}, \gamma, \delta_{B}, r_{D}, \delta_{D}\right)$ is given by Eq. (1), and where the two last terms constrain $r_{D}$ and $\delta_{D}$ to the values $r_{D}^{(m)}$ and $\delta_{D}^{(m)}$ of Ref. [8] within their errors $\sigma_{r}$ and $\sigma_{\delta}$. The choice of $\left(\mathcal{R}_{D K}^{+}, \mathcal{R}_{D K}^{-}\right)$rather than $\left(\mathcal{R}_{D K}, \mathcal{A}_{D K}\right)$ is motivated by the fact that the set of variables $\left(\mathcal{R}_{D K}, \mathcal{A}_{D K}\right)$ is not well behaved (the uncertainty on $\mathcal{A}_{D K}$ depends on the central value of $\left.\mathcal{R}_{D K}\right)$, while $\left(\mathcal{R}_{D K}^{+}, \mathcal{R}_{D K}^{-}\right)$are two
statistically independent observables. In the same way, the two pairs of ADS observables $\left(\mathcal{R}_{\left(D \pi^{0}\right) K}^{*+}, \mathcal{R}_{\left(D \pi^{0}\right) K}^{*-}\right)$ and $\left(\mathcal{R}_{(D \gamma) K}^{*+}, \mathcal{R}_{(D \gamma) K}^{*-}\right)$ are used to extract $r_{B}^{*}$, while accounting for the relative phase difference in the two $D^{*}$ decays [9]. We allow $0 \leq r_{B}^{(*)} \leq 1,-180^{\circ} \leq \gamma \leq 180^{\circ}$, and $-180^{\circ} \leq \delta_{B}^{(*)} \leq 180^{\circ}$. The minimum of the $\chi^{2}$ for the $r_{B}^{(*)}, \gamma, \delta_{B}^{(*)}, r_{D}$, and $\delta_{D}$ parameter space is calculated first $\left(\chi_{\text {min }}^{2}\right)$. We then scan the range of $r_{B}^{(*)}$ minimizing the $\chi^{2}$


FIG. 10 (color online). Constraints on $r_{B}^{(*)}$ from the combined $B^{-} \rightarrow[K \pi]_{D^{(*)}} K^{-}$ADS measurements. The solid (dotted) curve shows the 1 minus the confidence level to exclude the abscissa value as a function of $r_{B}^{(*)}$. The horizontal lines show the exclusion limits at the 1 and 2 standard deviation levels.

TABLE VIII. Constraints on $r_{B}^{(*)}$ from the combined $B^{-} \rightarrow$ $[K \pi]_{D^{(i)}} K^{-}$ADS measurements.

| Parameter | $1 \sigma$ measurement | $90 \%$ C.L. upper limit |
| :--- | :---: | :---: |
| $r_{B}$ | $\left(9.5_{-4.1}^{+5.1}\right) \%$ | $<16.7 \%$ |
| $r_{B}^{*}$ from | $\left(13.1_{-6.1}^{+4.2}\right) \%$ | $<19.5 \%$ |
| $D^{* 0} \rightarrow D^{0} \pi^{0}$ | $\left(12.0_{-12.0}^{+10.0}\right) \%$ | $<24.5 \%$ |
| $D^{* 0} \rightarrow D^{0} \gamma$ | $\left(9.6_{-5.1}^{+3.5}\right) \%$ | $<15.0 \%$ |
| all $D^{* 0}$ decays |  |  |

$\left(\chi_{m}^{2}\right)$ by varying $\delta_{B}^{(*)}, \gamma, r_{D}$, and $\delta_{D}$. A C.L. for $r_{B}$ is calculated using $\Delta \chi^{2}=\chi_{m}^{2}-\chi_{\text {min }}^{2}$ and $1^{\circ}$ of freedom.

The results of this procedure are shown in Fig. 10 for the C.L. curve as a function of $r_{B}^{(*)}$. The results are summarized in Table VIII. For $B^{-} \rightarrow[K \pi]_{D} K^{-}$, we find the minimum $\chi^{2}$ at $r_{B}=\left(9.5_{-4.1}^{+5.1}\right) \%$. This leads to the upper limit: $r_{B}<$ $16.7 \%$ at $90 \%$ C.L., to be compared to $r_{B}<23 \%$ at 90\% C.L. for the previous ADS analysis as performed by $B A B A R$ [4] with $232 \times 10^{6} B \bar{B}$ pairs, and to $r_{B}<19 \%$ at $90 \%$ C.L. for the corresponding ADS analysis as performed by Belle [6] with $657 \times 10^{6} B \bar{B}$ pairs. We exclude $r_{B}=0$ with a C.L. of $95.3 \%$. Similarly, for $B^{-} \rightarrow$ $[K \pi]_{D^{*}} K^{-}$we find $r_{B}^{*}=\left(9.6_{-5.1}^{+3.5}\right) \%$. This leads to the upper limit: $r_{B}^{*}<15.0 \%$ at $90 \%$ C.L., to be compared to $r_{B}^{*}<16 \%$ at $90 \%$ C.L. for the previous $B A B A R$ ADS analysis [4]. We exclude $r_{B}^{*}=0$ with a C.L. of $83.9 \%$.

Using the above procedure we also determine the $2 D$ confidence intervals for $\gamma$ vs $\delta_{B}^{(*)}$ shown in Figs. 11 and 12. Choosing the solution with $0<\gamma<180^{\circ}$ favors a positive sign for the strong phase $\delta_{B}\left(\mathcal{A}_{D K}<0\right)$, and a negative sign for the strong phase $\delta_{B}^{*}\left(\mathcal{A}_{\left(D \pi^{0}\right) K}^{*}>0\right)$. This result is in good agreement with the values of the strong phases determined in Refs. [5,7]. Finally, Fig. 13 shows the C.L. curve as a function of $\gamma$ when combining the $D K$ and $D^{*} K$ results.


FIG. 11 (color online). One minus confidence level isocontours on $\gamma$ vs $\delta_{B}$ from the $B^{-} \rightarrow[K \pi]_{D} K^{-}$ADS measurement.


FIG. 12 (color online). One minus confidence level isocontours on $\gamma$ vs $\delta_{B}^{*}$ from the combined $B^{-} \rightarrow[K \pi]_{D^{*}} K^{-}$ADS measurements.


FIG. 13 (color online). Constraints on $\gamma$ from the combined $B^{-} \rightarrow D^{(*)}\left[K^{+} \pi^{-}\right] K^{-}$ADS measurements. The solid curve shows the (1-C.L.) to exclude the abscissa value. The horizontal lines show the exclusion limits at the 1 and 2 standard deviation levels.

## VII. SUMMARY

In summary, using a data sample of $467 \times 10^{6} B \bar{B}$ pairs, we present an updated search of the decays $B^{-} \rightarrow D^{(*)} K^{-}$ where the neutral $D$ meson decays into the $K^{+} \pi^{-}$final state (WS). The analysis method is first applied to $B^{-} \rightarrow$ $D^{(*)} \pi^{-}$, where the $D$ decays into the Cabibbo-favored ( $K^{-} \pi^{+}$) and doubly suppressed modes ( $K^{+} \pi^{-}$). We measure $\mathcal{R}_{D \pi}=(3.3 \pm 0.6 \pm 0.4) \times 10^{-3}, \mathcal{R}_{\left(D \pi^{0}\right) \pi}^{*}=(3.2 \pm$ $0.9 \pm 0.8) \times 10^{-3} \quad$ and $\quad \mathcal{R}_{(D \gamma) \pi}^{*}=(2.7 \pm 1.4 \pm 2.2) \times$ $10^{-3}$, in good agreement with the ratio $R_{D}$ of the suppressed to favored $D^{0} \rightarrow K \pi$ decay rates, $R_{D}=(3.36 \pm$ $0.08) \times 10^{-3}$ [8]. Both the branching fraction ratios and the $C P$ asymmetries measured for those modes,
$\mathcal{A}_{D \pi}=(3 \pm 17 \pm 4) \times 10^{-2}, \mathcal{A}_{\left(D \pi^{0}\right) \pi}^{*}=(9 \pm 27 \pm 5) \times$ $10^{-2}$ and $\mathcal{A}_{(D \gamma) \pi}^{*}=\left(65 \pm 55_{-24}^{+20}\right) \times 10^{-2}$, are consistent with the expectations discussed in Sec. I.

We see indications of signals for the $B \rightarrow D K$ and $B \rightarrow$ $D_{D \pi^{0}}^{*} K$ wrong-sign modes, with significances of $2.1 \sigma$ and $2.2 \sigma$, respectively. The ratios of the WS to RS branching fractions are measured to be $\mathcal{R}_{D K}=(1.1 \pm 0.6 \pm 0.2) \times$ $10^{-2}$ and $\mathcal{R}_{\left(D \pi^{0}\right) K}^{*}=(1.8 \pm 0.9 \pm 0.4) \times 10^{-2}$ for $B \rightarrow$ $D K$ and $B \rightarrow D_{D \pi^{0}}^{*} K$, respectively. The separate measurements of $\mathcal{R}_{D K}^{(*) \pm}$ for $B^{+}$and $B^{-}$events indicates large $C P$ asymmetries, with $\mathcal{A}_{D K}=-0.86 \pm 0.47_{-0.16}^{+0.12}$ for $B \rightarrow$ $D K$ and $\mathcal{A}_{\left(D \pi^{0}\right) K}^{*}=+0.77 \pm 0.35 \pm 0.12$ for $B \rightarrow D^{*} K$, $D^{*} \rightarrow D \pi^{0}$. For the $B \rightarrow D_{D \gamma}^{*} K$ WS mode, we see no statistically significant evidence of a signal. We measure $\mathcal{R}_{(D \gamma) K}^{*}=(1.3 \pm 1.4 \pm 0.8) \times 10^{-2}$ and $\mathcal{A}_{(D \gamma) K}^{*}=$ $+0.36 \pm 0.94_{-0.41}^{+0.25}$. These results are used to extract the following constraints on $r_{B}^{(*)}$ :

$$
r_{B}=\left(9.5_{-4.1}^{+5.1}\right) \%, \quad r_{B}^{*}=\left(9.6_{-5.1}^{+3.5}\right) \% .
$$

Assuming $0<\gamma<180^{\circ}$, we also extract constraints on the strong phases $\delta_{B}^{(*)}$, in good agreement with other measurements Ref. [5,7].

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