# Search for Structure in the $\boldsymbol{B}_{s}^{\mathbf{0}} \boldsymbol{\pi}^{ \pm}$Invariant Mass Spectrum 

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#### Abstract

The $B_{s}^{0} \pi^{ \pm}$invariant mass distribution is investigated in order to search for possible exotic meson states. The analysis is based on a data sample recorded with the LHCb detector corresponding to $3 \mathrm{fb}^{-1}$ of $p p$ collision data at $\sqrt{s}=7$ and 8 TeV . No significant excess is found, and upper limits are set on the production rate of the claimed $X(5568)$ state within the LHCb acceptance. Upper limits are also set as a function of the mass and width of a possible exotic meson decaying to the $B_{s}^{0} \pi^{ \pm}$final state. The same limits also apply to a possible exotic meson decaying through the chain $B_{s}^{* 0} \pi^{ \pm}, B_{s}^{* 0} \rightarrow B_{s}^{0} \gamma$ where the photon is excluded from the reconstructed decays.


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Interest in exotic hadrons has recently intensified, with a wealth of experimental data becoming available [1,2]. All the well-established exotic states contain a heavy quarkantiquark ( $c \bar{c}$ or $b \bar{b}$ ) pair together with additional light particle content. However, the D0 Collaboration has reported evidence [3] of a narrow structure, referred to as the $X(5568)$, in the $B_{s}^{0} \pi^{ \pm}$spectrum produced in $p \bar{p}$ collisions at center-of-mass energy $\sqrt{s}=1.96 \mathrm{TeV}$. The claimed $X(5568)$ state, if confirmed, would differ from any of the previous observations, as it must have constituent quarks with four different flavors $(b, s, u, d)$. As such, it would be unique among observed exotic hadrons in having its mass dominated by a single constituent quark rather than by a quark-antiquark pair. This could provide a crucial piece of information to help understand how exotic hadrons are bound; specifically, whether they are dominantly tightly bound (often referred to as "tetraquarks" and "pentaquarks") or loosely bound meson-meson or mesonbaryon molecules.

In this Letter, results are presented from a search for an exotic meson, denoted $X$, decaying to $B_{s}^{0} \pi^{ \pm}$in a data sample corresponding to $3 \mathrm{fb}^{-1}$ of $p p$ collision data at $\sqrt{s}=7$ and 8 TeV recorded by LHCb. The search is performed by scanning over the mass and width of the purported state, with dedicated fits for parameters corresponding to those of the claimed $X(5568)$ state. The $B_{s}^{0}$ mesons are reconstructed in decays to $D_{s}^{-} \pi^{+}$and $J / \psi \phi$ final states to obtain a $B_{s}^{0}$ yield approximately 20 times larger than that used by the D0 Collaboration. The inclusion of charge-conjugate processes is implied throughout the Letter. The analysis techniques follow closely those

[^0]developed for studies of the $B^{+} K^{-}[4], B^{+} \pi^{-}$and $B^{0} \pi^{+}$[5] spectra. As in previous analyses, the charged pion which is combined with the $B_{s}^{0}$ meson in order to form the $B_{s}^{0} \pi^{ \pm}$ candidate is referred to as the "companion pion".

The LHCb detector $[6,7]$ is a single-arm forward spectrometer covering the pseudorapidity range $2<\eta<5$, designed for the study of particles containing $b$ or $c$ quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the $p p$ interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm , and three stations of silicon-strip detectors and straw drift tubes placed downstream of the magnet. The tracking system provides a measurement of momentum, $p$, of charged particles with a relative uncertainty that varies from $0.5 \%$ at low momentum to $1.0 \%$ at 200 GeV (units in which $c=\hbar=1$ are used throughout). The minimum distance of a track to a primary vertex $(\mathrm{PV})$, the impact parameter, is measured with a resolution of $\left(15+29 / p_{T}\right) \mu \mathrm{m}$, where $p_{T}$ is the component of the momentum transverse to the beam, in GeV . Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors. Photons, electrons, and hadrons are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter, and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers. The online event selection is performed by a trigger, which consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction.

Simulations of $p p$ collisions are generated using PYTHIA [8] with a specific LHCb configuration [9]. Decays of hadronic particles are described by EVTGEN [10], in which final-state radiation is generated using pHOTOS [11]. The interaction of the generated particles with the detector, and


FIG. 1. Selected candidates for (left) $B_{s}^{0} \rightarrow D_{s}^{-} \pi^{+}$and (right) $B_{s}^{0} \rightarrow J / \psi \phi$ decays, with $p_{T}\left(B_{s}^{0}\right)>5 \mathrm{GeV}$, where the $B_{s}^{0}$ signal window requirements of $\left|m\left(D_{s}^{-} \pi^{+}\right)-5367 \mathrm{MeV}\right|<30 \mathrm{MeV}$ and $|m(J / \psi \phi)-5367 \mathrm{MeV}|<13 \mathrm{MeV}$ are indicated by dotted lines. Results of the fits described in the text are superimposed with the total fit result shown as a red line, the signal component as an unfilled area, the combinatorial background component as a dark blue area, and additional background contributions as a light green area.
its response, are implemented using the GEANT4 toolkit [12] as described in Ref. [13].

Candidate $B_{s}^{0}$ mesons are reconstructed through the decays $B_{s}^{0} \rightarrow D_{s}^{-} \pi^{+}$with $D_{s}^{-} \rightarrow K^{+} K^{-} \pi^{-}$, and $B_{s}^{0} \rightarrow J / \psi \phi$ with $J / \psi \rightarrow \mu^{+} \mu^{-}$and $\phi \rightarrow K^{+} K^{-}$. Particle identification, track quality, and impact parameter requirements are imposed on all final-state particles. Both $B_{s}^{0}$ and intermediate particle $\left(D_{s}^{-}\right.$and $\left.J / \psi\right)$ candidates are required to have good vertex quality and to have invariant mass close to the known values [14]. Specific backgrounds due to other $b$-hadron decays are removed with appropriate vetoes. A requirement is imposed on the multiplicity of tracks originating from the PV associated with the $B_{s}^{0}$ candidate; this requirement is about $90 \%$ efficient on the $B_{s}^{0}$ signal and significantly reduces background due to random $B_{s}^{0} \pi^{ \pm}$combinations. To further reduce background, the $p_{T}$ of the $B_{s}^{0}$ candidate, $p_{T}\left(B_{s}^{0}\right)$, is required to be greater than 5 GeV . Results are also obtained with this requirement increased to 10 or 15 GeV , to be more sensitive to scenarios in which the $X$ state is predominantly produced from hard
processes. The definition of the fiducial acceptance is completed with the requirements $p_{T}\left(B_{s}^{0}\right)<50 \mathrm{GeV}$ and $2.0<y<4.5$, where $y$ is the rapidity of the $B_{s}^{0}$ candidate.

The signals in the two $B_{s}^{0}$ decay modes are shown in Fig. 1. To estimate the $B_{s}^{0}$ yields, the data are fitted with functions that include a signal component, described by a double Gaussian function with a shared mean, and a combinatorial background component, described by a polynomial function. Backgrounds from $B_{s}^{0} \rightarrow D_{s}^{\mp} K^{ \pm}$ decays in the $D_{s}^{-} \pi^{+}$sample and from $\Lambda_{b}^{0} \rightarrow J / \psi p K^{-}$ decays in the $J / \psi \phi$ sample, where a final-state hadron is misidentified, are modeled using empirical shapes derived from simulated samples. An additional component, modeled with a Gaussian function, is included to account for possible $B^{0} \rightarrow J / \psi K^{+} K^{-}$decays [15] in the $J / \psi \phi$ sample. The results of these fits are reported in Table I. The signal-to-background ratio in the $B_{s}^{0}$ signal windows is about 10 for the $D_{s}^{-} \pi^{+}$sample and above 50 for the $J / \psi \phi$ sample.

The $B_{s}^{0}$ candidates are combined with each track originating from the associated PV that gives a good quality $B_{s}^{0} \pi^{ \pm}$vertex and that has $p_{T}>500 \mathrm{MeV}$. A loose pion identification requirement is imposed in order to suppress possible backgrounds involving misidentified particles. In case multiple candidates are obtained in the same event, all are retained. Mass and vertex constraints are imposed [16] in the calculation of the $B_{s}^{0} \pi^{ \pm}$invariant mass.

In order to obtain quantitative results on the contributions from resonant structures in the data, the $B_{s}^{0} \pi^{ \pm}$mass distributions are fitted with a function containing components for the signal and background. The signal shape is an $S$-wave Breit-Wigner function multiplied by a function that accounts for the variation of the efficiency with $B_{s}^{0} \pi^{ \pm}$mass. The efficiency function, determined from simulation, plateaus at high $B_{s}^{0} \pi^{ \pm}$mass and falls near the threshold to a value that depends on $p_{T}\left(B_{s}^{0}\right)$. The resolution is better

TABLE I. Yields, $N$, of $B_{s}^{0}$ and $X(5568)$ candidates obtained from the fits to the $B_{s}^{0}$ and $B_{s}^{0} \pi^{ \pm}$candidate mass distributions, with statistical uncertainties only. The values reported for $N\left(B_{s}^{0}\right)$ are those inside the $B_{s}^{0}$ signal window. The reported values for $X(5568)$ are obtained from fits with signal mass and width parameters fixed to those determined by the D0 Collaboration. Relative efficiencies $\epsilon^{\text {rel }}(X)$ of the $B_{s}^{0}$ and $X(5568)$ candidate selection criteria are also given. The reported uncertainties on the relative efficiencies are only statistical, due to the finite size of the simulated samples.

|  |  | $B_{s}^{0} \rightarrow D_{s}^{-} \pi^{+}$ | $B_{s}^{0} \rightarrow J / \psi \phi$ | Sum |
| :--- | :---: | :---: | ---: | ---: |
| $N\left(B_{s}^{0}\right) / 10^{3}$ | $p_{T}\left(B_{s}^{0}\right)>5 \mathrm{GeV}$ | $62.2 \pm 0.3$ | $43.6 \pm 0.2$ | $105.8 \pm 0.4$ |
|  | $p_{T}\left(B_{s}^{0}\right)>10 \mathrm{GeV}$ | $28.4 \pm 0.2$ | $13.2 \pm 0.1$ | $41.6 \pm 0.2$ |
| $N(X)$ | $p_{T}\left(B_{s}^{0}\right)>15 \mathrm{GeV}$ | $8.8 \pm 0.1$ | $3.7 \pm 0.1$ | $12.5 \pm 0.1$ |
|  | $p_{T}\left(B_{s}^{0}\right)>5 \mathrm{GeV}$ | $3 \pm 64$ | $-33 \pm 43$ | $-30 \pm 77$ |
|  | $p_{T}\left(B_{s}^{0}\right)>10 \mathrm{GeV}$ | $75 \pm 52$ | $12 \pm 33$ | $87 \pm 62$ |
| $\epsilon_{T}^{\mathrm{rel}}(X)$ | $14 \pm 31$ | $-10 \pm 17$ | $4 \pm 35$ |  |
|  | $p_{T}\left(B_{s}^{0}\right)>15 \mathrm{GeV}$ | $0.127 \pm 0.002$ | $0.093 \pm 0.001$ | $\ldots$ |
|  | $p_{T}\left(B_{s}^{0}\right)>5 \mathrm{GeV}$ | $0.213 \pm 0.003$ | $0.206 \pm 0.002$ | $\ldots$ |

than 1 MeV and does not affect the results. The background is modeled with a polynomial function. It is verified that this function gives a good description of backgrounds composed of either a real or a fake $B_{s}^{0}$ decay combined with a random pion, as determined from simulation or from data in $B_{s}^{0}$ candidate mass sideband regions, respectively.

For each choice of signal mass and width parameters, a binned maximum likelihood fit to the $B_{s}^{0} \pi^{ \pm}$candidate mass spectrum is used to determine the signal and background yields and the parameters of the polynomial shape that describes the background. The two $B_{s}^{0}$ decay modes are fitted simultaneously. The results of the fit where the mass and width are fixed according to the central values obtained by the D0 collaboration, $m=5567.8 \pm 2.9$ (stat $)_{-1.9}^{+0.9}$ (syst) MeV and $\Gamma=21.9 \pm 6.4(\mathrm{stat})_{-2.5}^{+5.0}($ syst $) \mathrm{MeV}$ [3], are shown in Fig. 2 for both $B_{s}^{0}$ decay modes combined. The $X(5568)$ yield is not significant for any minimum $p_{T}\left(B_{s}^{0}\right)$ requirement. In each case, the change in negative log likelihood between fits including or not including the signal component is less than 2 units for two additional free parameters corresponding to the yields in the two $B_{s}^{0}$ decay modes. The results of the fits are summarized in Table I.

The yields $N$ obtained from the fits are used to measure the ratio of cross sections

$$
\begin{align*}
\rho_{X}^{\mathrm{LHCb}} & \equiv \frac{\sigma(p p \rightarrow X+\text { anything }) \times \mathcal{B}\left(X \rightarrow B_{s}^{0} \pi^{ \pm}\right)}{\sigma\left(p p \rightarrow B_{s}^{0}+\text { anything }\right)}  \tag{1}\\
& =\frac{N(X)}{N\left(B_{s}^{0}\right)} \times \frac{1}{\epsilon^{\mathrm{rel}}(X)}, \tag{2}
\end{align*}
$$

where the cross sections $\sigma$ are for promptly produced particles within the LHCb acceptance. Since $\sigma\left(p p \rightarrow B_{s}^{0}+\right.$ anything) in the LHCb acceptance has been previously measured [17], any result for $\rho_{X}^{\mathrm{LHCb}}$ can be scaled to give a result for $\sigma(p p \rightarrow X+$ anything $) \times \mathcal{B}\left(X \rightarrow B_{s}^{0} \pi^{ \pm}\right)$in the LHCb acceptance. The relative efficiency $\epsilon^{\text {rel }}(X)=$ $\epsilon(X) / \epsilon\left(B_{s}^{0}\right)$ accounts for the reconstruction and selection efficiency of the companion pion as well as the requirement that it is within the LHCb acceptance. These effects are determined from simulation, weighted to reproduce the measured differential $B_{s}^{0}$ production spectrum [17], together with a data-driven evaluation [18] of the efficiency of the particle identification requirement on the companion pion. In the simulation, the $X$ state is assumed to be spinless; it has been verified that the systematic uncertainty associated with this choice is negligible. The quantities used to evaluate $\rho_{X}^{\text {LHCb }}$ are summarized in Table I.

Systematic uncertainties are assigned due to possible biases in the evaluation of $N(X), N\left(B_{s}^{0}\right)$, and $\epsilon^{\mathrm{rel}}(X)$. The signal shape is modified by varying the efficiency function, and separately by changing the assumed angular momentum in the relativistic Breit-Wigner function from $S$ wave to $P$ wave. In each case, the changes in $N(X)$ are assigned


FIG. 2. Results of the fit to the $B_{s}^{0} \pi^{ \pm}$mass distribution for candidates (both $B_{s}^{0}$ modes combined) with minimum $p_{T}\left(B_{s}^{0}\right)$ of (top) 5 GeV , (middle) 10 GeV , and (bottom) 15 GeV . The component for the claimed $X(5568)$ state is included in the fit but is not significant. The distributions of the normalized residuals, or "pulls," displayed underneath the main figures show good agreement between the fit functions and the data.
as the associated systematic uncertainties. Uncertainties associated with the determination of $N\left(B_{s}^{0}\right)$ arise due to the size of the $B_{s}^{0}$ sample and the estimation of the background in the signal region. In addition to the limited size of the
simulation sample, uncertainties associated with $\epsilon^{\mathrm{rel}}(X)$ arise due to the precision with which the companion pion reconstruction and particle identification efficiencies are known $[18,19]$. The uncertainties from different sources are combined in quadrature and give a total that is much smaller than the statistical uncertainty. To obtain results that can be compared to those for the claimed $X(5568)$ state reported by the D0 Collaboration, additional systematic uncertainties are assigned from the changes in the results for $\rho_{X}^{\mathrm{LHCb}}$ when the mass and width parameters are varied independently within $\pm 1 \sigma$ ranges from their central values. These are the dominant sources of systematic uncertainty.

To cross-check the results, candidates are selected with criteria similar to those used in the observation of $B_{c}{ }^{+} \rightarrow B_{s}^{0} \pi^{+}$decays [20], with consistent results. In addition, $B^{0} \rightarrow D^{-} \pi^{+}$decays are used to create $B^{0} \pi^{+}$ combinations, and the results on the excited $B$ states of Ref. [5] are reproduced.

The values of $\rho_{X}^{\mathrm{LHCb}}$ for the two $B_{s}^{0}$ decay modes are consistent and are therefore combined in a weighted average. In the average, systematic uncertainties are taken to be uncorrelated between the two $B_{s}^{0}$ decay modes. An exception is made when obtaining results corresponding to the claimed $X(5568)$ state, where the uncertainty due to the limited precision of the reported mass and width values [3] is treated as correlated between the two modes. These results are

$$
\begin{aligned}
\rho_{X}^{\mathrm{LHCb}}\left[p_{T}\left(B_{s}^{0}\right)>5 \mathrm{GeV}\right] & =-0.003 \pm 0.006 \pm 0.002 \\
\rho_{X}^{\mathrm{LHCb}}\left[p_{T}\left(B_{s}^{0}\right)>10 \mathrm{GeV}\right] & =0.010 \pm 0.007 \pm 0.005 \\
\rho_{X}^{\mathrm{LHCb}}\left[p_{T}\left(B_{s}^{0}\right)>15 \mathrm{GeV}\right] & =0.000 \pm 0.010 \pm 0.006
\end{aligned}
$$

where the first uncertainty is statistical and the second is systematic. Since the signal is not significant, upper limits on $\rho_{X}^{\mathrm{LHCb}}$ are obtained by integration of the likelihood in the positive region to find the value that contains the fraction of the integral corresponding to the required confidence level (C.L.). The upper limits at $90(95) \%$ C.L. are found to be

$$
\begin{gathered}
\rho_{X}^{\mathrm{LHCb}}\left[p_{T}\left(B_{s}^{0}\right)>5 \mathrm{GeV}\right]<0.011(0.012), \\
\rho_{X}^{\mathrm{LHCb}}\left[p_{T}\left(B_{s}^{0}\right)>10 \mathrm{GeV}\right]<0.021(0.024), \\
\rho_{X}^{\mathrm{LHCb}}\left[p_{T}\left(B_{s}^{0}\right)>15 \mathrm{GeV}\right]<0.018(0.020) .
\end{gathered}
$$

No significant signal for a $B_{s}^{0} \pi^{ \pm}$resonance is seen at any value of mass and width in the range considered. To obtain limits on $\rho_{X}^{\mathrm{LHCb}}$ for different values of these parameters, fits are performed for widths $(\Gamma)$ of 10 to 50 MeV in 10 MeV steps. For each width, the mass is scanned in steps of $\Gamma / 2$, starting one unit of width above the kinematic threshold and ending approximately one and a half units of width below 6000 MeV . The upper edge of the range is chosen because an exotic state with higher mass would be expected to give a clearer signature in the $B^{0} K^{ \pm}$final state [21]. The


FIG. 3. Upper limits (ULs) at $90 \%$ confidence level (C.L.) as functions of the mass and width of a purported exotic state $X$ decaying to $B_{s}^{0} \pi^{ \pm}$with minimum $p_{T}\left(B_{s}^{0}\right)$ of (top) 5 GeV , (middle) 10 GeV , and (bottom) 15 GeV . The same limits also apply to a possible exotic meson decaying through the chain $B_{s}^{* 0} \pi^{ \pm}, B_{s}^{* 0} \rightarrow$ $B_{s}^{0} \gamma$ where the photon is excluded from the reconstructed decays. In the latter case the nominal mass difference $m\left(B_{s}^{* 0}\right)-m\left(B_{s}^{0}\right)=$ $48.6_{-1.6}^{+1.8} \mathrm{MeV}$ [14] has to be added to the values on the $x$ axis to get the mass of the exotic meson under investigation.
results are obtained in the same way as described above, and converted into upper limits that are shown in Fig. 3. The upper limits are weaker when a broader width is assumed, due to the larger amount of background under the putative peak. The limits also become weaker when there is an excess of events in the signal region, although all such excesses are consistent with being statistical fluctuations. The method used to set the upper limits smooths out any negative fluctuations.

In summary, a search for the claimed $X(5568)$ state has been carried out using a data sample corresponding to $3 \mathrm{fb}^{-1}$ of $p p$ collision data at $\sqrt{s}=7$ and 8 TeV recorded by LHCb . No significant excess is found and thus the existence of the $X(5568)$ state is not confirmed. Upper
limits are set on the relative production rate of the claimed state in the LHCb acceptance. Limits are also set as a function of the mass and width of a possible exotic meson decaying to the $B_{s}^{0} \pi^{ \pm}$final state. The same limits also apply to a possible exotic meson decaying through the chain $B_{s}^{* 0} \pi^{ \pm}, B_{s}^{* 0} \rightarrow B_{s}^{0} \gamma$ where the photon is excluded from the reconstructed decays.

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[1] S. L. Olsen, A new hadron spectroscopy, Front. Phys. 10, 121 (2015).
[2] H.-Y. Cheng, Multiquark hadrons, The Universe 3, 33 (2015).
[3] V. M. Abazov et al. (D0 Collaboration), Evidence for a $B_{s}^{0} \pi^{ \pm}$State, Phys. Rev. Lett. 117, 022003 (2016).
[4] R. Aaij et al. (LHCb Collaboration), First Observation of the Decay $B_{s 2}^{*}(5840)^{0} \rightarrow B^{*+} K^{-}$and Studies of Excited $B_{s}^{0}$ Mesons, Phys. Rev. Lett. 110, 151803 (2013).
[5] R. Aaij et al. (LHCb Collaboration), Precise measurements of the properties of the $B_{1}(5721)^{0,+}$ and $B_{2}^{*}(5747)^{0,+}$ states
and observation of structure at higher invariant mass in the $B^{+} \pi^{-}$and $B^{0} \pi^{+}$spectra, J. High Energy Phys. 04 (2015) 024.
[6] A. A. Alves Jr. et al. (LHCb Collaboration), The LHCb detector at the LHC, J. Instrum. 3, S08005 (2008).
[7] R. Aaij et al. (LHCb Collaboration), LHCb detector performance, Int. J. Mod. Phys. A 30, 1530022 (2015).
[8] T. Sjöstrand, S. Mrenna, and P. Skands, PYTHIA 6.4 physics and manual, J. High Energy Phys. 05 (2006) 026; T. Sjöstrand, S. Mrenna, and P. Skands, A brief introduction to PYTHIA 8.1, Comput. Phys. Commun. 178, 852 (2008).
[9] I. Belyaev et al., Handling of the generation of primary events in Gauss, the LHCb simulation framework, J. Phys. Conf. Ser. 331, 032047 (2011).
[10] D. J. Lange, The EvtGen particle decay simulation package, Nucl. Instrum. Methods Phys. Res., Sect. A 462, 152 (2001).
[11] P. Golonka and Z. Was, PHOTOS Monte Carlo: A precision tool for QED corrections in $Z$ and $W$ decays, Eur. Phys. J. C 45, 97 (2006).
[12] J. Allison et al. (Geant4 Collaboration), Geant4 developments and applications, IEEE Trans. Nucl. Sci. 53, 270 (2006); S. Agostinelli et al. (Geant4 Collaboration), Geant4: A simulation toolkit, Nucl. Instrum. Methods Phys. Res., Sect. A 506, 250 (2003).
[13] M. Clemencic, G. Corti, S. Easo, C. R Jones, S. Miglioranzi, M. Pappagallo, and P. Robbe, The LHCb simulation application, Gauss: Design, evolution and experience, J. Phys. Conf. Ser. 331, 032023 (2011).
[14] K. A. Olive et al. (Particle Data Group Collaboration), Review of particle physics, Chin. Phys. C 38, 090001 (2014), and 2015 update.
[15] R. Aaij et al. (LHCb Collaboration), Amplitude analysis and branching fraction measurement of $\bar{B}_{s}^{0} \rightarrow J / \psi K^{+} K^{-}$, Phys. Rev. D 87, 072004 (2013).
[16] W. D. Hulsbergen, Decay chain fitting with a Kalman filter, Nucl. Instrum. Methods Phys. Res., Sect. A 552, 566 (2005).
[17] R. Aaij et al. (LHCb Collaboration), Measurement of $B$ meson production cross-sections in proton-proton collisions at $\sqrt{s}=7 \mathrm{TeV}$, J. High Energy Phys. 08 (2013) 117.
[18] M. Adinolfi et al., Performance of the LHCb RICH detector at the LHC, Eur. Phys. J. C 73, 2431 (2013).
[19] R. Aaij et al. (LHCb Collaboration), Measurement of the track reconstruction efficiency at LHCb, J. Instrum. 10, P02007 (2015).
[20] R. Aaij et al. (LHCb Collaboration), Observation of the Decay $B_{c}^{+} \rightarrow B_{s}^{0} \pi^{+}$, Phys. Rev. Lett. 111, 181801 (2013).
[21] A. Esposito, A. Pilloni, and A. D. Polosa, Hybridized tetraquarks, Phys. Lett. B 758, 292 (2016).

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(LHCb Collaboration)

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