

Segmentation and Measurement of the Cortex from 3D MR Images Using Coupled Surfaces Propagation

Xiaolan Zeng, Lawrence H. Staib, Robert T. Schultz and James S. Duncan

Abstract—The cortex is the outermost thin layer of gray matter in the brain; geometric measurement of the cortex helps in understanding brain anatomy and function. In the quantitative analysis of the cortex from MR images, extracting the structure and obtaining a representation for various measurements are key steps. While manual segmentation is tedious and labor intensive, automatic, reliable and efficient segmentation and measurement of the cortex remain challenging problems due to its convoluted nature. Here we present a new approach of coupled surfaces propagation using level set methods to address such problems. Our method is motivated by the nearly constant thickness of the cortical mantle and takes this tight coupling as an important constraint. By evolving two embedded surfaces simultaneously, each driven by its own image-derived information while maintaining the coupling, a final representation of the cortical bounding surfaces and an automatic segmentation of the cortex are achieved. Characteristics of the cortex such as cortical surface area, surface curvature and cortical thickness are then evaluated. The level set implementation of surface propagation offers the advantage of easy initialization, computational efficiency and the ability to capture deep sulcal folds. Results and validation from various experiments on both simulated and real 3D MR images are provided.

Keywords—3D segmentation, volumetric layer, coupled surfaces propagation, level set.

I. INTRODUCTION

A significant amount of recent anatomical MRI studies on the human brain have been focused on the cerebral cortex. As the outermost layer of gray matter in the brain, the cerebral cortex is composed of columns of neurons, aligned perpendicularly to the cortical surface, that serve as basic units of information processing. Cortical surface area is likely to be proportional to column number and therefore surface area should be related to functional capacities. In addition, regional cortical thickness and gray matter volume may relate to functional capacities, and alteration in each of these features has been suspected in specific neuropsychiatric disorders [32]. In the quantitative analysis of these features of the cortex, segmentation is the first step.

The cerebral cortex is characterized by its convoluted surface. Due to this convoluted nature, the segmentation of the cortex must be considered in 3D. For example, although the cerebral cortical layer is nearly 3mm thick [1] everywhere on the cortex, an oblique 2D slice that happens to be approximately parallel to a particular sulcus will give the appearance of a much thicker structure. Only

by going through the neighboring slices can we get complete information to perform segmentation. Slice by slice manual tracing of the cortex is extremely tedious and labor intensive, hence automatic, reliable and relatively efficient segmentation which enables automated measurement is a highly desirable goal.

A. Related Work

There are a variety of alternatives to our approach. The first group are region-based methods, which exploit homogeneity in images. They primarily depend on the underlying consistency of any relevant feature in different regions. Following the work of Geman & Geman [10], Markov Random Field(MRF)-based methods have been widely used for this purpose, which employ energy-minimizing techniques to reconstruct a piece-wise flat image from the noisy data. A multi-spectral voxel classification method [2] was used in conjunction with connectivity to segment the brain into different tissue types from 3D MR images. A material mixture model [19] was also used for the segmentation problem. Region-based methods typically require further processing to group segmented regions into coherent structures. Moreover, quantitative measurement of features other than volume does not follow immediately.

The most common second alternative strategy is boundary finding, of which active contour methods are of special note. They rely mainly on gradient features for segmentation of structures from an image. One of the most generic and popular methods of detecting boundaries is the snakes approach due to Kass *et al.* [13]. One concern regarding this method is that close initialization has to be provided in order to achieve good final results. A balloon model with a pressure force outward was then introduced as a way to generalize and solve some of the problems encountered with the above snake method. Deformable surface models using the finite-element method have been used to segment 3D images [3]. However, the need to override local smoothness to allow for significant protrusions that a shape may possess (which is highly desirable in order to capture the sulcal folds) remains a problem.

An alternative approach to deformable boundary finding was to use a 3D surface model with Fourier presentation due to Staib and Duncan [35], [36]. The advantage of this model is that it allows a wide variety of smooth surfaces to be described with a small set of parameters. However, it has limitations in capturing convoluted surfaces such as the cortical surface.

All of the above methods do not explicitly use constraints due to cortical structural information, hence are limited for

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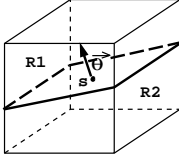


Fig. 1. A local operator to derive image information.

the purpose of cortical segmentation. However, there has been some effort made in this direction. MacDonald *et al.* presented an iterative algorithm for simultaneous deformation of multiple surfaces with inter-surface proximity constraints and self-intersection avoidance, where the deformation was formulated as a cost function minimization problem [21], [22]. This method was applied to 3D MR brain data to extract surface models for the skull and the cortical surfaces. This approach takes advantage of the information of the interrelation between the surfaces of interest. However, drawbacks lie in its extremely high computational expense, and the difficulty of tuning the weighting factors in the cost function due to the complexity of the problem.

Teo *et al.* [38] used a system that exploited knowledge of cortical anatomy, in which white matter and CSF regions were first segmented. After the connectivity of the white matter was verified in regions of interest, a representation of the gray matter was created by a constrained growing-out from the white matter boundary. The focus of this work was to create a representation of cortical gray matter for functional MRI visualization.

Davatzikos *et al.* introduced the concept of a ribbon for modeling the outer cortex in cross-sectional brain images [4] and then extended the model into 3D [5]. A deformable surface algorithm was constructed to find the central layer of the cortex. Based on this parameterization, the cortical structure was characterized through its depth map and curvature map. This method explicitly used the structural information of the cortex. However, close initialization and significant human interaction are needed to force the ribbon into sulcal folds. To compensate for this, Xu *et al.* further extended the method by using a new external force model called gradient vector flow for surface deformation [41].

Dale *et al.* [6] concentrated on cortical surface-based analysis. They started by deforming a tessellated ellipsoidal template into the shape of the inner surface of the skull under the influence of an MRI-based force and a curvature reducing force. White matter was then labeled and the cortical surfaces were reconstructed with validation of topology and geometry.

II. OUR APPROACH

The cortical layer to be recovered has an nearly constant thickness (there is variation across different regions) and is bounded by two surfaces: the CSF/gray matter boundary and gray/white matter boundary. Across each bounding surface, there is a local difference in the gray level values, while in between the two surfaces there is a homogeneity of

certain voxel statistics. For our purposes, the cortical layer is defined completely by its bounding surfaces and the homogeneity in between. Following our earlier work [42], we propose a new approach of coupled surfaces propagation via level set methods for the segmentation and measurement of the cortex. By evolving two embedded surfaces simultaneously, each driven by its own image-based information while maintaining the coupling, we are able to achieve an automatic and robust segmentation of the cortex, and simultaneously obtain a representation of the inner and outer cortical surfaces from which surface area can be calculated. Furthermore, curvature and thickness maps are easily obtained from this coupled level set formulation.

A. Image Information Derivation

Medical images consist of a number of different anatomical regions. The homogeneity of each region can usually be characterized by various voxel statistics inside. Thus, by using gradient features (information of gray level difference between neighboring voxels) alone, we actually lose important pieces of information. Here in our approach, instead of using gradient features, we design a local operator which makes use of the gray level information, and gives a measure of the likelihood of a voxel lying on the boundary between tissue *A* and tissue *B*. This model can also be extended to make use of a vector of registered parametric images (such as T1, T2 and PD MR images) or images from different modalities.

At each voxel site *s*, a small neighborhood around *s* is drawn (see Figure 1). Now given a possible boundary with normal direction $\vec{\theta}$, dividing the neighborhood into parts *R1* and *R2*, the probability that *s* lies on the boundary between tissue *A* and tissue *B* is:

$$p_{AB}(\vec{\theta}) = p(R1 \in \text{Tissue}A) \cdot p(R2 \in \text{Tissue}B) \quad (1)$$

Given an estimation $\vec{\theta}^*$ of $\vec{\theta}$, we can use $p(\vec{\theta}^*)$ as a measure of the likelihood that *s* lies on the boundary between tissue *A* and tissue *B*.

One way of estimating $\vec{\theta}^*$ is to first generate the vector $P = [p(\vec{\theta}_1), p(\vec{\theta}_2), \dots, p(\vec{\theta}_k)]^T$ where *k* is the number of possible directions corresponding to the 26 first order neighbors. Then, $\vec{\theta}^*$ is the direction which corresponds to the element in vector *P* that has the largest magnitude. Here we make the assumption of one single parametric image *X*, in which voxels belonging to tissue *A* are independently drawn from a Gaussian distribution $G(\mu_A, \sigma_A)$, and voxels belonging to tissue *B* are independently drawn from $G(\mu_B, \sigma_B)$. Thus, we have

$$p_{AB}(\vec{\theta}) = \prod_{r \in R1} \frac{1}{\sqrt{2\pi}\sigma_A} e^{-\frac{(X_r - \mu_A)^2}{\sigma_A^2}} \cdot \prod_{t \in R2} \frac{1}{\sqrt{2\pi}\sigma_B} e^{-\frac{(X_t - \mu_B)^2}{\sigma_B^2}} \quad (2)$$

In our implementation, *R1* and *R2* are now set to include one voxel each. A limited expansion to several voxels

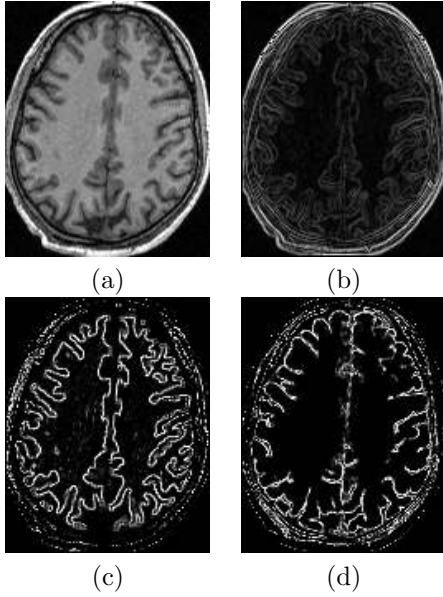


Fig. 2. Results from our local operator compared to image gradient. (a): an axial slice from original 3D brain images; (b): result from gradient operator; (c): result from our local operator $p_{BC}(\tilde{\theta}^*)$, B= gray matter, C=white matter; (d) $p_{AB}(\tilde{\theta}^*)$, A= CSF, B=gray matter.

could potentially further enhance the capability of capturing homogeneity. In Figure 2, we show an example of the results from our local operator showing how well it selects the appropriate gray level transition, which is crucial for subsequent processing. The local operator was applied to images after we reduced the effects of MR inhomogeneity by correcting using a simple fixed map. The map was determined manually by sampling tissue types throughout the field to decide the average inhomogeneity. Note that more complicated MR image models [10], [17], [18] can be used to calculate $p(\tilde{\theta})$.

B. Level Set Method

Level set methods are powerful numerical techniques for analyzing and computing interface motion, and have been used in image segmentation in recent years [23], [24], [25], [33], [34]. The essential idea of the level set methods is to represent the propagating surface (in our case) of interest as a front $\gamma(t)$, and embed this front as the zero level set of a higher dimensional function Ψ defined by $\Psi(x, t) = d$, where d is the signed distance from position x to $\gamma(t)$. An Eulerian formulation is produced for the motion of this surface propagating along its normal direction with speed F , where F can be a function of the surface characteristics (such as the curvature, normal direction etc.) and the image characteristics (e.g. gray level and gradient etc.). The equation of the evolution of Ψ , inside which the propagating surface is embedded as the zero level set is then given by:

$$\Psi_t + F |\nabla \Psi| = 0 \quad (3)$$

The major advantages of using this method over other active contour strategies include the following. First, al-

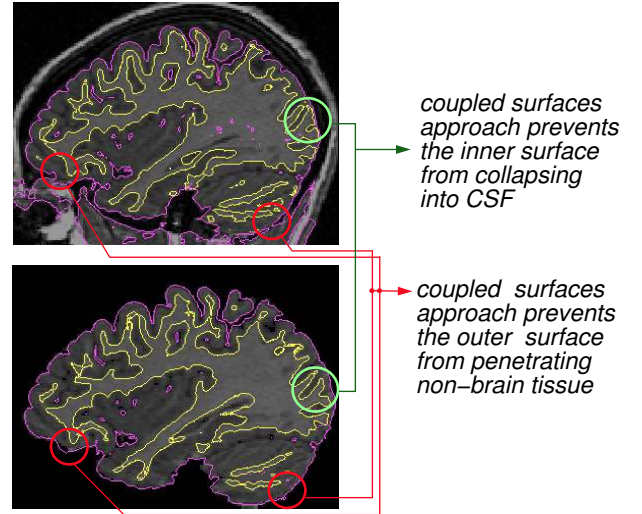


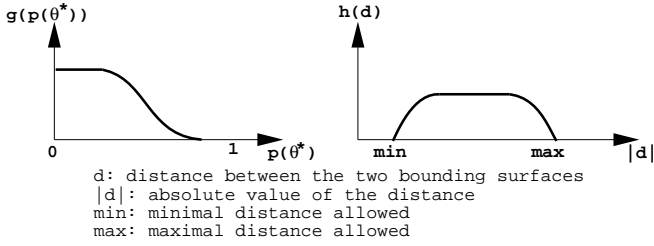
Fig. 3. Single vs. coupled surfaces approach on cortex segmentation. Top: surfaces resulting from single surface approach shown on a sagittal slice of original image (finding the inner and outer cortical surfaces separately); bottom: surfaces resulting from the coupled surfaces approach shown on a sagittal slice of the expert tracing result. Notice that the outer cortical surface resulted from the coupled 3D algorithm nicely fits the boundary from expert tracing.

though the evolving level function $\Psi(x, t)$ remains a function, the embedded propagating front $\gamma(t)$ may change topology, break, merge and form sharp corners as Ψ evolves. Second, the intrinsic geometric properties of the front may be easily determined from Ψ . For example, at any point of the front, the normal vector is given by $\vec{n} = \nabla \Psi$.

C. Single Surface Approach vs. Coupled Surfaces Approach

Because of the limitations of the imaging technique used and the volume averaging effect, it is often observed that in some regions, there is not enough information from the image data to clearly define either the outer or the inner bounding surface. When applying a single surface approach, we may very well end up with error in such a region. While using the coupled surfaces approach, information on the partner surface is available through the coupling and improves the performance of the surface finding.

In the case of MR brain images, due to volume averaging, in some regions the boundary between white matter and gray matter is not well shown, while the CSF appears clearly. The single surface approach may hence have the inner cortical surface collapse into CSF. However with the coupled surfaces approach, we maintain some minimal distance between the inner cortical surface and CSF, thus preventing the inner cortical surface from going into CSF. There are also places where structures such as eye sockets appear, so that the CSF can not be observed in the image. With the coupled surfaces approach, the white/gray matter boundary information is then used to stop the propagation of the outer cortical surface before it penetrates non-brain structures. Figure 3 shows examples of the above mentioned cases where the coupled surfaces approach outperforms the single surface approach.

Fig. 4. Functions g and h used in speed term design.

D. Coupled Surfaces Propagation: Speed Term Design

In solving the problem of segmenting the cortex, we consider two moving interfaces describing the inner and outer cortical bounding surfaces respectively. Starting from inside the inner cortical surface (*i.e.* inside the white matter), with an offset in between (see Figure 7), the interfaces propagate along the outward normal direction stopping at the desired place, while maintaining certain distance between them.

Embedding each surface as the zero level set in its own level function, we have two equations:

$$\Psi_{in_t} + F_{in} |\nabla \Psi_{in}| = 0 \quad (4)$$

$$\Psi_{out_t} + F_{out} |\nabla \Psi_{out}| = 0 \quad (5)$$

where F_{in} and F_{out} are functions of the surface normal direction, image-derived information and distance between the two surfaces. The coupling is embedded in the design of F_{in} and F_{out} . At places where the distance between the two surfaces is within a normal range, the two surfaces propagate according to the image-based information. Where the distance between the two surfaces is out of the normal range, the distance imposes a constraint on the propagation of the surfaces.

With the level set implementation, we have a natural way to establish a correspondence between the points on the two evolving surfaces through distance, which is evaluated with little extra computational expense. Recall that the value of the level function of a front at any point is simply the distance from this point to the current front, which as in [33], is calculated as the shortest distance from this point to all the points on the front. In our case of two moving surfaces, for any point on the inner moving surface, the distance to the outer moving surface is the value Ψ_{out} at this point, and vice versa for the point on the outer moving surface. Hence, we write

$$F_{in} = g(p_{BC}(\vec{\theta}^*))h(\Psi_{out}) \quad (6)$$

$$F_{out} = g(p_{AB}(\vec{\theta}^*))h(\Psi_{in}) \quad (7)$$

where g and h are the functions as shown in Figure 4, and A, B, C denote CSF, gray matter and white matter respectively.

Function g maps larger likelihood to slower speed, *i.e.*, as the likelihood gets larger, g tends to zero, while as the likelihood gets to near zero, g tends to a constant. Function h

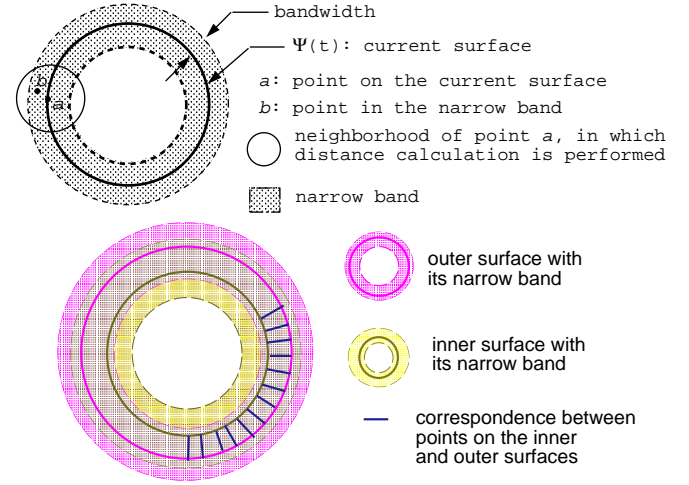


Fig. 5. Schematic of narrow band implementation for 2D curve case (same argument holds in 3D). Top: dynamic construction of the narrow band and the update of the level function Ψ within are performed in the neighborhood of the current surface. Bottom: inner and outer surfaces with their narrow bands. Notice the inner surface lies within the narrow band of the outer surface, and vice versa.

penalizes the distance off the normal range. As the distance goes out of normal range, h goes to zero. Thus, each surface moves with constant speed along its normal direction, and slows down when either the image-based information becomes strong or the distance to the other surface moves away from the normal range. Each surface finally stops when the image-derived information is strong enough or the distance to the other surface is out of the normal range.

Based on the fact that the speed terms are designed to force the propagating level set to stop at the desired boundary, the image dependent speed terms have meaning only on the front, *i.e.* the zero level set. However the level set equation of motion is written for the function Ψ defined over the entire image grid. We thus extend the speed terms from the zero level set to the whole image grid as in [33], *i.e.* point b takes on the speed of point a which is the closest point to b and lies on the zero level set.

Due to the level set formulation, we have a notion of the inside and outside of the current moving front, which is embedded in the outward normal direction \vec{n} . This information can be used to reduce the feasible space of possible $\vec{\theta}$ s, or \vec{n} can be used directly as an estimate of $\vec{\theta}^*$, thus obtaining a better result.

E. Narrow Band Method and Distance Correspondence

For computational efficiency, the algorithm is implemented using a narrow band method [33], which modifies the level set method so that it only explicitly updates the points close to the current propagating fronts. Our implementation of the narrowband method uses this idea, but is designed specifically for coupled level sets so that the distance between the two embedded surfaces (necessary for the computation of the speed terms) is available with no further computation after narrowband rebuilding.

Based on the fact that any point b in the narrow band

Algorithm Diagram

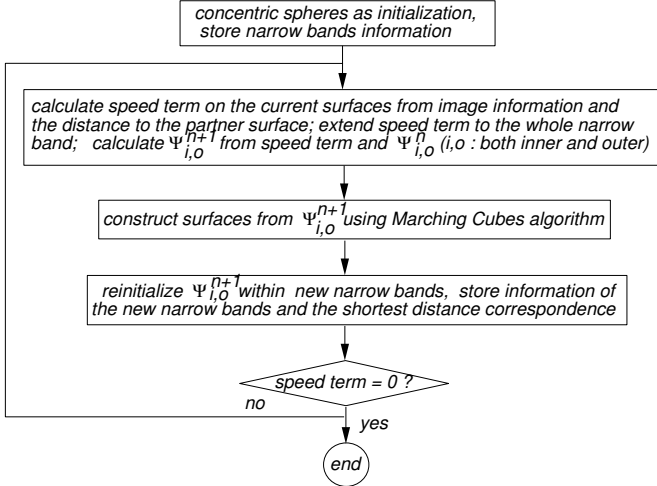


Fig. 6. Algorithm diagram

of the current surface should be within some neighborhood of a certain point a on the current surface, the narrow band is constructed dynamically in the 3D neighborhood of each point on the current surface by including points that lie within a certain distance range (*i.e.* bandwidth) away from that particular point. Also, since a point b in the narrow band can be within the neighborhood of several points a_1, \dots, a_l on the current surface, we update the value of the level function Ψ at b to be

$$\text{sign}(\Psi(b)) \cdot (\text{Min}_{i=1, \dots, l} \text{dist}(b, a_i))$$

where function dist gives the positive Euclidean distance.

The steps for rebuilding the narrow band and updating Ψ inside the band are as follows:

```

for every point  $a$  on the current front {
  for every point  $b$  in the neighborhood of  $a$  {
    if  $b$  is not already in the narrow band,
      then add  $b$  to the narrow band;
    if  $\text{dist}(b, a)$  is less than
      the absolute value of the current  $\Psi(b)$ ,
      then update  $\Psi(b)$  to be  $\text{sign}(\Psi(b)) \cdot \text{dist}(b, a)$ ;
  }
}

```

The size of the neighborhood depends on the allowed bandwidth, and therefore is fixed. Thus, for a surface represented using N points, the construction of its narrow band and the update of Ψ in the narrow band is an $O(N)$ calculation.

In our application, two different narrow bands are computed for the inner and outer interfaces respectively. As shown in Figure 5, to ensure that the distance-based correspondence between the coupled surfaces falls out automatically, the two bandwidth ranges (for the inner and outer narrow bands separately) are chosen such that the inner surface lies within the narrow band of the outer surface and vice versa. Thus, at each time step, the current position of

the propagating coupled surfaces and the surrounding narrow bands are estimated, and the whole process repeats until the speed terms for both the inner and outer surfaces reach a zero value everywhere. To summarize, the algorithm diagram is shown in Figure 6.

F. Measurement

With the coupled surfaces propagation via level set methods, it is easy to perform various measurements on the cortical layer with little extra computational expense. Whole brain volume, cortical gray matter volume, white matter volume, cortical surface area, cortical surface shape and cortical thickness maps are among the features most interesting in the study of brain structure and function. Different combinations of the above measurements may help in determining the pathobiology of various neuropsychiatric disorders. We now discuss one by one the above measurements from our coupled surfaces formulation.

Volume With the signed distance function Ψ , the level set formulation keeps track of the inside and outside of the current moving front. Once the evolution of the coupled surfaces is completed, the cortical gray matter voxels are those that lie inside the outer cortical surface while outside the inner cortical surface. In the same fashion, non-brain tissue voxels will be the ones that are outside the outer cortical surface, and voxels of white matter will lie inside the inner cortical surface except for sub-cortical gray matter and ventricles.

Because the signed distance based measures has a sub-voxel accuracy, we can obtain a sub-voxel segmentation instead of a binary segmentation on the data set. In other words, if the distance from a voxel to the zero level set surface is less than the voxel size in width, the voxel is considered to contain multiple tissue types.

Surface area A marching cubes algorithm [20] is performed on the signed distance functions, Ψ_{in} and Ψ_{out} , to extract the embedded zero level sets. The resulted surfaces are realized using a triangular representation. Surface area is then calculated as the sum of the areas of the triangles.

Surface curvature and shape index As discussed above, one advantage of the level set implementation is that geometric properties of the propagation front are easily calculated [33]. In our case of surfaces propagating in 3D space, there are many choices for the curvature of the front (for formal definitions of the curvatures, refer to [7]), including mean curvature, κ_M , and Gaussian curvature, κ_G . Both may be conveniently expressed [33] in terms of the level set function Ψ :

$$\kappa_M = \frac{\sum_{(i,j,k) \in C} ((\Psi_{ii} + \Psi_{jj})\Psi_k^2 - 2\Psi_i\Psi_j\Psi_{ij})}{2(\Psi_x^2 + \Psi_y^2 + \Psi_z^2)^{3/2}} \quad (8)$$

$$\kappa_G = \frac{\sum_{(i,j,k) \in C} (\Psi_i^2(\Psi_{jj}\Psi_{kk} - \Psi_{jk}^2) + 2\Psi_i\Psi_j(\Psi_{ik}\Psi_{jk} - \Psi_{ij}\Psi_{kk}))}{(\Psi_x^2 + \Psi_y^2 + \Psi_z^2)^2} \quad (9)$$

where $C = \{(x, y, z), (y, z, x), (z, x, y)\}$ is the set of circular shifts of (x, y, z) .

The maximum principle curvature, κ_1 , and the minimum principle curvature, κ_2 , are related to Gaussian and mean curvatures through the following formulas:

$$\kappa_1 = \kappa_M + \sqrt{\kappa_M^2 - \kappa_G}; \quad \kappa_2 = \kappa_M - \sqrt{\kappa_M^2 - \kappa_G};$$

We also adopt the classification of surfaces by Koenderink [15] using the numerical relationship between the two principal curvatures. A shape index function is defined as $si = \frac{2}{\pi} \arctan((\kappa_1 + \kappa_2)/(\kappa_1 - \kappa_2))$, which classifies the surfaces into nine types as show in Figure 11. With the shape index, gyri (mostly ridges) and sulci (mostly ruts) are automatically identified. Further potential use of the shape index includes the definition of an atrophy index (sulci widen with age).

Thickness map As discussed above, the value of the level function of a front at any point is the distance from this point to the current front. Also recall that the inner and outer surfaces are the zero level sets of Ψ_{in} and Ψ_{out} . Thus, for any point on the outer surface, the absolute value of Ψ_{in} at the point is simply the distance from the point to the inner surface. Using this measure, we obtain a thickness map between the inner and outer cortical surfaces, which can be used to study the normal thickness variations across different regions of the brain, and also the abnormalities in brain structures.

III. EXPERIMENTAL RESULTS

In this section, we show validations of our approach on various simulated and real MR data, as well as applications to specific cortical studies. We use only T1-weighted images because they provide the best gray/white contrast [31], and are therefore commonly used for neuroanatomical analysis.

A. Validation on Simulated MR Data with Ground Truth

We first present our segmentation results using the simulated MR brain images provided by the McConnell Brain Imaging Center at the Montreal Neurological Institute [12]. The images are generated using an MRI simulator [16] which allows users to independently control various acquisition parameters to obtain realistic MR images. The ground truth of the phantom is provided in the form of membership functions of each voxel belonging to different tissue types, such as the skull, CSF, gray matter and white matter.

The simulated data we tested our algorithm on were T1 images of normal brain, with the following parameter settings: voxel size= $1mm^3$, noise= 3%, intensity non-uniformity= 0%. Starting from the unedited images, no further user interaction is needed after specifying several pairs of concentric spheres as initialization. The spheres grow out and automatically lock onto the inner and outer cortical surfaces. As long as the spheres are placed inside the white matter, the algorithm is robust to starting position. Measurement of the volume is then done as described

TABLE I

COMPARISON OF OUR VOLUME MEASUREMENTS WITH THE PHANTOM GROUND TRUTH. WHOLE BRAIN: TOTAL BRAIN TISSUE (WHITE+GRAY MATTER); CORTICAL GRAY MATTER *: CORTICAL GRAY MATTER ON THE FRONTAL 49 CORONAL SLICES AND THE TOP 56 AXIAL SLICES;

%	whole brain	cortical gray matter *	white matter
TP rate	92.3	92.8	92.4
FP rate	2.0	6.0	3.3
volume ratio	96.3	103.2	98.1

in the previous section; we use a binary segmentation in this experiment. In our implementation of cortex segmentation, the allowed distance between the inner and outer surfaces is set to range from $1.5mm$ to $5.5mm$ based on knowledge from reported postmortem studies [1]. Therefore, to ensure the proper overlapping of the inner and outer narrow bands, the bandwidth ranges for the inner and outer interfaces are chosen to be $(-3mm, 6mm)$ and $(-6mm, 3mm)$ respectively.

To evaluate the segmentation result, we apply several measures defined as follows. For any tissue type T in the region of interest, we denote the voxels of tissue type T recovered from our 3D algorithm as V_a and the voxels that are mostly of tissue type T according to the phantom (*i.e.* the value of tissue T membership function is greater than 0.5) as V_e . We denote the overlap of V_a and V_e as V_{ae} , and the part that is in V_a but not in V_e as $V_{ae'}$. A *true positive (TP) rate* is then defined to be the size of V_{ae} relative to the size of V_e , while the *false positive (FP) rate* is defined to be the ratio of the size of $V_{ae'}$ to the size of V_e . We also define the *volume ratio* to be the volume of all the voxels segmented as of tissue type T by our algorithm to the total sub-voxel volume of tissue type T specified by the phantom (sub-voxel contribute in only part of the voxel volume).

Table I shows our measurement results over 3 types: total brain tissue (including white matter and gray matter), cortical gray matter in selected slices, and white matter. Since the algorithm is designed specifically for the nearly constant thickness of the cerebral cortex, it recovers only part of the gray matter in the brain stem and the cerebellum where the constant thickness constraint is not well satisfied. These regions account for most of the errors in the TP rate and volume ratio for whole brain tissue. For the same reason that the algorithm is specifically tailored for the cerebral cortex, we would compare the cortical gray matter volume only in the cerebrum. Since the phantom data does not provide the information related to partitioning cerebrum, the cerebellum and the brain stem, we only compare the cortical gray matter volume on selected slices where cerebellum and brain stem are excluded: frontal 49 coronal slices and top 56 axial slices. The resulting average error of the TP and FP rate is around 6% to 7%, and the volume ratio error is within 4%. For the white matter, the errors for the TP, FP rate and volume ratio are also low. These results show that our algorithm performs well in iso-

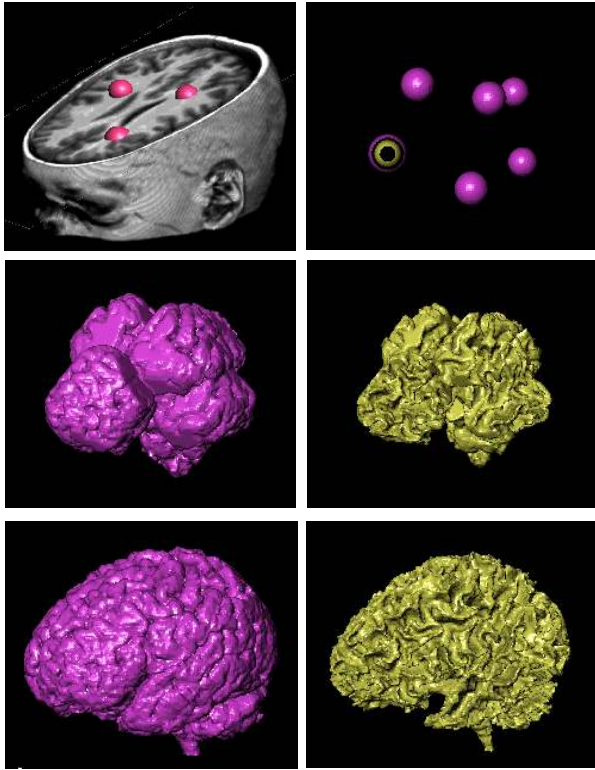


Fig. 7. Propagation of the outer (pink) and inner (yellow) bounding surfaces. Top: pairs of concentric spheres (only the outer ones are shown on the left, both are shown with a cutting plane on the right) as initialization in unedited 3D MR brain images; middle: intermediate step in surface propagation; bottom: final result of the outer and inner cortical surfaces.

lating the brain from non-brain tissues and in segmenting the cortex.

B. Validation on 20 Normal Brains

To further evaluate our segmentation approach under a wide range of imaging conditions, we tested the algorithm on real MR data and compared the results obtained with gray segmentation by manual experts. Since for 3D data it is a very labor intensive job to segment gray and white matter, we utilized the data provided by the Internet Brain Segmentation Repository (IBSR) of the Center for Morphometric Analysis (CMA) at Massachusetts General Hospital [11].

The purpose of IBSR is to encourage the development and evaluation of segmentation methods by providing test image data, human expert segmentation results, and methods for comparing segmentation results. It is one of the first efforts to offer solutions to the problem of validating and comparing new algorithms in this rapidly growing medical image analysis field. The test image data sets provided in this repository permit a standardized mechanism for evaluation of the sensitivity of a given analysis method to signal to noise ratio, contrast to noise ratio, shape complexity, degree of partial volume effect, etc.

We obtained 20 normal MR brain data sets and their manual segmentations from IBSR. These 20 coronal 3D T1-weighted spoiled gradient echo MRI scans were performed

on two different imaging systems. Ten FLASH scans on four males and six females were performed on a 1.5 tesla Siemens Magnetom MR System (Iselin, NJ) with the following parameters: TR = 40 msec, TE = 8 msec, flip angle = 50 degrees, field of view = 30 cm, slice thickness = contiguous 3.1 mm, matrix = 256x256, and averages = 1. Ten 3D-CAPRY scans on six males and four females were performed on a 1.5 tesla General Electric Signa MR System (Milwaukee, WI), with the following parameters: TR = 50 msec, TE = 9 msec, flip angle = 50 degrees, field of view = 24 cm, slice thickness = contiguous 3.0mm, matrix = 256x256, and averages = 1.

All data sets were positionally normalized at CMA by imposing a standard 3D brain coordinate system on each 3D MR scan using the midpoints of the decussations of the anterior and posterior commissures and the mid-sagittal plane at the level of the posterior commissure as points of reference for rotation and (non-deformation) transformation [37], [8]. The repositioned scans were then resliced into normalized 3.0mm coronal, 1.0mm axial, and 1.0mm sagittal scans which were used for subsequent analysis.

Manual segmentation was performed on the normalized scans by trained investigators at CMA using a semi-automated intensity contour mapping algorithm [14], [11]. Once the external border was determined by intensity contour mapping, grey-white matter borders were demarcated using signal intensity histograms. Using this technique, borders were defined as the midpoint between the peaks of the bimodal histogram for a given structure and its adjacent tissue. Other neuroanatomical structures were segmented similarly [9].

An overlap metric is used by IBSR to compare results from automatic segmentation and manual segmentation. While manual segmentations are not "ground truth", they provide reasonable way to compare automated segmentation methods. The overlap metric is defined for a given voxel class assignment as the number of voxels that have the class assignment in both segmentations divided by the number of voxels where either segmentation has the class assignment, which is equivalent to $TP/(1+FP)$. This metric ranges from 1.0, for perfect agreement, to 0.0, for no agreement of classified voxels.

We interpolated the image data into 1mm thick coronal slices, and then ran our coupled surfaces algorithm. Figure 8 shows the overlap metric for gray matter segmentation on 20 normal brains from the manual method, various automatic segmentation methods and our coupled surfaces algorithm. The results from the automatic segmentation provided by IBSR were from work done by Rajapakse, and partially based on the methods described in [26]. The gray matter overlap metric for our algorithm on the whole brain is 0.657, which is well above those from the other 6 listed automatic methods ranging from 0.473 to 0.564 (shown in column 1-6 in Figure 8). Since our algorithm is designed specifically for the cerebral cortex, we compute an improved overlap metric on the upper and frontal part of the brain (to exclude brain stem and cerebellum) of 0.701. Moreover, considering that the other 6 listed automatic

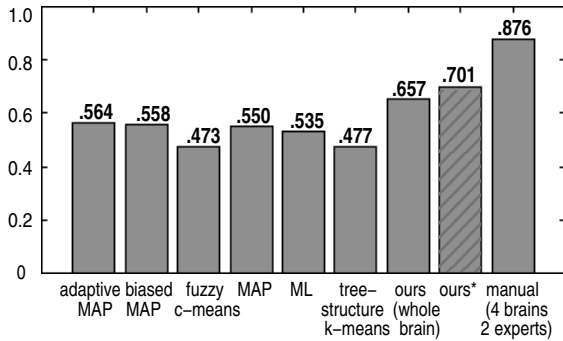


Fig. 8. Average overlap metric for gray matter segmentation on 20 normal brains from various segmentation methods. The results of automatic segmentation methods provided by IBSR were from work done by Rajapakse. MAP: Maximum A Posteriori Probability. ML: Maximum-Likelihood. *: using frontal 13 coronal slices and upper 50 axial slices of each brain to exclude brain stem and cerebellum.

methods started with brain-only data sets, while the coupled surfaces algorithm started with un-stripped brain images, the advantage of our method with geometric structural constraints is clear.

These 20 brain scans were chosen by IBSR because they have been used in published studies [26], and cover a range of image quality [11] with the worst ones having low contrast and relatively large intensity inhomogeneities. The overlap scores shown in Figure 8 from the automatic classification methods may appear low, however they need to be taken into the context of a wide range of image quality, and should not be compared with numbers from different studies. More recently acquired (i.e. better quality) data should result in far better results from the automatic classification methods, which holds for our coupled surfaces algorithm as well. In fact, as shown in the section above, the overlap metric for our phantom cortical segmentation is $0.928/(1 + 0.060) = 0.875$, which compares well with the manual overlap metric of 0.876 showing inter-operator reproducibility from tests on 4 brains averaged over 2 experts (see Figure 8). With the rapid growth of medical image processing, it is virtually impossible to implement all the novel methods published and compare results. However we take this study as our initial step towards more extensive evaluation of our algorithm with the help of IBSR, and we intend to carry out more studies.

C. Results on Real MR Data for Frontal Lobe Study

We then tested our algorithm on frontal lobes of 7 high resolution MRI data sets (SPGR, 2NEX, $1.2 \times 1.2 \times 1.2 \text{ mm}^3$ voxels) from a randomly chosen subset of young adult autistic and control subjects from our ongoing studies to measure frontal lobe volume. After preprocessing to reduce the effects of MR bias field inhomogeneity using a simple standard nonlinear map (this is also a step before expert manual tracing), we ran the coupled surfaces algorithm to isolate the brain tissue and segment the cortex (see Figure 7). The frontal lobe was then manually defined independently in the left and right hemispheres as all tissue anterior

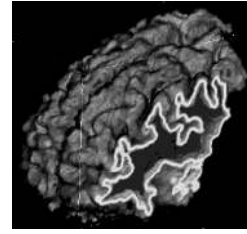


Fig. 9. 3D volume rendering of the frontal lobe cortex with an oblique cutting plane. The convoluted thin bright ribbon is the cortical gray matter captured on the cutting plane.



Fig. 10. Coronal slices from 3D images. Left: original image; middle: cortical gray matter from manual tracing; right: cortical gray matter from our 3D algorithm.

to the central sulcus, excluding sub-cortical nuclei [28]. We then create a mask of the frontal lobe, and use it to exclude the posterior part of the volume.

Figure 9 shows a 3D volume rendering of the cortical gray matter of a frontal lobe resulting from our algorithm. In Figure 10, 2D coronal slices of the same result are shown. As shown in Table II, over the 7 frontal lobes, the TP and FP rate (compared to manual tracing by our neuroanatomy specialist) of the whole frontal lobe averaged 94.1% and 2.1% respectively, which demonstrated that our algorithm nicely isolated the brain tissue from the non-brain tissue. The average TP and FP rate for the cortical gray matter (measured on 2 orthogonal slices, one coronal and one axial, to over the entire range of the frontal lobe) in the frontal lobe were 86.7% and 20.8%. As we see in Figure 10, the expert tracing tended to be more aggressive in defining the gray/white matter boundary, which resulted in the relatively larger value of the FP rate. Note that the FP rate on gray/white segmentation is a very sensitive measure, especially considering the fact that manually drawing a boundary between gray and white matter to some extent depends on subjective individual judgment. However, in quantifying the difference between populations, despite the FP rates, the volume measurements would still yield useful information as long as they are consistent.

The volume of the constituent parts of the brain is typically the measurement of interest for comparison among different subjects in studies of neuroanatomy. Thus, as a second way to analyze the utility of our algorithm, we compute reliability statistics on the volume measurements using the methods described in [31] (see also [42]). There was strong agreement between the algorithm and the expert on the volume of the frontal lobe (Pearson $r = .991$; intraclass correlation coefficient [ICC] = .901). The algorithm systematically estimated the frontal lobe volume to be less than the expert tracer (mean difference = 4%), and this accounts for the lower ICC than Pearson coefficient.

TABLE II

OUR MEASUREMENTS COMPARED WITH EXPERT TRACING RESULTS ON
7 FRONTAL LOBES

frontal lobe		frontal lobe cortex	
TP(%)	FP(%)	TP(%)	FP(%)
93.8	3.4	83.6	25.5
93.9	1.9	86.2	20.1
95.2	2.9	86.5	24.4
93.7	1.7	86.7	24.5
94.5	1.5	88.9	21.2
94.1	1.7	87.0	20.5
94.1	1.4	89.0	19.5

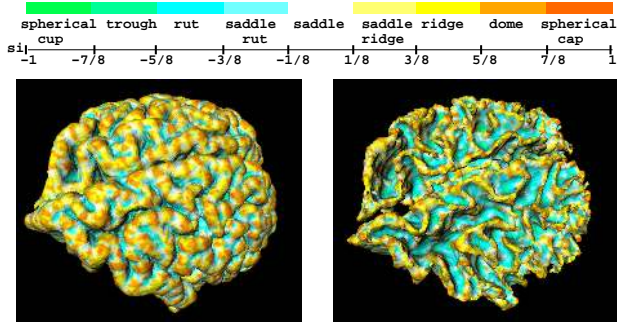


Fig. 11. The outer and inner cortical surfaces of a frontal lobe colored with the specified spectrum representing shape index *si*.

cient. Similarly, for gray matter volume of the frontal lobe there was also good agreement (Pearson $r = .96$). Thus, for both whole frontal lobe volume and frontal gray matter volume, the coupled surfaces algorithm produced measurements that were very similar to expert tracings.

Figure 11 shows the outer and inner cortical surfaces of a frontal lobe colored with their shape indices. As we can see, most parts of the gyri are automatically identified as ridge while most parts of the sulci are identified as rut, which coincides with our knowledge of the cortical structure.

D. Regional Cortical Thickness

We further applied our algorithm to 7 high resolution MRI data sets (SPGR, 2NEX, $1.2 \times 1.2 \times 1.2 \text{ mm}^3$ voxels) of normal males (average IQ = 109) to study the pattern of regional cortical thickness.

The lobes of the brain were labeled using locally developed software [29] in conjunction with the ANALYZE software package [30]. The frontal lobe was segmented by tracing the central sulci directly on 3D renderings of the brain, and then in successive 2D slices extending the traces to the depth of the sulci and through the white matter to the mid-line at an angle perpendicular to the inter-hemispheric fissure. Next, the temporal lobes were segmented by tracing the sylvian fissure on 3D renderings until the point where the fissure arched upward into the parietal lobe. At that point of inflection, a plane parallel to the AC-PC was used to segment the temporal and parietal lobes. The occipital-parietal boundary was set at mid-line by placing an oblique plane through the parietooccipital sulcus, and

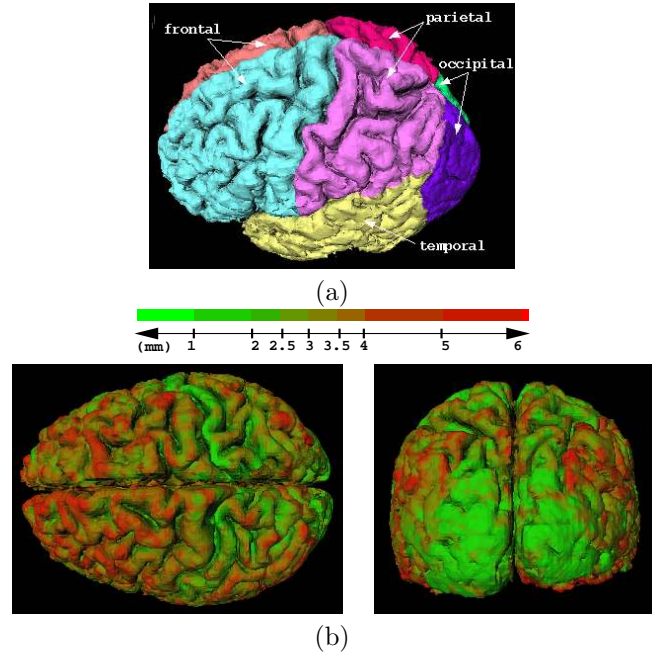


Fig. 12. Regional cortical thickness. (a): Parcellation of lobes where regional cortical thickness is measured. (b): Top and back views of an outer cortical surface colored with cortical thickness.

TABLE III

REGIONAL CORTICAL THICKNESS (IN *mm*) OF 7 NORMAL MALE
SUBJECTS

frontal	temporal	parietal	occipital
3.35	3.18	2.81	2.82
3.47	3.14	2.95	2.95
3.18	3.00	2.70	2.67
3.18	2.83	2.59	2.46
3.39	3.30	2.95	2.60
2.97	2.95	2.56	2.44
2.99	3.04	2.78	2.44

a coronal plane at the intersection of the parietooccipital sulcus and the calcarine fissure. Figure 12(a) shows the parcellation of the lobes of a cerebrum, as described above.

Shown in Figure 12(b) are the top and back views of an outer cortical surface colored with cortical thickness. Table III lists the cortical thickness measurements in 4 lobes over the 7 subjects. We compared the mean thickness of each lobe to the data on 63 males from the postmortem study by Pakkenberg and Gundersen [27], and found the exact same rank ordering of thickness; the frontal cortex was the thickest and the occipital the thinnest. The postmortem data measurements were 5 to 14% thinner by lobe than our in vivo data. This might be due to both the older age of the subjects, tissue shrinkage in the postmortem study, and volume averaging with our MRI data. However, it is important to note that the variability of thickness was the same for both samples (about 0.15 mm). This gradient of thickness from front to back in the brain is well known and due to the greater number of large pyramidal neurons in the anterior as compared to the posterior cortices.

A repeated measures analysis of variance (ANOVA) tested whether cortical thickness differed by lobe, and found significant differences between the 4 lobes ($F[3, 27] = 56.3$, $p < .0001$). Post hoc paired t tests showed that the frontal lobe and temporal lobes were each significantly thicker than either the parietal and occipital lobe (p 's $< .001$), but they did not differ in thickness from one another. Likewise, parietal and occipital lobe thickness were not significantly different.

E. User Interaction and Speed Issue

In addition to robustness and accuracy, minimum user interaction and computational efficiency have always been two important issues in the problem of segmenting and measuring the cortex. For an expert to manually isolate the non-brain tissue (using a combination of image thresholding, region growing, and fine editing with manual tracing slice by slice to carefully remove any non-brain voxels such as the CSF within sulci and the dura) alone can take about 2 hours. (Structures such as the dura and the CSF in sulci can only be removed by careful slice-by-slice inspection. Therefore, considering the thoroughness and obsessiveness of the fine editing, we believe 2 hours is a fair estimate of the processing time.) The manual tracing of cortical gray matter is even more time consuming. MacDonald *et al.* deformed two ellipsoids with inter-surface constraints to approximate the inner and the outer cortical surfaces. Their processing time for such segmentation on each subject was reported to be 100 hours on a SGI Origin 200 R10000 processor running at 180 MHz [22]. In [5], it was reported that the “ribbon” algorithm was a fairly computationally demanding iterative procedure; while manual placement of the initial cortical surface and a multi-scale formulation could decrease the computational load. The processing time per subject for Xu’s method was reported to vary between 4.5 to 6.5 hours on a SGI O2 workstation with a 174MHz R10000 processor [41].

The initialization for our algorithm only requires the user to specify several pairs of concentric spheres in the unedited images, which can be done with several mouse clicks within seconds. It should be emphasized that neither the number nor the placement of the spheres (within a broad range of acceptable values) affects the accuracy or the reproducibility of the final result. To illustrate this, Figure 13 shows the coupled surfaces propagation on the same brain as in Figure 7 but from a different set of initializing spheres. The final results of the surfaces show little visual difference. Quantitatively the TP rate of one with respect to the other is over 99.5%, and FP rate is less than 0.5%.

For a 3D image ($1.2 \times 1.2 \times 1.2 \text{ mm}^3$ in voxel size) of the whole brain, our algorithm runs in about 1 hour on a SGI Indigo2 machine with a 195MHz R10000 processor. **Skull-stripping, segmentation and measurement of the cortex are done simultaneously.** Comparatively, to our knowledge our algorithm outperforms other related techniques with respect to user interaction and computational efficiency.

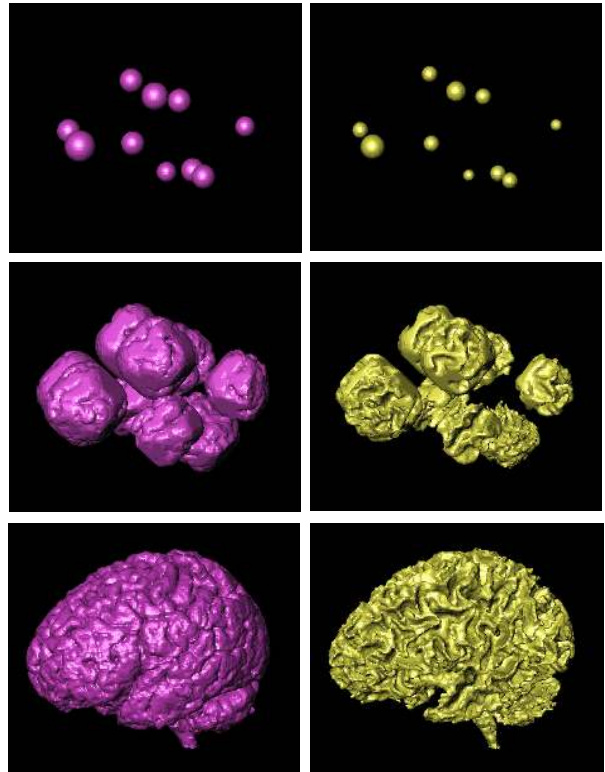


Fig. 13. Coupled surfaces propagation on the same brain image as in Figure 7 but with a different set of initializing spheres. For the two final results from different initialization, the TP rate of one with respect to the other is over 99.5%, and FP rate is less than 0.5%, which demonstrates our algorithm’s robustness to initialization.

IV. SUMMARY AND FUTURE DIRECTIONS

In this paper, we presented a new approach to the segmentation and measurement of cortical structure which is of great interest in the study of the structural and functional characteristics of the brain. Motivated by the fact that the cortex has a nearly constant thickness, we model the cortex as a volumetric layer, which is completely defined by the two bounding surfaces and the homogeneity in between. Starting from easily initialized concentric spheres, and driven by image-derived information, two interfaces evolve out to capture the inner and outer cortical boundaries, thereby segmenting out the cortical gray matter from the white matter, as well as isolating the brain tissue from the non-brain tissue. Cortical gray matter volume and cortical surface area (both inner and outer) are then measured. Due to the coupled level set implementation, the cortical surface curvature and cortical thickness map are also easily obtained. As seen from various experiments, our algorithm is automatic, accurate, robust and relatively computationally efficient.

We would like to mention that this segmentation method using coupled surfaces propagation has potential applications in other medical image analysis domains where a volumetric layer is the study of interest. Examples include the left ventricular (LV) myocardium of the heart and the bounding wall of the liver. Different coupling may be used

to tailor the algorithm for specific application. For example, the endocardial and epicardial walls which bound the thick LV myocardium are loosely coupled, instead of tightly coupled as the cortical surfaces.

Future directions for this work include the following: finer design of the local feature operator to better model the volume averaging effect, better capturing the homogeneity of the volume, volume measurement on the sub-voxel level, possible use of a vector image data set, and testing on image data of abnormal brains.

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