

# Self-Constructive High-Rate System Energy Modeling for Battery-Powered Mobile Systems

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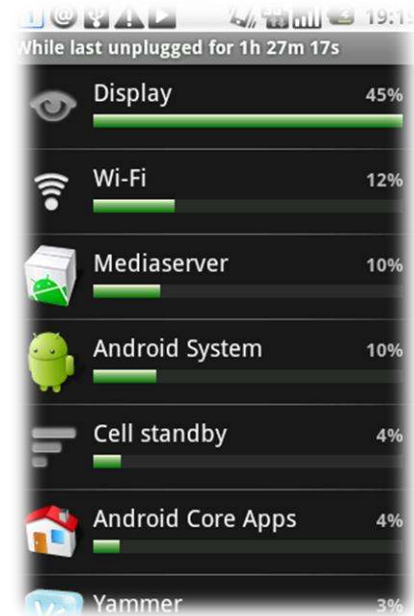
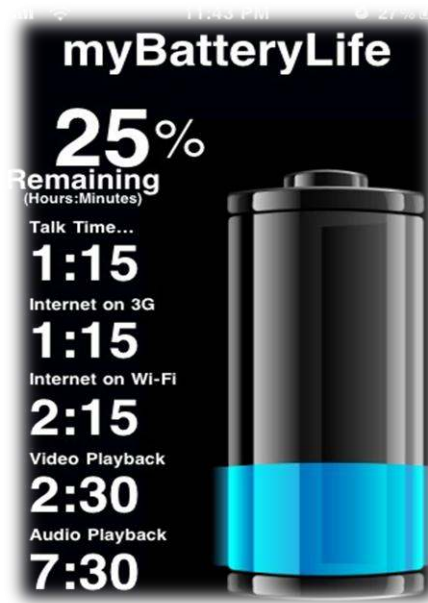
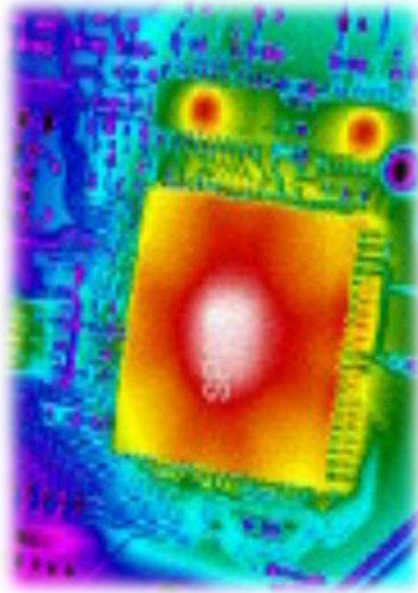
# System Energy Model

$$y(t) = f(x_1(t), x_2(t), \dots, x_p(t))$$

Response  $y(t)$ :  
Energy consumed  
by the system in  $t$

Predictors  $x_i(t)$ :  
System status  
variables in  $t$

# Rate ( $1/t$ )



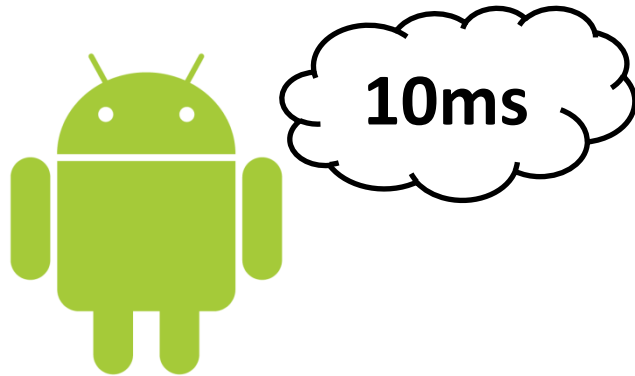
0.01Hz

1Hz

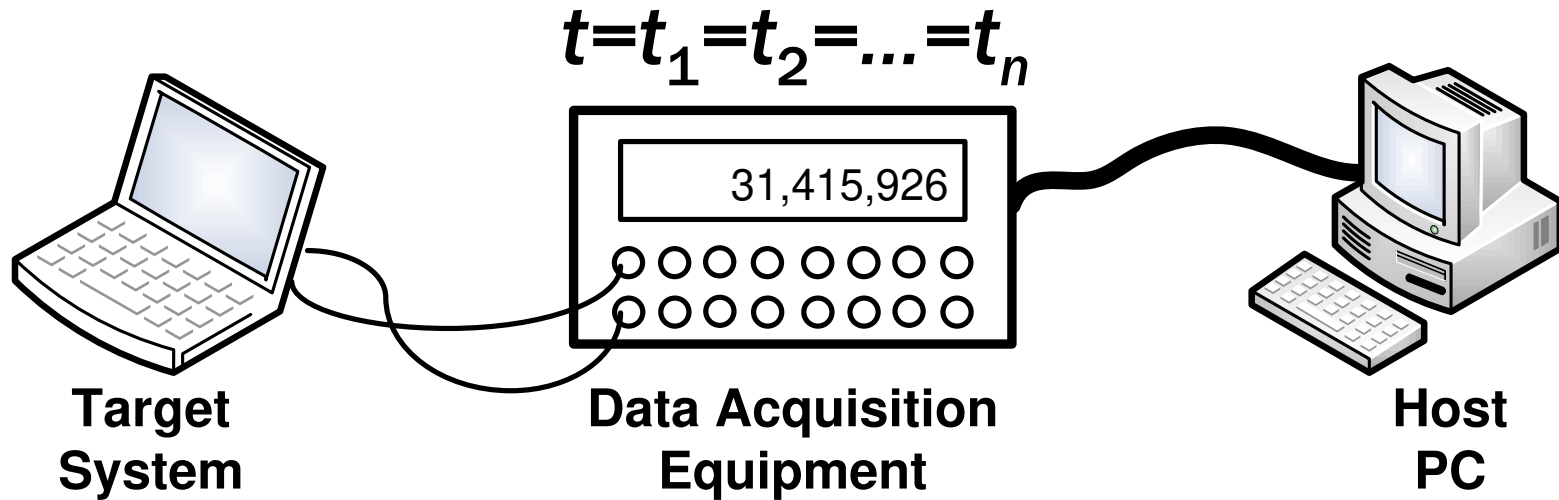
100Hz

# A High-Rate Energy Model

is needed to provide an energy reading  
at each OS scheduling interval



# Model Construction



$x_1(t_1) \ x_2(t_1) \ \dots \ x_p(t_1)$

$x_1(t_2) \ x_2(t_2) \ \dots \ x_p(t_2)$

$\vdots$

$\vdots$

$\ddots$

$\vdots$

$x_1(t_n) \ x_2(t_n) \ \dots \ x_p(t_n)$

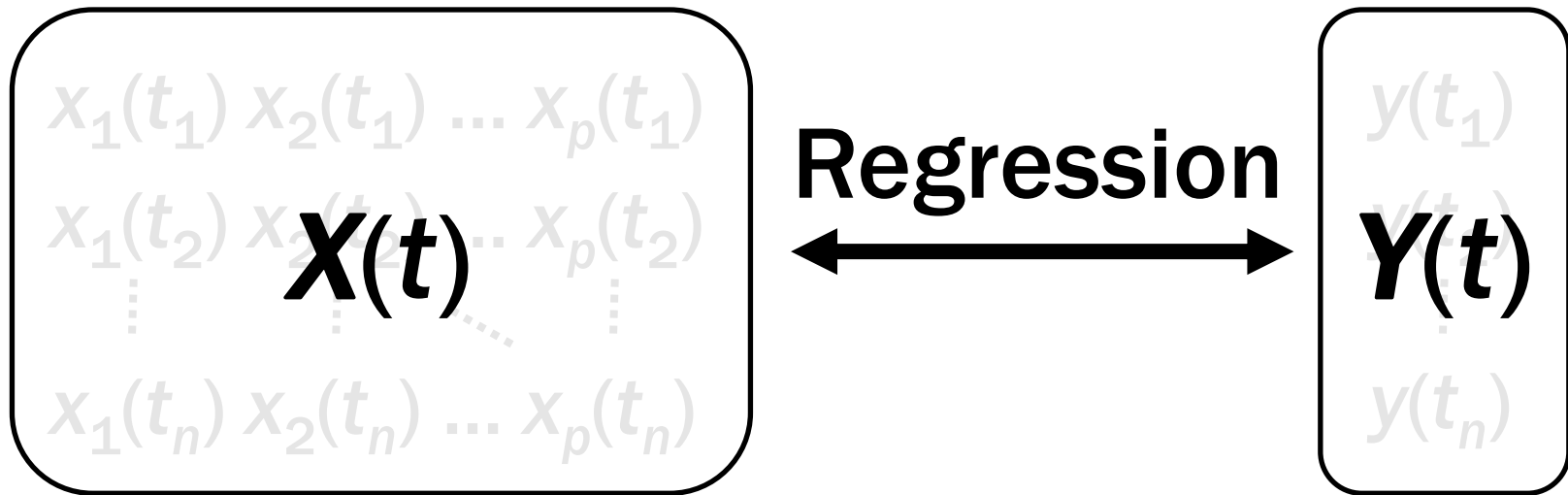
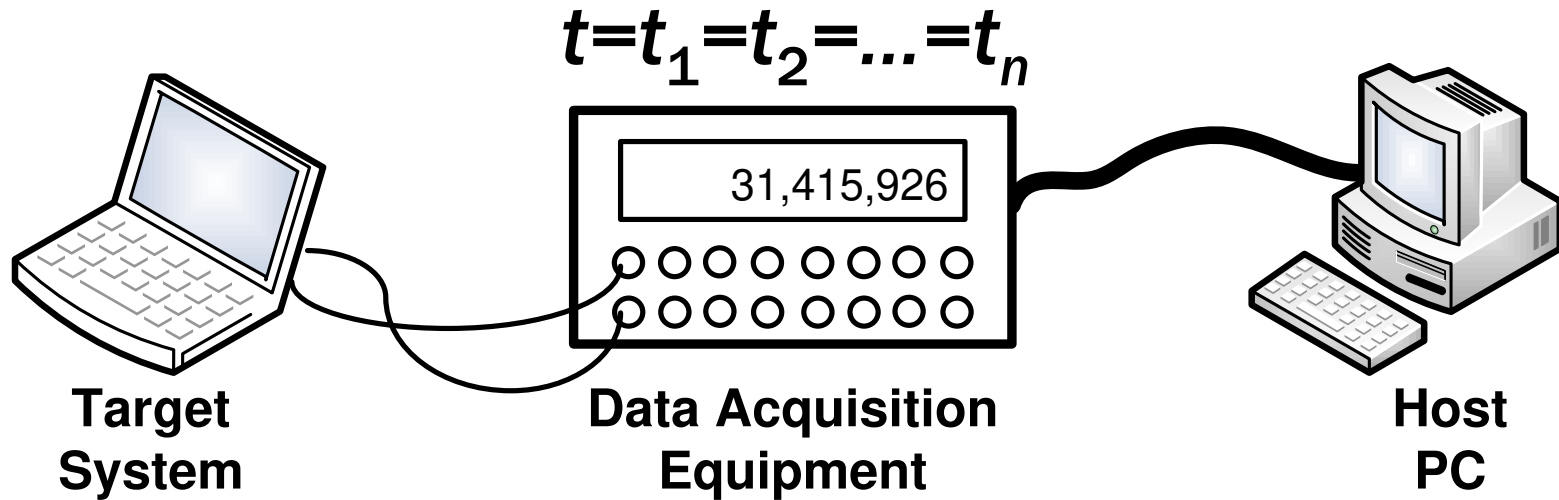
$y(t_1)$

$y(t_2)$

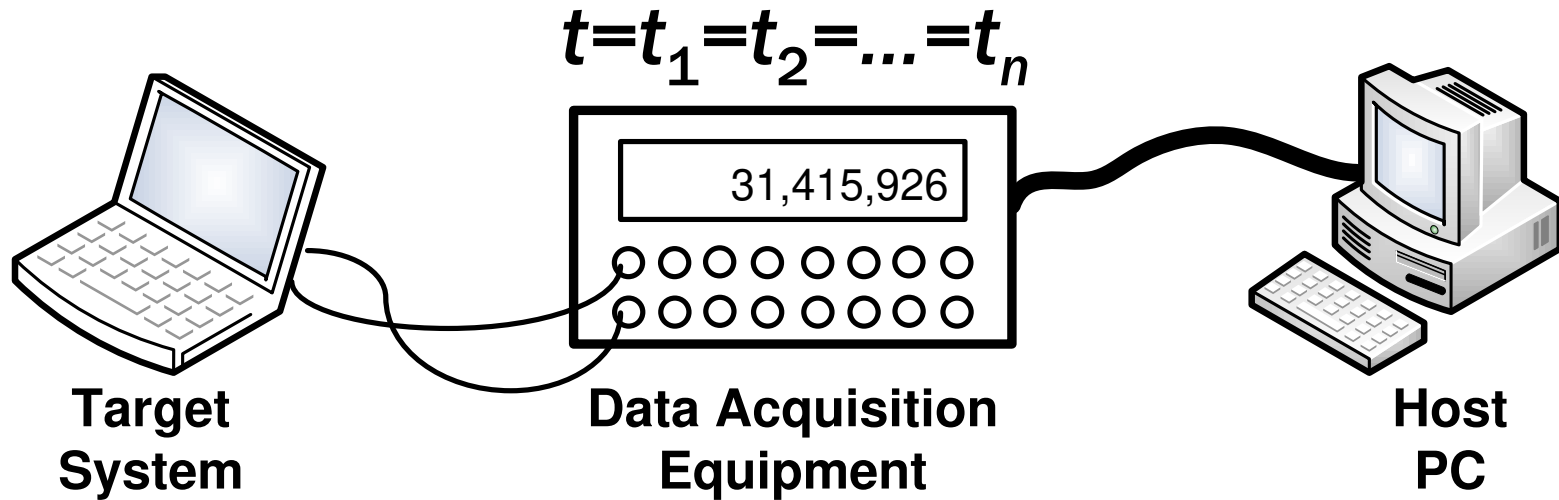
$\vdots$

$y(t_n)$

# Model Construction



# Model Construction

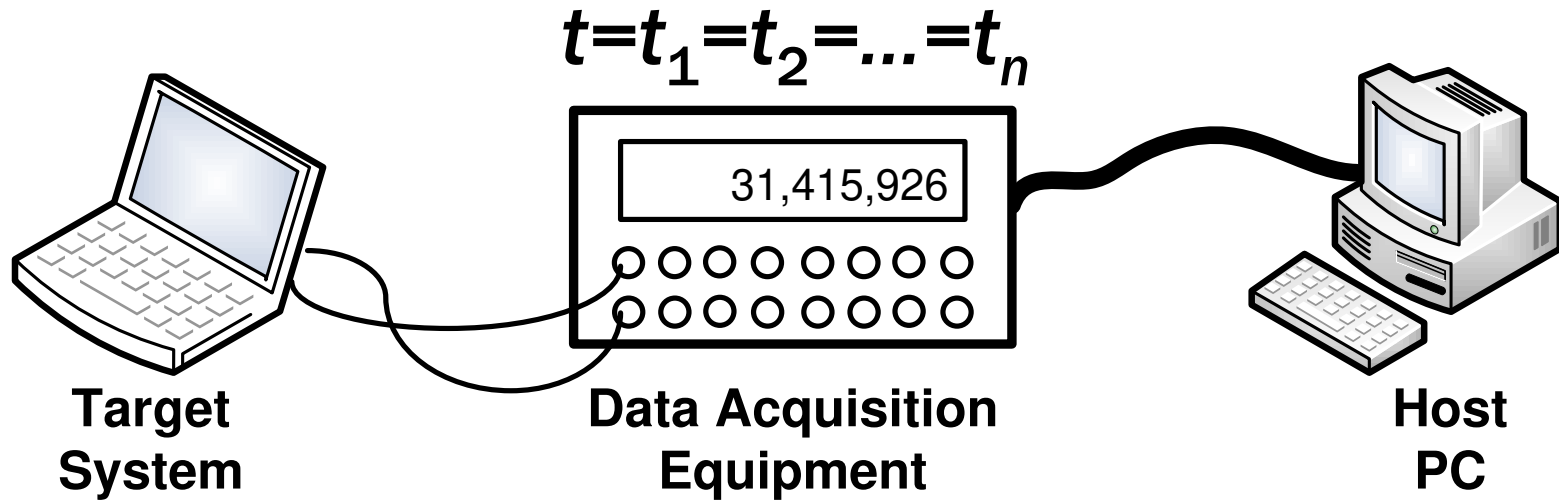


**Linear Model:**

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$

$$\hat{\beta} = \operatorname{argmin}_{\beta} (\|Y(t) - [\mathbf{1} \ X(t)]\beta\|_2)$$

# Model Construction



**Linear Model:**

$$\hat{y}(t) = \hat{\beta}_0 + \hat{\beta}_1 x_1(t) + \dots + \hat{\beta}_p x_p(t)$$

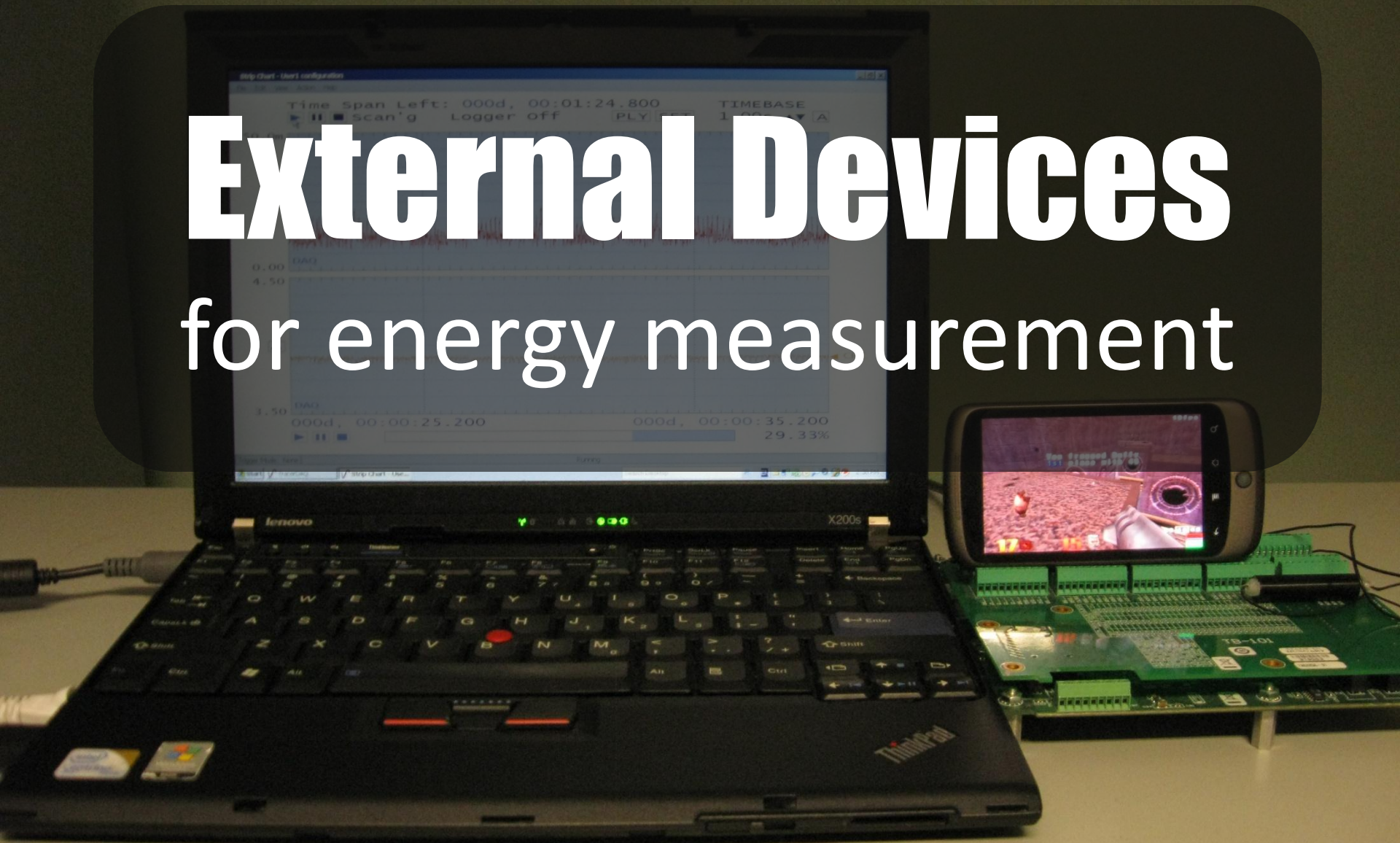
$$err(t_i) = \frac{\hat{y}(t_i) - y(t_i)}{y(t_i)}$$

Mean Absolute  
Root-Mean-Square



**What are the  
limitations?**

# External Devices for energy measurement

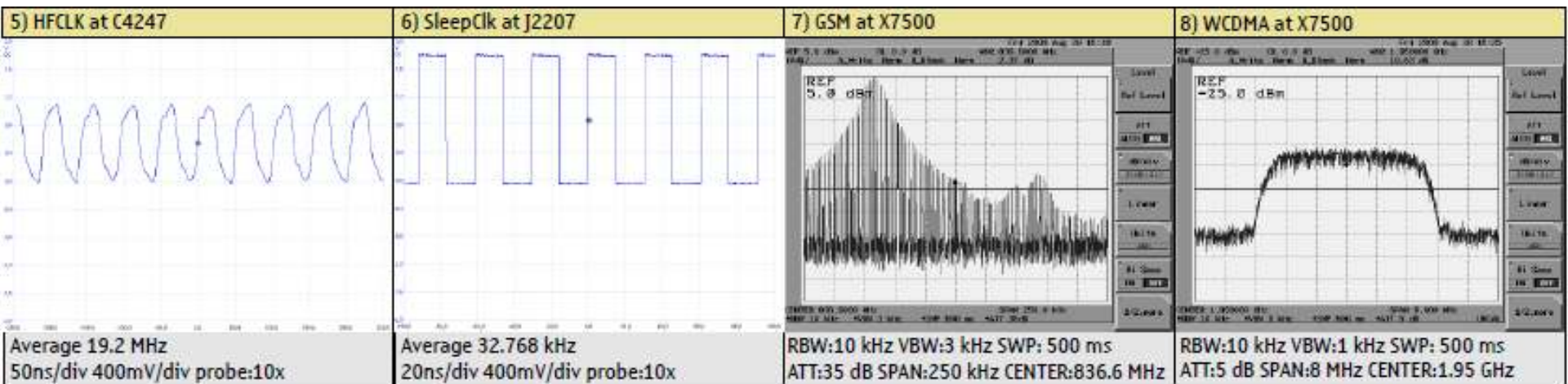




# Deep Knowledge for predictor collection



[www.nokia.com](http://www.nokia.com)







# **Exclusive Model** for a specific platform

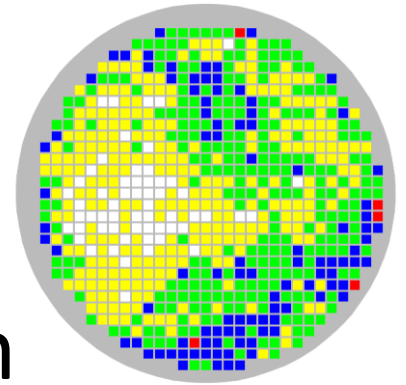




**Fixed Model** for all  
instances of the same platform



Dependencies of  
system energy models on  
**Hardware & Usage**  
suggest “personalized” models  
be constructed for a mobile system





# **Self-Constructive**

## System Energy Modeling

**External Devices**

**Deep Knowledge**

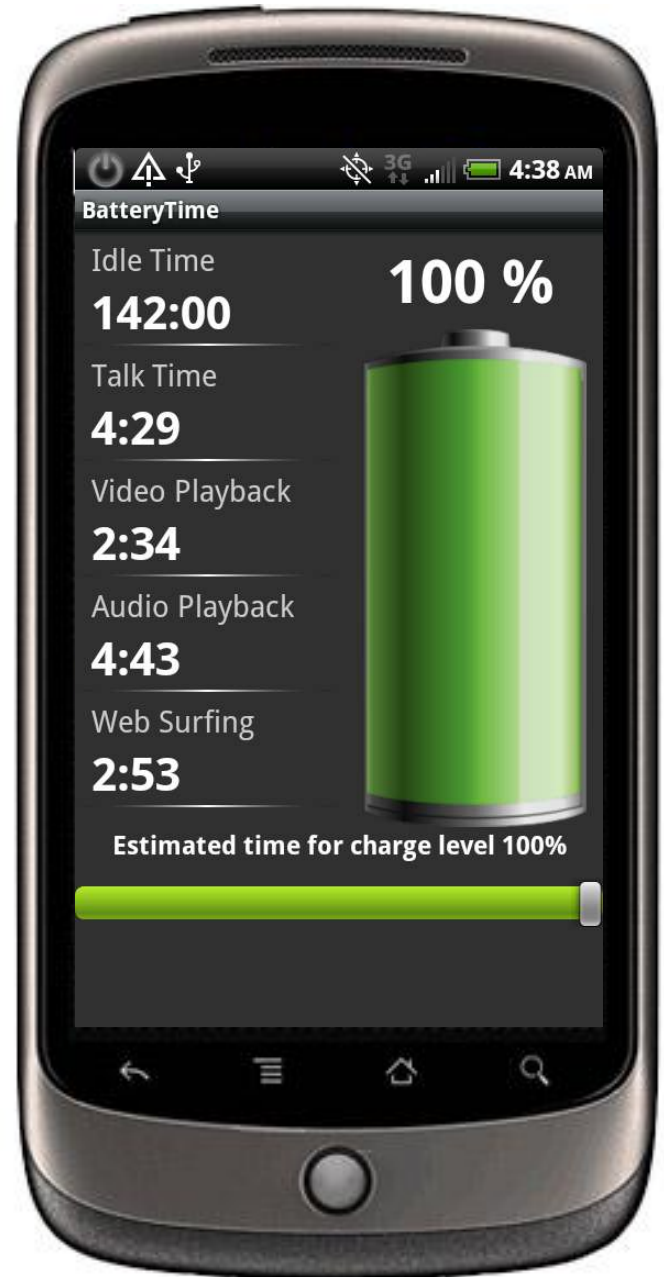
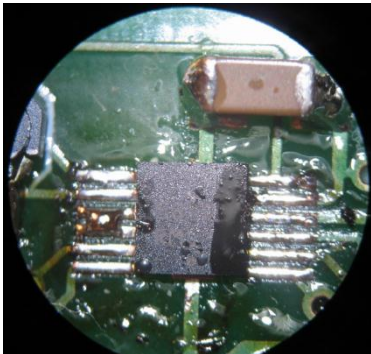
**Exclusive Model**

**Fixed Model**



**Battery Interface**  
**+**  
**Statistical Learning**  
**↓**  
**Personalized**  
**Model**

# Battery Interface

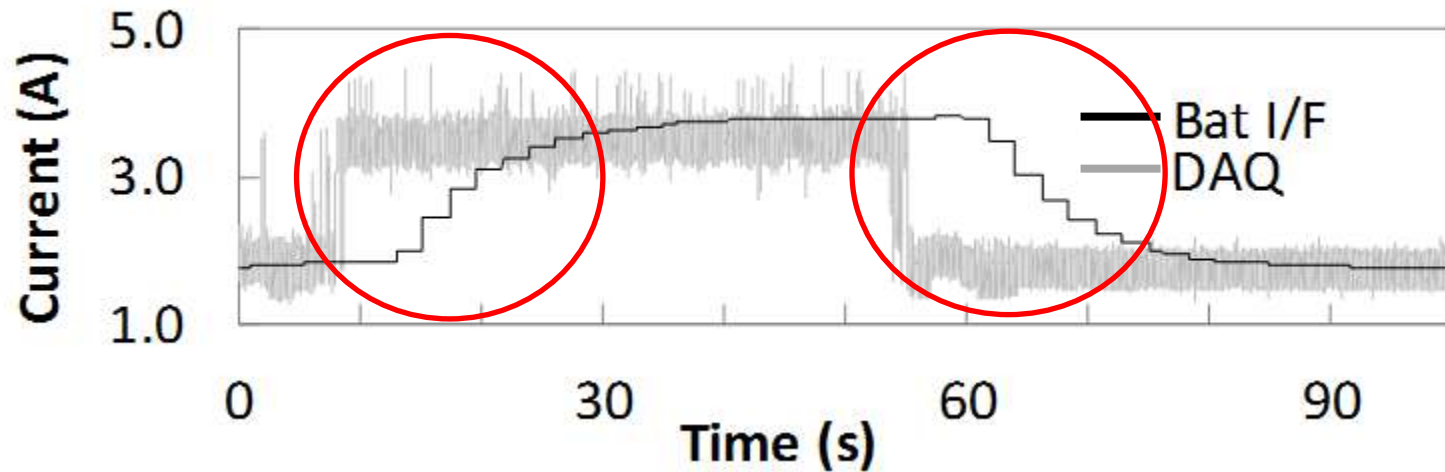


# State-of-the-art battery Interfaces are **Low-rate/Inaccurate**

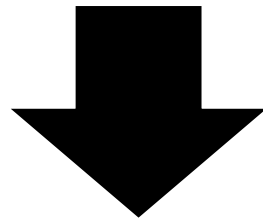
	N85	T61	N900
Max Rate	4Hz	0.5Hz	0.1Hz
Accuracy	67%	82%	58%

Accuracy = 100% – Root\_Mean\_Square(Instant\_Relative\_Error)

Errors in battery interface readings  
are **Non-Gaussian**



Low-Rate/Inaccurate  
Battery Interface



**Statistical  
Learning**

High-Rate/Accurate  
System Energy Model

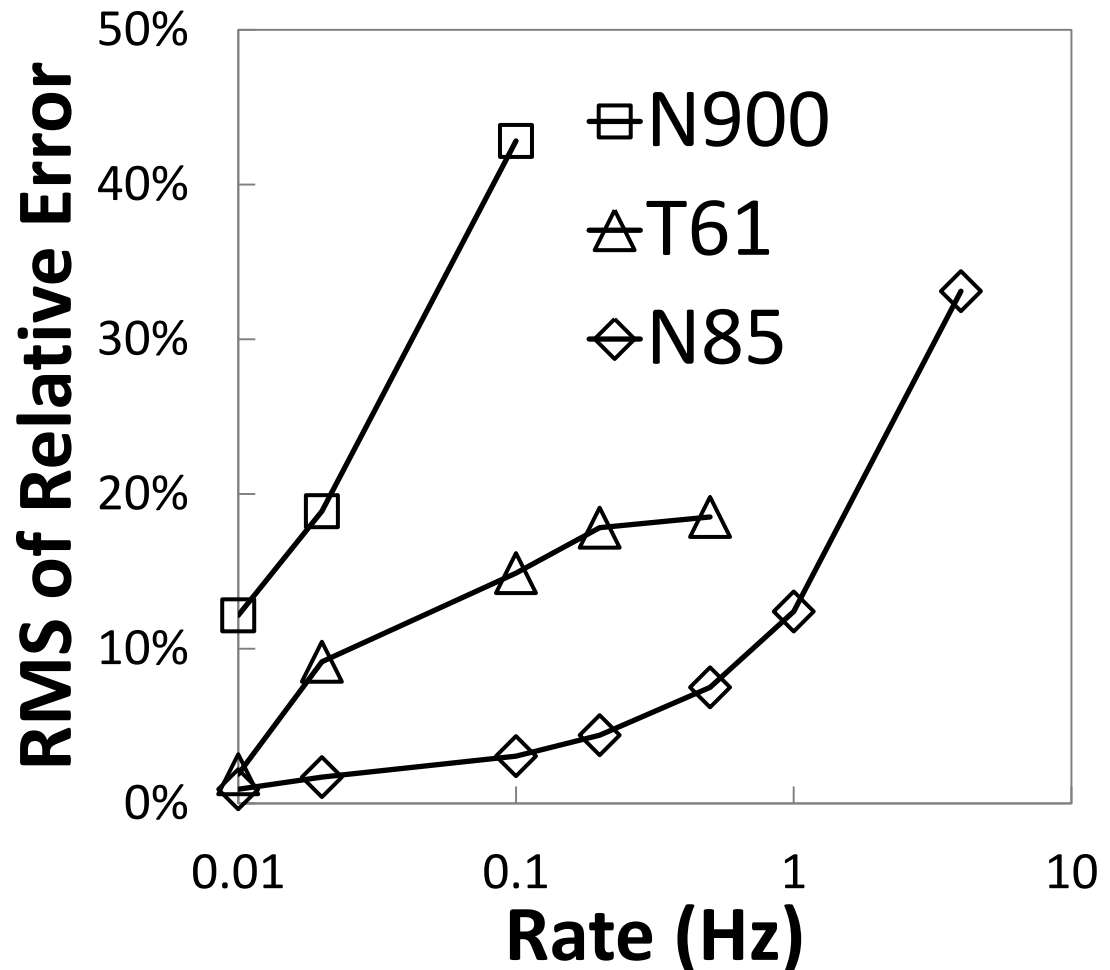
# **Averaged** battery interface readings

have

**Higher  
Accuracy**

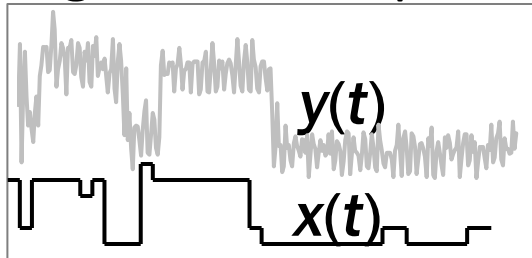
but

**Even Lower  
Rate**



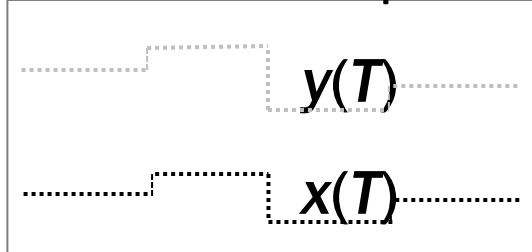
# Linear models are **Independent on Time**

High-rate data points



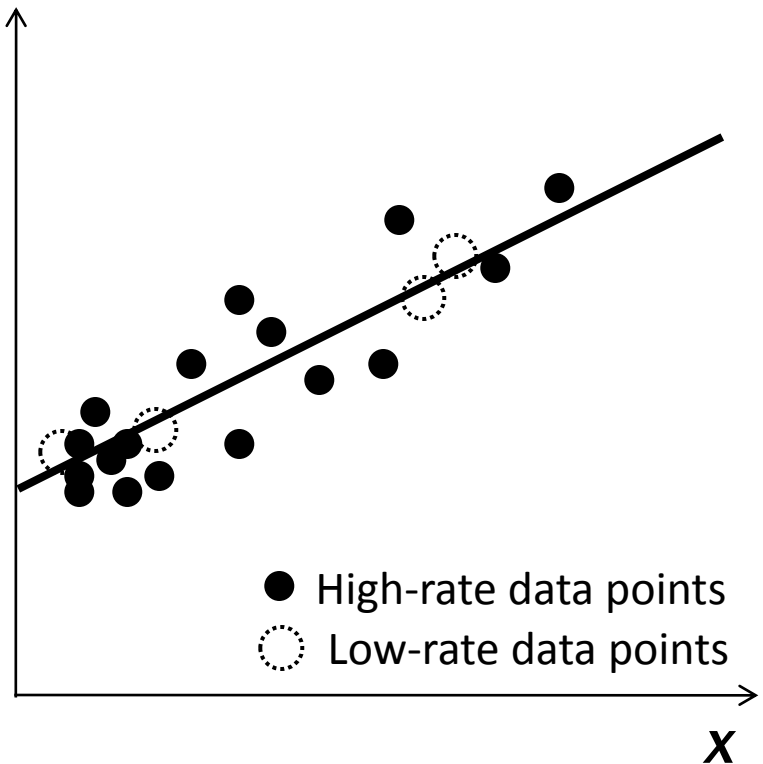
Time

Low-rate data points

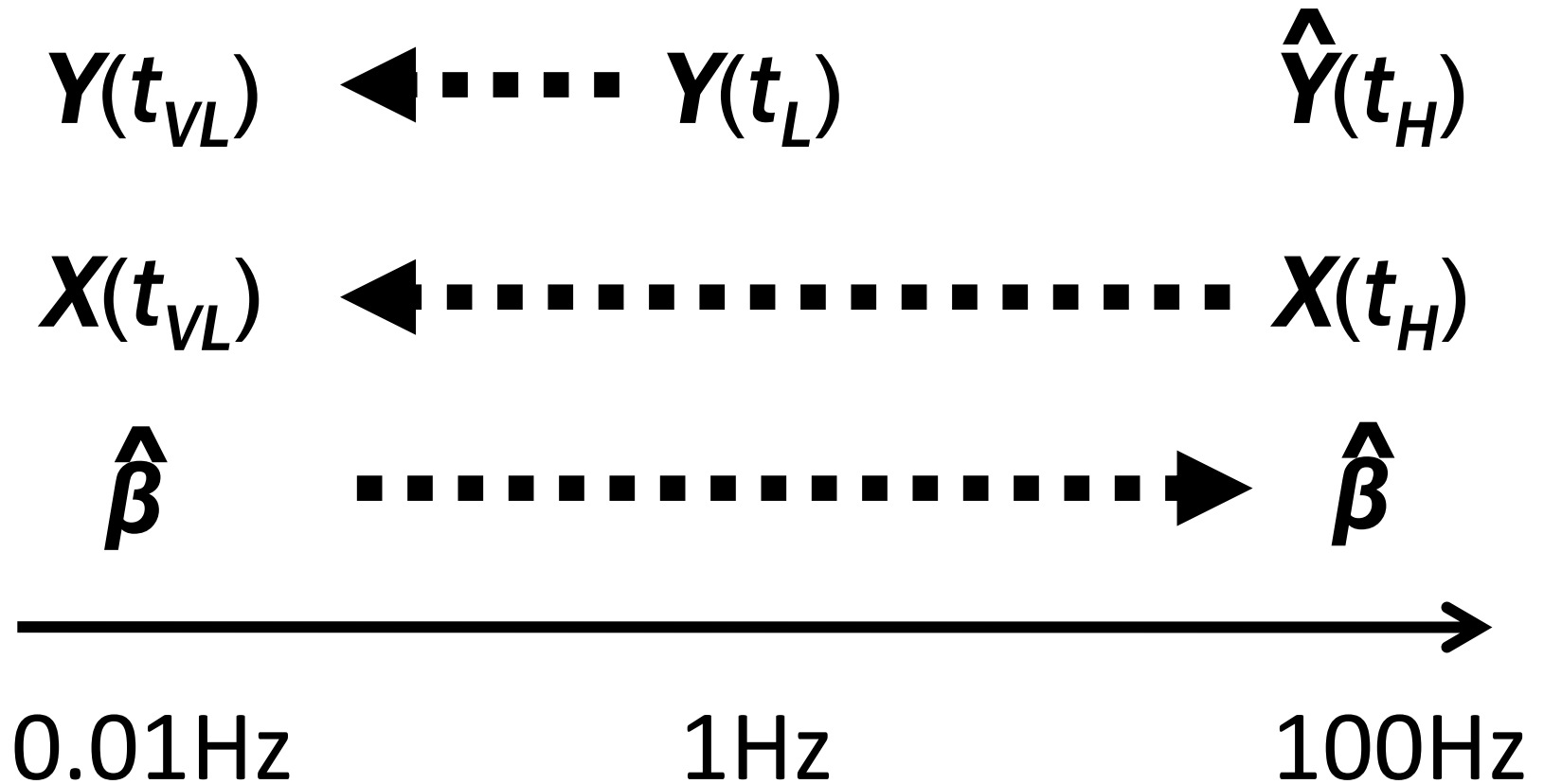


Time

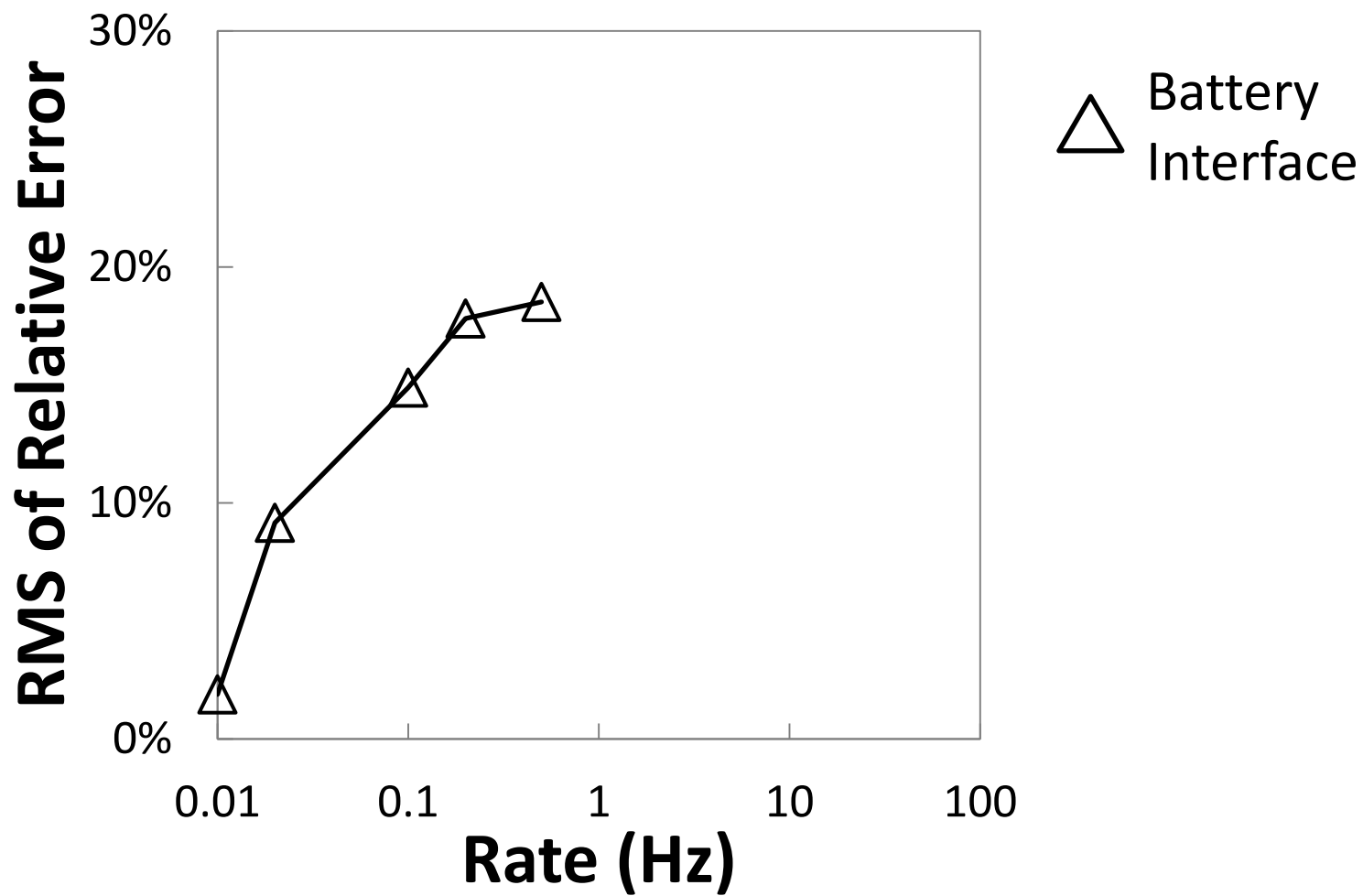
$y$



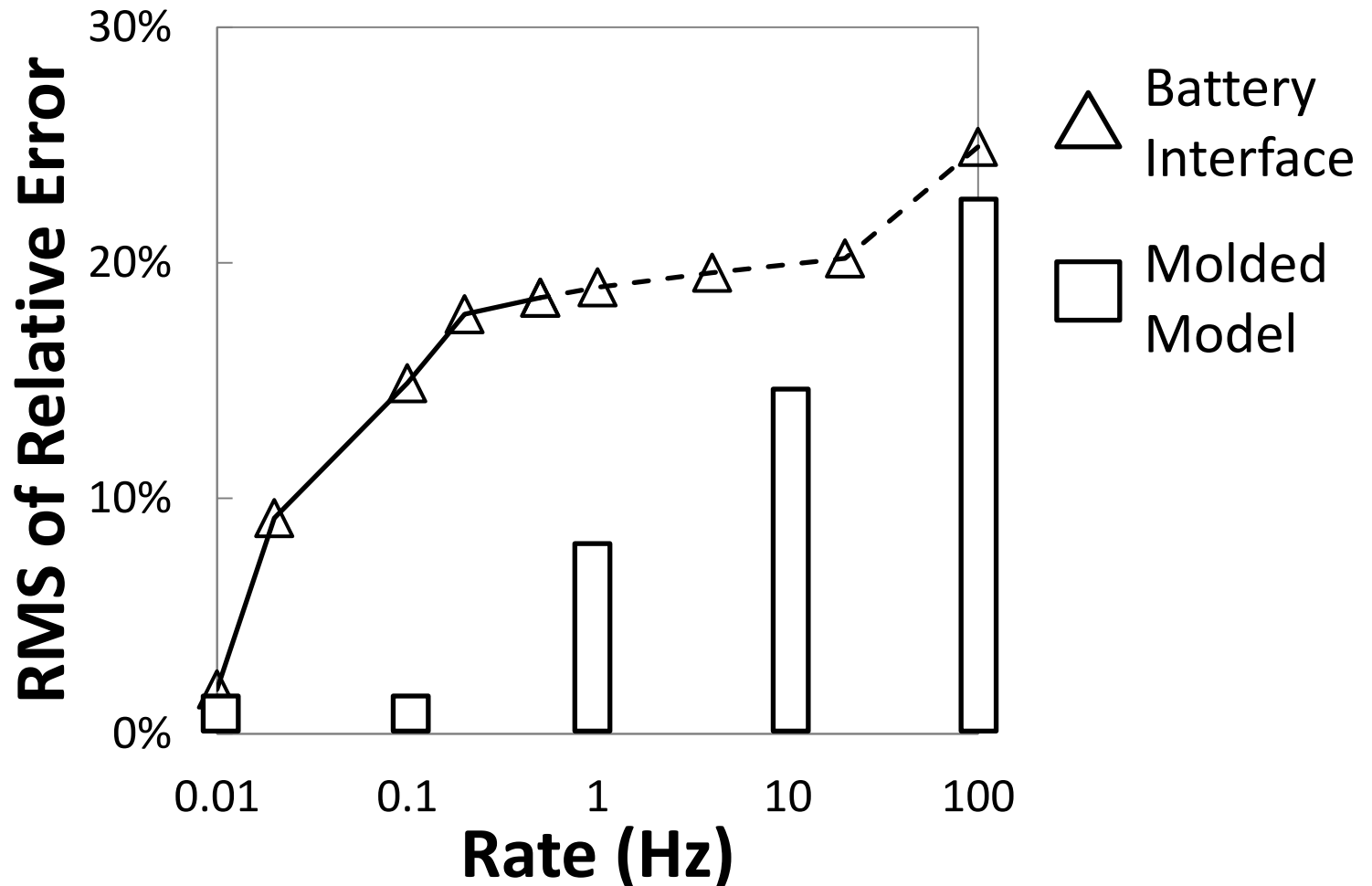
# 1. Model Molding





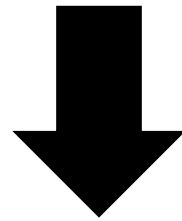


# Model Molding improves rate



## 2. Predictor Transformation

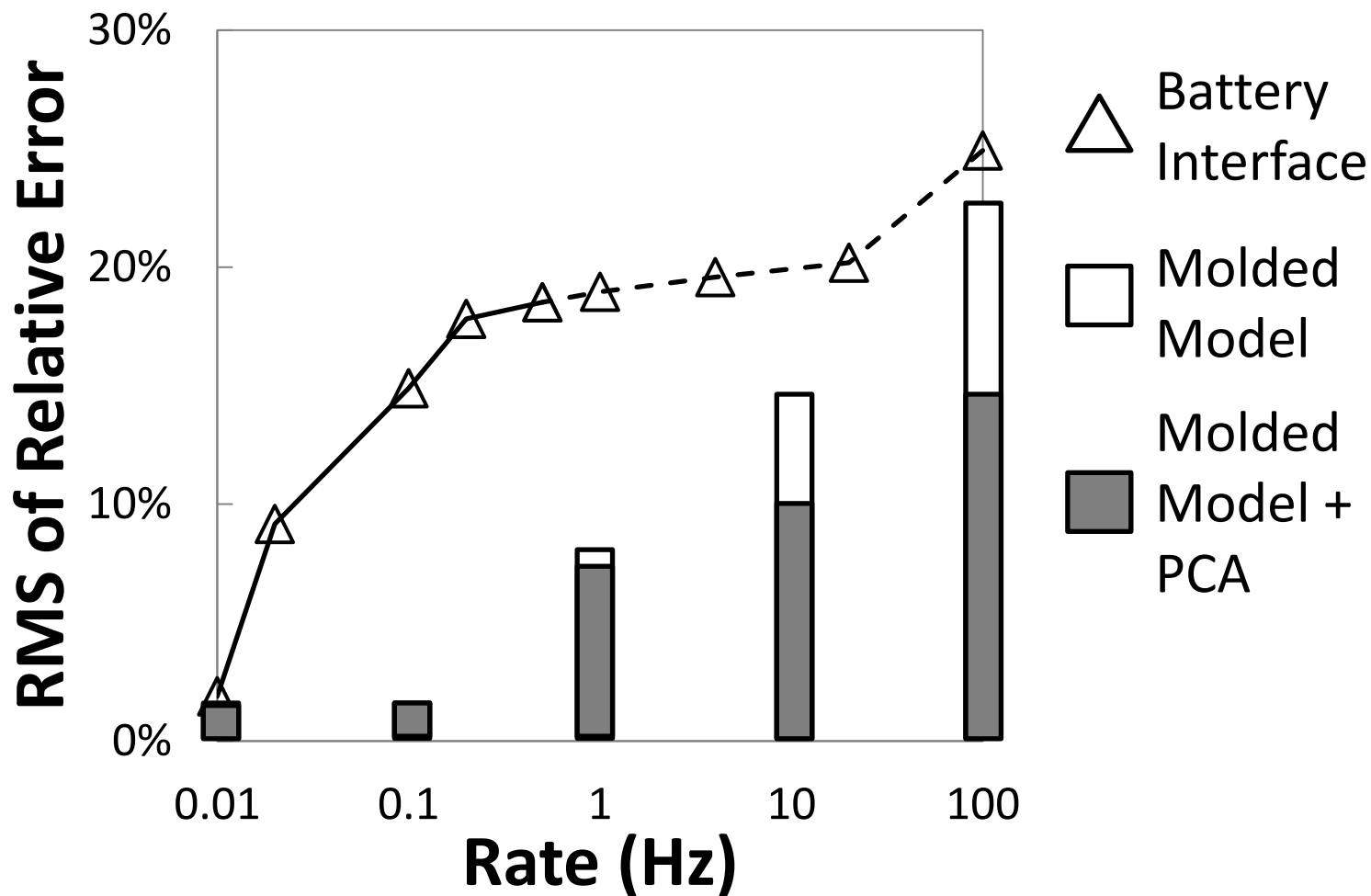
$$x_1(t), x_2(t), \dots, x_p(t)$$



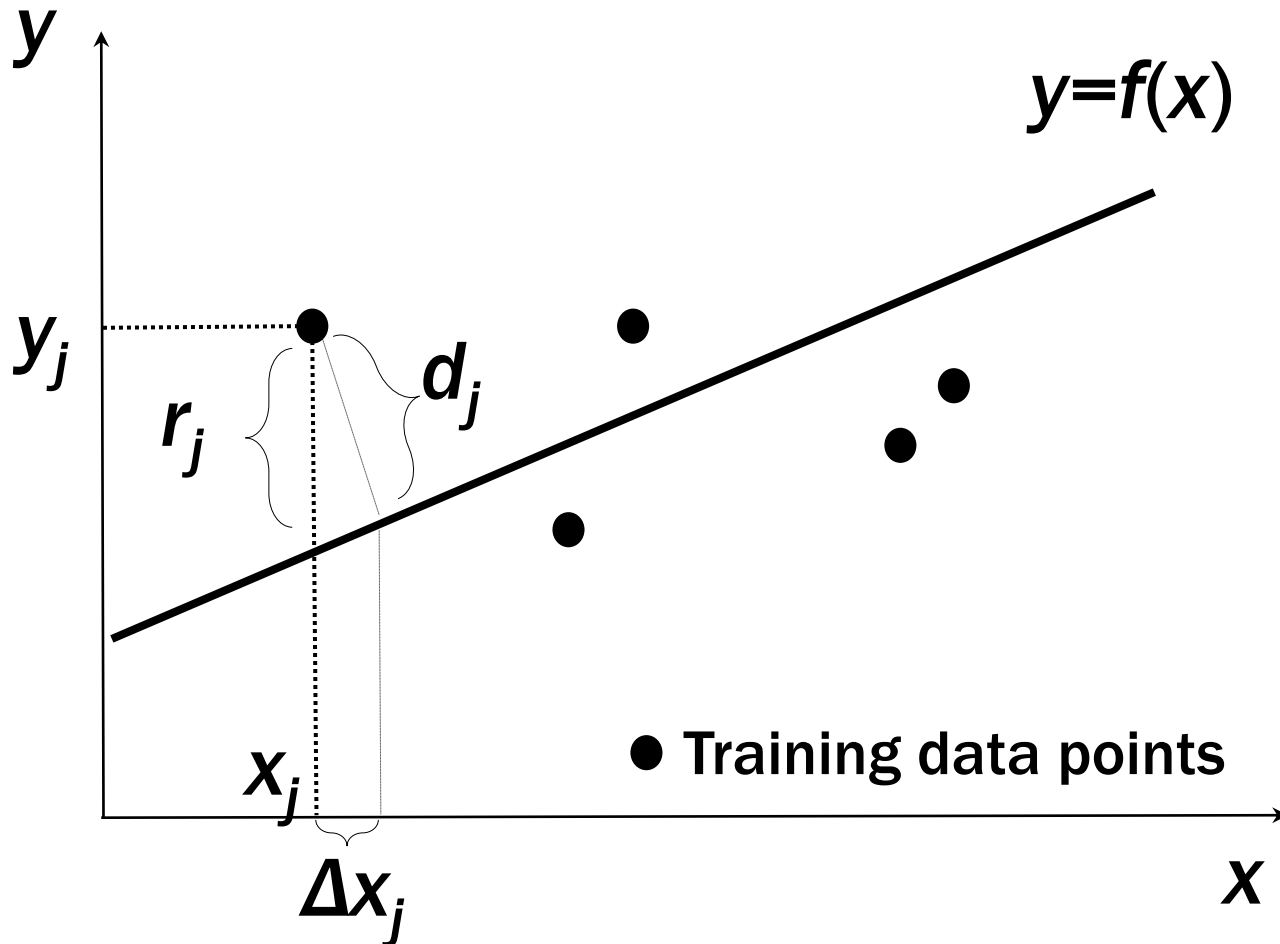
Principle  
Component  
Analysis

$$z_1(t), z_2(t), \dots, z_L(t) \quad L \leq p$$

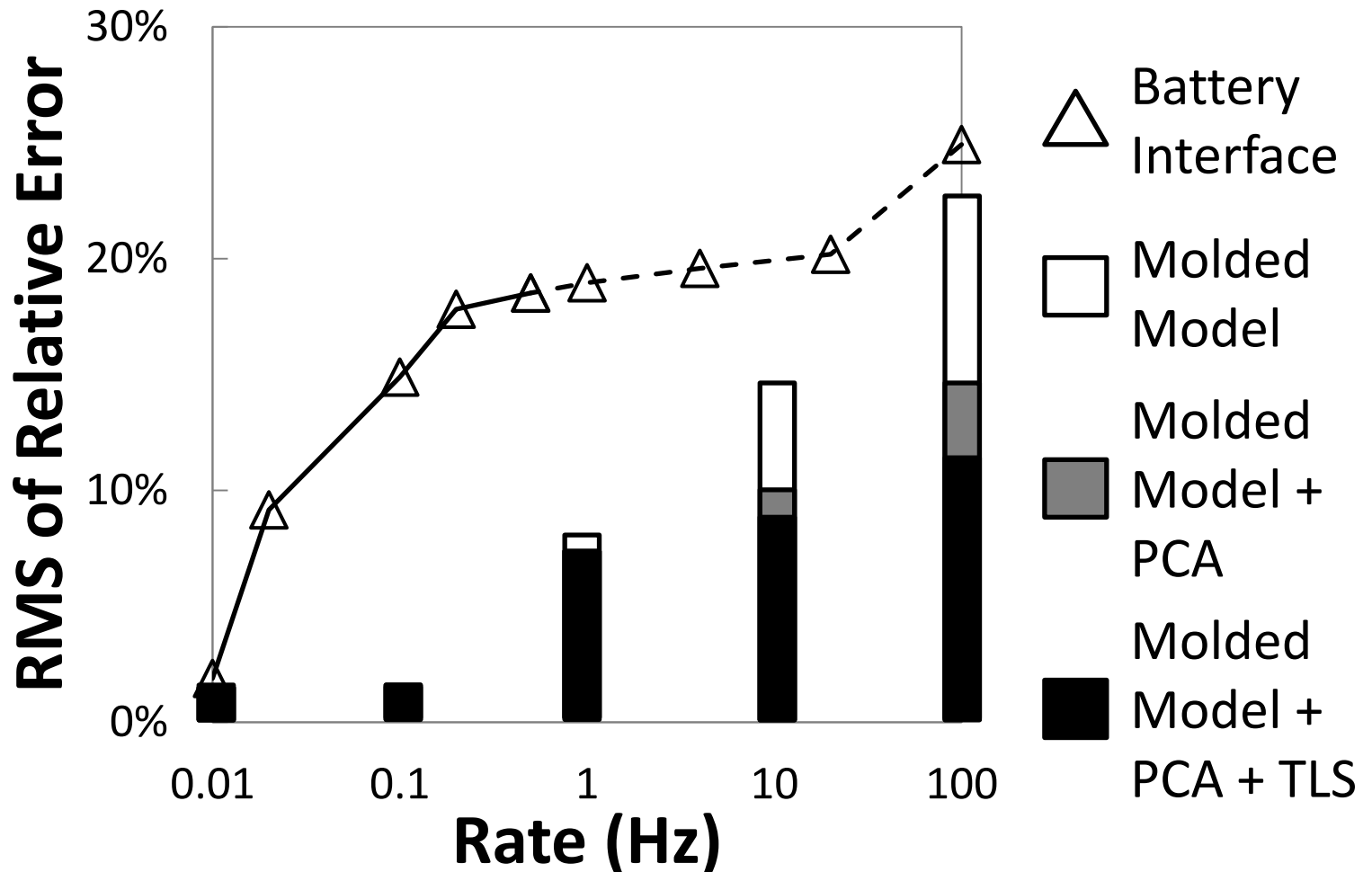
# PCA improves accuracy

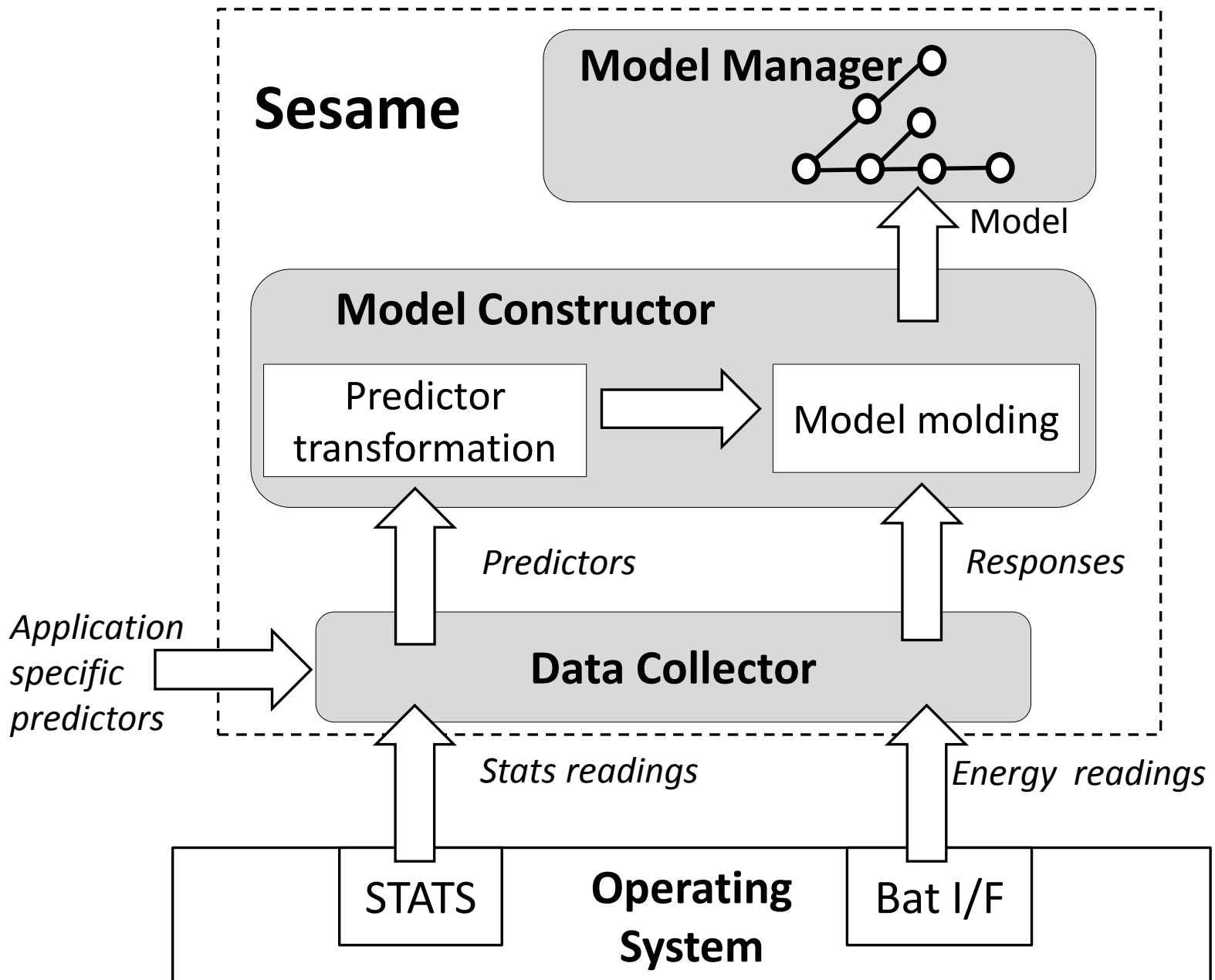


# 3. Total-Least-Square



# TLS improves accuracy at high rate





# Implementation



N900



T61



Sesame is able to generate energy  
models with a rate up to **100Hz**

	<b>T61</b>	<b>N900</b>
<b>1Hz</b>	95%	86%
<b>100Hz</b>	88%	82%

Accuracy = 100% – Root\_Mean\_Square(Instant\_Relative\_Error)

# Field Study



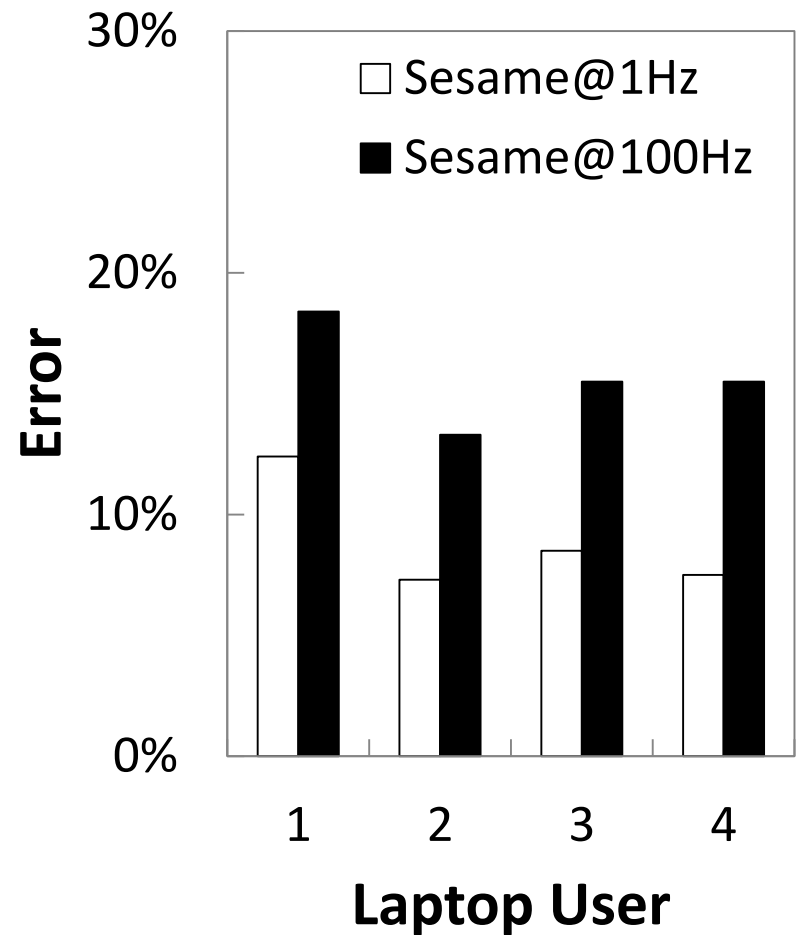
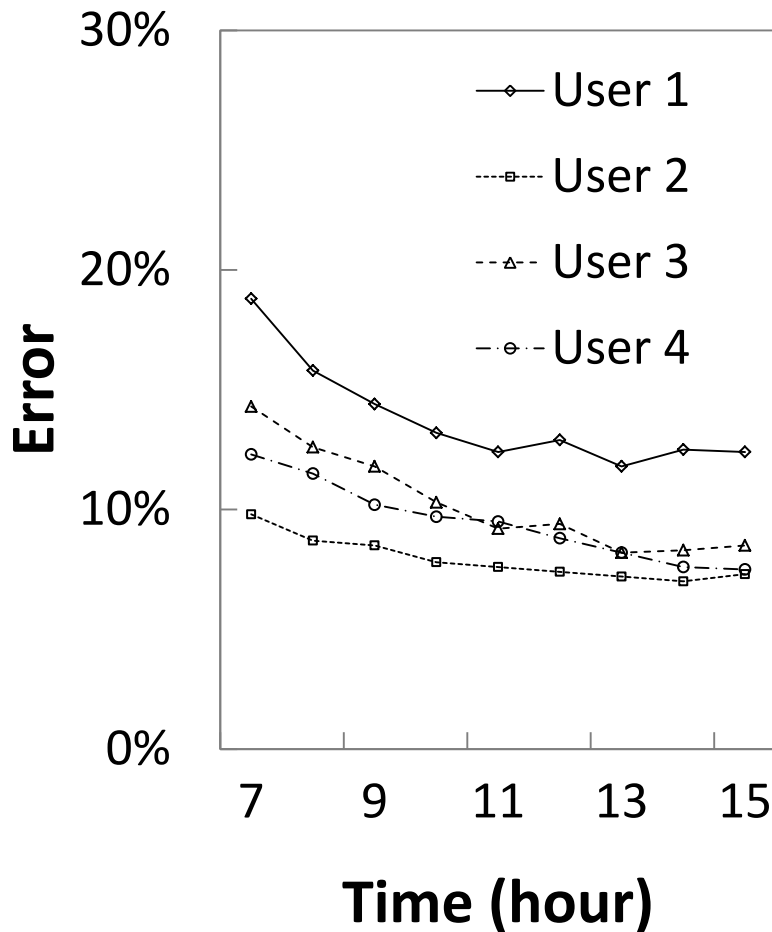
Day 1-5:  
Model Construction



Day 6:  
Model Evaluation



# Models were generated within **15** hours



Sesame is able to construct models of high accuracy because of

- 1. Sophisticated Statistical Methods**
- 2. Capability to Adapt Models**

Sesame is a high-rate/accurate  
**Virtual Power Meter**

and creates new opportunities in

# **Energy Optimization & Management**

# Software Optimization

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$



“Knob”

provided by  
target software

# Energy Accounting

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$

*n* Processes



# Energy Accounting

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$

$$x_1(t) = x_{1,1}(t) + \dots + x_{1,n}(t)$$

$$\vdots$$
$$\vdots$$
$$\vdots$$

$$x_p(t) = x_{p,1}(t) + \dots + x_{p,n}(t)$$

# Energy Contribution by Process j

$$y_j(t) = \beta_1 x_{1,j}(t) + \dots + \beta_p x_{p,j}(t)$$

Sesame can be also used for  
**Servers and Workstations**

# Conclusions

- Self-Modeling is necessary to adapt to the changes in hardware and usage
- Statistical methods help to construct high-rate /accurate models from low-rate/inaccurate battery interfaces
- Sesame creates new opportunities in system energy optimization and management