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Sensorless Battery Internal Temperature Estimation Using a Kalman Filter With Impedance Measurement — Source link

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Sensorless Battery Internal Temperature Estimation using a Kalman Filter with Impedance Measurement

Robert R. Richardson and David A. Howey, Member, IEEE

Abstract—This study presents a method of estimating battery cell core and surface temperature using a thermal model coupled with electrical impedance measurement, rather than using direct surface temperature measurements. This is advantageous over previous methods of estimating temperature from impedance, which only estimate the average internal temperature. The performance of the method is demonstrated experimentally on a 2.3 Ah lithium-ion iron phosphate cell fitted with surface and core thermocouples for validation. An extended Kalman filter, consisting of a reduced order thermal model coupled with current, voltage and impedance measurements, is shown to accurately predict core and surface temperatures for a current excitation profile based on a vehicle drive cycle. A dual extended Kalman filter (DEKF) based on the same thermal model and impedance measurement input is capable of estimating the convection coefficient at the cell surface when the latter is unknown. The performance of the DEKF using impedance as the measurement input is comparable to an equivalent dual Kalman filter using a conventional surface temperature sensor as measurement input.

Index Terms—Lithium-ion battery, impedance, temperature, thermal model, Kalman filter, state estimation.

I. INTRODUCTION

THE sustainable development of transportation relies on the widespread adoption of electric vehicle (EV) and hybrid electric vehicle (HEV) technology. Lithium-ion batteries are suitable for these applications due to their high specific energy and power density. However, their widespread deployment requires reliable on-board battery management systems to ensure safe and optimal performance. In particular, accurate on-board estimation of battery temperature is of critical importance. Under typical operating conditions, such as a standard vehicle drive cycle, cells may experience temperature differences between surface and core of 20 °C or more [1]. High battery temperatures could trigger thermal runaway resulting in fires, venting and electrolyte leakage. While such incidents are rare [2], consequences include costly recalls and potential endangerment of human life.

The conventional approach to temperature estimation is to use numerical electrical-thermal models [3], [4], [5], [6], [7]. Such models rely on knowledge of the cell thermal properties, heat generation rates and thermal boundary conditions. Models without online sensor feedback are unlikely to work in practice since their temperature predictions may drift from the true values due to small uncertainties in measurements and

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parameters. However, using additional online measurements typically of the cell surface temperature and of the temperature of the cooling fluid - coupled with state estimation techniques such as Kalman filtering, the cell internal temperature may be estimated with high accuracy [4], [5], [6], [7]. However, large battery packs may contain several thousand cells [8], and so the requirement for surface temperature sensors on every cell represents substantial instrumentation cost.

An alternative approach to temperature estimation uses electrochemical impedance spectroscopy (EIS) measurements at one or several frequencies to directly infer the internal cell temperature, without using a thermal model [9], [10], [11], [12], [13]. This exploits the fact that impedance is related to a type of volume averaged cell temperature, which we define later in this article. For brevity, we refer to the use of impedance to infer such a volume-averaged temperature as 'Impedance-Temperature Detection' (ITD). This has promise for practical application, since methods capable of measuring EIS spectra using existing power electronics in a vehicle or other application have been developed [14], [15], [16]. However, just like conventional surface temperature sensors, ITD alone does not provide a unique solution for the temperature distribution within the cell. Our previous work showed that by combining ITD with surface temperature measurements the internal temperature distribution could be estimated [17]. However, this approach still requires each cell to be fitted with a surface temperature sensor. Moreover, whilst the ITD technique was validated under constant coolant temperature conditions, the accuracy of the technique may be reduced if the temperature of the cooling medium is varied rapidly, as discussed in Section IV. Thus, if the cell electrical/thermal properties are known or can be identified, this information can be exploited to improve the estimate of the thermal state of the cell or reduce the number of sensors required.

In this study we demonstrate that ITD can be used as the measurement input to a thermal model in order to estimate the cell temperature distribution. First, an extended Kalman filter (EKF) is used to estimate the cell temperature distribution when all the relevant thermal parameters, including the convection coefficient, are known. The thermal model consists of a polynomial approximation (PA) to the 1D cylindrical heat equation. The measurement input consists of the cell current and voltage, along with periodic measurements of the real part of the impedance at a single frequency. Second, a dual extended Kalman filter (DEKF) is used to identify the convection coefficient online when the latter is not known. The predicted against core and surface thermocouple measurements, with

agreement to within 0.47 °C (2.4% of the core temperature increase). The performance of the combined thermal model plus ITD estimator is comparable to the performance of the same thermal model coupled with conventional surface temperature measurements. Table I shows the present study in the context of existing temperature estimation techniques, which highlights that this is the first study to use impedance as the measurement input to a thermal model.

$ \begin{array}{c c} T_{surf} \\ \hline $	f ITD
✓ ✓	
✓	
	√
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✓	√
	√

COMPARISON OF ONLINE TEMPERATURE ESTIMATION TECHNIQUES.

II. MEASUREMENT PRINCIPLE

The electrochemical impedance, $Z(\omega) = Z'(\omega) + jZ''(\omega)$, of lithium ion cells is a function of temperature, state of charge (SOC) and state of health (SOH). Within an appropriate frequency range, however, the dependence on SOC and SOH is negligible and the impedance can thus be used to infer information about the cell temperature [12]. Previous ITD studies have used as a temperature-dependent parameter the real part of the impedance at a specific frequency [10], the phase shift at a specific frequency [12], [9], and the intercept frequency [11]. To demonstrate our technique we use the real part of the impedance at f = 215 Hz. Our previous work showed that the real part of the cell admittance (the inverse of the cell impedance) at 215 Hz can be related to the temperature distribution using a second order polynomial fit. For an annular cell with inner radius r_i and outer radius r_o the real part of the admittance is given by [17]:

$$Y' = \frac{2}{r_o^2} \int_{r_i}^{r_o} r\left(a_1 + a_2 T(r) + a_3 T^2(r)\right) dr$$
(1)

where a_1 , a_2 and a_3 are the 1st, 2nd and 3rd coefficients of the polynomial relating impedance to uniform cell temperature $(Y' = a_1 + a_2 T_{uniform} + a_3 T_{uniform}^2)$, provided that the admittivity varies in the radial direction only. This assumption is valid if the heat transfer from the top and bottom ends of the cell is negligible, which is approximately true for cylindrical cells connected in series with identical cells on either end [18], a configuration which may apply to the majority of cells in a large battery pack. However, the application of this approach to cooling configurations involving substantial end cooling would require a more involved expression for the admittance than eq. 1, as well as an appropriate modification to the 1D thermal model described in the following section. Moreover, although the method is applied to a cylindrical cell, the proposed approach could be applied to other geometries in a similar fashion. The polynomial fit (Fig. 1) was obtained

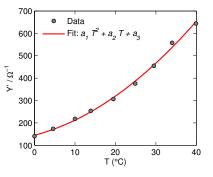


Figure 1. Polynomial fit to experimental data of admittance at f = 215 Hz vs. uniform cell temperature.

by offline impedance measurements on the cell at multiple uniform temperatures [17].

ITD can be viewed as identifying an EIS-based volume average temperature \overline{T}_{EIS} , which is defined as the uniform cell temperature that would give rise to the measured EIS¹. Thus the impedance input is similar to a conventional temperature measurement since it is a scalar function of the internal temperature distribution but does not uniquely identify the temperature distribution. Either measurement can therefore be used in conjunction with a thermal model, as shown in Fig. 2, to estimate core temperature.

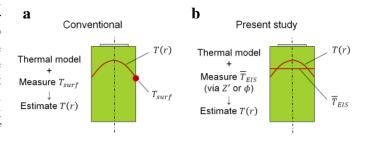


Figure 2. Schematic of (a) the conventional approach to temperature estimation and (b) the proposed approach based on ITD.

III. THERMAL-IMPEDANCE MODEL

A. Thermal Model

The cell thermal model consists of the heat equation for 1D unsteady heat conduction in a cylinder, given by the following Boundary Value Problem (BVP) [2]:

$$\rho c_p \frac{\partial T(r,t)}{\partial t} = k_t \frac{\partial^2 T(r,t)}{\partial r^2} + \frac{k_t}{r} \frac{\partial T(r,t)}{\partial r} + \frac{Q(t)}{V_b}$$
(2a)

where ρ , c_p and k_t are the density, specific heat capacity and thermal conductivity respectively, V_b is the cell volume, and Qis the heat generation rate. The boundary conditions are given

¹Note that, since the impedance temperature relationship is non-linear (as demonstrated in [19]), the EIS-based volume average temperature, \overline{T}_{EIS} , is not necessarily equal to the volume average temperature, \overline{T} . Although, it should also be noted that the two are typically close in value, particularly if the temperature variation within the cell is small.

by:

$$\left. \frac{\partial T(r,t)}{\partial r} \right|_{r=r_o} = -\frac{h}{k_t} (T(r_o,t) - T_\infty(t)) \qquad (2b)$$

$$\left. \frac{\partial T(r,t)}{\partial r} \right|_{r=0} = 0 \tag{2c}$$

where T_{∞} is the temperature of the heat transfer fluid, and h is the convection coefficient. A commonly employed expression for the heat source in a lithium ion battery is

$$Q = I(V - U_{OCV}) + IT \frac{\partial U_{OCV}}{\partial T}$$
(3)

which is a simplified version of the expression first proposed by Bernardi et al [20]. The first term is the heat generation due to ohmic losses in the cell, charge transfer overpotential and mass transfer limitations. The current I and voltage V for this expression are measured online. The open circuit voltage U_{OCV} is a function of SOC but is approximated here as a constant value measured at 50 % SOC, since the HEV drive cycles employed in this study operate the cell within a small range of SOC (47 - 63%) and therefore OCV variation. If necessary, an estimator of U_{OCV} could also be constructed (for example using a dynamic electrical model [21]), but for clarity and brevity we neglect this here. The second term, the entropic heat, is neglected in this study because (i) the term $\partial U_{avg}/\partial T$ is small $(0 < \partial U_{avg}/\partial T < 0.1 \text{ mVK}^{-1})$ within the operated range of SOC [3], and (ii) the net reversible heat would be close to zero when the cell is operating in HEV mode.

B. Polynomial Approximation

A polynomial approximation (PA) is used to approximate the solution of eq. 2a. The approximation was first introduced in [6] and is described in detail in that article, although the essential elements are repeated here for completeness.

The model assumes a temperature distribution of the form

$$T(r,t) = a(t) + b(t) \left(\frac{r}{r_o}\right)^2 + d(t) \left(\frac{r}{r_o}\right)^4 \tag{4}$$

The two states of the model are the volume averaged temperature \overline{T} and temperature gradient $\overline{\gamma}$:

$$\overline{T} = \frac{2}{r_o^2} \int_0^{r_o} rT dr, \qquad \overline{\gamma} = \frac{2}{r_o^2} \int_0^{r_o} r\left(\frac{\partial T}{\partial r}\right) dr \quad (5)$$

The temperature distribution is expressed as a function of \overline{T} , $\overline{\gamma}$, and the cell surface temperature, T_{surf} :

$$T(r,t) = 4T_{surf} - 3\overline{T} - \frac{15r_o}{8}\overline{\gamma} + \left[-18T_{surf} + 18\overline{T} + \frac{15r_o}{2}\overline{\gamma}\right] \left(\frac{r}{r_o}\right)^2 + \left[15T_{surf} - 15\overline{T} - \frac{45r_o}{8}\overline{\gamma}\right] \left(\frac{r}{r_o}\right)^4 \quad (6)$$

Using 2b, the surface temperature can be expressed as

$$T_{surf} = \frac{24k_t}{24k_t + r_oh}\overline{T} + \frac{15k_tr_o}{48k_t + 2r_oh}\overline{\gamma} + \frac{r_oh}{24k_t + r_oh}T_{\infty}$$
(7)

By obtaining the volume-average of eq. 2a and of its partial derivative with respect to r, a two-state thermal model consisting of two ODEs is obtained:

$$\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{u}$$

$$\mathbf{y} = \mathbf{C}\mathbf{x} + \mathbf{D}\mathbf{u}$$
 (8)

where $\mathbf{x} = [\overline{T} \ \overline{\gamma}]^T$, $\mathbf{u} = [Q \ T_{\infty}]^T$ and $\mathbf{y} = [T_{core} \ T_{surf}]^T$ are state, inputs and outputs respectively. The system matrices **A**, **B**, **C**, and **D** are defined as:

$$\mathbf{A} = \begin{bmatrix} \frac{-48\alpha h}{r_o(24k_t+r_oh)} & \frac{-15\alpha h}{24k_t+r_oh} \\ \frac{-320\alpha h}{r_o^2(24k_t+r_oh)} & \frac{-120\alpha(4k_t+r_oh)}{r_o^2(24k_t+r_oh)} \end{bmatrix}$$
$$\mathbf{B} = \begin{bmatrix} \frac{\alpha}{k_t V_b} & \frac{48\alpha h}{r_o(24k_t+r_oh)} \\ 0 & \frac{320\alpha h}{r_o^2(24k_t+r_oh)} \end{bmatrix}$$
$$\mathbf{C} = \begin{bmatrix} \frac{24k_t-3r_oh}{24k_t+r_oh} & -\frac{120r_ok_t+15r_o^2h}{8(24k_t+r_oh)} \\ \frac{24k_t}{24k_t+r_oh} & \frac{15r_ok_t}{48k_t+2r_oh} \end{bmatrix}$$
$$\mathbf{D} = \begin{bmatrix} 0 & \frac{4r_oh}{24k_t+r_oh} \\ 0 & \frac{r_oh}{24k_t+r_oh} \end{bmatrix}$$

where $\alpha = k_t / \rho c_p$ is the cell thermal diffusivity.

C. Impedance Measurement

Eq. 1 applies to an annulus with inner radius r_i and outer radius r_o . If the inner radius is sufficiently small, the cell may be treated as a solid cylinder, and eq. 1 becomes

$$Y' = \frac{2}{r_o^2} \int_0^{r_0} r\left(a_1 + a_2 T(r) + a_3 T^2(r)\right) dr \qquad (10)$$

Substituting eq. 6 in eq. 10, the real admittance can be expressed as a function of of T_{surf} , \overline{T} , and $\overline{\gamma}$

$$Y' = a_1 + a_2\overline{T} + 3a_3\overline{T}^2 + 2a_3T_{surf}^2 - 4a_3\overline{T}T_{surf} + \frac{15a_3r_o\overline{\gamma}^2}{32} + \frac{15a_3r_o\overline{T}\overline{\gamma}}{8} - \frac{15a_3r_oT_{surf}\overline{\gamma}}{8}$$
(11)

Noting from eq. 7 that T_{surf} is itself a function of \overline{T} , $\overline{\gamma}$ and T_{∞} and the cell parameters, admittance is ultimately a function of \overline{T} and $\overline{\gamma}$, along with the known thermal parameters and environmental temperature. In other words, for known values of r_o , k_t , c_p , ρ , and h, the impedance is a function of the cell state and T_{∞} , thus:

$$Z' = f(\overline{T}, \overline{\gamma}, T_{\infty}) \tag{12}$$

IV. FREQUENCY DOMAIN ANALYSIS

In this section we analyze the error associated with the polynomial approximation, by comparing the frequency response of the PA model to the frequency response of a full analytical solution of eq. (2a). We also examine the approximation employed in [17], which used a combination of impedance and surface temperature measurements but no thermal model. To achieve a unique solution in that case, it was necessary to impose the assumption of a quadratic solution to the temperature distribution, and so we refer to this here as the 'quadratic assumption' (QA) solution. As in [6], the frequency response function of the PA thermal system, H(s), is calculated by

$$\mathbf{H}(s) = \mathbf{D} + \mathbf{C}(s\mathbf{I} - \mathbf{A})^{-1}\mathbf{B}$$
(13)

where $s = j\omega$ and I is the identity matrix. The frequency response of the analytical model is derived in [22], and that of the QA solution is derived in Appendix A.

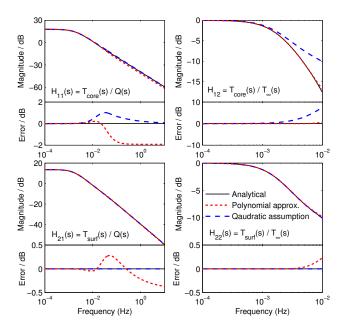


Figure 3. Comparison of frequency responses of (i) analytical solution to the 1D cylindrical heat transfer problem, (ii) the polynomial approximation used in the current study and (iii) the quadratic assumption used in [17].

Fig. 3 shows the impact of changes in heat generation on T_{core} and T_{surf} (H₁₁ and H₂₁ respectively), and the impact of changes in cooling fluid temperature T_{∞} on T_{core} and T_{surf} (\mathbf{H}_{12} and \mathbf{H}_{22} respectively), for each model along with the error relative to the analytical solution. The results in these plots were obtained using the thermal parameters of the 26650 cell used in the present study (Table II). The response of \mathbf{H}_{11} and \mathbf{H}_{21} for both the PA and QA models are in good agreement with the analytical solution (note that the error in the response of \mathbf{H}_{21} and \mathbf{H}_{22} for the QA model is 0 since it takes the measured surface temperature as one of its inputs). However, the responses for both cases to changes in T_{∞} are less satisfactory. In particular, the response \mathbf{H}_{12} for the QA model shows a rapid increase in error relative to the analytical solution at frequencies above $\sim 10^{-3}$ Hz. The PA performs well up to higher frequencies, although its error in \mathbf{H}_{21} and \mathbf{H}_{22} become unsatisfactory above $\sim 10^{-2}$ Hz. However, the frequency range at which the PA agrees with the analytical solution is broader than that of the QA model, and is considered satisfactory given the slow rate at which the cooling fluid temperature fluctuates in a typical battery thermal management system.

V. EXPERIMENTAL

Experiments were carried out with a 2.3 Ah cylindrical cell (A123 Model ANR26650 m1-A, length 65 mm, diameter 26

mm) with LiFePO₄ positive electrode and graphite negative electrode. The cell was fitted with two thermocouples, one on the surface and another inserted into the core via a hole which was drilled in the positive electrode end (Fig. 4). Cell cycling and impedance measurements were carried out using a Biologic HCP-1005 potentiostat/booster. The impedance was measured using Galvanostatic Impedance Spectroscopy with a 200 mA peak-to-peak perturbation current. The environmental temperature was controlled with a Votsch VT4002 thermal chamber. The chamber includes a fan which operates continuously at a fixed speed during operation.

In order to calibrate the impedance against temperature, EIS measurements were first conducted on the cell in thermal equilibrium at a range of temperatures. These experiments and the subsequent identification of the polynomial coefficients a_1 , a_2 , and a_3 are described in [17].

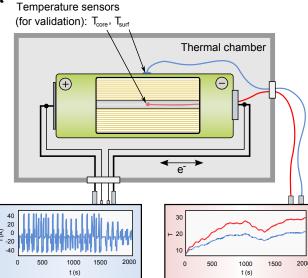
Dynamic experiments were then conducted using two 3500 s current excitation profiles - the first to parameterise the thermal model, and the second to validate the identified parameters and to demonstrate the temperature estimation technique. The profiles were generated by looping over different portions of an Artemis HEV drive cycle. The applied currents were in the range -23 A to +30 A. For the duration of the experiments, single frequency (215 Hz) impedance measurements were carried out every 24 s and the surface and internal temperatures were also monitored. In order to minimise heat loss through the cell ends, these were insulated using Styrofoam (Fig. 4). Before each experiment, the SOC was adjusted to 50% by drawing a 0.9 C current. The temperature of the thermal chamber was set to 8 °C and the cell was allowed to rest until its temperature equilibrated before experiments began.

Besides being a function of temperature and SOC, the impedance is also a function of DC current, mainly due to the charge transfer polarization decreasing with increasing current [23]. Previous results confirmed that when the EIS perturbation current is superposed over an applied DC current, the impedance measurement is altered [17]. To overcome this, the cell was allowed to rest briefly for 4 s before each EIS measurement was taken, i.e. 20 s periods of the excitation current followed by 4 s rests. The duration of this rest period was kept as short as possible to ensure that the thermal response of the cell to the applied cycle was not significantly altered, and it was found that the core cell temperature dropped by at most 0.25° C during these rest periods. The issue of impedance measurement under DC current warrants further investigation.

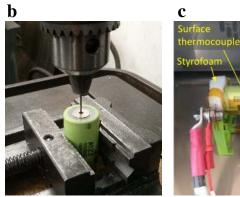
VI. MODEL PARAMETERISATION & VALIDATION

Parameterisation is performed to estimate the values of k_t , c_p , and h. The density ρ was identified in advance by measuring the cell mass and dividing by its volume. The values from the first excitation profile (comprising cell current, voltage plus surface, core and chamber temperatures) were used for the estimation.

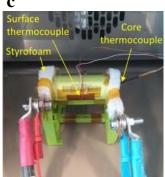
The parameterisation was carried out offline using *fmin-search* in Matlab to minimise the magnitude of the Euclidean distance between the measured and estimated core and surface



Power supply & impedance



Data acquisition module



d

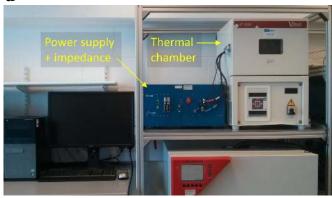


Figure 4. Experimental setup for parameter identification and validation. (a) schematic diagram with cutaway view showing cell core and jelly roll, (b) cell drilling procedure, (c) prepared cell inside thermal chamber, (d) power supply & thermal chamber.

temperatures, as in [4]. Table II compares the identified parameters with the initial guesses and parameters for the same cell from the literature. The estimated parameters are close to those reported in the literature. The deviations may be attributed to manufacturing variability, error in the heat generation calculation (due to the omission of entropic heating in all of these studies), heat generation in the contact resistances between the cell and connecting wires and/or measurement uncertainty in the temperature. The convection coefficient is within the range expected of forced convection air cooling [24].

Parameter	Units	Reference	Initial	Identified			
ρ	kg m ⁻³	2047-2118	-	2107			
		[4], [25], [26]					
c_p	J kg ⁻¹ K ⁻¹	1004.9-1109.2	1050	1171.6			
		[3], [7], [4]					
k_t	W m ⁻¹ K ⁻¹	0.488-0.690	0.55	0.404			
		[22], [25], [4]					
h	W m ⁻²	-	20	39.3			
Table II							

COMPARISON OF REFERENCE & ESTIMATED PARAMETERS

The measured core and surface temperatures (subscript 'exp') and the corresponding model predictions (subscript 'm') for the parameterised model are shown in Fig. 5. The root-mean-square errors (RMSE) in the surface and core temperatures are 0.19 °C and 0.18 °C respectively.

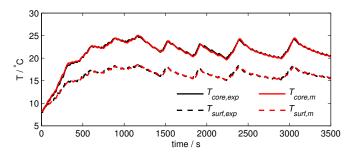


Figure 5. Model parameterisation: Comparison between measured and predicted core and surface temperatures in the parameterised model.

The model with identified parameters was validated against the second current excitation profile (Fig. 6). The RMSEs in the core and surface temperatures were 0.21 °C and 0.16 °C respectively in this case. These errors are only marginally greater than those in the parameterisation test, indicating that the estimation is satisfactory.

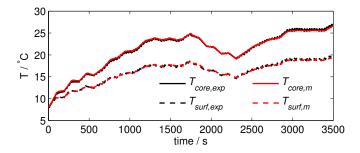


Figure 6. Model validation. Comparison between measured and predicted core and surface temperatures in the parameterised model applied to the second current excitation profile.

VII. STATE ESTIMATION

Kim et al. [6] showed that the effect of changes to the value of h on the predicted surface and core temperatures is greater

than the effect of changes to the other thermal parameters. Moreover, h depends strongly on the thermal management system settings and its calculation often relies on empirical correlations between coolant flow rates and heat transfer. Thus, there is a need to identify the convection coefficient online during operation. This section outlines the use of a dual extended Kalman filter (DEKF) [27] for estimating the core and surface temperatures and the convection coefficient. The DEKF reduces to an EKF if the convection coefficient is assumed known and provided to the model in advance.

We firstly modify eq. 9 by rewriting it as a discrete time model, setting the impedance as the model output, and explicitly including the dependency on the parameter, h_k :

$$\mathbf{x}_{k+1} = \mathbf{A}(h_k)\mathbf{x}_k + \mathbf{B}(h_k)\mathbf{u}_k + \mathbf{v}_k$$
(14)

$$y_k = f(\mathbf{x}_k, h_k) + n_k \tag{15}$$

$$h_{k+1} = h_k + e_k \tag{16}$$

where $y_k = Z'$ and $f(\mathbf{x}_k, h_k)$ is the non-linear function relating the state vector to the measurement (i.e. eq. 12), and \mathbf{v}_k , n_k and e_k are the noise inputs of the covariance matrices $\mathbf{R}^{\mathbf{v}}$, R^n and R^e . The states, inputs and measured outputs are thus $\mathbf{x} = [\overline{T} \ \overline{\gamma}]^T$, $\mathbf{u} = [Q \ T_\infty]^T$ and y = Z'. Note that, although the impedance is now the model output, the core and surface temperatures are also computed from the identified states and parameter at each time step using eq. 8, for validation against the thermocouple measurements. $\overline{\mathbf{A}}$ and $\overline{\mathbf{B}}$ are system matrices in the discrete-time domain, given by

$$\bar{\mathbf{A}} = e^{(\mathbf{A}\Delta t)}, \ \bar{\mathbf{B}} = \mathbf{A}^{-1}(\bar{\mathbf{A}} - \mathbf{I})\mathbf{B}$$
(17)

where Δt is the sampling time of 1 s. The update processes are then given as follows. The time update processes for the parameter filter are:

$$\hat{h}_{k}^{-} = \hat{h}_{k-1} \tag{18}$$

$$(P_k^h)^- = P_{k-1}^h + R^e \tag{19}$$

where \hat{h}_k^- and \hat{h}_k are the *a priori* and *a posteriori* estimates of the parameter *h*, and $(P_k^h)^-$ and P_{k-1}^h are the corresponding error covariances.

The time update processes for the state filter are:

$$\hat{\mathbf{x}}_{k}^{-} = \bar{\mathbf{A}}_{k-1}\hat{\mathbf{x}}_{k-1} + \bar{\mathbf{B}}_{k-1}\mathbf{u}_{k-1}$$
(20)

$$[\mathbf{P}_{k}^{\mathbf{x}})^{-} = \bar{\mathbf{A}}_{k-1}\mathbf{P}_{k-1}^{\mathbf{x}}\bar{\mathbf{A}}_{k-1}^{T} + \mathbf{R}^{\mathbf{v}}$$
(21)

where $\hat{\mathbf{x}}_k^-$ and $\hat{\mathbf{x}}_k$ are the *a priori* and *a posteriori* estimates of the state, and $(\mathbf{P}_k^{\mathbf{x}})^-$ and $\mathbf{P}_{k-1}^{\mathbf{x}}$ are the corresponding error covariances. The matrices $\bar{\mathbf{A}}_{k-1}$ and $\bar{\mathbf{B}}_{k-1}$ are calculated by:

$$\bar{\mathbf{A}}_{k-1} = \bar{\mathbf{A}}(h) \big|_{h=\hat{h}_k^-}, \ \bar{\mathbf{B}}_{k-1} = \bar{\mathbf{B}}(h) \big|_{h=\hat{h}_k^-}$$
(22)

Since the relationship between impedance and the cell state is non-linear, the measurement model must be linearised about the predicted observation at each measurement. The measurement update equations for the state filter are:

$$\mathbf{K}_{k}^{\mathbf{x}} = (\mathbf{P}_{k}^{\mathbf{x}})^{-} (\mathbf{H}_{k}^{\mathbf{x}})^{T} \left(\mathbf{H}_{k}^{\mathbf{x}} (\mathbf{P}_{k}^{\mathbf{x}})^{-} (\mathbf{H}_{k}^{\mathbf{x}})^{T} + R^{n} \right)^{-1}$$
(23)

$$\hat{\mathbf{x}}_{k} = \hat{\mathbf{x}}_{k}^{-} + \mathbf{K}_{k}^{\mathbf{x}} \left(z_{k} - f(\hat{\mathbf{x}}_{k}^{-}, \hat{h}_{k}^{-}) \right)$$
(24)

$$\mathbf{P}_{k}^{\mathbf{x}} = (\mathbf{I} - \mathbf{K}_{k}^{\mathbf{x}} \mathbf{H}_{k}^{\mathbf{x}})(\mathbf{P}_{k}^{\mathbf{x}})^{-}$$
(25)

where $\mathbf{K}_{k}^{\mathbf{x}}$ is the Kalman gain for the state, and $\mathbf{H}_{k}^{\mathbf{x}}$ is the Jacobian matrix of partial derivatives of f with respect to \mathbf{x} :

$$\mathbf{H}_{k}^{\mathbf{x}} = \frac{\partial f(\mathbf{x}_{k}, h_{k})}{\partial \mathbf{x}_{k}} \bigg|_{\mathbf{x}_{k} = \hat{\mathbf{x}}_{k}^{-}}$$
(26)

The measurement update processes for the parameter filter are:

$$K_{k}^{h} = (P_{k}^{h})^{-} (H_{k}^{h})^{T} \left(H_{k}^{h} (P_{k}^{h})^{-} (H_{k}^{h})^{T} + R^{n} \right)^{-1}$$
(27)

$$h_{k} = h_{k}^{-} + K_{k}^{n} \left(z_{k} - f(\hat{\mathbf{x}}_{k}, h_{k}^{-}) \right)$$
(28)

$$P_k^h = (I - K_k^h H_k^h) (P_k^h)^-$$
(29)

where H_k^h is the Jacobian matrix of partial derivatives of f with respect to h:

$$H_k^h = \frac{\partial f(\mathbf{x}_k, h_k)}{\partial h_k} \bigg|_{h_k = \hat{h}_k^-}$$
(30)

The above algorithm can be simplified to a standard EKF by omitting the parameter update processes (eqs. 16, 18-19 and 27-30) and assuming the convection coefficient is fixed. In the following section we investigate the performance of both the baseline EKF and the full DEKF algorithm.

VIII. RESULTS

We first investigate the performance of an EKF estimator whereby the convection coefficient is provided and assumed fixed. We then compare the performance of the DEKF algorithm with that of the baseline EKF when an incorrect initial estimate of the convection coefficient is provided. Lastly, we compare the performance of the DEKF with that of a dual Kalman filter (DKF) based on the same thermal model but with T_{surf} as the measurement input rather than Z'.

A. Convection Coefficient Known

The initial state estimate provided to the battery is $\hat{\mathbf{x}}_0 =$ [250], i.e. the battery has a uniform temperature distribution at 25 °C. The true initial battery state is a uniform temperature distribution at 8 °C. The covariance matrices are calculated as $R^n = \sigma_n^2$ and $\mathbf{R}^{\mathbf{v}} = \beta_v^2 diag(2,2)$. The first tuning parameter is chosen as $\sigma_n = 1 \times 10^{-4} \Omega$, which is a rough estimate of the standard deviation of the impedance measurement. The second tuning parameter was chosen as $\beta_v = 0.1$, by trial and error. Fig. 7 shows that, using the EKF, the core and surface temperatures quickly converge to the correct values and are accurately estimated throughout the entire excitation profile. The RMSEs of core and surface temperature are 1.35 °C and 1.34 °C respectively. In contrast, the RMSEs for the open loop model (subscript 'm') with no measurement feedback are 6.66 °C and 4.42 °C respectively. It should be noted that since the uncertainty of the impedance measurement typically increases as impedance decreases, the temperature estimates could be more uncertain at higher temperatures. Hence, the implementation of this technique could be more challenging at higher ambient temperature conditions than those studied here.

It should be noted that we also achieved similar performance using a simpler EKF based on Z' with the assumption that

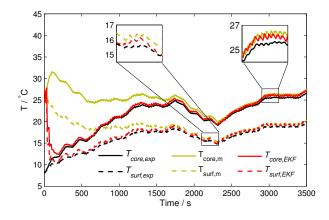


Figure 7. Temperature results for EKF using Z' as measurement input

the impedance is related directly to \overline{T} rather than to \overline{T}_{EIS} . However, this assumption may lead to unsatisfactory results for cells with a larger radius or when larger temperature gradients exist within the cell. Moreover, since this approach assumes that the impedance is a function of the state only (and not the parameter h), it is not suitable for the application of the DEKF discussed in the following section.

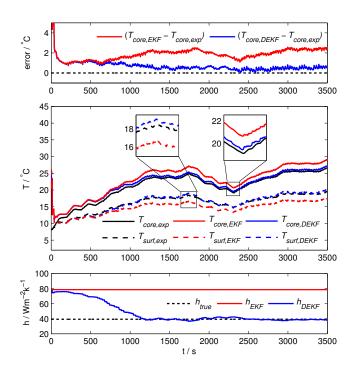


Figure 8. Temperature results for DEKF using Z' as measurement input

B. Convection Coefficient Unknown

Next we investigate the performance of the DEKF. The same incorrect initial state estimate is provided to the battery, $\hat{x}_0 = [25 \ 0]$. Moreover, an incorrect initial estimate for the convection coefficient is provided, $\hat{h}_0 = 2 \times h_{true}$. This value of h is also provided to the EKF. The error covariance matrix for the parameter estimator is $R^e = \beta_e^2$ where the tuning parameter is chosen as $\beta_e = 2.5$. Fig. 8 compares the results of both of these cases against the thermocouple measurements. The EKF is shown to overestimate the core temperature and underestimate the surface temperature for the duration of the experiments. This is expected, since the impedance measurement ensures the accuracy of the volume averaged cell temperature but the model assumes that the convection coefficient is higher than in reality, and therefore the temperature difference across the cell is overestimated. In contrast, the DEKF corrects the convection coefficient, and thus improves the accuracy of the subsequent temperature predictions. This is evident from the errors in the core temperature estimate (top plot of Fig. 8), which initially are similar in both cases but drop to much smaller values for the DEKF once the correct convection coefficient is identified. The RMSEs of core and surface temperature in each case are shown in Table III, along with the values for the time period, 1200 < t < 3500 s (i.e. after the convection coefficient value has converged).

Finally, we investigate the case where T_{surf} is used as the measurement $(y = T_{surf})$ to the estimator rather than Z'. This results in a linear KF and DKF exactly equivalent to that studied in [4]. The tuning parameters for the covariance matrices are also chosen to be the same as those employed in [4]. The same initial state and parameter estimates are provided as for the DEKF. Fig. 9 shows that the standard

EKF in this case overpredicts the core temperature by a greater margin than the EKF based on Z', although the surface temperature estimate is much more accurate. This is because the surface thermocouple ensures an accurate surface temperature estimate and to reconcile this with the overestimated convection coefficient, the core temperature estimate is forced to be much greater. The DKF correctly identifies the correct convection coefficient, in the same way as the DEKF. Since the thermocouple measurement exhibits less noise than the impedance measurement, the model converges to the correct estimate for h more quickly than in the DEFK case, as shown by the RMSE values in Table III.

Method	0 < t < 3500 s		1200 < t < 3500 s	
	T_{core}	T_{surf}	T_{core}	T_{surf}
EKF + Z'	2.04	2.06	1.79	1.98
$KF + T_{surf}$	2.49	1.44	2.90	1.58
DEKF + Z'	1.43	1.24	0.47	0.42
DKF + T_{surf}	0.36	0.33	0.16	0.14

Table III

COMPARISON OF RMSES FOR CORE AND SURFACE TEMPERATURES (°C) WITH UNKNOWN CONVECTION COEFFICIENT.

In conclusion, the temperature and convection coefficient estimators using Z' as measurement input are capable of accurately estimating the core and surface temperatures and the convection coefficient. The performance is comparable to that of an estimator using the same thermal model coupled with surface temperature measurements. Moreover, the performance of the present method is superior to that of previous methods based on impedance measurements alone, which only provide an estimate of the average internal temperature of the cell.

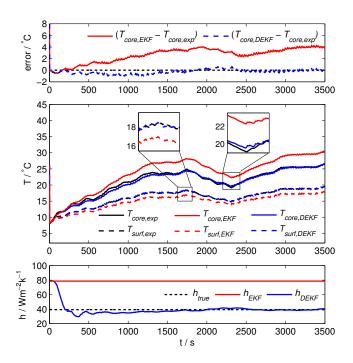


Figure 9. DKF using T_{surf} as measurement input.

IX. CONCLUSIONS

Impedance temperature detection enables both core and surface temperature estimation without using temperature sensors. In this study, the use of ITD as measurement input to a cell thermal model is demonstrated for the first time.

Previously, we estimated cell temperature distribution by combining ITD with a surface temperature measurement and imposing a quadratic assumption on the radial temperature profile. Frequency domain analysis shows that the QA solution may be inaccurate if the temperature of the cooling fluid has fluctuations on the order of 10^{-3} Hz or higher. The PA thermal model used in the present study is robust to higher frequency fluctuations (~ 10^{-2} Hz).

An EKF using a parameterised PA thermal model with ITD measurement input is shown to accurately predict core and surface temperatures for a current excitation profile based on an Artemis HEV drive cycle. A DEKF based on the same thermal model and measurement input is capable of accurately identifying the convection coefficient when the latter is not provided to the model in advance. The performance of the DEKF using impedance as measurement input is comparable to an equivalent DKF estimator using surface temperature as measurement input, although the latter is slightly superior due to the higher accuracy of the thermocouple.

Future work will investigate the application of ITD to multiple cells in a battery pack, as well as investigating methods of combining impedance with conventional sensors to enable more robust temperature monitoring and fault detection, and self-calibration.

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APPENDIX

A. Frequency Domain Analysis of Quadratic Assumption

The analysis leading to the frequency response plots of the QA model in Fig. 3 is outlined in this section. The QA model was used in [17] to obtain a unique solution for the temperature distribution when the impedance and surface temperature were measured but the cell thermal properties and heat generation rates were assumed unknown. To achieve a unique solution in that case, it was necessary to impose the assumption of a quadratic temperature distribution based on the solution of the 1D heat equation at steady state.

Muratori et al. [22] showed that the time domain PDE of eq. 2a, can be transformed into an equivalent ODE problem in the frequency domain which can be solved analytically. Using this approach the solution for the temperatures at the core and surface of the cell are shown to be:

$$T_{core}(s) = \frac{1}{k_t a^2} Q(s) + \frac{\frac{h}{k_t} (T_{\infty}(s) - \frac{1}{ka^2} Q(s))}{\frac{h}{k_t} J_0(ar_o) - a J_1(ar_o)}$$
(31)

$$T_{surf}(s) = \frac{1}{k_t a^2} Q(s) + \frac{\frac{k_t}{k_t} (I_{\infty}(s) - \frac{1}{k_t a^2} Q(s))}{\frac{h}{k_t} J_0(ar_o) - a J_1(ar_o)} J_0(ar_o)$$
(32)

where $a^2 = s\alpha^{-1}$, Q(s) is the transform of Q(t), and J_i is the *i*th-order Bessel function of the first kind [28]. Eqs. 31 and 32 can be interpreted as the outputs of a continuous time dynamic system [22], where $\mathbf{u}(t) = [Q(t), T_{\infty}(t)]^T$ and $\mathbf{y}(t) = [T_{core}(t), T_{surf}(t)]^T$, such that the solution of the BVP is equivalent to the impulse response of the system:

$$\begin{bmatrix} T_{core}(s) \\ T_{surf}(s) \end{bmatrix} = \begin{bmatrix} \mathbf{H}_{11}(s) & \mathbf{H}_{12}(s) \\ \mathbf{H}_{21}(s) & \mathbf{H}_{22}(s) \end{bmatrix} \begin{bmatrix} Q(s) \\ T_{\infty}(s) \end{bmatrix}$$
(33)

where the H matrix is formed by the transfer functions:

$$\mathbf{H}_{11}(s) = \frac{1}{k_t a^2} \frac{\frac{h}{k_t} J_0(ar_o) - a J_1(ar_o) - \frac{h}{k_t}}{\frac{h}{k_t} J_0(ar_o) - a J_1(ar_o)}$$
(34)

$$\mathbf{H}_{12}(s) = \frac{\overleftarrow{k_t}}{\frac{h}{k_t}J_0(ar_o) - aJ_1(ar_o)}$$
(35)

$$\mathbf{H}_{21}(s) = \frac{1}{k_t a^2} \frac{-aJ_1(ar_o)}{\frac{h}{k_t} J_0(ar_o) - aJ_1(ar_o)}$$
(36)

$$\mathbf{H}_{22}(s) = \frac{\frac{\hbar}{k_t} J_0(ar_o)}{\frac{\hbar}{k_t} J_0(ar_o) - a J_1(ar_o)}$$
(37)

This system of transfer functions gives frequency responses for the analytical solution results plotted in Fig. 3. Using a similar approach, we can develop an analytical solution to the QA model used in [17], where we denote the new transfer function $\mathbf{H}_{QA}(s)$. In this case, both the volume-averaged cell temperature (identified via the impedance²) and the surface temperature were measured directly, and it is assumed that no other information was available. Since these two inputs alone are not sufficient to achieve a unique solution for the temperature distribution, it was also necessary to impose the following constraint on the temperature profile:

$$T_{QA}(r) = T_{surf} + (T_{core, QA} - T_{surf}) \left(1 - \frac{r^2}{r_o^2}\right)$$
(38)

This is the 1D steady-state solution of the heat equation for a cylinder with uniform heat generation [24], with T(r) and T_{core} replaced by $T_{QA}(r)$ and $T_{core, QA}$.

The volume average of the QA temperature distribution is set equal to the true volume average temperature, giving:

$$\overline{T}_{QA} = \frac{2}{r_o^2} \int_0^{r_o} r T_{QA}(r) \mathrm{d}r = \overline{T}$$
(39)

Substituting eq. 38 in eq. 39 and integrating, the QA core temperature becomes

$$T_{core, QA} = 2\overline{T} - T_{surf} \tag{40}$$

Thus, an estimate for the core temperature is obtained directly from the surface and volume averaged temperature measurements. Since the surface temperature is measured, the values of $\mathbf{H}_{QA, 21}(s)$ and $\mathbf{H}_{QA, 22}(s)$ are identical to the corresponding values of the unsteady thermal model. The values of $\mathbf{H}_{QA, 11}(s)$ and $\mathbf{H}_{QA, 12}(s)$ can be obtained as follows: Substituting \overline{T} from eq. 5 into eq. 40, the QA approximation of the core temperature can be expressed as a function of the temperature distribution:

$$T_{core,QA} = \frac{4}{r_o^2} \int_0^{r_o} \left(rT(r) \mathrm{d}r - T_{surf} \right) dr \qquad (41)$$

Substituting eqs. 31 and 32, for T(r) and T_{surf} , respectively, and integrating (noting that $\int_0^{r_o} r J_0(ar) dr = r_o J_1(ar_o)/a)$, we obtain:

$$T_{core, QA} = \frac{Q(s)}{k_t a^2} + \frac{\frac{h}{k_t} (T_{\infty}(s) - \frac{1}{k_t a^2} Q(s))}{\frac{h}{k_t} J_0(ar_o) - a J_1(ar_o)} \left[\frac{4J_1(ar_o)}{ar_o} - J_0(ar_o) \right]$$
(42)

Thus, the QA system model is given by:

$$\begin{bmatrix} T_{core, QA}(s) \\ T_{surf, QA}(s) \end{bmatrix} = \begin{bmatrix} \mathbf{H}_{QA, 11}(s) & \mathbf{H}_{QA, 12}(s) \\ \mathbf{H}_{QA, 21}(s) & \mathbf{H}_{QA, 22}(s) \end{bmatrix} \begin{bmatrix} Q(s) \\ T_{\infty}(s) \end{bmatrix}$$
(43)

²As discussed in Section I, the impedance actually identifies \overline{T}_{EIS} , which is not necessarily equal to \overline{T} . However, the assumption that $\overline{T}_{EIS} = \overline{T}$ is satisfactory for the purpose of identifying the frequencies at which errors relative to the analytical solution become significant, and is only used for this purpose in this article.

where the **H** matrix is formed by the functions:

$$\mathbf{H}_{QA,\,11}(s) = -\frac{k_t a^2 r_o J_1(ar_o) - 2hr_o a J_0(ar_o) + 4h J_1(ar_o)}{k_t r_o a^3 \left(h J_0(ar_o) - k_t a J_1(ar_o)\right)}$$
(44)

$$\mathbf{H}_{QA,\,21}(s) = \frac{-hk_t a^3 J_0 a r_o + 4hk_t a^2 J_1 a r_o}{k_t r_o a^3 \left(h J_0 a r_o - k_t a J_1(a r_o)\right)} \tag{45}$$

$$\mathbf{H}_{QA, 12}(s) = \mathbf{H}_{21}(s)$$
(46)

$$\mathbf{H}_{QA,22}(s) = \mathbf{H}_{22}(s) \tag{47}$$

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