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1 **Shoreline instability under low-angle wave incidence**

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11 **Abstract.**

12 The growth of megacusps as shoreline instabilities is investigated by ex-
13 amining the coupling between wave transformation in the shoaling zone, long-
14 shore transport in the surf zone, cross-shore transport, and morphological
15 evolution. This coupling is known to drive a potential positive feedback in
16 case of very oblique wave incidence, leading to an unstable shoreline and the
17 consequent formation of shoreline sandwaves. Here, using a linear stability
18 model based on the one-line concept, we demonstrate that such instabilities
19 can also develop in case of low-angle or shore-normal incidence, under cer-
20 tain conditions (small enough wave height and/or large enough beach slope).
21 The wavelength and growth time scales are much smaller than those of high-
22 angle wave instabilities and are nearly in the range of those of surf zone rhyth-
23 mic bars, $O(10^2 - 10^3 \text{ m})$ and $O(1 - 10 \text{ days})$, respectively. The feedback
24 mechanism is based on: (1) wave refraction by a shoal (defined as a cross-
25 shore extension of the shoreline perturbation) leading to wave convergence
26 shoreward of it, (2) longshore sediment flux convergence between the shoal
27 and the shoreline, resulting in megacusp formation, and (3) cross-shore sed-

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28 iment flux from the surf to the shoaling zone, feeding the shoal. Even though
29 the present model is based on a crude representation of nearshore dynam-
30 ics, a comparison of model results with existing 2DH model output and lab-
31 oratory experiments suggests that the instability mechanism is plausible. Ad-
32 ditional work is required to fully assess whether and under which conditions
33 this mechanism exists in nature.

1. Introduction

34 Rhythmic shorelines featuring planview undulations with a relatively regular spacing or
35 wavelength are quite common on sandy coasts. In the present study, we focus on undu-
36 lations that are linked to submerged bars or shoals and are generally known as shoreline
37 sandwaves [*Komar, 1998; Bruun, 1954*]. These sandwaves can be classified according to
38 their length scale as short and long sandwaves (see, e.g., *Stewart and Davidson-Arnott*
39 [1988]).

40 The spacing of short sandwaves ranges from several tens to several hundreds of meters
41 and their seaward perturbations are known as megacusps. Observations show that these
42 megacusps can develop shoreward of crescentic bar systems during the typical “Rhythmic
43 Bar and Beach” morphological beach state or can develop from the shore attachment
44 of transverse bars that characterise the “Transverse Bar and Beach” state [*Wright and*
45 *Short, 1984*]. These transverse bars can appear where the horns of a previous crescentic
46 bar approach the shoreline [*Wright and Short, 1984; Sonu, 1973; Ranasinghe et al., 2004;*
47 *Lafon et al., 2004; Castelle et al., 2007*]. On the other hand, transverse bars can also
48 develop freely, independently of any offshore rhythmic system (e.g. the “transverse finger
49 bars” [*Sonu, 1968, 1973; Ribas and Kroon, 2007*]). The formation of rhythmic surf zone
50 bars and associated megacusps is believed to be due primarily to an instability of the
51 coupling between the evolving bathymetry and the distribution of wave breaking (bed-
52 surf coupling) [*Falqués et al., 2000*]. The developing shoals and channels cause changes in
53 wave breaking, which in turn cause gradients in radiation stresses and thereby horizontal
54 circulation with rip currents. If the sediment fluxes carried by this circulation converge

55 over the shoals and diverge over the channels, a positive feedback arises and the coupled
56 system self-organizes to produce certain patterns, both morphological and hydrodynamic
57 (see, e.g., *Reniers et al.* [2004]; *Garnier et al.* [2008]). In the case of oblique wave inci-
58 dence, a meandering of the longshore current is also essential to the instability process
59 [*Garnier et al.*, 2006]. Two important characteristics of all available models of the self-
60 organized formation of rhythmic surf zone bars are that they (1) are essentially based
61 on sediment transport driven by the longshore current and rip currents only, i.e. ignore
62 cross-shore transport induced by undertow and wave non-linearity and (2) do not consider
63 morphological changes beyond the offshore reach of the rip-current circulation.

64 Rhythmic shorelines can also develop as a result of an instability not related to bed-
65 surf coupling. *Ashton et al.* [2001] and *Ashton and Murray* [2006a, b] have shown that
66 sandy shorelines are unstable for wave angles (angle between wave fronts and the local
67 shoreline orientation) larger than about 42° in deep water, leading to the formation of
68 shoreline sandwaves, cusped features and spits. *Falqués and Calvete* [2005] have found
69 that the initial characteristic wavelength of the emerging sandwaves is in the range of 3 to
70 15 km, i.e., much larger than that of surf zone rhythmic bars. This instability caused by
71 high-angle waves will henceforth be referred to as HAWI (High-Angle Wave Instability).
72 The physical mechanism can be explained as follows. For oblique wave incidence, there
73 are essentially two counteracting effects. On one hand, the angle relative to the local
74 shoreline is larger on the lee of a cusped feature than on the updrift side. This tends to
75 cause larger alongshore sediment flux at the lee and thereby divergence of sediment flux
76 along the bump, which therefore tends to erode. On the other hand, since the refractive
77 wave ray turning is stronger at the lee than at the updrift flank, there is more wave energy

78 spreading due to crest stretching at the lee causing smaller waves and smaller alongshore
79 sediment flux. This produces convergence of sediment flux at the bump, which therefore
80 tends to grow. For high angle waves the latter effect dominates and, if the bathymetric
81 perturbation associated with the shoreline feature extends far enough offshore, it leads to
82 the development of the cusped feature. In contrast to the bed-surf instability for rhythmic
83 surf zone bars, this instability mechanism depends essentially on the coupling between the
84 surf and shoaling zones. Indeed, the gradients in alongshore sediment flux that induce
85 bathymetric changes in the surf zone occur because of wave field perturbations induced by
86 bathymetric features in the shoaling zone. Thus, in order to achieve a positive feedback,
87 the shoals (or the bed depressions) in the surf zone must extend into the shoaling zone.
88 This is achieved by the cross-shore sediment fluxes induced, for instance, by wave non-
89 linearity, gravity and undertow, which force the cross-shore shoreface profile to reach an
90 equilibrium profile. HAWI may provide an explanation for the self-organized formation
91 of some long shoreline sand waves which are reported in the literature [*Verhagen, 1989*;
92 *Inman et al., 1992*; *Thevenot and Kraus, 1995*; *Ruessink and Jeuken, 2002*; *Davidson-*
93 *Arnott and van Heyningen, 2003*].

94 On the other hand, some observations for low incidence angles show that longshore
95 currents can converge on megacusps because of wave refraction [*Komar, 1998*]. Such cur-
96 rent convergence may lead to longshore sediment flux convergence and hence to megacusp
97 growth. If the submerged part of the megacusp grows and extends far enough into the
98 shoaling zone (due to the cross-shore transport leading to an equilibrium profile), wave
99 refraction would be enhanced and a positive feedback would arise. This might provide a
100 mechanism for shoreline instability formation under low-angle wave incidence that bears

101 some similitude with HAWI in the sense that the coupling between the surf and shoaling
102 zones is essential, in contrast to the bed-surf instability. We will refer to this potential
103 mechanism as Low-Angle Wave Instability (LAWI). The aim of the present contribution
104 is to investigate this new morphodynamic instability mechanism and discuss whether the
105 resulting shoreline instability may be found in nature.

106 The lay-out of this paper is as follows. First (Section 2), we introduce the 1D-morfo
107 model [*Falqués and Calvete, 2005*] that we used to investigate LAWI. Numerical experi-
108 ments of idealized cases are presented and analyzed in Section 3. We find that shoreline
109 sandwaves can indeed develop because of LAWI, with a length scale comparable to those
110 of megacusps and rhythmic surf zone bars. In Section 4, we analyze the physics of the
111 instability mechanism. We conclude our paper with a discussion and a summary of the
112 main results.

2. The shoreline stability model: 1D-morfo

113 Owing to the similitude with HAWI [*Ashton et al., 2001; Falqués and Calvete, 2005*], the
114 LAWI mechanism is assumed to be un-related to surf zone processes like rip or longshore
115 meandering currents. Thus, the engineering simplification of one-line modeling [*Dean
116 and Dalrymple, 2002*] is used, where the shoreline dynamics are based on alongshore
117 gradients in the total alongshore transport rate, Q (i.e., the total volume of sand carried
118 by the wave-driven longshore current that crosses a cross-section of the surf zone area
119 for unit of time (m^3/s)). Using such a simple model, which neglects numerous aspects
120 of surf zone dynamics, including rip current circulation, longshore current meandering,
121 and thus the bed-surf coupling phenomena, allows to investigate properly whether the
122 LAWI mechanism is supported by the governing equations. Furthermore, the consistency

123 of the sediment transport patterns from the one-line modelling has been confirmed by
124 using a 2DH model (delft3D) [List and Ashton, 2007], at least in case of HAWI. These
125 reasons, in addition to the fact that HAWI has been studied and reproduced with a linear
126 stability model called 1D-morfo based on the one-line concept, lead us to use the same
127 model to investigate LAWI and its differences with HAWI. A very brief description of the
128 1D-morfo model is given here. The reader is referred to *Falqués and Calvete* [2005] for
129 further details.

130 The model describes the dynamics of small amplitude perturbations of an otherwise rec-
131 tilinear coastline. Following the one-line concept, the dynamics are governed by gradients
132 in the total alongshore wave-driven transport rate Q :

$$\bar{D} \frac{\partial x_s}{\partial t} = - \frac{\partial Q}{\partial y} \quad (1)$$

133 A Cartesian coordinate system is used, with x increasing seaward in the unperturbed
134 cross-shore direction and y running alongshore (Figure 1). The position of the shoreline
135 is given by $x = x_s(y, t)$, where t is time and \bar{D} is the active water depth (as defined by
136 *Falqués and Calvete* [2005]), which is of the order of the depth of closure. This active
137 water depth is directly related to the one-line model concept, for more details, see *Falqués*
138 *and Calvete* [2005]. The transport rate Q is computed according to the longshore sediment
139 transport equation of *Ozasa and Brampton* [1980]. In this formulation, Q is the sum of
140 two terms: the first one (Q_1) is driven by waves approaching the shore at an angle and
141 is equivalent to the CERC formula [USACE, 1984], and the second one (Q_2) takes into
142 account the influence of wave set-up induced currents related to the alongshore gradient
143 in the wave height.

Figure 1

144 The equation of the sediment transport rate Q can be written as follows:

$$Q = Q_1 + Q_2 \quad Q = \mu H_b^{5/2} \left(\sin(2(\theta_b - \phi)) - r \frac{2}{\beta} \cos(\theta_b - \phi) \frac{\partial H_b}{\partial y} \right) \quad (2)$$

145 where H_b is the (rms) wave height at breaking (index b), θ_b is the angle between wave
146 fronts and the unperturbed coastline at breaking, and $\phi = \tan^{-1}(\partial x_s / \partial y)$ is the local
147 orientation of the perturbed shoreline. β is the beach slope at the instantaneous shoreline
148 (i.e. the waterline). The constant μ is proportional to the empirical parameter K_1 of
149 the original CERC formula and is $\sim 0.1 - 0.2 \text{ m}^{1/2}\text{s}^{-1}$. For the reference case of this
150 paper, a value, $\mu = 0.15 \text{ m}^{1/2}\text{s}^{-1}$, was chosen, which corresponds to $K_1 = 0.525$. The
151 nondimensional parameter r is equal to K_2/K_1 , where K_2 is the empirical parameter of
152 *Ozasa and Brampton* [1980]. According to *Horikawa* [1988], r ranges between 0.5 and 1.5,
153 whereas *Ozasa and Brampton* [1980] suggest a value of 1.62. The value $r = 1$ is used for
154 the present reference case, which is equivalent to $K_2 = K_1$ and has been used in several
155 earlier studies on shoreline instabilities [*Bender and Dean*, 2004; *List et al.*, 2008; *van den*
156 *Berg et al.*, 2011]. However, the term Q_2 is not always taken into account, and its validity
157 and application range are uncertain. In section 3.2, we will study the sensitivity of our
158 results to the value of r .

159 Some discussion exists about the capacity of the CERC formula (Q_1) to predict correctly
160 gradients in alongshore sediment transport in the presence of bathymetric perturbations
161 [*List et al.*, 2006, 2008; *van den Berg et al.*, 2011]. The results of *List and Ashton* [2007]
162 suggest that the CERC formula predicts qualitatively correct transport gradients for large
163 scale shoreline undulations (alongshore lengths of 1-8 km). The term Q_2 was introduced to
164 describe the sediment transport resulting from alongshore variations in the breaker wave
165 height induced by diffraction near coastal structures. These breaker-height variations in-

166 duce alongshore gradients in set-up, which drive longshore currents and hence sediment
167 transport. In our work, alongshore variability in breaker heights is related to wave re-
168 fraction rather than to wave diffraction, but the subsequent mechanism for alongshore
169 sediment transport remains the same.

170 To compute the sediment transport rate according to eq. 2, $H_b(y, t)$ and $\theta_b(y, t)$ are
171 needed. The procedure to determine them is as follows. It is assumed that the wave
172 height and wave angle are alongshore uniform in deep water. Then, wave transformation,
173 including refraction and shoaling, is performed from deep water up to the breaking point
174 so that $H_b(y, t)$ and $\theta_b(y, t)$ are determined and Q can be computed. To do the wave
175 transformation, a perturbed nearshore bathymetry coupled to the shoreline changes is
176 assumed:

$$D(x, y, t) = D_0(x) - \beta f(x) x_s(y, t) \quad (3)$$

177 where $D(x, y, t)$ and $D_0(x)$ are the perturbed and unperturbed water depth, respectively,
178 and $f(x)$ is a shape function. Figure 2a shows some examples of possible perturbation
179 profiles: constant bed perturbation in the surf zone and decreasing exponentially in the
180 offshore direction (P1), bed perturbation decreasing exponentially in the offshore direction
181 from the coast (P2), and bed perturbation similar to a shoal (P3 and P4).

Figure 2

182 The offshore extension of the bathymetric perturbation is controlled by its “charac-
183 teristic” length, xl , which is a free parameter in the model. It was shown by *Falqués*
184 *and Calvete* [2005] that the coupling between the surf and shoaling zones is crucial for
185 HAWI. This is accomplished only if xl is at least a couple of times larger than the surf
186 zone width. The parameter xl can be seen as a way to parameterise cross-shore sediment
187 transport, especially between the surf and shoaling zones. This makes HAWI essentially

188 different from the surf zone morphodynamic instabilities that lead to rhythmic bars and
189 rip channels. The changes in the shoreline cause changes in the bathymetry (both in the
190 surf and shoaling zones), which in turn cause changes in the wave field. The changes in
191 the wave field affect the sediment transport that drives shoreline evolution. Therefore,
192 the shoreline, the bathymetry and the wave field are fully coupled.

193 Following the linear stability concept, the perturbation of the shoreline is assumed to
194 be

$$x_s(y, t) = ae^{\sigma t + iKy} + c.c. \quad (4)$$

195 where a is a small amplitude. For each given (real) wavenumber, K , this expression is
196 inserted into the governing equation (eq. 1), and into the perturbed bathymetry equation
197 (eq. 3). By computing the perturbed wave field and inserting H_b and θ_b in eq. 1, the
198 complex growth rate, $\sigma(K) = \sigma_r + i\sigma_i$, is determined. All of the equations are linearized
199 with respect to the amplitude, a . Then, for those K such that $\sigma_r(K) > 0$ a sandwave with
200 wavelength $\lambda = 2\pi/K$ tends to emerge from a positive feedback between the morphology
201 and the wave field. The pattern that has the maximum growth rate is called the Linearly
202 Most Amplified mode (LMA mode).

3. Numerical experiments on idealised cases

203 To investigate the possible mechanism causing shoreline instabilities under low wave
204 incidence angles, numerical experiments on idealised cases are performed. First, numerical
205 experiments and results are given. Then, a sensitivity study is done to assess better the
206 results.

3.1. Instabilities versus beach slope and wave incidence angle

207 3.1.1. Configuration

208 A Dean profile (Figure 2b) is chosen as the equilibrium profile, using various beach
209 slopes (Figures 2b and c). The adopted profile is given by:

$$D_0(x) = b \left((x + x_0)^{2/3} - x_0^{2/3} \right) \quad (5)$$

210 which has been modified from the original Dean profile to avoid an infinite slope at the
211 shoreline. The constants b and x_0 are determined from the prescribed slope β at the
212 coastline and the prescribed distance x_c from the coastline to the location of the closure
213 depth D_c (see *Falqués and Calvete* [2005] for details). The forcing conditions are waves
214 with $H_{rms} = 1.5$ m and $Tp = 8$ s at a water depth of 25 m. The wave direction ranges
215 from 0° to 85° in increments of 5° . A closure depth $\bar{D} = 20$ m is chosen. To perform the
216 linear stability analysis, the shape function for the bathymetric perturbations is assumed
217 to be constant in the surf zone and to decrease exponentially seaward. Its cross-shore
218 extent is given by the characteristic distance xl corresponding to the closure depth of 20
219 m, i.e. $xl = 1410$ m for the present case (P1-perturbation in Figure 2a).

220 3.1.2. Results

221 Figure 3a shows the growth rate of the LMA mode versus the wave angle and the beach
222 slope. The wave angle is given for a water depth of 25 m. The beach slope is defined as
223 the beach slope at the shoreline. For small beach slopes (< 0.04) the coast behaves as
224 expected: it is unstable only if the wave incidence angle is large enough. In this case, the
225 shoreline instabilities clearly correspond to HAWI. For instance, for a beach slope of 0.02,

Figure 3

226 a wave incidence of 70° leads to the largest growth rate ($3.13 \times 10^{-9} \text{ s}^{-1}$), corresponding
227 to a wavelength of 7000 m (Figure 3b).

228 However, for larger beach slopes, instabilities occur for all wave directions, and espe-
229 cially for low wave incidence angles. These instabilities correspond to what will be called
230 LAWI in the present paper. Furthermore, among all the wave incidence angles, the most
231 amplified mode is for shore-normal wave incidence. For a beach slope of 0.1, an angle of
232 0° leads to the largest growth rate ($1.82 \times 10^{-6} \text{ s}^{-1}$), corresponding to a wavelength of
233 571 m (Figure 3b).

3.2. Sensitivity analysis

234 The sensitivity analysis is performed using a planar beach, as the aim is to focus on the
235 mechanisms. However, simulations with other (e.g. barred) profiles also lead to LAWI
236 (not shown).

3.2.1. Wave height and beach slope

238 Keeping the same reference configuration as above and focusing on shore-normal wave
239 incidence, we investigate the sensitivity of the instability to the wave height for a range
240 of beach slopes. For normally incident waves, instabilities develop only for a beach slope
241 that exceeds 0.04 (Figure 4). In this case, there is an optimum in the wave height for
242 which the growth rate is largest. This wave height increases with the beach slope. For
243 instance, for a beach slope of 0.1 and 0.18), the optimal wave height H_{rms} is 1.75 m and
244 2.5 m, respectively. A wave height increase also leads to an increase in the LMA mode
245 wavelength, which is due to the corresponding increase in surf zone width.

Figure 4

3.2.2. Bathymetric perturbation length

247 The influence of the parameter xl was previously investigated by *Falqués and Calvete*
248 [2005], who showed that xl must exceed a threshold to initiate HAWI (the perturbation
249 must extend across both the surf and shoaling zones). Similar behaviour is found here
250 by exploring the range between $xl = 10$ and $xl = 10^4$ m. Figure 5 shows that there is a
251 threshold, $xl > 100$ m, above which shoreline instabilities may occur. This value appears
252 physically reasonable since the width of the surf zone in the reference case is about 73
253 m. For $125 \leq xl \leq 250$ m, the shoreline instability wavelength decreases significantly
254 (from 1040 to 530 m) with increasing perturbation length, whereas for $xl \geq 250$ m, the
255 wavelength increases only slightly until reaching a nearly constant value of 574 m. The
256 growth rate increases with increasing xl for values below 500 m but decreases for xl
257 exceeding 500 m, reaching a nearly constant value for large perturbation length scales.
258 The main conclusion is that instabilities occur only if the perturbation extends far enough
259 into the shoaling zone. When the perturbation length is about the width of the surf zone,
260 it influences the wavelength and growth rate of the LMA mode strongly, whereas for larger
261 perturbation length values, this influence is negligible.

Figure 5

262 **3.2.3. Initial perturbation shape**

263 To evaluate the influence of the bathymetric perturbation shape function on the results
264 we have presented so far, several shapes were investigated using the same wave-boundary
265 conditions and a perturbation length xl of 2000 m. The shape functions we consider are
266 (Figure 2a):

- 267 • Perturbation P1: bed perturbation constant in the surf zone and decreasing expo-
268 nentially in the offshore direction

269 • Perturbation P2: bed perturbation decreasing exponentially from the coast in the
270 offshore direction

271 • Perturbation P3: P2 perturbation with a shoal located only in the shoaling zone,
272 from 400 to 800 m, with a maximum height at $x_1 = 600$ m.

273 • Perturbation P4: P2 perturbation with a shoal located in both the surf and shoaling
274 zones, from 0 to 1400 m, with a maximum height at $x_1 = 600$ m.

275 The reference configuration is still the same ($H_{rms}=1.5$ m, $T = 8$ s, $\theta = 0^\circ$). The four
276 shape functions result in LMA mode wavelengths of 571, 571, 608 and 608 m, respectively,
277 and growth rates of 1.7, 1.5, 1.7, 1.7×10^{-6} s⁻¹, respectively. Thus, the results are
278 slightly sensitive (mean wavelength of 598 m and a standard deviation of 18 m) to the
279 bed perturbation type, but all perturbation types cause LAWI with similar growth rates.

280 3.2.4. Sediment transport equation

281 To investigate the sensitivity of the results to the sediment transport equation, compu-
282 tations were carried out with $r = 0$, which reduces eq. 2 to the CERC equation. This
283 sensitivity study is done in beach slope - wave angle space. The LMA characteristics are
284 quite similar with $r = 1$ (Figure 3) and $r = 0$ (Figure 6), except for the case of normal
285 wave incidence. In this case ($r = 0$), for small beach slopes, all of the perturbations are
286 damped, as for $r = 1$. For larger beach slopes, the growth rate increases with decreasing
287 perturbation wavelength without reaching a local maximum (Figure 7). Thus there is no
288 LMA mode for shore-normal wave incidence (X symbol on Figure 6). This specific case for
289 shore-normal wave incidence will be discussed in section 4. To summarize, the previous
290 results are not highly sensitive to the second term of the sediment transport equation,
291 except for the case of shore-normal wave incidence.

Figure 6

Figure 7

4. The physical mechanism

292 Here we investigate the physics behind the model prediction of shoreline instabilities
 293 caused by low wave incidence angles. The physical processes are analysed based on the
 294 study of the growth rate components, and the hydrodynamic and sediment transport
 295 patterns, before identifying the main mechanisms.

4.1. Growth rate analysis

296 In the perturbed situation where the shoreline position is given by eq. 4, the wave
 297 height and wave angle at breaking are given by:

$$\begin{aligned}
 H_b(y, t) &= H_b^0 + (\hat{H}'_{br} + i\hat{H}'_{bi})e^{\sigma t + iKy} + c.c. \\
 \theta_b(y, t) &= \theta_b^0 + (\hat{\theta}'_{br} + i\hat{\theta}'_{bi})e^{\sigma t + iKy} + c.c.
 \end{aligned} \tag{6}$$

298 where H_b^0, θ_b^0 are the wave height and angle for the unperturbed situation. Then, according
 299 to *Falqués and Calvete* [2005], the growth rate (the real part of the complex growth rate)
 300 is:

$$\sigma_r = \underbrace{2\frac{\mu}{D}H_b^0K^2\cos(2\theta_b^0)}_{e_0} \left(\underbrace{-1}_{e_1} + \underbrace{\frac{\hat{\theta}'_{bi}}{aK}}_{e_2} + \underbrace{\frac{5\hat{H}'_{bi}}{4aKH_b^0}\tan(2\theta_b^0)}_{e_3} - r \underbrace{\frac{\hat{H}'_{br}\cos(\theta_b^0)}{a\beta\cos(2\theta_b^0)}}_{e_4} \right) \tag{7}$$

301 A clue to the physical mechanism is provided by a careful analysis of the meaning and
 302 behaviour of each term:

303 • e_0 : common to all terms. It does not contribute to the stability/instability since it
 304 is positive. This is because we can assume that $\theta_b^0 < 45^\circ$ due to wave refraction. It is the
 305 magnitude of the growth rate.

306 • e_1 : always negative. It represents the contribution due to the changes in shoreline
 307 orientation when there is no perturbation in the wave field. This is the only term arising

308 in case of the classical analytical one-line modeling (Pelnard-Considère equation) [Dean
309 and Dalrymple, 2002]. It is a damping term describing the shoreline diffusivity in that
310 approach.

311 • e_2 : its sign depends on $\hat{\theta}'_{bi}$. Numerical computations [Falqués and Calvete, 2005]
312 demonstrates that it is always positive. This results from the fact that refracted wave
313 rays tend to rotate in the same direction as the shoreline. Thus e_2 is a growing term.

314 • e_3 : its sign depends on \hat{H}'_{bi} . Numerical computations [Falqués and Calvete, 2005]
315 show that $\hat{H}'_{bi} > 0$ for long sandwaves and < 0 for short sandwaves. This term is related
316 to energy spreading due to wave crest stretching as waves refract. Thus e_3 is a growing or
317 damping term, depending on the sandwave wavelength, $2\pi/K$. Moreover, its magnitude
318 increases with an increasing incident wave angle. These two properties explain that e_3 is
319 an essential growing term for HAWI formation Falqués and Calvete [2005], whereas, for
320 LAWI, its magnitude is smaller and it is, most of the time, negative.

321 • e_4 : this term stems from the alongshore gradients in H_b in the sediment transport
322 equation (eq. 2). Its sign is the opposite to that of \hat{H}'_{br} , which is numerically found to be
323 always positive. This is related to the fact that the maximum in wave energy is always
324 located close to the sandwave crest (wave focusing). Thus e_4 is a damping term.

325 The corresponding growth rate contributions, $\sigma_1 = e_0e_1$, $\sigma_2 = e_0e_2$, ... are plotted in
326 Figure 8. It can be seen that σ_2 is always positive leading to the development of shoreline
327 sandwaves, whereas σ_1 and σ_4 are always negative, leading to the damping of the sand-
328 waves. The term σ_3 can be either positive, for small beach slope (eg smaller than 0.05
329 to 0.08), or negative, for larger beach slopes. Even if the behaviour of this term is not
330 monotonous, σ_3 generally increases with the wave angle. It is remarkable that σ_2 becomes

Figure 8

331 very large for large beach slopes and for small wave angles. For normal wave incidence
332 ($\theta_b^0 = 0$), $\sigma_3 = 0$ and σ_2 is the only contribution leading to the instability. We therefore
333 conclude that wave refraction is responsible for LAWI in the case of very steep beach
334 slopes.

335 Based on the growth rate results, it is also possible to analyse the relative influence
336 of the wave incidence induced Q_1 and wave set-up induced Q_2 sediment transport. The
337 analysis of the growth rate versus the perturbation wavelength for $r = 0$ or $r = 1$ and
338 several wave incidence angles θ (Figure 9) shows that the relative influence of Q_2 decreases
339 with increasing the wave incidence angle. In other words, wave height gradients (wave set-
340 up induced sediment fluxes) largely influence (damp) the shoreline instability for low wave
341 angle incidence (LAWI), whereas their impact is almost negligible for large wave incidence
342 angles (HAWI). The main driving term of the LAWI is due to the wave incidence induced
343 sediment transport flux Q_1 . This means that the use of the CERC equation alone, taking
344 into account wave refraction in the shoaling zone, can cause LAWI. The Q_2 term influences
345 this instability by changing the growth rate and the favored wavelength. This influence
346 increases with decreasing wave incidence until the case of perfectly shore-normal waves,
347 for which there is a preferred wavelength (LMA mode) only if the Q_2 term is taken into
348 account (Figure 6).

Figure 9

4.2. Model results analysis: Hydrodynamic and sediment transport

349 To understand better how wave refraction causes shoreline instabilities, hydrodynamic
350 and sediment transport model results are analysed next. Here, we focus on the case
351 of shore-normal wave incidence, considering the LMA mode obtained for a beach slope
352 equal to 0.1 (case a). The model results are compared with the same wave incidence, but

353 a smaller beach slope (0.02) for which the shoreline is stable (case b). The perturbation
354 wavelength (571 m) is the same for both cases, corresponding to the LMA mode of case
355 (a). Although the linear stability analysis is strictly valid only in the limit $a \rightarrow 0$ we
356 choose a shoreline sandwave amplitude $a = 10$ m (for visualization and comparison of
357 the different sources of sediment transport). In addition, to make the analysis simpler,
358 we assume shore-normal waves and $r = 0$. Figures 10a and b show planviews of the
359 wave angle, as well as a longshore cross-section of several quantities along the breaking
360 line. First, it can be noted that the breaking line is much farther offshore in case (b)
361 because of the shallower bathymetry. This is directly linked with the bathymetry. These
362 planviews illustrate the wave focussing on the cusp, which implies increasing wave height
363 and converging waves at the cusps.

364 Looking at the alongshore cross-section (Figure 10c), the wave angle amplitude is much
365 larger for case (a) than for case (b), about 14° versus 3.2° , indicating a stronger refraction
366 up to the breaking line in case (a). The corresponding amplitude of the oscillation in
367 the shoreline angle is about 6.3° , and is thus within the range of those two values. This
368 means that the angle of the wave fronts with respect to the local shoreline reverses when
369 passing from case (a) to (b), implying a reversal in the direction of sediment transport.
370 This can be traced back to equation 6. The wave angle amplitude is much larger for case
371 (a). Coming back to equation 6, in the case of shore-normal waves and $r = 0$, there are
372 only two terms left: e_1 , which is the contribution due to shoreline change only, and e_2 ,
373 which represents the wave refraction-induced sediment flux. The analytical computation
374 for the present case leads to: $e_1 = -1$ for both cases, whereas $e_2 = 2.23$ for case (a) and
375 $e_2 = 0.507$ (case b), consistent with the different amplitudes of alongshore wave angle

Figures 10

376 oscillation. This clearly shows that the growth rate is positive for case (a) and negative
377 for case (b). The alongshore cross-section of the resulting sediment flux Q (Figure 10c)
378 illustrates the opposite behaviour for the two cases. Our sign convention is that positive
379 Q represents sediment transport directed in the direction of the increasing y coordinate
380 (i.e. to the right on the cross-sections). A positive (negative) longshore gradient indicates
381 a convergence (divergence), assumed to cause shoreline accretion (erosion). Thus Figure
382 10c shows that Q for case (a) has a spatial phase-lag compared to the shoreline such that
383 the shoreline perturbation should be amplified, whereas Q for case (b) has an opposite
384 phase-lag, leading to the damping of the perturbation. This spatial phase-lag change
385 results from the continuous amplitude changes of the terms e_1 and e_2 : the phase-lag
386 between shoreline and longshore sediment fluxes is either 90° or -90° , implying that
387 there is no migration and either amplification or damping of the shoreline perturbation.
388 Thus, for shore-normal waves and neglecting the damping term related with wave set-
389 up induced sediment flux (second term in eq. 2), the instability of the shoreline results
390 from an alongshore oscillation in the angle of wave refraction, which is stronger than the
391 oscillation in the angle of shoreline orientation.

4.3. Mechanism

392 From the above, we can draw the following conclusion: the main growing term is re-
393 lated to the wave refraction toward the cusp, leading to wave incidence induced sediment
394 transport converging at the cusp. This term strongly increases with beach slope. The
395 damping is due to three components: (1) longshore sediment transport due to the shore-
396 line orientation only (and not refraction, term e_1), (2) wave energy spreading (term e_3),

397 and (3) wave height gradients (set-up) (term e_4), the second component having a smaller
398 damping effect than the two others.

399 Now we can figure out how LAWI works (Figure 11). Let us consider shore-normal
400 wave incidence. In this case, the wave energy spreading has no influence on the instability
401 ($e_3 = 0$). If a cusped feature with an associated shoal develops on a coastline, wave
402 refraction bends wave rays towards the tip of the feature. Depending on the orientation
403 of the refracted wave fronts with respect to the local shoreline along the cusped feature,
404 the alongshore sediment flux can be directed towards the tip, reinforcing it and leading to
405 a positive feedback between flow and morphology. Whether the transport is directed to
406 the tip, depends on the bathymetry and wave conditions. For a given offshore extent, xl ,
407 of the associated shoal and a given wave height, the surf zone will become narrower if the
408 beach slope increases. Then, the shoal will extend a longer distance beyond the surf zone,
409 and the waves will be refracted strongly when they reach the breaking point, increasing
410 the wave incidence related sediment flux (e_2) convergence whereas the divergence term
411 (e_1) is constant. As shown by the model results (Figure 10), the contribution of the
412 refracted wave angle (e_2) can exceed the contribution of the shoreline orientation to the
413 sediment flux (e_1), such that Q_1 (resulting from e_1 and e_2) converges near the cusp. This
414 leads to the development of the cusp. If the beach slope is mild, the surf zone will be
415 wider, and wave refraction over the shoal before breaking will be less intense, leading to
416 smaller wave incidence angle induced sediment fluxes, which are dominated instead by the
417 diverging sediment flux induced by shoreline orientation changes. In this case, as shown
418 in the model results (Figure 10c), the sediment flux is directed away from the tip of the
419 cusp.

Figure 11

5. Discussion

5.1. Linear stability analysis validity

420 The 1D-morfo model has been applied to investigate HAWI and to study the sandwaves
421 generation along the Dutch coast [*Falqués, 2006*], El Puntal beach - Spain [*Medellín et al.,*
422 2008, 2009]. The results indicated similarities with the wavelengths observed in nature.
423 This supports the use of this linear stability model to investigate the mechanisms of shore-
424 line sandwave formation. In the present paper, it is clear that LAWI is a robust output
425 of the 1D-morfo model, and the physical mechanism causing instabilities is wave refrac-
426 tion induced by an offshore shoal associated with a cusped feature. This wave refraction
427 leads to two counter-acting phenomena: sediment transport induced by converging waves
428 counteracted by diverging wave height gradients. The present paper investigates the lin-
429 ear generation only. The pros and cons of linear stability analysis have been discussed
430 extensively in [*Blondeaux, 2001; Dodd et al., 2003; Falqués et al., 2008; Tiessen et al.,*
431 2010]. In any case, the fundamental assumption of infinitesimal amplitude growth makes
432 comparisons to field data questionable. Nonlinear model studies for other rhythmic fea-
433 tures, such as crescentic sandbars and sand ridges [*Calvete, 1999; Damgaard et al., 2002*],
434 have sometimes shown the finite-amplitude dynamics to be dominated by the LMA mode
435 ; in other cases, modes other than the LMA became dominant. We leave the nonlinear
436 modeling of LAWI, including the study on cessation of the growth, to future work.

5.2. Analogy with megacusps: growth rates and circulation patterns

437 Although the model results are given for a planar beach, LAWI is also found in the
438 presence of a shore-parallel bar (not shown). Thus, for intermediate morphological beach
439 state where crescentic bars and associated megacusp systems usually develop, the model

440 predicts LAWI. To survive in the finite amplitude domain, the LAWI must grow at a
441 rate comparable to that of co-existing instabilities. Our sensitivity studies indicate LAWI
442 growth rates to range from 10^{-6}s^{-1} (for a beach slope of 0.05) to 10^{-5}s^{-1} (for a beach
443 slope of 0.2). The typical generation time scale thus ranges from 1.5 to 11.5 days. These
444 time scales were obtained for shore-normal waves having a moderate wave height of 1.5
445 m and wave period of 8 s. A typical time scale for the LMA mode of crescentic bars is
446 several days [Damgaard et al., 2002; Garnier et al., 2010]. Thus, for specific beach slope
447 and wave conditions, the LMA shoreline instabilities have comparable initial growth rates
448 as those of crescentic bar patterns.

449 Computations for the idealized cases gives LAWI wavelengths of the same order of
450 magnitude as the observed spacing of crescentic bars and associated megacusps. The
451 distinction between these two kinds of instabilities is therefore difficult and the validation
452 of the presence of LAWI in a Rhythmic Bar and Beach morphological environment is not
453 straightforward. More generally, a proper validation of the present results would need
454 dataset of shoreline evolution, together with bathymetric, wave and current data, starting
455 from an initial longshore uniform beach. To our knowledge, such data do not exist.

456 Although we cannot validate the model results with wavelengths observed in the field,
457 it is possible to discuss whether the type of nearshore circulation linked to LAWI, that is,
458 a longshore sediment flux pointing toward the cusped feature at both sides, is realistic or
459 not in nature and in the framework of 2DH modeling. According to Komar [1998], both
460 types of longshore current patterns, either converging or diverging at a megacusp, are
461 observed in nature. Another example showing that this type of circulation is realistic is
462 the case of a submerged breakwater. Both observations and numerical modelling indicate

463 that if the breakwater is beyond the breaker line, the waves drive longshore currents that
464 converge at the lee of the breakwater to build a salient [Ranasinghe *et al.*, 2006]. This
465 converging type of circulation at a megacusp was also observed by *Haller et al.* [2002] in
466 laboratory experiments on barred beaches with rip channels. One of their six experimental
467 configurations may be quite close to a LAWI configuration. This configuration had the
468 largest average water depth at the bar crest and the smallest rip velocity at the rip neck,
469 such that, in addition to the rip current circulation, they found a secondary circulation
470 system near the shoreline, likely forced by the breaking of the larger waves that propagated
471 through the channel. As these waves are breaking close to the shoreline, they drove
472 longshore currents away from the rip channels into the shallowest area. This experiment
473 shows that breaking close to the shoreline counteracts the rip-induced circulation, leading
474 to current convergence in the shallowest area.

475 The studies of *Calvete et al.* [2005] and *Orzech et al.* [2011] give other elements to
476 investigate the plausibility of the LAWI mechanism, in rip channels configurations. For
477 the case of a barred-beach, *Calvete et al.* [2005] developed a 2DH linear stability model,
478 having a fixed shoreline, that describes the formation of rip channels from an initially
479 straight shore-parallel bar. For shore-normal waves, the circulation linked to rip channel
480 formation is offshore through the channels and onshore over the shoals or horns of the
481 developing crescentic bar as is clearly observed in nature (e.g. [MacMahan *et al.*, 2006]).
482 However, they also noticed small secondary circulation cells near the shoreline flowing in
483 the opposite direction, leading to presence of megacusp formed in front of the horns of
484 the crescentic bar; therefore, the shoreline undulations were out of phase (spatial phase-
485 lag of 180°) with the crescentic bars, meaning that the amplitude of the wave-refracted

486 terms should dominate the amplitude of the wave set-up terms (Eq. 2). The formation of
487 those megacusps was not part of the instability leading to the crescentic bar development
488 but was forced by the hydrodynamics associated with it. More importantly, the small
489 secondary circulation cells were essentially related to wave refraction: if wave refraction
490 from the model was eliminated, they did not develop. Thus, wave refraction by offshore
491 shoals (those of the crescentic bar in this case) can induce a circulation that may move
492 sediment toward a developing cusped feature. A recent study, based on both observation
493 (video images) and non-linear morphodynamic modeling [*Orzech et al.*, 2011] also showed
494 the occurrence of two types of megacusp (shoreward of the shoal or shoreward of the
495 rip), and the associated converging sediment fluxes toward the megacusps. This tends to
496 support our mechanism analysis of LAWI formation.

497 The similarity between LAWI and megacusps in both wavelength and growth time
498 is certainly intriguing given the fact that 1D-morfo is mainly based on the gradients
499 in longshore sediment transport and wave set-up induced sediment transport (damping
500 term), but neglects many surf zone processes like rip current circulation, which is known
501 to be essential to crescentic bar dynamics [*Calvete et al.*, 2005; *Garnier et al.*, 2008].
502 However, the analysis above tends to show that there could be configurations, where the
503 processes taken into account in 1D-morfo are dominant in the system, at the initial stage.
504 This could explain why similarities are observed with the various numerical experiments
505 done with more sophisticated models. Furthermore, we should keep in mind the fact that
506 the LAWI mechanism is not related to any longshore bar, and thus that short shoreline
507 sandwaves such as megacusps could develop without a bar, whereas it was thought that,
508 for barred beaches, short shoreline sandwaves develop due to surf zone sand bar variability.

6. Conclusions

509 A one-line linear stability model, which was initially created to describe the formation of
510 shoreline sandwaves under high-angle wave incidence, has revealed shoreline instabilities
511 for low to shore-normal wave incidence (LAWI). The most amplified mode has wavelengths
512 of ~ 500 m and characteristic growth time scales of a few days, which are smaller than
513 those of the high angle wave instabilities. Sensitivity analyses focusing on wave height,
514 wave incidence angle, beach slope, beach profile, model free parameters and the sediment
515 transport equation show that, for low to shore-normal wave incidence, instabilities develop
516 for sufficiently large beach slopes (e.g. 0.06) and for sufficiently small wave heights (smaller
517 than 2 m for a beach slope of 0.06).

518 The main process causing the instabilities for low to shore-normal wave incidence is wave
519 refraction on a shoal in the shoaling zone, which focuses wave fronts onshore of it, leading
520 to wave incidence induced sediment transport converging at the cusp. This effect strongly
521 increases with beach slope. The damping is due to three longshore transport components:
522 (1) that caused by shoreline orientation only (and not refraction), (2) that caused by
523 wave energy spreading (minor effect for low-angle wave incidence), (3) that caused by
524 wave height gradients (set-up). Whether LAWI develops or not depends on the balance
525 between these growing and damping terms. If this shoreline sand accumulation can feed
526 the initial shoal through cross-shore sediment transport, a positive feedback arises.

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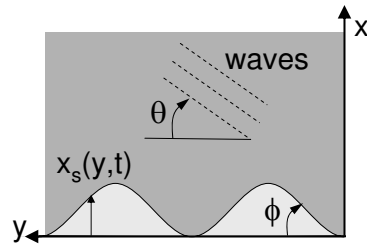


Figure 1. Sketch of the geometry and the variables. The angle between the wave fronts and the local shoreline is $\alpha = \theta - \phi$.

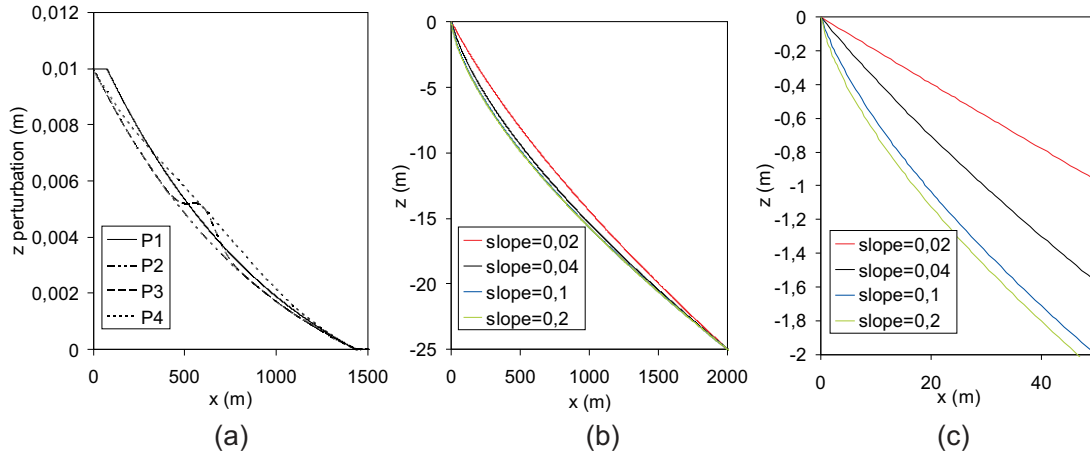


Figure 2. Bathymetric perturbations (a) and cross-shore Dean beach profile for a various beach slopes (b,c). P1-perturbation: constant in the surf zone and exponential decrease, P2-perturbation: exponential decrease, P3-perturbation: exponential decrease with a shoal in the shoaling zone, P4-perturbation: exponential decrease with a shoal in the surf and shoaling zones.

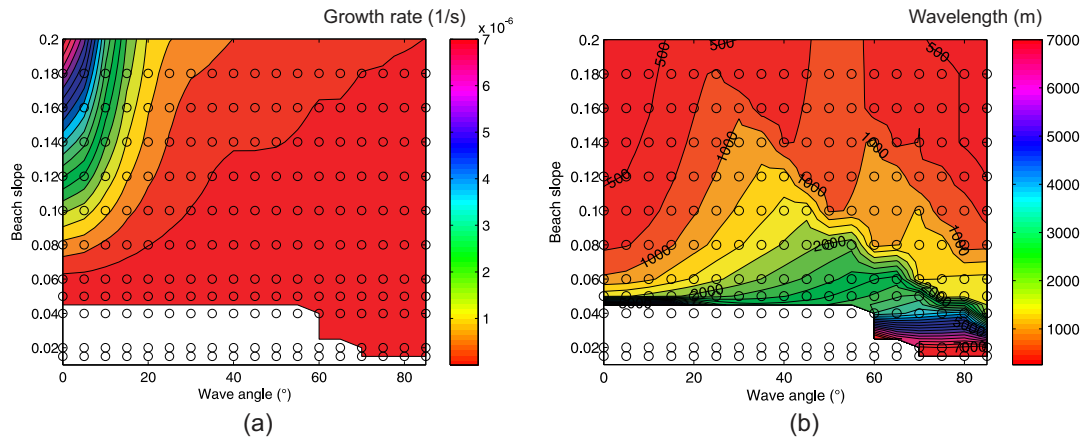


Figure 3. LMA (a) growth rate and (b) wavelength as a function of beach slope and angle of incidence. Circles indicate the 1D-morfo computations. In white: no growing perturbation. The model parameters are : $\mu = 0.15$, $r = 1$, P1-Perturbation and $xl=1410$ m for Dean profiles with $H_{rms} = 1.5$ m and $T_p = 8$ s at a water depth of 25 m.

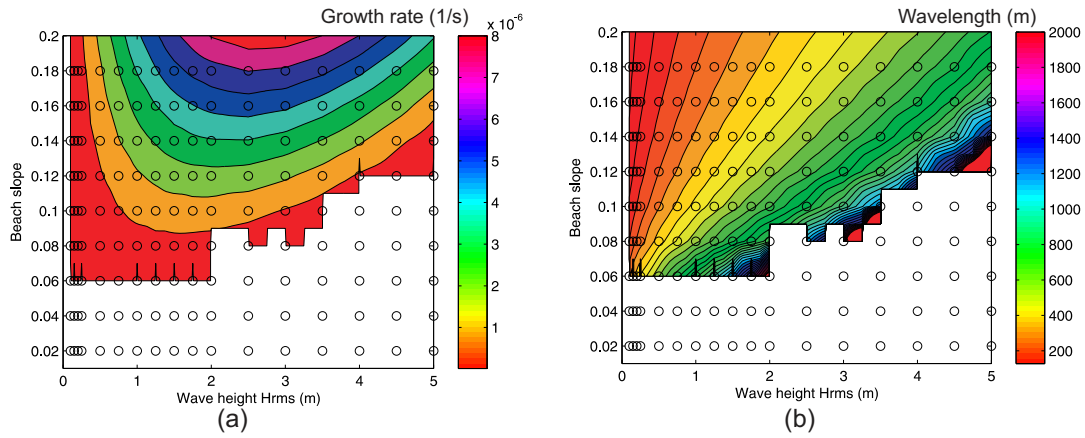


Figure 4. LMA (a) growth rate and (b) wavelength as a function of beach slope and wave height, for shore-normal waves. Circles indicate the 1D-morfo computations. In white: no growing perturbation. The model parameters are : $\mu = 0.15$, $r = 1$, P1-Perturbation and $xl=1410$ m for Dean profiles with $\theta = 0^\circ$ and $T_p = 8$ s at a water depth of 25 m.

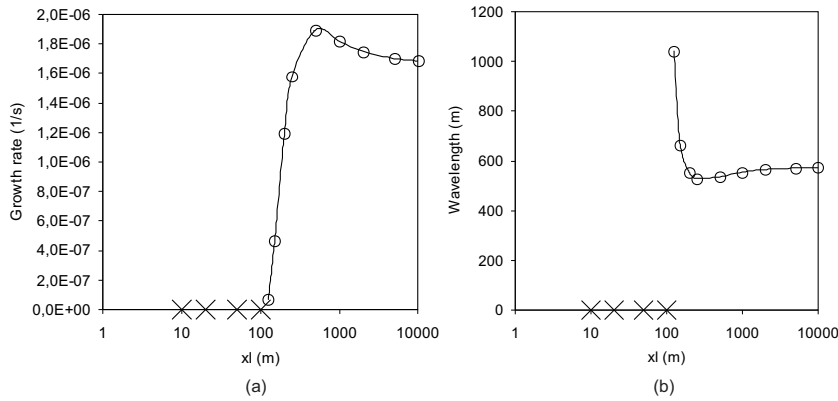


Figure 5. LMA mode (a) growth rate and (b) wavelength as a function of the shoreline perturbation length xl for a Dean profile with a beach slope of 0.1. Crosses on the xl axis ($10 \leq xl \leq 100$) indicate that there is no LMA mode for the given shoreline perturbation length.

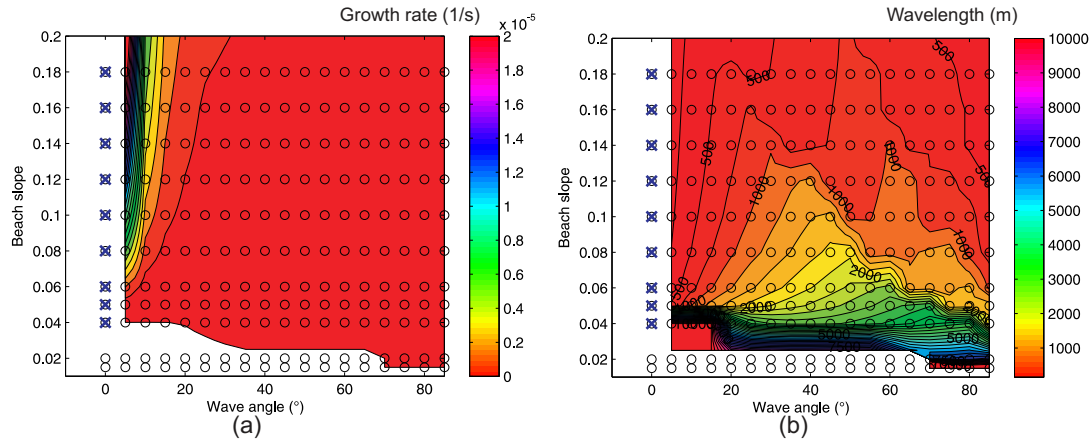


Figure 6. LMA (a) growth rate and (b) wavelength as function of beach slope and wave angle, for $r = 0$. Circles indicate the 1D-morfo computations. In white: no LMA mode. The symbol x indicates that, even if the growth rate was positive, there was a singularity at $\theta = 0^\circ$ (growth rate continuously increasing with decreasing wavelength), and therefore no LMA mode (see Figure 7).

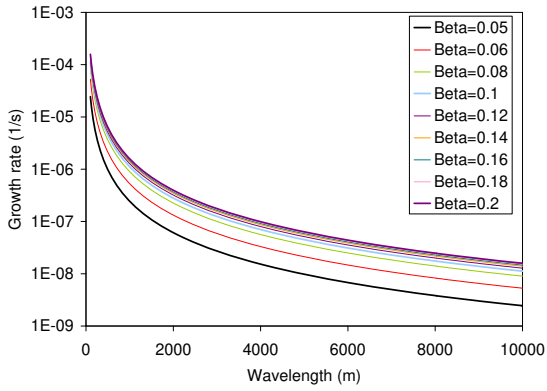


Figure 7. LMA growth rate versus wavelength for various beach slopes, using $r = 0$ and shore-normal waves. The shoreline is stable for a beach slope $\beta < 0.05$. The model parameters are : $\mu = 0.15$, P1-Perturbation and $xl=1410$ m for the Dean profile with $H_{rms} = 1.5$ m and $T_p = 8$ s at a water depth of 25 m.

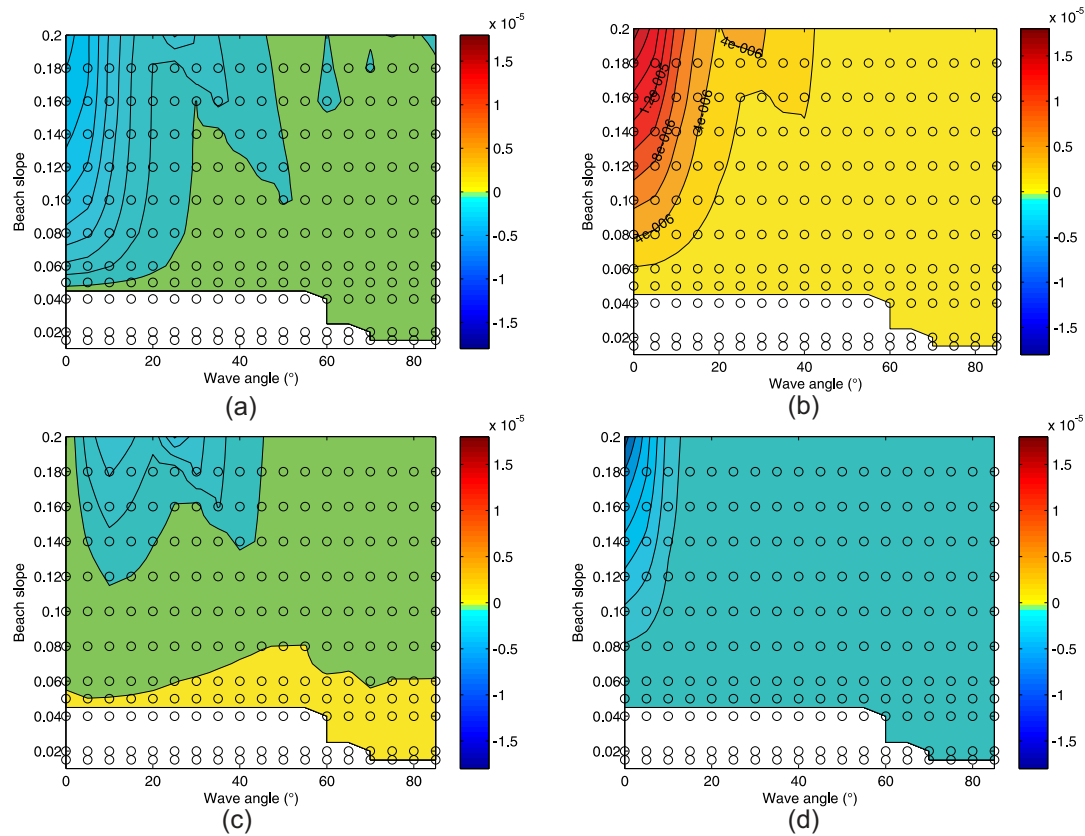


Figure 8. Growth rate components for the LMA mode as a function of beach slope and angle of incidence. Model parameters are: $H_{rms} = 1.5$ m, $T_p = 8$ s and cross-shore perturbation of type P1 with $x_l = 1410$ m. (a) σ_1 , (b) σ_2 , (c) σ_3 , (d) σ_4 . Circles indicate the 1D-morfo computations. In white: no LMA mode.

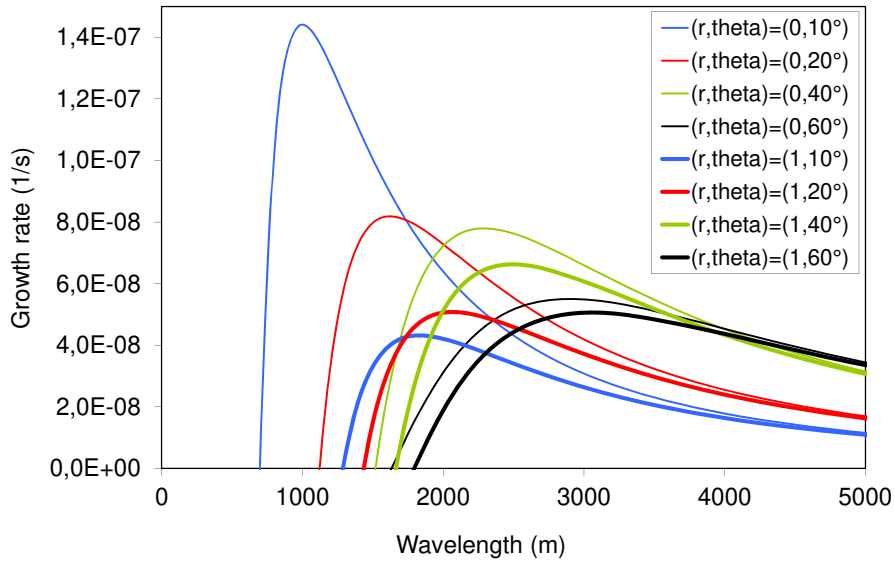


Figure 9. Growth rate versus wavelength for several combinations of r and wave incidence angle θ . The beach slope is 0.05.

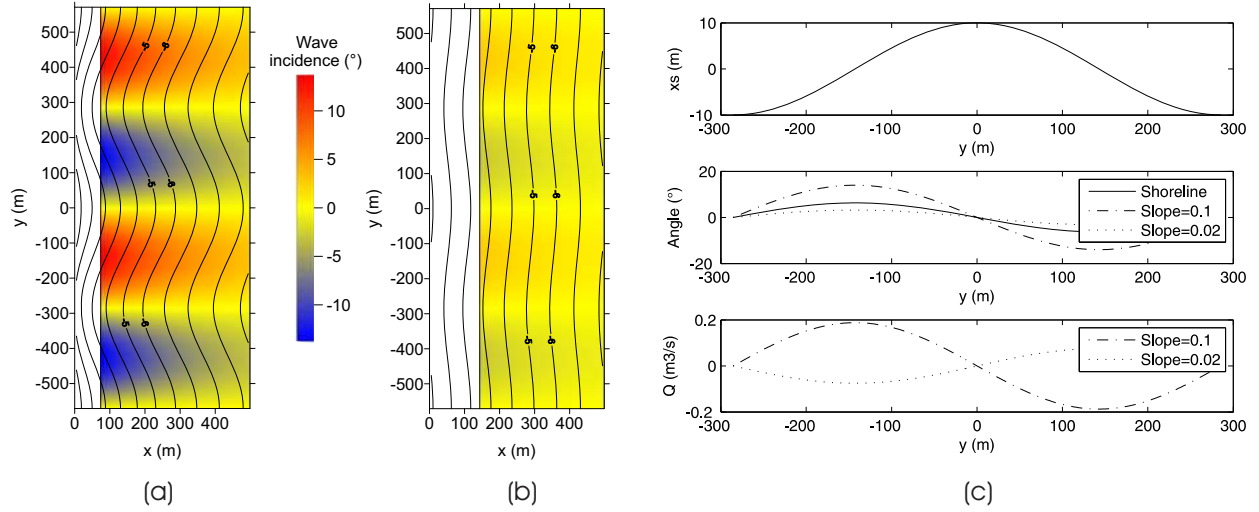


Figure 10. Model results for a perturbation wavelength of 571 m (LMA mode for a beach slope of 0.1), shore-normal wave incidence, and a shoreline wave amplitude of $a = 10$ m. (a) and (b) show the topographic contours and the refracted wave angle for beach slopes of 0.1 (a) and 0.02 (b). (c) shows the longshore profiles of (Top) the shoreline position, (Middle) the shoreline angle (solid line) and refracted wave angles and (Bottom) the sediment fluxes. Dashed-dotted lines, and dotted lines represent a beach slope of 0.1 and 0.02, respectively.

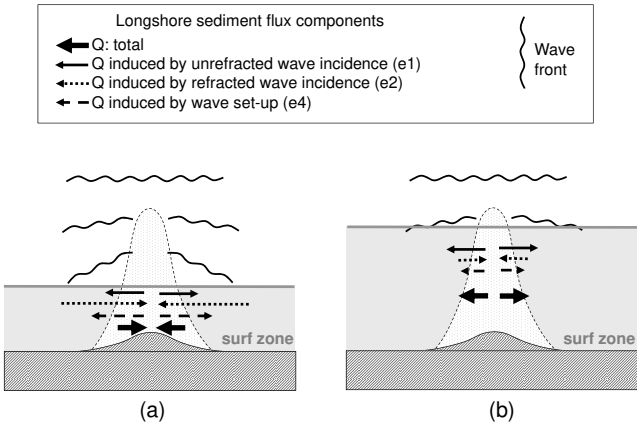


Figure 11. Sketch of the physical mechanisms causing LAWI. Sediment transport components induced by a shoal for unstable (a) and stable (b) situations, corresponding to a narrow and wide surf zone, respectively.