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Stabilized Radio-Frequency Transfer using Optical Phase Sensing and Actuation

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We describe and experimentally evaluate a stabilized radio-frequency transfer technique that employs optical phase sensing and optical phase actuation. This technique can be achieved by modifying existing stabilized optical frequency equipment and also exhibits advantages over previous stabilized radio-frequency transfer techniques in terms of size and complexity. We demonstrate the stabilized transfer of a 160 MHz signal over an 160 km fiber optical link, achieving an Allan deviation of 9.7×10^{-12} Hz/Hz at 1 s of integration, and 3.9×10^{-14} Hz/Hz at 1000 s. This technique is being considered for application to the Square Kilometre Array SKA1-low radio telescope.

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Fiber-optic frequency transfer networks, such as the European NEAT-FT [1 - 3] and the Beijing regional time and frequency network [4, 5], are now being rolled-out on national and international scales, driven by cutting-edge research in metrology and other physical sciences including the distant comparison of optical atomic clocks, high-precision remote spectroscopy, radio astronomy, geodesy, and tests of fundamental physics [1, 6, 7]. The NEAT-FT network, and other long-distance frequency comparison experiments [2, 8, 9], have typically transmitted stabilized optical-frequency signals because of their superior fractional frequency stability over optically-disseminated radio-frequency (RF) and microwave (MW) signals [1, 6]. However, many applications of stabilized frequency transfer in science, commerce, and industry require RF transmissions [7], and will benefit even at the expense of inferior stability performance compared to optical frequency transfer. These applications cannot be interfaced directly with optical frequencies, and while optical-to-RF conversion methods

exist [10, 11, 12], the required equipment remains expensive and complex.

Stabilized RF and MW dissemination systems typically require bulky group-delay actuators (thermally controlled fiber spools) [13, 14] or a separate remote-site transmission system operating in a phase-locked-loop [15, 16], and are not compatible with existing optical frequency transfer infrastructure such as that demonstrated in [2], [8] and [9].

In this paper, we present a modification of the technique reported in [17] to create a simple and compact stabilized RF transfer system that uses only the optical and electronic components used in standard stabilized optical transfer systems [18], to enable existing optical transfer infrastructure to readily be converted to provide stabilized RF transfer.

As shown in Figure 1, an optical signal with frequency ν_L , is generated by a laser located at the **Local Site**. Just as is the case in standard stabilized optical transfer techniques [18], the optical signal enters an imbalanced Michelson interferometer (MI) via an optical isolator (to prevent reflections returning to the laser). The short arm of the MI provides the physical reference for the optical phase sensing. The optical reference signal ν_{ref} at the photodetector is

$$\nu_{\text{ref}} = \nu_L + \frac{1}{2\pi} (2\Delta\phi_{\text{MI}}), \quad (1)$$

where $\Delta\phi_{\text{MI}}$ is the undesirable phase noise picked up by the optical signals passing through the MI reference arm.

In the long arm of the MI the optical signal is then split into two arms of a Mach-Zehnder interferometer (MZI), each arm of which contains an acousto-optic modulator (AOM).

In the case shown in Figure 1, the servo AOM, with frequency $\nu_{A-\text{srv}}$, is shown at the bottom arm; and a local 'anti-reflection' AOM, with frequency $\nu_{A-\text{lar}}$, is shown in the top arm. (Note — the anti-reflection AOM is not essential for this technique. It serves to provide reflection mitigation as well as increase the frequency separation.) A combination of up- and down-shifting AOMs gives the greatest RF separation, but any unique combination can be used.

The servo AOM is used to apply the frequency correction Δv_{A-srv} for the stabilization system. Frequency changes due to phase fluctuations in the optical path length in the arms of the MZI are represented by $\Delta\dot{\phi}_{MZI,1}$ for the top path, and $\Delta\dot{\phi}_{MZI,2}$ for the bottom path.

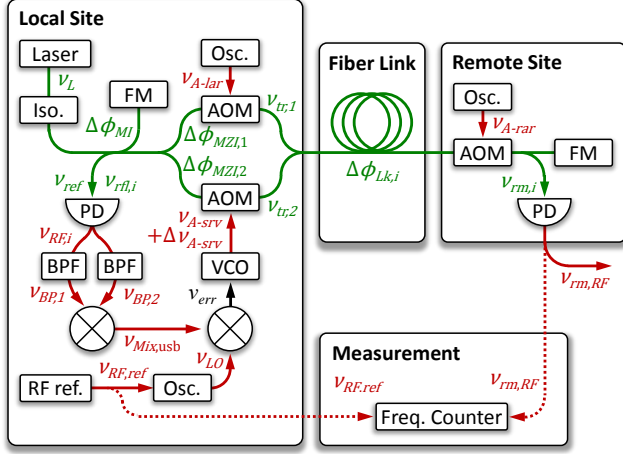


Fig. 1. Schematic diagram of our stabilized radio-frequency transfer technique. Optical-frequency signals are shown in green; radio-frequency signals in red; and the error signal in black. AOM acousto-optic modulator; Osc. Oscillator; Iso. optical isolator; FM Faraday mirror; PD photodetector; VCO voltage-controlled oscillator; BPF bandpass filter; and RF ref. radio-frequency reference.

At the output of the MZI, the two optical signals to be transmitted are now:

$$v_{tr,1} = v_L + v_{A-lar} + \frac{1}{2\pi} \Delta\dot{\phi}_{MZI,1}, \text{ and} \quad (2)$$

$$v_{tr,2} = v_L + (1 + \Delta)v_{A-srv} + \frac{1}{2\pi} \Delta\dot{\phi}_{MZI,2}. \quad (3)$$

As the two optical signals pass through the link, they pick-up frequency fluctuations, $\Delta\dot{\phi}_{Lk,i}$, due to optical path length changes in the link that are unique to their specific transmitted frequency.

At the remote site, the two optical signals pass through a remote anti-reflection AOM (again, this AOM is not essential for the technique) to give:

$$v_{rm,1} = v_L + v_{A-lar} + v_{A-rar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{Lk,1}), \quad (4)$$

and

$$v_{rm,2} = v_L + (1 + \Delta)v_{A-srv} + v_{A-rar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,2} + \Delta\dot{\phi}_{Lk,2}). \quad (5)$$

At the **Remote Site**, the signal is split with one part going to a photodetector. The electronic signal $v_{rm,e}$ from the beat of $v_{rm,1}$ and $v_{rm,2}$ is

$$v_{rm,e} = \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,2} - \Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{Lk,2} - \Delta\dot{\phi}_{Lk,1}) + (1 + \Delta)v_{A-srv} - v_{A-lar}. \quad (6)$$

A mirror reflects the two optical signals back through the link to the **Local Site** where they then pass back through the MZI. The

returning reflected optical signals reaching the photodetector for the MI are then:

$$v_{rf,1} = v_L + 2 \left(v_{A-lar} + v_{A-rar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{Lk,1}) \right), \quad (7)$$

$$v_{rf,2} = v_L + 2 \left((1 + \Delta)v_{A-srv} + v_{A-rar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,2} + \Delta\dot{\phi}_{Lk,2}) \right), \quad (8)$$

and

$$v_{rf,3j} = v_L + (1 + \Delta)v_{A-srv} + v_{A-lar} + 2v_{A-rar} + 2\Delta\dot{\phi}_{Lk,j} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{MZI,2}), \quad (9)$$

where j is 1 or 2 corresponding to the signals on the link. The three signals are at unique frequencies as long as v_{A-srv} does not equal v_{A-lar} . At the photodetector these optical frequencies mix with v_{ref} to give the following RF signals.

$$v_{RF,1} = 2 \left(v_{A-lar} + v_{A-rar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{Lk,1} - \Delta\dot{\phi}_{MI}) \right), \quad (10)$$

$$v_{RF,2} = 2 \left((1 + \Delta)v_{A-srv} + v_{A-rar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,2} + \Delta\dot{\phi}_{Lk,2} - \Delta\dot{\phi}_{MI}) \right), \quad (11)$$

and

$$v_{RF,3j} = (1 + \Delta)v_{A-srv} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{MZI,2} + 2\Delta\dot{\phi}_{Lk,j}) + v_{A-lar} + 2v_{A-rar}, \quad (12)$$

as well as intermodulation signals. In the electronic domain, the signals are split and bandpass filtered. The RF bandpass filter values are set to $v_{BP,1} = 2(v_{A-lar} + v_{A-rar})$ and $v_{BP,2} = 2(v_{A-srv} + v_{A-rar})$.

The bandpass filters eliminate $v_{RF,3j}$, the intermodulation signals, and the opposing RF signal. The filtered signals are then mixed together, producing the following upper- and lower-sideband frequency products:

$$v_{Mix,1} = 2 \left((1 + \Delta)v_{A-srv} + v_{A-lar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{MZI,2} + \Delta\dot{\phi}_{Lk,1} + \Delta\dot{\phi}_{Lk,2} - 2\Delta\dot{\phi}_{MI}) \right), \quad (13)$$

and

$$v_{Mix,2} = 2 \left((1 + \Delta)v_{A-srv} - v_{A-lar} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,1} - \Delta\dot{\phi}_{MZI,2} + \Delta\dot{\phi}_{Lk,1} - \Delta\dot{\phi}_{Lk,2}) \right). \quad (14)$$

Note that in $v_{Mix,2}$ the frequency perturbation $\Delta\dot{\phi}_{MI}$ cancels out. A bandpass filter with the center frequency at $2 \times (v_{A-srv} - v_{A-lar})$ is used to reject $v_{Mix,1}$, before mixing $v_{Mix,2}$ with the servo local oscillator v_{LO} also set at $v_{LO} = 2(v_{A-srv} - v_{A-lar})$ to produce an error signal of

$$v_{err} = 2 \left(v_{A-srv} + \frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,2} - \Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{Lk,2} - \Delta\dot{\phi}_{Lk,1}) \right). \quad (15)$$

When the servo is engaged, the error signal is driven to zero, $v_{err} = 0$, so:

$$v_{A-srv} = -\frac{1}{2\pi} (\Delta\dot{\phi}_{MZI,2} - \Delta\dot{\phi}_{MZI,1} + \Delta\dot{\phi}_{Lk,2} - \Delta\dot{\phi}_{Lk,1}). \quad (16)$$

Substituting this into equation 6 gives:

$$\nu_{\text{rm,e*}} = \nu_{A\text{-srv}} - \nu_{A\text{-lar}}, \quad (17)$$

where $\nu_{\text{rm,e*}}$ is the electronic remote signal with the servo engaged.

We describe an experiment using 160 MHz RF transfer, with all optical elements fiberized. An NKT Photonics Koheras BASIK X15 laser (spectral linewidth <100 Hz) situated at the **Local Site**, and operating at a wavelength of 1552 nm, produced a laser signal $\nu_L = 193$ THz. The AOMs were Gooch & Housego with $\nu_{A\text{-srv}} = +75$ MHz, $\nu_{A\text{-lar}} = -85$ MHz, and $\nu_{A\text{-rar}} = 40$ MHz. All fiber in the **Local Site** was polarization maintaining to ensure the optical power output of the MZI remains maximized. The signal was transmitted through AARNet-managed metropolitan optical fiber networks 160 km in length, with two IDIL Fibres Optiques bi-directional optical amplifiers used to boost the signal strength as required.

Menlo FPD-510 photodetectors were used for the optical-to-electronic conversion in both the **Local Site** and **Remote Site**. Faraday mirrors were used at the ends of the two arms of the MI to ensure the signals mixing at the transmitter side photodetector were aligned in polarization.

The combination of AOM frequencies resulted in the following electronic signals within the servo electronics; $\nu_{\text{RF},1} = 90$ MHz, $\nu_{\text{RF},2} = 230$ MHz, and $\nu_{\text{RF},3} = 70$ MHz. The mixer frequencies are $\nu_{\text{Mix},1} = 140$ MHz and $\nu_{\text{Mix},2} = 320$ MHz. After filtering, $\nu_{\text{Mix},2}$ was mixed with a 320 MHz LO frequency.

Both the **Local Site** and **Remote Site** were co-located in the same laboratory, permitting an independent measure of the transfer stability. The 160 MHz received signal was terminated on a Π -type Microsemi 5125A phase noise test set to produce an Allan deviation estimate of the fractional frequency stability.

Figure 2 shows the Allan deviation measured for the stabilized (filled blue circles, solid lines) and unstabilized (open blue circles, dashed lines) 160 MHz signal transmitted over the 160 km link.

Figure 2 shows that the stabilization system produces an Allan deviation of 9.7×10^{-12} Hz/Hz at 1 s of integration, dropping to 3.9×10^{-14} Hz/Hz at 1000 s integration time.

We have described and experimentally demonstrated the function of a stabilized radio-frequency transfer technique. This technique exploits several advantages of optical phase-sensing and optical phase-actuation over other radio- and microwave-frequency transfer techniques.

The use of AOMs for optical phase-actuation allows the **Local Site** transmitter units to have a more compact construction than systems using fiber stretchers or thermal spools. AOMs also provide an infinite feedback range, avoiding any potential need for integrator-reset or range-limit monitoring circuits. The rapid response of AOMs allows for better optimization of the servo gains for short links where the feedback bandwidth is limited by electronic delay rather than the light round-trip time.

This technique actively suppresses phase noise introduced in the **Local Site** MZI as well as the transmission link. Along with the simplicity of the remote site optical and electronic components, this makes the system very resistant to the effects of environmental perturbations (such as temperature variation or vibration) on the system hardware.

By using AOMs to generate shifts of the optical frequency at the local and remote sites, this technique avoids the need to use additional lasers at the remote sites to circumvent the effects of unwanted reflections on the transmission link. This reduces the

complexity and cost of the system. In addition, on links where unwanted reflections are minimal, it is possible to remove an anti-reflection AOM from the stabilized transfer system (either the remote AOM, or the local AOM), to further reduce the cost and complexity. The local and the remote anti-reflection AOMs mitigate unwanted reflections by generating unique RF frequencies at the photodetectors. Sensible choices of AOM frequencies allow this to happen without overlapping with signals of interest.

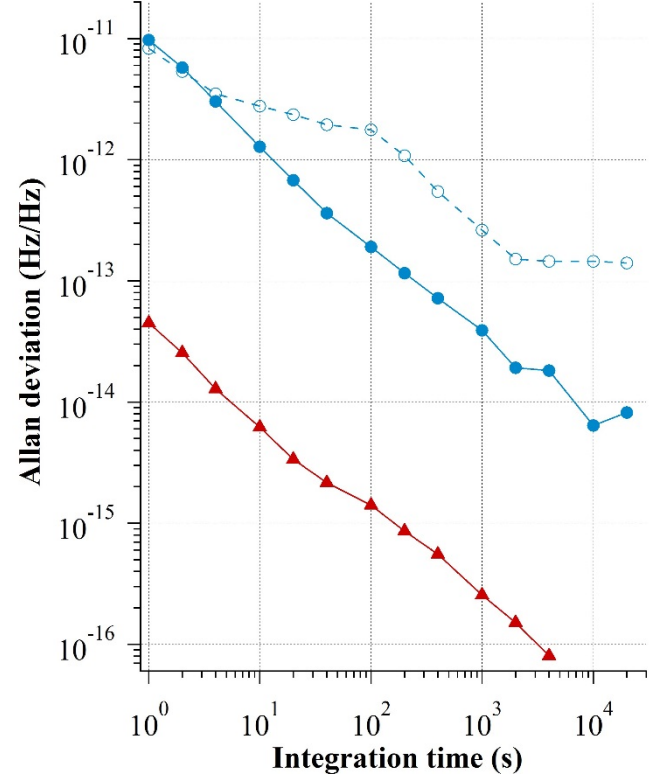


Fig. 2. Allan deviation of 160 MHz transfer over 160 km of metropolitan fiber. Stabilization servo engaged — filled blue circles, solid line. Stabilization disengaged — open blue circles, dashed line. Electronic noise floor of the phase-noise test set — filled red triangles, solid line.

The use of Faraday mirrors at the end of the MI arms ensures that the maximum signal is available at the photodetectors without the need for any initial polarization alignment or ongoing polarization control or polarization scrambling.

Because the RF signal being transmitted is the product of only two optical signals, and not three as is the case in standard intensity modulation, the system avoids potential problems of signal fading that is caused by the destructive interference of the modulation sidebands at specific intervals along the link. This also means that the transmission frequency can be varied arbitrarily without needing to consider the link length. The techniques employed mean that the system does not require the use of specialized fiber such as dispersion compensating fiber or polarization maintaining fiber. Furthermore, the technique is compatible with data transmission on the same link, allowing the

system to make use of active telecommunications links if the non-bi-directional components of the link are bypassed as in [6] and [19]. Bi-directional optical amplifiers can be used to simply extend the range of the system without the use of signal regeneration stations at certain points along the link.

The technique of splitting and frequency shifting the signal from a single laser source is also considerably simpler than offset-locking a master and slave laser, however, the range of possible transmission frequencies is limited to the RF domain (that is, < 1 GHz) by the practical limitations of existing AOM technology.

While testing other transmission frequencies, we found that when the system is configured correctly — that is, optical and electronic signal levels are optimized and adequate filters are employed — the absolute frequency stability of the transmitted signal is very similar regardless of the transmission frequency. Therefore, the fractional frequency stability can be improved by transmitting higher transmission frequencies. The largest frequency shifts produced by commercially available AOMs at the time of publication are +/-110 MHz. Including additional passive AOMs can further increase the transmission frequency. However, due to the optical power loss of the AOMs, it is not currently practical to achieve stabilized MW transmission (> 1 GHz) using the technique presented here. Stabilized MW transmissions using optical phase-sensing and actuation require the more extensive modifications presented in [17].

This stabilized RF transfer technique is one of two being considered for selection as the phase-synchronization system for the Square Kilometre Array SKA1-low radio telescope [20, 21].

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