# Simulation and Experiments of a *W*-Band Extended Interaction Oscillator Based on a Pseudospark-Sourced Electron Beam

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Abstract—This paper presents the first experimental results of an extended interaction oscillator (EIO) based on a pseudospark-sourced electron beam, which produced a peak output power over 38 W at W-band. The advantages of the newly developed device are: 1) transport of the electron beam by the positive-ion focusing channel without the need of an external magnetic field and 2) high interaction impedance and high gain per unit length of the EIO circuit. The experimental results agree well with the 3-D particle-in-cell simulations.

*Index Terms*—Extended interaction oscillator (EIO), pseudospark-sourced electron beam, vacuum electronics.

## I. INTRODUCTION

**P**SEUDOSPARK discharge systems based on the hollow cathode can produce axially symmetric-pulsed electron beams along the axis of the cathode cavity [1]–[3]. The production of higher current density electron beams, compared with thermionic cathodes, from pseudospark discharges has been convincingly demonstrated [4]. This property meets the urgent need of very high current density electron beams in the generation of coherent millimeter-wave and tera-hertz wave radiation.

At millimeter and submillimeter wavelengths (terahertz frequencies), the achievable output power of the conventional O-type vacuum electronic devices is greatly limited by the electron beam current that can transport through the device at a particular voltage. The current density of a pseudospark-sourced electron beam is of the order of hundreds of A/cm<sup>2</sup> or higher [5], [6], which enables a wide range of applications in generating millimeter-wave and submillimeter-wave radiation [7]. Yin *et al.* [8] demonstrated that the electron beam pulses with a 3-mm diameter can



Fig. 1. Experimental setup of the *W*-band EIO based on a pseudospark-sourced electron beam and the schematic drawing of the experiment.

be transported distances up to 20 cm without a guiding magnetic field. To work with the pseudospark-sourced pulsed electron beam, automatic optimization techniques can be used to shorten the klystron interaction structure [9]. An alternative technique is to use the extended interaction oscillator (EIO) circuit, which has the advantages of high interaction impedance and high gain per unit length [10].

A W-band (75–110 GHz) EIO circuit operated in the  $2\pi$  mode was selected for our first experiment because of its shorter interaction length as compared with a backward wave oscillator. The beam voltage was designed to be centered at 30.5 kV, which is suitable for a four-gap pseudospark discharge. This newly developed device combines the merit of a short interaction circuit in the EIO and the high current density property of the pseudospark-sourced electron beam to generate W-band coherent radiation. The design and optimization of the W-band EIO with a pseudospark-sourced electron beam has been carried out. Experimental results show that with a 35-kV discharge voltage, the oscillator produced W-band microwave radiation pulses with a 38-W peak power and 20-ns duration, which agrees well with the 3-D particle-in-cell (PIC) simulations using MAGIC.

A photograph of the *W*-band oscillator based on a pseudospark-sourced electron beam and the EIO circuit, which includes a schematic drawing of the experiment, is shown in Fig. 1. It does not need an external focusing magnetic field and is capable of operating in a high repetition rate (up to a few kilohertz) [11]. From a review of the literature, this is the first experiment of an EIO based on a pseudospark-sourced

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Fig. 2. Layout of the EIO circuit.



Fig. 3. Dispersion curve of the EIO circuit.

electron beam. It provides a compact and affordable way to generate tens of watts in *W*-band.

#### II. CIRCUIT DESIGN AND FABRICATION

## A. Circuit Design

The EIO operates at the  $2\pi$  mode, and the number of the slots was optimized to achieve efficient circuit impedance. The layout of the EIO circuit is shown in Fig. 2. The circuit consists of identical nine-slot slow-wave structures that are strongly coupled by coupling cavities on both sides. The two coupling cavities (up and down) form the extended resonant cavity of the EIO circuit. The power is extracted out through a standard WR-10 waveguide attached to one of the cavities through circular apertures sized to provide the optimum  $Q_e$ , which defines the ratio between the stored energy in the cavity at stable resonant conditions and the output power (with a perfect matched load) in one period. A 0.5-mm diameter beam tunnel passes through the center of the slots and intersects with the slow-wave structure. The total length of this circuit is 10 mm, and there is no external magnetic field.

The dispersion curve of the EIO circuit, in synchronism with a 30.5-kV beam, is shown in Fig. 3 (solid line). The velocity of the electron beam (or the beam energy) was chosen, so that the time interval of the electron travels from one slot to the adjacent slot is equal to the period of the electromagnetic wave supported by the slow-wave structure, therefore ensuring an efficient interaction between the beam and the interaction circuit.

Through optimizing the dimensions of the coupling cavity, slot, and coupling hole, the maximum interaction impedance (R/Q) of 41.6  $\Omega$  was achieved. The voltage difference between the undesirable modes  $(2\pi + 1 \mod)$  and



Fig. 4. Contour plots of the electric field component Ez at x = 0 and z = 0 planes, and the field strength along the *z*- and *y*-directions.

 $(2\pi - 1 \mod)$  was maximized to about 6.3 kV, as shown in Fig. 3. The frequencies of the  $2\pi$  and  $2\pi - 1$  modes are 93.8 and 94.6 GHz, respectively.

### **B.** PIC Simulation

The PIC codes MAGIC 3-D [12] and CST Particle Studio [13] were used to investigate the behavior of the EIO and to optimize its performance. In the simulations, a dc beam with 30.5-keV energy was injected into the interaction circuit. The beam diameter was 0.5 mm, and the current density was assumed to be  $\sim$ 500 A/cm<sup>2</sup> giving a total beam current of 950 mA. An axial magnetic field of 0.4 T was applied for beam focusing. When the beam–wave synchronous condition is satisfied, our simulation showed that the oscillation could build up and power be extracted out from the output structure.

The oscillation could become stable about 11 ns after the beam was injected into the circuit. A contour plot of the electric field component Ez at the x = 0 and z = 0 planes, and the electric field strength along the z- and y-directions are shown in Fig. 4. The top two diagrams in Fig. 4 show the electric field strength along the axis of the beam tunnel (z-direction) and along the center of the output waveguide (y-direction). The strong field in the center slot allows the  $2\pi$  mode to have sufficient coupling to the output waveguide located in the center of the upper coupling cavity. The electric field strength ratio between the center slot and the others can be adjusted by changing the length of the coupling cavity.

Fig. 5(a) shows the phase space plot of electrons in Z-Pz space at 11 ns, and Fig. 5(b) shows the trajectory of the electrons in the zy plane. Pz is the normalized electron momentum  $\gamma v_e$ . Because of the interaction between the circuit and the electrons, some electrons lose their energy to the electromagnetic field. Fig. 6 gives the time-dependent output power at the output waveguide. The relations between the beam voltages to the output power and oscillation startup time were simulated and are shown in Fig. 7. The fast falling edges of the output power at 34 kV are due to the change of the operating mode from  $2\pi$  to  $2\pi - 1$  mode (refer to Fig. 3). When operating in the  $2\pi - 1$  mode,  $Q_0$ , which defines the ratio between the stored energy in the cavity at stable resonant conditions and the power loss in the cavity in one period, would decrease, and  $Q_e$  would increase; this would lower the



Fig. 5. (a) Phase space of the electrons. (b) Beam trajectory in the zy plane.



Fig. 6. Time-dependent output power at the output waveguide.



Fig. 7. Output power and oscillation startup time versus the beam voltage.

interaction efficiency as well as the output power dramatically. With the decrease in the voltage, the change in the operating mode from  $2\pi$  to  $2\pi + 1$  mode would also cause the output power to become zero at 27 kV. The simulated operating voltage region of the  $2\pi$  mode in this EIO is 5.5 kV, which is in excellent agreement with what was estimated from the dispersion curve (6.3 kV).

The electron beam from the pseudospark discharge is usually very stable, especially when no beam-wave interaction exists in the system and the working gas was fed into the system from the anode side at a very slow rate ( $\sim$ 1 mtorr/s). A typical electron beam pulse measured immediately after the anode, which had an aperture diameter of 0.6 mm, is



Fig. 8. Temporal evolution of the electron beam produced from a four-gap pseudospark discharge.



Fig. 9. (a) Beam voltage and (b) output power as a function of time.

shown in Fig. 8. From this measurement, it was estimated that the beam current at the beginning of the interaction region was 950 mA.

To reduce the complexity of the simulation, a stable beam current and a time-varying beam voltage, as shown in Fig. 9(a), were used to simulate the beam-wave interaction in the EIO circuit [14]. To reduce the computation time, the self-focusing of the beam in the ion channel was not included in the simulation, as well as the plasma generated by the pseudospark discharge. Instead, an axial magnetic field of 0.4 T was applied to guide the electron beam. Typically, for the full discharge process, it takes  $\sim$ 30–100 ns when the voltage changed from the applied 34 to 0 kV. The voltage change rate was  $\sim 1$  kV/ns and can be varied by adjusting the capacitance of the external capacitor  $C_{\text{ext}}$  used to maintain the discharge. When the voltage of the pseudospark beam changed from 34 to 0 kV in 100 ns, an output power of 5.6 kW with a full-width at half-maximum of 20 ns was predicted from the simulation and is shown in Fig. 9(b). The time duration that output power is generated is dependent on the voltage range of the EIO.

# C. Fabrication and Cold Test

The whole EIO circuit was divided into three parts and fabricated individually, as shown in Fig. 10. The coupling



Fig. 10. Left: three parts of the circuit. Right: assembled EIO circuit.



Fig. 11. Millimeter-wave measurement setup and measurement result.

cavities with and without the output structure were manufactured by a computer numerical control machine at the University of Strathclyde. The slow-wave structure was manufactured by wire erosion technology. The three parts were then connected together to form the EIO circuit with millimeterwave measurements carried out using an Anritsu ME7808B (75-110 GHz) vector network analyzer (VNA). A photograph of the millimeter-wave measurement setup and the measured  $S_{11}$  parameters is shown in Fig. 11. The center frequency of the circuit is 93.8 GHz, and the 3-dB bandwidth is 275 MHz. The VNA millimeter-wave measurement result agrees well with the CST MWS simulations when assuming the effective conductivity of the copper to be 75% of the ideal value  $(5.8 \times 10^7 \text{ S/m})$ . The beam tunnel is in the middle of the slowwave structure; therefore, its alignment tolerance is determined by the manufacturing process that avoids further assembly tolerance.

#### **III. EXPERIMENTAL RESULTS AND ANALYSIS**

Experimental measurement of the W-band EIO based on the pseudospark-sourced electron beam was carried out at the University of Strathclyde. A four-gap pseudospark discharge chamber, which can hold off a discharge voltage up to 40 kV, was used. The discharge voltage swept from 38 to 25 kV to achieve the maximum output power. Two W-band horns, one for the output from the EIO and the second horn for the



Fig. 12. Typical test results of the voltage and the microwave pulse.

microwave detector, were used. The two horns are positioned at a distance of 20 cm. The microwave radiation pulse was measured by a *W*-band crystal detector. A typical measurement of the voltage and the microwave signal are shown in Fig. 12. The duration of the microwave waveform agrees well with the simulation result, as shown in Fig. 9(b).

To estimate the radiation power, the crystal detector was calibrated twice using a 1.5-W, 90-97-GHz solid-state source. First, the detector was connected to the solid-state source through an attenuator to measure the response curve at different input powers. The other calibration used dual horns with a separation distance of 20 mm (the same distance used in the EIO experiment). One horn was connected to the solidstate source, and the other was connected with the crystal detector. The response of the detector at different output powers was recorded. From the calibration data, the direct ratio of the radiation power to the amplitude of the crystal detector was obtained. The peak power of the radiation was found to be  $\sim$ 38 W. The output frequency was examined using a high-pass waveguide cutoff filter, which operated above 92 GHz. The radiation frequency was found to be above 92 GHz, which also coincides with the VNA millimeter-wave measurement result of 93.8 GHz.

A few factors may cause the measured microwave power to be less than the simulation results, such as the beam current, beam quality, and output circuit properties. While the output circuit might cause a substantial loss of the generated radiation due to  $Q_e$  and ohmic losses, the effects due to the discrepancies in electron beam parameters might contribute much more in our case. For example, in the PIC simulation, an ideal beam of zero energy and velocity spreads was used to interact with the circuit, while the pseduospark-generated electron beam may have a relatively large energy spread due to the scattering of the electrons with the plasma and the collision with the neutral gas. In addition, due to the beam instability accompanying the beam-wave interaction in the plasma, it is possible that a significant part of electron beam might be lost in the interaction region. In effect, the loss of the beam could be evaluated by a reduction of the beam current density. The impact of these factors are difficult to evaluate exactly; however, the effect of the current density and the axial velocity spread  $(\Delta v_7/v_7)$  on the output power were evaluated through the PIC simulation, and are plotted in Fig. 13. It was found that an increase in the axial velocity spread affects



Fig. 13. Relation between the current density to the output power and the axial velocity spread.

the interaction efficiency adversely due to reduced overall synchronism between the beam and the wave. Fig. 13 shows that the combined effects from the axial velocity spread and beam loss in the interaction are possible reasons of reduced output power in the experiment. Future experiments will add an inline beam diagnostic at the end of the interaction region to measure the beam current at the end of the interaction region. This would give more accurate information on the velocity spread of the beam.

#### IV. CONCLUSION AND DISCUSSION

The pseudospark-sourced electron beam, which is selffocused by the positive-ion channel generated from the pseudospark discharge process, was successfully used to drive a *W*-band EIO circuit to generate coherent radiation. The background unmagnetized plasma can be considered as a dielectric media with a dielectric constant of  $\varepsilon_r = 1 - \omega_{pe}^2/\omega^2$ . As the operating frequency is far away from the plasma frequency, the plasma would have negligible effect on the output power of the EIO. However, the plasma would upshift the output frequency slightly, and from the dispersion equation, it is ~10%. The measurement of the exact frequency with a mixer is scheduled for a future experiment.

There are two possible ways to increase the output power of this device. The first one to use a beam voltage with slower decrease, this will allow more electrons to be located in the oscillating voltage range over relatively longer time, thus increasing the output power of the device. In the pseudospark discharge, the discharge duration can be adjusted by using different external capacitances. The second way is to minimize the energy spread of the pseudospark-sourced electron beam, such as using the postacceleration technique [4] which can reduce the axial velocity spread of the pseudospark-sourced electron beam to  $\sim 5\%$ .

This experiment demonstrates an original type of compact and affordable radiation source for the generation of millimeter-wave and submillimeter-wave radiation. The pseudospark-sourced electron beam has higher current density than a thermionic electron beam, and the beam formation and focusing does not require an external magnetic field. It is an excellent affordable, compact, and robust pulsed electron beam source to drive an EIO circuit operating at higher frequencies with reasonably high radiation power.

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