

Solar-pumped fiber laser using a solid-state luminescent solar collector

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Abstract: We have developed a fully planar solar-pumped fiber laser using a solid-state luminescent solar collector (LSC). This laser does not use any focusing device, such as a lens or mirror; thus, it can lase without tracking the sun. Our developed device with an aperture of 30 cm emits 15 mW, corresponding to an optical-to-optical conversion efficiency of 0.023% and a collection efficiency of 0.21 W/m². A 12-fold improvement over a previously developed liquid LSC is achieved by combining the total internal reflection of the solid-state LSC with dielectric multilayer mirrors. The observed laser power is in good agreement with that predicted via numerical simulation, demonstrating the effectiveness of our proposed method.

1. Introduction

Solar pumped lasers (SPLs) are optically pumped lasers that use natural sunlight as a pump source. Oscillation through various media, including gas, liquid and solid media, has been reported thus far, but the current mainstream research is on solid-state lasers using the trivalent neodymium ion (Nd³⁺) as the laser medium due to its high optical-to-optical conversion efficiency [1–4].

Potential applications of SPLs are expected in the energy field. For example, the conversion of sunlight into coherent laser light can generate high temperatures beyond the thermodynamic limit, and a Mg/MgO energy storage concept has been proposed [5]. Since the thermal relaxation loss is minimal for monochromatic light with wavelengths close to the bandgap of a silicon photovoltaic device, a highly efficient optical wireless power transmission (OWPT) based on the solar-pumped fiber laser has been proposed [6,7]. In addition, laser light can be converted to ultraviolet (UV) light via nonlinear crystals; thus, the combination of SPL with photocatalytic water splitting, which is efficient in UV [8,9], can enhance its overall efficiency of hydrogen production. The very simple structure of the SPL, which in principle has neither active electronics nor moving parts, has advantages over other lasers, especially in space. There are numerous proposed extraterrestrial applications, such as propulsion [10], power transmission [11,12] and communication [13,14].

The challenge with conventional SPLs is that the pump light source, sunlight, is incoherent white light that requires tight focusing to achieve sufficient population inversion in the laser medium. For this reason, all SPLs published to date have relied on a primary concentrator comprised of a large lens or mirror [15]. In turn, this requires precise tracking of the sun to maintain illumination of the laser medium [16]. These issues are notable obstacles to the practical application of SPLs.

To address this fundamental problem of SPLs, we have proposed an SPL without condenser optics. The schematic of the “fully planar solar-pumped fiber laser (SPFL)” is shown in Fig. 1. The basic principle of this laser is described as follows: An Nd^{3+} -doped active optical fiber is contained in a thin, bowl-shaped housing, which is made entirely of highly reflective mirrors (HRM). In addition, the surface facing the sun is a dichroic mirror (DM) that transmits shorter wavelengths and reflects longer wavelengths. The housing is filled with a liquid sensitizer in which the fiber is immersed. Sunlight transmitted through the dichroic mirror is absorbed by the sensitizer and fluoresces at wavelengths longer than the absorbed wavelength. Because the cutoff of the dichroic mirror is set shorter than the wavelength of the fluorophore, fluorescence cannot exit the housing and travels back and forth within the housing until it is absorbed by the fiber. The active fiber then generates gain, and the laser oscillates.

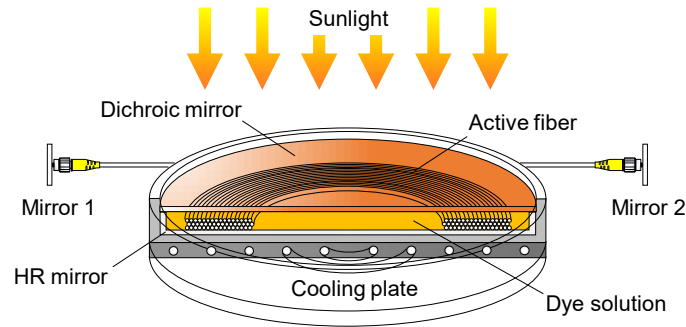


Fig. 1. Schematic drawing of a fully planar SPFL

Based on this principle, we previously fabricated a device with a diameter of 30 cm [17]. Initial studies showed that the population density of the lower laser level (${}^4I_{11/2}$) of Nd^{3+} ions at room temperature interfered with the positive gain generation [18]; thus, the entire device was cooled below -30°C by conductive cooling. Furthermore, the simulation calculations showed that the maximum output power was achieved at a fiber length of 10 km for a 30 cm diameter device [19]; however, the fiber length was limited to 190 m due to budget constraints. Therefore, this experimental device was a proof-of-principle device. As a result of the above experiments, a maximum laser power of 1.3 mW was obtained [17]. Since the sunlight power density at the Earth’s surface is 1 kW/m^2 , the incident power can be calculated to be 70 W; thus, the optical-to-optical conversion efficiency is only 2×10^{-5} . To our knowledge, this is the first time that an SPL has been successfully oscillated without a “hard” focusing device, such as a lens or a mirror.

2. Methods

2.1 Current challenges of the fully planar SPL

The main reason for the low optical-to-optical conversion efficiency is the short fiber, as mentioned above; however, there are two additional issues that need to be addressed. One is the use of an organic dye (Rhodamine 6G) that fluoresces orange as a sensitizer such that the cutoff of the dichroic mirror is set at 570 nm [17], removing a significant portion of the spectral components of sunlight. The other issue is that the top layer of the dielectric multilayer coating of the DM and HRM needs to be in contact with a liquid that has a refractive index closer to that of the dielectric; thus, in principle, high reflectivity cannot be achieved, and photon confinement is impeded.

To address the first problem, we plan to use and develop perovskite quantum dots as sensitizers instead of organic dyes. We have already demonstrated the tunability of the fluorescence wavelength in preliminary experiments, and laser oscillation was accomplished under $50\times$ sunlight with a primary concentrator [20]. To address the second problem, we then propose the use of solid-state LSCs [21,22]. Fig. 2 (a) and (b) shows a cross section of a fully planar SPFL with a conventional configuration and using a solid-state LSC, respectively.

In the conventional configuration, the active fiber is immersed in a liquid; conversely, in our proposed system, the fiber is attached to a quartz substrate with an optical adhesive. On the opposite side, the LSC is coated with a fluorinated polyurethane film impregnated with a sensitizer. The DM/HRM is the same as in the liquid LSC; however, its confinement efficiency is dramatically improved when the top layer of the dielectric multilayer is in contact with air. Although efficient light confinement is expected from total internal reflection (TIR) between the LSC and air [23], previous research has shown that DM/HR is a necessary component, with 40% of all photons confined by TIR, while the remaining 60% are confined by DH/HRM [22].

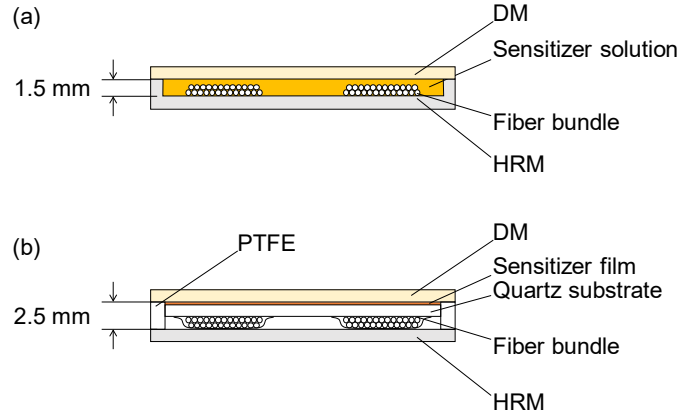


Fig. 2. Cross-sectional view of a fully planar SPFL using a (a) liquid LSC (conventional) and (b) solid-state LSC (proposed).

2.2 Configuration of the solid-state LSC

The solid-state LSC fabricated in this study consisted of a 30 cm diameter, 1.0 mm thick fused quartz plate, with the coiled fiber attached to it using InvisiSil™ OP1012 optical adhesive (Momentive), and a thin film sensitizer layer. The optical fiber was the same as that used in previous studies (Furukawa Electric) [17,18], with a core diameter of 16 μm and a Nd^{3+} concentration of 0.5 at%. Before attaching the fiber to the substrate, the protective resin layer was removed, leaving the 125 μm diameter cladding exposed.

A dye film was applied to the opposite side of the substrate. The dye film was a fluoropolymer polyurethane of Lumiflon™ (AGC Chemicals) and Duranate™ (Asahi Kasei) impregnated with a mixture of Lumogen F Orange 240 and Yellow 083 (BASF) dye. The film thickness was 80 μm , and the density was adjusted such that the optical density (OD) at a wavelength of 532 nm was 0.6. For details of the dye film, refer to previous studies [21,22].

A polytetrafluoroethylene (PTFE) ring was placed on the side of the LSC and sandwiched between the DM and the HRM. The HRM of the liquid LSC had a bowl shape due to the need to keep it watertight, creating technical difficulties in applying a highly reflective dielectric layer on the sides. Since a previous study showed that a diffuse side reflector could achieve 90% of the performance of specular reflectors [22], a combination of a flat HRM and a PTFE ring was used; this also functioned as the support of the DM, providing the necessary clearance between the DM and HRM.

In this study, two disks were fabricated: one with a fiber length of 105 m and the other with a fiber length of 290 m. The disk with the shorter fiber length was a prototype to learn the technique for designing, fabricating, and conducting experiments with a solid-state LSC. A disk with approximately three times the fiber length was subsequently fabricated and tested outdoors, but a fiber inside the disk was accidentally broken before sufficient data could be obtained.

2.3 Experimental setup

In this study, small-signal gain measurements and laser oscillation experiments were performed on a fully planar SPFL with a solid-state LSC using natural sunlight as the pump source.

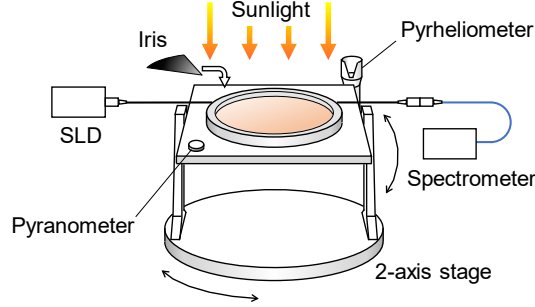


Fig. 3. Schematic drawing of the gain measurement setup

The gain measurement setup is shown in Fig. 3. A fiber-coupled superluminescent diode (SLD, Thorlabs SFC1050P) was injected into the active fiber at one end, and the emitted light was received at the other end by a fiber spectrometer (Ocean Optics NIRQuest). $A(\lambda)$ is the spectral intensity of the probe signal measured by the spectrometer with solar illumination and $B(\lambda)$ is the spectral intensity without solar illumination. Since the spontaneous emission from the sunlight absorbed by the active fiber contributed a significant fraction of the measured intensity of $A(\lambda)$, we measured the spectral intensity of the spontaneous emission by turning off the SLD and illuminating the sunlight. $C(\lambda)$ is this spectral intensity. In this case, the following relationship is obtained:

$$G(\lambda) = \frac{A(\lambda) - C(\lambda)}{B(\lambda)} \quad (1)$$

This relationship is the one-pass differential gain of the SPL; however, it is not the net gain because the attenuation of the probe light due to fiber loss is not considered. Though, this expression is useful as a simple gain measurement method.

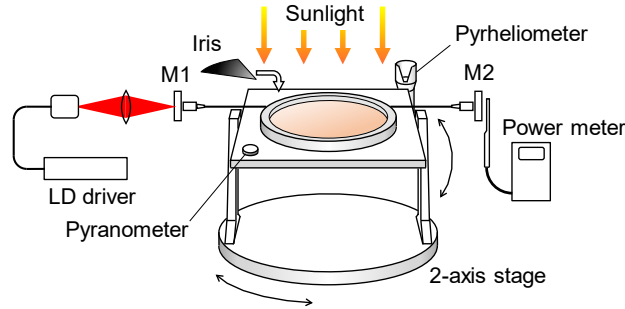


Fig. 4. Schematic drawing of the laser oscillation experiment setup

The setup for the laser oscillation experiment is shown in Fig. 4. The optical resonator consisted of a highly reflective mirror M1 and a partially transmissive mirror M2; M1 was a dichroic mirror with transmission at 808 nm. The fiber was terminated with a ferrule connector (FC)-type fiber receptacle that contacted the mirror to form a pigtail resonator [24]. The advantages of pigtail resonators were that the transmittance of M2 can be changed easily, quickly, and nondestructively (without splicing the fiber). The scattering loss of the pigtail mirror was reported to be 0.07 dB [24], which was comparable to the splice loss of a single-mode fiber.

The loss in the pigtail mirror was sensitive to the distance between the fiber end and the mirror. Therefore, before performing solar pumping experiments, the laser was longitudinally pumped by an 808 nm laser diode (LD) from M1, and the relative positions of the mirror and connector were adjusted to minimize resonator loss. The LD was then turned off, sunlight was irradiated from the front of the disk, and the laser output was measured with an optical power meter (ADC 82311B) placed at the M2 end.

The apparatus was rotated by a 2-axis manual stage such that it always faced the sun. Adjustments were made immediately before the experiment, and the apparatus was fixed during the experiment (several minutes). Direct solar irradiance was measured with a pyrheliometer (EKO MS-57). It varied from day to day and ranged from 850 to 950 W/m². Moreover, the total irradiance, including the diffuse part of sunlight, was measured with a pyranometer (EKO ML-02) installed on the surface of the 2-axis stage (tracking the sun). It also varied from day to day, ranging from 900 to 1000 W/m². For both the small signal gain and laser oscillation experiments, a variable iris was installed to partially block the aperture and adjust the irradiated solar power.

3. Results and discussion

3.1 Small-signal gain measurement

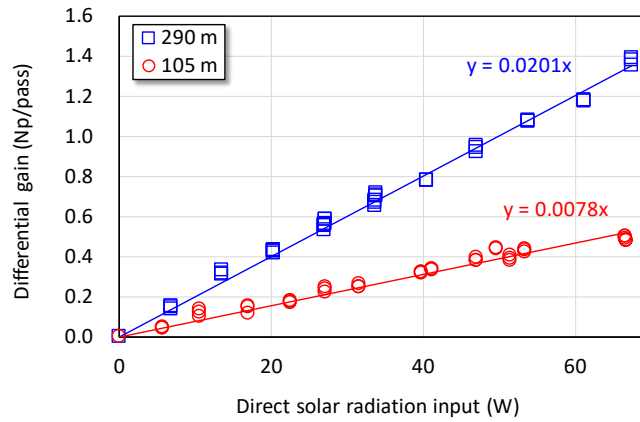


Fig. 5. One-way gain as a function of the direct solar radiation input for two different fiber lengths (105 m and 290 m).

Fig. 5 shows the results of the small-signal gain measurements. The horizontal axis is the direct solar power incident on the DM, and the vertical axis is the one-way differential gain. The active fiber used in this study has a broadband gain in the range 1050 to 1130 nm, with a peak near 1064 nm [22]. The vertical axis of the graph represents $\ln(G) = \gamma_0 l$ at 1064 nm, where γ_0 is the small signal gain coefficient and l is the fiber length. The red circle plots show the results for the 105 m-long fiber, and blue square plots show the results for the 290 m-long fiber.

The gain is proportional to the incident power and to the fiber length. The small signal gain coefficient γ_0 is proportional to the pump power density, i.e., the photon density confined by the LSC. As the fiber length increases, gain saturation will be observed because optical absorption by the fiber reduces the photon density. However, there is no evidence for this in Fig. 5 because the fiber length used in this study is not sufficient for saturation; our calculations indicate that the ideal fiber length for maximum laser power in a 30 cm disk is approximately 3 km [21]. The maximum gain achieved with the 290 m-long fiber was 1.4 Np/pass ($4.1\times$).

3.2 Laser oscillation experiment

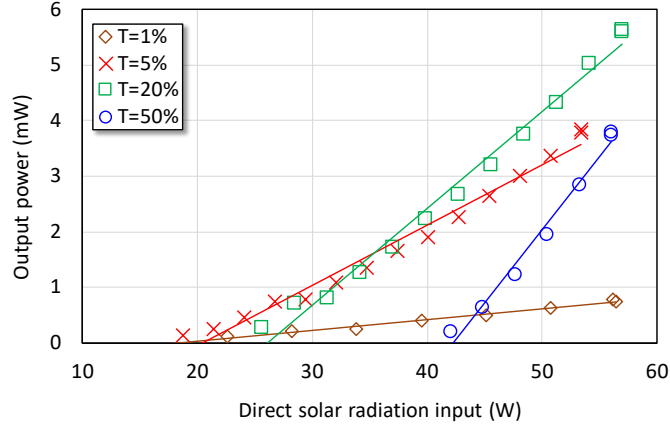


Fig. 6. Laser output power as a function of the direct solar radiation input for the 105-m long fiber. The mirror transmittance is varied as a parameter.

Fig. 6 shows the relationship between the direct solar input and the laser power that was observed on the 105 m-long fiber. Partial reflectors with 1, 5, 10, 20, 30, and 50% transmittance were used. The results for 1, 5, 20, and 50% are shown. The relationship between pump power and output power was close to a linear function. However, the slope tended to be small near the oscillation threshold. This occurred potentially because the fiber laser in this study simultaneously oscillated in many longitudinal modes, and only some of the longitudinal modes began to oscillate near the threshold. This phenomenon was also observed in other broadband fiber lasers [25,26].

For each mirror transmittance, the relationship between pump power and laser power was approximated as a linear function near the oscillation threshold, and the oscillation threshold was determined from the intersection with the x -axis. The oscillation threshold at 1% mirror reflectance was 17 W. This was only 24% of typical natural sunlight and a significant improvement over a previous study [17].

The graph in Fig. 7 plots the mirror transmittance on the horizontal axis and the oscillation threshold power on the vertical axis. As expected, the relationship was linear. Extrapolating the mirror transmittance to zero, the oscillation threshold power at zero transmittance was 15 W. Applying this to Fig. 5, the laser oscillation threshold gain for this condition (0.117 Np/pass) was 0.51 dB/pass. Subtracting the loss of the pigtail mirror from this value, 0.44 dB/pass was the value at which the gain generated in the fiber was balanced by the intrinsic loss of the fiber. This corresponded to 4.2 dB/km, which was between the manufacturer's nominal value of 3 dB/km [17] and the measured value in our previous study of 5.4 dB/km (1.25 km^{-1}) [18].

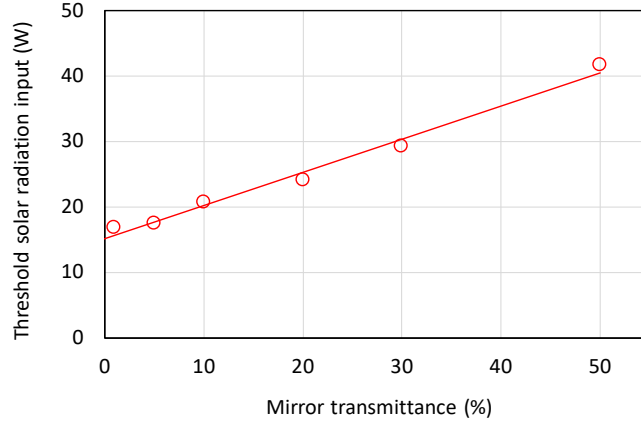


Fig. 7. Oscillation threshold power (direct sunlight) as a function of the output coupler transmittance.

Fig. 8 shows a plot of mirror transmittance on the horizontal axis and laser power on the vertical axis for the 105 m-long and 290 m-long fibers. For the 290 m-long fiber, the reliability of the data was low, except for the highest powers at $T = 20\%$ and $T = 50\%$, because the fiber in the disk was broken after a few oscillation runs. Even though the fiber was broken, it was held in place with adhesive; thus, it did not become completely disconnected, and laser oscillation was assumed to occur. The maximum laser power at the 290 m-long fiber was 15 mW, more than 10 times the maximum of liquid LSC [17]. The optical-to-optical conversion efficiency was 0.023%, and the collection efficiency was 0.21 W/m².

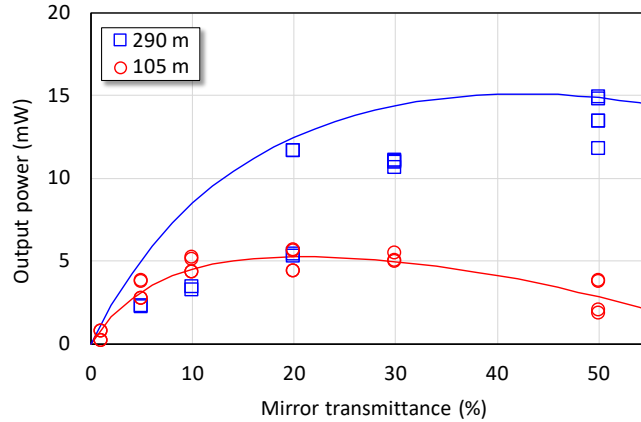


Fig. 8. Laser output power as a function of the mirror transmittance for two different fiber lengths (105 m and 290 m). Plots: experimental, lines: Rigrod fit.

3.3 Rigrod Analysis

The Rigrod equation [27] describes the laser power with a homogeneously broadened laser medium as a function of the mirror transmittance, as follows:

$$P = \frac{\gamma_0 l + \ln \sqrt{R_1 R_2}}{(1 + \sqrt{R_2/R_1})(1 - \sqrt{R_1 R_2})} I_s A T, \quad (2)$$

where $R_1 = 1 - a - a_M$ and is the reflectivity of M1, $R_2 = 1 - a - a_M - T$ and is the reflectivity of M2, a is the scattering loss of the resonator mirror, T is the transmittance of M2, γ_0 and I_s are the small signal gain coefficient and the saturation intensity of the medium, respectively, and l

and A are the length and cross-sectional area of the medium, respectively [28]. $a_M = 1 - e^{-\alpha l}$ and represents the nonsaturable losses in the laser medium as the mirror losses, where α is the loss coefficient. This approximation is correct when $\gamma_0 \gg \alpha$ [29]. In our previous study (laser oscillation by liquid LSC) [17], this approximation did not hold, and the exact solution was computed numerically. In this study, however, the approximate solution is used because it was confirmed that there is little difference between the two.

Using γ_0 , I_s , and α as parameters, the best fit the experimental results for the 105 m-long fiber was determined. The results were $\gamma_0 l = 0.62$ Np, $I_s = 8.5$ kW/cm², and $\alpha = 1.4$ dB/km. Compared to the experimental values, $\gamma_0 l$ is larger (Fig. 5), and α is smaller (4.2 dB/km). The reason for this is currently unknown. The possibility of inhomogeneous broadening of the medium was investigated [29], but the result was negative.

The red curve in Fig. 8 shows the calculated laser power for the 105 m-long fiber as a function of the mirror transmittance using the optimal parameter set. The Rigrod model is a good representation of the laser power dependence on the mirror transmittance.

We now have a model that predicts the output power of the SPL with a solid-state LSC for any given fiber length, input solar irradiance, and resonator coupling. Using this model, the calculated laser power for the 290 m-long fiber is shown in Fig. 8 with a blue curve. The highest laser powers observed at 20% and 50% transmittance are well represented by the Rigrod model.

The model was then used to calculate the relationship between incident solar power and laser power for the combination of the 290 m-long fiber and the $T = 50\%$ mirror. As a result, the calculated laser oscillation threshold pump power was 22 W, and the slope efficiency was 0.031%.

3.4 Comparison with numerical calculations

We confirmed the effectiveness of solid-state LSCs via numerical calculations and published the results [21]. The laser power of a 30 cm diameter LSC with 190 m fiber length was predicted to increase from 1.3 mW for the liquid LSC to a maximum of 39 mW. Now, this result could be compared with the experimental results.

In the numerical calculations, the 190 m-long fiber was assumed to be embedded in a disk of dye-impregnated PMMA. In the present study, however, the fiber was attached to the substrate, which increased the overall thickness of the LSC, and the distance between the DM and the HRM increased from 1.5 mm to 2.5 mm. Moreover, the fiber length was 1.5 times longer than the calculation condition. In the first-order approximation, the expected output power was inversely proportional to the DM-HR distance and proportional to the fiber length. Thus, the experimental results were directly comparable to the numerical calculation with a mirror distance of 1.5 mm and a fiber length of 190 m.

Consequently, the laser power obtained in the experiment was lower than that calculated. We speculated that this was because the fiber was attached to the quartz substrate. This created an uneven surface on the LSC and prevented total internal reflection. In Ref. [21], we predicted that the laser power of Design 1, in which the fiber was placed outside the disk, was 17 mW, and the experimental results were similar to this value. Based on the above results, the effectiveness of our proposed method was experimentally confirmed.

4. Conclusions

We investigated a fully planar solar pumped fiber laser (SPFL) without any focusing device, such as a lens or mirror. To achieve this goal, we developed a confinement mechanism that combined a fluorescent sensitizer with a chamber consisting of a dichroic mirror (DM) and a highly reflective mirror (HRM) to efficiently couple solar photons into an optical fiber. In the past, dye molecules dissolved in a liquid were used as sensitizers. However, in that case, high reflectivity could not be achieved due to the direct contact of DM and HRM with the liquid sensitizer. In our study, a solid-state luminescent solar collector (LSC) was achieved by impregnating the sensitizer into a resin and coating it on a quartz substrate. Although solid-

state LSCs were not usually combined with DM or HRM, a previous study showed that the use of DM and HRM increased the photon density by more than a factor of two compared to the total internal reflection alone. This was an immense advantage of our concept, which was characterized by extremely low gain per unit length.

A fully planar SPFL with a solid-state LSC was fabricated with the same aperture as that of the liquid sensitizer. LSC disks with a 105 m-long fiber and a 290 m-long fiber were fabricated, and the small signal gain and laser power were measured for both disks under the illumination of natural sunlight. The laser with a 105 m-long fiber had a one-way gain of 0.5 Np (65%/pass) and a maximum output power of 5.6 mW. Experiments with different sunlight intensities showed that the laser oscillation threshold was 24% of natural sunlight, which was significantly lower than that in a previous study (60%). However, the laser with a fiber length of 290 m did not provide sufficient data because the fiber broke inside the disk during the first set of experiments. Nevertheless, a one-way gain of 1.4 Np (310%/pass) and a maximum output power of 15 mW were obtained. It had a 12-fold larger output power than the liquid LSC and corresponded to an optical-to-optical conversion efficiency of 0.023% and a collection efficiency of 0.21 W/m².

A Rigrod model was constructed from the results of laser oscillation experiments on the 105 m-long fiber to predict the performance of the 290 m-long fiber. The results were in good agreement with the limited experimental results. Although it was not possible to obtain the slope efficiency for the 290 m-long fiber, it was estimated to be 0.031% from the Rigrod model.

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Data availability. Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

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