# SOLAR SOFTWARE APPLIED TO DESIGN A PHOTOVOLTAIC SYSTEM TO SUPPLY THE ENERGY DEMAND OF AN ITALIAN SCHOOL

ABSTRACT

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This paper has as objective to describe the use of SOLAR 1.1 software to design a system for supplying a part of the electric demand of a school situated in Umbertide, comparing the use o SOLAR 1.1 to real results of a system implanted yet. This software version helps also to conduce the economic analysis for grid connected or standalone photovoltaic systems for the choice of convenient values of investment rate and annuity factor and it calculates the payback period of investment in the photovoltaic plant.

**Keywords:** economic analysis, photovoltaic cell, photovoltaic systems, solar radiation.

# NOMENCLATURE

А	PV panel surface, m <sup>2</sup>
C <sub>b</sub>	cost of battery, US\$
$C_d$	cost of acquisition and installation of
peripheral	components, US\$
C <sub>el</sub>	cost of electric energy production in the
photovolta	aic system, US\$/kWh
C <sub>el</sub>	cost of electricity production in the PV
system, U	S\$/kWh
C <sub>m</sub>	cost of a photovoltaic module, US\$
C <sub>ma</sub>	maintenance cost, US\$/kWh
C <sub>mex</sub>	marginal cost of expansion of the electric
energy off	fer, US\$/kWh
Cop	operation costs, US\$/kWh
E	daily demand energy, Wh/day
Ep	produced energy in a year, kWh/year
F	annuity factor, year <sup>-1</sup>
H <sub>i</sub>	number of daily operation of the i-load,
h/day	
I <sub>pl</sub>	total investment in the plant, US\$
K	amortisation period, years
n <sub>i</sub>	number of the i-load
n <sub>m</sub>	number of module in the PV system
n <sub>w</sub>	number of working months, generally 13
n <sub>tec</sub>	number of technicians needed for the
operation	
P <sub>el</sub>	electric tax, US\$/kWh
Pi	power of the i-load, W

P<sub>p</sub> peak power, W<sub>p</sub>

R annual mean daily insolation, Wh/m<sup>2</sup>.day

R annual interest rate, %

 $R_A$  annual insolation, kWh/m<sup>2</sup>.year

 $S_{al}$  monthly salary of a technicians, US\$/month

S<sub>e</sub> expected annual saving, US\$/year

 $S_{ub}$  governmental subsidy rate for the installation,  $\ensuremath{\%}$ 

#### Greek symbols

η panel efficiency, %

 $\eta_{\rm M}$  module efficiency, %

# INTRODUCTION

Solar energy is largely used to produce heat and electricity around the world, where the photovoltaic (PV) technology allows transforming it in electric energy and the photothermal (PT) technology, in heat (NREL, 2009).

Particularly, photovoltaic energy represents an opportunity to produce electricity in the worldwide, mainly in the development countries, in those there are places where electricity grids are unreliable or non-existent and is inconvenient to make investments in a grid expansion. In far places often photovoltaic power supply is presented as the most economic option. In addition, many developing countries have high radiation levels year round (NREL, 2009).

#### Ciência/Science

Photovoltaic systems cause few environmental problems commonly related to their manufacturing. The generating component produces electricity silently and does not emit any harmful gas during operation. The basic photovoltaic material for most common modules made out of silicon is entirely benign, and is available in abundance (NREL, 2009).

One criticism of early PV modules was that they consumed more energy during their production than they generated during their lifetime. With modern production methods and improved operational efficiencies this allegation is no longer true (NREL, 2009).

Many authors have been studied technologies involved into manufacturing of solar panels, specifically solar collectors, their applications, costs minimisation, conversion optimisation etc. (Barker, Jr. and Power, 1979; Reindl et al., 1990a; Reindl et al., 1990b; McCormick and Suehrcke, 1991; Al-Nimr and Alkam, 1998; Al-Nimr et al., 1998; Alkam and Al-Nimr, 1999).

The exact energy payback is directly dependent on the available solar resource and on the degree to which the system is operational. High levels of solar irradiation and a high utilization factor will offer more rapid energy paybacks than if there is less sun and less usage, but typically energy payback will be realized within three to four years (NREL, 2009).

Besides, in the economic remarks relative to the using of energetic sources, the caused environmental damages are not considered. If that was done, the energy produced by photovoltaic, and also the energy produced by others renewable sources, would conquest more competitiveness in confrontation with the traditional non renewable sources (NREL, 2009).

In example, applications in which photovoltaic technologies can be used are related following.

Agriculture:

- water pumping, irrigation;
- electric fencing for livestock and range management.

Community:

- water pumping, desalination and purification systems;
- lighting for schools and other community buildings.

Domestic:

- lighting, enabling studying, reading, income-producing activities and general increase in living standards;
- TV, radio, and other small appliances;
- water pumping.

Healthcare:

- lighting forwards, operating theatre and staff quarters;
- medical equipment;
- refrigeration for vaccines;
- communications (telephone, radio communications systems);
- water pumping;

• security lighting.

Small enterprises:

- lighting systems, to extend business hours and increase productivity;
- power for small equipment, such as sewing machines, freezers, grain grinders, battery charging;
- lighting and radio in restaurants, stores and other facilities.

Photovoltaic systems create no emission in the electricity generation. Avoided emissions are a very positive aspect. In a study made by Kroposki and De Blasio (2000) is resulted that a 10kW photovoltaic system in Colorado (USA) avoids 10,105kg in  $CO_2$  emissions and 1,801kg in  $NO_x$  emissions.

No pollution of the photovoltaic systems can be inserted in the economic analysis. The Denver Service Guideline estimated the costs associated with the production of carbon dioxide (CO<sub>2</sub>) in 0.0088US\$/kg, sulphur dioxide (SO<sub>2</sub>) in 1.65US\$/kg, and nitrogen oxides (NO<sub>x</sub>) in 7.48US\$/kg (Effert and Thompson, 2000).

The mean installation costs (including the devices) of photovoltaic systems were 5.7US\$/Wp for grid connected systems and 13.9US\$/Wp for standalone system in USA (Mortensen, 2001). These costs make high also the cost of electricity generated by photovoltaic plant.

The panels' costs influence considerably the final installation cost, from 40% to 75% (Delahoy and Kiss, 2000). The photovoltaic energetic source will be viable when the panels cost will be decreased, as is the perspective.

Hybrid options based on sustainable resources, mainly photovoltaic, have been studied as solution for small rural villages' energy demand, such as (Chendo and Salawu, 1989; Dhere, 1989; Bailey et al., 1991; Song, 1994; Leitch and Van Der Linde, 1995; De Groot, 1997; Harford, 1998; Valente and Almeida, 1998), also connection to grid and its control (Lamas et al., 2008).

#### METHODOLOGY

The study presents the software SOLAR 1.1 developed with purpose of helping the choice of photovoltaic panels available commercially including electric needs calculation for the installation applied to a case study for a school placed at Umbertide, near Perugia, Italy.

This new version of program help also to conduce the economic analysis for grid connected or standalone photovoltaic systems for the choice of convenient values of investment rate and annuity factor and it calculates the payback period of investment in the photovoltaic plant.

For these evaluations, exergoeconomic modelling were used, such as reported in Annex 1.

# PROJECT OF PHOTOVOLTAIC SYSTEM FOR SUPPLYING A SCHOOL

In this item, it will be shown a project made by the software SOLAR 1.1 for supplying a part of the electric demand of a school placed in Umbertide.

In this school a photovoltaic system is already existent, so the object of this paper is to compare the existent system with the project resultant from SOLAR 1.1 with intention to validate it.

The photovoltaic plant of this school is one of the research activity of the Department of Industrial Engineering at University of Perugia.

#### **Description of the Existent PV Plant**

In the school were implanted 220 photovoltaic panels PL 800 in multicrystalline silicon, connected in groups of 10 to form 22 arrays. Each array is connected to an inverter that transforms the direct current in alternating current, producing a voltage of  $220V_{AC}$ , as it is needed to supply the loads and to send the electricity into the grid.

The total surface of the photovoltaic field is  $169.4m^2$  and the nominal power of the plant is 15,400Wp. Other panels characteristics are shown in the Table 1.

Table 1	<ol> <li>Panels</li> </ol>	characteristics.
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Model	PL 800
Туре	Multicrystalline
	silicon
Length	1,220 mm
Width	555 mm
Surface	$0.68 \text{ m}^2$
Weight	8 kg
Peak power	70 W <sub>p</sub>
Voltage of maximum	17.2 V
power	
Current of maximum	4 A
power	
Open circuit voltage	21.3 V
Short circuit current	4.4 A

The system is grid connected, it was stipulated a contract with the electricity concessionary ENEL, in which is approved that the surplus of energy production is send into the grid and paid by ENEL at the same price of the sold electricity. This can be do until the energy produced by photovoltaic system is minor or equal to the energy bought from the grid, so the school cannot receive a monetary recompense by ENEL, but only a reduction of the payment till its resetting (ENEL, 2011).

This contract secures that the surplus of produced energy did not waste but it was sold to ENEL. It specially happens in summer, when the school is close, so the electricity consumption is low and the production is high for the major value of insolation. The contract secures also that the school can consume electricity from the grid when the electricity produced is lower than the demand.

The energy produced by the photovoltaic plant is about 17,000kWh in a year, the energy consumed by the school is about 45,000kWh in a year, so meanly, during the year, the condition of a photovoltaic production minor than the consumptions is respected.

#### Project of Photovoltaic Plant by SOLAR 1.1

To project a photovoltaic plant through SOLAR 1.1, the values of latitude, annual mean cloudiness, and demand energy are required. The value of latitude of Umbertide is 43°18'25''. The value of the annual mean cloudiness can be taken from meteorological tables, this value results equal to 5.4 tenths of overcast sky (Barra, 1981).

Inserting these values, the software draws the curve of daily insolation shown in Fig. 2.



Figure 2. Estimate of the place insolation.

The annual mean insolation results equal to 3,452Wh/m<sup>2</sup>.day for Umbertide region.

The Fig. 3 shows the window for insertion of energy values to calculate the peak power. In this case the value of peak power for this plant is known, it can be taken equal to the value of the existent photovoltaic plant that has a nominal peak power of 15,400Wp.

		En	ergy	Loads		
	Nro.	Watt	h/day	TOTAL [Wh/day]	ANNUAL MAR	N INSOLATION
Television	1				3452	
Lights	1					trigin ouy
Refrigerator	1	-				1
Washing Machine	1			<b></b>		St Clear
Microwave oven	1					1
Radio FM/AM	1					릅 Calculate
Radio Broadcasting	1					- 1
Computer	1					Print
Printer	1				ſ	1
Battery charger	1					Back
Hi-Fi	1					
Videorecorder	1				ENERGY	PEAK POWER
Satelliatar plant	1				1	15400
Water pump	1			[	Whiday	Wp
Other	1					
					1	Choose Panels

Figure 3. Peak power of the photovoltaic plant.

Now, it is possible to click the button Choose Panels to start the choice of the panels.

The panels chosen are shown in Fig. 4.

choice of	Comme		e runeis					
	PRODUCTER	CODE	TOTAL POWER	EFFICI	TOTAL ENCY COST [US S]	TOTAL	TOTAL SURFA	CIE
MONOCRYSTALLINE	AstroPower	AP-1206	15480	12,3	73937.64	129	125.67	Mo
MULTICRYSTALLINE	SOLON	SOLON alpha	15400	10,7	59202.00	220	143.95	Mo
AMORPHOUS	BP Solarex	MST-43-LV	15437	5,3	60250.97	359	295.04	Mo
	J Demand	Power 15400 Wp						

Figure 4. Panels chosen.

In the economic analysis, to make this project similar to the existent plant, it is taken the multicrystalline panels, model Solon Alpha and the grid connected system. Also, the multicrystalline panel have a cost lower than the monocrystalline and the amorphous ones (Fig. 4).

The panels Solon Alpha required in the plant are 220 and occupy an area of 143.5m<sup>2</sup>.

Other characteristics of these panels are shown in the Fig. 5.

Registro	Producer	Code	
192	SOLON	SOLON alpha	-
Power	70 We	open circ. Volt. 21,1	Volt
Tolerance	[+ <del>1</del> ·3 %	short circuit Curr. 4.50	Am
Efficiency	10,7 %	Voltage a -18°C 23,8	Volt
Voltage	16,7 Volt.	Voltage a 70°C 13,2	Volt
Current	4,20 Amp.	Surf. 0,6543 m <sup>a</sup> Mass 8,5	Kg
Type of Cell	poli	Dimension 1205×543×35	mm
Price 269,1	US\$ Nation Germany	Internet www.solonag.com	_

Figure 5. Panel Solon Alpha.

As it can be seen by confronting the Table 2 and the Fig. 5, the characteristics values of the panels in the existent plant and panels chosen by SOLAR 1.1 are similar.

For the economic analysis of a photovoltaic system implantation connected to grid, it can be considered an electricity price around 0.18US\$/kWh and a governmental subsidy rate of 75% into the investment cost.

The maximum value of subsidy that can be gave for photovoltaic plant with a nominal power from  $1kW_p$  to  $20kW_p$  is 75%, connected to the electric grid, as it is instituted by a program of Ministero dell'Ambiente e della Tutela del Territorio in the law of March 16th, 2001.

The results of calculation of costs operated by the software are shown in the Fig. 6.

Panel: MU	LTICRYSTALLINE S	DLON SOLON alpha sistema GRID CONNECTE
Peak Power:	15400 Wp	
Panel Power:	70.00 Watt	
Num. Panels:	220	
Total Power of Panels:	15400.00 Watt	S ELECTRICITY COST
Energy in a year	21761.83 kWh	EXDECTED ANNUAL SAVING
Panel Price:	269.10 US\$	
Total Cost of Panels:	59202.00 US\$	APAY BACK PERIOD
Cost for peak Watt	3.84 USS/Wp	
ost for peak Watt with subsidy	0.96 USS/Wp	Print
Num. of Technicians:	2	Dr] Other Panel
Total investment on the plant:	65122.20 US\$	
rotal investment with subsidy:	16280.55 US\$	🗶 Exit
Operation costs:	0.06 USSAWh	
Maintenance Costs:	0.30 USSAWh	

Figure 6. Calculation of costs.

Among the results, there is the energy producing during a year that, with these panels, is about 21,700kWh. This value is higher than the value of 17,000kWh produced in a year by the existent plant. The cause of the difference is different values of panels' efficiency for: PL 800 is 6.97%; and Solon Alpha is 10.7%.

In Fig. 7 is shown the trend of electricity cost in the photovoltaic production in function of the amortisation period for different values of interest rate and in the situation of null subsidy and with subsidy of 75%.



Figure 7. Electricity cost in photovoltaic production.

In this diagram it is possible to see that when the subsidy is null, the electricity cost is always higher than the grid electricity cost. When the subsidy is 75%, the electricity cost becomes lower than the grid electricity cost.

The values of the amortisation period, for which the electricity cost in the photovoltaic production is equal to the electricity cost bought from the grid are shown in the zoom of diagram (Fig. 8).



Figure 8. Zoom of electricity cost diagram.

These values are: 11 years for interest rate of 4%; and 16 years for interest rate of 8%.

It is evident that in case of absence of the subsidy rate, the photovoltaic plant is not convenient by economic view because the cost of electricity that is generated by the plant is higher than the electricity of the grid. So there is not benefit in consuming a electricity produced with a major cost and there is a loss in selling the electricity to the grid with a cost lower than the cost spend in the generation.

In other way, in case of subsidy rate, the cost of the electricity produced in photovoltaic system is lower than the grid electricity price so, selling the electricity to the grid there is a profit.

In the Fig. 9 is shown the diagram of the trend of the expected annual saving.



Figure 9. Expected annual saving.

In this diagram it can see that the plant produces economic benefit only in case of subsidy and the payback period of the investment is 11 years if the interest rate is 4% or 16 years if it is 8% (Figs. 10 and 11).

Calculation of PAY BACK PERIOD
system GMID CONNECTED panels MOLTICATSTALLINE SOLON SOLON appra
Subsidy Rate 75 💽 %
Interest rate 4 * *
PAY BACK PERIOD: years 11

Figure 10. Payback with interest rate of 4%.

		Calculati	ion of PAY	BACK PERI	OD
system	GRID CONNEC	TED panels MULT	TICRYSTALLINE SO	LON SOLON alpha	
	Subsidy Rate	75 • %			
	Interest rate	• %			
	PAY BACK PER	RIOD: years <mark>16</mark>			
		E Calcolate	- Print	¥ Evit	

Figure 11. Payback with interest rate of 8%.

### CONCLUSIONS

The photovoltaic systems can be a good alternative source to satisfy energetic problem for the low environmental impact deriving by their utilisation. But they result not completely competitive in the economic confrontations with others energy sources for their high costs of implantation.

The benefits and the observations about using of photovoltaic is reassumed in the following:

Energetic:

- the stand alone PV systems offer the possibility to have electric energy in remote place where the electric grid is inexistent and then there is no convenience to install it;
- the grid connected PV systems can be located at both residential and commercial locations, they can be used to reduce peak demand when its output is properly matched with load usage.

Environmental:

- photovoltaic energy is a clean renewable resource. The fuel supply for these systems although variable is also free and unending;
- photovoltaic systems create no emission in the electricity production. Avoided emissions is a very positive aspect. In a study made by Kroposki and De Blasio (2000) is resulted that a 10kW PV system in Colorado avoids 10,105kg in CO<sub>2</sub> emissions and 1,801 kg in NO<sub>x</sub> emissions.

Economic:

- the mean installation costs (including the devices) of photovoltaic systems in 2000, were 5.7US\$/W<sub>p</sub> for grid connected systems and 13.9US\$/W<sub>p</sub> for standalone system in USA (Mortensen, 2001). These high costs make high also the cost of the electricity produced by the photovoltaic plant;
- the panels costs influence much the final installation cost, from 40% to 75% (Delahoy and Kiss, 2000). The PV energetic source will be very alternative when the panels cost will be decreased, as is the perspective;
- in the case studied in this work was seen as in situation in which the electric tariff is low, as in the Brazilian condition (electricity price is 0.08US\$/kWh), the PV energy can be competitive only if the government incentives the installation with subsidy;
- no pollution of the PV systems can be inserted in the economic analysis. The Denver Service Guideline estimated the costs associated with the production of carbon dioxide (CO<sub>2</sub>) in 0.0088US\$/kg, of sulphur dioxide (SO<sub>2</sub>) in 1.65US\$/kg, and of nitrogen oxides (NO<sub>x</sub>) in 7.48 US\$/kg (Effert and Thompson, 2000).

If the environmental benefits due to the no emissions of polluting substances was considered in the economic analysis, the economic benefit would be 13,000US\$/year only for the absence of emitted  $NO_x$  in a 10kW<sub>p</sub> plant, as it results by combining the environmental studies of Kroposki and De Blasio (2000) and the economic studies of the Denver Service Guideline.

The objective of this work was the development of a new version of the software Solar in which is contained the instruments to conduce the economic analysis of PV system.

The software can be update in future with the introduction of new archives for the selection of the devices necessary for the plant. So, it will can be inserted an archive with the models of batteries and one with the models of inverters.

In the software can also be inserted a function that considers the benefit of the no emission in the economic analysis.

Another upgrade that can be done is a technical function that premise to operate the calculation relative to the modules connection. Knowing the values of wanted power, voltage and current, through this function it is possible to find the number of the modules branch in parallel and the number of modules connected in series in each branch.

In conclusion, it can be told that with the subsidy rate, the high cost of the technologies in photovoltaic production can be reduced. This decrease does become the photovoltaic an energy source economically competitive with traditional energy sources.

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#### ANNEX 1

**Electric Energy Production Cost** 

$$C_{el} = \frac{I_{pl} \times \left(1 - \frac{S_{ub}}{100}\right)}{E_p} \times f + C_{op} + C_{ma}$$
(A1)

**Annuity Factor** 

$$f = \frac{q^k \times (q-1)}{q^k - 1} \tag{A2}$$

$$q = 1 + \frac{r}{100} \tag{A3}$$

**Energy Produced** 

$$E_p = \frac{\eta_M}{100} \times R_A \times A \tag{A4}$$

**Total Investment Cost** 

$$I_{pl} = C_m \times n_m + C_d + C_b \tag{A5}$$

**Operation Costs** 

$$C_{op} = \frac{n_{tec} \times S_{al} \times n_m}{E_p} \tag{A6}$$

**Expected Annual Saving** 

$$S_e = E_p \times \left( P_{el} - C_{el} \right) \tag{A7}$$

Expected Annual Saving for Standalone System

$$S_e = E_p \times \left( C_{m_{ex}} - C_{el} \right) \tag{A8}$$

**Daily Demand Energy** 

$$E = \sum_{i=1}^{k} n_i \times P_i \times H_i \tag{A9}$$

Nominal Plant Power (Peak Power)

$$P_p = \frac{E \times 1,000}{0.9 \times R} \tag{A10}$$

In Eq. (A10), "1,000" is a standard value of irradiance, in  $W/m^2$ .

#### **Energy Produced in a Year**

$$E_{P} = R_{A} \times A \times \frac{\eta}{100} \tag{A11}$$

**Annual Insolation** 

$$R_A = \int_0^{365} Rdt \tag{A12}$$

Cost of Panel in Function of the Nominal Power for: Monocrystalline Panels, Eq. (A13); Multicrystalline Panels, Eq. (A14); and Amorphous Panels, Eq. (A15)

$$C_m = 182.322875 \times 1.013406^{P_p} \tag{A13}$$

$$C_m = 306.118327 \times 1.008568^{P_p} \tag{A14}$$

$$\log(C_m) = 0.0180791 \times P_p + 4.73025$$
 (A15)

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