Solid-state NMR proves the presence of penta-coordinated Sc site in MIL-100(Sc)

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Abstract: Advanced solid-state NMR methods and first-principles calculations demonstrate for the first time the formation of pentacoordinated scandium sites. These coordinatively unsatured sites were shown during the thermal activation of scandium-based Metal-Organic Frameworks (MOFs). ⁴⁵Sc NMR experiment allows their specific observation in activated Sc₃BTB₂ and MIL-100(Sc) MOFs. The assignment of the ScO₅ groups is supported by the DFT calculations of NMR parameters. The presence of ScO₅ Lewis acid sites in MIL-100(Sc) explains furthermore its catalytic activity. We also introduce the first NMR experiment to probe ¹³C-⁴⁵Sc distances. This advanced solid state NMR pulse sequence allows us to demonstrate the shrinkage of the MIL-100(Sc) network when the activation temperature raises.

Introduction

Metal-Organic Frameworks (MOFs) materials offer rich physical and chemical properties due to their adjustable architectures and porosity.^[1] Thus, they present possible applications in multiple domains including gas storage, heterogeneous catalysis, drug delivery... Amongst the wide variety of MOFs, MIL-100 compound exhibits a porous framework incorporating large cavities with diameter up to 34 Å, related to the MTN zeolite topology (ZSM-39). Firstly reported with chromium(III),^[2] MIL-100 has then been isolated with other trivalent metals, such as iron,^[3] aluminium,^[4] vanadium,^[5] scandium^[6, 7] or indium.^[8] These MOFs have been widely investigated owing to their numerous interesting properties including (i) high surface areas, (ii) Lewisacidity, and (iii) remarkable thermal stability.^[4, 9] In particular, the Lewis acidity of activated MIL-100(Al or Cr) has been ascribed to the presence of penta-coordinated metal sites (AIO₅ or CrO₅),^{[9-} ^{11]} which are generated upon thermal activation. The CrO₅ sites were detected by CO sorption Infra-Red (IR) study,^[9, 11] whereas

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the AlO₅ ones were observed either by solid-state Nuclear Magnetic Resonance (NMR)^[12] or IR^[13] spectroscopy. Conversely, to the best of our knowledge, the nature of Lewis acid sites in MIL-100(Sc) has remained elusive.^[14, 15] IR and H₂ adsorption studies have recently demonstrated the formation of five-fold coordinated scandium atoms, ScO₅, upon the thermal activation of another MOF: [Sc₃O(BTB)₂(H₂O)₃](OH)(H₂O)₅(DMF), with H₃BTB = 1,3,5-tris(4-carboxyphenyl) benzene, called Sc₃BTB₂ hereafter.^[16] Nevertheless, the Lewis acidity of this MOF has not been investigated and hence it has not been possible to relate the Lewis acidity of Sc-based MOFs to the formation of ScO₅ sites.

⁴⁵Sc solid-state NMR a priori looks to be a promising technique to study the local environment of Sc atoms. ⁴⁵Sc nucleus has favorable NMR properties, including 100% natural abundance and a gyromagnetic ratio close to that of ¹³C, γ (⁴⁵Sc) \approx 0.967y(¹³C).^[6, 17, 18] Furthermore, ⁴⁵Sc chemical shifts are known to be very sensitive to the coordination number of the scandium^[17, 19, 20] and their assignment can be supported by Density Functional Theory (DFT) calculations,[19, 21, 22], notably in Sc-based MOFs.^[15] For Sc nuclei surrounded by similar atoms, it has been shown that the ⁴⁵Sc isotropic chemical shift decreases when the coordination number of the scandium site increases.^{[17,} ^{22]} Nevertheless, the ⁴⁵Sc isotropic chemical shift is also quite sensitive to the other structural differences, such as bond angles and bond distances^[19, 20] and hence the shift regions of the different Sc coordinations in different families of materials overlap heavily. Furthermore, this spin-7/2 isotope is subject to large quadrupolar interactions [19, 20] and hence the second-order quadrupolar broadening can obscure the chemical shift information. Such quadrupolar interaction is especially large for asymmetrical Sc environments, such as ScO₅. An additional difficulty for the NMR detection of ⁴⁵ScO₅ sites is the low concentration of those sites, since most materials contain mainly six, seven or eight-coordinated scandium environments.[17, 20] Despite these difficulties, penta-coordinated Sc sites have been recently observed by solid-state NMR in Sc-doped BaZrO3 containing oxygen vacancies.^[16] However, in MOFs, only hexacoordinated Sc sites have been seen by solid-state NMR so far.^[6, 15]

The NMR observation of carbon-scandium proximities would also provide valuable information about the structure of Scbased MOFs. However, an instrumental limitation of NMR spectroscopy is that usual multiple channels NMR probes cannot be tuned simultaneously to two close Larmor frequencies, such as those of ¹³C and ⁴⁵Sc isotopes (100.6 and 97.2 MHz, respectively at the magnetic field of 9.4 T). Therefore, to the best of our knowledge, ¹³C-⁴⁵Sc double resonance experiments have not been reported so far. Nevertheless, we have demonstrated

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recently that the use of a frequency splitter^[23] can circumvent this limitation since this device allows tuning and matching a single probe channel to two close frequencies. We have notably used such device to acquire double-resonance ²⁷Al-¹³C^[24, 25] and ¹³C-⁵¹V^[26] solid-state NMR experiments.

Herein, we demonstrate the formation of ScO₅ sites during the thermal activation of Sc₃BTB₂ using ¹H and ⁴⁵Sc NMR at high magnetic field. The assignment of penta-coordinated Sc site is supported by DFT calculations. Furthermore, during the thermal activation of MIL-100(Sc), we also observe ⁴⁵Sc NMR signals at similar chemical shifts, which demonstrate the presence of penta-coordinated scandium species, which can react as Lewis acid sites. We report furthermore the first NMR observation of ¹³C-⁴⁵Sc proximities in activated MIL-100(Sc). These double-resonance ¹³C-⁴⁵Sc experiments allow observing the shrinkage of MOFs structure upon its thermal activation.

Results and Discussion





Figure 1. Representation of (a) the MTN topology of MIL-100(Sc), (b) the structure of $S_{C_3}BTB_2$ (c) the trigonal trimer of scandium; (d) the trimesate ligand found in the MIL-100(Sc) structure; and (e) the 1,3,5-tris(4-carboxyphenyl)benzene ligand found in the $S_{C_3}BTB_2$ structure.

The structures of Sc₃BTB₂ and MIL-100(M) (M= metal) have been solved by X-ray diffraction (XRD) of single-crystals.^[2, 27] The building unit of Sc₃BTB₂ and MIL-100(Sc) consists in a trimer of corner sharing ScO₆ octahedra linked by a μ_3 -oxo ligand. Thus, each Sc³⁺ ion is hexa-coordinated to: (i) one μ_3 -O, (ii) four oxygen atoms from carboxylate groups, and (iii) a terminal hydroxyl group or a terminal water molecule (Fig. 1c). Carboxylate ligands bridge the corner sharing ScO₆ octahedra of the trimer. Conversely, the ligands differ between Sc₃BTB₂ and MIL-100(Sc). The former is built up from 1,3,5-tris(4-carboxyphenyl)benzene (Fig. 1e) and the latter from trimesic acid (Fig. 1d). The crystal structures of Sc₃BTB₂ and MIL-100(Sc) also differ. The Sc₃BTB₂ crystallizes in the hexagonal space group *P*62c forming hexagonal channels with a diameter of approximately 23 Å (Fig. 1b). Its unit cell contains two crystallographically inequivalent scandium sites. Conversely, MIL-100(Sc) adopts the topology corresponding to the MTN zeolite (Fig. 1a) and its unit cell includes seven crystallographically inequivalent scandium sites.^[16]

X-ray thermodiffraction analysis allows probing modifications of the long-range positional order versus temperature for Sc_3BTB_2 and MIL-100(Sc) (Fig. S4 and S5, respectively). Up to 400°C, no drastic change occurs in the diffractogram of Sc_3BTB_2 indicating that the crystal structure of this MOF is preserved up to this temperature. Above 400°C, the diffraction peaks vanish because of the ligand decomposition, which results in a collapse of the crystal structure. The rehydration of the different compounds activated at different temperatures does not perturb the 3D organization of the structure, since their corresponding powder X-ray diffraction patterns are similar (Fig. S6).

For MIL-100(Sc), no significant change occurs in terms of diffractogram upon heating up to 220°C (blue curves in Fig. S5). Above 220°C, diffraction Bragg peaks progressively broaden and decrease in intensity suggesting the formation of defects (green curves). At 300°C, diffraction peaks vanish, which indicates the collapse of the MIL-100(Sc) framework (red curves).

2. Solid-state NMR spectra of Sc₃BTB₂

2.1. 1D NMR spectra

As already shown for MIL-100(Al or Cr), the penta-coordinated metal sites cannot be observed by diffraction techniques owing to their lack of long-range order.^[9-11, 27] Their observation hence



requires techniques, such as IR and NMR, which can probe the local structure at atomic level.^[9, 11-13] Fig. 2 displays the ⁴⁵Sc and ¹H NMR spectra of Sc₃BTB₂ as-synthesized materials (Fig. 2a) and after thermal treatment up to 325°C (Fig. 2b-d) recorded at high magnetic field (18.8T).

Figure 2. ⁴⁵Sc (left) and ¹H (right) NMR spectra of Sc₃BTB₂: (a) assynthesized; (b-d) after thermal treatment under vacuum of one night at (b) 170, (c) 275 and (d) 325 °C. The spectra were recorded at 18.8 T and a MAS frequency of v_R = 20 kHz. Spinning side bands are labeled with *. The vertical scale of the (b-d) ¹H spectra is multiplied by 2 compared to that in (a).

⁴⁵Sc NMR spectrum of the as-synthesized material shows a single resonance around 50 ppm, assigned to a scandium species in an octahedral environment (ScO₆). This assignment is in agreement with the literature.^[6, 15] The resolution does not allow distinguishing the two scandium crystallographic sites, even if the line-shape differs from the typical powder pattern of a single ⁴⁵Sc site and must be produced by overlapping signals from distinct Sc local environments. This line subsumes the contributions of scandium sites attached to terminal hydroxo and agua ligands in the trinuclear μ_3 -oxo-centered inorganic sub-unit. When the temperature increases at 170°C (Fig. 2b), a high field shift of the most intense ⁴⁵Sc signal is observed. This shift is tentatively ascribed to the evacuation of the pores and the flips of the ligand phenyl rings around the single bonds between sp² hybridized carbon atoms (Fig. 1e). For the terephtalic ligand, such phenyl flips have been observed using ²H NMR.^[28] Moreover, the lineshape of ScO₆ signal at 170°C is broader than for the as-synthesized material. Such broadening stems from a distribution in the orientation of the phenyl ring at higher temperature. Weak and deshielded ⁴⁵Sc peaks are also observed at 170°C. Their intensities grow when the temperature raises (compare Figs. 2c-d) to reach 34% of the total integrated intensity at 325°C. It has been shown that the isotropic chemical shift of ⁴⁵Sc nuclei increases for lower coordination number,^[20, 22] and especially the ${}^{45}Sc$ signals of ScO_5 sites are more deshielded than those of ScO₆ ones.^[29] Therefore these sites can be assigned to penta-coordinated scandium. This attribution is in agreement with the literature where the ScO₅ sites have been evidenced by IR and H₂ adsorption in activated Sc₃BTB₂.^[16] But to the best of our knowledge, the NMR observation of ScO₅ site in MOFs has not been reported so far. Furthermore, the fraction of 34% of penta-coordinated scandium is in agreement with the structure (Fig. 3) and with results already published for analogous MOFs.^[3, 9, 10] As stated above, the slight disorder and the emergence of the penta-coordinated sites observed by NMR do not lead to main changes in the longrange order of the structure according to the XRD (Fig. S4).



Figure 3. Illustration of the dehydration process in scandium trimer $Sc_3(\mu_3$ -oxo) and the formation of the penta-coordinated Sc site.

¹H NMR spectrum of the as-synthesized material is dominated by a high intensity water signal resonating at 3.7 ppm (Fig. 2a). To better display, its intensity has been cut. Two other groups of signals are observed in the spectrum. Between 0 and 3 ppm, low intensity signals are assigned to residual solvent or impurities trapped into the pores, while between 5 and 12 ppm, signals are assigned to the ligand. The more precise assignment of those resonances requires 2D correlation spectra and is beyond the scope of this article. When the temperature increases to 170°C (Fig. 2b), the water signal dramatically decreases and the intensities of the peaks resonating between 0 and 3 ppm strongly decrease. This observation is consistent with volatiles species trapped into the pores (solvent), which are evacuated at high temperature. At 170°C, a broad peak is observed at 3.8 ppm and is ascribed to H₂O and OH attached to Sc atoms. The intensity of this peak decreases at 275 and 325°C, which is consistent with the elimination of aqua ligand (see Fig. 3). Conversely the signals resonating between 5 and 12 ppm are barely affected by the thermal activation, which suggests that the integrity of the ligand is preserved up to 325°C. This NMR observation confirms the XRD data of Fig. S4.

2.2. 2D MQ-MAS spectra



Figure 4. ^{45}Sc 3Q-MAS sheared 2D spectra of (a) as-synthesized Sc₃BTB₂, and (b-d) after thermal treatment at: (b) 170, (c) 275, and (d) 325 °C. Spectra were recorded at 18.8 T and v_R = 20 kHz. The peaks inside the black circles correspond to ScO₅ sites.

The resolution of ⁴⁵Sc NMR experiments is drastically improved by acquiring 3Q-MAS 2D spectra (Fig. 4), to the extent that the two crystallographic-distinct sites of ScO₆ are observable in the spectrum of the as-synthesized material (Fig. 4a). The fits of this spectrum (Fig. S9) lead to the quadrupolar parameters reported in Table S1. The relatively high C_Q values (11.7 and 13.5 MHz) suggest a non-symmetrical octahedral environment for the scandium sites. At higher temperature (170°C, Fig. 4b), a broader distribution of quadrupolar parameters and chemical shifts is observed. At least six different scandium sites can be distinguished (Fig. S10, Table S2). Amongst them the two most deshielded signals at 77 and 92 ppm, which experience a smaller quadrupole interaction with C_Q ≈ 8.0 MHz, can be assigned to two penta-coordinated scandium sites. By increasing the temperature at 275°C (Fig. 4c, Fig. S11 and Table S3) and 325°C (Fig. 4d, Fig. S12 and Table S4), the intensity of those deshielded signals increases in agreement with the 1D spectra (Fig. 2b, c and d), whereas the C_Q and δ_{iso} values remain similar. This result suggests an increase of the amount of ScO₅ in the material. To summarize, in Sc₃BTB₂, hexa- and penta-coordinated scandium sites exhibit different ranges for the NMR parameters C_Q and δ_{iso} (see Table 1). It is noted that in the 3Q-MAS 2D spectrum of the 170°C material, the peak resonating at 66 ppm cannot be safely attributed to ScO₅ or ScO₆ since its quadrupolar parameters and isotropic chemical shift are not characteristic of neither scandium site.

Table 1. Ranges of isotropic chemical shifts and CQ values of the penta-
and hexa-coordinated sites experimentally observed in Sc ₃ BTB ₂ .

Site	ScO₅	ScO ₆
δ _{iso} (ppm)	70-100	20-60
C _Q / MHz	≈ 8	9-14

3. Calculation of NMR parameters of ScO_5 and ScO_6 sites

First-principles calculations of ⁴⁵Sc NMR parameters in Scbased MOFs were carried out to further support the assignment of ScO5 signal. However, the large number of atoms in the unit cell of Sc₃BTB₂ and MIL-100(Sc) precludes DFT calculations using CASTEP code to converge within reasonable amount of time. Therefore, the DFT calculations were carried out on the MIL-88(Sc) compound. The crystalline structure of this MOF (Fig. S18a) is built from the same Sc trimers as Sc₃BTB₂ and MIL-100(Sc) but with the 2,5-dihydroxyterephtalate ligand (Fig. S18b). However, its structure can be described by a much smaller unit cell. We performed first the calculations on the unmodified MIL-88(Sc) structure (see Table S5).^[30] The difference in δ_{iso} between ScO₆ sites, (a,d) on the one hand and (b,c,e,f) on the other hand, is about 6-7 ppm, which is similar to that between the two ScO₆ sites of Sc₃BTB₂ (see Table S1). The calculated C_{Q} values of ScO₆ site in MIL-88(Sc) are comparable to those measured for similar Sc environments in Sc₃BTB₂ (see Table S1). Calculations were also performed on the modified MIL-88(Sc) structure in which a H₂O ligand had been removed from the structure in order to form a five-fold coordinated scandium (see Table S6). For such structure, the DFT calculations predict distinct chemical shifts for the five ScO₆ sites contained within the unit cell. The δ_{iso} of (a) and (f) sites are about 8-9 ppm higher than that of (d) site and 17-19 ppm higher than that of (b) and (c) sites. Such differences are similar to the one measured for the three most shielded ScO₆ sites of Sc₃BTB₂ heated at 275°C (see Table S3). The calculated C_Q values of ScO₆ site in modified MIL-88(Sc) agree reasonably well with those measured for those sites in Sc₃BTB₂ heated at 170, 275 or 325°C (see

Table S1 to S4). Furthermore, the DFT calculations predict a δ_{iso} for the ScO₅ site, which is 74 ppm higher than that of the most shielded ScO₆ site. Such prediction agrees with the measured isotropic chemical shift difference between sites (a) and (f) in Sc₃BTB₂ heated at 275°C (see Table S3) as well as sites (a) and (d) in Sc₃BTB₂ heated at 325°C (see Table S4). Furthermore, the higher isotropic chemical shift of ScO5 site with respect to ScO₆ one is consistent with the already reported increase in isotropic chemical shift for decreasing coordination number of Sc atom.^[17, 22] The calculated C_Q values of ScO₅ site in modified MIL-88(Sc) is significantly higher than that measured for those sites in Sc₃BTB₂ heated at 170, 275 or 325°C (see Table S1 to S4). Such discrepancy can stem from (i) the different ligands in Sc₃BTB₂ and MIL-88(Sc) and (ii) the absence of NMR signals for ⁴⁵Sc nuclei subject to large C_Q values in the 3Q-MAS 2D spectra, from which the experimental C_Q value is measured. The 3Q-MAS experiment does not excite efficiently nuclei subject to large quadrupolar interaction. Experimentally, the number of inequivalent 45 Sc sites in Sc₃BTB₂ heated at 170 and 275°C exceeds that predicted by DFT calculations for modified MIL-88(Sc). Such discrepancy stems from the structural differences between MIL-88(Sc) and Sc3BTB2 as well as the lack of periodicity of ScO₅ defects in the Sc₃BTB₂ crystal contrary to the modified MIL-88(Sc) structure used for the DFT calculations.

4. Solid-state NMR spectra of MIL-100(Sc)

4.1 1D NMR spectra



Figure 5. ⁴⁵Sc (left) and ¹H (right) NMR spectra of MIL-100(Sc): (a) assynthesized and (b-d) after thermal treatment of one night at (b) 100, (c) 150, (d) 220, and (e) 300°C. The spectra were recorded at 18.8 T with a MAS frequency of v_R = 20 kHz. The fraction of integrated intensity corresponding to ⁴⁵ScO₅ signal after deconvolution is indicated in (b-d) on the left. The integrated intensity of the water ¹H signal after deconvolution is also indicated on the right spectra and is normalized with respect to that of water ¹H signal in (a). * and F label the spinning sidebands and an impurity signal, respectively.

Fig. 5 shows the ⁴⁵Sc and ¹H NMR spectra of MIL-100(Sc) assynthesized (Fig. 5a) and after thermal treatment at temperature ranging from 100 to 300°C (Fig. 5b-e). The ⁴⁵Sc NMR spectrum of the as-synthesized material is similar to that already reported and it exhibits a broad and asymmetric line-shape resonating around 70 ppm (Fig. 5a), which is assigned to ScO₆ sites.^[6, 15] The seven crystallographically inequivalent sites for the scandium are not resolved. As stated for the Sc₃BTB₂ material, the asymmetric line-shape is attributed to the distribution of quadrupolar and chemical shift parameters. Thermal activation at temperatures ranging from 100 to 220°C produces a broadening of the ScO₆ signal (Fig.5b-e) due to a possible increase in the quadrupolar interaction. Moreover, a weak resonance at about 100 ppm becomes more intense for higher activation temperature. The deconvolution of the ⁴⁵Sc signals is shown in Fig. S7 for MIL-100(Sc) activated at 220°C. Thus, the signal with a resonance frequency higher than ScO₆ site is assigned to ScO5 environment since: (i) the results obtained in the first part of this article prove that the isotropic chemical shift of ScO₅ is higher than that corresponding to ScO₆ sites, (ii) in MIL-100(Al or Cr), thermal activation removes the aqua ligands of AIO₆ sites and hence forms Lewis acid AIO₅ or CrO₅ sites, and activated MIL-100(Sc) is also a Lewis acid catalyst,^[14, 15] and (iii) this signal cannot correspond to a ⁴⁵Sc satellite transition since a corresponding peak is observed in the 3Q-MAS spectrum (see below). As seen in Fig. 5, the integrated intensity fraction corresponding to the most deshielded ⁴⁵Sc signal increases from 100 to 220°C. This result indicates an increasing amount of ScO₅ defects at higher activation temperature, up to 7 % of scandium sites. Nevertheless, the fraction indicated in Fig. 5 is much lower than that found in Sc₃BTB₂ and MIL-100(AI) for penta-coordinated Sc or AI species, respectively.^[10] This may be due to the less thermally stable structure of MIL-100(Sc), which collapses at 220 °C, while this temperature is required for Sc₃BTB₂ and MIL-100(AI) in order to reach 30 % of ScO₅ and AIO₅ site, respectively. The ⁴⁵Sc NMR spectrum of MIL-100(Sc) activated at 300°C displays a very broad line-shape, which indicates a large distribution of local Sc environments. Such distribution is consistent with the collapse of the MOF framework observed by X-ray diffraction (Fig. S5).

Fig. 5 also shows the ¹H NMR spectra of MIL-100(Sc) after different thermal treatments. Multiple resonances are observed in the ¹H NMR spectrum of the as-synthesized material (Fig. 5a), in agreement with the previously published ¹H NMR spectrum of the analogous MIL-100(AI).[10] Upon heating, the intensity of water and solvent ¹H signals strongly decreases, showing that thermal activation removes the physisorbed molecules in the pores. As seen in Fig. 5, thermal activation at 100°C results in a 30-fold decrease in the amount of water in MIL-100(Sc). Such dehydration at moderate temperature corresponds to the evacuation of physisorbed water,^[10] which is pursued at higher temperatures (Fig. 5c-d). This water reduction at high temperature corresponds to the loss of aqua ligands, in agreement with the formation of ScO₅ sites (see above). Moreover, the activated MIL-100(Sc) displays an additional ¹H signal at 1.7 ppm (indicated with T), which is ascribed to impurities coming from the degradation of the DMF. This signal decreases for increasing activation temperature. The activated MIL-100(Sc) also displays a ¹H signal at 3.5 ppm ascribed to Sc-OH sites. The OH signals in activated MIL-100(Sc) are broader than in the as-synthesized sample since in the latter the exchange between OH protons and physisorbed molecules reduce 1 H- 1 H dipolar coupling. The dramatic broadening of the 1 H signals after thermal activation at 300°C (Fig. 5e) confirms the collapse of the MIL-100(Sc) structure.

4.2 2D 3Q-MAS NMR spectra

Proof of the presence of ScO₅ sites can be confirmed by the high resolution ⁴⁵Sc 3Q-MAS 2D spectra (Fig. 6). The one of the as-synthesized MIL-100(Sc) (Fig. 6a) displays a broad distribution of isotropic shifts due to the unresolved seven scandium sites, in contrast with Sc₃BTB₂ that exhibits only two crystallographic sites (Fig.4a). The 3Q-MAS spectrum of the MIL-100(Sc) activated at 220°C (Fig. 6b) permits to resolve the signals of ScO5 and ScO6 sites. With respect to the assynthesized sample, the ScO₆ signal (i) exhibits a narrower distribution of isotropic shifts and (ii) corresponds to a larger quadrupole interaction, since the removal of physisorbed molecules within the pores reduces the structural disorder and increases the electric field gradients for ScO₆ sites. The 3Q-MAS spectrum of the MIL-100(Sc) activated at 300°C (Fig. 6c) confirms the broad distribution of ⁴⁵Sc environments produced by the collapse of the MOF structure.

As a conclusion, the formation of ScO_5 in thermally activated MIL-100(Sc) is confirmed by solid-state NMR upon temperature by removing a water molecule (Fig. 5). The presence of this coordinatively unsatured site explains the Lewis acidity already observed in this material.^[14, 15]



Figure 6. ⁴⁵Sc 3Q-MAS sheared 2D spectra at 18.8 T of (a) as-synthesized MIL-100(Sc), and after thermal treatment at (b) 220 and (c) 300°C.

4.3 2D D-HMQC NMR spectra

The proximities between ¹H and ⁴⁵Sc nuclei have been probed by ⁴⁵Sc-{¹H} *D*-HMQC 2D spectra (Fig. 7). In those spectra, the most intense correlation peak is that between the btc ligand and the ScO₆ sites. A cross-peak between the signals of Sc-OH groups and ScO₆ sites is also detected. This cross-peak is weak in the as-synthesized material since the proton exchange between OH groups and physisorbed water and ethanol molecules decreases the ¹H-⁴⁵Sc dipolar couplings. In the MIL-100(Sc) heated at 220°C, the cross-peak between Sc-OH proton and ScO₆ sites becomes more intense since the physisorbed molecules are removed, thus preventing the proton exchange. The collapse of the structure at 300°C is confirmed by the broadening of the cross-peaks.



Figure 7. ⁴⁵Sc-{¹H} *D*-HMQC 2D spectra of (a) as-synthesized MIL-100(Sc), and after thermal treatment at (b) 220, and (c) 300 °C. 2D spectra were recorded at 18.8 T with a spinning speed of $v_R = 20$ kHz.

4.4 ¹³C-{⁴⁵Sc} S-RESPDOR NMR spectra

 $^1\text{H} \rightarrow ^{13}\text{C}$ CPMAS spectra exhibit three resonances corresponding to the three distinct carbon sites of the btc ligand (Fig. S8), consistently with the previously published spectra.^[6] The ^{13}C signals are only marginally modified for increasing activation temperature up to 220°C. However, at 300°C a dramatic broadening occurs owing to the collapse of the MOF framework (see above). Thus, thermal activation up to 220°C leads to the formation of ScO₅ sites (Fig. 5), but the integrity of the ligand is preserved below 220°C (Fig. S8).



Figure 8. Comparison between the ¹³C-{⁴⁵Sc} SFAM-RESPDOR curves at 9.4 T and v_R = 12.5 kHz for the three carbon sites: a) C3, b) C2 and c) C1 of assynthesized MIL-100(Sc) (blue diamonds), and after thermal treatment at 100 (red crosses), 150 (green triangles), 220 (black squares) and 300°C (orange circles). The S/N of the C2 signal of the sample heated at 300°C is too low to measure the SFAM-RESPDOR fraction.

Probing ¹³C-⁴⁵Sc proximities is useful to detect changes in the structure of Sc-based MOFs during the heating. To this end, the ¹³C-⁴⁵Sc distances were measured by SFAM-RESPDOR experiments.^[24] Fig. 8 displays the ¹³C-{⁴⁵Sc} S-RESPDOR signal fractions, ΔS/S₀, as a function of the recoupling time for each of the three carbons of MIL-100(Sc) after thermal activation at different temperatures. Those heteronuclear experiments between isotopes with close Larmor frequencies were performed using a frequency splitter,^[23] and a SFAM-RESPDOR sequence suitable for the splitter (see Fig. S1).^[24] The comparison of the ¹³C-{⁴⁵Sc} SFAM-RESPDOR fractions for the three carbon sites shows that the dephasings of ¹³C transverse magnetization

under ¹³C-⁴⁵Sc dipolar couplings are the fastest for COO⁻ site, the slowest for C_{ar}, and intermediate for CH. These results suggest that d_(Sc...COO⁻) < d_(Sc...CH) < d_{(Sc...Car}). It is noted that a low S/N is obtained for the C_{ar} site due to the smaller efficiency of the cross polarization for the quaternary carbon (Fig. S8). Thus, the $\Delta S/S_0$ fraction of this site exhibits a lower accuracy. For each materials, the uncertainties of the signal fraction are reported in the Fig. S13-S17 using the S/N and the equation 4 of the ref.^[24] Obviously for each carbon sites, the $\Delta S/S_0$ fractions globally increase for higher activation temperature. These NMR observations indicates shorter distances between the ¹³C and ⁴⁵Sc nuclei at higher temperature and are consistent with the shrinkage of the unit cell of MIL-100(Sc) at higher temperature. Such shrinkage has already been reported for MIL-100(Cr).^[9]

Conclusions

Solid-state NMR has demonstrated the formation of ScO5 in Sc₃BTB₂ and MIL-100(Sc) upon thermal activation. To the best of our knowledge, this result represents the first NMR observation of these sites in Sc-based MOFs. In agreement with the already reported decrease in the ⁴⁵Sc isotropic chemical shift for higher coordination number, the ScO₅ signal is more deshielded than the ScO₆ one. The assignment of ScO₅ signal is supported by DFT first-principles calculations. The formation of ScO₅ sites is concomitant with the decrease of water ¹H NMR signal. Thus, the ScO₅ sites are produced from ScO₆ one by the removal of an agua ligand. The formation of ScO5 sites in activated MIL-100(Sc) explains the Lewis acidity of this material. ¹H NMR also shows the evacuation of the physisorbed molecules from the pores, whereas ⁴⁵Sc NMR indicates a change in the local environment of ScO₆ sites in activated MOFs. Moreover, ¹³C-⁴⁵Sc proximities have been probed for the first time using NMR. Even if ¹³C and ⁴⁵Sc isotopes exhibit close Larmor frequencies the combination of a frequency splitter and an adapted NMR pulse sequence has permitted the estimate of ¹³C-⁴⁵Sc distances in MIL-100(Sc). This technique has enabled to detect a shrinkage of the structure when the temperature increases.

Experimental Section

Synthesis of materials

Sc₃**BTB**₂: It was synthesized, based on an upscale version of the procedure reported in the literature^[16] using ScCl₃.xH₂O (0.27 g, 1.35 mmol) and H₃BTB (0.20 g, 0.45 mmol) dispersed in a mixture of *N*,*N*-dimethylformamide (DMF, 6 mL), tetrahydrofuran (THF, 8 mL), CH₂Cl₂ (6 mL), H₂O (6 mL) and HNO₃ (69.5%, 6 drops). The reaction was carried out in a 125 mL Teflon-liner within a Parr-type autoclave heated at 120°C for 48 h and then cooled down to room temperature over a period of 12 h.

 $\mbox{\it MIL-100(Sc):}$ This compound was synthesized according to the procedure reported in the literature and Sc(NO_3)_3.3H_2O was used as the scandium source. $^{[6]}$

Thermodiffraction

Thermodiffractions of Sc₃BTB₂ and MIL-100(Sc) were performed under 5 L.h⁻¹ air flow in an Anton Paar HTK1200N of a D8 Advance Bruker diffractometer (θ - θ mode, Cu_{Ka1/a2} radiation) equipped with a Vantec1 linear position sensitive detector (PSD). Each powder pattern was recorded in the range 6-60° for 2 θ (at intervals of 20°C between RT and 800°C) with a 1s/step scan, corresponding to an approximate duration of 27 min. The heating rate between two patterns was 5°C.min⁻¹.

The PXRD analysis for the Sc₃BTB₂ rehydrated sample was carried out on a Bruker D8 Advance diffractometer (Cu_{Kα} radiation) equipped with a Lynx Eye[®] fast detector. Each pattern was recorded in the 2*θ* range 5-50° with a 0.3 s/step scan.

Sample preparation for NMR measurements

Sc₃**BTB**₂. As described in the literature,^[16] as-synthesized product was first soaked in acetone during 96 h, and then degassed under vacuum (10⁻⁶ bar) at the desired temperature (170, 275 or 325°C) overnight. The resulting product was then cooled down to room temperature and transferred in an argon glovebox to be packed in a 3.2 mm zirconia rotor, which was closed with a Vespel cap.

MIL-100(Sc). As-synthesized samples were packed in a 3.2 mm zirconia rotor without a cap and heated in an oven at the desired temperature (100, 150, 220 or 300°C) for one night. At the end of the night, the rotor was closed with a Vespel cap.

NMR experiments

The employed NMR pulse sequences are depicted in Figs. S1-S3 of the Electronic Supporting Information. The ¹H and ¹³C chemical shifts were referenced to tetramethylsilane (TMS), whereas the ⁴⁵Sc chemical shifts were referenced to 1M Sc(NO₃)₃.3H₂O aqueous solution.

For both MIL-100(Sc) and Sc₃BTB₂ samples, ¹H, ⁴⁵Sc and ⁴⁵Sc-¹H NMR experiments were carried out using a Bruker Avance III 18.8 T (800 MHz for proton) spectrometer equipped with a 3.2 mm double resonance probe spinning at a Magic-Angle Spinning (MAS) frequency of $v_{\rm R} = 20$ kHz. In the ¹H experiments, a DEPTH sequence was used to remove the background signal,^[31] and the RF-amplitude was 73 and 71 kHz for MIL-100(Sc) and Sc₃BTB₂ respectively. The ⁴⁵Sc NMR spectra were acquired using direct excitation under MAS (DEMAS) using a ⁴⁵Sc pulse lasting 0.93 µs and an RF amplitude of 67 kHz for MIL-100(Sc) and 1 µs and an RF amplitude of 62.5 kHz for Sc₃BTB₂. The ¹H DEMAS spectra result from averaging 16 transients with a recovery delay $\tau_{\rm RD} = 5$ s, i.e. an experimental time of 80 s. The ⁴⁵Sc DEMAS spectra result from averaging 1024 transients with a recovery delay $\tau_{\rm RD} = 0.5$ s, i.e. an experimental time of 8 min 32 s.

For the dipolar-mediated Heteronuclear Multiple-Quantum Correlation (*D*-HMQC) 2D experiments with ⁴⁵Sc detection and ¹H indirect detection (⁴⁵Sc-{¹H}), the heteronuclear coherence transfer is mediated by ¹H-⁴⁵Sc dipolar interactions, which are reintroduced by the SR4²₁ symmetry-based recoupling sequence.^[32] This recoupling scheme suppresses the homonuclear ¹H-¹H dipolar interactions in the first-order average Hamiltonian.^[33] ¹H RF amplitudes for the 90° pulses and the SR4²₁ recoupling were equal to $v_{ff} = 71$ and 40 kHz (twice v_{R}), respectively. The RF amplitude of the ⁴⁵Sc pulses selective of the Central Transition (CT) was equal to 18 kHz. Each of the two dipolar recoupling periods, $\tau_{rec}/2$, was equal to 600 µs = 12T_R (where T_R corresponds to a rotor period). No ¹H dipolar decoupling was applied during the acquisition. Spectra were recorded with an accumulation of 600 transients and a recovery delay of $\tau_{RD} = 1$ s, leading to an experimental time of 8 hours.

⁴⁵Sc triple-quantum (3Q-MAS) 2D experiments were acquired using a zfiltered pulse sequence.^[34] Excitation and reconversion pulses lasted 3.5 and 1.0 μ s, respectively, with v_{rf} = 62.5 kHz for Sc₃BTB₂ and 3.6 and 1.2 μ s with v_{rf} = 52 kHz for MIL-100(Sc). The CT selective $\pi/2$ last pulse employed ν_{ff} = 7.6 and 9 kHz for MIL-100(Sc) and Sc₃BTB₂, respectively. The recovery delay, the number of transients and the experimental time were (0.5 s, 960, 6h30) for Sc₃BTB₂ and (2 s, 504, 12 h) for MIL-100(Sc). The ⁴⁵Sc quintuple-quantum MAS (5Q-MAS) spectra of MIL-100(Sc) were also acquired (not shown) but they exhibit similar resolution as the 3Q-MAS ones and lower signal-to-noise ratio (S/N).

The $^{1}\text{H} \rightarrow ^{13}\text{C}$ cross-polarization (CPMAS) 1D experiments and the Resonance-Echo Saturation-Pulse DOuble-Resonance (RESPDOR) one with ^{13}C detection and ^{45}Sc as dephaser nuclei ($^{13}\text{C}-[^{45}\text{Sc}]$) were performed on a 9.4 T Bruker spectrometer (400 MHz for proton) equipped with an AVANCE-II console. Spectra were recorded with a 3.2 mm three-channels HXY probe used in double-resonance mode and the rotor was spun at v_{R} = 12.5 kHz. For the $^{1}\text{H} \rightarrow ^{13}\text{C}$ CPMAS 1D experiments of MIL-100(Sc), the recovery delay was τ_{RD} = 2 s, the contact time was τ_{CP} = 3 ms, the ^{13}C RF field was 94 kHz, and the ^{1}H RF field amplitude was linearly ramped from 50 to 100 kHz. SPINAL-64 ^{1}H decoupling with 80 kHz rf was applied during the acquisition of ^{13}C spectra.[^{35}] The number of scans was NS = 512, which lead to 17 minutes experimental time.

¹³C-{⁴⁵Sc} RESPDOR experiments employ Simultaneous Frequency and Amplitude Modulation (SFAM₁) scheme^[36] as heteronuclear dipolar recoupling and are denoted SFAM-RESPDOR hereafter. The SFAM₁ heteronuclear recoupling has been chosen because it is robust and efficient when the irradiated spins are not subject to large homo-nuclear dipolar couplings, as it is the case here for the ¹³C nuclei in this isotopically unmodified MOFs. In RESPDOR experiments, the RF field amplitude of ⁴⁵Sc saturation pulse was 50 kHz, and the sum of the two dipolar SFAM₁ recoupling periods, τ_{rec} , was varied from 0 to 4 ms. Continuous wave ¹H decoupling with an RF field amplitude of 80 kHz was applied during SFAM₁ recoupling periods. SPINAL-64 ¹H decoupling with v_{rf} = 80 kHz was also applied during acquisition. The recovery delay of this experiment was $\tau_{RD} = 2$ s. The number of scans was NS = 2048 and the experiments lasted for 23 hours.

First-principles calculations

Calculations were performed with the CASTEP DFT code (version 8)^[37] using the GIPAW (gauge including projected augmented wave) algorithm.^[37, 38] Perdew-Burke-Ernzerhof generalized gradient approximation^[39] was used and the valence electrons were described by ultra-soft pseudopotentials.^[40] The integrals over the first Brillouin zone were performed using a Monkhorst-Pack grid^[41] and k point spacing was 0.04 2π Å⁻¹. The cut-off energy used was 60 Ry. Scalar relativistic effects were included at the zero-order relativistic approximation (ZORA) level.^[42] A semi-empirical dispersion correction (SEDC) scheme was used.^[43] DFT calculations were first performed on the already published structure of MIL-88(Sc),^[30] which contains six ScO₆ sites. Then, the crystallographic data of MIL-88(Sc) containing ScO₅ sites were derived by removing one H₂O molecule from the MIL-88(Sc) unit cell. This modified unit cell contains five ScO₆ sites and one ScO₅ site.

Geometry optimizations of the structures were performed using a variable unit cell with an energy tolerance of 0.0001 eV. The ^{45}Sc isotropic chemical shifts were referenced by converting the absolute magnetic shielding $\sigma_{iso,i}$ into the chemical shift $\delta_{iso,i} = \sigma_{ref,i} - \sigma_{iso,i}$ so that $\delta_{iso}(^{45}Sc) = -48.2$ ppm for ScPO4.

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