

Solving Practical Economic Dispatch Problems Using Improved Artificial Bee Colony Method

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Abstract— This paper presents an improved artificial bee colony (IABC) optimization method to solving practical economic dispatch taking into account the nonlinear generator characteristics such as valve-point loading effects. In order to exploit the performance of this new variant based ABC method to solving practical economic dispatch, a new local search mechanism (LSM) associated to the original ABC algorithm; it allows exploiting effectively the promising region to locate the best solution. The proposed approach has been examined and applied to many practical electrical power systems, the 13 generating units, and to the large electrical system with 40 generating units considering valve point loading effects. From the different case studies, it is observed that the results compared with the other recent techniques demonstrate the potential of the proposed approach and show clearly its effectiveness to solve practical and large ED.

Index Terms— Global optimization, Artificial bee colony, Economic dispatch, Optimal power flow, Valve point effect, Prohibited zones, Local search.

I. INTRODUCTION

During the last two decades, the interest in applying global optimization methods in power system field has grown rapidly. Economic dispatch strategy is one of the fundamental issues of power system operation and planning, its main objective is to schedule the committed generating units of a power system by optimizing a particular objective function, while satisfying certain specified operating constraints. In its most general formulation, the economic power dispatch (EPD) is a nonlinear, nonconvex, large-scale problem with both continuous and discrete control variables. It becomes even more complex when practical generators constraints (prohibited zones, valve point effects, pollution control) are taken in consideration [1]. The literature on the application of the global optimization in the OPF problem is vast and [1] represents the major contributions.

Huge number mathematical optimization techniques have been employed for solving the economic dispatch problem, this first category includes, linear programming (LP), nonlinear programming (NLP), quadratic programming (QP), and interior point methods [2-3]. All these techniques rely on initial condition and convexity to find the global optimum; methods based on these

assumptions do not guarantee to find the global optimum when considering practical of generator constraints (Prohibited zones, Valve point effect, and multi-fuel options), in [4], authors present a review of the major contributions in this area.

The second category includes many heuristic and stochastic optimization methods known as global optimization techniques (GOT). Many evolutionary algorithms such as the genetic algorithm (GA) [5], particle swarm optimization (PSO) [6], simulated annealing (SA) [7], tabu search (TS) [8], ant colony optimization (ACO) [9], and differential evolution (DE) [10], were proposed to solve the practical economic dispatch problem. In [1]-[11], authors present the major contributions of this second category in power system operation and control.

The third category includes, a variety of hybrid methods based conventional methods (mathematical methods) and global optimization techniques, like genetic algorithm (GA) and quadratic programming (GA-QP), or combination of artificial techniques with metaheuristic methods, like: Fuzzy logic and genetic algorithm (Fuzzy-GA), artificial neural network and genetic algorithm (ANN-GA), Fuzzy logic and particle swarm optimization (Fuzzy-PSO) [12]. In the literature various modified global optimization methods have been proposed to solving various problems related to power system operation and control, the major contributions related to this category reviewed by authors in [11].

Recently, a new family of global optimization methods, have been developed and applied with success to solving complex optimization methods such as; Harmony search [13], biogeography based optimization method [14], honey bee algorithm [15], teaching learning based optimization (TLBO) [16], and Fuzzy-TLBO [17]. Artificial Bee Colony (ABC) algorithm [18-19-20] is one of the most recently introduced swarm-based algorithms. ABC simulates the intelligent foraging behavior of a honey bee swarm. This paper presents an improved artificial bee colony algorithm for the solution of practical and large economic dispatch considering valve point loading effects and power transmission loss.

II. MATHEMATICAL FORMULATION OF ACTIVE POWER PLANNING

The main strategy of economic dispatch (ED) is to minimize the total generation cost of power system but still satisfying specified constraints (generators constraints and security constraints).

A. Simple objective function

For optimal active power dispatch, the objective function f is the total generation cost expressed as follows:

$$\text{Min } f = \sum_{i=1}^{NG} (a_i + b_i P_{gi} + c_i P_{gi}^2) \quad (1)$$

Where NG is the number of thermal units, P_{gi} is the active power generation at unit i and a_i, b_i and c_i are the cost coefficients of the i^{th} generator.

B. Constraints

1. Equality constraints: Power balance constraints

The total power generation must cover the required total demand P_D and the active power loss in transmission line P_{loss} , the equality constraint expressed as follows:

$$\sum_{i=1}^{NG} P_{gi} - P_D - P_{loss} = 0 \quad (2)$$

C. The inequality constraints: Generating units security constraints

- Upper and lower limits on the active power generations:

$$P_{gi}^{\min} \leq P_{gi} \leq P_{gi}^{\max} \quad (3)$$

P_{gi}^{\min} and P_{gi}^{\max} are the minimum and maximum outputs of the i^{th} generation unit;

D. Objective function with valve point effect

The valve-point loading is taken in consideration by adding a sine component to the cost of the generating units [12-14].

Typically, the fuel cost function of the generating units with valve-point loading is represented as follows:

$$f_T = \sum_{i=1}^{NG} (a_i + b_i P_{gi} + c_i P_{gi}^2 + |d_i \sin(e_i (P_{gi}^{\min} - P_{gi}))|) \quad (4)$$

d_i and e_i are the cost coefficients of the unit with valve-point effects. The input-output performance curve for a typical thermal unit can be represented as shown in figure 1.

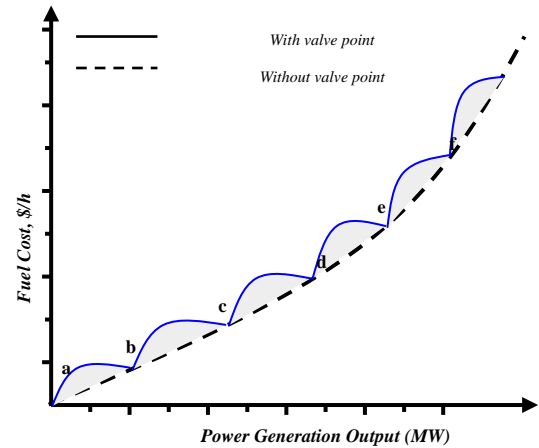


Fig. 1. Fuel cost characteristic under valve-point loading effects.

III. ARTIFICIAL BEE COLONY OPTIMIZATION METHOD

Artificial Bee Colony (ABC) algorithm, proposed by Karaboga in 2005 for real parameter optimization, is a recently introduced optimization algorithm and simulates the foraging behavior of bee colony [18] for unconstrained optimization problems [19].

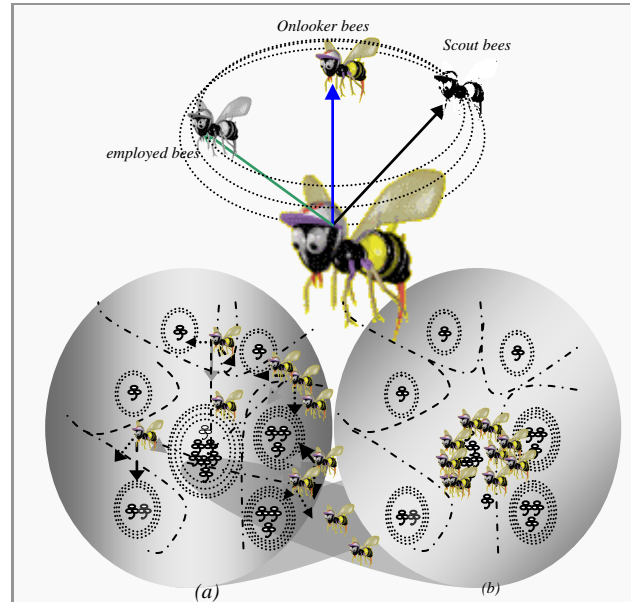


Fig. 2. Basic mechanism search of ABC: a) Initial situation, b) Final situation.

A. Mechanism search of the original ABC

As well illustrated in figure 2, the colony of artificial bees consists of three groups of bees called employed bees, onlookers and scouts. While a half of the colony consists of the employed artificial bees, the other half includes the onlookers.

There is only one employed bee for every food source. It means that the number of employed bees is equal to the number of food sources around the hive. The basic mechanism search of ABC is well presented in figure 2.

B. Artificial Bee Colony algorithm

The main steps of the algorithm described as below:

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1: Initialize Population
2: repeat
3:   Place the employed bees on their food sources
4:   Place the onlooker bees on the food sources
   depending on their nectar amounts
5:   Send the scouts to the search area for discovering
   new food sources
6:   Memorize the best food source found so far
7: until Stopping condition

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The steps of the basic ABC algorithm can be explained in details as follow:

1. Producing initial food source sites

Initial food sources are produced randomly within the range of the boundaries of the control parameters.

$$x_{i,j}^{(0)} = x_j^{(L)} + rand[0,1] * (x_j^{(U)} - x_j^{(L)});$$

$$i = 1, 2, 3, \dots, NP;$$

$$j = 1, 2, 3, \dots, D;$$

Where,

NP : is the number of food sources;

D : is the number of decision variables;

$rand[0,1]$: denotes a uniformly distributed random value between 0 and 1.

$x_j^{(L)}$ and $x_j^{(U)}$ are lower and upper bounds of the j th decision variable;

2. Searching process

In the second step of the algorithm, for each employed bee, a new source is produced by:

$$v_{ij} = x_{ij} + \varphi_{ij}(x_{ij} - x_{kj}), \quad (6)$$

Where, $k \in \{1, 2, \dots, NP\}$, $j \in \{1, 2, \dots, D\}$, φ_{ij} is a uniformly distributed real random number within the range $[-1, 1]$, it controls the production of neighbour food sources around x_{ij} and represents the comparison of two food positions visually by a bee.

The total number of employed bee equals to the half of the number of food source. In this study the value of the control parameter exceeding its boundary (active power generation in this case) is set to its limits based on the following conditions:

$$\text{if } x_i > x_i^U \text{ then } x_i = x_i^U,$$

$$\text{if } x_i < x_i^L \text{ then } x_i = x_i^L$$

3. Evaluation phase

3.1 Exchange information: In this stage the employed bees share their information related to the nectar amounts and the positions of their sources with the onlooker bees on the dance area.

3.2 Fitness evaluation: An onlooker bee evaluates the nectar information taken from all employed bees and chooses a food source site with a probability related to its nectar amount.

3.3 Selection probability: The probabilistic selection depends on the fitness values of the solutions in the population. In the original ABC this probabilistic selection scheme formulated based on (7), as the nectar amount of food sources (the fitness of solutions) increases, the number of onlookers visiting them increases, too.

$$p_i = \frac{a \cdot fitness_i}{\max(fitness)} + b \quad (7)$$

Where, $fitness_i$ is the fitness of the solution x_i .

C. Improved Artificial Bee Colony (IABC)

The basic disadvantage of the original ABC algorithm is that it may fail to locate the global optimum and provide near optimum solution, in order to exploit the performance of this new method to enhance the solution quality to solving practical economic dispatch a new local search mechanism associated to the original ABC algorithm it allows exploiting effectively the promising region to locate the best solution.

Figure 3 shows the basic principle of the local mechanism search coordinated with the original ABC algorithm; figure 4 shows the flowchart of the proposed improved ABC using simple dynamic local search mechanism.

$$a_i = [x_1, x_2, \dots, x_n]_{1,ng}, \quad b_i = [y_1, y_2, \dots, y_n]_{1,ng} \quad (8)$$

$-a_i, b_i$ are the initial lower and upper limits on the active power generations constraints.

The best solution found ($P_{g_i}^{best}$) using ABC is considered as an initial solution for the local search procedure (LSP).

1-Generate new power limits according to the following equations:

$$\Delta_i^{\min} = P_{g_i}^{best} - Rand() (P_{g_i}^{best} - P_{g_i}^{\min}) \quad (9)$$

$$\Delta_i^{\max} = P_{g_i}^{best} - Rand() (P_{g_i}^{\max} - P_{g_i}^{best}) \quad (10)$$

Where;

$\Delta_i^{\min}, \Delta_i^{\max}$ are the two estimated regions.

a_i^{new}, b_i^{new} are the new estimated lower and upper limits on the active power generation constraints.

2- The objective function (minimum fuel cost) values are calculated:

- New data base is generated at each level: $[a_i, b_i^{new}]$, $[a_i^{new}, b_i]$, $[a_i^{new}, b_i^{new}]$
- Save the new range a_i^{new}, b_i^{new} as an initial search range to the next generation,

- Save the new feasible generation units limits ($P_{g_i}^{\min}(new), P_{g_i}^{\max}(new)$).

3-Repeat processes search until the last level is reached:

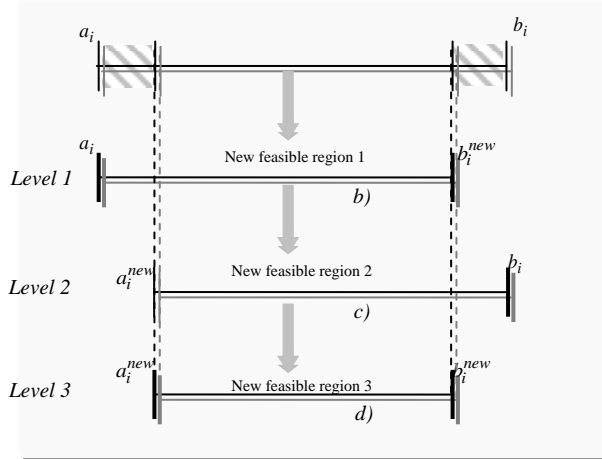


Fig. 3. Local search mechanism: a) initial lower and upper bounds, b), c), d) are the new estimated generated bounds.

D. Parameters settings of IABC

The initial values of IABC parameters are selected as depicted in Table 1:

Table. 1 THE PARAMETERS USED IN THE PROPOSED ALGORITHM

Parameter	Explanation	Value	
NP	colony size	20-30	Based on the problem size
$Limit$		20	Based on the problem size
$Food\ Number$	the number of food sources	$NP / 2$	
a	Coefficient associated to probabilistic selection	0.85	
b		0.15	
$Max\ cycle$	Maximum Generation	100-500	Based on the problem size

Table 2. ECONOMIC DISPATCH RESULTS FOR 13-GENERATING UNITS USING THE PROPOSED APPROACH: PD=1800 MW

N°	Our approach: IABC	PS [24]	QPSO [25]
1	628.2986	538.5587	538.560
2	149.0807	224.6416	224.70
3	223.8643	149.8468	150.09
4	109.6659	109.8666	109.87
5	109.6171	109.8666	109.87
6	109.8320	109.8666	109.87
7	60.0000	109.8666	109.87
8	109.8660	109.8666	109.87
9	109.7754	109.8666	109.87
10	40.0000	77.4666	77.41
11	40.0000	40.2166	40.00
12	55.0000	55.0347	55.01
13	55.0000	55.0347	55.01
TP (MW)	1800	1800	1800
Cost (\$/h)	17964.469	17969.17	17969.01

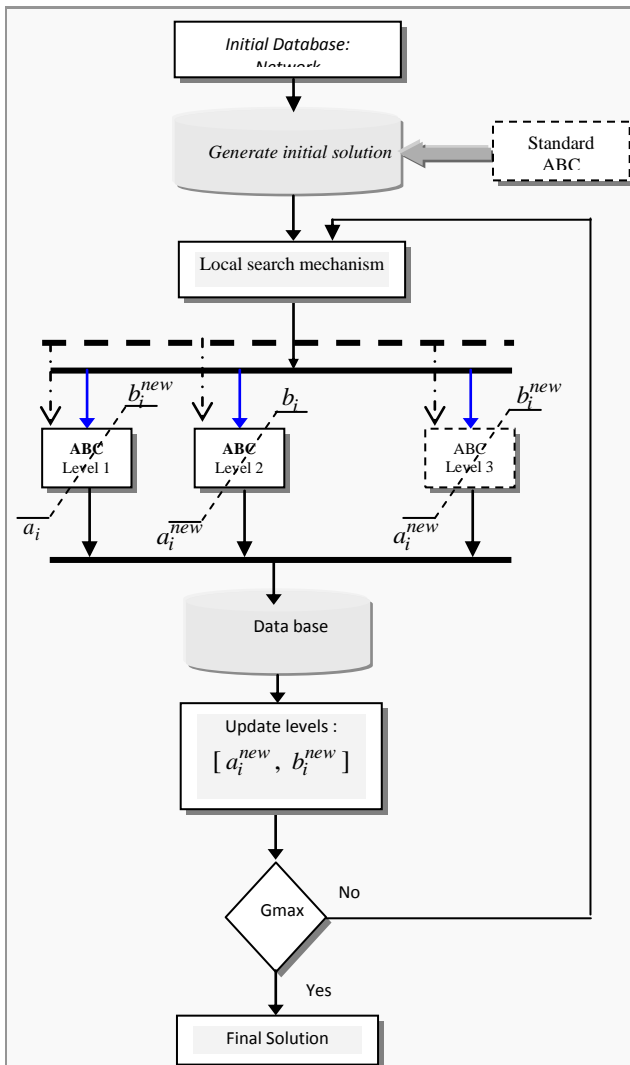


Fig. 4. Proposed IABC based dynamic local search mechanism.

IV. CASE STUDIES

In order to investigate the robustness and performance of the proposed variant termed IABC algorithm, two standard practical electrical test systems are considered, 13 generating units and to the 40 generating units considering valve-point loading effects.

A Test System 1: 13 generating units with valve loading effects

This test system consists of 13 generating units with consideration of valve-point loading effects, the total load demand expected to be satisfied was PD= 1800 MW. The power losses are ignored in this case. The convergence of the IABC process is shown in Figure 5. The best results were compared to many recent global optimization

techniques. Table 2 shows the optimal solutions obtained by the proposed approach based IABC method for the 13 generating units. Table 3 shows a comparative study with various recent global optimization methods cited in the literature [24-25]. Figure 6 shows convergence characteristics comparison of ABC and the proposed IABC.

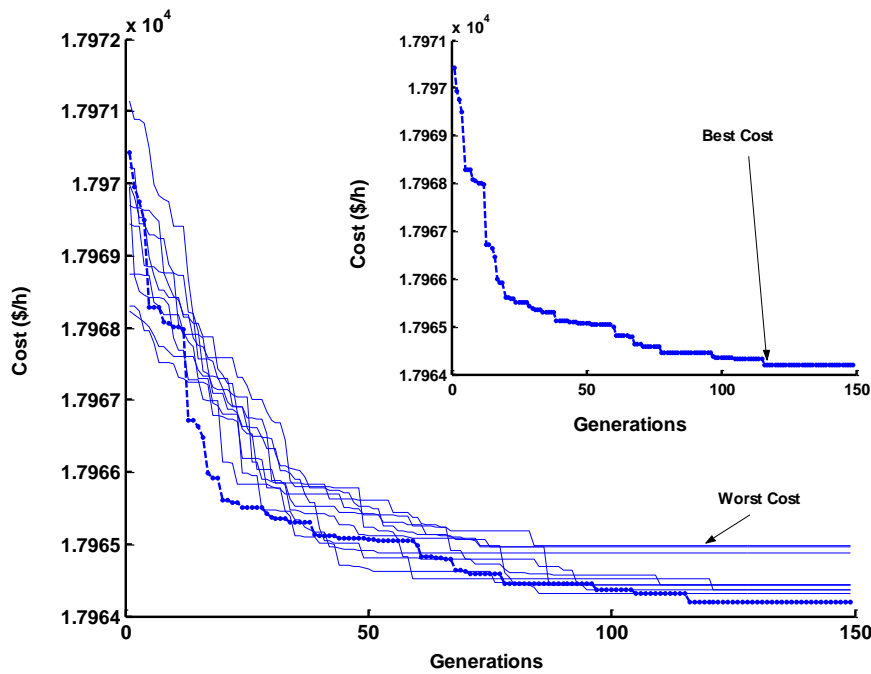


Fig. 5. Convergence characteristic: test system 1: 13 generating units using the proposed IABC.

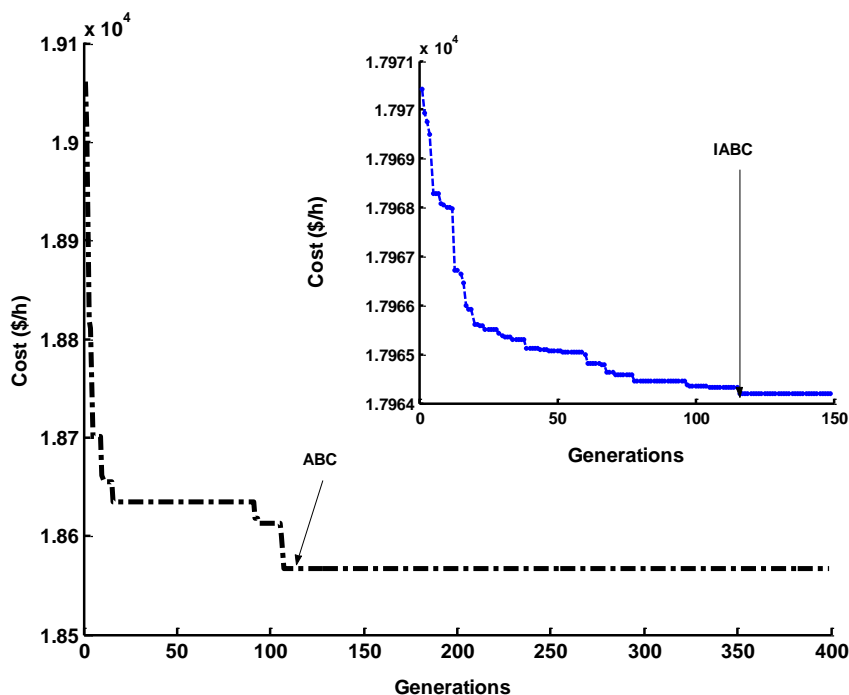


Fig. 6. Convergence characteristic: test system 1: using ABC and IABC.

Table 3. COMPARISON OF BEST RESULTS FOR FUEL COSTS: CASE STUDY 13 THERMAL UNITS.

Methods: Ref [28]	Minimum Cost (\$/h)	Average Cost(\$/h)
CEP	18048.21	18190.32
FEP	18018.00	18200.79
MFEP	18028.09	18192.00
IFEP	17994.07	18127.06
EGA	18019.15	18144.95
FIA	18014.61	18136.97
SPSO	17988.15	18102.48
QPSO	17969.01	18075.11
Proposed approach: IABC	17964.469	17965.124

B. Test System 2: Large system: 40 generating units with valve-point loading effects

A system with 40 generators with the valve-point loading effects was studied in this third case. Total load demand of the system is 10500 MW. This is a larger system, the number of local optima, complexity and nonlinearity to the solution procedure is enormously increased. The convergence characteristic of the IABC is shown in figure 7; the best results of the proposed approach compared with other methods are illustrated in Tables 4-5, shows clearly the superiority of the proposed approach.

Table 4. ECONOMIC DISPATCH RESULTS FOR 40-GENERATING UNITS USING THE PROPOSED APPROACH: PD =10500 MW

N°	P_{g_i} (MW)			N°	P_{g_i} (MW)		
	[QPSO] [25]	[DEBBO] [14]	Our Approach		[QPSO] [25]	[DEBBO] [14]	Our Approach
1	111.20	110.7998	110.8266	21	523.28	523.2794	523.2788
2	111.70	110.7998	110.8333	22	523.28	523.2794	523.2796
3	97.40	97.3999	97.3988	23	523.29	523.2794	523.2813
4	179.73	179.7331	179.7341	24	523.28	523.2794	523.2794
5	90.14	87.9576	87.8002	25	523.29	523.2794	523.2811
6	140.00	140.000	139.9999	26	523.28	523.2794	523.2794
7	259.60	259.5997	259.5997	27	10.01	10.00	10.0000
8	284.80	284.5997	284.6077	28	10.01	10.00	10.0000
9	284.84	284.5997	284.6005	29	10.00	10.00	10.0000
10	130.00	130.000	130.0000	30	88.47	97.000	92.6787
11	168.80	168.7998	168.8012	31	190.00	190.000	190.0000
12	168.80	94.000	168.7998	32	190.00	190.000	190.0000
13	214.76	214.7598	214.7597	33	190.00	190.000	190.0000
14	304.53	394.2794	394.2794	34	164.91	164.7998	164.8037
15	394.28	394.2794	394.2790	35	165.36	200.00	164.7999
16	394.28	304.5196	304.5198	36	167.19	200.00	164.8005
17	489.28	489.2794	489.2794	37	110.00	110.0000	110.0000
18	489.28	489.2794	489.2794	38	107.01	110.0000	110.0000
19	511.28	511.2794	511.2798	39	110.00	110.0000	110.0000
20	511.28	511.2794	511.2795	40	511.36	511.2794	511.2797
TP (MW)					10,500	10,500	10,500
TC (\$/h)					121448.21	121420.89	121414.749

TP: Total Power Generation, TC: Total Cost

Table 5. COMPARISON OF THE PROPOSED APPROACH WITH OTHER GLOBAL OPTIMIZATION METHODS 40-GENERATING UNITS PD =10500 MW

Methods: Ref [28]	Minimum Cost(\$/h)	Average Cost(\$/h)
CEP	123488.29	124793.48
FEP	122679.17	124119.37
MFEP	122647.57	123489.74
IFEP	122624.35	123382.00
EGA	122022.96	122942.66
FIA	121823.80	122662.48
SPSO	121787.39	122474.40
QPSO	121448.21	122225.07
<i>Proposed Approach: IABC</i>	121414.749	121423.145

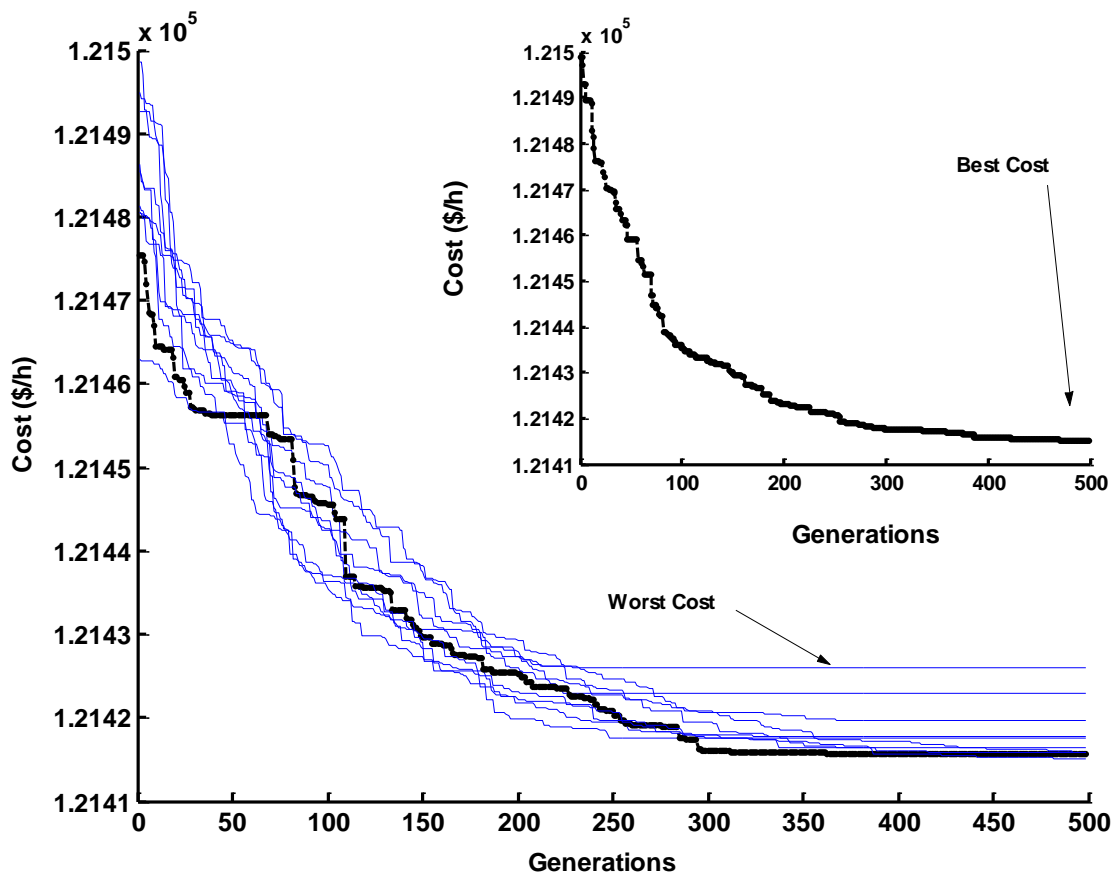


Fig. 7. Convergence characteristic: test system 3: 40 generating units.

V. CONCLUSION

In this paper, a new variant algorithm based artificial bee colony termed IABC has been successfully adapted and applied for solving practical economic dispatch taking into account the nonlinear generator characteristics such as valve-loading effects. A new coordinated local search mechanism (LSM) associated to the original ABC algorithm; it allows exploiting effectively the promising region to locate the best solution. The performance of the proposed approach has been tested with three standard test systems: the 13 generating units with valve point effect, and to the large electrical test system, 40

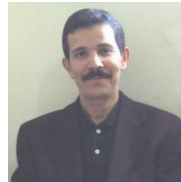
generating units considering the valve-point loading effects. The results of the proposed strategy compared with many recent global optimization methods. It is observed that the proposed variant based ABC is capable to improving the solution of large economic dispatch considering practical generator constraints.

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