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Article

Keywords: Kagome-lattice, 3d-transition Metals, Novel Quantum Phases, Magnetic Kagome Materials, Angle-resolved Photoemission Spectroscopy, Multi-orbital Magnetism

Posted Date: December 4th, 2020

DOI: <https://doi.org/10.21203/rs.3.rs-114140/v1>

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Version of Record: A version of this preprint was published at Nature Communications on May 25th, 2021. See the published version at <https://doi.org/10.1038/s41467-021-23536-8>.

Spin-polarized Dirac cone, flat band and saddle point in kagome magnet YMn_6Sn_6

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Kagome-lattice of 3d-transition metals hosting Weyl/Dirac fermions and topological flat bands exhibit non-trivial topological characters and novel quantum phases, such as anomalous Hall effect and fractional quantum Hall effect. With consideration of spin-orbit coupling and electron correlation, several instabilities could be induced. The complete characters of the electronic structure of kagome lattice, *i.e.* the saddle point, Dirac-cone, and flat band, around the Fermi energy (E_F) remain elusive in magnetic kagome materials. We present the first experimental observation of the complete features in ferromagnetic kagome layers of YMn_6Sn_6 helically coupled along the c -axis, by using angle-resolved photoemission spectroscopy and band structure calculations. We demonstrate a Dirac dispersion near E_F arising from a spin-polarized orbital, which carries an intrinsic Berry curvature and contributes to the anomalous Hall effect in transport measurements. In addition, a flat band and a saddle point with a high density of states and with orbital-selective characters near E_F are observed. These multi-orbital kagome features could cause multi-orbital magnetism. The Dirac fermion, flat band and saddle point in the vicinity of E_F open an opportunity in manipulating the topological properties in magnetic materials.

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The frustrated kagome lattice, made up of the geometry of corner-sharing triangles, has been studied intensively due to the magnetic frustration-induced quantum spin liquid state [1, 2]. Meanwhile, the construction of topological band theory in recent years has greatly enriched in the electronic band structure of kagome lattice [3–5]. Theoretical studies show the kagome lattice systems as an ideal platform for understanding the topological states with novel topological excitations [6–8]. For example, a flat band (FB) can be constructed by completely destructive interference of Bloch wave functions in two-dimensional (2D) kagome lattice with nearest-neighbor (NN) interaction. Such FBs, just like a counterpart of the Landau level, can be characterized by a Chern number [3, 7]. Representing a highly degenerate and quenched kinetic energy of electron state may give rise to the abundant exotic emergent effects, such as ferromagnetism, high-temperature superconductivity, Wigner crystal, and fractional quantum Hall effects [9–16]. Besides, the kagome lattice system shares similar topological physics with honeycomb, Dirac cone-type dispersions in the momentum-space K point. Once a net magnetization and intrinsic spin-orbit coupling (SOC) are present, a well-separated non-trivial Chern bands, Chern gap and intrinsic quantum anomalous Hall effect could present when the Fermi energy (E_F) is tuned properly [17, 18].

The band structure studies of $3d$ transition-metal kagome compounds, which are usually strong correlated and exhibit magnetism, remain challenging albeit theoretical predictions [19–32]. A typical electronic structure of the kagome lattice is the existence of Dirac point (DP) at the Brillouin zone (BZ) corner, a saddle point (SP) at BZ boundary, and a FB over the whole BZ (Fig. 1b). Topological non-trivial electronic properties were observed in kagome lattices constituted of $3d$ -transition metallic element, *i.e.*, large intrinsic anomalous Hall effect originating from the Berry curvature of Dirac cone-type dispersion of K point both in ferromagnetic (FM) and antiferromagnetic (AFM) materials [18, 20–24]. Another important feature is the dispersionless electronic structure in magnetic kagome materials [25, 30–32] and in paramagnetic (PM) kagome materials [27–29]. In PM kagome materials, extremely flat bands close to E_F have been reported in CoSn [28, 29] and YCr₆Ge₆ [27]. However, in magnetic systems, the direct evidence of the FBs is either unobserved (Fe₃Sn₂, Co₃Sn₂S₂ [22, 30]), or far away from E_F (FeSn [25]), due to the strong correlation of $3d$ electrons, the complexity with magnetic structure, and the interplay between electron correlation and topological properties. Thus, searching for the FBs, and saddle point, in addition to the Dirac fermions near E_F in magnetic kagome systems serves as the main objective to manipulate the topological properties in magnetic materials.

In this paper, we study the electronic structure of kagome lattice YMn₆Sn₆ with in-plane ferromagnetism and helical anti-ferromagnetism along c -axis by combining angle-resolved photoemission spectroscopy (ARPES) and density functional theory plus dynamical mean-field theory (DFT+DMFT) calculations. We report the first experimental observation of the complete characters of kagome electronic structure: Dirac cone, flat band and saddle point, in such a magnetic system. One complete set of the characteristic of kagome lattice includes a Dirac point (DP1) above E_F , a saddle point (SP) near E_F and a flat band (FB1) locates at ~ 0.4 eV below E_F across the whole BZ. They show negligible k_z dispersion, suggesting the major 2D characters of the kagome structure in YMn₆Sn₆. The DFT+DMFT calculations with orbital-resolved electronic structures further confirm the 2D features with the in-plane orbital composition of $d_{xy}/d_{x^2-y^2}$. Moreover, we detected the existence of extra kagome characters, including a Dirac point (DP2) and a flat band (FB2) in the vicinity of E_F . The DP2 has a $d_{xy}/d_{x^2-y^2}$ with mixture of d_{z^2} orbital character, and presents a weak dispersion along k_z , while the FB2 is mainly dominated by d_{xz}/d_{yz} orbitals. In the presence of SOC, the flat band and Dirac point have Chern numbers arising from the non-trivial Berry phase and supporting the orbital magnetism [32]. Altogether, these topological non-trivial bands in the kagome material will help understand the relationship between electronic/magnetic correlation and peculiar lattice geometry, and open an opportunity in manipulating the topological properties in magnetic materials.

Results

The crystal structure and transport property of YMn₆Sn₆. Kagome compound YMn₆Sn₆ has a hexagonal structure with space group $P6/mmm$ (No. 191). It contains three kinds of Sn sites, stacking of Y-Sn3 layer and Mn-Sn1-Sn2-Sn1-Mn slab, with double Mn kagome lattice layers as shown in Fig. 1c. The Sn2 atoms form the honeycomb lattice located at the center of Mn-Sn1-Sn2-Sn1-Mn slab. As for the Mn kagome layers, neutron diffraction experiments reported FM coupling in each kagome bilayer, along with c -axis AFM coupling between the bilayer to the next bilayer below room temperature [33, 34].

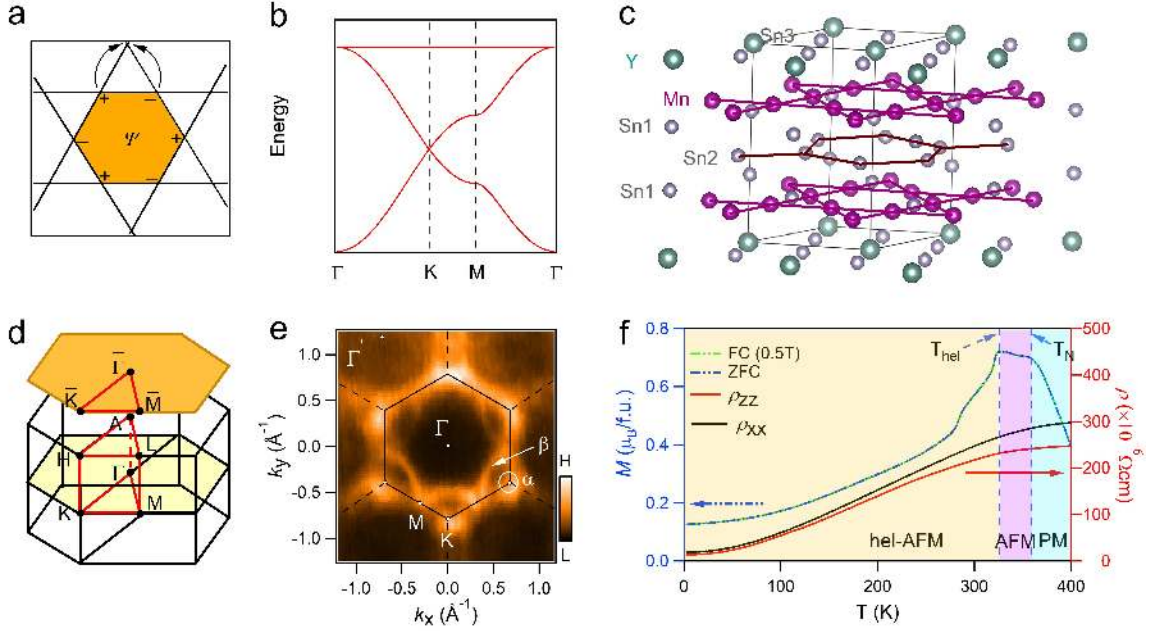


Fig. 1 Crystal and electronic structures of YMn_6Sn_6 . (a) Confinement of electron eigenstate induced by destructive interference in kagome lattice with NN hopping. (b) Tight-binding calculation of band structure of kagome lattice with NN in-plane hopping without SOC, featuring the Dirac cone at the BZ corner K point, a saddle point at BZ boundary M point, and a FB over the whole BZ. (c) Crystal structure of YMn_6Sn_6 with space group $P6/mmm$ (No. 191). (d) 3D and projected BZs of YMn_6Sn_6 with marked high-symmetry points. (e) Photoemission intensity plot measured with 138-eV photons at $E_F \pm 10$ meV in the $k_z \sim 0$ plane. Hexagonal BZs are marked with black lines. (f) Magnetization as a function of temperature with zero field-cooling and field-cooling at $B = 0.5$ T along the $[100]$ direction. Temperature dependence of longitudinal resistivity ρ_{xx} and ρ_{zz} with zero-field.

46 Figure 1d shows the 3D BZ with high-symmetry points and projected BZ along c -axis. In Fig. 1e, the integrated intensity at E_F
 47 ± 10 meV obtained from ARPES measurement at $k_z \sim 0$ plane is shown to represent the Fermi surfaces. There exist two pockets
 48 centered at \bar{K} point as marked, both with strong matrix element effects. The large one (β) is clearly identified in the 1st BZ
 49 but weaker in the 2nd BZ. It looks like an “arc-like” band in the 1st BZ and crosses the zone boundary near M , forming a closed
 50 “triangle”-like Fermi pocket. The small one (α) is more clearly visible in the 2nd BZ than in the 1st BZ, and forms a smaller
 51 pocket around \bar{K} . Figure 1f shows the magnetization as a function of temperature with zero field-cooling and field-cooling at
 52 $B = 0.5$ T along the $[100]$ direction. Two transformative peaks at $T_N = 359$ K and $T_{hel} = 326$ K are observed. The former
 53 temperature corresponds to the paramagnetism-antiferromagnetism phase transition. The latter corresponds to a transition from
 54 an AFM order along the c -axis above T_{hel} to a c -axis helical order with in-plane FM order at low temperature, consistent with
 55 the previous results [33–36]. Moreover, the temperature dependence of longitudinal resistivity ρ_{xx} and ρ_{zz} with zero-field shows
 56 a metallic behavior with weak anisotropy, similar to $GdMn_6Sn_6$ [37].

57 **The complete characteristics of kagome structure.** In order to investigate the kagome lattice related topological electronic

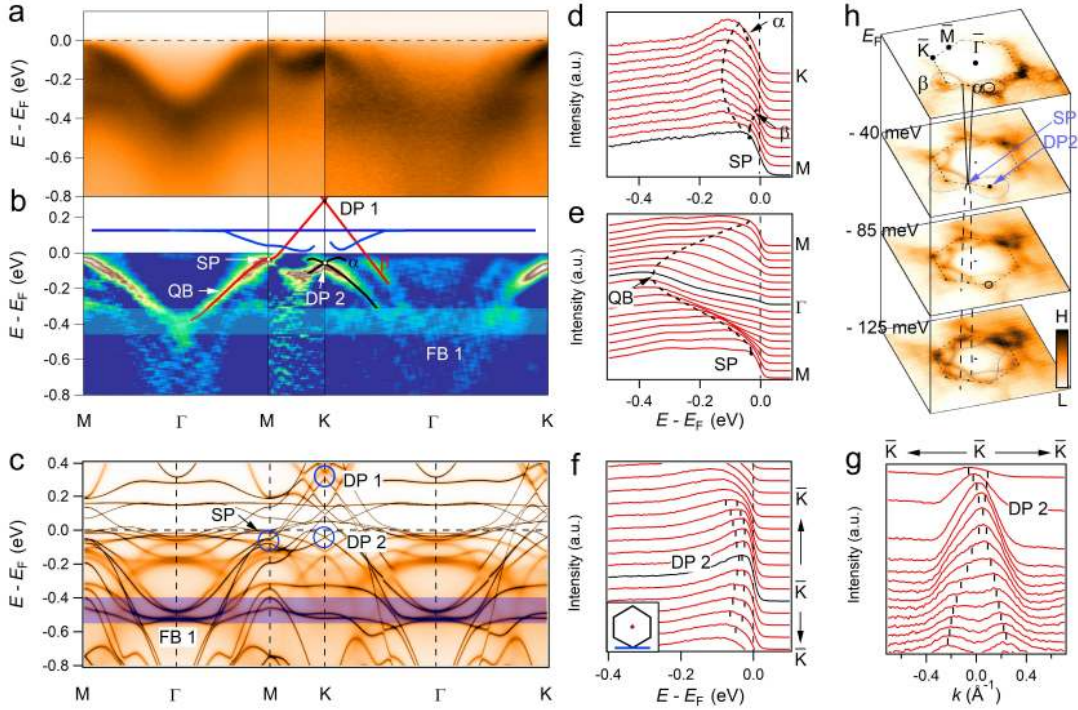


Fig. 2 Band structure evolution in the 1st BZ. (a) Photoemission intensity plots of YMn_6Sn_6 along Γ - M - K - Γ in the $k_z \sim 0$ plane. (b) Corresponding second derivative plots of (a). The blue-colored region highlights the manifestation of the kagome flat band at the binding energy of about 0.4 eV. The appended colored lines serve as guides to the bands, which are extracted from DFT+DMFT calculations. (c) DFT+DMFT calculated ARPES in the FM state with SOC and with the experimentally determined E_F shifted downwards about 76 meV. Dirac point (DP1 and DP2), saddle point (SP) and flat band (FB1) are indicated by the blue circles and blue-colored region, respectively. (d,e) EDC plots along K - M and M - Γ - M , respectively. (f,g) EDC and MDC plots along the \bar{K} - \bar{K} - \bar{K} direction, with the momentum path indicated as inset. (h) Constant energy maps at different binding energies.

58 structure, we measured the band structures in the 1st BZ at $k_z \sim 0$ plane along with the high-symmetry lines. The intensity plots
 59 along the Γ - M - K - Γ line and the corresponding second derivative plots are shown in Fig. 2a, 2b, respectively. Along Γ - M , one
 60 can clearly see a quadratic band (QB) with its bottom at about 0.4 eV below E_F at Γ dispersing upward towards M , and gradually
 61 becoming flat at the M point. Along M - K , an electron-like band disperses linearly upward towards E_F and crosses E_F about
 62 one third between M and K , labeled as β in Fig. 1e. At M point, it conforms to the dispersion of SP at $E_B \sim 40$ meV, as marked
 63 in Fig. 2b. From intensity plot along Γ - K , the β band passes through the E_F , forming a large holelike FS around K point, which
 64 can be more clearly seen in second derivative plots (Fig. 2b). This β band forms a Dirac point (DP1) at about 0.3 eV above E_F ,
 65 as indicated by the blue circle in Fig. 2c. Another feature is a flat band at about 0.4 eV below E_F , FB1, which exists through
 66 the whole BZ. It can be regarded as a direct consequence of quantum phase interference effects in the kagome lattice, as shown
 67 in Fig. 1a. This flat band feature has a narrow bandwidth and the intensity is enhanced along Γ - K due to the matrix element
 68 effect. The band dispersion closely follows the DFT+DMFT calculations shown in Fig. 2c. In particular, it exhibits the complete
 69 characteristics of kagome electronic structure, a flat band (FB1) over the whole BZ touching a quadratic band at Γ point that
 70 emerges from the Dirac band (DP1) at K point and forms a saddle point (SP) at M .

71 At the K point, a linearly dispersing Dirac point (DP2) is also found at around 45 meV below E_F , which is also characteristic
 72 of the band structure as a result of kagome lattice as previously observed in FeSn and CoSn [25, 28, 29]. According to our
 73 DFT+DMFT calculated orbital-resolved electronic structures in FM configuration, the DP2 arises from the spin-polarized band

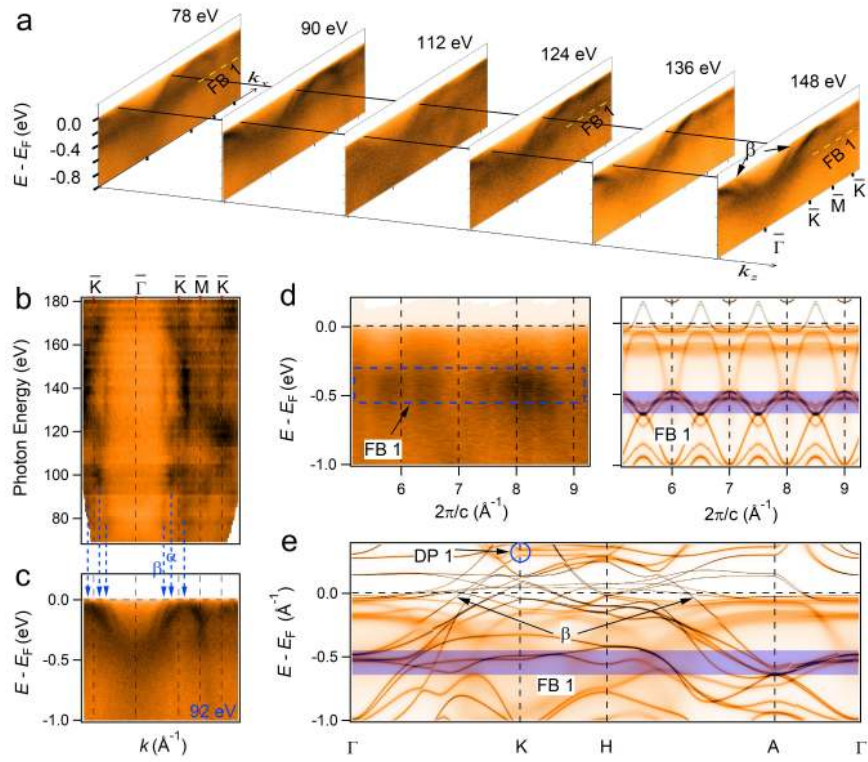


Fig. 3 Photon-energy-dependence measurement of YMn_6Sn_6 . (a) Photoemission intensity plots of YMn_6Sn_6 with variable photon energies along $\Gamma(A)-K(H)$, the flat band (FB1) locates at the binding energy of about 0.4 eV through the whole BZ. The β band appears in every photon energy. (b) ARPES intensity map at E_F in the $k_{\parallel}-k_z$ plane with variable photon energies along $\Gamma(A)-K(H)$, showing a well defined 2D-like band structure. (c) Energy-momentum dispersion of YMn_6Sn_6 measured at $h\nu = 92$ eV ($k_z \sim 0.6 \pi/c$). (d) Photoemission intensity plot and DFT+DMFT calculated ARPES in the FM state with SOC along the $\Gamma-A$ direction, respectively. (e) DFT+DMFT calculated ARPES in the FM state with SOC along $\Gamma-K-H-A-\Gamma$, with the experimentally determined E_F shifted downwards about 76 meV. The blue-colored region highlights the manifestation of the kagome flat band.

74 with minority-spin state, as shown in the Fig. S5. The DP2 can be also clearly seen from the energy distribution curves (EDCs)
 75 and momentum distribution curves (MDCs) in Fig. 2f and Fig. 2g, respectively. With consideration of SOC, a small bandgap
 76 <10 meV opens at DP2, adding a mass term to the linearly dispersive band, and a massive Dirac fermion thus can be formed.
 77 In consideration of in-plane FM configuration, it could realize a spin-polarized Dirac fermion with a non-trivial Chern gap in
 78 YMn_6Sn_6 as previously observed in TbMn_6Sn_6 by scanning tunneling microscopy/spectroscopy (STM/S) measurement [18].
 79 In our result, this non-trivial Dirac fermion is in the occupied state and closer to E_F than in TbMn_6Sn_6 , and contributes to the
 80 intrinsic anomalous Hall effect in transport measurement [38].

81 Figure 2h shows a series of constant energy evolution maps in the $k_z \sim 0$. We notice that the β band constitutes a hole pocket
 82 and the α band holds an electron pocket around K point. Along with the energy going from E_F to higher binding energy, the hole
 83 pockets gradually expand and the branches of β band get closer to each other along $K-M-K$, finally, touching at SP with the
 84 binding energy of ~ 40 meV. Further away from the SP, the band forms a hole band along $\Gamma-M$. At M point, the band dispersion
 85 conforms a SP at ~ 40 meV below E_F . The α pocket firstly shrinks into a single point and then expands forming a DP at about
 86 $E_B = 45 \pm 10$ meV.

87 In Figs. 3a and 3b, we show the ARPES data along $\Gamma-K-M-K$ with photon energies from 70 to 180 eV, which covers near
 88 four BZs along k_z . In Fig. 3a, one can see that the band dispersions show no qualitative change at various photon energies.
 89 Especially, the β band shows no noticeable k_z dependence, which is better identified by the constant crossing point of $k_{F,\parallel}$ in

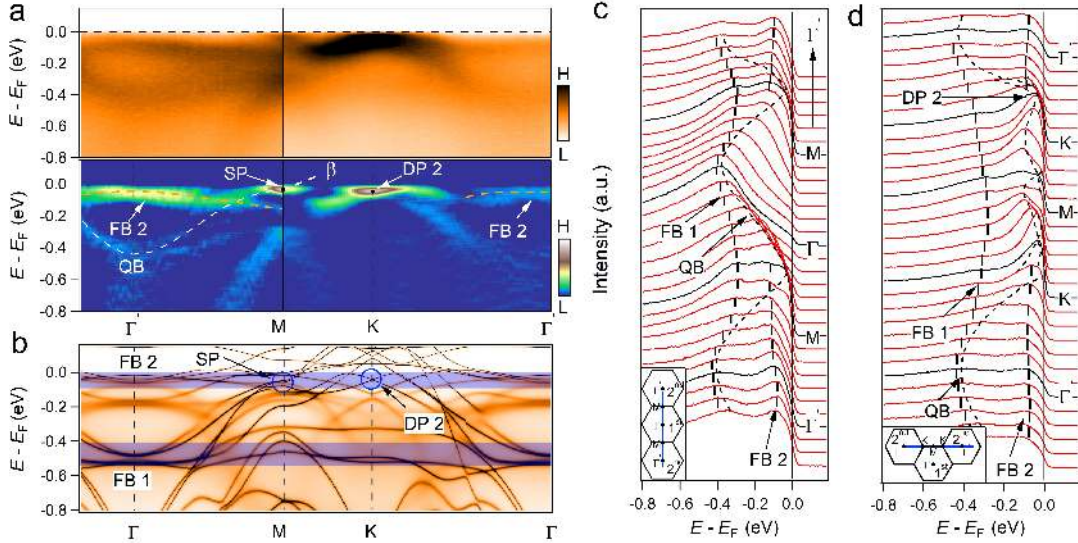


Fig. 4 Band structure evolution in the 2nd BZ. (a) Photoemission intensity plots and corresponding second derivative plots of YMn_6Sn_6 in 2nd BZ along Γ -M-K- Γ in the $k_z \sim 0$ plane. The dashed lines are served as guides to the eyes. (b) DFT+DMFT calculated ARPES in the FM state with SOC to according to the corresponding path of (a) and with experimental E_F . Dirac point (DP2), saddle point (SP) and flat band (FB) are indicated by the blue circles and blue-colored regions, respectively. (c,d) EDC plots along the high-symmetry lines, with the momentum paths indicated as inset. The flat bands (FB1 and FB2) and the parabolic band (QB) are indicated by the black dashed lines with thick and thin, respectively.

90 Fig. 3b. The FB1 at about 0.4 eV below E_F is also presented in every photon energy, with a limited bandwidth (does not exceed
 91 150 meV) along Γ -A as shown in Fig. 3d, indicating a near 2D character of the band. Figure 3b shows the integrated intensity
 92 at $E_F \pm 10$ meV in Γ K-AH plane which covers part of K-M-K at extended in-plane BZs. The β band shows a little variation,
 93 further confirms the 2D-like character and ensures the 2D Dirac cone of DP1. The Dirac-related α band around \bar{K} also displays
 94 a negligible dispersion along k_z , while one branch has a strong intensity modulation around the Dirac fermion associated with
 95 strong matrix element effect, similar to FeSn and CoSn [25, 29]. All the k_z dependence supports the quasi-2D characters of the
 96 DP1, DP2 and FB1 bands. An explanation of the 2D-like band structure is that the bands mainly originate from the orbitals
 97 confined by the kagome lattice.

98 To confirm the speculation of the orbital characters in the helical magnetic state along c -axis, we carry out the DFT+DMFT
 99 calculations in FM configuration with SOC and show the results in Fig. 3e and Fig. S4. In the DFT+DMFT calculated spectra,
 100 we downshift the chemical potential of 76 meV to match the experiment value E_{exp} mostly caused by a chemical doping of
 101 the sample. The DFT+DMFT calculated orbital-resolved ARPES in FM configuration without SOC is shown in Fig. S5. The
 102 calculations in the FM configurations agreed well with the observation, it shows that the β band mainly originates from the
 103 minority-spin branch of $d_{xy}/d_{x^2-y^2}$ orbitals. It forms the DP1 at ~ 0.3 eV above E_F and shows negligible dispersion along K-H
 104 as shown in Fig. 3e. The FB1 passing through the whole in-plane BZ originates from the minority-spin branch of the in-plane
 105 $d_{xy}/d_{x^2-y^2}$ orbitals, and has a limited bandwidth at the entire BZ district.

106 **Signature of phase-destructive flat band near E_F .** A feature that is faint in the 1st BZ but more clearly visible in the 2nd BZ is

107 the existence of another flat band near E_F at the BZ center, labeled as FB2 in Fig. 4. In Fig. 4a, the ARPES intensity plots and
 108 the corresponding second derivative plots along the Γ - M - K - Γ lines of the 2nd BZ at $k_z \sim 0$ plane are shown. In the 2nd BZ, a
 109 spectral weight close to E_F with binding energy $\sim 60 \pm 20$ meV is clearly seen and extends over a large part of the BZ except
 110 around the K points due to the intensity leakage from the Dirac bands. In comparison, the intensity of the β and FB1 bands
 111 are stronger in the 1st BZ but become feeble in the extended BZ. We assign the contrasting behaviors between FB2 and FB1+ β
 112 bands to the strong matrix element effect [27, 39] due to the different parity, symmetries or spin-polarization of the bands. In
 113 Fig. 4b, we present the DFT+DMFT calculations of the band structure in the FM state with SOC, with a downshift adjustment of
 114 the chemical potential of 76 meV as in Fig. 3e. Figure 4c, 4d show EDC plots over more than one BZ along the high-symmetry
 115 line as marked in the insets. The contrast of the intensity among different BZs is shown, and the flat bands (FB1 and FB2) and
 116 the Dirac point (DP2) can be confirmed unambiguously. For the FB1, it is degenerate with the QB bottom at the center of the
 117 BZ (Γ) without SOC. With the consideration of SOC, the two bands further hybridize and open a gap $\sim 40 \pm 10$ meV, which
 118 is similar to the results in PM CoSn [28]. The FB2 declines weakly close to M and K points. It is noticed that the peak width
 119 becomes broader and the intensity becomes weaker near M and K points, which cause the expected Dirac points feature blurry
 120 and nearly indistinguishable and in agreement with the DFT+DMFT calculations in Fig. 4b. In conventional DFT calculations,
 121 there should be more band features in magnetic state, and several kagome-related structures are expected. However, in the
 122 DFT+DMFT calculations with consideration of correlation effect which is normally present in magnetic system, the broadness
 123 and the weaker intensity cause the smearing out of the band, *e.g.* some band features around M , K and along M - K .

124 We also present the evolution of the FB2 as a function of out-of-plane momentum k_z measured in the in-plane-2nd-BZ along
 125 Γ '- A' as shown in Fig. S3. The FB2 displays a weak dispersion over more than one BZ along k_z . Combining its in-plane flat
 126 dispersion in the $k_z \sim 0$ plane, weak dispersion along k_z , and the DFT+DMFT calculated orbital-resolved ARPES as shown
 127 in Fig. S5, we assign the orbital character of FB2 to d_{xz}/d_{yz} orbitals. It is worth notice that there exists an out-of-plane d_{z^2}
 128 orbital with a steep k_z dispersion and crossing E_F at certain k_z , it thus might contribute to the c -axis conductivity in our transport
 129 measurements. Further, the FB1 displays a limited bandwidth (<150 meV) along k_z in the 2nd BZ as shown in Fig. S3. It
 130 is consistent with results in the 1st BZ with the in-plane $d_{xy}/d_{x^2-y^2}$ orbital composition, as discussed earlier. According to the
 131 spin-polarized DFT+DMFT calculations, FB2 with a high density of states (DOS) around the E_F is from the majority-spin state,
 132 indicating its singly spin degenerate origin. FB2 is the first momentum-space evidence of the flat band really close to E_F in the
 133 magnetic kagome system, which could give interesting phenomena such as orbital magnetism [32].

134
 135 **The band calculations and discussions.** To take into account the strong electronic correlation effect of the Mn 3d electrons, in
 136 the DFT+DMFT calculations, we include an onsite Coulomb interaction parametrized with a Hubbard $U = 4.0$ eV and a Hund's
 137 coupling $J = 0.7$ eV among the Mn 3d electrons in both the PM and FM states. In the PM state, the mass enhancements of the
 138 Mn 3d electrons near the E_F are about 5-7, which are similar to the values in some iron chalcogenide superconductors [40]. The
 139 fluctuating local moment of Mn 3d electrons, namely, the average value of $g[S(S + 1)]^{1/2}$, is about $3.9 \mu_B$ with an effective spin
 140 $S=1.5$, indicating YMn₆Sn₆ has a large fluctuating local moment due to the Hund's rule coupling. Combining with its metallic
 141 behavior, we conclude that YMn₆Sn₆ is a strongly correlated Hund's metal [40].

142 When the Mn 3d local moments are partially frozen and form long-range static FM order in the hexagonal ab plane, the mass
 143 enhancements of the Mn 3d electrons near the E_F are substantially reduced to about 2-3. The fluctuating local moment of Mn
 144 3d electrons remains the same value as in the PM state whereas the statically ordered moment is $2.1 \mu_B$, which is in excellent
 145 agreement with experimental measurement [33, 38].

146 In the PM state, the YMn₆Sn₆ has two major characters, including the strong electronic correlation and the kagome related
 147 features. The kagome structure has a flat band, while the strong correlation gives extra mass enhancement. These combinations
 148 will contribute large DOS around E_F and could cause several instabilities, such as charge density waves [41], superconductivity
 149 [12, 42] or magnetic instability [9, 43]. In the magnetic state, the spin degeneracies are lifted, and a few spin-polarized branches
 150 shift below E_F . ARPES data reveal the existence of flat band with large DOS and Dirac point near E_F in YMn₆Sn₆, these bands
 151 are thus of singly spin degenerate branches. With consideration of SOC, Chern gaps are opened and Chern numbers are assigned

152 to each band correspondingly.

153 These spin-polarized bands carry Berry curvatures and also cause the orbital magnetism. The existence of an orbital magnetic
154 moment has been reported in $\text{Co}_3\text{Sn}_2\text{S}_2$, and was attributed to the kagome flat band [32]. However, the ARPES observation
155 of flat band near E_F has not been reported in $\text{Co}_3\text{Sn}_2\text{S}_2$ yet. The orbital magnetism of the flat band of tight-binding model in
156 kagome lattice with Kane-Mele SOC was calculated in Fig. S7, which is closely related to the Berry curvature. Both the FB
157 with non-zero group velocity part and the massive Dirac fermion will contribute to the orbital magnetism. Our ARPES results
158 first reveal FB and Dirac fermion near E_F with orbital-selective characters, so multi orbital-magnetisms are expected.

159 In summary, based on ARPES measurement and in combination with theoretical calculations, we have fully revealed the
160 band structure of magnetic kagome YMn_6Sn_6 , and presented the first experimental observation of the complete characteristics
161 of kagome lattice near E_F with spin polarization and non-trivial topological properties. The Dirac point and flat band near E_F
162 arise from the spin-polarized band with intrinsic Berry curvature may explain the anomalous Hall effect observed in transport
163 measurements and the orbital magnetic moment observed in STM/S measurement. As an ideal candidate for magnetic kagome
164 lattice material with the electronic structure near E_F , it opens up a new avenue to comprehend the intrinsic properties of magnetic
165 topological electronic material. Furthermore, if the non-trivial band structures—Dirac points, flat band and/or saddle point are
166 further tuned properly, it would possibly realize more versatile quantum phenomena in such material.

167 **Methods**

168 **Sample growth and characterizations** Single crystals of YMn_6Sn_6 were grown by using Sn flux. Y lumps (purity 99.99 %),
169 Mn granules (purity 99.9 %) and Sn grains (purity 99.99 %) with a molar ratio of Y:Mn:Sn=1:6:30 were put into an alumina
170 crucible and sealed in a quartz ampoule under partial argon atmosphere. The sealed quartz ampoule was heated up to 1273 K
171 and held for 24 hours. Then it was cooled down slowly to 873 K at a rate of 5 K/hours. Finally, the ampoule was taken out
172 from the furnace and decanted with a centrifuge to separate YMn_6Sn_6 crystals from excess Sn flux. Magnetization and electrical
173 transport measurements were carried out by using Quantum Design PPMS-14 T.
174

175 **ARPES measurements.** ARPES measurement were performed at the Dreamline and 03U beamline of the Shanghai Synchrotron
176 Radiation Facility (SSRF), and 1-squared ARPES end-station of BESSY. The optimal energy and angular resolutions were set
177 to 20 meV and 0.2° , respectively. Samples were cleaved *in situ* along (001) surface. During the measurements, the temperature
178 was kept at 25 K and the pressure was maintained less than 5×10^{-11} Torr.
179

180 **DFT+DMFT calculations.** The electronic structures of YMn_6Sn_6 were computed by using DFT+DMFT [44]. The DFT part is
181 based on the full-potential linear augmented plane wave method implemented in WIEN2k [45]. The Perdew-Burke-Ernzerhof
182 generalized gradient approximation [46] is used for the exchange correlation functional. DFT+DMFT was implemented on
183 top of WIEN2k and was described in details in Ref. 47. In the DFT+DMFT calculations, the electronic charge was computed
184 self-consistently on DFT+DMFT density matrix. The quantum impurity problem was solved by the continuous time quantum
185 Monte Carlo method [48, 49] with a Hubbard $U = 4.0$ eV and Hund's rule coupling $J = 0.7$ eV. The experimental crystal
186 structure [50] (space group P6/mmm, No. 191) of YMn_6Sn_6 with lattice constants $a = b = 5.512 \text{ \AA}$ and $c = 8.984 \text{ \AA}$ was used in
187 the calculations.
188

189 **ACKNOWLEDGEMENTS** This work was support by the National Natural Science Foundation of China (NO. 11774421,
190 U1875192, 11674030, 11774423, 11822412), the National Key R&D Program of China (Grants NO. 2016YFA0302300,
191 2016YFA0401002, 2017YFA0403401, 2018YFE0202600, 2016YFA0300504), the Fundamental Research Funds for the Cen-
192 tral Universities, and the Research Funds of Renmin University of China (RUC) (18XNLG14, 19XNLG17). Z.P.Y., G. W.,
193 and Z.H.Y. were supported by the Fundamental Research Funds for the Central Universities (Grant No. 310421113). The
194 ARPES experiments were performed on the Dreamline beamline of SSRF and supported by the CAS Pioneer Hundred Talents
195 Program. Part of this research used Beamline 03U of the SSRF, which is supported by ME2 project (11227902) from NSFC. The
196

197 calculations used high performance computing clusters at BNU in Zhuhai and the National Supercomputer Center in Guangzhou.

198

199 **AUTHOR CONTRIBUTIONS** Z.L., Z.P.Y., H.L., and S.W. provided strategy and advice for the research. M.L., W.S., R.L.,
 200 Z.L., Y.H., and S.W. performed the ARPES measurements. Z.P.Y., G.W., and Z.H.Y. performed the theoretical calculations.
 201 Q.W., and H.L. synthesized the single crystals. All authors contributed to the manuscript.

202

203 **Competing Interests**

204 The authors declare no competing interests.

205

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 208 H.L. (hlel@ruc.edu.cn) and S.W. (scw@ruc.edu.cn).

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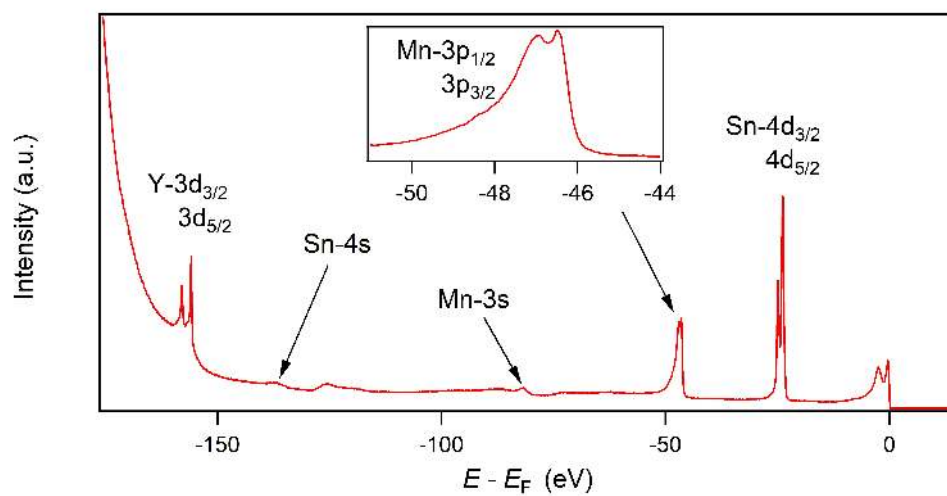
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Supplementary Information:

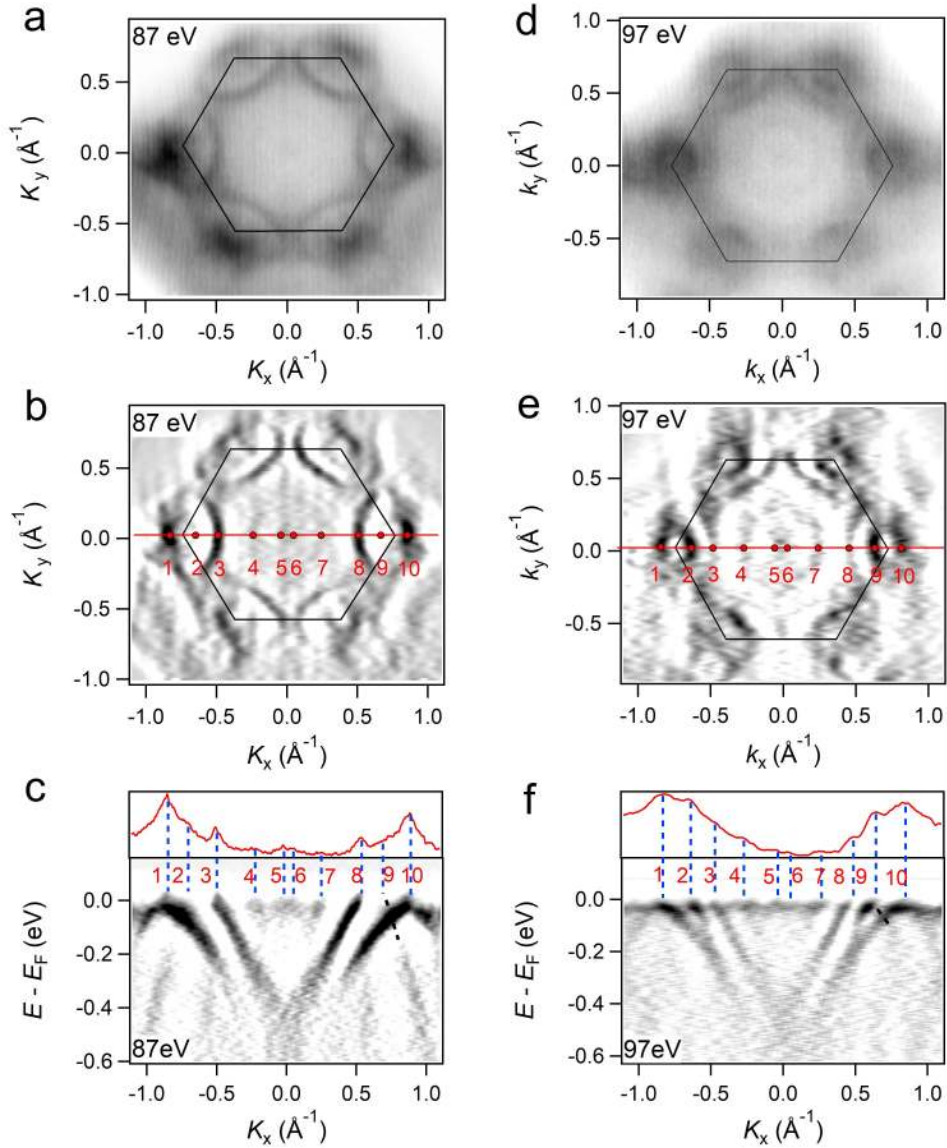
Spin-polarized Dirac cone, flat band and saddle point in kagome

magnet YMn_6Sn_6

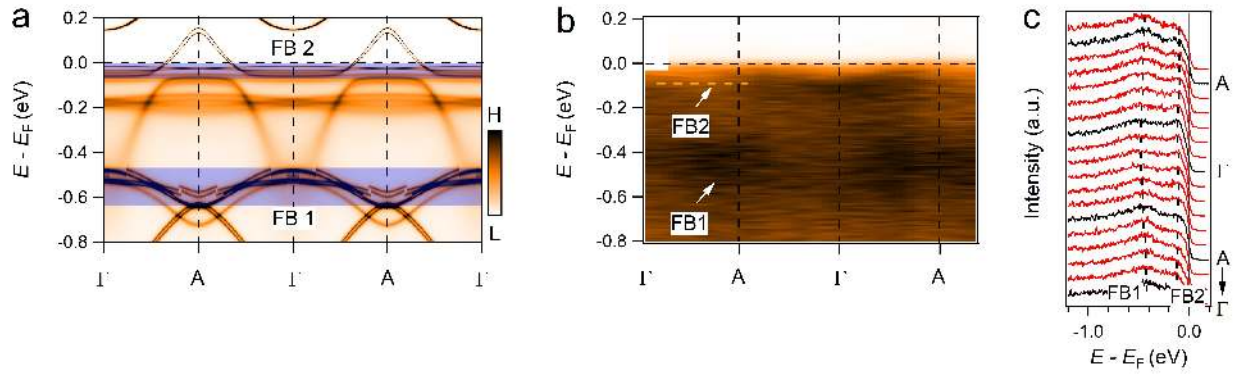
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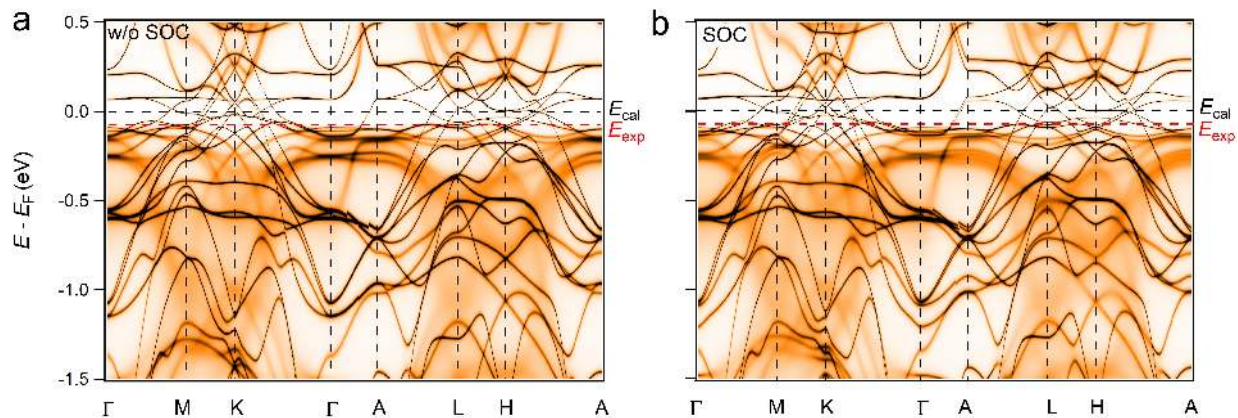
Supplementary Figure 1. Core-level spectrum of YMn_6Sn_6 taken with $h\nu = 200$ eV. The total angular momentum quantum numbers are labelled for peaks.



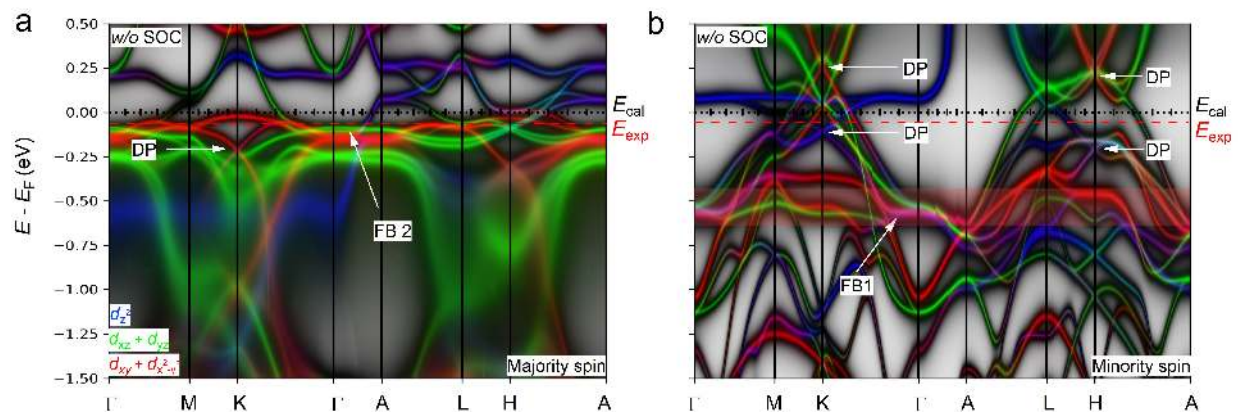
Supplementary Figure 2. (a) Fermi surfaces of YMn_6Sn_6 measured with $h\nu = 87$ eV. The BZ is marked with the black solid hexagon. (b) The corresponding second derivative plot of a. (c) Energy-momentum dispersions of YMn_6Sn_6 along the high-symmetry direction, marked as the solid red line in b. Momentum distribution curve at Fermi energy is overlaid, with a dashed blue line indicating peaks at k_F . (d-f) Same as (a-c), but taken with 97-eV photons.



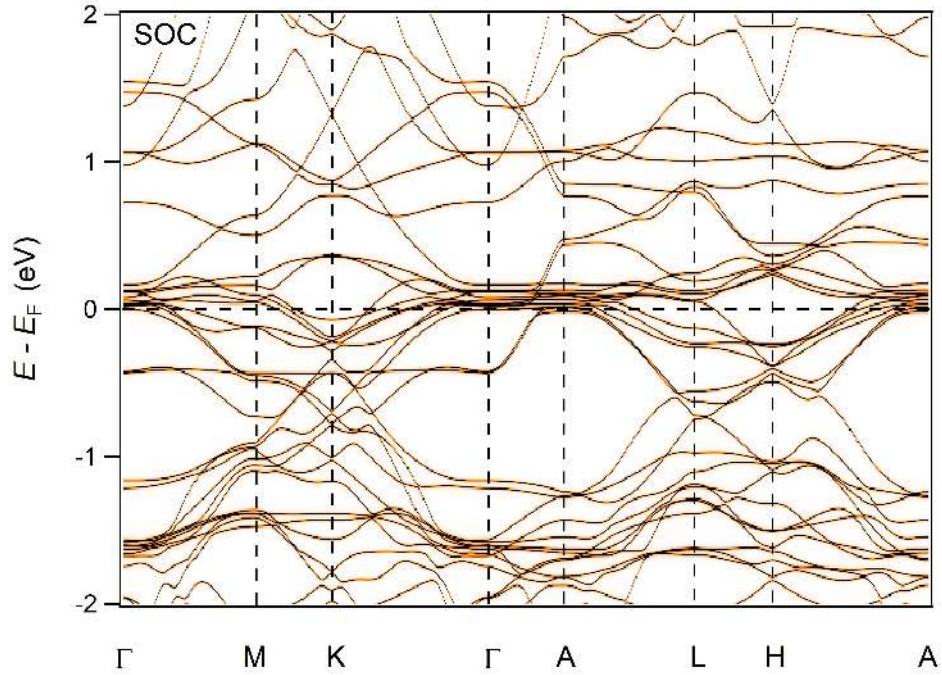
Supplementary Figure 3. (a) The DFT+DMFT calculation in the FM state with SOC along k_z . Flat bands, FB1 and FB2, are indicated by the color-shaded regions. (b) Intensity plot along the Γ -A direction in the in-plane- 2^{nd} BZ. The two flat bands are indicated by the white arrows. The dashed lines are served as guides for eyes. (c) EDCs plot of (b). The FB1 and FB2 are indicated by the black dashed lines.



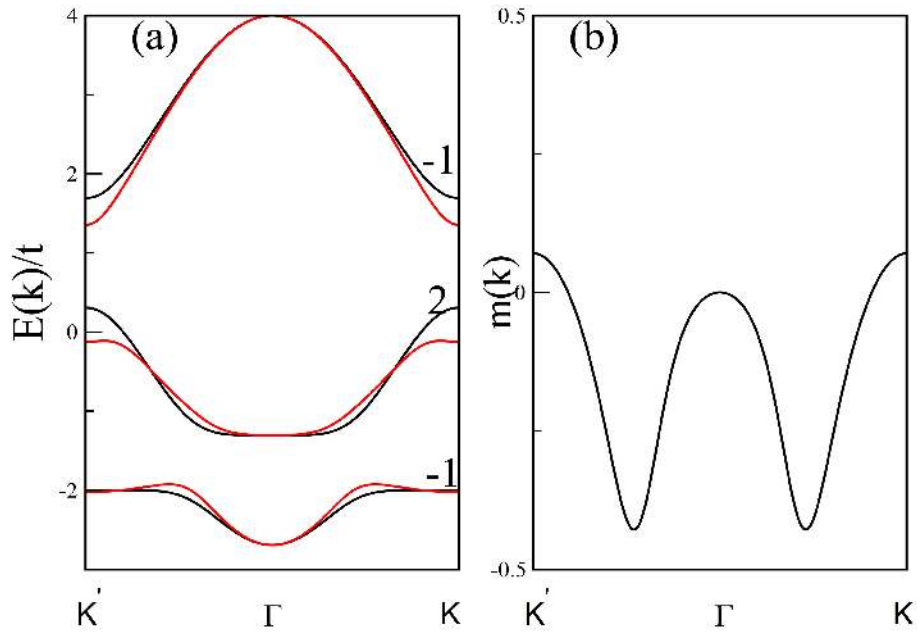
Supplementary Figure 4. The DFT+DMFT calculation of YMn_6Sn_6 in the FM state and (a) without SOC and (b) with SOC along the high-symmetry directions. The dashed red line indicates the experimental Fermi level.



Supplementary Figure 5. The DFT+DMFT calculation with (a) spin-majority and (b) spin-minority states along the high-symmetry directions without SOC and with 3d orbitals projections. The red, green and blue lines indicate the orbitals components of $d_{xy}/d_{x^2-y^2}$, d_{xz}/d_{yz} and d_{z^2} , respectively. The magenta, cyan and light yellow are color mixings of red, green and blue, respectively.



Supplementary Figure 6. The DFT calculation of YMn₆Sn₆ in the nonmagnetic phase with SOC along the high-symmetry directions.



Supplementary Figure 7. (a) Band dispersion along $K' - \Gamma - K$ with $\lambda = 0.2t$. Chern numbers of each band are also shown. Red lines are bands coupling to $m(k)$. (b) $m(k)$ (unit of $\frac{e}{2h}$) of the flat band in (a).

Supplementary Note 1. Sample growth and characterizations. Single crystals of YMn_6Sn_6 were grown by using Sn flux. Y lumps (purity 99.99 %), Mn granules (purity 99.9 %) and Sn grains (purity 99.99 %) with a molar ratio of Y : Mn : Sn = 1 : 6 : 30 put into an alumina crucible and sealed in a quartz ampoule under partial argon atmosphere. The sealed quartz ampoule was heated up to 1273 K and held for 24 hours. Then it was cooled down slowly to 873 K at a rate of 5 K/hour. Finally, the ampoule was taken out from the furnace and decanted with a centrifuge to separate YMn_6Sn_6 crystals from excess Sn flux. Magnetization and electrical transport measurements were carried out by using Quantum Design PPMS-14 T.

Supplementary Note 2. Angle-resolved photoemission spectroscopy experiments. ARPES measurements were performed at the Dreamline and 03U beamline of the Shanghai Synchrotron Radiation Facility (SSRF), and 1-squared ARPES end-station of BESSY. The combined energy resolutions were set to around 20 meV at low photon energies and 28 meV at high photon energies. The angular resolution is 0.2° . Samples were cleaved *in situ*, yielding a flat mirrorlike (001) surface. During the measurements, the temperature was kept at 25 K and the pressure was maintained less than 5×10^{-11} Torr.

We conducted core-level spectroscopy with the photon energy of 200 eV. In supplementary Fig. 1, we present the core-level photoemission intensity plot of YMn_6Sn_6 where the characteristic peaks of Y-3d, Sn-4s/4d, and Mn-3s/3p orbitals are clearly observed, with no extra peaks observed, suggesting the high quality of the crystal and the bulk origin with no surface contribution.

We measured the intensity plots and corresponding second derivative plots of YMn_6Sn_6 with 87-eV and 97-eV photons, as shown in supplementary Fig. 2. The high symmetry cuts with ten crossing points are observed between $K-\Gamma-K$ line, as indicated with blue dotted lines along the solid red line of supplementary Fig. 2b,e. The Dirac cones locate on the marked between the "1" and "2" or "9" and "10". One branch of the Dirac-like bands could be observed and another one is faint due to the matrix element effect associated with the chirality of the Dirac fermions similar to CoSn and FeSn [1, 2].

Supplementary Figure 3 shows the intensity plots along $\Gamma-A$ in the 2nd Brillouin zone (BZ). The FB2 is missed in the first BZ due to the matrix element effect, but clearly presented in the second BZ. The FB1 locates at ~ 0.4 eV below E_F with a narrow bandwidth (< 150 meV). The FB2 locates at ~ 0.06 eV below E_F showing nearly no dispersion along k_z .

Supplementary Note 3. Calculations. The electronic structures of YMn_6Sn_6 were computed by using density functional theory combined with dynamical mean field theory (DFT+DMFT) [3]. The density functional theory part is based on the full-potential linear augmented plane wave method implemented in Wien2K [4]. The Perdew-Burke-Ernzerhof generalized gradient approximation [5] is used for the exchange correlation functional. DFT+DMFT was implemented on top of Wien2K and was described in details in Ref. 6. In the DFT+DMFT calculations, the electronic charge was computed self-consistently

on DFT+DMFT density matrix. The quantum impurity problem was solved by the continuous time quantum Monte Carlo (CTQMC) method [7, 8] with a Hubbard $U=4.0$ eV and Hund's rule coupling $J=0.7$ eV. The experimental crystal structure [9] (space group P6/mmm, No. 191) of YMn_6Sn_6 with lattice constants $a=b=5.512$ Å and $c=8.984$ Å was used in the calculations.

Supplementary Note 4. Orbital magnetism. The orbital magnetism of a wave packet is related to its angular momentum [10, 11],

$$\mathbf{m}_n(\mathbf{k}) = -i \frac{e}{2\hbar} \langle \nabla_{\mathbf{k}} u_n | \times [H(\mathbf{k}) - \epsilon_n(\mathbf{k})] | \nabla_{\mathbf{k}} u_n \rangle \quad (1)$$

$$= -i \frac{e}{2\hbar} (\langle \frac{\partial u_n}{\partial k_x} | H(\mathbf{k}) - \epsilon_n(\mathbf{k}) | \frac{\partial u_n}{\partial k_y} \rangle - c.c.) \mathbf{e}_z \quad (2)$$

$$= -i \frac{e}{2\hbar} \sum_{m \neq n} \left[\frac{\langle u_n | \frac{\partial H(\mathbf{k})}{\partial k_x} | u_m \rangle \langle u_m | \frac{\partial H(\mathbf{k})}{\partial k_y} | u_n \rangle}{\epsilon_m(\mathbf{k}) - \epsilon_n(\mathbf{k})} - c.c. \right] \mathbf{e}_z \quad (3)$$

where n, m are band indices. The derivation of Eq.3 can be found in Ref [12], which is similar to the equations of Berry curvature $\Omega_n(\mathbf{k})$ [12, 13].

$$\Omega_n(\mathbf{k}) = i \langle \nabla_{\mathbf{k}} u_n | \times | \nabla_{\mathbf{k}} u_n \rangle \quad (4)$$

$$= i (\langle \frac{\partial u_n}{\partial k_x} | \frac{\partial u_n}{\partial k_y} \rangle - \langle \frac{\partial u_n}{\partial k_y} | \frac{\partial u_n}{\partial k_x} \rangle) \quad (5)$$

$$= i \sum_{m \neq n} \left[\frac{\langle u_n | \frac{\partial H(\mathbf{k})}{\partial k_x} | u_m \rangle \langle u_m | \frac{\partial H(\mathbf{k})}{\partial k_y} | u_n \rangle}{(\epsilon_m(\mathbf{k}) - \epsilon_n(\mathbf{k}))^2} - c.c. \right] \quad (6)$$

The only change of $\Omega_n(\mathbf{k})$ and $\mathbf{m}_n(\mathbf{k})$ is the extra factor of $H(\mathbf{k}) - \epsilon_n(\mathbf{k})$ in the numerator cancels a $\epsilon_m(\mathbf{k}) - \epsilon_n(\mathbf{k})$ in the denominator.

Supplementary Note 5. Kagome lattice with Kane-Mele SOC and Ferromagnetism. We consider a unit cell of the kagome lattice spanned by the primitive lattice $2\mathbf{a}_1 = (2, 0), 2\mathbf{a}_2 = (1, \sqrt{3})$ and define $\mathbf{a}_3 = \mathbf{a}_2 - \mathbf{a}_1$. In the ferromagnetic kagome lattice with SOC strength λ , the spinless Hamiltonian in k-space is

$$H(k) = 2t \begin{bmatrix} 0 & \cos \mathbf{k} \cdot \mathbf{a}_1 & \cos \mathbf{k} \cdot \mathbf{a}_2 \\ \cos \mathbf{k} \cdot \mathbf{a}_1 & 0 & \cos \mathbf{k} \cdot \mathbf{a}_3 \\ \cos \mathbf{k} \cdot \mathbf{a}_2 & \cos \mathbf{k} \cdot \mathbf{a}_3 & 0 \end{bmatrix} + 2\lambda i \begin{bmatrix} 0 & \cos \mathbf{k} \cdot (\mathbf{a}_2 + \mathbf{a}_3) & -\cos \mathbf{k} \cdot (\mathbf{a}_3 - \mathbf{a}_1) \\ -\cos \mathbf{k} \cdot (\mathbf{a}_2 + \mathbf{a}_3) & 0 & \cos \mathbf{k} \cdot (\mathbf{a}_1 + \mathbf{a}_2) \\ \cos \mathbf{k} \cdot (\mathbf{a}_3 - \mathbf{a}_1) & -\cos \mathbf{k} \cdot (\mathbf{a}_1 + \mathbf{a}_2) & 0 \end{bmatrix} \quad (7)$$

We choose $\lambda = 0.2t$. The dispersion along $K' - \Gamma - K$ is shown in supplementary Fig. 7(a). Orbital magnetism $\mathbf{m}_n(\mathbf{k})$ of the flat band is shown in supplementary Fig. 7(b).

Supplementary references

[1] Kang, M. *et al.* Dirac fermions and flat bands in the ideal kagome metal FeSn. *Nat. Mater.* **19**, 163–169 (2020).

- [2] Kang, M. *et al.* Topological flat bands in frustrated kagome lattice CoSn. *Nat. Commun.* **11**, 4004 (2020).
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Figures

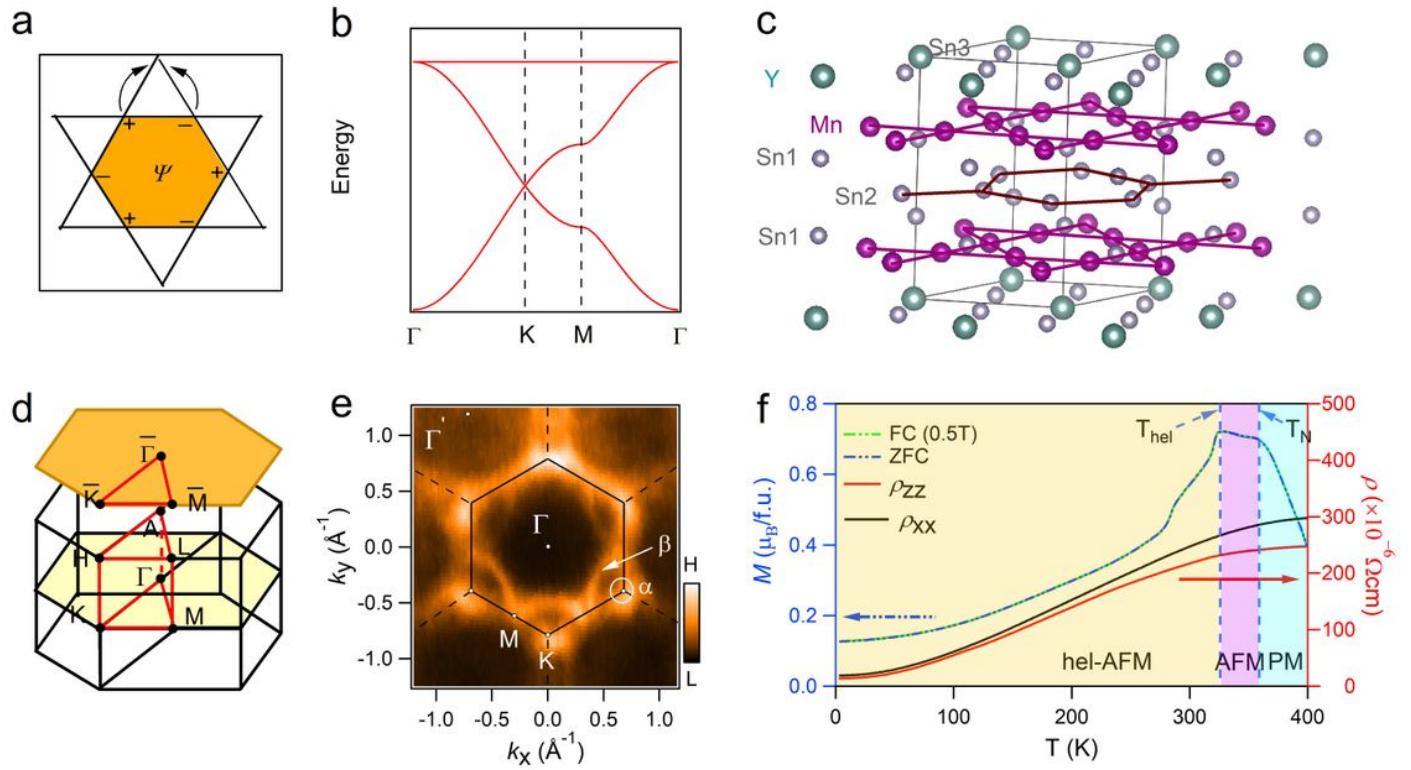


Figure 1

Crystal and electronic structures of YMn₆Sn₆. (a) Confinement of electron eigenstate induced by destructive interference in kagome lattice with NN hopping. (b) Tight-binding calculation of band structure of kagome lattice with NN in-plane hopping without SOC, featuring the Dirac cone at the BZ corner K point, a saddle point at BZ boundary M point, and a FB over the whole BZ. (c) Crystal structure of YMn₆Sn₆ with space group P6₃/mmm (No. 191). (d) 3D and projected BZs of YMn₆Sn₆ with marked high-symmetry points. (e) Photoemission intensity plot measured with 138-eV photons at $E_F \pm 10$ meV in the $k_z \sim 0$ plane. Hexagonal BZs are marked with black lines. (f) Magnetization as a function of temperature with zero field-cooling and field-cooling at $B = 0.5$ T along the [100] direction. Temperature dependence of longitudinal resistivity ρ_{xx} and ρ_{zz} with zero-field.

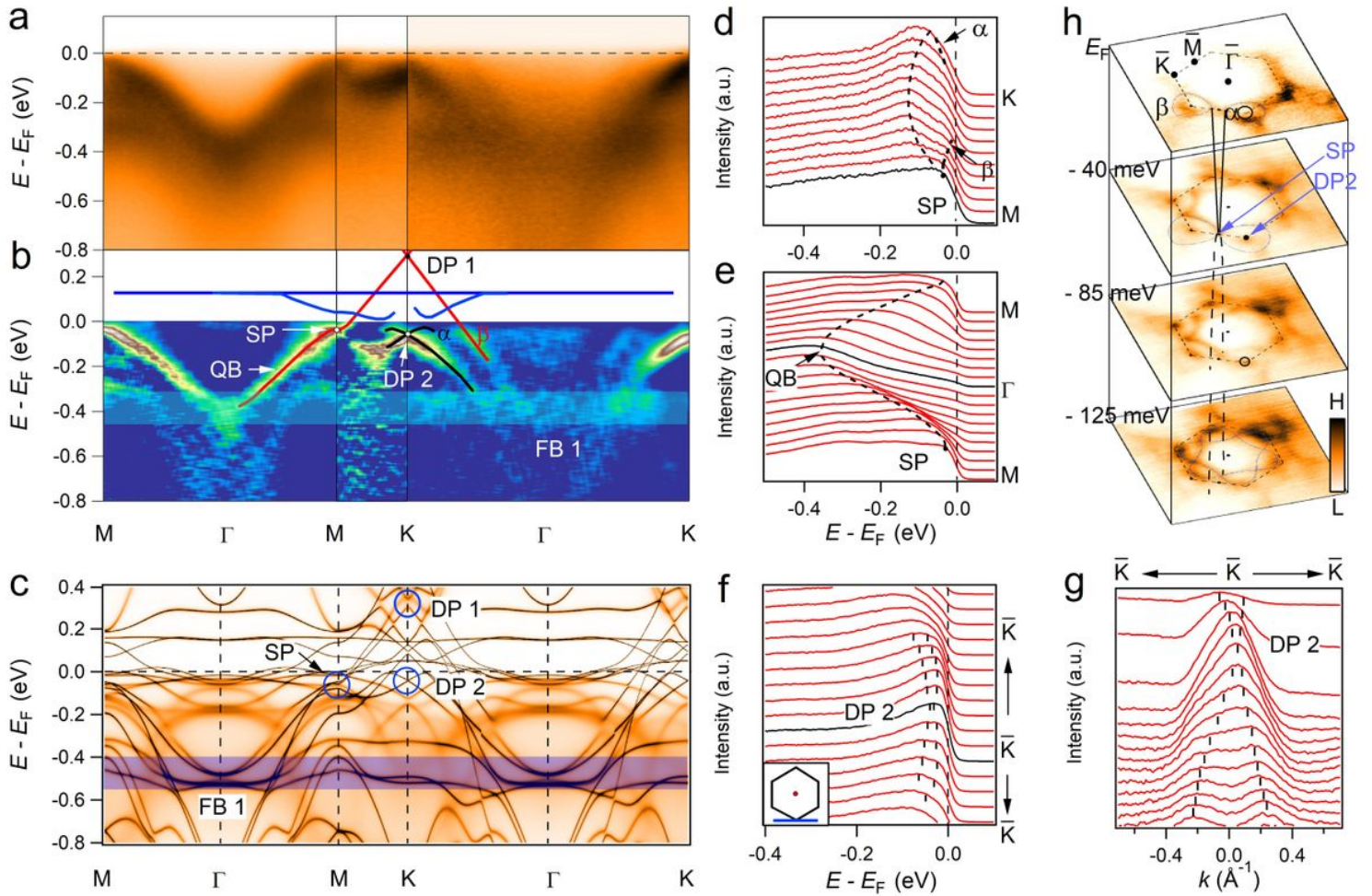


Figure 2

Band structure evolution in the 1st BZ. (a) Photoemission intensity plots of YMn_6Sn_6 along Γ -M-K- Γ in the $k_z = 0$ plane. (b) Corresponding second derivative plots of (a). The blue-colored region highlights the manifestation of the kagome flat band at the binding energy of about 0.4 eV. The appended colored lines serve as guides to the bands, which are extracted from DFT+DMFT calculations. (c) DFT+DMFT calculated ARPES in the FM state with SOC and with the experimentally determined E_F shifted downwards about 76 meV. Dirac point (DP1 and DP2), saddle point (SP) and flat band (FB1) are indicated by the blue circles and blue-colored region, respectively. (d,e) EDC plots along K-M and M- Γ -M, respectively. (f,g) EDC and MDC plots along the $\bar{K}^- - \bar{K}^- - \bar{K}^-$ direction, with the momentum path indicated as inset. (h) Constant energy maps at different binding energies.

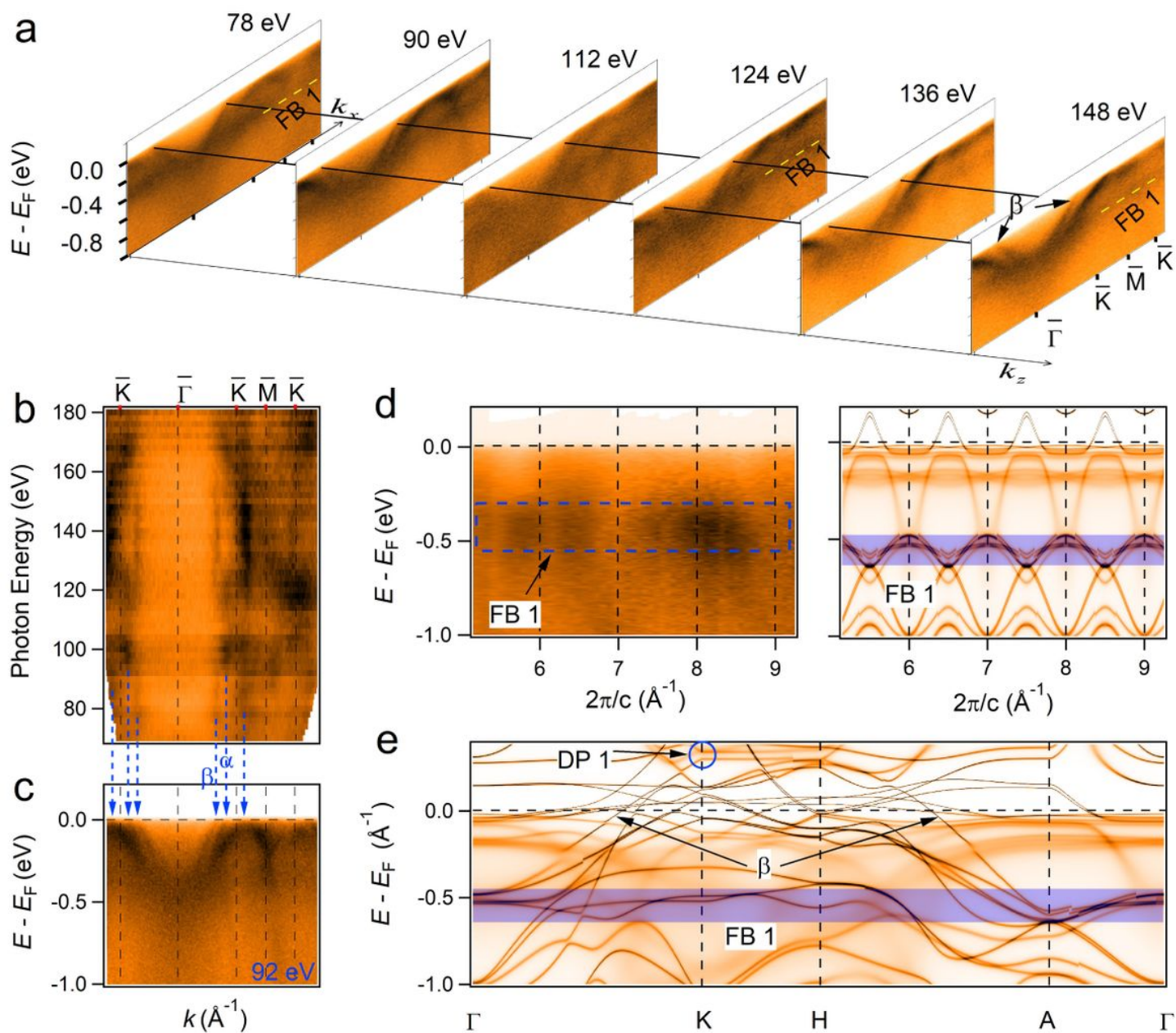


Figure 3

Photon-energy-dependence measurement of YMn6Sn6. (a) Photoemission intensity plots of YMn6Sn6 with variable photon energies along Γ (A)-K(H), the flat band (FB1) locates at the binding energy of about 0.4 eV through the whole BZ. The β band appears in every photon energy. (b) ARPES intensity map at E_F in the k_x - k_z plane with variable photon energies along Γ (A)-K(H), showing a well defined 2D-like band structure. (c) Energy-momentum dispersion of YMn6Sn6 measured at $h\nu = 92$ eV ($k_z \approx 0.6 \pi/c$). (d) Photoemission intensity plot and DFT+DMFT calculated ARPES in the FM state with SOC along the Γ -A di-rection, respectively. (e) DFT+DMFT calculated ARPES in the FM state with SOC along Γ -K-H-A- Γ , with the experimentally determined E_F shifted downwards about 76 meV. The blue-colored region highlights the manifestation of the kagome flat band.

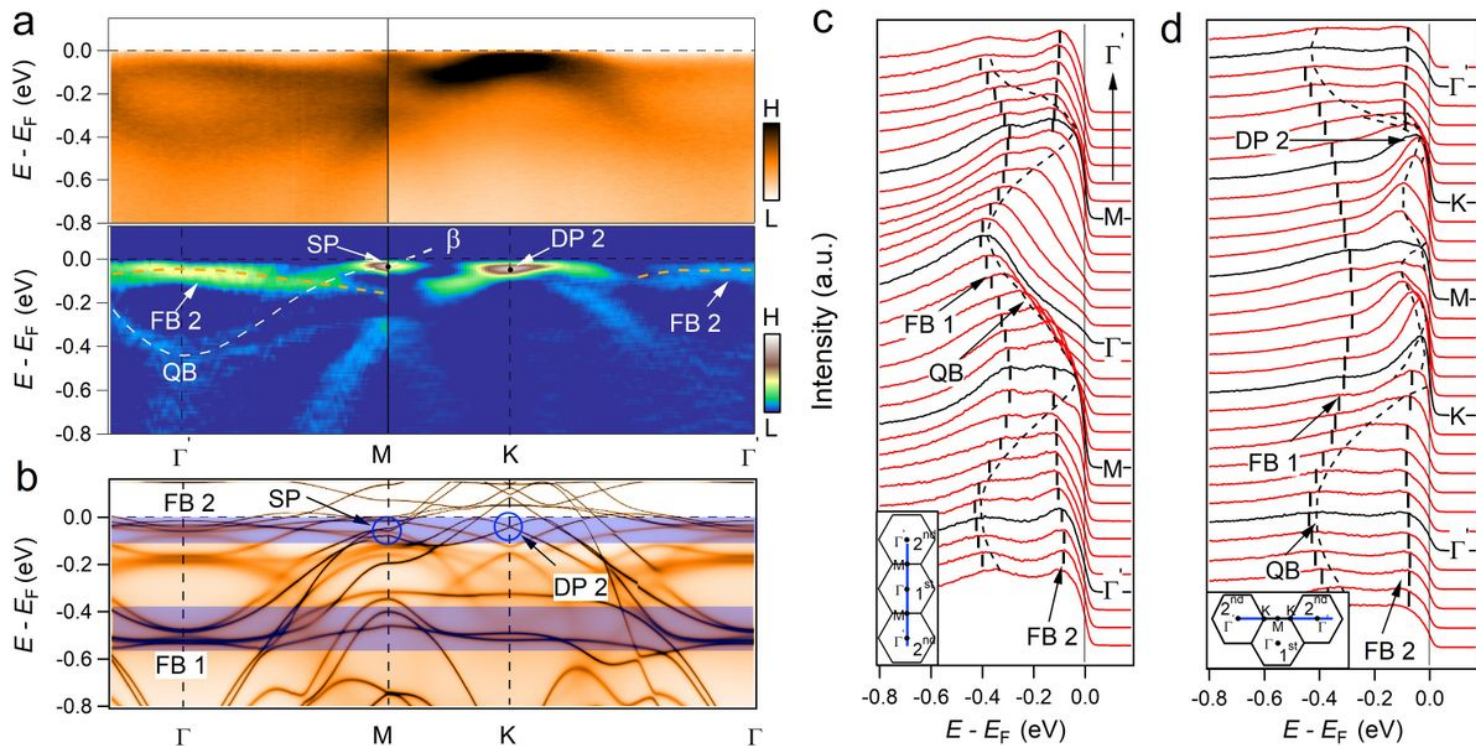


Figure 4

Band structure evolution in the 2nd BZ. (a) Photoemission intensity plots and corresponding second derivative plots of YMn6Sn6 in 2nd BZ along Γ -M-K- Γ in the $k_z = 0$ plane. The dashed lines are served as guides to the eyes. (b) DFT+DMFT calculated ARPES in the FM state with SOC to according to the corresponding path of (a) and with experimental EF. Dirac point (DP2), saddle point (SP) and flat band (FB) are indicated by the blue circles and blue-colored regions, respectively. (c,d) EDC plots along the high-symmetry lines, with the momentum paths indicated as inset. The flat bands (FB1 and FB2) and the parabolic band (QB) are indicated by the black dashed lines with thick and thin, respectively.