

Spin Splitting and Even-Odd Effects in Carbon Nanotubes

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The level spectrum of a single-walled carbon nanotube rope, studied by transport spectroscopy, shows Zeeman splitting in a magnetic field parallel to the tube axis. The pattern of splittings implies that the spin of the ground state alternates by $\frac{1}{2}$ as consecutive electrons are added. Other aspects of the Coulomb blockade characteristics, including the current-voltage traces and peak heights, also show corresponding even-odd effects. [S0031-9007(98)06652-6]

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The spin state of small multielectron systems is an important testing ground for our understanding of interacting quantum systems. For N noninteracting electrons in non-degenerate levels with spin, the single-particle states are occupied in order of energy, leading to a total spin $S = 0$ for even N and $S = \frac{1}{2}$ for odd N . Coulomb interactions among the electrons can alter this behavior, however. In atoms, for example, the exchange interaction among electrons in a shell leads to Hund's rule and a spin-polarized ground state for a partially filled shell. Recently, attention has been focused on similar questions in quantum dots. In small 3D metallic dots, Zeeman splitting consistent with an alternation between $S = 0$ and $\frac{1}{2}$ was found [1]. This may be understood within the constant interaction (CI) model [2], where the energy for adding an electron is the noninteracting level spacing ΔE plus a constant charging energy U . On the other hand, in two-dimensional dots evidence for spin polarization in the ground state has been found in recent experiments on both high symmetry [3] and low symmetry dots [4], requiring explanations beyond the CI model.

Of considerable interest is the situation in 1D, where Coulomb interactions are predicted to profoundly influence the properties of the system [5]. Here exact theoretical results are available for many model systems. For instance, for electrons in a box in strictly one dimension (1D), Lieb and Mattis [6] proved that in spite of interactions the ground state has the lowest possible spin. In real systems, however, a variety of factors, such as finite transverse dimensions, multiple 1D subbands, and spin-orbit coupling, may lead to a spin-polarized ground state.

Here we present measurements of the spin state of single-walled carbon nanotubes, a novel quasi-1D conductor where the current is carried by two 1D subbands [7]. It has recently been shown experimentally [8,9] that when contacts are attached, these nanotubes behave as quasi-1D quantum dots. Here we concentrate on a very

short (~ 200 nm) dot in a nanotube bundle (known as a "rope" [10]), with a correspondingly large level spacing. To study the spin state, we apply a magnetic field along the axis of the nanotube rope and examine the Zeeman effects in the transport spectrum. From the pattern of the spin splitting, we conclude that as successive electrons are added, the ground state spin oscillates between S_0 and $S_0 + \frac{1}{2}$, where S_0 is most likely zero. This results in an even/odd nature of the Coulomb peaks which is also manifested in the asymmetry of the current-voltage characteristics and the peak height. It may also be reflected in the excited state spectrum.

The devices are made [9] by depositing single-walled nanotubes [10] from a suspension in dichloroethane onto 1- μm -thick SiO_2 . The degenerately doped silicon substrate is used as a gate electrode. A single rope is located relative to prefabricated gold alignment marks using an atomic force microscope (AFM). Chromium-gold contacts are then deposited on top using 20 keV electron beam lithography. An AFM image of a 5-nm-diameter rope (consisting of about a dozen tubes) with six contacts is shown in the inset to Fig. 1. Leads labeled s (source), d (drain), and V_g (gate) are drawn in to indicate the typical measurement configuration.

Figure 1 shows the linear-response two-terminal conductance, G , versus gate voltage, V_g , at magnetic field $B = 0$ and temperature $T = 100$ mK. It exhibits a series of sharp Coulomb blockade oscillations [2,8,9] that occur each time an electron is added to the nanotube dot. For $T \lesssim 10$ K all the peaks have the same width, proportional to T [9], and a T -independent area, indicating that the level spacing ΔE is $\gg k_B T$ and that transport is through a single quantum level. We deduce that the dot electrostatic potential V_{dot} is linearly related to V_g , with a coefficient $\alpha \equiv dV_{\text{dot}}/dV_g = 0.09$.

Figure 2(a) is a greyscale plot of the differential conductance dI/dV as a function of V and V_g at $B = 0$.

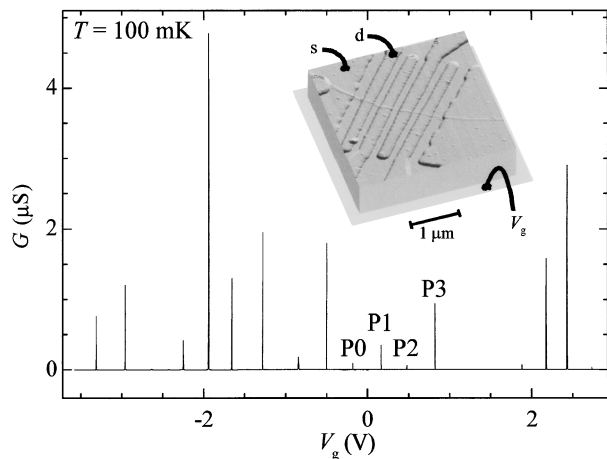


FIG. 1. Conductance G of a nanotube rope vs gate voltage V_g . Inset: AFM image of a device with schematic wires added.

Dark lines here are loci of peaks in dI/dV . Crosses $P0$ and $P1$ are formed by the identically labeled Coulomb peaks in Fig. 1. The interpretation of such a plot in the CI model is well known [3]. Each line is produced by the alignment of a quantized energy level in the dot with the Fermi level in a contact. From the spacing of the lines, we infer a typical level spacing $\Delta E \sim 5$ meV, and from the average Coulomb peak spacing we obtain a charging energy $U \sim 25$ meV. These values are consistent with expectations based on previous measurements [8,9] for a 100–200 nm length of tube. Thus we find as before [9] that the portion of nanotube rope forming the dot appears roughly equal in length to the distance between the contacts (nominally 200 nm).

Figure 2(b) shows the results of the same measurement at $B = 5$ T. Most of the lines observed at $B = 0$ have split into parallel pairs. The splitting is linearly proportional to B . This can be seen in Fig. 2(c), where the relative positions of the peaks in dI/dV at $V = -7$ mV [dotted line in Fig. 2(a)] are plotted as a function of B . One group of peaks (denoted by open symbols) moves downward in V_g relative to the other (solid symbols) by an amount proportional to B . Note that not all the lines at $B = 0$ split. Over a series of ten consecutive crosses in the range $-2 < V_g < +1$ V [11], the following pattern emerges: on alternate peaks ($P0, P2$, etc.), the leftmost lines in the cross (such as T) do not split, while on the other peaks ($P1, P3$, etc.), the rightmost lines (such as Z) do not split.

These measurements can be used to obtain information about the ground-state spin S_N of the dot with N electrons, as we now discuss. The analysis is based on the following spin selection rules: since the tunneling electron carries spin $\frac{1}{2}$, both the total spin, S , and its component along the magnetic field axis, S_z , must change by $\pm\frac{1}{2}$ for observable transitions [12].

The energy required for a tunneling process is the energy difference between the N - and $(N + 1)$ -electron states. In the absence of orbital effects [13], this depends

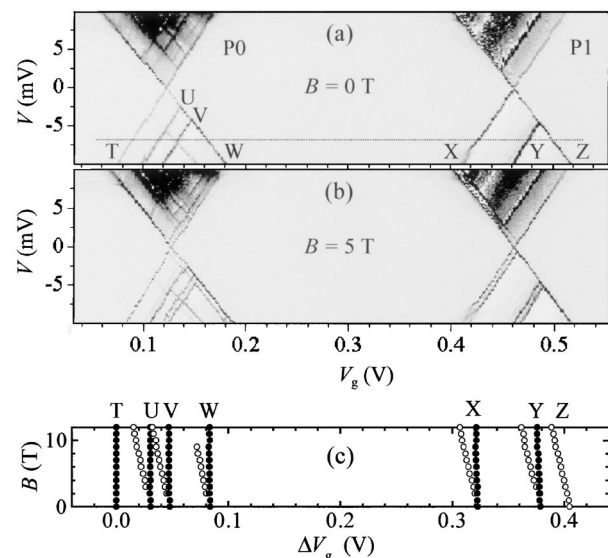


FIG. 2. (a) Greyscale plot of the differential conductance dI/dV of Coulomb peaks $P0$ and $P1$ at $B = 0$ (darker = more positive dI/dV). (b) Same as (a) but at $B = 5$ T. (c) B dependence of the relative positions of the peak in dI/dV labeled T - Z in (a), at a bias of $V = -7$ mV as indicated by the dashed line in (a). On the x axis we plot $\Delta V_g = V_g - V_g^T$, where V_g^T is the position of peak T , to remove unreplicable temporal drift of the characteristics along the V_g axis.

on B only through the Zeeman term $-g\mu_B B \Delta S_z$, where g is the electronic g factor, ΔS_z is the change in S_z , and μ_B is the Bohr magneton. In Fig. 2(c) we therefore associate the open-symbol transitions with $\Delta S_z = +\frac{1}{2}$ and the closed-symbol transitions with $\Delta S_z = -\frac{1}{2}$. Fitting their separation to $g\mu_B B/\alpha$ yields $g = 2.04 \pm 0.05$, which is consistent with $g = 2.0$ for graphite and with the value $g = 1.9 \pm 0.2$ obtained previously for a single excited state in a nanotube [8].

From the pattern of splittings of the lowest-energy transitions [the edges of the crosses in Fig. 2(a)], one can deduce the change in ground-state spin, $\Delta S = S_{N+1} - S_N = \pm\frac{1}{2}$, across each Coulomb peak. The reason is as follows [1]. First consider an electron tunneling into the N -electron ground state in a magnetic field, where initially the total spin is aligned with the field, so that $S_z = -S_N$. For the case $\Delta S = +\frac{1}{2}$, after tunneling S_z may be either $-(S_N + \frac{1}{2})$ or $-(S_N - \frac{1}{2})$. The corresponding line therefore splits with B . However, for the case $\Delta S = -\frac{1}{2}$, only $S_z = -(S_N - \frac{1}{2})$ is possible for the final state, because of the requirement $|S_z| \leq S_{N+1} = S_N - \frac{1}{2}$. The corresponding line therefore does not split with B . A similar argument for an electron tunneling out of the $N + 1$ ground state shows that if $\Delta S = -\frac{1}{2}$ the line splits, while if $\Delta S = +\frac{1}{2}$ it does not. To summarize: if $\Delta S = +\frac{1}{2}$ for a Coulomb peak, the lines on the right edge of the cross do not split, while if $\Delta S = -\frac{1}{2}$ the lines on the left edge do not split.

This general result is also predicted by the CI model, as indicated in Fig. 3. If N is even, $S_N = 0$, and the next electron can be added to either spin-up or spin-down state of the next orbital level (left sketch), resulting in $S_{N+1} = \frac{1}{2}$. On the other hand, if N is odd, $S_N = \frac{1}{2}$ and the next electron can be added only to the one empty spin state of that level (right sketch), resulting in $S_{N+1} = 0$. A corresponding story can be told for removing an electron. The predicted pattern of splittings is the same as in the previous paragraph, but with the additional implication that N is even if $\Delta S = +\frac{1}{2}$ and odd if $\Delta S = -\frac{1}{2}$.

Comparing the above predictions with Fig. 2, we find that $\Delta S = +\frac{1}{2}$ for peak $P0$ and $\Delta S = -\frac{1}{2}$ for peak $P1$. Since the pattern of splitting alternates between the two types over ten Coulomb peaks, we deduce that S_N oscillates between some value S_0 and $S_0 + \frac{1}{2}$ as ten successive electrons are added. Most probably $S_0 = 0$, as in the CI model, for the following reasons. First, polarization of a system is usually related to states near the Fermi level. In this system we see the spin alternating as these states are filled. Second, if a transition splits in a magnetic field, the line for decreasing $|S_z|$ should be suppressed by a factor of $2S + 1$ relative to the line for increasing $|S_z|$ [14]. In the data, however [see Fig. 2(b)], these lines are of similar strength, implying that the initial spin S is zero or small. Therefore, the behavior is consistent with the prediction of Ref. [6] for 1D electrons; the ground state spin alternates between 0 and $\frac{1}{2}$ [15]. This is our principal result. We subsequently describe Coulomb peaks where N changes from odd to even on addition of an electron ($P0, P2$, etc.) as *odd-to-even* peaks, and the other peaks ($P1, P3$, etc.) as *even-to-odd* peaks. This is indicated in Fig. 3.

The alternating spin of the ground state should also be reflected in the I - V characteristics at zero magnetic field, if the source and drain contacts have different tunnel resistances. If, for instance, the source contact dominates the resistance, the magnitude of the current I_- at negative source bias V is determined by transitions from the N to the $N + 1$ electron ground state, as long as the bias is less than the level spacing. On the other hand, the current I_+ at positive V is determined by transitions from the $N + 1$ to the N electron ground state. The ratio $\beta = I_+/I_-$ therefore reflects the differences caused by the spin selection rules in these two situations. This

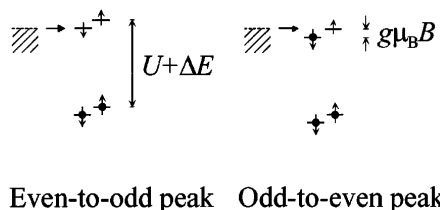


FIG. 3. Explanation of splitting pattern within the CB model. The lowest-energy transition splits for an even-to-odd peak, but not for an odd-to-even peak.

can easily be understood in the CI model, as illustrated for an odd-to-even peak ($\Delta S = -\frac{1}{2}$) in Fig. 4(a). For negative V (left sketch) an electron tunneling in from the source can go into only one available spin state. On the other hand, for positive V (right sketch), either of two electrons can tunnel out. The current is therefore larger for positive V . An elementary calculation gives $\beta = (G_s + 2G_d)/(2G_s + G_d)$, where G_s and G_d are the source and drain barrier conductances, respectively. For $G_s < G_d$, this predicts $1 < \beta < 2$. In contrast, for an even-to-odd peak ($\Delta S = \frac{1}{2}$), the inverse ratio is found, and $\frac{1}{2} < \beta < 1$ is predicted.

The solid line in Fig. 4(b) is the I - V characteristic measured at the center of peak $P0$. Near $V = 0$, the I - V is Ohmic, but for $|V| \geq 0.5$ mV the current saturates into a slowly varying form. The saturation current is larger for positive than for negative V . Moreover, if the same data are plotted (dashed line) with the current scaled by a factor $-\beta$, where $\beta = 1.57$, the I - V 's in the two bias directions can be brought onto the same interpolated curve

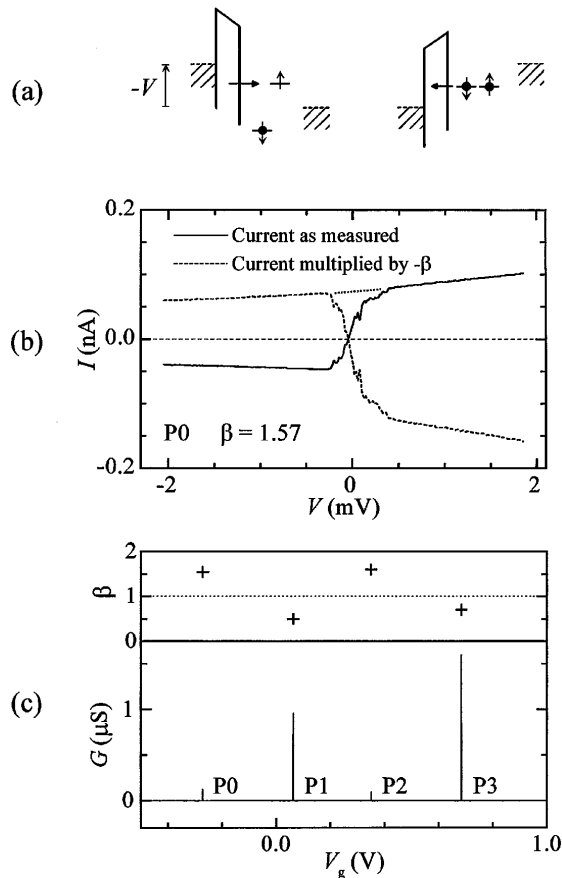


FIG. 4. (a) Current flow at high bias in the CI model. Only the larger barrier, between source and dot, is drawn. (b) Solid line: I - V measured at the center of peak $P0$ in Fig. 1. Dashed line: the same trace with I multiplied by $-\beta = -1.57$. Dotted line: interpolation between these. (c) Lower: expanded view of the peaks $P0$ - $P3$. Upper: measured values of β for these peaks. The oscillating value of β implies that successive electrons are added with opposite spin directions (see text).

(dotted line). For each peak an appropriate value of β can be chosen to achieve a similar matching. The results are plotted in the top panel of Fig. 4(c). We find that $1 < \beta < 2$ for $P0$ and $P2$, while $\frac{1}{2} < \beta < 1$ for $P1$ and $P3$. Comparing these values with the predictions for $\beta = I_+/I_-$ in the previous paragraph, we see that they are perfectly consistent with our assignments of $\Delta S = +\frac{1}{2}$ or $-\frac{1}{2}$ from the Zeeman splitting [16].

We have seen from the Zeeman splitting and the I - V characteristics that the ground state spin behaves as is predicted by the CI model. However, this implies not that effects such as exchange are small, but only that they do not change the spin of the N -electron ground state of the system. Exchange might, for instance, be manifested in the excited state spectra, where one would anticipate a difference between odd-to-even and even-to-odd peaks. For even-to-odd peaks, the added electron simply goes into higher unoccupied orbital levels, giving rise to a single-particle spectrum. For odd-to-even peaks, however, the added electron can form singlet and triplet states with the original unpaired electron, leading to exchange splitting. A singlet-triplet splitting has indeed been seen in the excitation spectra of semiconductor dots [17]. We observe indications of this predicted behavior in peaks $P0$ – $P3$. The lowest excited states visible at negative V on odd-to-even peaks in each case form a pair [such as lines U and V on peak $P0$ in Fig. 2(a)], while those on even-to-odd peaks do not (such as line Y on $P1$). This will be investigated further in future work.

A contradiction with the CI model is also seen in the peak heights. These are predicted to be identical for a pair of peaks arising from a single orbital level [18]. However, we find that the even-to-odd peaks tend to be considerably larger than the odd-to-even peaks, as apparent in Fig. 4(c). This behavior is not understood and deserves further investigation.

In summary, our transport measurements of a short nanotube quantum dot show that the ground state of this 1D electronic system alternates between $S = 0$ and $S = 1/2$. A variety of even-odd effects are seen in the addition spectrum, some of which, such as an alternation of the peak heights, require explanations beyond the simple Coulomb blockade picture.

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