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Stability trends of MAX phases from first principles

M. Dahlqvist,^{*} B. Alling, and J. Rosén

Department of Physics, Chemistry, and Biology, IFM, Linköping University, SE-581 83 Linköping, Sweden

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We have developed a systematic method to investigate the phase stability of $M_{n+1}AX_n$ phases, here applied for $M=Sc, Ti, V, Cr, \text{ or } Mn$, $A=Al$, and $X=C$ or N . Through a linear optimization procedure including all known competing phases, we identify the set of most competitive phases for $n=1-3$ in each system. Our calculations completely reproduce experimental occurrences of stable MAX phases. We also identify and suggest an explanation for the trend in stability as the transition metal is changed across the $3d$ series for both carbon- and nitrogen-based systems. Based on our results, the method can be used to predict stability of potentially existing undiscovered phases.

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The MAX phases are a class of nanolaminated materials with the general composition $M_{n+1}AX_n$ ($n=1-3$), where M is an early transition metal, A is an A-group element, and X is either carbon or nitrogen.^{1,2} Lately, these compounds have attracted extensive attention due to their combination of both ceramic and metallic properties,³ which makes them potentially useful in, e.g., high-temperature structural, electrical, and tribological applications. From a vast number of combinatorial possibilities of three MAX phase elements, approximately 60 phases have been synthesized to date. A majority are 211 phases ($n=1$) while Ti_2AlC and Ti_3SiC_2 are the most well known and most studied.⁴

Theoretical studies related to MAX phase properties are numerous, ranging from investigations of, e.g., elastic properties to electronic-structure calculations.⁵⁻¹¹ Such work is relevant to gain knowledge and understanding of existing phases. However, surprisingly little has been done to reflect on whether or not studied phases not yet synthesized can be expected to exist experimentally. There are several relevant aspects of stability where one is the intrinsic stability, i.e., that the Gibbs free energy of the structure is in a local minimum with respect to small deformations. Recently Cover *et al.*¹² did a comprehensive study on 240 M_2AX phases, where approximately 20 are intrinsically unstable. However, even if they are intrinsically stable, a phase does not necessarily exist since there are competing phases which might be thermodynamically favorable. Palmquist *et al.*¹³ investigated the stability of $M_{n+1}AX_n$ phases in the Ti-Si-C system, by comparing the total energy of the MAX phases with the total energy of *ad hoc* chosen competing equilibrium phases. They found $n=1,2,3$ to be stable although Ti_2SiC has not been observed experimentally.¹³ Only recently, Keast *et al.*¹⁴ did an ambitious study of the phase stability for a selection of $M_{n+1}AX_n$ phases ($n=1-4$), including Ti_2SiC , and found agreement with experiment.

In this work, we perform a systematic investigation of the phase stability of known as well as hypothetical MAX phases using first-principles calculations. An important subset of the $M_{n+1}AX_n$ elemental combinations is studied, where $M=Sc, Ti, V, Cr, \text{ and } Mn$, $A=Al$, and $X=C$ and N . In order to avoid *ad hoc* selected competing phases, careful investigations of phase diagrams and experimental work have been conducted in order to include all known, as well as some hypothetical, phases in each system, see, e.g., Refs. 15 and 16. In Table I,

the phases included in this work are presented. Compounds with several phases are included in the form of their low-temperature thermodynamically stable phase, serving as a “lowest-energy” representation, and, as such, the most competitive phase. Furthermore, in order to make the correct, and in ternary and multinary systems nontrivial, choice of most competitive set of rivalrous phases, a linear optimization problem is solved.¹⁷ As an example, we find the most competing phases for Ti_2AlC to be Ti_3AlC_2 and $TiAl$ in contrast to the *by-hand* identified combination Ti_3AlC , TiC , and $TiAl_3$ suggested by Keast *et al.*¹⁴ Our systematic approach allows us to investigate trends in phase stability for compositionally different MAX phases.

All calculations are based on density-functional theory (DFT),¹⁸ as implemented in the Vienna *ab initio* simulation package (VASP),^{19,20} wherein the projector augmented wave²¹ method and the generalized gradient approximation²² for the exchange-correlation energy and one-electron potential are used. Reciprocal-space integration was performed within the Monkhorst-Pack scheme²³ with a plane-wave cut-off energy of 400 eV. The convergence was 0.1 meV for the total energy, and the k -point density was converged below 1 meV per formula unit, for each phase separately. All phases were optimized with respect to cell volume, c/a ratio, as well as internal parameters. All Cr- and Mn-containing phases were allowed to be magnetic. Ferromagnetic as well as different antiferromagnetic structures were tested and the configuration with lowest total energy was included in the study.

The analysis of the phase stability has been divided in two parts, where the first concerns the formation enthalpy of $M_{n+1}AlX_n$ with respect to its non-MAX competing phases: single elements, binary, and other ternary compounds. In the second part, the $M_{n+1}AlX_n$ phases are compared to all known phases, including those with $M_{n+1}AlX_n$ structure. The latter to emphasize the possibility of $M_{n+1}AlX_n$ phases with different n competing with each other.

Even if all known phases of a ternary phase diagram are taken into consideration, it is a nontrivial task to choose among them the most competitive set of rivalrous structures at each $M_{n+1}AlX_n$ composition.¹⁷ Therefore, a systematic scheme to search for the most competitive combination of phases at a given elemental composition b^M , b^A , and b^X was applied, using the simplex linear optimization procedure to solve the equation

TABLE I. Included phases in each M - A - X system. Phases in *italic* have not been found experimentally and are treated as hypothetical phases.

M	M - A	M - X	A - X
Sc	ScAl ₃ , ScAl ₂ , B2-ScAl, Sc ₂ Al	Sc ₃ C ₄ , ScC, ScC _{0.875} , Sc ₄ C ₃ , Sc ₂ C ScN, ScN _{0.875}	Al ₄ C ₃ AlN
Ti	TiAl ₃ , TiAl ₂ , TiAl, Ti ₃ Al	TiC, TiC _{0.875} , Ti ₂ C TiN, TiN _{0.875} , Ti ₂ N	Al ₄ C ₃ AlN
V	VAl ₁₀ , V ₇ Al ₄₅ , V ₃ Al ₁₀ , VAl ₃ , V ₅ Al ₈ , V ₃ Al	VC, VC _{0.875} , V ₆ C ₅ , V ₄ C ₃ , α -V ₂ C, β -V ₂ C VN, VN _{0.875} , V ₂ N	Al ₄ C ₃ AlN
Cr	Cr ₇ Al ₄₃ , Cr ₅ Al ₂₁ , Cr ₄ Al ₉ , Cr ₅ Al ₈ , Cr ₂ Al	Cr ₃ C ₂ , Cr ₇ C ₃ , Cr ₃ C, Cr ₂₃ C ₆ o-CrN, c-CrN, c-CrN _{0.875} , Cr ₂ N	Al ₄ C ₃ AlN
Mn	MnAl ₆ , Mn ₃ Al ₁₀ , Mn ₄ Al ₁₁ , MnAl, Mn ₇ Al ₄₃	MnC, Mn ₇ C ₃ , Mn ₅ C ₂ , Mn ₃ C, Mn ₂₃ C ₆ MnN, MnN _{0.875} , Mn ₄ N, Mn ₃ N ₂ , Mn ₂ N	Al ₄ C ₃ AlN
M	M - A - X		
Sc	<i>Sc₂AlC, Sc₃AlC₂, Sc₄AlC₃, Sc₃AlC, ScAl₃C₃</i> <i>Sc₂AlN, Sc₃AlN₂, Sc₄AlN₃, Sc₃AlN</i>		
Ti	<i>Ti₂AlC, Ti₃AlC₂, Ti₄AlC₃, c-Ti₃AlC, o-Ti₃AlC</i> ^a <i>Ti₂AlN, Ti₃AlN₂, Ti₄AlN₃, c-Ti₃AlN, o-Ti₃AlN</i> ^a		
V	<i>V₂AlC, V₃AlC₂, V₄AlC₃, V₁₂Al₃C₈, V₃AlC</i> <i>V₂AlN, V₃AlN₂, V₄AlN₃, V₃AlN</i>		
Cr	<i>Cr₂AlC, Cr₃AlC₂, Cr₄AlC₃, Cr₃AlC</i> <i>Cr₂AlN, Cr₃AlN₂, Cr₄AlN₃, Cr₃AlN</i>		
Mn	<i>Mn₂AlC, Mn₃AlC₂, Mn₄AlC₃, Mn₃AlC</i> <i>Mn₂AlN, Mn₃AlN₂, Mn₄AlN₃, Mn₃AlN</i>		

^aRe₃B-type structure.

TABLE II. Calculated formation enthalpies ΔH_{comp} for $M_{n+1}AX_n$ phases including the most competing phases. ΔH_{comp} is calculated using Eq. (2). Phases with $\Delta H_{comp} < 0$ are in bold.

M	n	$M_{n+1}AC_n$		$M_{n+1}AN_n$	
		Most competing phases	ΔH_{comp} (eV/atom)	Most competing phases	ΔH_{comp} (eV/atom)
Sc	1	Sc ₃ AlC, ScAl ₃ C ₃	0.100	ScN, ScAl ₂ , Sc ₃ AlN	0.088
	2	Sc ₃ AlC, Sc ₃ C ₄ , ScAl ₃ C ₃	0.155	ScN, ScAl ₂ , Sc ₃ AlN	0.036
	3	Sc ₃ AlC, Sc ₃ C ₄ , ScAl ₃ C ₃	0.191	ScN, ScAl ₂ , Sc ₃ AlN	0.020
Ti	1	Ti ₃ AlC ₂ , TiAl	-0.027	Ti ₃ AlN ₂ , TiAl ₂ , o-Ti ₃ AlN	-0.050
	2	Ti ₂ AlC, Ti ₄ AlC ₃	-0.012	Ti ₂ AlN, Ti ₄ AlN ₃	0.013
	3	Ti ₃ AlC ₂ , TiC	0.000	Ti ₃ AlN ₂ , TiN	-0.022
V	1	V ₂ C, VAl ₃ , V ₃ AlC ₂	-0.072	V ₂ N, VAl ₃ , AlN	0.015
	2	V ₂ AlC, V ₆ C ₅ , Al ₄ C ₃	-0.005	V ₂ N, AlN, VAl ₃	0.154
	3	V ₃ AlC ₂ , V ₆ C ₅ , Al ₄ C ₃	0.006 ^a	V ₂ N, AlN	0.204
Cr	1	Cr ₂ Al, Cr ₃ C ₂ , Al ₄ C ₃	-0.067	Cr, AlN	0.353
	2	Cr ₂ AlC, Cr ₃ C ₂ , C	0.079	Cr, Cr ₂ N, AlN	0.324
	3	Cr ₂ AlC, Cr ₃ C ₂ , C	0.106	Cr ₂ N, AlN	0.306
Mn	1	MnAl, C, Mn ₃ AlC	0.005	Mn, AlN	0.376
	2	C, Mn ₃ AlC	0.094	Mn ₂ N, Mn ₄ N, AlN	0.363
	3	C, Mn ₃ AlC, Mn ₂₃ C ₆	0.153	Mn ₂ N, AlN	0.311

^a $\Delta H_{comp} = -0.012$ eV/atom with 11% vacancies on the carbon sublattice in a V₁₂Al₃C₈ structure (Ref. 27).

$$\min E_{comp}(b^M, b^A, b^X) = \sum_i^n x_i E_i, \quad (1)$$

where x_i and E_i is the amount and energy of compound i , respectively. E_{comp} is the energy that should be minimized subject to the constraints

$$x_i \geq 0; \quad \sum_i^n x_i^M = b^M, \quad \sum_i^n x_i^A = b^A, \quad \sum_i^n x_i^X = b^X,$$

where x_i^M is the amount of M atoms in x_i of compound i , etc. For the $M_{n+1}AX_n$ composition, $b^M = n+1$, $b^A = 1$, and $b^X = n$. The formation enthalpy with respect to the identified most competitive combination of phases is thus calculated according to

$$\Delta H_{comp}(M_{n+1}AX_n) = E(M_{n+1}AX_n) - E_{comp}(b^M, b^A, b^X), \quad (2)$$

where the term E_{comp} is given by Eq. (1).

$M_{n+1}AlX_n$ phase formation enthalpies based on all non-*MAX* competing phases are summarized in Fig. 1. Panel (a) shows the formation enthalpies, $\Delta H_{elements}$, with respect to only the pure elements in their most stable structure. In this comparison, the nitrogen containing $M_{n+1}AlX_n$ phases would have a maximum stability with Sc as M element. In the carbon case, $\Delta H_{elements}$ displays a clear minimum with Ti as M element. However, these trends change, see panel (b), when applying the relevant stability criteria ΔH_{comp} , including comparison also to binaries and other ternary phases (excluding competing *MAX* phases). The nitrogen *MAX* phases now display a minimum in the region of Ti as M element while the carbon *MAX* phases has a minimum around $M = V$ for $n=1$ and in between Ti and V for $n=2$ and 3. As n increases the identified minima for ΔH_{comp} is shifted slightly to the left which is influenced by the addition of the energetically favorable *MX* block (most pronounced for $M=Ti$) in the $M_{n+1}AX_n$ phase. No Sc or Mn-based *MAX* phase has a negative ΔH_{comp} . To explain the shift in trends between panels (a) and (b) in Fig. 1 we need to look at the stabilities of the competing phases, especially the binaries with *MC*, *MN*, and *MAI* stoichiometry (or corresponding combinations, e.g., $V_6C_5 + C = VC$). These are shown in panel (c). The *MN* binaries shows a minimum value of $\Delta H_{elements}$ at $M=Sc$, which corresponds to filling the bonding electronic states in the rocksalt structure. Approximately the same band filling is obtained at $M=Ti$ in the carbide TiC , also rocksalt.²⁴ $\Delta H_{elements}$ of the metal-aluminum compounds show smaller variations as the transition metal is changed. The similarities in the trends of $\Delta H_{elements}$ of *MAX* phases, panel (a), and the *MN* and *MC* binaries, panel (c), suggest that the bonding physics of the *MX* layers of the *MAX* phases are similar to the case in, e.g., rocksalt transition-metal nitrides and carbides in line with soft x-ray spectroscopy experiments.^{25,26} Thus, the competition with *MX* binaries in panel (c) shifts the stability maxima of the *MAX* phases to higher valence in M , as seen by comparing $\Delta H_{elements}$ in panel (a) and ΔH_{comp} in panel (b). Furthermore, for the nitrogen-based $M_{n+1}AX_n$ phases, AlN enters as a highly competing phase for the higher valence systems ($M=V, Cr, \text{ and } Mn$) giving rise to a substantial difference between ΔH_{comp} of the carbide and ni-

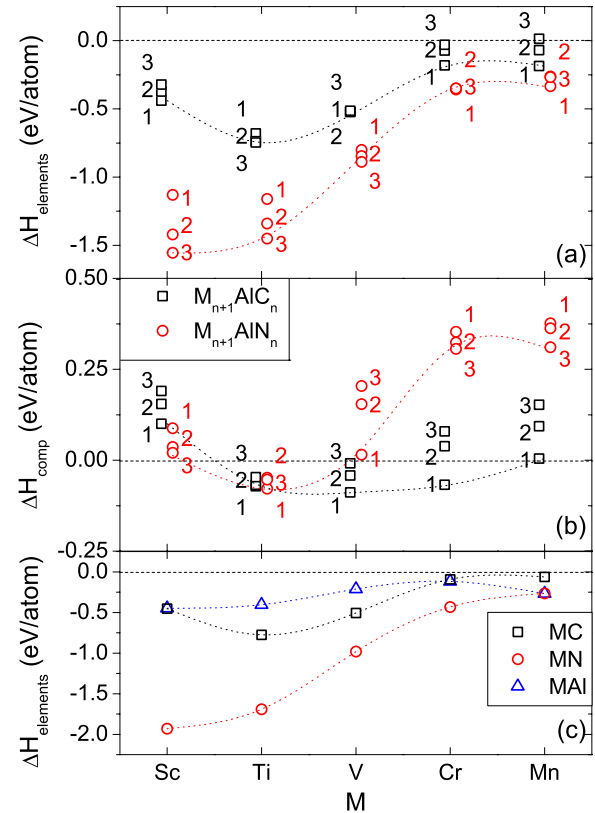


FIG. 1. (Color online) Calculated formation enthalpy of $M_{n+1}AlX_n$ with respect to (a) its single elements and (b) most competing phases using Eqs. (1) and (2) (competing *MAX* phases not included). X is either C (black square) or N (red circle), and A is Al. Phases with $n=1$ (M_2AX) are marked as 1, $n=2$ (M_3AX_2) as 2, and $n=3$ (M_4AX_3) as 3. (c) Calculated formation enthalpy of binaries (or combinations corresponding to binaries) of *MC*, *MN*, and *MAI* stoichiometries with respect to its single elements. Dotted lines serve as guide for the eye.

tride *MAX* phases in these cases. The high stability of AlN (in comparison to the lower stability of Al_4C_3) may explain why so few nitride $M_{n+1}AlN_n$ phases have been synthesized.

These results illustrate the importance of including all competing phases, not only single elements, to elucidate trends in phase stabilities. In addition to the result in panel (b) of Fig. 1, a full comparison including also competing *MAX* phases have been performed. In Table II, resulting ΔH_{comp} as well as the most competitive combination of phases for $M_{n+1}AX_n$ is presented. Note that only seven $M_{n+1}AX_n$ phases have $\Delta H_{comp} < 0$, in comparison to the ten phases in panel (b) of Fig. 1. Comparing these results to experimentally known phases, see Table III, the only discrepancy was initially found for V_4AlC_3 with $\Delta H_{comp} = 0.006$ eV/atom. This inconsistency might be correlated to observed C site vacancies of approximately 11%.²⁷ A corresponding superstructure of $V_{12}Al_3C_8$ was therefore taken into consideration, resulting in phase stabilization of $\Delta H_{comp} = -0.012$ eV/atom, as compared with the most competing set of phases V_2AlC and V_6C_5 .

As a complement to Table II, the competition between different $M_{n+1}AX_n$ phases is illustrated by calculating ΔH_{comp} relative to *MX* and *MA* stoichiometry along a line across the

TABLE III. *MAX* phases with calculated negative formation enthalpy ($\Delta H_{comp} < 0$), compared to experimentally observed *MAX* phases within the herein investigated systems.

<i>MAX</i> with $\Delta H_{comp} < 0$	Experimentally observed <i>MAX</i> phases ^a
Ti ₂ AlC, Ti ₃ AlC ₂ , Ti ₄ AlC ₃ ^b	Ti ₂ AlC, Ti ₃ AlC ₂
V ₂ AlC, V ₃ AlC ₂ , V ₄ AlC ₃ ^c	V ₂ AlC, V ₃ AlC ₂ , V ₄ AlC ₃
Cr ₂ AlC	Cr ₂ AlC
Ti ₂ AlN, Ti ₄ AlN ₃	Ti ₂ AlN, Ti ₄ AlN ₃

^aReference 4.

^bTi₄AlC₃ have $\Delta H_{comp} = 0.000$ eV/atom to the level of accuracy in our work.

^c11% carbon vacancies stabilize the 413 *MAX* phase as observed in Ref. 27.

phase diagram, see Fig. 2. Included are the four ternary systems shown in panel (b) of Fig. 1, where at least one $M_{n+1}AX_n$ phase has $\Delta H_{comp} < 0$. Note that phases with filled symbols in Fig. 2 are considered stable whereas those with hollow symbols are considered unstable. An explanation to why Ti₃AlN₂ has not been found experimentally is given through its higher formation enthalpy as compared with a combination of Ti₂AlN and Ti₄AlN₃. Looking at Ti₄AlC₃, it is found on the line between Ti₃AlC₂ and TiC and can be considered as a borderline case, possibly unstabilized by TiC_x off-stoichiometry. It is also found that V₄AlC₃ is unstable relative to V₃AlC₂ and VC (corresponding to V₆C₅ + C), though as mentioned earlier carbon vacancies can stabilize a 413-like *MAX* phase. When comparing the here identified stable $M_{n+1}AX_n$ phases, i.e., those with $\Delta H_{comp} < 0$ in Table II and Fig. 2, with experimentally known $M_{n+1}AX_n$ phases as presented in Table III, the complete reproduction of experimental occurrence demonstrate the strength and potential of our approach.

In conclusion, we have investigated the phase stability of $M_{n+1}AX_n$ phases using DFT calculations in combination with linear optimization procedures. We identify and suggest an explanation to the here observed trend in phase stability as the transition metal is changed across the 3*d* series. For carbon containing *MAX* phases, a maximum stability is reached

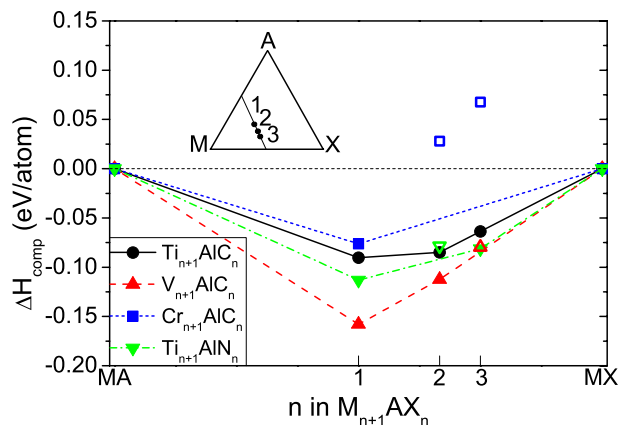


FIG. 2. (Color online) Formation enthalpy of $M_{n+1}AX_n$ with respect to binaries of *MX* and *MA* stoichiometry. Filled symbols represent stable phase and hollow symbols those considered unstable. The inset shows the position of the $M_{n+1}AX_n$ phases on the line between *MX* and *MA* in the phase diagram.

around V as transition metal, while for nitrogen, a maximum stability is reached for Ti. Even though the calculations are for 0 K, the calculated phase stability reflects experimental occurrence very well, which indicates that the formation of $M_{n+1}AX_n$ are mainly governed by the total energy term in the Gibbs free energy, although for borderline cases the vibrational effects comes into play at high temperatures.²⁸ $M_{n+1}AX_n$ phases are highly ordered compounds where a considerable energetic driving force and sufficient diffusion is needed to stabilize the structure during synthesis. This explains the remarkable agreement between our predictions and the experimentally reported phases, and indicates a considerable challenge in synthesizing metastable $M_{n+1}AX_n$ phases. Furthermore, our method is a reliable tool that can be used as guidance for further search of new $M_{n+1}AX_n$ phases, as well as other multinary compounds, before time consuming and expensive experimental investigations are attempted.

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*madah@ifm.liu.se

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