

# Star formation rates in luminous quasars at $2 < z < 3$

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Accepted 2016 February 2. Received 2016 January 31; in original form 2015 October 8

## ABSTRACT

We investigate the relation between star formation rates ( $\dot{M}_s$ ) and AGN properties in optically selected type 1 quasars at  $2 < z < 3$  using data from *Herschel* and the SDSS. We find that  $\dot{M}_s$  remains approximately constant with redshift, at  $300 \pm 100 M_\odot \text{ yr}^{-1}$ . Conversely,  $\dot{M}_s$  increases with AGN luminosity, up to a maximum of  $\sim 600 M_\odot \text{ yr}^{-1}$ , and with C IV FWHM. In context with previous results, this is consistent with a relation between  $\dot{M}_s$  and black hole accretion rate ( $\dot{M}_{\text{bh}}$ ) existing in only parts of the  $z - \dot{M}_s - \dot{M}_{\text{bh}}$  plane, dependent on the free gas fraction, the trigger for activity, and the processes that may quench star formation. The relations between  $\dot{M}_s$  and both AGN luminosity and C IV FWHM are consistent with star formation rates in quasars scaling with black hole mass, though we cannot rule out a separate relation with black hole accretion rate. Star formation rates are observed to decline with increasing C IV equivalent width. This decline can be partially explained via the Baldwin effect, but may have an additional contribution from one or more of three factors;  $\dot{M}_i$  is not a linear tracer of  $L_{2500}$ , the Baldwin effect changes form at high AGN luminosities, and high C IV EW values signpost a change in the relation between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$ . Finally, there is no strong relation between  $\dot{M}_s$  and Eddington ratio, or the asymmetry of the C IV line. The former suggests that star formation rates do not scale with how efficiently the black hole is accreting, while the latter is consistent with C IV asymmetries arising from orientation effects.

**Key words:** galaxies: evolution – quasars: general – galaxies: starburst – galaxies: star formation – infrared: galaxies.

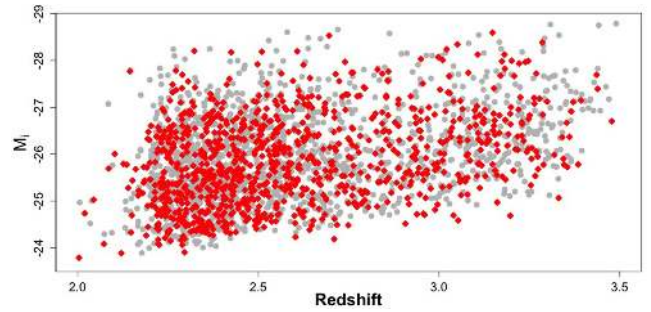
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## 1 INTRODUCTION

Three lines of evidence suggest that, at all redshifts, there is a deep connection between star formation rates in galaxies, and the presence and properties of active galactic nuclei (AGN) in their centres. First, there is a strong similarity in the evolution of comoving luminosity density of AGN and star formation (e.g. Madau & Dickinson 2014). For AGN, the optical luminosity function of quasars plateaus between  $2 < z < 3$  (e.g. Richards et al. 2006a; Delvecchio et al. 2014). For star formation, the comoving star formation rate density increases by a factor of at least 10 over  $0 < z < 1$  (e.g. Lilly et al. 1996; Dickinson et al. 2003; Merloni, Rudnick & Di Matteo 2004; Wang et al. 2013a), peaks at  $z \sim 2$  (e.g. Connolly et al. 1997; Somerville, Primack & Faber 2001; Lanzetta et al. 2002; Hopkins et al. 2006) and then declines at higher redshifts (e.g. Pérez-González et al. 2005; Wall, Pope & Scott 2008; Wuyts et al. 2011; Béthermin et al. 2012). Secondly, there is a positive relationship between stellar and supermassive black hole (hereafter just black hole) mass in quiescent galaxies, with more massive black holes being found in systems with, on average, a higher bulge stellar mass (e.g. Magorrian et al. 1998; Tremaine et al. 2002). Finally, observations find luminous star formation and AGN in the same galaxies at rates significantly higher than expected by chance (e.g. Genzel et al. 1998; Farrah et al. 2003; Alexander et al. 2005; Lonsdale, Farrah & Smith 2006; Coppin et al. 2010; Mainieri et al. 2011; Farrah et al. 2013; Wang et al. 2013b; Casey, Narayanan & Cooray 2014; Pitchford et al. 2016).

The scaling relations, or lack thereof, between star formation rates and AGN properties as a function of variables such as redshift, luminosity, stellar mass and environment, are fundamental to understanding the nature of this connection, and by extension to understanding the mass assembly history of galaxies throughout the history of the Universe. The existence and nature of such scaling relations give insights into how initially free baryons are converted into stars and black holes, and how these conversions are affected by factors such as free gas availability. They also give insights into more apparent manifestations of this connection, such as the idea that star formation and AGN activity can directly affect each other. One example of this is ‘AGN quenching’, where winds or jets from an AGN curtail star formation in its host galaxy on time-scales much shorter than gas depletion time-scales (see e.g. Fabian 2012, for a review). AGN quenching is motivated both by models (Croton et al. 2006; Somerville et al. 2008; Hirschmann et al. 2014; Schaye et al. 2015), which in many cases require quenching to bring their predictions in line with observations, and by some observations that find massive outflows of gas that are plausibly linked to both AGN winds, and reductions in star formation rates (Chung et al. 2011; Farrah et al. 2012; Trichas et al. 2012; Guillard et al. 2015). Another example is the suggestion that, in some circumstances, the AGN can trigger star formation (e.g. King 2005; Gaibler et al. 2012; Ishibashi & Fabian 2012; Silk 2013; Zubovas et al. 2013).

In this paper we explore the connection between AGN activity and star formation in optically luminous type 1 quasars at  $2 < z < 3$ . We choose this class of object since they are straightforward to find, correspond to a specific stage in the AGN duty cycle, and reside at the epoch where the comoving luminosity density arising from both star formation and AGN activity is expected to peak. We assemble our sample from the Sloan Digital Sky Survey, restricted to fields with high-quality far-infrared imaging, from which we derive star formation rates. We compare host star formation rates to the properties of the AGN as derived from the SDSS data to see how star formation rates depend on AGN properties across the quasar



**Figure 1.** The  $z - M_i$  plane showing both all SDSS DR9 quasars in Stripe 82 with uniform flag  $> 0$  and  $2.15 < z < 3.5$  (grey points), and our sample of quasars (red points). The distributions of the red and grey points are identical by visual inspection, and indistinguishable via a K–S test (Section 2.1).

population. We adopt AB magnitudes, and assume a spatially flat cosmology with  $\Omega_m = 0.3$  and  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ .

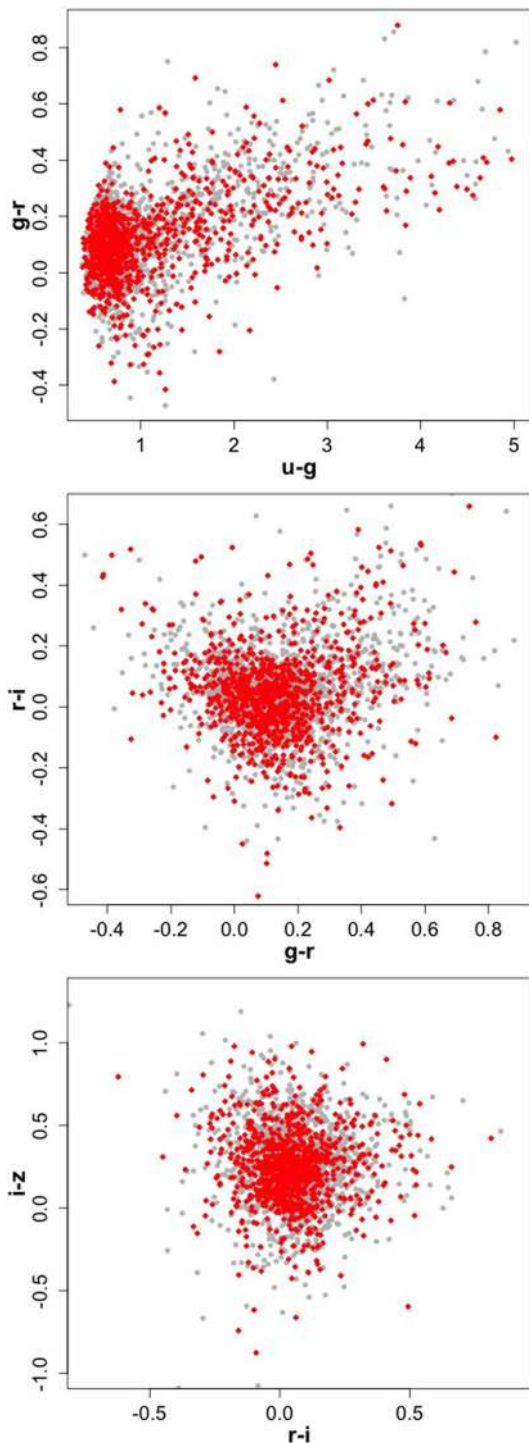
## 2 DATA

### 2.1 Sample selection

We selected our sample from the Baryonic Oscillation Spectroscopic Survey (BOSS), itself part of the Sloan Digital Sky Survey Data Release 9 Quasar catalogue (SDSS DR9Q; Paris et al. 2012). By selecting from BOSS, we can assemble the necessary number of quasars to subdivide into multiple bins based on various criteria, and still have sufficient objects per bin to perform stacking analyses (see Section 3).

We start with the 61 931 SDSS DR9 quasars at  $z > 2.15$ . Our selection comprises four steps. First, we excluded all BOSS quasars that did not lie within Stripe 82. This left 9520 objects. Secondly, we excluded all quasars with a uniform flag of zero or below, leaving only those with a uniform flag of 1 or 2. The remaining quasars are the CORE quasar selection within BOSS. The CORE selection is both homogeneous and uniform, and is highly, but not entirely complete over the range  $2.15 \leq z \leq 3.5$  (Ross et al. 2012; White et al. 2012). We discuss the issue of completeness further in Section 5.1. This step left 6516 objects. Third, we excluded all quasars at  $z > 3.5$  and  $z < 2.15$ , leaving 3256 objects. Fourth, we excluded quasars that lie outside or within 20 pixels of the edge of the HerS and/or HeLMS data (Section 2.2), so that there were sufficient pixels in the stacked images to allow for clustering corrections (Section 3.1). The pixel sizes differ for each band, with the largest being for  $500 \mu\text{m}$ . We therefore used the  $500 \mu\text{m}$  image for this step, which left 1002 objects. Our selection does not include steps to remove either Broad Absorption Line (BAL) quasars, or sources with radio data. The effects of this decision are described in Section 5.4.

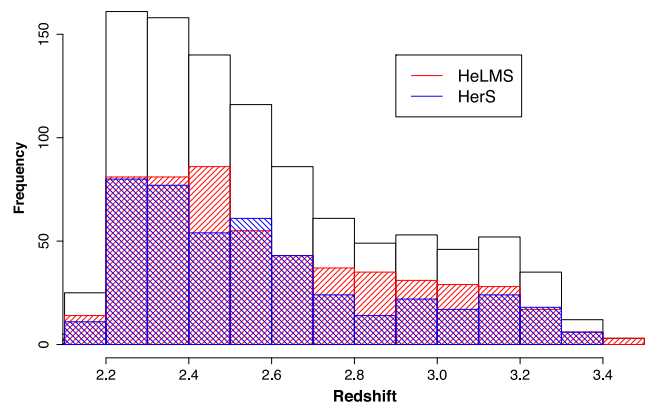
We checked how our sample compared to all of the SDSS BOSS quasars within Stripe 82. The absolute  $i$ -band magnitudes as functions of redshift of the two samples are qualitatively identical (Fig. 1). A KS test yields a  $p$ -value of 0.685; high enough to accept the null hypothesis that they are from the same parent population. Comparing their SDSS colours (Fig. 2) again gives qualitatively identical distributions, and  $p$ -values high enough to accept that they are drawn from the same parent population ( $\geq 0.18$  in all cases). Their redshift distributions (Fig. 3) show no differences, and yield a  $p$ -value of 0.86. We repeated these tests with the HerS and HeLMS fields separately, and found no significant differences. We conclude that our sample is representative of the SDSS BOSS Stripe 82 quasar population at  $2.15 < z < 3.5$ .



**Figure 2.** Observed-frame colour–colour diagrams for our sample (red) and all SDSS DR9 quasars in Stripe 82 with uniform flag  $>0$  and  $2.15 < z < 3.5$  (grey). The distributions are identical by visual inspection, and indistinguishable via a K–S test.

## 2.2 Far-infrared imaging

We assembled far-infrared imaging data from the *Herschel* Stripe 82 Survey (HerS; Viero et al. 2014) and the HerMES Large-Mode Survey (HeLMS; Oliver et al. 2012, map version 0.2). Both surveys were performed using the Spectral and Photometric Imaging Receiver instrument (SPIRE; Griffin et al. 2010) onboard the *Herschel*



**Figure 3.** Redshift distributions for the quasars in HeLMS and HerS (red and blue hatched histograms, respectively) and for all SDSS DR9 quasars in Stripe 82 with uniform flag  $>0$  and  $2.15 < z < 3.5$  (white solid).

Space Observatory (Pilbratt et al. 2010), in the 250  $\mu\text{m}$ , 350  $\mu\text{m}$  and 500  $\mu\text{m}$  bands. Both of the surveys form part of the *Herschel* Multi-tiered Extragalactic Survey (HerMES; Oliver et al. 2012). HeLMS cover 270  $\text{deg}^2$  and HerS covers 79  $\text{deg}^2$ , with an overlap between the two of 6  $\text{deg}^2$ . The HerS and HeLMS surveys together cover 115 of the 255  $\text{deg}^2$  SDSS Stripe 82 field (Abazajian et al. 2009). *Herschel* map-making details can be found in Patanchon et al. (2008) and Viero et al. (2014).

## 3 ANALYSIS

The high redshifts of our sample mean they are virtually all individually undetected by *Herschel*. Of the 1002 quasars, only  $\sim 5$  per cent have a catalogue flux density in at least one band, and in all cases those flux densities are close to the detection limit. To measure their star formation rates we thus stack the *Herschel* data for sets of objects selected according to specific criteria, and then fit model spectral energy distributions (SEDs) to the stacked flux densities to extract mean star formation rates for that set. We describe the stacking and SED fitting procedures in the following subsections.

### 3.1 Stacking

We stacked our sample as a function of six variables, all taken from Paris et al. (2012): redshift; absolute  $i$ -band magnitude ( $M_i$ );  $\Delta[g - i]$  colour; and the (rest-frame) equivalent width (EW), Full Width at Half Maximum (FWHM), and FWHM asymmetry of the  $\text{C IV } \lambda 1549 \text{ \AA}$  line (hereafter we refer to this line as  $\text{C IV}$ ). The  $M_i$  values include a correction for Galactic extinction and assume a power law continuum index of  $\alpha = -0.5$ . The  $K$ -corrections are pegged to the  $i$ -band for a quasar at  $z = 2$  rather than  $z = 0$  as  $K$ -correcting to a redshift close to the median redshift of the sample substantially reduces systematic error. The consequence is that the  $M_i$  values are distance-corrected to 10 pc but are  $K$ -corrected to the equivalent of the  $i$ -band filter observing at  $z = 2$ , i.e. rest-frame 2500  $\text{\AA}$ . The  $K$ -corrections are computed using the values in table 4 of Richards et al. (2006a). The  $\Delta[g - i]$  values are the Galactic extinction corrected difference in observed-frame  $g - i$  colour between a quasar and the mean for all SDSS DR9 quasars at the same redshift. The  $\text{C IV}$  asymmetry is the ratio of the blue-side FWHM to the red-side FWHM.

We found that each *Herschel* stack needed a minimum of 20 quasars to give detections or useful limits. We thus arranged



the bin spacing of the variables to ensure at least 20 quasars per bin as a first priority, and to be approximately equally spaced as a second priority. The resulting bins were as follows:

(i)  $z$ : 11 bins with mean values: 2.205, 2.286, 2.370, 2.452, 2.540, 2.639, 2.746, 2.854, 2.970, 3.108, 3.266. These intervals correspond to  $\Delta t = 0.1$  Gyr.

(ii)  $M_i$ : eight bins with mean values:  $-24.33$ ,  $-24.75$ ,  $-25.25$ ,  $-25.75$ ,  $-26.25$ ,  $-26.75$ ,  $-27.25$ , and  $-27.88$ .

(iii)  $\Delta[g - i]$ : eight bins with mean values:  $-0.34$ ,  $-0.24$ ,  $-0.14$ ,  $-0.05$ ,  $0.05$ ,  $0.15$ ,  $0.25$ ,  $0.35$ . The histogram of  $\Delta[g - i]$  is approximately a Gaussian centred at zero with an FWHM of  $\sim 0.16$ . Hence, to ensure  $>20$  objects per bin we restrict the  $\Delta[g - i]$  to this range. We do however explore  $\Delta[g - i]$  values outside this range in Section 4.2.

(iv)  $C_{IV}$  FWHM ( $F_C$ ): 10 bins with mean values: 2467, 2991, 3474, 3858, 4200, 4543, 4873, 5281, 5859, and 6986  $\text{km s}^{-1}$ .

(v)  $C_{IV}$  EW ( $E_C$ ): 11 bins with mean values: 20.48, 28.59, 33.50, 37.76, 41.71, 47.52, 54.95, 63.92, 78.40, 96.16, and 136.30 nm.

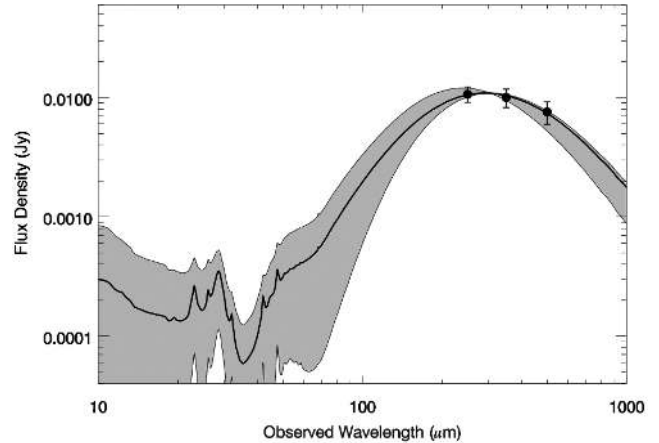
(vi)  $C_{IV}$  FWHM asymmetry ( $A_C$ ): 10 bins with mean values: 0.492, 0.607, 0.679, 0.740, 0.804, 0.862, 0.915, 0.987, 1.108, and 1.468.

To perform the stacking we followed the approach of previous authors (B  thermin et al. 2010, 2012; Heinis et al. 2013). Sub-images of  $41 \times 41$  pixels were extracted around each object and placed in a data cube. This sub-image size gives a spatial scale, at  $z = 2$ , of  $\sim 2$  Mpc for the  $250 \mu\text{m}$  band and  $\sim 4$  Mpc for the  $500 \mu\text{m}$  band. The stacked flux density in each pixel is then the mean of that column in the data cube. The flux density is found by fitting to the stacked profile a model point-spread function (PSF) for SPIRE, as implemented within the *Herschel* Interactive Processing Environment (HIPE) v12 (Ott et al. 2010). The random error for each stacked pixel was calculated via bootstrap resampling; multiple samples of images were selected without withdrawal from each data cube, stacked, and the resulting pixel flux densities calculated. In the six  $\text{deg}^2$  overlap region between HerS and HeLMS, we used only the HeLMS data, which are deeper, since adding the HerS data to the HeLMS data made a negligible difference to the results.

### 3.2 Clustering correction

The coarse spatial resolution of SPIRE means that flux density measurements of individual sources may be boosted due to the presence of other, individually undetected sources in the area covered by the SPIRE beam. It is however straightforward to derive a reasonably accurate correction for this effect. Star formation in high-redshift systems typically spans scales of  $\lesssim 30$  kpc (e.g. Carniari et al. 2013; Wiklind et al. 2014; Simpson et al. 2015), or  $\lesssim 3.72$  arcsec at  $z = 2.5$ . This star formation will be unresolved by SPIRE. Thus, if host galaxy star formation alone is present in the *Herschel* beam, the detections in the stacked images will be point sources. Any deviations from a point source profile can thus be ascribed to contributions from other far-infrared-emitting sources around the quasars.

To correct for these sources we compared the profiles of the stacked images to that of the SPIRE PSF. We found that in all cases there was a small but clear excess over a pure PSF profile. To model these excesses we fitted a model consisting of the SPIRE PSF plus a power law with slope of 1.8 to each stacked profile (B  thermin et al. 2010, 2012; Heinis et al. 2013). The power-law profiles are then the clustering correction for each stack, and were removed. The sizes of the clustering corrections ranged from  $\sim 10$  per cent for  $250 \mu\text{m}$  to  $\sim 22$  per cent for  $500 \mu\text{m}$ .



**Figure 4.** An example fit of a starburst model to the SPIRE fluxes extracted from the stacked data (Section 3.3). This fit is for the seventh  $M_i$  bin (see supplementary online materials). The black line shows the best-fitting SED, while the shaded region shows the range in SED shapes that are consistent with the range in starburst luminosity for this fit.

We checked the effect of image cutout size on the derived clustering correction by repeating the clustering analysis, starting with a size of  $11 \times 11$  pixels and increasing it until no effect on the clustering correction was seen. We found that  $41 \times 41$  pixels was the smallest size that produced a clustering correction not dependent on the image size, and so adopted this size for the stacking.

### 3.3 Star formation rates

We estimate star formation rates by fitting the SPIRE data with radiative transfer models for a star-forming region (Efstathiou, Rowan-Robinson & Siebenmorgen 2000; Efstathiou & Siebenmorgen 2009). There is substantial theoretical (e.g. Pier & Krolik 1992; Fritz, Franceschini & Hatziminaoglou 2006; Schartmann et al. 2008) and observational (e.g. Schweitzer et al. 2006; Netzer et al. 2007; Hatziminaoglou et al. 2010; Shao et al. 2010; Mullaney et al. 2011; Rosario et al. 2012; Magdis et al. 2013; Delvecchio et al. 2014; Zakamska et al. 2016) evidence that radio-quiet AGN are at least 0.5–1 dex less luminous than star formation at  $\lambda_{\text{rest}} > 60 \mu\text{m}$ . Since the SPIRE bands always sample  $\lambda_{\text{rest}} > 80 \mu\text{m}$  at  $z < 3$ , it is plausible that the contribution from AGN-heated dust to the SPIRE flux densities is insignificant. We do however explore the possibility of an AGN contribution in Section 5.3.

The fits are excellent, with  $\chi^2_{\text{red}} < 1$  in all cases. An example fit is shown in Fig. 4. We determine starburst luminosities and their errors by combining the acceptable fits into a weighted probability distribution function (PDF) and then extracting the peak and 68 per cent confidence interval of the PDF. As such, the errors include uncertainty arising from both the formal error on the best fit, as well as from the range in acceptable SED shapes and the SPIRE absolute calibration error. In all cases the PDFs are consistent with Gaussian profiles.

The starburst models vary in age, initial optical depth of the molecular clouds, and e-folding time,  $\tau$ , of the star formation rate (assuming a decline of the form  $e^{-t/\tau}$ ) over the ranges 0–70 Myr, 50–125, and 10–40 Myr, respectively. With only three flux densities we cannot constrain these parameters. We adopt this approach rather than fitting a modified blackbody for two reasons. First, using a

**Table 1.** The SPIRE fluxes used to produce Fig. 5. The data for the other plots are given in the supplementary online materials.

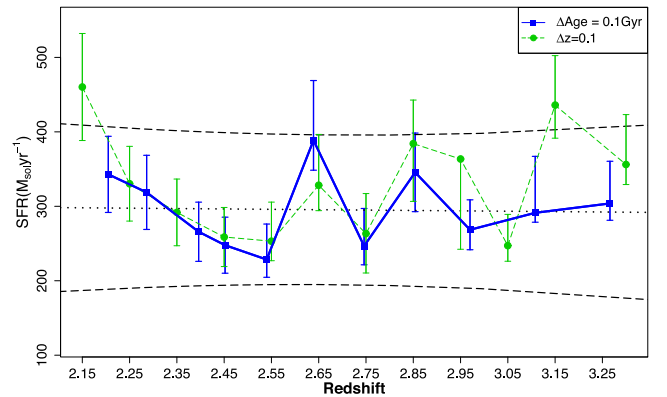
	Redshift	250 $\mu\text{m}$ flux (mJy)	350 $\mu\text{m}$ flux (mJy)	500 $\mu\text{m}$ flux (mJy)
$\Delta t = 0.1$ Gyr	2.20	$9.12 \pm 0.87$	$11.91 \pm 1.96$	$5.96 \pm 1.78$
	2.29	$7.71 \pm 1.13$	$7.92 \pm 1.16$	$5.71 \pm 1.29$
	2.37	$6.20 \pm 1.04$	$5.89 \pm 1.15$	$3.53 \pm 1.12$
	2.45	$5.84 \pm 1.02$	$5.64 \pm 1.38$	$3.06 \pm 1.19$
	2.54	$4.67 \pm 1.11$	$5.09 \pm 1.20$	$4.33 \pm 1.23$
	2.64	$7.63 \pm 1.37$	$9.98 \pm 1.65$	$4.24 \pm 1.61$
	2.75	$3.63 \pm 1.34$	$6.97 \pm 1.41$	$2.24 \pm 1.43$
	2.85	$5.85 \pm 1.80$	$8.64 \pm 1.83$	$1.12 \pm 1.80$
	2.97	$3.83 \pm 1.66$	$5.85 \pm 1.73$	$2.95 \pm 1.95$
	3.11	$3.80 \pm 1.58$	$5.52 \pm 1.81$	$5.00 \pm 1.78$
$\Delta z = 0.1$	3.27	$3.83 \pm 1.44$	$4.89 \pm 1.44$	$4.24 \pm 1.50$
	2.25	$7.65 \pm 1.25$	$8.27 \pm 1.15$	$4.93 \pm 1.43$
	2.35	$6.68 \pm 0.96$	$5.49 \pm 1.02$	$5.49 \pm 1.10$
	2.45	$6.35 \pm 1.06$	$5.75 \pm 1.37$	$2.65 \pm 1.31$
	2.55	$5.05 \pm 1.48$	$5.94 \pm 1.43$	$4.51 \pm 1.28$
	2.65	$6.64 \pm 1.34$	$8.19 \pm 1.63$	$3.42 \pm 1.55$
	2.75	$3.91 \pm 1.33$	$7.33 \pm 1.37$	$2.27 \pm 1.45$
	2.85	$6.69 \pm 1.78$	$9.14 \pm 1.75$	$1.11 \pm 1.88$
	2.95	$0.10 \pm 2.54$	$3.07 \pm 2.24$	$5.04 \pm 2.60$
	3.05	$2.67 \pm 2.54$	$5.46 \pm 2.47$	$3.24 \pm 2.52$
	3.15	$6.60 \pm 2.05$	$8.31 \pm 2.34$	$4.19 \pm 1.98$
	3.28	$4.68 \pm 1.75$	$4.28 \pm 1.96$	$5.71 \pm 1.57$

reasonable range of starburst SED shapes gives a better estimate of the uncertainties on the star formation rates. Secondly, a modified blackbody does not include mid-IR emission from PAHs and hot dust species and hence underestimates the IR emission due to star formation by approximately 10 per cent.

### 3.4 Sources of uncertainty

We considered five potential sources of uncertainty to assess their impact on subsequent analyses. First, we checked to see if a small number of objects were unduly affecting the stacked flux densities. To do so we tested each stack with jackknife resampling. The jackknife test was run 20 times on a random selection of samples. Each stack was split into two equal size subsamples, stacked, and the flux density measured. The values for each half were in all cases within the errors of the value for the full stack. Secondly, we inspected the optical spectra of all our sample for signs of contaminating sources along their lines of sight, but found none. Thirdly, we assumed that no colour corrections were required, since such colour corrections are negligible for objects with a quasar spectral index (Griffin et al. 2010). Fourthly, we did not attempt to correct for contributions from Galactic dust emission (e.g. Wang et al. 2015). If Galactic dust does contribute, it would systematically overestimate the flux densities by at most 10 per cent at 250  $\mu\text{m}$ , and 30 per cent at 500  $\mu\text{m}$ . Fifthly, we have no *a priori* knowledge of the actual distribution of the *Herschel* flux densities of our sample. Thus, we do not know how close the mean signal from the stacks is to the mode, or typical signal, of the population. The results from the jackknife test suggest however that the mean and mode are close to each other.

There remain further caveats to our results; the completeness of the sample, the effect of starburst SED choice, the potential contribution to the far-infrared emission from an AGN, and the contribution from BAL and radio-loud quasars. These caveats are reviewed in Section 5.



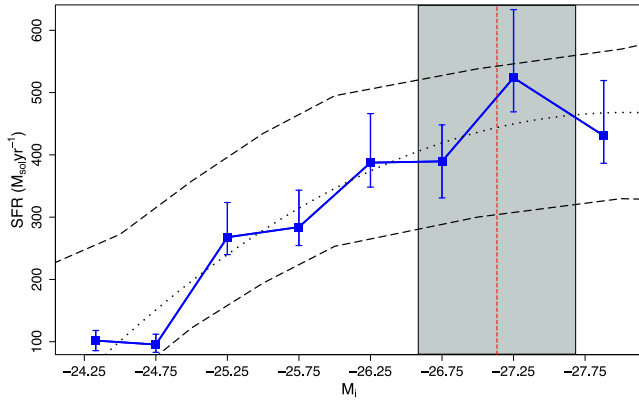
**Figure 5.** The evolution with redshift of star formation rates in quasar hosts (Section 4.1). The data are shown for bins of equal width in both age (blue) and redshift (green). The black lines show the model fit in equation (1) and the 90 per cent confidence interval.

## 4 RESULTS

This section presents the correlations between star formation rates and catalogue quantities given in Paris et al. (2012). The relations with quantities derived from these quantities are presented in the discussion. The star formation rates can be converted to infrared luminosities via equation (4) of Kennicutt (1998). The flux densities used to infer the results are tabulated; in Table 1 for the results in Section 4.1 and in the supplementary online material for the remainder.

### 4.1 Redshift

The evolution of  $\dot{M}_s$  with redshift is shown in Fig. 5. There is significant scatter, but the data are consistent with an approximately constant mean star formation rate across  $2.15 < z < 3.5$  of  $\sim 300 M_\odot \text{ yr}^{-1}$ . This result is independent of whether the data



**Figure 6.** Star formation rate as a function of  $M_i$  (Section 4.2). The blue points show the data and the black lines show the model in equation (2) and its 90 per cent confidence interval. The vertical red line and grey shaded region show the  $M_i$  and uncertainty for  $L^*$  quasars at  $2.5 < z < 3.8$  (Delvecchio et al. 2014, with  $K$ -correction to  $z = 2$  from Richards et al. (2006b)).

are binned by redshift or lookback time. Fitting a linear model to the  $\Delta t$  points gives

$$\dot{M}_s = (-5 \pm 48)z + (309 \pm 130) \quad (1)$$

where  $\dot{M}_s$  is in units of  $M_\odot \text{ yr}^{-1}$ . This is consistent to within  $1\sigma$  with no evolution. For this model to reproduce the data, the 90 per cent confidence interval is  $\pm 100 M_\odot \text{ yr}^{-1}$ . The bins in Fig. 5 correspond approximately to  $\Delta t = 100 \text{ Myr}$ , which is of order the length of the quasar duty cycle (Kelly et al. 2010). However, since we are averaging together  $>20$  quasars, each of which represents a (probably) random point in that duty cycle, the bins should be uncorrelated.

Considering smaller ranges in redshift; the group of five bins spanning  $2.15 < z < 2.55$  shows a decrease in star formation rate from bin to bin, of about  $200 M_\odot \text{ yr}^{-1}$  in total. Moreover, the rise appears statistically significant; the Pearson correlation coefficient for just these five points is  $-0.99$ . The rise is unlikely to be an artefact of the binning, since we see the same trend in bins of equal  $\Delta z$ .

#### 4.2 Absolute magnitude

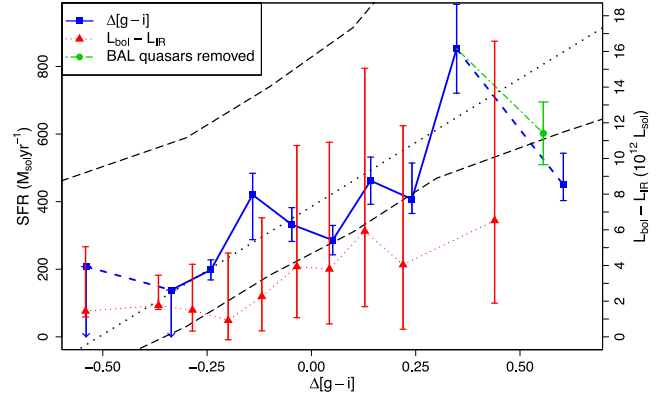
Fig. 6 shows the relation between  $\dot{M}_s$  and  $M_i$  (recall from Section 3.1 that  $M_i$  samples rest-frame  $2500 \text{ \AA}$ ). There is a rise in star formation rate with increasing  $M_i$ . Fitting, purely as a phenomenological choice, a quadratic model yields

$$\dot{M}_s = -(29 \pm 16)M_i^2 - (1638 \pm 825)M_i - (22\,505 \pm 10\,744) \quad (2)$$

The flattening, or possible decline in star formation rate in the highest  $M_i$  bin coincides approximately with the  $M_i$  for  $L^*$  quasars at  $z \sim 3$  (Delvecchio et al. 2014). However, the decline is not statistically significant.

#### 4.3 Colour

Fig. 7 shows the relation between  $\dot{M}_s$  and  $\Delta[g-i]$ . The distribution of  $\Delta[g-i]$  values means we have sufficient objects to investigate this relation only over the range  $-0.35 < \Delta[g-i] < 0.35$ . We see



**Figure 7.** Star formation rate versus  $\Delta[g-i]$  (Section 4.3). The blue points show the data. The solid blue line shows the range in  $\Delta[g-i]$  over which we have enough objects to be confident of the results (Section 3.1). The black lines show the model in equation (3) and its 90 per cent confidence interval (Section 4.2). The points connected by dashed blue lines are those for which we have only a few objects, and are thus less trustworthy. The green point is the same as the last blue point but with the BAL quasars removed. The red line shows the difference between the bolometric and infrared luminosities as a function of  $\Delta[g-i]$ , according to the right-hand scale (Section 6.2).

increasing star formation rates with increasing  $\Delta[g-i]$ . Fitting a linear model yields:

$$\dot{M}_s = (758 \pm 213)\Delta[g-i] + (385 \pm 47) \quad (3)$$

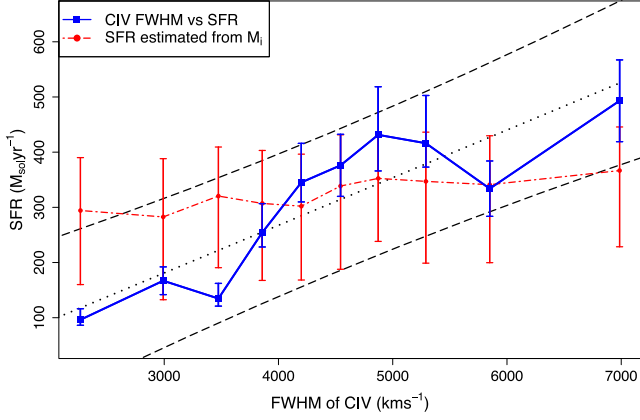
We also explored the relation between  $\dot{M}_s$  and  $\Delta[g-i]$  outside the range  $-0.35 < \Delta[g-i] < 0.35$ . The bins in question have only a few objects so we do not include them in the fit. They are consistent with the  $\dot{M}_s - \Delta[g-i]$  relation remaining flat at low  $\Delta[g-i]$  and turning over at high  $\Delta[g-i]$ .

We checked for four possible contributions to these trends. First, we examined the relation between redshift and  $\Delta[g-i]$ . We found no clear relationship, suggesting that the trends in Fig. 7 are not dominated by emission lines moving into and out of the  $g$  and  $i$  bandpasses. Secondly, we examined how  $\Delta[g-i]$  varied with redshift *within* each bin. Again we found no clear trends; each bin in  $\Delta[g-i]$  has approximately the same mean and median redshift. Thirdly, we tested to see if BAL quasars could be affecting the results in any of the bins. The only bin with a significant number of BAL quasars is the last bin. We removed the BAL quasars from this bin and restacked, obtaining the green point in Fig. 7. This point is consistent with the original, suggesting that BAL quasars are not dominating our results. Finally, we examined the *difference* in bolometric and infrared luminosity as a function of  $\Delta[g-i]$ , shown by the red line in Fig. 7. This comparison is discussed in Section 6.4.

#### 4.4 Emission line properties

The redshifts of our sample means that SDSS catalogue measurements of C IV are available for nearly all objects (958/1002). Moreover, the FWHM ( $F_C$ ), EW ( $E_C$ ), and asymmetry ( $A_C$ , see also Section 3.1) of C IV can be related to physical properties of the AGN. The FWHM scales with black hole mass ( $M_{\text{bh}}$ ) and rest-frame continuum ultraviolet luminosity ( $L_{\text{UV}}$ ) as:

$$M_{\text{bh}} \propto F_C^2 L_{\text{UV}}^{0.5} \quad (4)$$



**Figure 8.** Star formation rate versus CIV FWHM (Section 4.4). The blue points show the data, while the black lines show the model in equation (6) and the 90 per cent confidence interval. The red line is the result of using equation (2) to calculate the *predicted* star formation rate associated with the mean  $M_i$  for each bin.

(Baskin & Laor 2005; Vestergaard & Peterson 2006; Sulentic et al. 2007), the EW scales with UV continuum luminosity as

$$E_C \propto L_{UV}^{-0.8} \quad (5)$$

(Baldwin 1977; Kinney, Rivolo & Koratkar 1990), while  $A_C$  may signpost the presence of AGN winds or other large-scale non-virial motions. We therefore compare star formation rates to these CIV properties.

First, we examine the  $\dot{M}_s - F_C$  relation (Fig. 8). We see a positive relationship. A linear model gives a good fit:

$$\dot{M}_s = (0.086 \pm 0.016)F_C - (78 \pm 73) \quad (6)$$

though the data are also consistent with a power-law with index fixed at 0.5:

$$\dot{M}_s = (-455 \pm 129)F_C^{0.5} + (12 \pm 2) \quad (7)$$

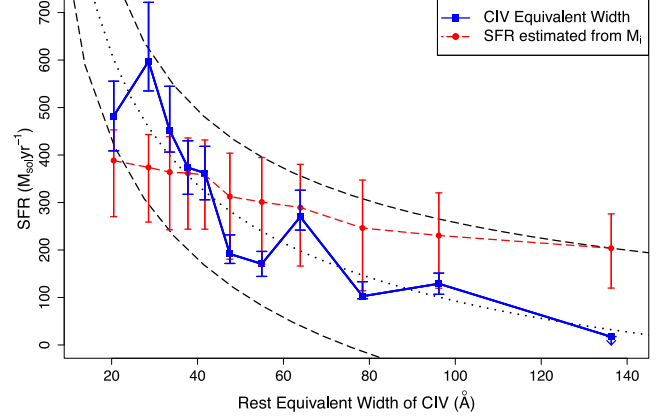
and if the intercept and slope vary freely then any power-law index below about 1.5 fits the data adequately.

We performed two tests to see if this rise is driven by a rise in  $M_i$  (recalling that  $M_i$  samples rest-frame 2500 Å). First, we compared the  $F_C$  and  $M_i$  values of our sample, but found no relation. Secondly, we used equation (2) to convert the average  $M_i$  for each  $F_C$  bin into an  $M_i$ -based star formation rate. These rates are shown by the red line in Fig. 8. We still observe an increase in star formation rate, but the trend is shallower. Fitting a linear model to the red line and comparing to that obtained from the fit to the blue line (i.e. assuming that both relations are linear and comparing their distributions of slopes) reveals that the slopes are different at over  $4\sigma$  significance. Thus, it is plausible that the increase in  $\dot{M}_s$  with  $F_C$  is not (primarily) driven by the 2500 Å luminosity of the quasar, or vice versa.

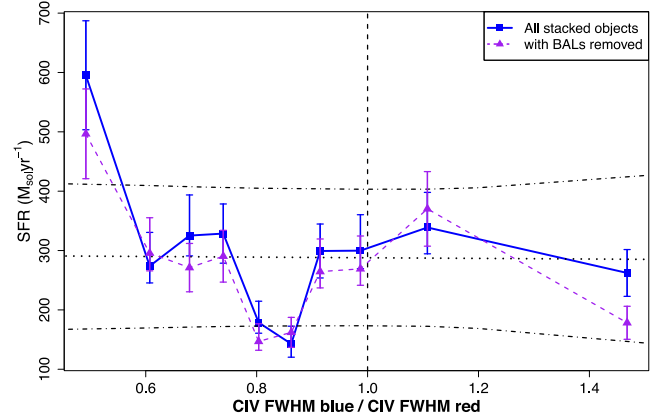
Next, we examine the  $\dot{M}_s - E_C$  relation (Fig. 9). We see a decline in star formation rate as  $E_C$  increases. A power-law model with index  $-0.5$  fits the data well:

$$\dot{M}_s = (4205 \pm 651)E_C^{-0.5} - (328 \pm 98) \quad (8)$$

but the constraints on the index are only that it must be  $\gtrsim -1.8$ . We again checked to see if this trend could be explained by the dependence on  $M_i$ , by using equation (2) to convert the average  $M_i$  for each  $E_C$  bin into an  $M_i$ -based star formation rate. These rates are shown by the red line in Fig. 9. The  $M_i$  based trend has a flatter slope at well over  $4\sigma$  significance. It is thus plausible



**Figure 9.** Star formation rate versus CIV EW (Section 4.4). The blue points show the data, while the black lines show the model in equation (8) and the 90 per cent confidence interval. The red line is the result of using equation (2) to calculate the *predicted* star formation rate associated with the mean  $M_i$  for each bin.



**Figure 10.** Star formation rate versus CIV asymmetry, measured via the blue over red side  $E_C$  (Section 4.4). The blue points show the data, while the black lines show the model in equation (9) and the 90 per cent confidence intervals. The purple line reproduces the blue line, but with the BAL quasars removed.

that the relation between  $\dot{M}_s$  and  $E_C$  is not driven solely by the 2500 Å luminosity of the quasar.

Finally, we examine star formation rate as a function of  $A_C$  (Fig. 10). Most points are consistent with a flat relation. There are however two bins,  $A_C = 0.49$  and  $A_C = 0.86$ , that may deviate from a flat relation. Excluding these bins, and fitting a linear model, yields

$$\dot{M}_s = (5 \pm 76)A_C + (293 \pm 72) \quad (9)$$

This fit is consistent with a flat relation, with a mean close to that of the  $\dot{M}_s - z$  relation. The deviations of the  $A_C = 0.49$  and  $A_C \simeq 0.85$  bins from this relation are significant, but only barely so. We assessed the impact of BAL quasars on these trends by excluding them from the stacking. This gives the purple line in Fig. 10. This line is qualitatively identical to the blue line, suggesting that BAL quasars are not the origin of these results.



## 5 CAVEATS

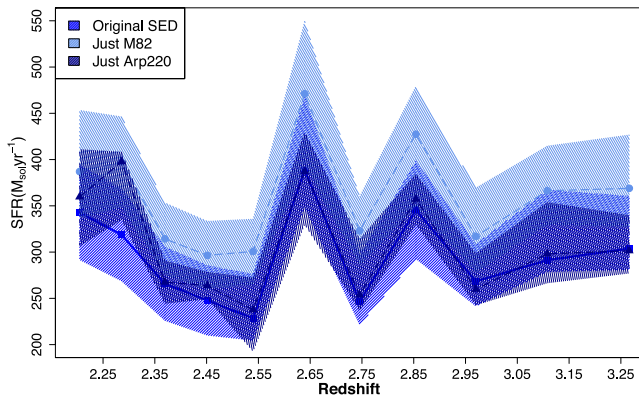
### 5.1 Completeness

Our sample is the CORE quasar sample from SDSS DR9, and thus is uniformly selected, with a well-understood selection function. In this sense it is among the best available  $z > 2.2$  quasar samples. It is however not complete. At redshifts close to  $z = 2.2$ , quasar selection is aided by the strong UV excess of quasars, while at  $z > 2.2$  the presence of the Ly  $\alpha$  forest in the BOSS spectrograph bandpass also helps quasars stand out clearly from stars. At around  $z = 2.7$  however, quasar colours in the SDSS filters become harder to separate from those of A-type stars, meaning that the completeness at these redshifts is lower.

The completeness of SDSS DR9Q is discussed in Ross et al. 2012, their fig. 14. They find that the completeness from single-epoch data varies from 70 per cent at  $z = 2.2$  to 40 per cent at  $z = 2.7$ . However, our sample is entirely within Stripe 82. The deeper, multi-epoch data in this field means that the completeness in this field, and thus our sample, should be higher than that in fig. 14 of Ross et al. 2012 (see also Palanque-Delabrouille et al. 2011; Paris et al. 2012; McGreer et al. 2013). Nevertheless, completeness in our sample will vary as a function of redshift, and will be lower at  $z = 2.7$  than at  $z = 2.2$ . We think it unlikely, though not impossible, that completeness could affect either the global flat trend we find, or the apparent upturn at lower redshifts. It is more plausible that some of the  $1\sigma$ – $2\sigma$  ‘structure’ in Fig. 5 could arise from completeness effects, but we lack the data to assess this possibility. A related issue, the potentially varying contribution from BAL quasars as a function of redshift, is discussed in Section 5.4.

### 5.2 Choice of starburst models

We infer star formation rates by fitting starburst models spanning a broad range in parameters. We do so because we have no a priori knowledge of the star formation. Nevertheless, this approach is atypical. Most other studies use either a modified blackbody model, or smaller libraries of SEDs that resemble either M82 or Arp220. We thus explore the effect on our results by adopting a more limited model set. In Fig. 11 we reproduce the  $\dot{M}_s - z$  relation in Fig. 5 and add the relations obtained using limited libraries corresponding closely to the shape of M82 and Arp220. The M82 library gives star formation rates that are approximately 20 per cent higher than the



**Figure 11.** The effect of SED library choice on the  $\dot{M}_s - z$  relation. This plot reproduces the  $\Delta t$  binned data in Fig. 5 (medium blue), and adds the same relation derived using more restricted SED libraries; ones that closely resemble M82 (light blue) and Arp220 (dark blue).

original values, while the Arp220 library gives star formation rates that are comparable to the original values, albeit with a larger error. In both cases however the form of the  $\dot{M}_s - z$  relation is consistent. A similar investigation for the other parameters in Section 4 yields similar results. We conclude that our results are not significantly altered by choice of SED library. We regard our errors as more reliable than those computed using a limited model set, since they include uncertainty arising from lack of knowledge of the mode of star formation.

### 5.3 Far-infrared emission from AGN

There is controversy over how much far-infrared emission a ‘pure’ AGN (that is, a system whose IR emission is dominated by dust heated by an AGN, with no significant contribution from dust heated by young or main-sequence stars) can produce. Radiative transfer models for dust around AGN generally predict that the rest-frame far-infrared flux is, for the same total infrared luminosity, factors of at least several lower than the far-infrared flux from a starburst (e.g. Fritz et al. 2006; Netzer et al. 2007; Mullaney et al. 2011). However, such AGN models usually do not include kpc-scale dust distributions around the AGN. Such a dust distribution could in principle produce substantially greater far-infrared emission. We thus examined the possibility of an AGN contribution to the *Herschel* data via four approaches.

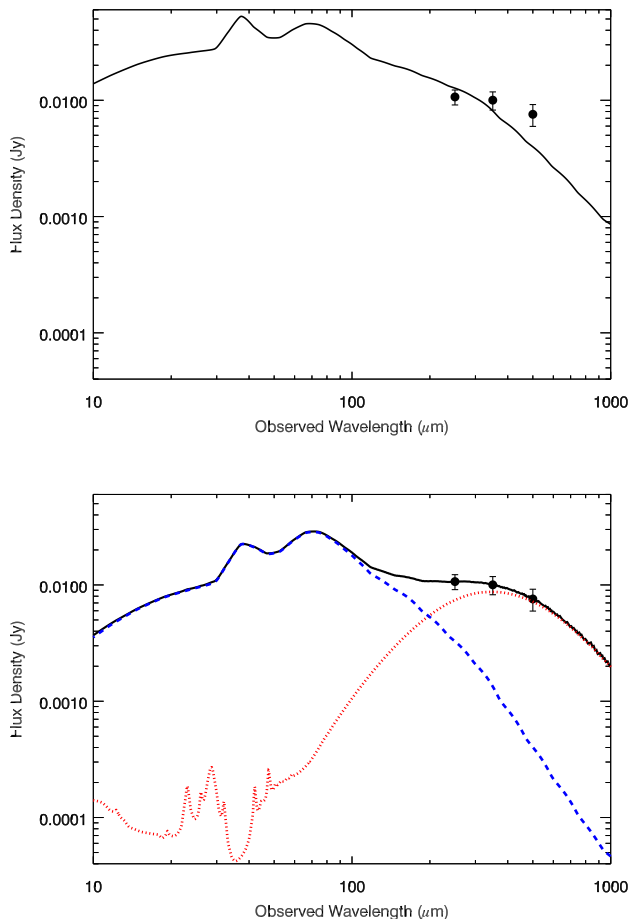
First, we fitted the *Herschel* flux densities with a library of radiative transfer torus models for AGN. We used a different model set to those used in the above-mentioned studies; the library of Efstathiou & Rowan-Robinson (1995). We also imposed the condition that the broad-line region be visible in direct light (in other words, that the viewing angle measured from equatorial is greater than the torus opening angle). As may be expected, the pure AGN fits are in almost all cases both formally rejected, and much worse than the pure starburst fits. We also attempted to fit both the AGN and starburst libraries to the *Herschel* data simultaneously; while the results are highly under-constrained, in all cases a starburst-dominated fit is the best, or joint-best, fit to the data. Examples of both fits are shown in Fig. 12. In all cases where a stack has a detection in all three bands, it is the *shape* of the *Herschel* fluxes that demands a starburst; an AGN model can explain the 250  $\mu\text{m}$  emission but then not the 350  $\mu\text{m}$  or 500  $\mu\text{m}$  emission.

Second, we fitted the same library of torus models to the SDSS *griz* data, and used the best fits to extract predicted *Herschel* flux densities. The results from this test were conceptually the same as from the above test. The AGN models can adequately reproduce the *griz* data but in doing so nearly always predicted *Herschel* flux densities well below those in the stacks. Those few models that could explain most of the 250  $\mu\text{m}$  emission always fell well below the 350  $\mu\text{m}$  and 500  $\mu\text{m}$  emission.

Third, we tried fitting AGN and starburst models simultaneously to the SPIRE, *WISE* and SDSS data in each stack. Since AGN will contribute significantly to the *WISE* and SDSS data, this gives an alternative way to constrain the AGN contribution to the SPIRE data. However, this approach dramatically increased the complexity of the fits but with no significant increase in the accuracy of either the starburst luminosities, or the far-IR contribution from AGN.

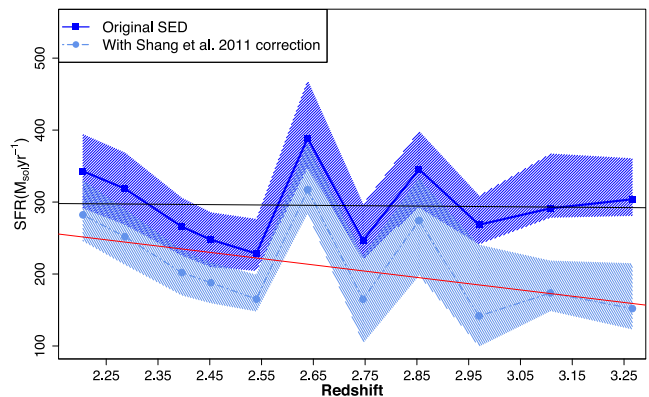
The above tests do not include extremely spatially extended AGN-heated dust. We do not have models with such distributions, and we lack observations that can disentangle the far-infrared emission on sub-kpc scales. So, as a final test we take a different approach, the use of a composite *observed* quasar SED to predict *Herschel* flux densities. Composite quasar SEDs are brighter in the





**Figure 12.** Examples of including AGN models when fitting to the SPIRE data. The top panel shows the best-fitting pure AGN model to the same SPIRE flux densities as in Fig. 4. The model can reproduce the 250  $\mu\text{m}$  and 350  $\mu\text{m}$  data but misses the 500  $\mu\text{m}$  data. The lower panel shows the result of simultaneously fitting both AGN (blue) and starburst (red) models to the data. The fit is under constrained but still predicts that the starburst contributes most of the SPIRE emission.

far-infrared than models for dusty torii around AGN (Elvis et al. 1994; Richards et al. 2006b; Shang et al. 2011). Conversely, in all cases composite SEDs are sparsely sampled at rest-frame  $\geq 70 \mu\text{m}$  and use far-infrared data of sufficiently coarse resolution that they will include emission from star formation in the quasar hosts; the Elvis et al. (1994) sample spans  $0 < z < 0.5$  and uses *IRAS* data, while the Richards et al. (2006b) and Shang et al. (2011) sample have only *Spitzer* (Werner et al. 2004) MIPS 160  $\mu\text{m}$  data. Hence, a composite quasar SED will overcorrect – it will remove both any AGN contribution and the mean star formation rate in the hosts. Nevertheless, we took the composite SED of Shang et al. (2011), normalized it to the  $M_i$  values for each quasar individually, extracted predicted *Herschel* flux densities, and used these to construct a ‘corrected’ version of Fig. 5. The result is shown in Fig. 13. This plot shows a systematically lower star formation rate, by  $\sim 30$  per cent, and a slight negative slope, but the relation between redshift and star formation rate is still consistent with a flat relation. Constructing versions of the other plots with this correction applied reveals similar behaviour – the star formation rates are lower by  $\sim 30$  per cent but the forms of the relations are consistent with our original findings. We deduce that the *maximum possible* downward correction to the star formation rates due to AGN contamination is approximately



**Figure 13.** The effect of using the composite observed quasar SED of Shang et al. (2011) to correct the  $M_s - z$  relation in Fig. 5. The dark blue region shows the original relation while the light blue region shows the relation after normalizing the Shang et al. 2011 SED to the median  $M_i$  of that bin, extracting predicted SPIRE fluxes, and removing them before fitting. As discussed in Section 5.3 this is an overcorrection, so the light blue region should be regarded as a lower limit. Fitting a linear model to the light blue points gives a slight negative slope, but consistent to within  $2\sigma$  with a flat relation.

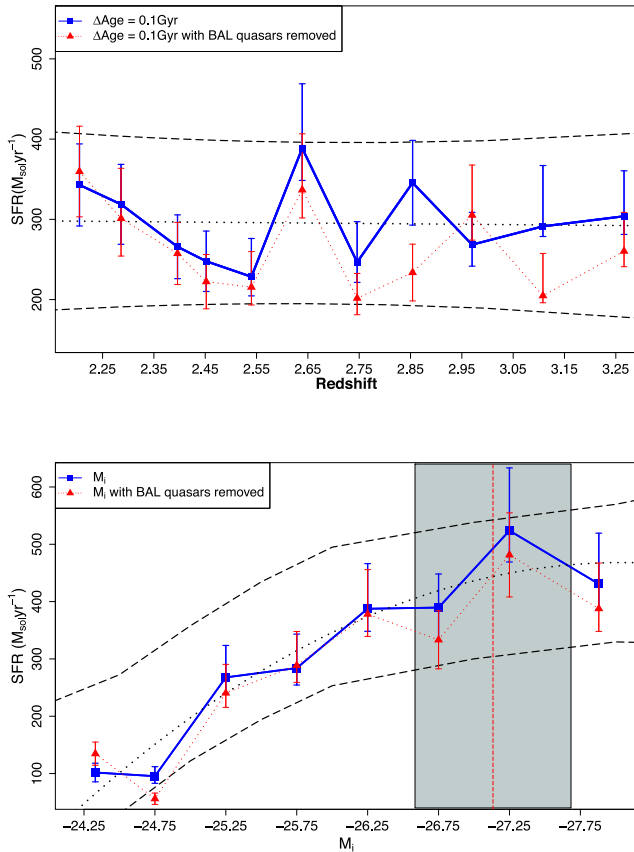
30 per cent, and that the forms of the relations we find are unlikely to change as a result.

Overall, none of our tests reveal evidence for a significant AGN contribution to the *Herschel* fluxes. We cannot, however, rule out such a contribution, as all of the tests we can perform have issues; those based on models may miss extended dust, and those based on observed SEDs likely oversubtract due to host galaxy star formation in those SEDs. However, *the balance of evidence* suggests that rest-frame emission at  $\geq 70 \mu\text{m}$  from quasars is dominated by star formation, so we interpret our results under the assumption that the *Herschel* data arise purely from star formation.

#### 5.4 Radio-loud and BAL quasars

A small fraction (8.3 per cent) of our sample are BAL quasars, mostly High Ionization BAL (HiBAL) quasars, which we have treated identically to the non-BAL quasars. In doing so we assume that HiBALs have indistinguishable far-infrared properties from the general quasar population, which is reasonable based on previous results (Gallagher et al. 2007; Priddey et al. 2007; Pitchford et al. 2016). An even smaller fraction (1.9 per cent) have radio data, and it is likely that many of these objects are radio-loud. However, we have not excluded these objects from our samples. We here explore the effects of these decisions.

Both the BAL quasars and the quasars with radio data have identical (within the errors) distributions in redshift and absolute magnitude as the rest of the sample. However, previous papers have shown that both BAL and radio-loud quasars differ in other respects from classical quasars. The radio detected quasars comprise less than 4 per cent of the quasars in virtually all the stacks. Even if all these quasars are radio-loud, it is unlikely that their inclusion has a significant effect. The BAL quasars on the other hand, while comprising less than 10 per cent of the quasars in most stacks, are in a few cases over 15 per cent. We thus investigated the impact of BAL quasars on our results by repeating the stacking analyses with the BAL quasars removed. Two examples, for redshift and  $M_i$ , are shown in Fig. 14. A further example is shown in Fig. 7. In no case did we find any significant differences, either in terms of mean values or shapes of



**Figure 14.** The effect on Figs 5 and 6 if we remove BAL quasars from the stacks. In neither case do we see significant differences, despite the varying fraction of BAL quasars in each bin.

trends. We conclude that neither the BAL or radio-loud objects in our sample are significantly affecting the trends we observe.

## 6 DISCUSSION

Our results provide insight on both the evolution with redshift of star formation rates in quasar host galaxies, and on the relationship between star formation and AGN activity, at  $2.15 < z < 3.5$ . By stacking *Herschel* SPIRE photometry for a sample of 1002 optically selected quasars, we examine *typical* star formation rates in high-redshift, optically luminous, unobscured AGN, rather than individually detected objects that represent the more extreme star formation events. However, because we require a minimum of 20 objects per bin to achieve robust detections, we can investigate at most 10–12 bins in total, so we cannot reliably explore degeneracies in relationships between parameters. Moreover, when discussing relationships between star formation rate and C IV line properties, we assume that the C IV line arises exclusively from the AGN.

### 6.1 Redshift

We find no evidence for strong evolution of star formation rates in quasar hosts with redshift across  $2.15 < z < 3.5$ . Instead, we find an approximately constant mean star formation rate of  $300 \pm 100 M_{\odot} \text{ yr}^{-1}$ . Our mean rate is higher than the star formation rates seen in  $z \lesssim 2$  AGN (Lacy et al. 2007; Silverman et al. 2009; Floyd et al. 2013; Huseman et al. 2014; Banerji et al. 2015), but

lower than those found in far-infrared luminous (i.e. individually detected) quasars at similar redshifts (Lutz et al. 2008; Pitchford et al. 2016). Finally, if the stellar masses of the host galaxies are of order  $10^{11} M_{\odot}$  then our mean rate lies on or somewhat above the ‘main-sequence’ star formation rate at  $z \sim 2$  (Elbaz et al. 2011; Gruppioni et al. 2013; Magnelli et al. 2013).

The simplest interpretation of this result, together with the relatively flat comoving star formation and quasar luminosity densities over  $2 < z < 3.5$ , is that the processes that trigger quasars evolve in a similar way to the processes that trigger star formation. Furthermore, it is consistent with the bulk of star formation in quasar hosts at this epoch not being in the ‘starburst’ mode (Rodighiero et al. 2011). However, further interpretation depends on the quasar host masses. There is evidence that, at  $z > 1$ , the  $M_{\text{bh}}/M_s$  ratio is higher than at low redshift (that is, the hosts of high-redshift quasars are less massive than low-redshift quasars for the same black hole mass), though the redshift and luminosity evolution of this ratio remain uncertain (Peng et al. 2006; Shields et al. 2006; Salvander et al. 2007; Woo et al. 2008). There also exists a wide range in stellar mass for a given star formation rate at  $z > 1$ ; our mean star formation rate spans a range of over 1 dex in stellar mass (Wuyts et al. 2011). Since we have no measures of the host galaxy masses, we cannot make further inferences from the flat star formation rate relation.

The factor of  $\sim 2$  rise in  $\dot{M}_s$  from  $z = 2.5$  to  $z = 2.1$  is not straightforward to explain. This  $\Delta z$  corresponds to  $\Delta t = 0.5$  Gyr, a factor of a few longer than the quasar duty cycle (Kelly et al. 2010). However, the (rest-frame ultraviolet) galaxy luminosity function does not evolve substantially over  $2 < z < 3$  (Arnouts et al. 2005; Reddy & Steidel 2009; Hathi et al. 2010; Khostovan et al. 2015). Using a Schechter function then  $\phi^*$  and  $\alpha$  change little over this redshift range, while  $M^*$  may change somewhat more (Parsa et al. 2016). A factor of  $\sim 2$  change in  $\dot{M}_s$  over  $2.1 < z < 2.5$  could thus plausibly have a physical origin, related to the masses of galaxies in which quasar activity is triggered. It is however also plausible that this rise is due to an unaccounted for effect in the selection of the DR9 quasar catalogue.

### 6.2 Black hole accretion rate

The  $M_i$  values in Fig. 6 can be converted into a bolometric accretion luminosity  $L_b$  via:

$$\frac{L_b}{L_{\odot}} = \kappa (3.72 \times 10^{21}) 10^{-0.4[M_i + 49.79]} \quad (10)$$

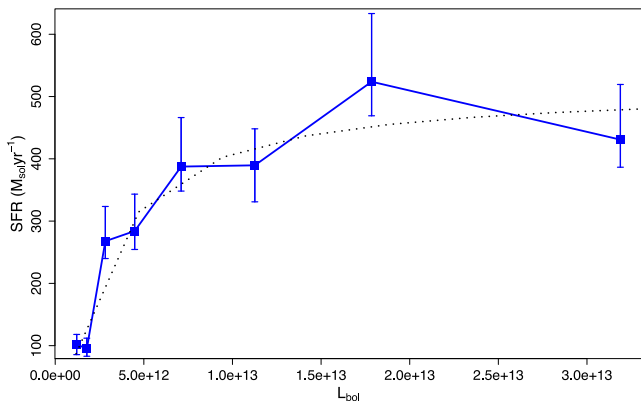
(see also Richards et al. 2006a, their equation 4) where  $\kappa \simeq 5$  is the correction from  $\nu L_{\nu}$  at  $2500 \text{ \AA}$ . This leads to the  $\dot{M}_s - L_b$  relation shown in Fig. 15. An unwieldy expression reproducing this relation can be obtained by substituting equation (10) into equation (2), but a more palatable expression that almost exactly reproduces it is:

$$\dot{M}_s = (11 \pm 135) + (504 \pm 114) \exp \left[ \frac{(2.4 \pm 1.5) \times 10^{12}}{L_b} \right]^{-1} \quad (11)$$

Assuming that the relation between  $L_b$  and  $\dot{M}_{\text{bh}}$  is linear:

$$L_b = \eta \dot{M}_{\text{bh}} c^2 \quad (12)$$

(where  $M_{\text{bh}}$  is the mass of the black hole and  $\eta$  is the fraction of gravitational potential energy radiated away by infalling material, thought to range between 0.06 and 0.42 for a Schwarzschild and Kerr black hole) means that equation (11) is also the form of the relation between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$ .



**Figure 15.** Star formation rate as a function of bolometric accretion luminosity. The  $L_b$  values were computed via equation (10). The dotted line is the relation in equation (11).

Fig. 15 and equation (11) are consistent with the idea that there may be a ‘maximal’ typical star formation rate in optically selected type 1 quasar hosts of  $\sim 600 M_\odot \text{ yr}^{-1}$ , beyond which star formation rates do not rise with increasing accretion rate. Below this value (i.e. neglecting the last point in Fig. 15), the points are consistent with models ranging from a linear relation with a zero intercept

$$\frac{\dot{M}_s}{M_\odot \text{ yr}^{-1}} = (3.56 \pm 0.50) \times 10^{-11} \frac{L_b}{L_\odot} \quad (13)$$

to a power law with index 0.5. Assuming a linear model, converting to SI units and substituting from equation (12) yields

$$\frac{\dot{M}_{\text{bh}}}{\dot{M}_s} = \frac{1.91 \pm 0.27}{\eta} \times 10^{-3} \quad (14)$$

A maximal star formation rate is consistent with the idea that star formation rates in quasar hosts (at least in the domain examined here) ‘saturate’ at high luminosity, perhaps due to supernova winds (see also Geach et al. 2013; Silk 2013). However, the existence of a correlation below this value is more controversial. Our finding of a correlation is consistent with some previous studies on quasars, obscured AGN and star-forming galaxies, although most of these studies sample lower  $L_b$  and  $z$  ranges (e.g. Netzer 2009; Hatziminaoglou et al. 2010; Imanishi et al. 2011; Rafferty et al. 2011; Mullaney et al. 2012b, 2013; Young et al. 2014; Delvecchio et al. 2015; Xu et al. 2015). Moreover, the form of the relation we find is consistent with these studies, which also find that it is linear, or close to linear (e.g. Mullaney et al. 2012b find a linear relation while Netzer 2009; Xu et al. 2015 find  $L_{\text{SF}} \propto L_{\text{AGN}}^{0.8}$ ). Conversely, other studies find a weak, or no relation between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$ , although again these studies are mostly at lower  $L_b$  and/or  $z$  (e.g. Priddey et al. 2003; Shao et al. 2010; Dicken et al. 2012; Harrison et al. 2012; Mullaney et al. 2012a; Rosario et al. 2013; Stanley et al. 2015; Pitchford et al. 2016).

To uncover the origin of this contrast, we consider the ways in which our study differs from previous work; we sample higher AGN luminosities, we have more objects at  $z > 2$ , and we infer relationships via stacking, rather than individual detections. These three differences mean that there are three possible reasons why we see a relationship between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$ , while some other studies have not.

The first is that an  $\dot{M}_s - \dot{M}_{\text{bh}}$  relation only emerges at high redshift, around  $z = 2$  (see also Hatziminaoglou et al. 2010; Rovilos

et al. 2012; Delvecchio et al. 2015). A motivation for this possibility is that the total free gas to stellar mass fraction,  $f_{\text{gas}}$ , rises with redshift as  $\sim (1+z)^2$  up to at least  $z = 1$ , and may plateau at  $z \sim 3$  (e.g. Leroy et al. 2008; Saintonge et al. 2011; Magdis et al. 2012; Tacconi et al. 2013; Troncoso et al. 2014; Popping, Behroozi & Peeples 2015; Lagos et al. 2015). Other studies have suggested that systems with higher  $f_{\text{gas}}$  are more likely to have higher star formation rates, and that there is a strong connection between available cold gas and the probability that a black hole is accreting rapidly (e.g. Genzel et al. 2010; Vito et al. 2014). This possibility would explain the emergence of trends in our study, which (some) previous studies did not find. It is also consistent with the idea that both star formation and black hole accretion depend on the availability of free baryons.

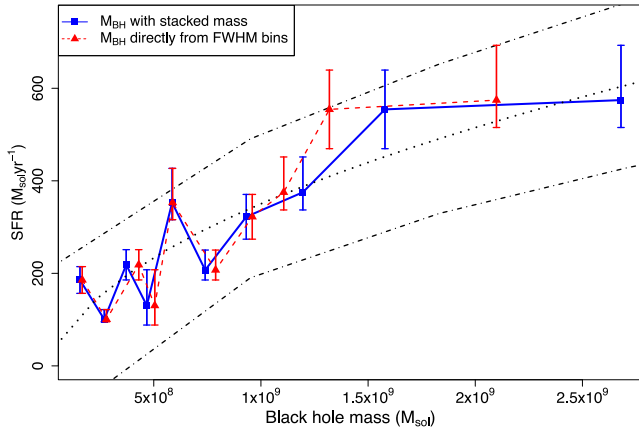
The second is that short-term ( $< 100$  Myr) AGN variability introduces scatter in the  $\dot{M}_s - \dot{M}_{\text{bh}}$  relation derived from measurements of objects individually. This possibility has been suggested both from simulations (Gabor & Bounaud 2013; Volonteri et al. 2015) and observations (Hickox et al. 2014; Stanley et al. 2015). Since we stack large numbers of objects together, any reasonable level of AGN variability would be averaged out. This possibility could thus also explain the contrast between our results and previous work.

The third is that an  $\dot{M}_s - \dot{M}_{\text{bh}}$  relation only emerges at high  $L_b$ , around  $3 \times 10^{12} L_\odot$  (see also Lutz et al. 2008; Shao et al. 2010; Rosario et al. 2012; Rovilos et al. 2012; Banerji et al. 2015). A motivation for this possibility is that black hole growth may correlate with star formation on  $\sim$ sub-kpc scales, but not with star formation on  $\gtrsim$ kpc scales (e.g. Diamond-Stanic & Rieke 2012; Volonteri et al. 2015). If, at high  $L_b$ , star formation in quasar hosts shifted to smaller spatial scales (perhaps because of a higher fraction of merger-triggered rather than secular star formation), then the emergence of a  $\dot{M}_s - \dot{M}_{\text{bh}}$  relation in our sample is natural. This explanation is however not wholly satisfactory. It is in tension with the studies of lower luminosity AGN that do find a correlation, and with studies of quasar hosts with extremely high star formation rates that do not find a strong  $\dot{M}_s - \dot{M}_{\text{bh}}$  relation (Pitchford et al. 2016).

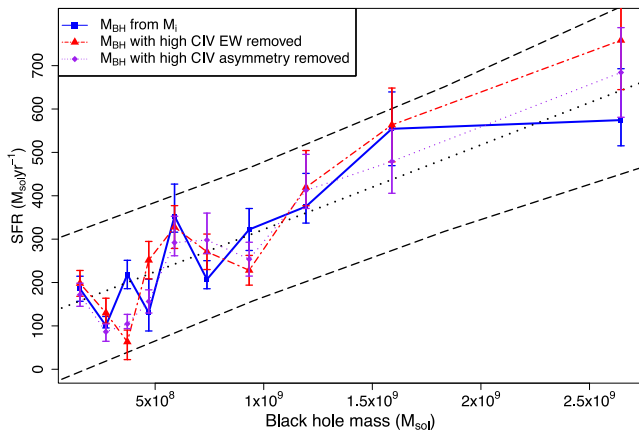
We cannot discriminate between these three possibilities, as to do so requires a larger sample, and X-ray data. We thus speculate, based on our results and previous work, that a correlation between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$  exists in certain parts of the  $z - \dot{M}_s - \dot{M}_{\text{bh}}$  parameter space, dependent on the availability of free baryons, the trigger for activity (major mergers, secular processes, etc.), the potential positive and negative effects of AGN on star formation. Moreover, the form of the correlation – how strong it is, how non-linear it is – also may vary based on the same factors.

### 6.3 Black hole mass

Fig. 8 is consistent with the idea that higher star formation rates are found in quasars with more massive black holes. The data in Paris et al. (2012) preclude an optimal calculation of black hole mass, but the  $M_i$  values sample the rest-frame UV (Section 3.1 and Paris et al. 2012). We thus estimate black hole masses by converting the  $M_i$  values to a monochromatic luminosity at  $1450 \text{ \AA}$  ( $L_{1450}$ ) using equation (3) of Richards et al. (2006a) and then use these luminosities and the  $F_C$  values to compute  $M_{\text{bh}}$  via equation (7) of Vestergaard & Peterson (2006). We performed the stacking in two ways; stacking directly on black hole mass, and calculating the mean black hole masses for each bin in Fig. 8. The results from both approaches are shown in Fig. 16, and are identical within the errors. We see a positive correlation. A power-law model fits the



**Figure 16.** Star formation rate as a function of black hole mass. The results from two approaches are presented; stacking on black hole mass directly, and computing the mean black hole masses for the bins in Fig. 8. The results from both are identical within the errors. The black lines show the model in equation (15) and the 90 per cent confidence interval.



**Figure 17.** The effect on the relation in Fig. 16 if quasars with high  $E_C$  or high  $A_C$  values are removed from the stacks. In neither case do we see significant differences.

data well but the constraints on the index are weak. An index of 0.5 gives an acceptable fit:

$$\dot{M}_s = [(1.3 \pm 0.22) \times 10^{-2}] M_{bh}^{0.5} - (47 \pm 65) \quad (15)$$

but so does a linear model:

$$\dot{M}_s = [(1.92 \pm 0.35) \times 10^{-7}] M_{bh} + (103 \pm 41) \quad (16)$$

and a model with an index of 1/5. As a check on the validity of using the  $M_i$  values to compute  $L_{1450}$ , we estimated  $L_{1450}$  from the SDSS  $g$ -band magnitudes using the same spectral index, and then used these data to compute  $M_{bh}$ . The resulting fit was virtually identical to that obtained by using  $M_i$ . We also checked the effect on these results if the quasars with high  $E_C$  or high  $A_C$  values were removed from the stacks. For  $E_C$  we removed those objects in the last bin in Fig. 9 while for  $A_C$  we removed those objects in the first and last bins in Fig. 10. The results are shown in Fig. 17. In neither case did we see significant differences.

It is illuminating to compare this result to the relations between  $\dot{M}_s$  and both  $F_C$  and  $\dot{M}_{bh}$ . From Section 4.4 we can conclude that  $\dot{M}_s \propto F_C^\alpha$ , where  $0.5 \lesssim \alpha \lesssim 1.4$ . From Section 6.2 we can conclude that  $\dot{M}_s \propto L_b^\beta$ , where  $0.4 \lesssim \beta \lesssim 1.1$ . Assuming that equation (4)

holds then the above findings mean that a relation of the form in equation (15) is expected.

We now address the question; do star formation rates in quasar hosts scale with black hole mass, black hole accretion rate, or both? Given the limitations of our data we can only address this question in a simple way. If  $\dot{M}_s$  scaled solely with  $\dot{M}_{bh}$  then we would not expect to see a strong  $\dot{M}_s - F_C$  relation, but we clearly do. If however  $\dot{M}_s$  scaled solely with  $M_{bh}$ , via e.g.  $\dot{M}_s \propto M_{bh}$ , then we would expect  $\dot{M}_s - F_C$  and  $\dot{M}_s - L_b$  relations that were both power laws, which is what we find. Thus, our results are consistent with star formation rates in quasar hosts scaling with black hole mass. We find no evidence that favours an additional (i.e. beyond that implied by equation 4) scaling between  $\dot{M}_s$  and  $\dot{M}_{bh}$ .

This is consistent with a common gas reservoir fueling both the growth of the black hole and star formation, such that a larger (or more optimally distributed) reservoir leads to both a larger black hole and higher star formation rates. This scaling relation would manifest on time-scales of 100–200 Myr, comparable to both the lifetime of a starburst, and the quasar duty cycle. We thus cautiously propose that the scaling between  $\dot{M}_s$  and  $M_{bh}$  is the most important one for understanding the relationship between black hole mass and stellar mass in quasar hosts. This idea though depends on the starburst ‘saturating’ so as to allow equation (11) to be interpreted as we do.

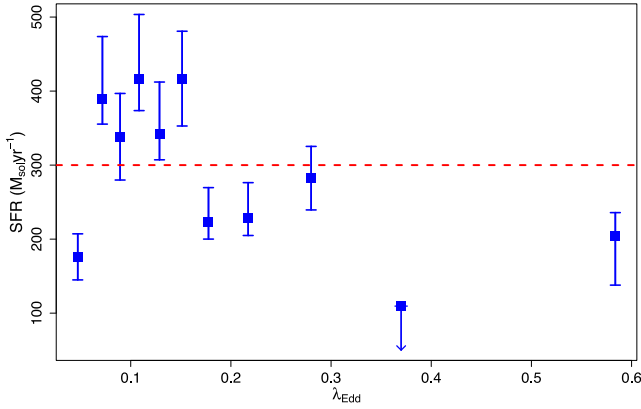
We cannot, however, rule out a separate relation between  $\dot{M}_s$  and  $\dot{M}_{bh}$ . There is room within the uncertainties on the scaling relations between  $\dot{M}_s$  and both  $F_C$  and  $L_b$  such that we can have a relation between  $\dot{M}_s$  and  $L_b$  as implied by a  $\dot{M}_s \propto M_{bh}$  relation, and an additional dependence on  $L_b$ . Such a dependence could be driven on time-scales comparable to those required for significant change in  $\dot{M}_{bh}$ , of order tens of Myr. These processes could include how efficiently gas is channeled into the  $\lesssim$  kpc regions of the host, thus regulating both  $\dot{M}_s$  and  $\dot{M}_{bh}$ .

Two related points are worth noting. First, some authors have argued that C IV is a worse tracer of  $M_{bh}$  at high luminosities than Mg II or H $\beta$  (Baskin & Laor 2005; Netzer et al. 2007). Possible sources of contamination could include the C IV emission arising from greater distances than the other lines, and/or significant non-virial motions. However, the overall scaling between  $F_C$  and  $M_{bh}$  has been argued to be reliable (Assef et al. 2011). Moreover, excluding the objects with highly asymmetric C IV lines does not appreciably change the relation (Fig. 17). We conclude that the C IV lines, at least for a study like ours which averages over tens of objects, is a reasonable way to obtain black hole masses. Secondly, there is controversy over the relation between accretion rate and black hole mass; Netzer et al. (2007) find no correlation of  $L/L_e$  (in which  $L_e$  is the Eddington luminosity) with  $M_{bh}$ , while Bonfield et al. (2011) do, albeit with a large scatter.

## 6.4 AGN colour

The  $\Delta[g - i]$  variable is a crude measure (i.e. using broad filters, and without accounting for the contribution from lines) of the UV continuum slope over  $2 < z < 3$ , spanning (1500 Å–1200 Å)/(2500 Å–1900 Å). There is evidence that the UV continua of quasars become bluer with increasing bolometric luminosity (Sakata et al. 2011; Kokubo et al. 2014; Xie et al. 2015, but also Krawczyk et al. 2013), so the positive correlation of  $\Delta[g - i]$  with star formation rate in Fig. 7 is plausibly a manifestation of the relation with  $M_i$  in Fig. 6. The possible turnover at the most positive  $\Delta[g - i]$  values could be a separate, evolutionary effect, namely low star formation rates in slightly dust-reddened quasars in a post-starburst phase.





**Figure 18.** Star formation rate as a function of  $\lambda_{\text{edd}}$  (equation 17). The red horizontal line is the mean star formation rate derived from the model fit in Fig. 5.

There may also be a rise in  $L_b - L_{\text{IR}}$  with increasing  $\Delta[g - i]$  (the red line in Fig. 7), which could suggest an AGN origin for part of the infrared emission. We do not however regard this as likely, for the reasons given in Section 3.3 and Section 5. Instead, if this rise is real, we interpret it as a larger fraction of the total output arising from star formation.

### 6.5 Eddington ratio

Assuming opacity via Thompson scattering through Hydrogen, the Eddington ratio,  $\lambda_{\text{edd}}$ , of a quasar is given by

$$\lambda_{\text{edd}} = \frac{L_b}{L_e} \simeq \frac{\epsilon \dot{M}_{\text{bh}} c^2 \sigma_T}{4\pi G M_{\text{bh}} m_p} \quad (17)$$

in which  $L_e$  is the Eddington luminosity,  $\sigma_T$  is the Thompson scattering cross-section for the electron, and  $m_p$  is the mass of the proton. Bolometric luminosities are calculated from equation (10). This examination has the caveat that the resulting  $\lambda_{\text{edd}}$  distribution is skewed towards values at  $< 0.2$ , so, to ensure enough objects per bin to obtain reasonable error bars, we place most of the bins at  $\lambda_{\text{edd}} < 0.2$ , with only a few at higher values.

The results are shown in Fig. 18. There is, ostensibly, a trend; low  $\lambda_{\text{edd}}$  values mostly correspond to higher star formation rates than do high  $\lambda_{\text{edd}}$  values. The uneven, sparse binning means however that we cannot be certain of this, as the data are also consistent with a flat relationship with a mean that is approximately the same as the mean star formation rate with redshift in Fig. 5.

A lack of any obvious trend between  $\dot{M}_s$  and  $\lambda_{\text{edd}}$  is straightforward to understand in the context of the  $\dot{M}_s - M_{\text{bh}}$  and  $\dot{M}_s - \dot{M}_{\text{bh}}$  relations. If the underlying driver is the relation between star formation rate and black hole mass, with a weaker or no independent relation with accretion rate, then there would no reason to expect a relation between star formation rate and how *efficiently* the black hole is accreting.

It is however informative to speculate on the opposite case, that the hint of a trend of low  $\lambda_{\text{edd}}$  values corresponding to higher star formation rates is real. There are two straightforward interpretations. First, that this is a manifestation of smaller mass black holes accreting more efficiently. Secondly, that the peak star formation rate occurs some time before or after the peak in the AGN luminosity.

### 6.6 AGN winds

We find an approximately constant  $\dot{M}_s$  as a function of  $A_C$  (Fig. 10 and equation 9). This relation is consistent with the idea that line asymmetries arise due to the relative orientation of the quasar (Richards et al. 2002); assuming that the infrared emission from star formation is optically thin, then variations in line asymmetry would be accompanied by no net variation in star formation rate.

There are two deviations from the model in equation (9). First is a dip in  $\dot{M}_s$  at  $A_C \simeq 0.85$ . Second is an enhancement in  $\dot{M}_s$  at  $A_C \simeq 0.5$ . Both features are barely significant, however, we explore their implications further. The idea that line asymmetries arise due to the relative orientation of the quasar does not explain either deviation. Instead, we speculate that these features are evidence for the black hole affecting star formation in the host. In this context the asymmetric C IV emission signposts outflowing gas. The rise at very blue asymmetric values is consistent with the idea that such outflows can *trigger* starbursts in gas-rich systems (e.g. Zubovas et al. 2013). Conversely, the dip at moderately blue asymmetries is consistent with the idea that AGN outflows can quench star formation (e.g. Fabian. 2012). The weakness of both effects could be due to the AGN duty cycle being much longer than the time-scale for feedback, leading to only a faint signal in a statistical study such as ours. Neither explanation is however wholly satisfactory. Quenching in particular is more commonly associated with BAL winds (e.g. Farrah et al. 2012), and there is no motivation for why we should only see quenching over a certain range in C IV asymmetry.

### 6.7 The Baldwin effect

We observe a declining  $\dot{M}_s - E_C$  relation in Fig. 9, and a rising  $\dot{M}_s - M_i$  relation in Fig. 6. At face value, this is consistent with the Baldwin effect. This effect (e.g. Baldwin 1977; Wilkes et al. 1999; Green, Forster & Kuraszkiewicz 2001; Xu et al. 2008; Wu et al. 2009) – a rise in  $L_{2500}$  accompanied by a decline in C IV EW – has a proposed origin in a non-linear relation between 2500 Å luminosity and optical to X-ray spectral slope ( $\alpha_{\text{ox}}$ ). In it, a rise in the number of optical photons is met with a relative decrease in the number of X-ray photons that can *produce* C IV, meaning that  $M_i$  rises as  $E_C$  declines. Models for the Baldwin effect include a quasar SED that is softer at higher luminosities (Netzer, Laor & Gondhalekar 1992; Dietrich et al. 2002, see also Section 6.4), and that ultraviolet luminosity is less isotropic than X-ray luminosity (e.g. Wilkes et al. 1999). There is no evidence that the Baldwin effect evolves with redshift at  $z \geq 2$  (Osmer, Porter & Green 1994; Dietrich et al. 2002; Xu et al. 2008; Bian et al. 2012) and controversy over the relation with (C IV derived) black hole mass (Xu et al. 2008; Bian et al. 2012). However, C IV EW anticorrelates with  $\lambda_{\text{edd}}$  (Boroson, Persson & Oke 1985; Bachev et al. 2004; Warner, Hamann & Dietrich 2004; Baskin & Laor 2004), including with Eddington ratios derived from Mg II (Bian et al. 2012).

We propose however that the Baldwin effect alone cannot explain the relation in Fig. 9. The dynamic range in  $\dot{M}_s$  in Fig. 9 is greater than the dynamic range in  $\dot{M}_s$  in Fig. 15. Moreover, taking the mean  $M_i$  for each bin in Fig. 9 and then using equation (2) to derive the *expected* star formation rates for the EW-binned data yields the red line in Fig. 9, a significantly flatter relation. It is likely therefore that additional factors contribute to what we see.

There are four possible candidates for these additional factors. First is that  $M_i$  is not a linear tracer of  $L_{2500}$ . Second is that the Baldwin effect changes form at high  $L_b$ . Third is that high  $E_C$  values signpost a change in the scaling relation between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$  (see

also Section 6.3). Fourth is that this is evidence for quenching of star formation by the AGN; if the EW of C IV is a proxy for the radiant intensity available to drive winds into the host then large C IV EWs would signpost the *population* of quasars in which the AGN could exert maximal influence on star formation.

The first, second, and third candidates seem plausible, but we lack the data to confirm or refute them. The fourth possibility is also, at face value, plausible, since we find lower star formation rates for the highest  $E_C$  values compared to the lowest  $M_i$  values. We do not however regard it as a likely contributor. Assuming a two component disc+wind model, then a high X-ray luminosity will suppress a line-driven wind by over-ionizing the gas in the BELR. Furthermore, strongly blueshifted C IV is associated with weaker X-ray spectra, and quasars with high  $E_C$  and highly blueshifted C IV are depopulated in SDSS DR9 (Richards et al. 2011). The only way (within the above framework) that quenching could contribute is if the wind is disc-launched, and having the continuum filtered through a more ionized continuum makes a more powerful outflow more likely.

## 7 CONCLUSIONS

We have stacked *Herschel* SPIRE data on the positions of 1002 optically selected type 1 quasars with  $-28.6 < M_i < -23.8$  spanning  $2.15 < z < 3.5$ . We used the resulting flux densities at 250, 350 and 500  $\mu\text{m}$  to infer star formation rates as a function of redshift, black hole accretion rate, black hole mass, Eddington ratio, optical colour, and C IV line asymmetry. Our conclusions are:

(1) Star formation rates in quasar hosts remain approximately constant with redshift across  $2.15 < z < 3.5$ , at  $300 \pm 100 M_\odot \text{ yr}^{-1}$ . This is consistent with the processes that trigger quasars evolving in a similar way to the processes that trigger star formation. There is a rise in mean star formation rate from  $z = 2.5$  to  $z = 2.1$ , which could be connected to evolution in the mass of the quasar hosts, but could also be due to selection effects in the DR9 catalogue.

(2) Higher rates of star formation are seen in more UV-luminous quasars, consistent with higher star formation rates correlating with higher accretion rates. We obtain the following relation between star formation rate and bolometric accretion luminosity

$$\dot{M}_s = (11 \pm 135) + (504 \pm 114) \exp \left[ \frac{(2.4 \pm 1.5) \times 10^{12}}{L_b} \right]^{-1}$$

This is consistent with a ‘maximal’ *typical* star formation rate of  $\sim 600 M_\odot \text{ yr}^{-1}$ , in quasar hosts, perhaps due to saturation of the starburst by supernova winds. At lower star formation rates the relation between  $\dot{M}_s$  and black hole accretion rate is consistent with a power law with index  $0.4 \lesssim \alpha \lesssim 1.1$ ; a linear fit gives

$$\frac{\dot{M}_{\text{bh}}}{\dot{M}_s} = \frac{1.91 \pm 0.27}{\eta} \times 10^{-3}$$

The existence of such a correlation in our study, when some previous studies have found no correlation, can be explained via a combination of two factors. First, that an  $\dot{M}_s - \dot{M}_{\text{bh}}$  becomes stronger with increasing redshift, especially around  $z = 2$ , corresponding to an epoch with a higher free gas fraction. Secondly, that short-term ( $\lesssim 100 \text{ Myr}$ ) AGN variability introduces scatter in the  $\dot{M}_s - L_b$  relation derived from measurements of objects individually, but which is averaged out in our stacking analyses. It is also plausible that very high or very low star formation rates and black hole accretion rates may not correlate with each other. This implies that a correlation between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$  exists in certain parts of the  $z - \dot{M}_s - \dot{M}_{\text{bh}}$

parameter space, dependent on the availability of free baryons, the trigger for activity, and the potential positive and negative effects of AGN on star formation.

(3) Higher rates of star formation are seen in quasars with more massive black holes. Assuming a relation of the form  $\dot{M}_s \propto M_{\text{bh}}^\alpha$  and allowing slope and intercept to vary then an index of  $0.2 \lesssim \alpha \lesssim 1.1$  fits the data. Further assuming that  $M_{\text{bh}} \propto FWHM_{\text{CIV}}^2 L_{\text{UV}}^{0.5}$ , and with the dependences on  $z - \dot{M}_s - \dot{M}_{\text{bh}}$  parameter space noted above, then our results are consistent with star formation rates in quasars scaling with black hole mass. An additional, separate scaling with accretion rate is possible, but our results do not require it. A plausible physical origin is that star formation rates and black hole mass are both driven by the available gas reservoir.

(4) We see no clear relationship between star formation rate and Eddington ratio. There is a possibility that higher star formation rates are seen in systems with lower Eddington ratios, but the data are consistent with a flat relation. A flat relation is straightforward to understand if the underlying driver is the relation between star formation rate and black hole mass, since there would no reason to expect a relation between star formation rate and how *efficiently* the black hole is accreting. If however low  $\lambda_{\text{edd}}$  values do correspond to higher star formation rates, then this may be due to smaller mass black holes accreting more efficiently, and/or that the peak star formation rate occurs some time before the peak in the AGN luminosity.

(5) We see no clear relation between star formation rate and the asymmetry of the C IV line. This relation is consistent with the idea that line asymmetries arise due to the relative orientation of the quasar; assuming that the infrared emission from star formation is optically thin then variations in line asymmetry would be accompanied by no net variation in star formation rate. There are two deviations from this flat relation, one consistent with AGN winds quenching star formation and one consistent with triggering, but both deviations are barely significant.

(6) There is a decline in star formation rate with rising C IV EW. The rise in star formation rate with rest-frame UV-luminosity suggests that part of this decline is a symptom of the Baldwin effect, but the dynamic range in star formation rate with C IV EW is wider than the dynamic range in star formation rate with  $M_i$ . The most plausible explanation for this additional dynamic range is a contribution from three factors. First is that  $M_i$  is not a linear tracer of  $L_{2500}$ . Second is that the Baldwin effect changes form at high  $L_b$ . Third is that high C IV EW values signpost a change in the scaling relation between  $\dot{M}_s$  and  $\dot{M}_{\text{bh}}$ .

## ACKNOWLEDGEMENTS

We thank the referee for a very helpful report. *Herschel* is an ESA space observatory with instruments provided by European-led Principal Investigator consortia and with participation from NASA. The *Herschel* spacecraft was designed, built, tested, and launched under a contract to ESA managed by the *Herschel/Planck* Project team by an industrial consortium under the overall responsibility of the prime contractor Thales Alenia Space (Cannes), and including Astrium (Friedrichshafen) responsible for the payload module and for system testing, Thales Alenia Space (Turin) responsible for the service module, and Astrium (Toulouse) responsible for the telescope, with in excess of a hundred subcontractors. SPIRE has been developed by a consortium of institutes led by Cardiff Univ. (UK) and including: Univ. Lethbridge (Canada); NAOC (China); CEA, LAM (France); IFSI, Univ. Padua (Italy); IAC (Spain); Stockholm Observatory (Sweden); Imperial College London, RAL, UCL-MSSL,

UKATC, Univ. Sussex (UK); and Caltech, JPL, NHSC, Univ. Colorado (USA). This development has been supported by national funding agencies: CSA (Canada); NAOC (China); CEA, CNES, CNRS (France); ASI (Italy); MCINN (Spain); SNSB (Sweden); STFC, UKSA (UK); and NASA (USA). Funding for SDSS-III has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Science Foundation, and the U.S. Department of Energy Office of Science. SDSS-III is managed by the Astrophysical Research Consortium for the Participating Institutions of the SDSS-III Collaboration including the University of Arizona, the Brazilian Participation Group, Brookhaven National Laboratory, Carnegie Mellon University, University of Florida, the French Participation Group, the German Participation Group, Harvard University, the Instituto de Astrofísica de Canarias, the Michigan State/Notre Dame/JINA Participation Group, Johns Hopkins University, Lawrence Berkeley National Laboratory, Max Planck Institute for Astrophysics, Max Planck Institute for Extraterrestrial Physics, New Mexico State University, New York University, Ohio State University, Pennsylvania State University, University of Portsmouth, Princeton University, the Spanish Participation Group, University of Tokyo, University of Utah, Vanderbilt University, University of Virginia, University of Washington, and Yale University. AF acknowledges support from the ERC via an Advanced Grant 321323-NEOGAL.

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Additional Supporting Information may be found in the online version of this article:

**Table2.ImagFluxes.online.dat**

**Table3.colorFluxes.online.dat**

**Table4.FWHMCIVFluxes.online.dat**

**Table5.EWCIVFluxes.online.dat**

**Table6.CIVAsymFluxes.online.dat**

**Table7.MBHFfluxes.online.dat**

**Table8.LambdaEddFluxes.online.dat**

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