

# **STATISTICAL INFERENCE IN ELLIPTICALLY CONTOURED AND RELATED DISTRIBUTIONS**

edited by  
**Kai-Tai Fang & T.W. Anderson**

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## STATISTICAL INFERENCE IN ELLIPTICALLY CONTOURED AND RELATED DISTRIBUTIONS

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