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Statistical mechanics and molecular dynamics in evaluating thermodynamic properties of biomolecular recognition

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Abstract

Molecular recognition plays a central role in biochemical processes. Although well studied, understanding the mechanisms of recognition is inherently difficult due to the range of potential interactions, the molecular rearrangement associated with binding, and the time and length scales involved. Computational methods have the potential for not only complementing experiments that have been performed, but also in guiding future ones through their predictive abilities. In this review, we discuss how molecular dynamics (MD) simulations may be used in advancing our understanding of the thermodynamics that drive biomolecular recognition. We begin with a brief review of the statistical mechanics that form a basis for these methods. This is followed by a description of some of the most commonly used methods: thermodynamic pathways employing alchemical transformations and potential of mean force calculations, along with end-point calculations. Finally, a few of the fundamental findings that have resulted from these methods are discussed, such as the role of configurational entropy and solvent in intermolecular interactions, along with selected results of the model system T4 lysozyme to illustrate potential and current limitations of these methods.

1. Introduction

A key component of the physical basis for many cellular functions, such as molecular trafficking, signal transduction, and genetic expression, is the non-covalent interaction of biomolecules with themselves and one another, a process referred to as *biomolecular recognition* (Gellman, 1997; McCammon, 1998). Understanding biomolecular recognition is therefore of prime importance not only for advancing our knowledge of chemistry and biology, but also in the development of therapeutics for the treatment of disease. Although based on the laws of physics, this is inherently complicated due to the range of potential interactions (hydrophobic, electrostatic, etc.), the complex interaction networks between groups of atoms in both the biomolecules and their surrounding solvent, and the multiple timescales upon which events occur. It is therefore not surprising that a wealth of experimental and computational tools have been developed to probe these processes, each of which possesses its own strengths and weaknesses.

There are several experimental techniques that have proved invaluable in the study of biomolecular recognition. For example, X-ray crystallography and NMR methods provide

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atomicresolution, three-dimensional structures of biomolecules. These methods describe not only the intra- and intermolecular orientation of molecules in a complex but also order parameters (the B-factor in crystallography and S^2 in NMR) may give details about the degree of local motions in the observed state (Petsko & Ringe, 1984; Stone, 2001; Zidek et al. 1999). Isothermal titration calorimetry (ITC) can be used to accurately measure not only the free energy change associated with biomolecular recognition, but also to decompose it into enthalpic and entropic contributions (Ladbury & Chowdhry, 1996; Olsson et al. 2008). Still, it is difficult to get a complete picture of intermolecular interactions from experiments alone, hence computational work may be helpful in not only interpreting observed results but also in guiding future experiments. Molecular dynamics (MD) simulations, in which each atom of a system is allowed to evolve over time under the forces acting on it by the rest of the system, have become an important tool in the study of biomolecules, as they offer atomic-resolution models for the system of interest (Adcock & McCammon, 2006; Gilson & Zhou, 2007; Guvench & MacKerell, 2009; Levy & Gallicchio, 1998). Current methods and computing power allow for the simulation of systems under a million atoms (large enough for a majority of proteins of interest) for hundreds of nanoseconds, boundaries that are constantly being pushed back by continued developments in computer architecture and design (Shaw et al. 2008; Stone et al. 2007).

In this review, we provide an introduction to the use of MD simulations in the calculations of thermodynamic properties important to biomolecular recognition. To lay the theoretical framework for methods used in the field, we begin with a brief overview of the statistical mechanics that underlie the methods, specifically discussing the origins of the microcanonical and canonical ensembles, and their relation to free energy and the equilibrium binding constant. We recognize that some may find this section overly technical, therefore we have structured the remainder of this review such that this section may be skimmed on an initial reading without a significant loss. Then we discuss a few of the major methods used for the computation of free energy differences, such as alchemical transformation, potential of mean force, and end point calculations, followed by a description of methods for the determination of conformational entropies. We conclude with a discussion of a few interesting results that highlight the utility of these tools, first in the general areas of the role conformational entropy and solvent play in biomolecular recognition, then to the specific case of T4 lysozyme which has become a model system for the study of protein-ligand interactions. We do not discuss the important details of the MD 'force-field', although the interested reader may find these in one of several reviews (Best et al. 2008; Mackerell, 2004).

2. Theoretical basis of entropy and free energy calculations

2.1 A brief review of statistical mechanics

If one is interested in the thermodynamic properties of a system containing *N* particles, then in theory these may be determined by solving the 3*N*Newtonian equations of motion for infinite sampling time. In practice, this is both impossible and unnecessary. It is impossible in that, until the development of MD simulations, only the deterministic equations for systems composed of a handful of particles could be solved, and even with modern computing resources simulations are limited both in size and length. However, instead of considering the deterministic motions of its particles, a wealth of information may be obtained about a particular system by concentrating on its probabilistic configurations. This is the field of *statistical mechanics*, which treats systems at equilibrium by probability functions, and with some elementary assumptions, connects the microstates of a system to macroscopic thermodynamic quantities (such as temperature, chemical potential and free energy). The increasing popularity of MD, which solves the Newtonian equations of motion for each atom in a system, makes recognizing the connection between statistical mechanics

Wereszczynski and McCammon

with thermodynamics particularly relevant for understanding how we deal with the thermodynamics of molecular recognition. Therefore, we start this section with a brief review of the microcanonical and canonical ensembles from statistical mechanics. For brevity, this review is not meant to be complete, and the reader is referred to one of many outstanding textbooks or reviews on the subject (Chandler, 1987; Kirkwood, 1935; Toda *et al.* 1992; Zhou & Gilson, 2009).

2.1.1 The microcanonical ensemble—We begin to examine the microscopic realm by considering a system of classical particles that is isolated from the outside world such that the macroscopic properties N(number of particles), V(the volume), and E(the total energy of the system) remain constant (as is illustrated in Fig. 1). Such a system is referred to as the *microcanonical ensemble* or the NVE ensemble (for constant Number, Volume, and Energy). This system can be in one of Ω accessible microstates. If one assumes that transitions to and from each microstate are permissible (the *ergodic hypothesis*), then the *principle of equal probability* states that each is equally likely with probability:

$$p_{i}=1/\Omega_{-}(1)$$

Boltzmann derived that the entropy of a system, S, is related to a weighted sum of the logarithms of each accessible state, that is

$$S = -k \sum_{\text{states}} p_i \log p_i, \quad (2)$$

where k is the Boltzmann constant. Substituting Eq. (1) into Eq. (2) we arrive at the famous definition for entropy:

 $S = k \log \Omega$ (3)

This fundamental equation states that the entropy of a system (a macroscopic quantity) is directly related to the number of accessible microscopic states.

While there are several interesting results that may be derived from this model, the one most relevant to our discussion concerns the interactions of two microcanonical ensembles. If two microcanonical systems are interacting such that they are allowed to exchange energy but not particles or other macroscopic quantities with one another, then the total energy of the system may be defined as $E_{I}+E_{II} = E_{Total}$. The total number of states for both systems is represented by the product of the number of states for the smaller systems (each of which is a function of their energy), that is

$$\mathbf{\Omega}_{\text{Total}} = \mathbf{\Omega}_{\text{I}}(E_{\text{I}})\mathbf{\Omega}_{\text{II}}(E_{\text{II}}) = \mathbf{\Omega}_{\text{I}}(E_{\text{I}})\mathbf{\Omega}_{\text{II}}(E_{\text{Total}} - E_{\text{I}}). \quad (4)$$

The most probable energy distribution between the two systems corresponds to the value of $E_{\rm I}$ that maximizes the value of $\Omega_{\rm Total}$, which also corresponds to the maximum entropy of the combined system (in accord with the second law of thermodynamics). As it is at a maximum, we may set the first derivative of the combined system entropy to zero, yielding:

$$\frac{\mathrm{d}\ln\mathbf{\Omega}_{\mathrm{Total}}(E_{\mathrm{I}})}{\mathrm{d}E_{\mathrm{I}}} = \frac{\mathrm{d}\ln\mathbf{\Omega}_{\mathrm{I}}(E_{\mathrm{I}})}{\mathrm{d}E_{\mathrm{I}}} - \frac{\mathrm{d}\ln\mathbf{\Omega}_{\mathrm{II}}(E_{\mathrm{Total}} - E_{\mathrm{I}})}{\mathrm{d}(E_{\mathrm{Total}} - E_{\mathrm{I}})} = 0, \quad (5)$$

which, with some reorganizations, results in

Wereszczynski and McCammon

$$\frac{\mathrm{d}\ln\mathbf{\Omega}_{\mathrm{I}}(E_{\mathrm{I}})}{\mathrm{d}E_{\mathrm{I}}} - \frac{\mathrm{d}\ln\mathbf{\Omega}_{\mathrm{II}}(E_{\mathrm{Total}} - E_{\mathrm{I}})}{\mathrm{d}(E_{\mathrm{Total}} - E_{\mathrm{I}})} = 0. \quad (6)$$

Since Ω_{I} and Ω_{II} may be unique from one another, their first derivatives are equal if and only if they are constant, which we have defined as the value of β . It can be shown that β has the property that it is inversely related to the absolute temperature *T*, that is $\beta = 1/kT$. Systems I and II are said to be in *thermal equilibrium* when only small energy transfers between the two systems are observed as system I fluctuates around an equilibrium energy value of E_{I}^{*} and system II around energy $E_{Total} - E_{I}^{*}$.

2.1.2 The canonical ensemble—In the microcanonical ensemble, a system completely isolated from the outside world with a constant number of particles N, constant volume V and constant energy E is considered. However, for our purposes, a more pertinent system is one that still has a constant N and V, but that is in thermal equilibrium with its environment and thus has a non-constant E but a constant temperature T (see Fig. 1*b*). This is the *canonical*, or NVT (constant Number, Volume, and Temperature), ensemble. This may be thought of as a special case of the two interacting microcanonical systems in which one system (system II) is much larger than its counterpart (system I), and is often referred to as a *heat bath* or *heat reservoir*. The total energy and number of states for each system and the combined systems are defined as $E_{\rm I}$ and $\Omega_{\rm I}$, for $i = {\rm I}$, II, Total. If we take Eq. (4), and set the total number of states to a constant, $\Omega_{\rm Total}=1/C$, rearrangement of terms yields:

$$\frac{1}{\mathbf{\Omega}_{\mathrm{T}}(E_{\mathrm{T}})} = C\mathbf{\Omega}_{\mathrm{TI}}(E_{\mathrm{Total}} - E_{\mathrm{T}}).$$
 (7)

Using the principle of equal probability Eq. (1), we note that the probability of observing system I in a state with energy $E_{\rm I}$ is entirely dependent on the number of states in the heat bath (system II) at energy $E_{\rm Total}-E_{\rm I}$. That is

$$\rho_{\rm I}(E_{\rm I}) = C \mathbf{\Omega}_{\rm II}(E_{\rm Total} - E_{\rm I}). \quad (8)$$

The assumption that system II is much larger than system I implies that $E_{\text{Total}} \approx (E_{\text{Total}} - E_{\text{I}})$, thus we may take the logarithm of each side and perform a Taylor expansion about the point E_{Total} to the term containing Ω_{II} to obtain:

$$\ln(\rho_{\rm I}(E_{\rm I})) = C' \frac{\mathrm{d} \ln \mathbf{\Omega}_{\rm II}(E)}{\mathrm{d}E} E_{\rm I}.$$
 (9)

Borrowing from Eq. (6) and exponentiating each side of Eq. (9) we find that, when normalized over all possible states j, the probability for system I to exist in a microstate n with energy E_n is

$$\rho_{I}(E_{n}) = \frac{\exp(-\beta E_{n})}{\sum_{j} \exp(-\beta E_{j})} = \frac{\exp(-\beta E_{n})}{Z}.$$
 (10)

Equation (10) is one of the fundamental equations in statistical mechanics. It states that, unlike in the microcanonical ensemble where the system is evenly distributed among microstates with a specific energy, in the canonical ensemble interactions with a heat bath cause the energy of the system to fluctuate, with representative points in phase space distributed by the factor $\exp(-\beta E)$, the *Boltzmann factor*. In addition, although the system and the heat bath are coupled, the assumption that the heat bath (system II) is much larger

than system I means that the thermodynamic properties of system I may be solved for with knowledge of only the term β (the inverse temperature, $\beta = 1/kT$, where *k* is the Boltzmann constant) from system II. To compute thermodynamic averages of a physical quantity *A*, a weighted average of *A* is computed based on the Boltzmann factor.

The denominator of Eq. (10), which has been introduced to normalize the probability of states and is denoted as Z, is referred to as the *partition function* of the ensemble. The partition function is a particularly important concept. All thermodynamic quantities may be expressed in terms of it, which therefore implies that knowledge of the partition function is sufficient for understanding the macroscopic properties of a system. For example, by substituting Eq. (10) into Eq. (2), we recover the definition of entropy in the canonical ensemble, which depends solely on the average enthalpic energy U and Z:

$$S = k\beta U + k \ln Z \quad (11)$$

From thermodynamics, we know that the maximum amount of work a system can do, the Helmholtz-free energy, is defined as a difference of enthalpic (the internal energy, U) and entropic (*TS*) terms F = U - TS. By substituting Eq. (11) into this relation, we obtain

 $F = U - TS = -kT \ln Z. \quad (12)$

Therefore, we see that computing the partition function is the fundamental challenge in computing thermodynamic properties for equilibrium processes, including molecular recognition. For classical systems, it is convenient to describe the accessible energies as a function of the system's momentum and position vectors (6N coordinates), and if we assume these are continuous variables (as opposed to quantum ones), then the partition function may be rewritten as

$$Z = \sum_{j} \exp(-\beta E_{j}) \propto \iint \exp[-\beta H(x, p)] dx dp, \quad (13)$$

where H(x, p), the Hamiltonian, is the total energy composed of a sum of the kinetic and potential energies (determined by the momentum and position values). The canonical ensemble assumes a constant number of particles, volume and temperature; however, it is often desirable to consider a system in which the volume is allowed to fluctuate to maintain a constant pressure. This is referred to as the isothermal–isobaric, or NPT (constant Number, Pressure, and Temperature), ensemble. Derivation of this ensemble is similar to the canonical ensemble, with the major difference being the weight of a microstate becomes $\exp[-\beta(E+PV)]$, with a corresponding modification to the partition function. The appropriate free energy becomes the Gibbs free energy (*G*), which is similar to the Helmholtz free energy except for a modification to the enthalpic term to account for the system volume. That is

$$G=U+PV-TS=-kT\ln Z.$$
 (14)

As a more general case, the system of interest may be allowed to exchange particles with its environment in the *Grand Canonical Ensemble*, where the chemical potential is considered a constant instead of the number of particles in the system. In general, the canonical ensemble provides a sufficient description for our purposes, making the grand canonical ensemble beyond the scope of this review. For details on either of these cases, the interested reader is referred to a statistical physics textbook, such as Toda *et al.* (1992)

2.1.3 Equilibrium binding constant—Let us consider the case of a ligand *L* and a receptor *R* in chemical equilibrium, such that the [*L*], [*R*] and [*LR*] are the concentrations of the free ligand, free receptor, and bound ligand–receptor complex, which are invariant over time. Then, the equilibrium constant K_b for the reaction $[L]+[R] \rightleftharpoons [LR]$ is defined as

$$K_{\rm b} = \frac{[LR]}{[L][R]}.$$
 (15)

If we take the view of a single receptor molecule, the probabilities for observing this receptor bound to and free from a ligand, P_{bound} and P_{free} , respectively, are proportional to the solution concentrations [*LR*] and [*R*], such that Eq. (15) becomes

$$K_{\rm b} = \frac{1}{[L]} \frac{P_{\rm bound}}{P_{\rm free}}.$$
 (16)

To determine the ratio of any ligand bound to the unbound receptor, $P_{\text{bound}}/P_{\text{free}}$, let us focus on the probability of the receptor being bound to (state 1) or free from a particular ligand (state 0), P_1/P_0 . The probability of each of these states may be expressed in terms of the system's partition function over the space in which ligand L is bound or in bulk. That is

$$P_{\text{bound}} \propto \int_{\text{bound}} \exp[-\beta H(x, p)] dx, \quad (17)$$

where we have omitted the integration over momentum space from Eq. (13) for simplicity. If we assume that the bulk solution is homogeneous, then a point x^* , which is sufficiently far from the receptor to prevent ligand–protein interaction, may be arbitrarily chosen such that

$$\frac{P_1}{P_0} = \frac{\int_{\text{bound}} \exp[-\beta H] dx}{V_{\text{bulk}} \int_{\text{bulk}} \delta(x_l - x^*) \exp[-\beta H] dx}, \quad (18)$$

where V_{bulk} is the volume of the bulk solution and x_{l} is the ligand's position. Since the ligands are identical, the probability for any one of the *N* ligands in solution to be bound to the receptor is simply NP_{l}/P_{0} , which is equivalent to the ratio $P_{\text{bound}}/P_{\text{free}}$. Therefore, Eq. (16) becomes

$$K_{b} = \frac{1}{[L]} \frac{N \int_{\text{bound}} \exp[-\beta H] dx}{V_{\text{bulk}} \int_{\text{bulk}} \delta(x_{l} - x^{*}) \exp[-\beta H] dx} = \frac{Z_{\text{bound}}}{Z_{\text{free}}}.$$
 (19)

where Z_{bound} is the partition function over states with the ligand in the binding pocket, and Z_{free} for states when the ligand is a distance x^* away. If one takes the natural log of Eq. (19) and multiplies by -kT, then by using Eq. (12), we recover the familiar expression:

$$-kT\ln(K_b) = -kT(\ln Z_{\text{bound}}) + kT\ln Z_{\text{free}} = F_{\text{bound}} - F_{\text{free}}.$$
 (20)

That is, the natural log of the equilibrium binding constant is the difference in free energy between a ligand in a free state (typically referred to as infinitely far away) and one in a bound state. As a matter of convenience, F_{free} is typically defined as 0. This derivation relies solely on the canonical ensemble (Deng & Roux, 2006). An alternative derivation based on

the chemical potentials of the species *L*, *R* and *LR* may be derived from the grand canonical ensemble with similar results (Gilson *et al.* 1997a).

3. Methods for calculating free energy and entropy differences

From the previous section, we see that the calculation of free energy and entropy differences is possible by considering each accessible microstate of the system, and its corresponding energy, to determine the partition function for use in Eqns. (11) and (12). To do this requires significant computation, which is impractical for even small systems. However, we are generally concerned with a free energy difference (as in Eq. (20)), and not the absolute free energy of a system. Several methods have been developed to sample the regions of phase space most important to the recognition process, thereby providing approximations to free energy and entropy changes of a system, which have a trade-off between speed and accuracy (see Fig. 2). For example, docking methods may estimate the free energy gained when a ligand binds to the binding site of a protein without any previous knowledge of the bound state in a matter of minutes, but the error in the free energies tends to be quite high. In contrast, free energies estimated via alchemical transformations tend to correlate much better to experimental values, yet they not only require knowledge of the bound state but may also require hundreds or thousands of computer hours. Here, we discuss two major techniques used in the field for calculating free energy differences: thermodynamic pathways and end point calculations, followed by a discussion of methods that exist for the calculation of the conformational entropy component of a system. For further details on docking, the reader is referred to one of the many reviews on the subject (Brooijmans & Kuntz, 2003; Durrant & McCammon, 2010; Fuentes et al. 2011; Halperin et al. 2002; Kitchen et al. 2004; Klebe, 2006).

3.1 Thermodynamic pathways

In Section 2.1, we derived Eq. (12), which states that the absolute free energy of a system is related to the partition function Z. To compute the free energy change of a biomolecular process, such as binding of a ligand to a protein, one could compute the partition functions of the system before and after the molecular association (Z_0 and Z_1), and subtract the logarithms of the two. However, this requires extensive sampling of phase space for both states, a task that is difficult for small systems and nearly impossible for protein-sized ones. If we take advantage of the fact that (in general) we are interested in the *change* in free energy of a system, ΔF , we may instead focus on this by computing:

$$\Delta F_{0->1} = -kT\ln\frac{Z_1}{Z_0}.$$
 (21)

If we assume a classical system, as is described in Eq. (13), then the microstates that are identical between the two macrostates cancel each other out, and our problem simplifies to calculating the portions of phase space which differ from one another in states 0 and 1. Several methods have been developed to solve Eq. (21), which rely on enhancing sampling along one or a few dimensions known as the 'reaction coordinate(s)' (that we denote as ξ), which may be largely divided into two categories. In the first, ξ is constrained such that it has only a single value over the simulation, and the free energy between states is calculated by either a direct calculation of Eq. (21) or by integration of the derivative of $dF/d\xi$. In the second class of methods, ξ is biased with a restraint that enhances sampling of phase space for regions which have a low probability functions $P^*(\xi)$ along with the form of the bias, one may recover free energy profiles along ξ , and thus the free energy difference between states 0 and 1.

Keeping with the example of a ligand binding to the binding site of a protein, Fig. 3 shows two potential pathways for calculating the free energy of binding. In the direct method, ΔG bind may be obtained directly by computing the free energy along a physical pathway that takes the ligand from a distance far away from the binding pocket into it. For systems in which the ligand binds to a solvent exposed site on the protein, this may be an appropriate method as it is direct and (relatively) straightforward. However, for many systems, such as T4 lysozyme (see Section 4.3), the binding site is partially or fully hidden from solvent, requiring significant conformational rearrangement of the protein upon binding that may be difficult to sample with physical pathways. As an alternative, one can draw a thermodynamic cycle (as in Fig. 3) that connects the free and bound states through unphysical pathways that relies on transferring the ligand from its original system into a vacuum, which is termed ' annihilation ' or 'decoupling '. This requires two sets of calculation. In the first, ΔG water is computed as the free energy of decoupling the unbound ligand from its interactions with solvent, while in the second, ΔG protein is the free energy of decoupling from the bound protein state. The free energy of moving a decoupled ligand into the binding site of a protein is zero (since it is not interacting with the system, the bottom path in Fig. 3) so the binding free energy may be computed as ΔG bind = ΔG waterx ΔG protein (Chipot & Pohorille, 2007).

3.1.1 Constrained free energy calculations—To solve Eq. (21), let us define the Hamiltonian of system 1 as a sum of the Hamiltonian of system 0 plus a perturbation term $\Delta H = \Delta U$ (where ΔU is a change in potential energy). If we substitute this term into the partition function for state 1, and we utilize Eq. (10) for the probability of observing state 0 to have a specified Hamiltonian, it can be shown that the free energy of going from state 0 to 1 is (Straatsma & McCammon, 1992; Zwanzig, 1954):

$$\Delta F_{0->1} = -kT \ln \langle \exp(-\beta \Delta U) \rangle_0.$$
 (22)

That is, in free energy perturbation (FEP), the free energy difference between states 0 and 1 may be calculated by the natural log of the average Boltzmann factor of the potential energy difference between states 1 and 0 over equilibrium configurations from state 0. The value ΔU may be thought of as the work required to instantaneously transform the system from state 0 to 1. In principle, this is a thermodynamically exact relation, but in practice if the energy ΔU is larger than a few kcal/mol, the exponential term creates computational havoc and produces unreliable results. If there is a large perturbation to the system (such as the decoupling of a ligand from solvent or a protein's binding site), then it is advantageous to divide the free energy into smaller segments, or 'windows', which follow an order parameter λ such that the Hamiltonian for a system with a λ value is defined as

 $H(\lambda) = \lambda H_1 + (1 - \lambda)H_0.$ (23)

Such a transformation between two physical end states through an unphysical pathway is termed an *alchemical free energy calculation*. In practice, one performs a series of simulations with λ values varying between 0 and 1, and through utilization of Eq. (22) the free energy between successive windows is calculated. The total free energy to go from states 0 to 1 is therefore the sum of the free energies between each of the simulated λ -points.

Increasing the number of windows in an alchemical transformation may decrease the variance in the calculated free energies, yet the exponential averaging in FEP may still produce numerical errors. Therefore, alternative methods have been developed to improve the convergence of calculated free energies. In thermodynamic integration (TI) the derivative of H with respect to λ , followed by integration of λ from 0 to 1, is used to compute ΔF (Straatsma & McCammon, 1991, 1992):

$$\Delta F_{0->1} = \int_{0}^{1} \left\langle \frac{\mathrm{d}H(\lambda)}{\mathrm{d}\lambda} \right\rangle_{\lambda} \mathrm{d}\lambda \quad (24)$$

For the case of an alchemical transformation, the $dH(\lambda)/d\lambda$ term reduces to the derivative of the electrostatic potential plus the derivative of the van der Waals potential terms with respect to λ for the part of the system which varies between the two endpoints, both of which have analytic solutions. One caveat of TI is that, since λ has discrete values, it relies on proper integration techniques (Jorge *et al.* 2010). A newer alternative for improving the convergence of alchemical transformations was recently introduced by Shirts *et al.*, in which the free energy between two λ points may be estimated by using the work functions from both windows in the maximum likelihood estimator developed by Bennett (Shirts *et al.* 2003). The Bennett acceptance ratio (BAR) provides the optimal asymptotically unbiased estimate of the free energy difference (Shirts & Pande, 2005). The multistate Bennett acceptance ratio (MBAR) was later developed as a generalization to BAR that incorporates work functions between all windows into the estimator, resulting in further reduced variances of the calculated free energies (Shirts & Chodera, 2008).

Regardless of the free energy estimator used (FEP, TI, BAR, or MBAR), there are several practical challenges in alchemical free energy transformations (Shirts *et al.* 2007). The first is that all of these methods rely on extensive sampling of the equilibrium state of the system in each λ point, which may require several nanoseconds for the decoupling of a ligand bound to a protein. Even with several nanoseconds of simulations, simulations may become trapped in metastable states, resulting in free energy estimates that may not accurately represent the complete ensemble of bound and unbound conformations. This may partially be avoided through multiple free energy calculations (Lawrenz *et al.* 2009) or through the use of enhanced sampling techniques to improve phase space sampling (Fajer *et al.* 2008; Hamelberg *et al.* 2004; Jiang & Roux, 2010; Wereszczynski & McCammon, 2010; Woods *et al.* 2003), both of which are active fields of research. In addition, special problems exist for the states in which the protein–ligand interactions are nearly entirely eliminated, such as excessive sampling of the simulation box by the ligand and numerical instabilities, both of which may be addressed by the introduction of restraining (Hamelberg & McCammon, 2004; Wang *et al.* 2006) and soft-core potentials (Beutler *et al.* 1994; Zacharias *et al.* 1994).

3.1.2 Free energy pathways via biased simulations—As an alternative, the free energy between two states may be derived through the probability of observation of those states. If we have a state, 0, then the probability of observing this state (P_0) is proportional to its partition function, Z_0 . Thus, when determining the free energy difference between states 0 and 1, Eq. (21) may be rewritten as

$$\Delta F = -kT \ln \frac{P_1}{P_0}.$$
 (25)

Determining the probability of observing one state over another is therefore equal to determining the free energy difference. One could perform a simulation and directly determine the free energy difference by counting the number of configuration in states 0 and 1 and use these values as unnormalized probabilities in Eq. (25) (Thomas & Elcock, 2006). However, if these states are separated by energy barriers of even a few kcal/mol, or significant diffusion is required to process from one state to another, then the simulation length required to directly compute ΔF may easily be several orders of magnitude more than what is available by today's computers. To alleviate this practical problem, several methods have been developed which enhance the sampling of phase space through biased simulations and, with proper reweighting, allow for the calculation of an unbiased ΔF .

Perhaps the most widely used of these methods is *umbrella sampling* (Torrie & Valleau, 1977). In umbrella sampling, sampling of phase space is enhanced by biasing the simulation with an additional potential, the *umbrella potential*, along one (or a few) reaction coordinate(s). The choice of the reaction coordinate is critical, as it is assumed that motions along this dimension dominate the free energy of the observed changes in the system. In some cases, the choice of a reaction coordinate is straightforward, for example, when pulling a ligand out of a protein's binding site the center of mass separation distance may suffice, while in other cases more complex reaction coordinates may be required. Still, if we assume that the motions along the reaction coordinate(s) are sufficient for describing the system, then by utilizing several simulations with umbrella potentials that span the interesting regions of the reaction coordinate, sampling of phase space may be dramatically improved relative to unbiased simulations. The weighted histogram analysis method (WHAM) may then be used to combine the probability distributions from the multiple biased simulations into a single unbiased probability profile, which, when used with Eq. (25), produces a free energy profile along the reaction coordinate(s) (Kumar *et al.* 1992; Roux, 1995).

Other biased simulations techniques, such as adaptive biasing force (Darve *et al.* 2008) and metadynamics (Laio & Parrinello, 2002), are also routinely used for calculating free energy profiles related to conformational transitions in biomolecules. In both of these methods, an external bias is adaptively added to the simulation based on the conformational space sampled at a particular time, making unnecessary the use of multiple simulation windows for sampling a wide region of phase space (although they may be employed if desired). While these methods do have practical advantages and can increase the convergence rate for some systems, slow conformational changes may benefit more from traditional umbrella sampling techniques that actively force sampling of phase space instead of relying on diffusion of the biased systems along the reaction coordinate(s).

3.1.3 Emerging free energy methods—While there are several novel methods for the calculation of free energy differences relating to biomolecular recognition processes, for brevity we highlight two of these methods to provide the reader with a flavor of these emerging techniques. One interesting method combines the ideas of alchemical transformations, in which the Hamiltonian is defined by the parameter λ (Eq. (23)) with biased simulation techniques. In λ -dynamics, the λ parameter is a dynamical variable that fluctuates throughout a simulation based on Newtonian mechanics with a fictitious mass and a biasing potential (Knight & Brooks, 2009; Kong & Brooks, 1996). In this way, a ligand can 'appear' and 'disappear' to a protein several times throughout a single simulation, which may have the advantages of enhancing sampling by avoiding conformational traps and negating the necessity of multiple simulation windows. Additionally, a series of ligands may be simulated in a single run (each with their own λ values) which may further improve computational efficiency. Analogously, simulations may be performed in which an unphysical fourth spatial dimension is introduced, along which the free energy of removing the ligand from a protein's binding site may be calculated with methods such as umbrella sampling (Beutler & van Gunsteren, 1994; Rodinger et al. 2005).

As mentioned above, the relative free energy difference between two states may be reliably calculated if the simulation sufficiently samples both endpoints, negating the need for intermediate states. In the one-step perturbation technique, a single unphysical state (the 'reference' state) is simulated which has a partition function that is the sum of the two end states (Oostenbrink & van Gunsteren, 2003, 2005). In theory, this should enhance sampling of the important regions of phase space for both endpoints ; however, in practice, this may be complicated if the Hamiltonians of the two states differ significantly. This method has evolved into envelope-distribution sampling with the introduction of an iterative method for the calculation of an ideal reference state, which has a straightforward extension to the case

of calculating relative free energies between multiple end states (instead of just two) (Christ & van Gunsteren, 2007, 2008). While these simulations may still require significant simulation time for convergence, they show promise in the calculation of multiple free energies from a single run. For example, they may be useful in calculating the free energy change resulting in the modification of a ligand's functional group to multiple possible end states, a key problem in the lead optimization stage of a drug-design project.

3.2 End point calculations

Calculations of free energy differences based on thermodynamic pathways tend to require extensive sampling of conformations not only at the end points of interest but also in between, thus requiring sizeable computational cost. A computationally less expensive approach is to simulate only the two end states of interest (such as a protein free from and bound to a ligand) to estimate their absolute free energies, and to subtract them from one another (Gilson *et al.* 1997a, b; Swanson *et al.* 2004). Keeping with the example of a ligand binding to a receptor, the free energy gained through binding is

 $\Delta G_{\text{bind}} = G_{\text{complex}} - (G_{\text{receptor}} + G_{\text{ligand}}) \quad (26)$

Each of these free energies is then decomposed into four terms:

$$G = \langle E_{\rm MM} \rangle - T \langle S_{\rm MM} \rangle + \langle G_{\rm Solv} \rangle + \langle G_{\rm np} \rangle, \quad (27)$$

where $\langle E_{\rm MM} \rangle$ represents the mean enthalpic energy of the solute, $\langle S_{\rm MM} \rangle$ the mean solute entropy, $\langle G_{\rm Solv} \rangle$ the polar solvation free energy and $\langle G_{\rm np} \rangle$ the non-polar solvation free energy. To calculate these values, trajectories resulting from short simulations (of the order of 1–5 ns) of each state in Eq. (26) are post-processed. The solute enthalpic term ($\langle E_{\rm MM} \rangle$) is taken as an average over the molecular mechanical force-field terms for the solute molecule(s) in the simulation (which are typically composed of bond, angle, torsion and non-bonded terms). The solute entropy ($\langle S_{\rm MM} \rangle$) is typically calculated by either a normal mode or quasi-harmonic analysis (the preferred method), as described in Section 3.3. The polar solvation free energy is generalized-Born (GB) (Still *et al.* 1990) analysis on snapshots from the trajectory, whereas the non-polar solvation free energy is assumed to be directly proportional to the solvent-exposed surface area (Sitkoff *et al.* 1994). This method has become known as MM-PBSA (or MM-GBSA if the generalized-Born solvation energy is used) for the mix of molecular mechanics (MM), PB, and surface area (SA) energy terms (Kollman *et al.* 2000; Srinivasan *et al.* 1998).

MM-PBSA calculations for binding affinities often rely on taking the difference of two large numbers (the absolute free energies before and after binding, typically of the order of hundreds or thousands of kcal/mol) to determine relatively small free energy changes (of the order of tens of kcal/mol) (Barril *et al.* 2001). Therefore, the simulation length is of vital importance, as averages of energy terms should converge to values which are invariant of sampling time and have relatively low variance. Depending on the initial conformation, short simulations may also neglect the effects of molecular strain, a vital component of biomolecular recognition. Also, since the solvent molecules are ignored in analysis, it is often tempting to run simulations without explicit solvent. While this may produce reliable results, for some systems calculations with explicit solvent molecules have been shown to produce results more consistent with experiments (Weis *et al.* 2006). Results also depend on computing conformational entropies (discussed in the following section), which are often times difficult and have their own issues with convergence and accuracy. Finally, there are also several adjustable parameters in the PB and SA calculations which may affect the obtained results. Despite all these caveats, end point calculations may provide surprisingly

good estimates of solvation and binding free energies. For example, some studies have shown the t^2 correlation with experiments can be above 0.8, and in some cases end-point calculations may improve estimates of binding affinity relative to docking (Guimaraes & Cardozo, 2008; Lee & Sun, 2007; Lyne *et al.* 2006; Wang *et al.* 2001; Weis *et al.* 2006). Therefore, end-point calculations should be viewed as fairly reliable estimates of free energy differences that may be obtained at much lower computational cost than thermodynamic pathway calculations.

An alternative end point method, termed 'mining minima,' estimates the partition function through a harmonic approximation to the Hessian matrix (described below in the context of normal mode analysis). The exploration of minima local to the starting configuration, by transformations along low-frequency eigenvectors, allows for the inclusion of multiple relevant states to the partition function estimate with an efficient search algorithm. The method of mining minima appears promising as results for small host–guest systems, and recently for inhibitor binding to HIV-1 protease, show quite good agreement to experimental results (Chang & Gilson, 2004; Chen *et al.* 2004, 2010).

3.3 Methods for the calculation of configurational entropies

Free energy calculations are useful in describing the degree and methods of recognition ; however, it is oftentimes desirable to decompose the association process into separate enthalpic and entropic parts to gain further insight into the energetics driving the processes. Calculations of vibrational entropies allow for not only this, but are a key component of MM-PBSA calculations. While brute force methods that attempt to directly solve Eq. (11) are possible, convergence is quite difficult for even moderately sized systems of biological interest (Carlsson & Åqvist, 2005, 2006). If it is assumed that rotational, translational and vibrational motions are independent from one another (Levy *et al.* 1984), and that the potential energy for each of the 3N-6 vibrational degrees of freedom are harmonic with frequencies ω_i and not correlated with one another, then we may calculate the total entropy as a sum of the entropies for each mode. For example, if each mode is modeled as a quantum mechanical harmonic-oscillator the total entropy is (Andricioaei & Karplus, 2001):

$$S_{\text{ho}} = \sum_{i}^{3N-6} \frac{k\alpha_i}{\exp(\alpha_i) - 1} - \ln(1 - \exp(-\alpha_i)), \quad (28)$$

where $\alpha_i = \hbar \omega / kT$. Therefore, the problem of calculating the total conformational entropy reduces to determining the harmonic frequencies that best describe the internal molecular motions. If the effective potential energy for a system in state *x* (where *x* is a vector of length 3*N*) is defined as:

$$U_{\text{eff}} = \frac{1}{2} x^{\mathrm{T}} F x, \quad (29)$$

then a diagonalization of F yields the harmonic frequencies. In a normal mode analysis, the elements of F are constructed from a single conformation of the solute molecule by taking the Hessian matrix of the system's potential energy:

$$F_{ij} = \left(\frac{\mathrm{d}^2 U}{\mathrm{d}x_i \mathrm{d}x_j}\right). \quad (30)$$

The derivation of normal mode analysis assumes that the system is at a potential energy minimum (so that $dU/dx_i = 0$ and $d^2U/dx_i dx_j > 0$ for each *i* and *j*) (Brooks & Karplus, 1983; Brooks *et al.* 1995; Wilson *et al.* 1955), thus it is imperative that a system be energy

minimized before analysis or else non-physical negative modes will be recovered. Normal mode analysis is relatively inexpensive, as dynamics are not required, but this results in the computed entropy reflecting only the (small) region of phase space surrounding the energy minimum considered (see Fig. 4).

Through the introduction of dynamics, quasi-harmonic analysis attempts to determine an effective potential from the states sampled in a simulation by fitting the observed probability distribution along a degree of freedom to a Gaussian (as would result from a harmonic potential along that coordinate) (Karplus & Kushick, 1981; Levy *et al.* 1984). The key difference from normal mode analysis is that the matrix *F* is constructed from the covariance matrix, which describes the fluctuations in a simulation of each Cartesian coordinate relative to it average:

$$F_{ij} = kT[\sigma]_{ij},$$

$$\sigma_{ij} = \langle (x_i - \langle x_i \rangle) \rangle \langle (x_j - \langle x_j \rangle) \rangle, \qquad (31)$$

where (x_i) is the average value of x_i throughout the simulation. This results in frequencies which represent a larger range of phase space than in normal mode analysis, as shown in Fig. 4.

Since it relies on extensive phase space sampling, convergence of quasi-harmonic calculations is often obtained only with extensive simulations (Baron *et al.* 2006; Harris *et al.* 2001). Even with an infinitely long simulation, the quasi-harmonic approximation will only give an upper-bound to the absolute entropy due to the effects of two key assumptions: the harmonic assumptions and the correlations between probability distributions. It has recently been shown that the effects of anharmonicity are relatively small and only affect the lowest few frequencies (Baron *et al.* 2009; Chang *et al.* 2005). In contrast, the correlations between modes may be quite significant. Corrections for both of these have been proposed, but they too are quite expensive and require significant sampling such that corrections beyond pairwise may be computationally infeasible (Baron *et al.* 2009). Despite these drawbacks, the quasi-harmonic approximation has become a powerful method for the estimation of absolute entropies in biomolecular systems.

4. Interesting results

The methods discussed in the previous section have been extensively utilized throughout the literature in the past three decades. To demonstrate some of their strengths, we present selected results that shed light on the thermodynamic basis of biomolecular recognition. We first address the role configurational entropy plays, and in particular how it relates to the oft discussed 'entropy/enthalpy compensation' phenomena. We leave the discussion of solvent entropies to the second part, where the general role of solvent is described. Finally, we present a brief historical view for simulations performed on the model T4 lysozyme system to show not only the evolution of these methods but also their strengths and weaknesses.

4.1 Configurational entropy in biomolecular recognition

Molecular flexibility, which may be thermodynamically quantified as conformational entropy, plays an important role in the thermodynamics of biomolecular recognition. Oftentimes it is observed that the free energy change upon binding can be decomposed into an enthalpic term which favors binding and entropic terms that oppose it. This phenomenon of entropy–enthalpy compensation has been widely discussed in both the experimental and theoretical literature (Baron & McCammon, 2008; Gallicchio *et al.* 2000; Levy & Gallicchio, 1998; Lumry & Rajender, 1970; Olsson *et al.* 2008; Stone, 2001). The physical basis for this is the intuitive idea that the tighter two molecules bind to one another (higher

enthalpic interaction), the more restricted their motions are, which results in a lower configurational entropy of the complex. However, the origin of these restricted motions is not entirely clear. For a small host–guest system, mining minima results showed that, counter to what one may expect, binding does not significantly reduce the number of states accessible to the bound system relative to the free one, rather it reduces the motions within these states (Chang & Gilson, 2004; Chen *et al.* 2004). In contrast, quasiharmonic calculations on long timescale simulations of the major urinary protein binding to 2-methoxy-3-iosbutylpyrazine showed little change in the protein's or ligand's configurational entropy upon binding (restrictions of motions in one region were offset by increased motion in another), with the only entropic penalty resulting from a loss of rotational degrees of freedom (Roy & Laughton, 2010). Clearly, the nature and degree of entropic penalties are highly complex and system dependent, but their presences play a key role in biomolecular recognition.

The role of conformational entropy opposing complex formation is believed to be common in nature, but it is by no means a requirement of thermodynamics (Gallicchio *et al.* 1998; Zidek *et al.* 1999). In fact, some binding interfaces, such as that between protein kinase A (PKA) and any of the numerous A-kinase-anchoring proteins (AKAPs) it binds to, have evolved such that there is an *increase* in configurational entropy upon binding which aids in stabilizing the complex (Colledge & Scott, 1999; Fayos *et al.* 2003). Simulations of the PKA D/D domains in complex with the binding peptide from one AKAP, Ht31, demonstrated an increase in side-chain flexibility upon binding relative to the free state (Chang *et al.* 2008). It is believed that, when free in solution, the hydrophobic side chains of Ht31 were limited to forming intramolecular contacts, but when bound to PKA the hydrophobic environment of the protein surface creates a fluid-like region that allows for an increase in the number of states accessible to the side chains, and hence an increased entropy. This mechanism may help explain the promiscuous nature of PKA, as its interaction with diverse protein partners may be stabilized through non-specific hydrophobic contacts.

4.2 The role of solvent

Much of the focus on biomolecular recognition is, quite rightly, concerned with the interactions between the solute molecules of interest. However, statistical mechanics does not partition a system into components (such as 'protein, 'ligand' and 'solvent'); rather, the partition function is a function of the *system's* Hamiltonian (see Eq. (13)). Therefore, a complete understanding of biomolecular recognition requires consideration of the solvent as well. Two models for the role of solvent exist: it may play a passive role, filling space and screening electrostatics, or it may play a more active role, such as stabilizing biomolecular complexes through interactions with solute molecules. Increasingly it is becoming clear that the latter is often the case.

Oftentimes, individual water molecules play crucial roles in stabilizing biomolecular complexes. Using TI, Hamelberg *et al.* calculated the binding free energies associated with water molecules directly stabilizing protein–ligand interactions for two complexes, trypsin bound to benzylamine and HIV-1 protease bound to the inhibitor KNI-272 (Hamelberg & McCammon, 2004). These individual water molecules were shown to contribute 2–3 kcal/ mol in free energy to the complex. Using the same technique, Samsonov *et al.* examined the role of water molecules in stabilizing protein–protein interactions, and showed that water molecules have diverse roles in mediating protein contacts (Samsonov *et al.* 2008). In one case it was shown that hydrogen bonds between two water molecules resulted in cooperative stabilization of protein interactions, indicating that complex interaction dynamics between multiple solvent molecules and solute sites may be important for providing a complete understanding of recognition processes.

The heterogeneous roles of solvent molecules in biomolecular recognition have made it difficult to discern general principles describing water interactions. Recent simulations on a model system addressed this question. Through the use of umbrella sampling calculations at multiple temperatures on the simple model system of a spherical ligand binding into a hemispherical cavity, Baron et al. decomposed the entropic and enthalpic contributions to ligand binding or rejection for neutral and charged ligands binding to neutral and charged receptors (Baron et al. 2010; Hummer, 2010; Setny et al. 2010). Results demonstrated that water dominated the binding thermodynamics. Surprisingly, the hydrophobic binding of a neutral ligand to a neutral receptor was found to be more stable than that of a charged ligand to an oppositely charged receptor. This hydrophobic association is enthalpically driven due to the increased number of water-water hydrogen bonds when the ligand is bound in the receptor, since in the unbound state water molecules must occupy the receptor and are forced into geometries that are sub-optimal for hydrogen bonding with neighboring water molecules. The polarity of the water molecules also resulted in a charge asymmetry, with a positively charged ligand binding stronger to a negative receptor than a negatively charged ligand binding to a positive receptor, largely due to increased entropic costs in the latter case which are not prevalent in the former.

The increased focus on individual water molecules in biomolecular recognition has led to the development of new tools to aid in addressing their thermodynamics. Two recent tools, JAWS and WaterMap, attempt to address this by using grand canonical Monte Carlo and explicit-solvent MD simulations, respectively, to compute the 'hydration sites' (regions with high-water density) in a protein's binding site, along with the thermodynamics of expulsion of a water molecule in that site to the bulk solvent (Abel et al. 2008, 2010; Michel et al. 2009b; Young et al. 2007). This free energy difference dictates whether displacement of the water molecule by a ligand is thermodynamically favorable or not, and early results indicate that, for a congeneric series of ligands, the correlation between these scores and experimental binding energies is quite good, suggesting that this is a fundamentally important component in the thermodynamics of protein-ligand interaction which may not have been accurately accounted for in the past (Beuming et al. 2009; Guimãraes & Mathiowetz, 2010; Michel et al. 2009b; Pearlstein et al. 2010). However, because these methods do not directly account for protein-ligand interactions, they may only be expected to perform well for ligands that form a near-optimal number of polar and apolar contacts with the host protein.

4.3 The case of T4 lysozyme

The association of a ligand into a protein's binding site is not only conceptually more straightforward than protein-protein recognition, it has obvious pharmaceutical implications. Therefore, it is not surprising that a majority of work in the field has gone towards the development of methods to predict both the binding configurations and energies of small molecules in protein binding sites. To effectively advance these methods, model systems are required which may be easily studied by both experimental and computational techniques. The T4 lysozyme has become one of these systems (Wei et al. 2002). Mutation of a leucine to an alanine at position 99 creates a cavity that is small, hydrophobic, and free from solvent interactions, thus creating a simple binding site for small, apolar ligands (see Fig. 5a, b) (Eriksson et al. 1992; Morton & Matthews, 1995; Morton et al. 1995). A single hydrogen bond acceptor can be introduced into this cavity through the mutation of the methionine at position 102 to glutamine (the L99A/M102Q mutant), creating a model site that preferentially binds small molecules that have one or two hydrogen bond donors (see Fig. 5c) (Boyce et al. 2009). Here, we present a brief overview of some of the applications of the free energy methods described above, and their limitations, to both of these model binding sites.

Hermans and Wang provided an early example of applying alchemical transformation methods to protein-ligand interactions with their calculations of the binding energy for benzene in the L99A cavity (Hermans & Wang, 1997). Although computational power limited their simulation length (relative to modern simulations), calculations with mobile protein atoms that were initiated from the L99A/benzene crystal structure showed remarkably good agreement with experimental binding energies (-5.14 kcal/mol versus -5.19 kcal/mol). The importance of receptor flexibility and the initial configuration was highlighted in a series of simulations in which the protein was held rigid in various conformations, resulting in inaccurate free energies varying from -3.5 to -8.9 kcal/mol. In a subsequent study, Mann and Hermans used similar technique (with longer simulation times) to analyze the binding of noble gases into the L99A binding pocket, with results agreeing well with crystallographic data for binding site locations and occupancy thermodynamics of xenon, argon and krypton ions at high pressure (Mann & Hermans, 2000). The longer simulations also allowed for the observation of large and slow interdomain motions, while intradomain structures were relatively rigid, consistent with previous MD simulations (de Groot et al. 1998; Hayward & Berendsen, 1998).

As free energy methods have developed, T4 lysozyme has been used to test their effectiveness, such as in the introduction of restraint potentials necessary for ensuring that the species being decoupled in alchemical transformations retains pertinent locations and orientations (Boresch et al. 2003; Deng & Roux, 2006). Mobley et al. focused on testing alchemical methods in the pharmaceutically relevant context of predicting highly accurate binding affinities for a series of small molecules to a specific binding site (Mobley et al. 2007b). First, they examined the binding of 13 aromatic molecules into the binding cavity of L99A, 11 of which ITC experiments had previously established binding affinities for, and two of which were known to be non-binders. When only a single initial configuration was accounted for, calculations showed a root mean square (RMS) error of 3.51 kcal/mol and a correlation, R, of 0.51 to experimental values. These values could be improved to 2.55 kcal/ mol and 0.72 by including multiple initial configurations. The authors noted the side chain of valine 111 reoriented upon binding in crystal structures but not in their simulations (due to high energy barriers), and achieved improved agreement to experiments (2.24 kcal/mol and R = 0.72) by forcing rotation of this side chain using the 'confine-and-release' method (Mobley et al. 2007a). Their best agreement to experimental values came upon replacement of the charge model of the ligands with a model closer to the one used in parameterizing the protein, for a final RMS of 1.89 kcal/mol and R = 0.79. The group then used this method on a blind test of five small molecules predicted to bind with docking algorithms while subsequently experimentally determining their docking poses with X-ray crystallography and binding affinities by ITC. Not only did the free energy calculations provide docking poses close to the experimentally observed ones, they correctly discriminated between binders and non-binders and had an RMS error of only 0.57 kcal/mol, both of which were substantial improvements upon docking results.

In a follow up study by the same groups, Boyce *et al.* performed similar blind tests on the polar cavity of the L99A/M102Q mutant and showed that the inclusion of polarity reduced the reliability of alchemical calculations (Boyce *et al.* 2009). In this work, 13 small molecules were tested, yielding correct predictions on the binary question of whether a molecule would bind or not for 10 of these. The RMS error to experiments was 1.8 kcal/mol (excluding the non-binders for which affinity could not be measured), and the rank ordering of ligands did not agree with experiments. Relative free energies within congeneric series were also calculated, and it was shown that the reliability of free energies within a series was related to the accuracy of the ligand poses. For the best series (modifications of the ligand catechol), the RMS error was only 1.1 kcal/mol and the rank ordering of modifications agreed with experiments. It is worth noting that results for both this site and the L99A cavity

were much improved (although more expensive) over end-point calculations using MM-GBSA calculations, which had difficulty discerning between binders and non-binders (Graves *et al.* 2008).

5. Conclusion

Through the use of methods grounded in statistical mechanics, computer simulations have proved invaluable in advancing our understanding of thermodynamic properties important in biomolecular recognition. Thermodynamic pathway calculations, while expensive, provide the best agreement to experimental free energy results, with errors typically of the order of 1-2 kcal/mol, while quicker end-point calculations provide a decent approximation with higher errors. Harmonic and quasi-harmonic calculations may be used to compute the conformational entropy of a protein through the use of either static structures or simulation results. The refinement of these techniques and the development of new ones show promise for improving our ability to calculate thermodynamics with increased precision. These simulations should be viewed as a complement to experimental methods, and as both the methods and the computing power increase so too should our ability to interpret and guide future experiments.

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(a) Microcanonical ensemble



Fig. 1.

The microcanonical ensemble (a) consists of a constant number of particles (N) in a box of constant volume (V) with constant energy (E) that are isolated from the outside world. The canonical ensemble (b) is an extension of this ensemble, in which N and V are still constants, but the system is allowed to exchange energy with the outside world while the temperature (T) is a constant.

Accuracy

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Fig. 2.

The major types of free energy calculations can be divided into three categories: biomolecular docking, end point and thermodynamic pathway calculations. In general, there is a trade-off between the speed and accuracy of these methods. Wereszczynski and McCammon



Fig. 3.

The thermodynamic cycle used in free energy calculations. Potential of mean force calculations attempt to compute ΔG_{bind} directly by computing the free energy along a path to bring a ligand into a protein's binding pocket. Alchemical transformations take an alternative route by calculating ΔG_{water} and $\Delta G_{\text{protein}}$ through decoupling of the ligand from a solvated and protein-bound environment, respectively. Because free energy is a state function, and the bottom leg of the free energy cycle equals zero (since in that part nothing is moved into the protein's binding pocket) ΔG_{bind} may be calculated as the difference of ΔG_{water} and $\Delta G_{\text{protein}}$.



Fig. 4.

Estimation of effective harmonic potentials $U_{\rm eff}$ to fit the underlying potential energy surface with a normal mode and quasi-harmonic analysis. The normal mode analysis computes an effective potential based on the landscape local to a minimum energy structure, whereas quasi-harmonic analysis fits an effective potential to the area sampled through a simulation.

Wereszczynski and McCammon



(a) L99A T4 Lysozyme

(b) L99A active site (c) L99A/M102Q active site

Fig. 5.

Structure of the L99A mutant of T4 lysozyme with a benzene molecule bound in the nonpolar binding site (PDB ID: 181L, Morton & Matthews, 1995) (*a, b*), and the polar L99A/ M102Q mutant with a bound catechol molecule (PDB ID: 1XEP, Graves *et al.* 2005) (*c*). These two mutants have become model systems upon which numerous computational studies have been performed. Side chains for residues Val111 and Met102 (Gln102 in (*c*)) are shown.