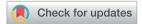
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Strain induced valley degeneracy: a route to the enhancement of thermoelectric properties of monolayer WS₂†

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Two-dimensional transition metal dichalcogenides show great potential as promising thermoelectric materials due to their lower dimensionality, the unique density of states and quantum confinement of carriers. Here the effects of mechanical strain on the thermoelectric performances of monolayer WS₂ have been investigated using density functional theory associated with semiclassical Boltzmann transport theory. The variation of the Seebeck coefficient and band gap with applied strain has followed the same type of trend. For n-type material the relaxation time scaled power factor $(S^2\sigma/\tau)$ increases by the application of compressive strain whereas for p-type material it increases with the application of tensile strain due to valley degeneracy. A 77% increase in the power factor has been observed for the n-type material by the application of uniaxial compressive strain. A decrease in lattice thermal conductivity with the increase in temperature causes an almost 40% increase in ZT product under applied uniaxial compressive strain. From the study, it is observed that uniaxial compressive strain is more effective among all types of strain to enhance the thermoelectric performance of monolayer WS₂. Such strain induced enhancement of thermoelectric properties in monolayer WS₂ could open a new window for the fabrication of high-guality thermoelectric devices.

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Introduction

Low dimensionality of materials opens a new window to enhance thermoelectric properties due to their unique density of states (DOS) and the quantum confinement effect. Due to the unique layered structure, two dimensional (2D) materials have attracted much attention. The first synthesized 2D layered material graphene is well known for its very high mobility but opening a reasonable band gap in graphene is still a challenging problem.1 Therefore 2D transition metal dichalcogenides (TMDCs) came into the picture owing to their tunable bandgap, high electrical mobility, low thermal conductivity, chemical stability, etc.2 The fantastic combination of electrical and thermal transport in these 2D materials can lead to a significantly large thermoelectric figure of merit (ZT). TMDCs show a great potential in thermoelectric application to convert waste heat to electricity because of their high electrical conductivity and low thermal conductivity. Theoretical calculation of the thermoelectric properties of monolayer TMDCs suggests that the ZT product of these materials is generally low³ as compared to well-known thermoelectric materials such as Bi₂Te₃ and Bi₂Se₃. Various efforts like chemical doping and

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functionalization,⁵ strain engineering,⁶ defect engineering,⁷ making heterostructures⁸ have been taken into consideration to enhance the thermoelectric properties. Among these strain engineering is one of the most popular methods to tune the electronic and thermoelectric properties of these materials.

The effect of layer numbers on the thermoelectric power factor (PF) and ZT product has been predicted theoretically for MoS₂, MoSe₂, WS₂ and WSe₂ and the enhancement of ZT product in TMDCs is due to the increased degeneracy of the band edges.9,10 High ZT value close to 1 has been predicted in suspended monolayer and bilayer MoS₂ which is much higher than that of bulk suggests that low dimensionality may be a possible way to enhance the thermoelectric properties. 11 By layer mixing or forming heterostructures of different TMDCs thermoelectric performance is enhanced due to increased DOS and reduction of band gap near the Fermi level. 12,13 Theoretical calculation predicted the value of lattice thermal conductivity $(k_{\rm ph})$ of monolayer MoS₂ nanoribbon to be 29.2 W m⁻¹ K⁻¹ (ref. 14) which is higher than previous value of 1.35 W m^{-1} K $^{-1}$ (ref. 15) but matched closely with experimental value of 34.5 W m⁻¹ K⁻¹. Experimental observation of very large power factor of 8.5 m W m⁻¹ K⁻² at room temperature in exfoliated few layer MoS₂ because of the increased DOS and 2D confinement of electrons near the band edge suggests that 2D TMDCs may turn out to be promising thermoelectric materials. Enhanced thermoelectric properties have been observed both experimentally and theoretically in monolayer MoS2 with applied external electric field

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due to the change in valley degeneracy. 17,18 The effect of mechanical strain on the electronic and vibrational properties in different TMDCs has been investigated theoretically and suggests that TMDCs are very sensitive to mechanical strain¹⁹⁻²³ and monolayer MoS2 is dynamically stable up to 15% biaxial tensile strain.24 Enhancement of thermoelectric power factor by the application of compressive strain on monolayer MoS₂ has been predicted theoretically and maximum PF has been found for n-type doping with applied 3% uniaxial zigzag compressive strain. A 2-4% biaxial tensile strain results a reduction in $k_{\rm ph}$ of monolayer suggests that strain engineering could be an effective way to increase ZT product.26 Uniaxial compressive strain induced enhancement of layered oxychalcogenides BiCuOCh (Ch = S, Se and Te) has been predicted and an increment of the power factor by 11.4% by applying -6% compressive strain is also observed.27,28

Though in TMDCs, MoS₂ is the most widely studied material a thorough investigation of the role of strain on WS₂ is highly warranted. In this work to the best of our knowledge for the first time we have performed a systematic investigation of electronic, vibrational and thermoelectric properties of monolayer WS2 and the effect of different types of strain on electronic and thermoelectric properties of monolayer WS2. We have shown the variation of thermoelectric properties with chemical potential as well as carrier concentration and our study show that both the approaches lead to same results. The first principle calculation shows that the ZT product can be enhanced by 38.5% with applied uniaxial compressive strain and we have found the highest ZT product of 0.72 in monolayer WS2. Such compressive strain induced enhancement of thermoelectric properties in monolayer WS2 can have potential application in thermoelectric devices for the efficient conversion of wastage heat to electricity.

Computational details

First principles calculation has been performed using density functional theory (DFT) with projector augmented wave (PAW)29 potentials and the Perdew-Burke-Ernzerhof (PBE)30 generalized gradient approximation (GGA)31 as exchange correlation functional in Quantum Espresso (QE) package. 32 A sufficient vacuum of 17 Å along C axis was created to avoid the interaction between layers in periodic boundary condition for monolayer of WS₂. A $12 \times 12 \times 1$ dense mesh grid was used to optimize the geometry and energy cutoff for the electronic wavefunctions was set to 50 Ry throughout all the calculations. For the density of state (DOS) and thermoelectric parameter calculations a high dense mesh of K points $48 \times 48 \times 1$ was used. The strain is calculated as $\varepsilon = \frac{|a - a_0|}{a_0} \times 100\%$ where a_0 and a are the lattice constant of relaxed and strained structures respectively. For the thermoelectric and transport properties, a semi classical Boltzmann transport theory was used with constant scattering time approximation (CSTA) as implemented in BoltzTrap³³ code. In CSTA we assume that scattering time has very less dependency on energy and both the group velocity of carriers and DOS

contribute to the transport function. The group velocity (ν_g) of carriers in a specific band can be described as

$$v_{\alpha}(i, \mathbf{k}) = \frac{1}{\hbar} \frac{\partial \varepsilon(i, \mathbf{k})}{\partial \mathbf{k}_{\alpha}}, \tag{1}$$

where \mathbf{k}_{α} is the α^{th} component of wavevector \mathbf{k} and $\varepsilon(i,\mathbf{k})$ is the i^{th} energy band and the conductivity tensor can be obtained in terms of group velocity as

$$\sigma_{\alpha\beta}(i,\mathbf{k}) = e^2 \tau(i,\mathbf{k}) v_{\alpha}(i,\mathbf{k}) v_{\beta}(i,\mathbf{k}), \tag{2}$$

The Seebeck coefficient, electrical conductivity and thermal conductivity due to electron can be calculated by using the values of group velocity $v_{\alpha}(i,\mathbf{k})$ as implemented in BoltzTrap³³ code by following equations

$$S_{\alpha\beta}(T,\mu) = \frac{1}{eT} \frac{\int v_{\alpha}(i,\boldsymbol{k})v_{\beta}(i,\boldsymbol{k})(\varepsilon-\mu) \left[-\frac{\partial f_{\mu}(T,\varepsilon)}{\partial \varepsilon} \right] d\varepsilon}{\int v_{\alpha}(i,\boldsymbol{k})v_{\beta}(i,\boldsymbol{k}) \left[-\frac{\partial f_{\mu}(T,\varepsilon)}{\partial \varepsilon} \right] d\varepsilon}, \quad (3)$$

$$\frac{k_{\alpha\beta}^{\rm el}(T,\mu)}{\tau(i,\mathbf{k})} = \frac{1}{TV} \int v_{\alpha}(i,\mathbf{k}) v_{\beta}(i,\mathbf{k}) (\varepsilon - \mu)^2 \left[-\frac{\partial f_{\mu}(T,\varepsilon)}{\partial \varepsilon} \right] d\varepsilon, \quad (4)$$

$$\frac{k_{\alpha\beta}^{\text{el}}(T,\mu)}{\tau(i,\boldsymbol{k})} = \frac{1}{TV} \int v_{\alpha}(i,\boldsymbol{k}) v_{\beta}(i,\boldsymbol{k}) (\varepsilon - \mu)^{2} \left[-\frac{\partial f_{\mu}(T,\varepsilon)}{\partial \varepsilon} \right] d\varepsilon, \quad (5)$$

where $e,\,T,\, au,\,\mu$, V are electronic charge, temperature, relaxation time, chemical potential, volume of a unit cell respectively and $f_{\mu}(T,\varepsilon)=rac{1}{\mathrm{e}^{(\varepsilon-\mu)/K_{\mathrm{B}}T}+1}$ is the Fermi–Dirac distribution function.

The lattice thermal conductivity $(k_{\rm ph})$ has been calculated with the linearized phonon Boltzmann equation as implemented in Phono3py³⁴ code interfaced with Quantum Espresso (QE) package.³² $k_{\rm ph}$ can be expressed as

$$k_{\rm ph} = \frac{1}{NV_0} \sum_{\lambda} C_{\lambda} \nu_{\lambda} \otimes \nu_{\lambda} \tau_{\lambda} \tag{6}$$

where N, V_0 and λ are the total number of q points for sampling Brillouin Zone, volume of a unit cell and phonon mode respectively and C_{λ} , ν_{λ} and τ_{λ} are specific heat, phonon group velocity and phonon lifetime respectively. The phonon lifetime (τ_{λ}) can be expressed as

$$\tau_{\lambda} = \frac{1}{2\Gamma_{\lambda}(\omega_{\lambda})} \tag{7}$$

where $\Gamma_{\lambda}(\omega)$ is known as phonon linewidth and has following form:

$$\Gamma_{\lambda}(\omega) = \frac{18\pi}{\hbar^{2}} \sum_{\lambda'\lambda''} |\phi_{-\lambda\lambda'\lambda''}|^{2} \left[(n_{\lambda'} + n_{\lambda''} + 1)\delta(\omega - \omega_{\lambda'} - \omega_{\lambda''}) + (n_{\lambda'} - n_{\lambda''}) \right]$$

$$- n_{\lambda''} \left[\delta(\omega + \omega_{\lambda'} - \omega_{\lambda''}) - \delta(\omega - \omega_{\lambda'} + \omega_{\lambda''}) \right]$$
(8)

where $\phi_{-\lambda\lambda'\lambda''}$ and n_{λ} are the strength of interaction between three phonons λ , λ' and λ'' and phonon occupation number respectively. The detailed calculation can be found elsewhere.³⁴ For the 2nd and 3rd order of interatomic force constant

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calculation we construct a 2 \times 2 \times 1 supercell sampled with 6 \times 6×1 densed k-point meshes and for the computation of lattice thermal conductivity the reciprocal space of primitive cell was sampled by $20 \times 20 \times 1$ k-point meshes.

The thermoelectric figure of merit (ZT) has been calculated using the formula

$$ZT = \frac{S^2 \sigma T}{k_{\rm el} + k_{\rm ph}},\tag{9}$$

Where S, σ , T are Seebeck coefficient, electrical conductivity and temperature respectively and $k_{\rm el}$ and $k_{\rm ph}$ are thermal conductivity due to electron, and lattice thermal conductivity due to phonon respectively.

Results and discussions

Structural parameters

Monolayer WS2 has a hexagonal honeycomb structure belonging to P63/mmc space group with S-W-S layer where W atoms are sandwiched between two layers of S atoms connected with covalent bonds known as 1H phase as shown in Fig. 1a. Bilayer WS₂ (2H) consists of two such S-W-S monolayers which are separated by Vander Waals interaction. The optimized lattice constant of a = b =3.19 Å for a unit cell of monolayer agrees with previous calculations35 and experimental value.36 To apply biaxial strain lattice parameters (a = b = 3.19 Å) are varied up to $\pm 6\%$ in the steps of 1% where + and - signs represent tensile and compressive strain respectively as shown in Fig. 1c. But in case of uniaxial strain we only vary lattice constant "a" up to $\pm 6\%$ while keeping b=3.19 Å fixed as shown in Fig. 1d.

Thermoelectric properties

Fig. 2a shows the variation of carrier concentration of the WS₂ monolayer with chemical potential at three different temperatures namely 300 K, 600 K and 900 K. Carrier concentration is zero in the band gap region and increases as we go to the band edge. The variation of Seebeck coefficient (S) with chemical potential (μ) shows that very high S value has been observed near the bandgap region as shown on Fig. 2b. S decreases as we go away from band gap region to the valence band and conduction band. This is because as we go away from bandgap region carrier concentration increases as shown in Fig. 2a. And S is inversely proportional to carrier concentration. At 300 K the value of S is 2821 μ V K⁻¹ for p-type carriers and 2728 μ V K⁻¹ for n-type carriers respectively in monolayer WS2. The S values decreased to 1429 μ V K⁻¹ and 1446 μ V K⁻¹ at 600 K and 926 μ V K^{-1} and 967 $\mu V K^{-1}$ at 900 K for p-type and n-type carriers respectively. At 300 K electrical conductivity is almost zero in the region between the VBM and CBM but it increases at 600 K and 900 K as shown in Fig. 2c. This is due to the increase in the number of carriers at elevated temperatures. Because of high electrical conductivity the thermoelectric power factor $(S^2\sigma/\tau)$ has also increased. Fig. 2d shows how thermoelectric power factor $S^2\sigma/\tau$ (relaxation time scaled) varies with chemical potential $\mu(Ry)$. At 300 K the $S^2\sigma/\tau$ is observed to be 5.22 \times $10^{10} \text{ W m}^{-1} \text{ K}^{-2} \text{ s}^{-1}$ for n-type carriers $(\mu > E_f)$ which increases with temperature and becomes $23.88 \times 10^{10} \,\mathrm{W} \,\mathrm{m} \,\mathrm{K}^{-2} \,\mathrm{s}^{-1}$ at 900 K. The highest $S^2\sigma/\tau$ at 300 K, 600 K, and 900 K are observed to be $8.57 \times 10^{10} \,\mathrm{W m^{-1} K^{-2} s^{-1}}$, $19.49 \times 10^{10} \,\mathrm{W m^{-1} K^{-2} s^{-1}}$, and $33.35 \times 10^{10} \,\mathrm{W m^{-1} K^{-2} s^{-1}}$ for n-type region respectively. The corresponding $S^2\sigma/\tau$ at 300 K, 600 K, and 900 K for p-type

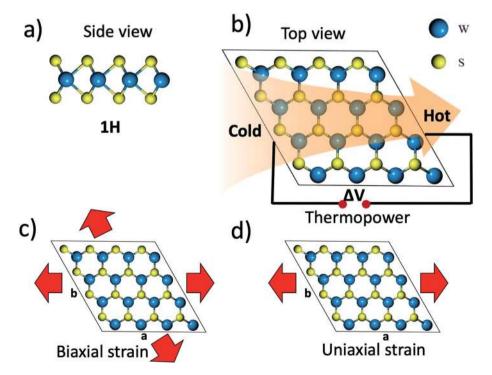


Fig. 1 Crystal structure of monolayer WS₂ (a) side view (b) top view and thermoelectric effect (c) application of biaxial strain (d) application of uniaxial strain.

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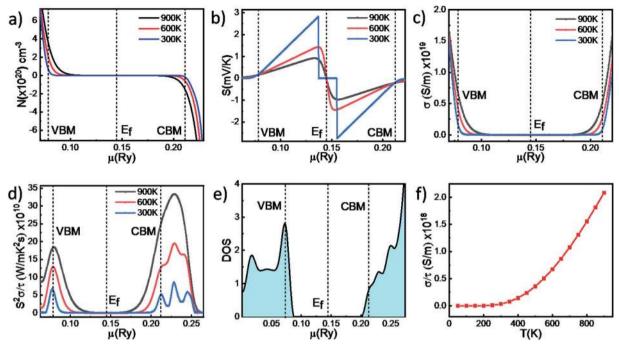


Fig. 2 Variation of (a) carrier concentration (b) Seebeck coefficient (S) (c) electrical conductivity (σ/τ) (d) relaxation time scaled thermoelectric power factor $(S^2\sigma/\tau)$ as a function of chemical potential μ (Rydberg unit). The dotted lines represent the valence band maximum (VBM), Fermi energy (E_t) and conduction band minimum (CBM) respectively (e) the density of states (DOS) as a function of chemical potential (f) variation of electrical conductivity with temperature in monolayer WS₂.

carriers are 6.77 \times 10^{10} W m^{-1} K^{-2} s $^{-1}$, 12.90 \times 10^{10} W m^{-1} K^{-2} $\rm s^{-1}$, and $18.4 \times 10^{10} \, \rm W \, m^{-1} \, K^{-2} \, s^{-1}$ at VBM respectively which are lower than the values obtained for n-type carriers at CBM which indicates that n-type doping is more effective than p-type doping in semiconducting WS₂. At 300 K in n-type region there are clearly three peaks in which first peak corresponds to the CBM. As temperature increases the two side peaks convert into two little hump and at 900 K there is one peak corresponding to highest power factor. But no such thing is observed in p-type region. This type of behavior can be explained from DOS near the band edge which is shown in Fig. 2e. Near the valence band edge there is only one peak which corresponds to the energy state at VBM but in conduction band edge there are three humps near the conduction band edge and among them 1st hump corresponds to the CBM at 0.211 Ry and the second hump at 0.228 Ry corresponds to the highest $S^2\sigma/\tau$ value near

the conduction band edge. As transport takes place near the band edge, we only check the peaks near the valence and conduction band edges. The variation of relaxation time scaled electrical conductivity *i.e.* σ/τ with temperature shows the semiconducting behavior of WS₂ and can be seen in Fig. 2f.

We have also shown the variation of Seebeck coefficient, $S^2\sigma/\tau$, σ/τ and $K_{\rm el}$ as a function of carrier concentration (*N*) (ESI Fig. S1†) and our results suggest that these values are similar to that calculated from chemical potential approach.

Effect of Bi-axial strain

Before studying the role of strain on various thermoelectric properties of WS_2 the stability of the structure was validated from the cohesive energy calculations³⁷ by varying the strain on the material. The detail of which is given in Fig. S7 of the ESI.†

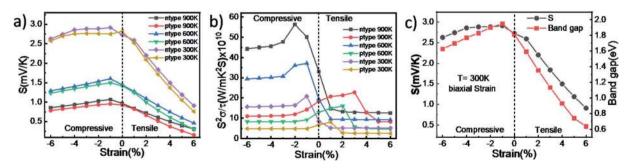


Fig. 3 Variation in (a) Seebeck coefficient and (b) $S^2\sigma/\tau$ with applied both biaxial compressive and tensile strain for n-type and p-type doping at 300 K, 600 K and 900 K. (c) Variation in Seebeck coefficient and band gap with the application of biaxial strain and these show similar type of trend.

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Table 1 Variation of S, $S^2\sigma/\tau$ and ZT product with different types of strain at 300 K, 600 K and 900 K for n-type and p-type carriers

		$S(\mu V K^{-1})$			$S^2 \sigma / \tau \ (W \ m^{-1} \ K^{-2} \ s^{-1})$			ZT		
Strain (%)		300 K	600 K	900 K	300 K	600 K	900 K	300 K	600 K	900 K
0%	n	2728	1446	968	8.50	19.50	33.15	0.067	0.308	0.516
	p	2821	1419	926	6.70	12.90	18.40	0.082	0.322	0.494
−1% Bi axial	n	2914	1603	1067	20.82	37.15	50.10	0.195	0.500	0.655
	p	2751	1496	956	4.80	9.170	14.24	0.060	0.268	0.440
−2% Bi axial	n	2887	1533	1032	16.35	36.10	56.35	0.165	0.504	0.700
	p	2760	1451	933	4.77	8.26	11.89	0.06	0.258	0.430
+2% Bi axial	n	2204	1090	718	5.18	9.38	13.14	0.074	0.304	0.478
	p	2088	996	665	2.70	16.00	21.30	0.168	0.363	0.550
-2% uniaxial	n	2890	1597	1066	20.17	37.19	50.63	0.192	0.506	0.660
	p	2757	1483	954	4.86	9.28	14.42	0.0624	0.274	0.453
-4% uniaxial	n	2861	1519	1029	15.65	39.16	59.00	0.153	0.520	0.720
	р	2753	1436	922	4.86	8.41	12.00	0.062	0.262	0.433
+4% uniaxial	n	2195	1084	714	5.262	9.43	13.13	0.069	0.296	0.478
	p	2081	997	668	13.83	16.56	22.60	0.152	0.370	0.568

The variation in Seebeck coefficient with applied biaxial strain (tensile and compressive) for n-type and p-type doping at 300 K, 600 K and 900 K is shown in Fig. 3a. In case of biaxial compressive strain (BCS) the value of S increases as we apply higher strain up to a point and after that point S starts decreasing. This behavior is observed for both p-type and n-type carriers, but S has higher value for n-type carriers than p-type carriers. The highest value obtained at 1% of BCS is 1067 μ V K^{-1} for n type and 955 μV K^{-1} for p-type at 900 K. But S decreases with application of biaxial tensile strain (BTS) for both types of carrier. The variation of band gap with applied strain follows the same trend as that of the Seebeck coefficient and is shown in Fig. 3c as described by Goldsmid-Sharp

relation³⁸ given by the formula, $E_{\rm g}=2e|S_{\rm m}|T_{\rm m}$ where $S_{\rm m}$ is the highest Seebeck coefficient, $T_{\rm m}$ is the corresponding temperature and E_g is the band gap. If we look at the electronic band structure of single layer WS₂ (ESI Fig. S2b†) it is clearly seen that at 1% BCS band gap is highest and remains direct and after 2% BCS it starts to decrease and becomes indirect. This is the reason for higher values of Seebeck coefficient at 2% BCS. But for BTS band gap decreases and becomes indirect at 1% BTS and as BTS increases band gap decreases rapidly by going to the point of semiconducting to metal transition at 10% of BTS (ESI Fig. S2g†). That is why Seebeck coefficient decreases by the application of BTS.

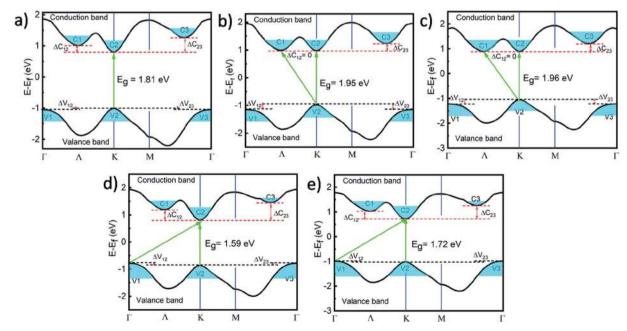


Fig. 4 Band structure and valleys of monolayer WS₂ under the application of (a) 0% strain (b) -1% biaxial strain (c) -2% uniaxial strain (d) +1% biaxial strain (e) +1% uniaxial strain. Here only the highest valence band and lowest conduction band is shown. The red dotted lines and black dotted lines represent energy levels of electron valleys in conduction band and hole valleys in valence band respectively. The green arrow represents direct/indirect band gap transition between hole and electron valleys

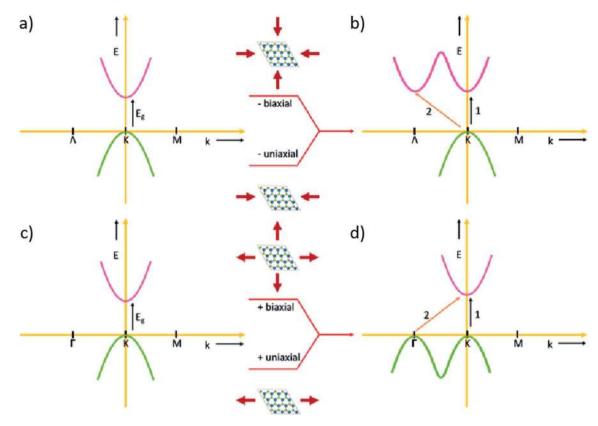


Fig. 5 Schematic representation of valley degeneracy in strained WS_2 . (a) Represents the E-k curve of an unstrained WS_2 monolayer. (b) The same dispersion curve under compressive biaxial or uniaxial strain. (c and d) The dispersion curve under the application of tensile strain which can be either uniaxial or biaxial in nature. In figure (b) and (d) one can clearly see double valleys in the conduction band and valence band respectively.

The power factor $S^2\sigma/\tau$ (PF) increases significantly by applying BCS for n-type carriers and highest PF is found at 2% compressive strain with a value of 56.35×10^{10} W m⁻¹ K⁻² s⁻¹ which is more than 50% higher than that of without strain at 900 K as shown in Fig. 3b. However, by applying BCS the PF decreases up to 2% of BCS and then remains constant afterwards for p-type carriers.

An opposite trend was observed with application of BTS. In this case PF decreases rapidly with increasing tensile strain up to 2% and then becomes constant with a very lower value than that without strain for n-type carriers which suggest that application of BTS is not favorable for n-type doping. But

thermoelectric PF increases for p-type carriers with the application of BTS. The highest PF is found to be $23.8 \times 10^{10}~W~m^{-1}~K^{-2}~s^{-1}$ which is 29% higher than that of without strain for p-

Table 2 Calculated deformation potential $(E_{\rm dp})$, stretching modulus $(C_{\rm 2D})$, effective mass (m^*) , relaxation time (τ) and mobility (μ^{2D}) of electron and hole in monolayer WS₂

	E_{dp} (eV)	C_{2D} (N m ⁻¹)	m*	τ (fs)	$\mu^{2D} \left(\text{cm}^2 \text{V}^{-1} \text{s}^{-1} \right)$
Electron	14.00	164.097	0.3500		97.33
Hole	6.582	164.097	0.5125		205.36

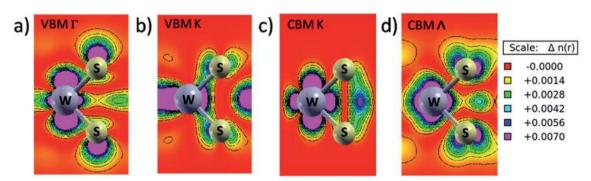


Fig. 6 Band decomposed charge density plot of WS₂. (a) The VBM at Γ point (b) the VBM at Κ point (c) the CBM at Κ point (d) the CBM at Λ point.

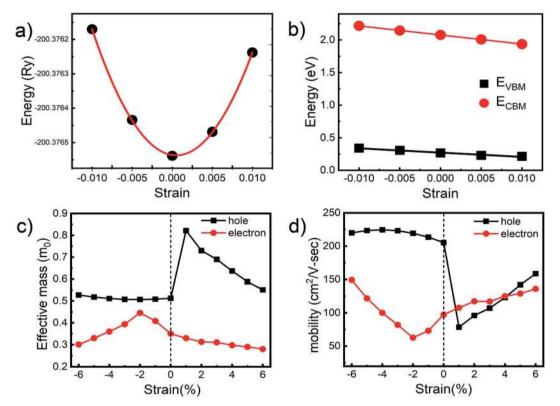


Fig. 7 The variation of (a) total energy with applied strain and (b) shift in the VBM and CBM with applied strain to determine deformation potential and variation in (c) effective mass and (d) carrier mobility as a function of biaxial strain at room temperature.

type carriers at 3% of BTS and at 900 K. So, at 900 K PF is highest by applying 2% of BCS for n-type carriers but for p-type carriers PF has a maximum value by applying 3% of BTS though the maximum PF for n-type is much higher than that of the p-type. From this analysis it is clear that BCS is most favorable for n-type doping whereas BTS is suitable for p-type doping.

The effect of uniaxial strain was also studied in the same system and it is found that the application of UCS affects more for n-type doping and UTS for p-type doping although the highest power factor at 4% of UCS for n-type is very much higher than that of p-type carriers. The detail study can be found in the ESI (SI3).†

The ZT product study also suggests that both UCS and BCS affect the ZT product positively and detail of which can be found in the ESI Fig. S8.† We have found highest ZT product of the value of 0.72 at 4% uniaxial compressive strain. All the parameters studied for WS $_2$ have been included in Table 1.

Electronic band structure and valley degeneracy

The electronic band structure of unstrained monolayer WS₂ is shown in Fig. 4a. To plot the band structure we choose the k path as Γ –K–M– Γ as previous calculation.³⁹ Our calculation shows that the highest valence band has two hole valleys at Γ point (V_1 and V_3) and one at K point (V_2) which are almost degenerate and the energy difference between the hole valleys, ΔV_{12} and ΔV_{23} are almost zero. In the conduction band three electron valleys at K point (C_2), at a point in between Γ and K point (let say Λ point) (C_1) and at the

point in between Γ and $M(C_3)$ and they don't show valley degeneracy as the energy difference of $\Delta C_{12} = 0.2045$ eV and $\Delta C_{23} =$ 0.46 eV are seen in Fig. 4a. The conduction band minima (C_2) and valence band maxima (V_2) both lie on same K points and a direct band gap of 1.81 eV has been observed in unstrained monolayers WS₂. When we apply 1% biaxial compressive strain electron valleys at K point (C_2) and Λ point (C_1) become degenerate as difference between these two valleys vanishes ($\Delta C_{12} = 0$ eV) and ΔC_{23} reduces hence the conduction band shows valley degeneracy as shown in Fig. 4b. Now both direct (K-K) and indirect (K- Λ) transition can take place and both the electron valleys C_1 and C_2 contribute to the transport. This is why thermoelectric properties enhanced initially for n-type carries under the application of compressive strain. At the same time the hole valley at K point (V_2) remains same but hole valleys at Γ point (V_1 and V_2) go downward and hole valley degeneracy in valence band is broken hence with the application of compressive strain thermoelectric performance of monolayer WS2 for p-type carries decreases. As we increase biaxial compressive strain the valley degeneracy in conduction band as well as valence band are broken after 2% compressive strain and the thermoelectric performances decrease (ESI Fig. S5a†). In the case of uniaxial compressive strain, the electron valley degeneracy occurs at 2% strain with a direct or indirect band gap of 1.96 eV and at this point hole valley degeneracy is broken as shown in Fig. 4c. Electron valley degeneracy disappeared slowly at higher strain and after 4% uniaxial strain degeneracy breaks (ESI Fig. S5b†).

As we apply 1% tensile strain (both biaxial and uniaxial) the hole valleys V_1 , V_2 , and V_3 in valence band are nearly degenerate

but the difference between conduction band valleys C_1 , C_2 and C_3 increases as shown in Fig. 4d and e. As CBM lies at K point an indirect (Γ –K) or direct transition (K–K) with a band gap of 1.59 eV and 1.72 eV for biaxial and uniaxial tensile strain respectively, can take place and both hole valleys at Γ point (V_1 and V_3) and K point (V_2) can take part in transport. This is the reason for thermoelectric power factor for the p-type doping initially increases with the application of tensile strain whereas thermoelectric properties for n-type doping decreases by tensile strain. Further enhancement of tensile strain results breaking of hole valley degeneracy very slowly (ESI Fig. S5c and d†) and the thermoelectric performances for p-type carriers also vary very slowly.

In general, the valley degeneracy in 2D materials is a phenomenon which was observed under the application of strain. The strain can be compressive or tensile in nature and can be applied in one direction or in both the directions. As shown in the schematic diagram of Fig. 5a and c, the VBM and the CBM are aligned for the unstrained WS2 and hence has a direct band gap but when a compressive strain is applied on it the transition from the valence band to the conduction band can follow multiple channels crossed as shown by paths 1 and 2 in Fig. 5b. Thus increasing the n-type carriers in the conduction band. Similarly, by the application of tensile strain the number of valleys having same energy in the valence band increases as shown in Fig. 5d, thus the number of p-type carriers in the valence band increases. So, the compressive strain and the tensile strain act in such a way that in one case it increases the number of carriers in the conduction band and in other case it increases the number of carriers in the valence band due to the valley degeneracy but limited to a lower percentage of strain. At higher strain (>4%) both the electron and hole valley degeneracy are broken because the threshold beyond which the material can't come back to the original unstrained state is crossed and as a result the thermoelectric properties decrease.

The reason for the valley degeneracy can be easily visualized from the band decomposed charge density plot shown in Fig. 6. The valence band at Γ point is mainly dominated by d_{z^2} orbital of W atom and p_z orbital of S atom whereas valence band at K point is contributed mainly by two degenerate states *i.e.* W atom's $d_{x^2-y^2}$ and d_{xy} orbitals and there is negligible contribution of S atoms at this point which is clearly seen in Fig. 6a and b. Similarly, the conduction band at K point is mainly dominated by W atom's $d_{x^2-y^2}$ and d_{xy} orbitals and there is very little contribution from S atoms at this point but the conduction band at Λ point (in between Γ and Kpoints) has contribution from both W and S atoms as shown in Fig. 6c and d. So, when strain is applied the bands at *K* point remain relatively unchanged as bands at K point are mainly dominated by W atom which is sandwiched between two outer S atoms plane hence less sensitive to strain but the strain affects more on the two outer S atoms plane hence the VBM at Γ point and CBM at Λ point are more sensitive to applied strain and undergo valley degeneracy.

Carrier's mobility and relaxation time

The phonon limited hole and electron mobility have been calculated using the values of effective mass and deformation potential theory. 40 According to this theory charge carrier mobility of 2D materials can be calculated by using the relation

$$\mu^{2D} = \frac{2e\hbar^3 C_{2D}}{3K_B T |m^*|^2 E_{dp}^2}$$
 (10)

From this value of mobility, the relaxation time (τ) can be determined as $\tau = m^* \mu / e$ where $C_{\rm 2D}$ and $E_{\rm dp}$ are stretching modulus and deformation potential respectively and $m^* = \hbar^2 [\partial^2 E/\partial k^2]^{-1}$ is the effective mass of the carriers. In 2D system $C_{\rm 2D}$ can be determined by $C_{\rm 2D} = [\partial^2 E/\partial \delta^2]/S_0$ where E, δ and S_0 are total energy, amount of strain and optimized area respectively. The deformation potential $(E_{\rm dp})$ can be determined for the hole and electron by denoting the shift in VBM and CBM with respect to applied strain respectively. All the calculated parameters are summarized in Table 2. and the values are in good agreement with previous calculation for monolayer MoS₂. In modular calculation that the calculation of the modular calculation for monolayer MoS₂.

The variation of effective mass and carrier mobility with application of biaxial strain is shown in Fig. 7c and d. The effective mass and mobility do not vary much for hole as compared to that of electron with applied compressive strain but for electron there is significant change implies that compressive strain is more effective for n-type carriers. There is a sharp fluctuation at 2% compressive strain for electron because of the shifting of CBM from high symmetry K point to a point in between Γ and K point resulting a direct to indirect band gap transition at this point. As tensile strain is applied the effective mass and mobility does not vary significantly for electron but significant changes are observed for hole indicates that tensile strain is more effective for p-type carriers. Here also a very sharp fluctuation is observed at 1% of tensile strain for hole due to the shifting of VBM from high symmetry K point to Γ point results a direct to indirect band gap transition at this point. So, these fluctuations are the indication of shifting of VBM and CBM resulting direct to indirect band gap transition. When the mobility of a nanoribbon of 2D materials is calculated, the values of mobility are different for zigzag and arm chair directions. 42,43 So, we have also calculated the directional mobility of WS₂, but as we have considered only the 2×2 super cell for the calculation, the variation in the carrier mobility for electrons is not appreciable except in the biaxial strain where it has increased three times that of due to uniaxial strain.

Conclusions

In conclusion, we have performed strain dependent studies of electronic and thermoelectric properties of monolayer WS_2 by using DFT and Boltzmann transport theory. We have calculated thermoelectric properties as a function of chemical potential and carrier concentration and found that both the approaches give same output. The enhancement of the thermoelectric performances has been found with the application of compressive strain for n-type doping and that of tensile strain for p-type doping. Among all types of strains uniaxial compressive strain has been found to be most effective and highest thermoelectric PF and ZT product have been found to

be $59 \times 10^{10} \, \mathrm{W \, m^{-1} \, K^{-2} \, s^{-1}}$ and 0.72 respectively at 900 K under 4% of uniaxial compressive strain. The enhancement of thermoelectric properties is due to the degeneracy of bands near the Fermi level and can be confirmed from the band decomposed charge density contours. These results clearly indicate that WS₂ could be a very promising material for thermoelectric applications under applied compressive strain.

Conflicts of interest

There are no conflicts to declare.

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