

STRESS IN AN ELASTIC BEDROCK HUMP DUE TO GLACIER FLOW

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ABSTRACT. The stress field in an isotropic elastic hump representing a typical bedrock feature is obtained for plane strain conditions. Gravity effects are included and the applied load is a normal pressure distribution deduced from an idealized model of glacier flow. A Coulomb failure criterion is applied, including the effective stress change due to pore-water pressure, and stresses on the predicted failure planes determined for different pressure amplitudes and relative gravity contributions. The latter make little difference to the maximum "failure stress" but influence the regions where such stress levels occur. Levels of cohesive stress required to inhibit Coulomb failure are obtained, and are low in general, implying that coherent rock in the adopted hump profile, subject to the model pressure, would not fail. That is, this profile is stable unless jointing introduces an easier failure mechanism.

RÉSUMÉ. *Efforts dus à l'écoulement d'un glacier dans une protubérance élastique du lit rocheux.* Le champ des contraintes dans une protubérance isotrope représentant une caractéristique typique du lit rocheux est obtenu pour des conditions de déformation dans un plan. Les effets de la gravité sont pris en compte et la charge appliquée est une distribution normale des pressions déduites d'un modèle idéal d'écoulement glaciaire. On applique un seuil de rupture de Coulomb, en tenant compte des changements réels introduits dans les contraintes par la pression capillaire de l'eau et des efforts sur les plans de rupture probables déterminés pour différents niveaux de pression et de contribution relative de la gravité. Cette dernière change peu de la valeur de la "charge de rupture" maximum mais modifie les régions où de tels niveaux de contrainte se produisent. L'intensité des forces de cohésion nécessaires pour empêcher la rupture de Coulomb est calculée et se trouve faible en général, ce qui implique qu'un rocher cohérent dans le profil adapté pour la protubérance, soumis aux pressions du modèle, ne rompra pas. C'est-à-dire que ce profil est stable, à moins qu'une diaclase n'introduise un mécanisme de rupture plus facile.

ZUSAMMENFASSUNG. *Spannung in einem elastischen Buckel am Felsuntergrund infolge des Gletscherflusses.* Der Spannungszustand in einem isotropen, elastischen Buckel als einer typischen Erscheinung am Felsuntergrund lässt sich als ebenes Spannungsfeld beschreiben. Schwerkraftwirkungen werden berücksichtigt; die aufgebrauchte Last ist eine Normaldruckverteilung, hergeleitet aus einem idealisierten Modell des Gletscherfließens. Ein Coulomb-Bruchkriterium wird eingeführt, das die wirksame Spannungsänderung infolge des Druckes im Porenwasser berücksichtigt; die Spannungen an den vorberechneten Bruchebenen werden für verschiedene Druckamplituden und relative Schwerkraftanteile bestimmt. Die letzteren verändern die maximale "Bruchspannung" nur wenig, beeinflussen aber die Bereiche, wo solche Spannungsflächen auftreten. Es ergeben sich Flächen kohäsiver Spannung, die zur Verhinderung des Coulomb-Bruches notwendig sind; sie liegen im allgemeinen tief, woraus zu folgern ist, dass kohärenter Fels in dem angenommenen Buckelprofil, dem das Druckmodell gilt, nicht nachgeben wird. Dies bedeutet, dass das Profil stabil ist, es sei denn, Gelenkbildung würde einen leichteren Bruchmechanismus bewirken.

I. INTRODUCTION

A recent paper by Morland and Boulton (1975) presents an analytic solution and computer calculation of the stress in an isotropic elastic hump in plane strain under applied surface loads. The effects of glacier flow are modelled by assuming an idealized normal pressure distribution deduced from Nye's (1969) wavy-bed sliding theory, ignoring the restriction to small slopes. On this basis the distribution of local maximum shear stress is determined in order to predict likely failure zones, and the global maximum shear stress is obtained to compare with a failure stress of any given material. The stress field is independent of the elastic moduli of the rock. This analysis is now complemented by including the effects of gravity on the stress field, and by making a more detailed examination of the stress field in

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relation to a Coulomb failure criterion. The body-force contribution was included in an analysis of flute formation on a horizontal bed by Morris and Morland (1976), and for completeness we now incorporate an inclination of the mean bed line to the horizontal.

The Coulomb criterion is expressed as an inequality between a dimensionless failure stress S , which depends on the local stress and the friction angle ϕ , and a critical value S_c which depends only on the cohesive stress τ_0 , angle ϕ , pore-water pressure p_w and the chosen stress unit. Failure occurs when S exceeds S_c . It is found that gravity influences the location of zones where S approaches its maximum value, and hence the likely regions of failure. However the gravity contribution has no significant effect on the maximum value of S attained, at least for the chosen hump profile and model pressure distribution, so will not seriously influence the predictions of failure. Essentially, the amplitude of the model pressure distribution far exceeds the variation of body-force stress through the depth of the hump, and the gravity terms are dominated by applied surface pressures.

Since the presence of pore-water pressure reduces the effective stress in the Coulomb criterion, the effect of pore pressure up to the ice overburden pressure is considered. However, it is found that for the adopted hump profile and model pressure distribution, Coulomb failure is unlikely in coherent rock except for glaciers with very high basal sliding velocities, implying a stable hump profile under the adopted conditions. A more skew hump, and corresponding pressure distribution, may lead to higher failure stress, or a jointed rock system to different and easier modes of failure. However, a more realistic determination of the applied pressure distribution, and possible tangential traction due to glacier flow over a hump with finite slope, is required before reliable predictions can be claimed.

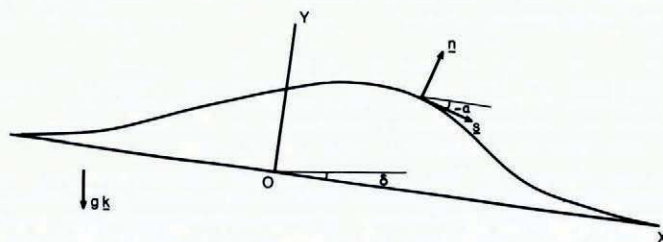


Fig. 1. A moderately skew hump on a mean bed line inclined at angle δ to the horizontal. \mathbf{n} and \mathbf{s} are unit vectors normal and tangential to the hump contour respectively. α is the local inclination of \mathbf{s} to OX . The gravity force per unit mass, $g\mathbf{k}$, acts vertically downwards.

2. STRESS FIELD IN THE ELASTIC HUMP

Consider a single plane hump on a mean bed line Ox inclined at angle δ to the horizontal (Fig. 1). The bed surface approaches Ox as $x \rightarrow \pm\infty$. Introduce dimensionless coordinates $\mathbf{X} = (X, Y)$ by

$$x = aX, \quad y = aY \quad (1)$$

so that the hump amplitude is approximately unity in (X, Y) coordinates. The moderately skew hump shown in Figure 1 has a boundary defined by $\text{Im}(\zeta) = 0$ in the conformal mapping

$$z = \zeta + \frac{0.5}{\zeta - i} + \frac{0.25}{\zeta - (0.5 + 0.5i)} \quad (2)$$

where $z = X + iY$, which is the hump used in the Morland and Boulton (1975) illustrations. Their theory and computer programme were developed for a class of rational mappings determining stress fields under conditions of zero body force and plane strain when the surface is

subjected to normal and tangential tractions t_n, t_s vanishing at infinity. If α is the local inclination of the surface tangent to Ox , then

$$\mathbf{n} = (-\sin \alpha, \cos \alpha), \quad \mathbf{s} = (\cos \alpha, \sin \alpha). \quad (3)$$

A gravity force per unit mass $g\mathbf{k}$ is now included, where

$$\mathbf{k} = (\sin \delta, -\cos \delta). \quad (4)$$

Introduce a stress unit C to normalize the applied pressure fluctuation due to the glacier flow, and let p_0 be the overburden pressure on the bed line Ox , outside the hump, under depth h of ice. Then

$$p_0 = \rho gh \cos \delta = CP_0 \quad (5)$$

where ρ is the ice density. If the stress σ is expressed in the form

$$\sigma = C(\Sigma - P_0 \mathbf{1}) \quad (6)$$

so Σ defines a dimensionless over-stress above an isotropic pressure P_0 , and assuming that there is an isotropic pressure p_0 near the bed surface outside the influence of the hump loading, Σ vanishes at the surface as $X \rightarrow \pm\infty$. Further, let

$$\Sigma = \Sigma^\circ - R(\mathbf{X} \cdot \mathbf{k})\mathbf{k} \times \mathbf{k}, \quad R = \frac{\rho_r g a}{C} \quad (7)$$

where ρ_r is the bedrock density, then Σ° is a self-equilibrating stress field (zero body-force) to which the Morland and Boulton (1975) theory applies. Note that T , and hence $(\mathbf{X} \cdot \mathbf{k})$, vanishes as $X \rightarrow \pm\infty$. If N, T are the normal and tangential tractions associated with Σ° , then

$$N = \frac{t_n}{C} + P_0 + R(\mathbf{X} \cdot \mathbf{k}) \cos^2(\alpha - \delta) \quad (8)$$

$$T = \frac{t_s}{C} + \frac{1}{2}R(\mathbf{X} \cdot \mathbf{k}) \sin(2(\alpha - \delta)) \quad (9)$$

The case of $\delta = 0$ (horizontal bed line) was used in an analysis of the formation of glacial flutes by Morris and Morland (1976).

Following Morland and Boulton (1975) a model pressure fluctuation based on Nye's (1969) theory, but ignoring the restriction to small slopes, is adopted, together with a crude cavitation approximation $t_n = 0$ whenever the predicted normal traction becomes tensile. Thus

$$\frac{t_n}{C} + P_0 = \begin{cases} -Q(X), & Q + P_0 \geq 0 \\ P_0, & Q + P_0 \leq 0 \end{cases} \quad (10)$$

where for the hump surface given by Equation (2) the pressure fluctuation is approximately

$$Q(X) = 0.29 \cos \left[\frac{\pi(x-0.3)}{2.4} \right] - 0.96 \sin \left[\frac{\pi(x-0.3)}{2.4} \right] \quad (11)$$

on $-1.87 \leq X \leq 2.93$, zero outside the range, and has amplitude unity.

$$C \approx 10\eta U/\lambda \quad \text{for } \lambda > 1 \text{ m} \quad (12)$$

where η is the ice viscosity, U is the basal sliding velocity and λ is the wavelength of the hump, approximately $4.8a$. Nye (1969) takes $\eta = 3 \times 10^{12} \text{ N s m}^{-2}$, $U = 3 \times 10^{-7} \text{ m s}^{-1}$, giving

$$C \approx (10^6 \rightarrow 10^7) \text{ N m}^{-2} \quad \text{as } \lambda \approx (10 \rightarrow 1) \text{ m}. \quad (13)$$

Note that

$$P_0 \approx \frac{10^4 h \cos \delta}{C} \approx (10^{-2} \rightarrow 10^{-3})(h/\text{m}) \quad (14)$$

for the stress unit given by Equation (13) and $\delta \ll \frac{1}{2}\pi$. Thus $P_0 < 1$ for $h < (10^2 \rightarrow 10^3)$ m and cavitation occurs under these conditions. Also a regelation layer is assumed, to provide perfect slip:

$$t_s = 0. \quad (15)$$

If $\rho_r = 3\rho \approx 3 \times 10^3 \text{ kg m}^{-3}$,

$$R \approx 7 \times 10^{-4} \lambda^2 \approx (7 \times 10^{-2} \rightarrow 7 \times 10^{-4}) \quad \text{as } \lambda \approx (10 \rightarrow 1) \text{ m}. \quad (16)$$

If R is small, Equations (7) to (9) show that gravity effects are not significant. However, since R is proportional to λ^2 and inversely proportional to U for a given hump profile, Equation (16) gives $R = O(1)$ if $\lambda = 40$ m, $U = 3 \times 10^{-7} \text{ m s}^{-1}$ or if $\lambda = 10$ m and $U = 2 \times 10^{-8} \text{ m s}^{-1}$, both practical conditions. Note that the term in R of Equation (8) increases the normal traction N associated with Σ° but has the opposite effect in the calculation of the actual overstress Σ by Equation (7). The net effect can only be determined by calculated examples. By Equations (12) and (14) P_0 is proportional to λ and inversely proportional to U . P_0 increases under the conditions which lead to an increase in R . In fact, since $a \ll h$,

$$\frac{R}{P_0} = \frac{0.6\lambda}{h \cos \delta} = O(\lambda/h) < 1 \quad (17)$$

for $\delta \ll \frac{1}{2}\pi$. Thus $R = O(1)$ implies $P_0 > 1$; that is, the pressure fluctuation is too small for cavitation and Equation (10) applies everywhere, making Σ° and Σ independent of P_0 for given R .

Consider a Coulomb failure criterion for the bedrock. Failure occurs if

$$|\tau| \geq \tau_0 - (\sigma + p_w) \tan \phi \quad (18)$$

where τ_0 is the cohesive stress, p_w the pore-water pressure, ϕ the friction angle ($0 < \phi < \frac{1}{2}\pi$) and τ , σ are the shear and normal tractions on the failure planes which have normals inclined at angles $\pm(\frac{1}{4}\pi - \frac{1}{2}\phi)$ to the maximum principal stress axis. If σ_1 , σ_2 are the local principal stresses, then Σ has the same principal axes with principal values given by

$$\sigma_1 = C(\Sigma_1 - P_0), \quad \sigma_2 = C(\Sigma_2 - P_0). \quad (19)$$

Defining a dimensionless failure stress S by

$$S = \frac{1}{2} |\Sigma_1 - \Sigma_2| \sec \phi + \frac{1}{2} (\Sigma_1 + \Sigma_2) \tan \phi \quad (20)$$

Equation (18) becomes

$$S \geq \frac{\tau_0}{C} + P_0 \left(1 - \frac{p_w}{p_0} \right) \tan \phi = S_c. \quad (21)$$

S is determined everywhere by Σ and ϕ for a given hump and boundary loading, while S_c depends only on the Coulomb parameters and the stress unit C . Failure is initiated whenever S_{\max} exceeds S_c . Pore-water pressure p_w can theoretically range from zero to p_0 when S_c takes its maximum and minimum values respectively.

$$\left. \begin{aligned} S_c &= P_0 \left(\frac{\tau_0}{p_0} + \tan \phi \right), & p_w &= 0, \\ S_c &= P_0 \frac{\tau_0}{p_0}, & p_w &= p_0. \end{aligned} \right\} \quad (22)$$

However, the permeabilities of coherent rocks are very small (Morris and Johnson, 1967). The highest values for intact rock are $\approx 5 \times 10^{-6} \text{ m s}^{-1}$ (medium-grained sandstone), $\approx 10^{-5} \text{ m s}^{-1}$ (oolitic limestone) and $\approx 10^{-6} \text{ m s}^{-1}$ (volcanic tuffs). Thus it is unlikely that S_c will be reduced to its minimum value by pore water within the voids of the coherent rock.

Of course, well-jointed rock has a secondary and much higher permeability arising from the presence of open and continuous cracks and in this case "clef water pressure" can reduce the strength of the rock significantly (Terzaghi, 1962).

By construction Σ and S_{\max} are of order unity, so failure can occur only if S_c is of order unity or less. Typical cohesive stresses are $\tau_0 = 5 \times 10^5 \text{ N m}^{-2}$ (siltstone), $(2 \rightarrow 5) \times 10^6 \text{ N m}^{-2}$ (sandstone) and 10^7 N m^{-2} (granite). For $h = 100 \text{ m}$ the respective values of τ_0/p_0 are

$$\frac{\tau_0}{p_0} = 0.5, 2 \rightarrow 5, 10, \quad h = 100 \text{ m}. \quad (23)$$

Thus, even in the case $p_w = p_0$, failure is possible only when $P_0 \leq O(2)$ for siltstone, and much smaller for the other rocks, unless $h \gg 100 \text{ m}$. The corresponding friction angles are $\phi = 30^\circ$, 35° and 45° , so for $p_w = 0$ the required factors are respectively

$$\frac{\tau_0}{p_0} + \tan \phi = 1.08, 2.7 \rightarrow 5.7, 11, \quad h = 100 \text{ m}. \quad (24)$$

We have used Nye's theory for the sliding of ice over obstacles with small surface slopes to define P_0 , the ratio of the overburden pressure to the amplitude of the pressure variation across the hump, in terms of U , η and λ . However, the restrictions on P_0 for failure to occur do not depend on the choice of sliding theory. Consideration of the overall equilibrium of the glacier indicates that it is unlikely that the amplitude of the pressure variation across a finite hump will be much greater than the overburden pressure. Thus we expect $P_0 \approx O(1)$. Nye's theory gives $P_0 = p_0 \lambda / 2\eta U$, which may take smaller values (Equation (14)). Larger h increases p_0 , and larger U decreases P_0 for given p_0 , both effects decreasing S_c .

Since the stress field cannot be influenced significantly by the gravity terms unless $R = O(1)$, which implies $P_0 > 1$ and hence $S_c > 1$, gravity will not affect failure conditions.

3. ILLUSTRATIONS

The stress fields in the elastic hump defined by Equation (2) have been calculated for various values of P_0 and R in the case $\delta = 0$. In Figure 2 the variation of S_{\max} with P_0 for $\phi = 30^\circ$ and $R = 0, 0.5, 1$ and the variation of S_c with P_0 for $\phi = 30^\circ$, $p_w = 0$ and $\tau_0/p_0 = 0, 0.5$ are compared. Failure will occur if $S_{\max} \geq S_c$. A siltstone hump under 100 m of ice ($\tau_0/p_0 = 0.5$) will fail if $P_0 \leq 0.3$ ($R = 0$), $P_0 \leq 0.45$ ($R = 0.5$) or $P_0 \leq 0.65$ ($R = 1$). The $R = 1$ curve is however not physically relevant for $P_0 \leq 1$. As h increases $\tau_0/p_0 \rightarrow 0$ and failure can occur at higher values of P_0 . The analogous curves for sandstone and granite are shown in Figures 3 and 4 respectively. In these cases also failure will only occur for low values of P_0 when $h = 100 \text{ m}$. Since from Nye's theory P_0 is inversely proportional to U and proportional to λ , for a given value of p_0 , failure is most likely for high basal sliding velocity and a small hump.

Figures 2 to 4 show that S_{\max} increases with P_0 to a level S_0 at $P_0 = 1$ and then remains constant at S_0 . Below $P_0 = 1$ the curve for $R = 0$ is not quite linear because the point of maximum stress moves from inside the hump to the surface of the down-stream flank. For $R \gtrsim 0.2$ the point of maximum stress is on the down-stream surface for all P_0 .

The failure criterion (18) holds if $P_0 \leq 1$ and

$$S_0 \geq \tan \phi + \frac{\tau_0}{p_0}. \quad (25)$$

That is, failure occurs if the cohesive stress satisfies

$$\tau_0 \leq \tau_f = 10\eta(S_0 - \tan \phi) U/\lambda \quad (26)$$

when $P_0 \leq 1$. For $P_0 \geq 1$ smaller τ_0 is required. Figure 5 shows the variation of τ_f with λ for $\phi = 30^\circ$, $p_w = 0$ and $R = 0$ (appropriate to low values of P_0). Failure will occur if

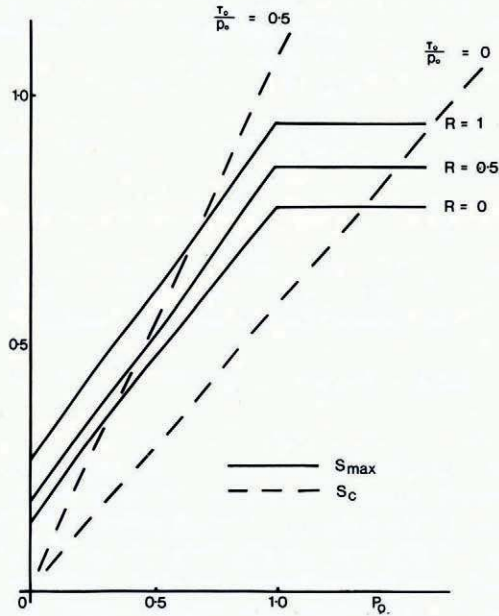


Fig. 2. S_{\max} and S_c as functions of P_0 for $\phi = 30^\circ$ and $p_w = 0$. For a siltstone hump under 100 m of ice ($\tau_0/p_0 = 0.5$) $S_{\max} > S_c$ and failure will occur when $P_0 \leq 0.3$ ($R = 0$), $P_0 \leq 0.45$ ($R = 0.5$) or $P_0 \leq 0.65$ ($R = 1$).

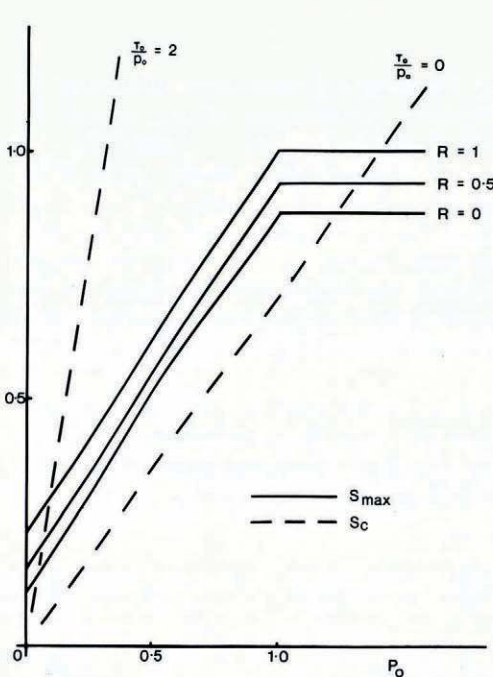


Fig. 3. S_{\max} and S_c as functions of P_0 for $\phi = 35^\circ$ and $p_w = 0$. For a sandstone hump under 100 m of ice ($\tau_0/p_0 \approx 2$) $S_{\max} > S_c$ and failure will occur when $P_0 \leq 0.04$ ($R = 0$), $P_0 \leq 0.06$ ($R = 0.5$) or $P_0 \leq 0.09$ ($R = 1$).

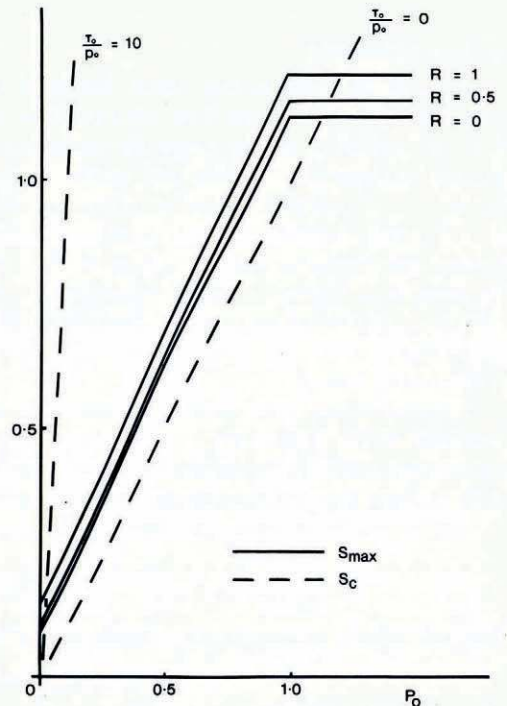


Fig. 4. S_{\max} and S_c as functions of P_0 for $\phi = 45^\circ$ and $p_w = 0$. For a granite hump under 100 m of ice ($\tau_0/p_0 \approx 10$) $S_{\max} > S_c$ and failure will occur when $P_0 \leq 0.01$ for $R \leq 1$.

$\tau_t \geq \tau_0$. Siltstone humps with $\tau_0 \approx 5 \times 10^5 \text{ N m}^{-2}$ will fail if $\lambda \leq 3 \text{ m}$ ($U = 3 \times 10^{-7} \text{ m s}^{-1}$), $\lambda \leq 12 \text{ m}$ ($U = 10^{-6} \text{ m s}^{-1}$) or $\lambda \leq 37 \text{ m}$ ($U = 3 \times 10^{-6} \text{ m s}^{-1}$). A basal sliding velocity of $U = 3 \times 10^{-6} \text{ m s}^{-1}$ is unusually fast for a normal (non-surging) temperate glacier to which the Nye theory is expected to apply. Analogous curves are shown for $\phi = 35^\circ$ in Figure 6. Sandstone humps, with a minimum τ_0 of $2 \times 10^6 \text{ N m}^{-2}$, will fail if $\lambda \leq 3 \text{ m}$ ($U = 10^{-6} \text{ m s}^{-1}$) or $\lambda \leq 10 \text{ m}$ ($U = 3 \times 10^{-6} \text{ m s}^{-1}$).

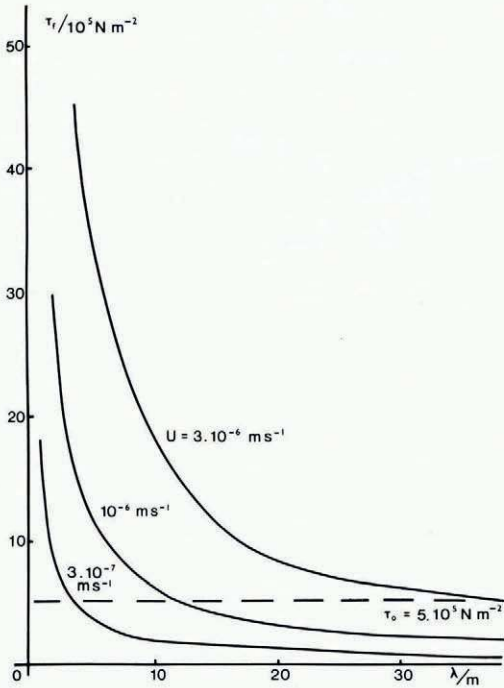


Fig. 5. τ_t as a function of λ for $\phi = 30^\circ$, $p_w = 0$ and $R = 0$. Failure occurs when $\tau_t \geq \tau_0$. Siltstone humps will fail if $\lambda \leq 3 \text{ m}$, ($U = 3 \times 10^{-7} \text{ m s}^{-1}$), $\lambda \leq 12 \text{ m}$ ($U = 10^{-6} \text{ m s}^{-1}$) or $\lambda \leq 37 \text{ m}$ ($U = 3 \times 10^{-6} \text{ m s}^{-1}$).

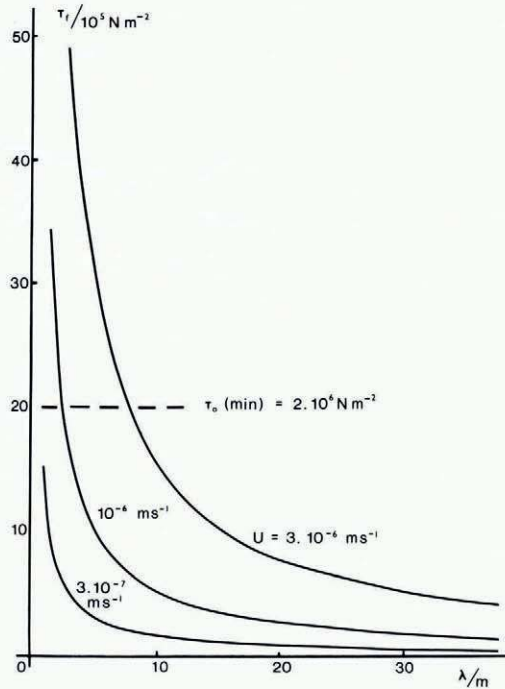


Fig. 6. τ_t as a function of λ for $\phi = 35^\circ$, $p_w = 0$ and $R = 0$. Failure occurs when $\tau_t \geq \tau_0$. Sandstone humps will fail if $\lambda \leq 3 \text{ m}$ ($U = 10^{-6} \text{ m s}^{-1}$) or $\lambda \leq 10 \text{ m}$ ($U = 3 \times 10^{-6} \text{ m s}^{-1}$).

The region of the hump where failure is most likely to occur is shown for various values of P_0 and R in Figures 7 to 10. Figure 7 shows the variation of S for $\phi = 35^\circ$, $R = 0$ and $P_0 = 0.5$. The maximum value, $S_{\max} = 0.51$, is not adjacent to the point of closure of the cavity as the previous analysis of this case (Morland and Boulton, 1975) suggested, but deep within the down-stream flank of the hump. If R is increased to 0.5, about the largest physically reasonable value if $P_0 = 0.5$, the maximum value of S increases slightly to 0.547 (Fig. 8) and is found on the down-stream surface just below the steepest portion but well up-stream of the point of closure of the cavity. Failure and subsequent removal of material in this region would tend to steepen the down-stream flank. Figure 9 shows the variation of S for $\phi = 35^\circ$, $R = 0$ and $P_0 = 1$. The maximum value of S is 0.872 and occurs on the surface just down-stream of the point where the ice exerts minimum pressure on the rock. Increasing the value of R to 1 (Fig. 10) leads to an increase in the magnitude of S_{\max} to 1.016. Its position does not change. Again any failure would tend to steepen the down-stream flank.

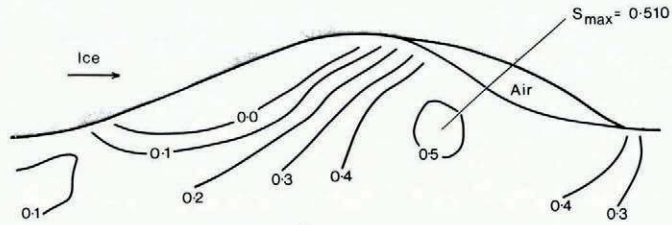


Fig. 7. The variation of S for $\phi = 35^\circ$, $R = 0$ and $P_0 = 0.5$.

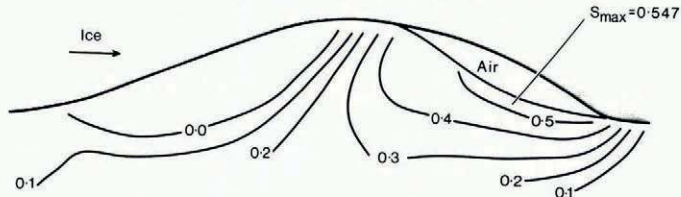


Fig. 8. The variation of S for $\phi = 35^\circ$, $R = 0.5$ and $P_0 = 0.5$.

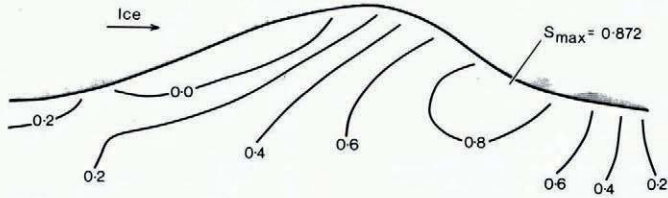


Fig. 9. The variation of S for $\phi = 35^\circ$, $R = 0$ and $P_0 = 1$.

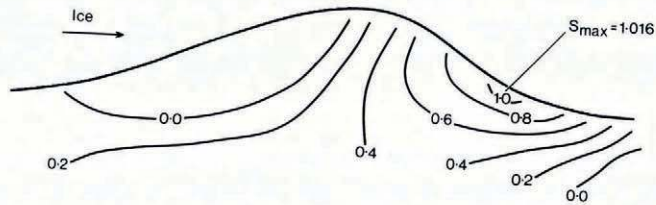


Fig. 10. The variation of S for $\phi = 35^\circ$, $R = 1$ and $P_0 = 1$.

4. CONCLUSION

We have shown that in general the force exerted by a glacier on an obstacle of a given *roche-moutonnée*-like shape will not be sufficient to produce Coulomb failure if the rock is coherent. This profile and all other less skew profiles are stable unless jointing introduces an easier failure mechanism. Thus we follow Lewis (1954) in suggesting that the typical "*roche-moutonnée*" profile of obstacles on a glacier bed, from large stream-lined boulders to valley steps, cannot develop unless the rock is already jointed.

5. ACKNOWLEDGEMENT

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