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Strong magnetophonon oscillations in extra-large graphene

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Van der Waals materials and their heterostructures offer a versatile platform for studying a variety of quantum transport phenomena due to their unique crystalline properties and the exceptional ability in tuning their electronic spectrum. However, most experiments are limited to devices that have lateral dimensions of only a few micrometres. Here, we perform magnetotransport measurements on graphene/hexagonal boron-nitride Hall bars and show that wider devices reveal additional quantum effects. In devices wider than ten micrometres we observe distinct magnetoresistance oscillations that are caused by resonant scattering of Landau-quantised Dirac electrons by acoustic phonons in graphene. The study allows us to accurately determine graphene's low energy phonon dispersion curves and shows that transverse acoustic modes cause most of phonon scattering. Our work highlights the crucial importance of device width when probing quantum effects and also demonstrates a precise, spectroscopic method for studying electron-phonon interactions in van der Waals heterostructures.

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wo-dimensional electronic systems exhibit a rich variety of quantum phenomena^{1,2}. The advent of graphene has not only provided a way to study these phenomena in the quasi-relativistic spectrum, but has also extended their experimental range^{3,4}, made some observations much clearer^{5–8} and, of course, revealed many more effects^{9–12}. These advances are mostly due to graphene's intrinsically high carrier mobility that is preserved by state-of-the-art heterostructure engineering in which graphene is encapsulated between hexagonal boron nitride layers^{13,14} and electrically tuned with atomically smooth metallic gates^{8,15}. Nonetheless, one of the first discoveries in quantum transport, well known for over 50 years^{16,17}, has remained conspicuously absent in graphene-magnetophonon oscillations^{18,19}.

In the presence of an applied magnetic field (B), electrons in pristine crystals become localised in closed orbits and their spectra take the form of quantised Landau levels (LLs) separated by energy gaps. However, an electrical current can still flow in the bulk due to carriers resonantly scattering between neighbouring orbits by the absorption or emission of phonons with energies equal to the LL spacing¹⁹ (Fig. 1a). In a semiclassical model, the resonant transitions occur between orbits which just touch in real space and induce figure of eight trajectories²⁰ (Fig. 1b), corresponding quantum mechanically to strong overlap of the tails of their wave functions in the vicinity of their classical turning point. This effect, known as magnetophonon resonance (MPR) causes magnetoresistance oscillations that are periodic in inverse magnetic field^{19,21}. Whereas magnetophonon oscillations have been used extensively for studying carrier-phonon interactions in bulk Si and Ge22, semiconducting alloys¹⁸ and heterostructures^{23–25}, there have been no reported observations in any van der Waals crystal, not even graphene, despite its exceptional electronic quality.

In this article, we consider a subtle yet crucial aspect concerning the design of electronic devices based on graphene, namely the lateral size of the conducting channel. It has so far remained small, only a few micrometres in most quantum transport experiments. Our measurements using graphene Hall bars of different widths show that wider samples start exhibiting pronounced magnetophonon oscillations.

Results

Phonon scattering in wide graphene channels. Our experiments involved magnetotransport measurements on graphene Hall bars encapsulated by hexagonal boron nitride, with particular attention paid to 'wide' devices with channel widths $W > 10 \,\mu\text{m}$. An optical image of one of our widest devices is shown in Fig. 1c (see Supplementary Note 1 for details of device fabrication). Because the electron-phonon coupling is so weak in graphene²⁶, charge carriers scatter more frequently at the device edges of micron-sized samples rather than with phonons in the bulk, especially at low temperature²⁷ (T). This is evident when comparing the Drude mean free path (L_{MFP}) for devices of different W and a fixed carrier density (n) of holes (Fig. 1d). At 5 K, all devices exhibit size-limited mobility $(L_{MFP} > W)$ because carriers propagate ballistically until they collide with the edges of the conducting channel. Even at 50 K, scattering is still dominated by the edges in most of our devices and L_{MFP} increases linearly with W. However, at these higher temperatures we find that L_{MFP} saturates around 8 µm (green line in Fig. 1d) and does not increase upon further widening of the device channel. This saturating behaviour tells us that L_{MFP} is no longer dependent on the device width and carriers scatter mostly with phonons in the bulk ($L_{MFP} < W$). In effect,



Fig. 1 Size-dependent magnetoresistance oscillations in mesoscopic graphene devices. **a** Landau level spectra of graphene. The diagram illustrates a carrier with momentum k_1 (black sphere) making a transition between Landau levels (blue and red rings) by resonant absorption of a phonon (brown arrow) with momentum $q = |\mathbf{k}_1 - \mathbf{k}_2|$ and energy $\hbar \omega_q$. Solid black arrows represent the magnitudes of wave vectors k_1 , k_2 and q. **b** The semiclassical motion of a carrier (black sphere) in real space for the resonance condition sketched in **a**. The red and blue circles which touch at a tangent point represent the initial and final semiclassical cyclotron orbits of two Landau-quantised states between which an electron is scattered by a phonon. During resonant scattering, the carriers follow a path that resembles the number 8 (figure of eight trajectory). The red and blue arrows show the motion of the charge carriers along this trajectory. The green arrow indicates direction of the applied current *l*. **c** Optical image of a graphene device with $W = 15 \,\mu$ m. The edges of the mesa are indicated by the white solid line. **d** Open circles plot experimentally determined Drude mean free path L_{MFP} as a function of *W* for two *T* and fixed $n = -2 \times 10^{12} \, \text{cm}^{-2}$. Black dashed line plots the equation $L_{MFP} = W$. Solid green line marks the phonon-limited mean free path (L_{e-ph}) at 50 K. Our measurements focussed on the valence band because our wide devices exhibited higher electronic quality for hole doping (**e**), longitudinal magnetoresistance data R_{xx} (*B*) for fixed $n = -3.3 \times 10^{12} \, \text{cm}^{-2}$ measured in our wide device (**c**) at two different *T*. The red arrows indicate peaks that are caused by magnetophonon resonance (MPR). The 50 K curve is off-set vertically for clarity. Inset: Hall resistance $R_{xy}(B)$ measured simultaneously as R_{xx} . The solid blue and dashed red lines are data measured at 5 and 50 K respectively. **f** R_{xx}/R_{xx} (B = 0T) measured at fixed

widening the channel makes our measurement more sensitive to bulk phenomena rather than edge effects.

Width-dependent magnetoresistance oscillations. The main observation of our work is presented in Fig. 1e, which plots the longitudinal resistance (R_{xx}) of a 15 µm wide Hall bar (Fig. 1c) as a function of *B*, at two *T* and fixed *n*. At 5 K we observe two distinct oscillatory features. The first, at relatively low B < 0.2 T, are the well-established semiclassical geometrical resonances that occur due to magnetic focussing of carriers between current and voltage probes⁴ (see Supplementary Note 2, Supplementary Fig. 2). At higher B (\sim 1T), quantised cyclotron orbits are formed and we observe 1/B-periodic Shubnikov de Haas (SdH) oscillations. Their origin is confirmed by noting that the charge carrier density n = $4e/(h\Delta(B^{-1}))$ extracted from the SdH period ($\Delta(B^{-1})$) agrees with that determined by Hall effect measurements (Fig. 1e, inset). At 50 K, the low-field geometric oscillations remain visible although their relative amplitudes are suppressed due to the reduced carrier mean free path. However, at higher |B| > 0.2T, an additional set of oscillations appears with five clear maxima (indicated by red arrows in Fig. 1e). These high T oscillations are also periodic in 1/Bbut are distinguished by their markedly slower period. In contrast to R_{xxy} the Hall resistance, R_{xyy} shows no oscillatory features and has the same value at both T (Fig. 1e, inset), confirming that n does not change upon warming the sample.

The observation of the high *T* oscillations depends critically on the sample width. This is shown in Fig. 1f which plots the normalised magnetoresistance, R_{xx}/R_{xx} ($_{B=0T}$), for devices with different *W* at fixed *T* and *n*. We note that the bulk channels in all our devices are intrinsically clean and free from defects (probed by ballistic transport experiments in Supplementary Note 3, Supplementary Fig. 3). Nonetheless, whereas these oscillations are well developed in the widest devices (resonances marked by purple arrows), they are poorly resolved for devices with *W* < 8 µm and completely absent in the narrowest one (*W* = 1.5 µm). As described below, we identify these size dependent, high *T* oscillations with MPR

A defining feature of magnetophonon oscillations is their unique non-monotonic temperature dependence, in which their amplitude first increases with *T* and then decays²⁵. Figure 2a shows the temperature dependence of R_{xx} (*B*) for fixed *n* between 5 and 100 K (5 K steps) for another wide Hall bar device (W = 15µm). In this sample, weak magnetophonon oscillations already appear at 5 K in the field range between the geometric and the SdH oscillations. The resonances are labelled p = 1 to 5, where the integer p refers to the number of LL spacings that are crossed during the transition; p = 1 corresponds to scattering between LLs adjacent in energy (Fig. 1a). With increasing T, the magnetophonon oscillations become more pronounced as more phonons are thermally activated, while the SdH oscillations are strongly suppressed. Although both phenomena require carriers that exhibit coherent cyclotron orbits $(\mu B > 1)$, where μ is the carrier mobility), MPR is not obscured by smearing of the Fermi-Dirac distribution across Landau gaps²⁵; rather it is enhanced due to an increased number of unoccupied states into which carriers can scatter. Hence magnetophonon oscillations persist to higher T than SdH oscillations. However, they are eventually damped at high enough T (Fig. 2b) when LLs become broadened by additional scattering ($\mu B \sim 1$). This non-monotonic behaviour is better visualised in Fig. 2c which plots the oscillatory amplitudes (ΔR_{xx}) as a function of T. Notably, the amplitude of all resonances peak at T below 60 K, corresponding to a thermal energy of a few meV.

MPR spectroscopy. For the doping levels and B-fields at which the oscillations occur, the charge carriers occupy high-index LLs $(N \sim 20 \text{ for } p = 1)$ separated by small energy gaps (~5 meV) with a classical cyclotron radius up to $R_c \sim \hbar k_F / eB \sim 300$ nm, where k_F is the Fermi-wave vector. Resonant inter-LL transitions occur due to inelastic scattering by low-energy acoustic phonons that induce figure of eight trajectories (Fig. 1b). This type of trajectory occurs with high probability because the wave functions of the initial (blue circle in Fig. 1b) and final states (red circle) have a large spatial overlap where they touch in real space²⁴. During figure of eight trajectories, the velocity of the carrier is reversed at the intersection of the two cyclotron orbits (see arrows in Fig. 1b). This process requires a phonon of specific momentum $q \approx 2k_{\rm F} \sim$ $10^9 \,\mathrm{m}^{-1}$ and energy $\hbar \omega_q (2k_{\mathrm{F}}) \sim 5 \,\mathrm{meV}$ that can back-scatter the carriers during the inter-LL transition. Energy and momentum conservation for such a process requires that $E_{N+p} - E_N = \hbar \omega_q$ $(2k_{\rm F})$, where E_N is the energy of an electron in the Nth LL, so that resonances occur at B values given by

$$B_p = \frac{nhv_s}{pev_F} \tag{1}$$

(see Supplementary Note 4 for a detailed derivation using the



Fig. 2 Temperature dependence of the magnetophonon effect. **a** Magnetoresistance R_{xx} (*B*) for *T* between 5 K (blue curve) and 100 K (black curve) in 5 K steps for fixed *n* measured in another Hall bar with $W = 15 \mu$ m. **b** Extended data set of **a** showing high *T* behaviour (10 K steps). **c** Temperature dependence of the amplitude of MPR peaks, ΔR_{xx} (*T*), indicated in **a** by colour coded letters, p = 1-5



Fig. 3 Density dependence of magnetophonon oscillations. **a** Longitudinal resistance R_{xx} (grey scale map) as a function of *n* and *B* measured at 5 K (W = 15 µm). Logarithmic grey scale: white: 1 Ω to black: 15 Ω . The blue dashed lines trace Landau gaps corresponding to high filling factors $\nu = nh/Be$. **b** Same as **a** measured at 50 K. Logarithmic grey scale: white: 5.5 Ω to black: 18 Ω . The red dashed lines plot Eq. (1) for p = 1 to 4 which corresponds to carriers scattering with transitions across 1 to 4 Landau level spacings. Features appearing for B < 0.2 T are the semiclassical geometrical oscillations⁴ not relevant in this work (see Supplementary Note 2 for details)

semiclassical model). Here, $v_{\rm F}$ and $v_{\rm s}$ are the Fermi velocity and low-energy acoustic phonon velocity in graphene respectively. This resonant condition is unique to massless Dirac electrons and is strikingly different to the case of massive electrons in a conventional two-dimensional electron gas (2DEG) system²⁴ where $B_{\rm p}$ scales with $n^{0.5}$. On resonance, inelastic scattering between neighbouring orbits (Fig. 1b) gives rise to a finite and dissipative current in the bulk. This behaviour causes maxima in ρ_{xx} at B_p ; the 1/B periodicity results in oscillations described by $\Delta \rho_{xx} \sim e^{-\gamma/2}$ ${}^{B}\cos(2\pi B_{\rm F}/B)$ where $B_{\rm F} \equiv pB_{\rm p}$ and the factor γ depends on temperature²⁸. Equation (1) predicts that the position of maxima scales linearly with n. With this in mind, Fig. 3a, b plot maps of R_{xx} (n, B) for one of our 15 µm devices at 5 K (Fig. 3a) and 50 K (Fig. 3b). In addition to the typical Landau fan structure that is dominant at low T (filling factors, v, are marked by blue dashed lines), the maps reveal a broader set of fans at lower B that are more prominent at 50 K (Fig. 3b). They are caused by MPR (p values are labelled in red) and demonstrate that their frequency scales linearly with n. Furthermore, the positions of MPR peaks in Fig. 3b can be fitted precisely by Eq. (1) (red dashed lines) with a constant $v_{\rm s}/v_{\rm F} = 0.0128$. By studying the temperature dependence of SdH oscillations in our graphene devices (Supplementary Note 5, Supplementary Fig. 4), we extract $v_{\rm F}$ and determine $v_{\rm s}$ accordingly. We note that $v_{\rm F}$ shows no significant dependence on *n*, as expected for graphene devices on hexagonal boron nitride at high doping²⁹, because e-e interactions that cause velocity renormalisation³⁰ are heavily screened. Hence, using the extracted $v_{\rm F} = 1.06 + 0.05 \times 10^6 \, {\rm ms}^{-1}$, we determined a phonon velocity, $v_s = 13.6 + 0.7 \text{ km s}^{-1}$. This value is close to the speed of transverse acoustic (TA) phonons in graphene ($\sim 13 \text{ km s}^{-1}$) calculated in numerous theoretical works³¹⁻³⁵. Therefore, we infer our oscillations arise from inter-LL scattering by low energy and linearly dispersed TA phonons.

Equation (1) is generic for linearly dispersed phonons in graphene. This motivated us to search for MPR arising from longitudinal acoustic (LA) phonons, which should occur at higher *B* due to their significantly higher $v_s^{34,35}$. Careful inspection of the data in Figs. 1 and 2 shows that the p = 1 resonance for TA phonons is followed by a weak shoulder-like feature at higher *B*. We therefore studied a dual-gated graphene device (Supplementary Fig. 1) that permitted measurements at higher $n \sim -1 \times 10^{13}$ cm⁻² which, according to Eq. (1), should better separate this

feature from the TA resonances. Figure 4a plots R_{xx} (*B*) for this device for several *n*. Measurements at these high *n* reveals that the shoulder-like feature develops into a well-defined peak (indicated by coloured arrows). Its position $(B_{p=1})$ is accurately described by Eq. (1) with a constant $v_s/v_F = 0.0198$. Using the experimentally extracted value of v_F , we obtained $v_s = 21.0 + 1.0 \text{ km s}^{-1}$. This value is indeed close to that calculated for LA phonons in graphene^{31,34,35}, and hence we attribute this feature to inter-LL scattering by LA phonons.

Further validation of our model is presented in Fig. 4b, which plots the magnetophonon oscillation frequency for TA phonons $(B_{\rm F} \equiv pB_{\rm p})$ as a function of *n* for several different devices (red symbols). It shows that a linear dependence (red line) fits the data to Eq. (1) for all our measured devices over a range of *n* spanning an order of magnitude. The weaker LA resonance was also found to occur at the same $B_{p=1} = B_F$ in different devices (blue symbols). Furthermore, the data in Fig. 4b can be transformed directly into phonon dispersion curves (inset of Fig. 4b) by noting that $q \approx 2k_{\rm F} = 2(n\pi)^{0.5}$ and $\hbar\omega_q \approx (2eB_{\rm F}v_{\rm s}v_{\rm F}\hbar)^{0.5}$. The extended tunability of the carrier density in our dual-gated devices allows measurement of phonon branches up to wave vectors $>10^9$ m⁻¹. Note that these dispersion plots are significantly more precise than those measured by X-ray scattering experiments in graphite³⁶ (purple stars). Studies of magnetophonon oscillations thus enable an all-electrical measurement of the intrinsic phonon dispersion curves in gate-tuneable materials.

Discussion

To understand why magnetophonon oscillations are absent in narrow samples, we first note that figure of eight trajectories (Fig. 1b) have a spatial extent ~4 R_c , which can reach values of several microns for the high-order resonances (p > 3). If the sample is too narrow, so that $4R_c$ is comparable to W, the carrier trajectories are skewed by elastic scattering at the device edges. In this case, they propagate along the edges of the device in skipping orbits², effectively short-circuiting the resistive behaviour of the bulk caused by MPR. However, if $W > 4R_c$, both MPR and skipping orbits contribute to R_{xx} . We can estimate the width of the device required to observe MPR by comparing the relative contributions of these two processes. Carriers that diffuse in MPR-induced figure of eight trajectories move a distance $2R_c$ in a characteristic time, $\tau_{e-ph} = L_{e-ph}/v_F$ with a drift velocity $v_{MPR} =$



Fig. 4 Phonon spectroscopy in graphene by measurement of magnetophonon oscillations. **a** Longitudinal resistance R_{xx} as a function of *B* measured for several high *n* of holes in our wide ($W = 13.8 \,\mu$ m) dual-gated graphene Hall bar. The curves have been off-set vertically for clarity. **b** Red symbols plot the fundamental frequency $B_F \equiv pB_p$ of magnetophonon oscillations as a function of absolute *n* for three different devices; open circles correspond to the dual-gated device which allowed high doping. The blue symbols mark the positions $B_{p=1}$ of the broad peak (indicated by coloured arrows in **a**) which appears clearly at high *n*. The red and blue solid lines represents Eq. (1) with $v_s/v_F = 0.0128$ and 0.0198 respectively. Knowing v_F (Supplementary Note 5) we extract the TA (v_{TA}) and LA (v_{LA}) phonon velocities. Inset: Data in main panel transformed to phonon dispersion curves. Coloured squares—experimental data points (error bars reflect the error in the experimentally extracted v_F), solid lines plot the equation $\hbar \omega_q = \hbar v_s q$ (same v_s as in the main panel), purple stars—data taken from ref. ³⁶. **c** Calculation of the oscillatory part of the resistivity $\Delta \rho_{xx}(\Omega)$ using the Kubo formula (see Supplementary Note 6 for details)

 $2R_c/\tau_{eph}$. This is significantly slower than skipping orbits which can have speeds approaching $v_{\rm F}$. On the other hand, skipping orbits occupy only a width $\sim R_{\rm c}$ at each edge, whereas MPR occurs approximately over the full width, W, of the bulk. By comparing these two contributions, we deduce that MPR dominates when $Wv_{\rm MPR} \gtrsim 2R_cv_{\rm F}$. This corresponds to the condition $W \gtrsim L_{\rm e-ph}$, in good agreement with the measured data in Fig. 1d, f.

Our measurements provide an important insight into the intrinsic electron-phonon interaction in graphene: namely, the dominance of carrier scattering by low-energy TA phonons. This is in agreement with several theoretical works^{35,37,38} and contrasts with a widely held view that deformation potential scattering by LA phonons prevails over TA phonons³⁹. To investigate this point further, we calculated magnetoresistance using the Kubo formula⁴⁰ (Supplementary Note 6). A typical calculation is shown in Fig. 4c, which plots the contribution $(\Delta \rho_{xx})$ of MPR for TA and LA phonon velocities of $v_s = 13.6$ and 21.4 km s⁻¹, respectively³⁵, and the Fermi velocity⁴¹ $v_F = 1 \times 10^6$ m s⁻¹. It accurately describes the oscillatory form of the measured data. Such good agreement is only possible when our calculations include the effect of carrier screening^{35,38,42,43} which significantly reduces the electron-LA phonon deformation potential coupling. Without screening, LA phonons would dominate the observed MPR (Supplementary Fig. 5). Our results therefore highlight the importance of carrier screening on electron-phonon interactions and thus helps resolve a long-standing discussion of the relative importance of LA^{39,44} and TA^{37,38,43} phonon scattering in graphene.

To conclude, we report the observation of pronounced magnetophonon oscillations in graphene, where the Dirac spectrum strongly modifies the resonant condition compared to previously studied electronic systems. Other two-dimensional crystals can also be expected to exhibit this phenomenon. The oscillations enable the study of low-energy acoustic phonon modes that are generally inaccessible by Raman spectroscopy^{45,46}. Our measurements combined with the Kubo calculations provide strong evidence that TA phonons limit temperature-dependent mobility in graphene^{35,37,38}. Most importantly, graphene's transport properties are shown to strongly depend on device size, even for conducting channels as wide as several microns. This should motivate further experiments on graphene and related twodimensional materials in a macroscopic regime beyond the scope of previous mesoscopic devices.

Methods

Quantum transport measurements. For measuring resistance in our graphene devices, we used standard low-frequency AC measurement techniques with a lockin amplifier at 10–30 Hz. The measurements of $R_{xx}(\Omega) = V_{xx}I_{xx}$ are obtained by driving a small AC excitation current ($I_{xx} = 0.1-1 \mu$ A) down the length of the Hall bar while simultaneously measuring the four probe voltage drop (V_{xx}) between two side contacts located on the edge of the Hall bar devices (Fig. 1c). We tune the Fermi level in our graphene devices by applying a DC voltage between the silicon substrate and the graphene channel, where the SiO₂ and bottom hexagonal boron nitride encapsulation layer serve as the dielectric (see Supplementary Note 1 for details on device fabrication). In our top gated device (see Supplementary Fig. 1), we simultaneously apply a potential to the metal top gate which allowed us to reach higher doping levels (see Fig. 4). All measurements were performed inside a variable temperature-inset of a wet helium-4 flow cryostat that allowed us to carry out temperature-dependent magnetotransport measurements using a cold super-conducting magnet.

Data Availability

The data that support plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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Author contributions

A.K.G., L.E., R.K.K. and P.K designed and supervised the project. P.K., D.P. and J.B. fabricated the studied devices. High-quality hexagonal boron-nitride crystals were provided by S.L. and J.H.E. Electrical transport measurements were performed by R.K.K., A.B. and J.W. Theoretical support and quantum calculations were carried out by M.T.G. and L.E. Data analysis was carried out by R.K.K., P.K., M.T.G., L.E. and A.K.G. The manuscript was written by R.K.K., L.E., P.K., M.T.G. and A.K.G. All authors contributed to discussion of the experimental data.

Additional information

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