

Structure of Herbig AeBe disks at the milliarcsecond scale

A statistical survey in the H band using PIONIER-VLTI[★]

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Received 13 July 2016 / Accepted 4 November 2016

ABSTRACT

Context. It is now generally accepted that the near-infrared excess of Herbig AeBe stars originates in the dust of a circumstellar disk.
Aims. The aims of this article are to infer the radial and vertical structure of these disks at scales of order 1 au, and the properties of the dust grains.

Methods. The program objects (51 in total) were observed with the H -band (1.6 μm) PIONIER/VLTI interferometer. The largest baselines allowed us to resolve (at least partially) structures of a few tenths of an au at typical distances of a few hundred parsecs. Dedicated *UBVR_IJHK* photometric measurements were also obtained. Spectral and 2D geometrical parameters are extracted via fits of a few simple models: ellipsoids and broadened rings with azimuthal modulation. Model bias is mitigated by parallel fits of physical disk models. Sample statistics were evaluated against similar statistics for the physical disk models to infer properties of the sample objects as a group.

Results. We find that dust at the inner rim of the disk has a sublimation temperature $T_{\text{sub}} \approx 1800$ K. A ring morphology is confirmed for approximately half the resolved objects; these rings are wide $\delta r/r \geq 0.5$. A wide ring favors a rim that, on the star-facing side, looks more like a knife edge than a doughnut. The data are also compatible with the combination of a narrow ring and an inner disk of unspecified nature inside the dust sublimation radius. The disk inner part has a thickness $z/r \approx 0.2$, flaring to $z/r \approx 0.5$ in the outer part. We confirm the known luminosity-radius relation; a simple physical model is consistent with both the mean luminosity-radius relation and the ring relative width; however, a significant spread around the mean relation is present. In some of the objects we find a halo component, fully resolved at the shortest interferometer spacing, that is related to the HAeBe class.

Key words. circumstellar matter – stars: variables: T Tauri, Herbig Ae/Be – stars: pre-main sequence – techniques: interferometric – techniques: photometric

* Full Tables B1–B3, as well as results of other parametric fits, are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/599/A85>
The calibrated interferometric data can be found as FITS format files at <http://oidb.jmmc.fr/collection.html?id=HAeBeLP>

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1. Introduction

Herbig Ae Be stars are intermediate-mass (2–8 M_{\odot}) pre-main sequence stars. They are surrounded by accretion disks that are believed to be the birth places of planetary systems. The remarkable diversity of discovered exo-planetary systems has renewed the strong interest in understanding the structure of such disks at

the astronomical unit (au) scale. The sublimation front at the inner rim contributes to define the physical conditions in the dusty planet-forming region.

Hillenbrand et al. (1992), Lada & Adams (1992) have recognized that the spectral energy distributions (SED) of Herbig Ae Be stars display near-infrared excesses in the 2–7 μm region that are too strong to be reproduced with the flaring hydrostatic disk models that are successfully applied to T Tauri stars (see e.g., Kenyon & Hartmann 1987; Chiang & Goldreich 1997). The initial proposition by Hillenbrand et al. (1992) that accretion heating could provide the near infra-red (NIR) excess flux can be ruled out on the arguments that, firstly, such accretion rates are not measured and secondly, they are incompatible with the presence of an optically thin inner cavity (Hartmann et al. 1993).

The first survey of Herbig Ae/Be stars using near-infrared optical interferometry by Millan-Gabet et al. (2001) concluded that the near-infrared emission size was indeed incompatible with the standard flared disk models. In order to explain both interferometric and photometric measurements Natta et al. (2001) have proposed that the rim vertical structure had to be taken into account in the global stellar energy reprocessing balance. Such a rim is frontally illuminated and therefore naturally hotter. It should emit at the dust sublimation temperature and puff up (Dullemond et al. 2001). Aperture-masking observations of a massive young star by Tuthill et al. (2001) revealed a doughnut shape NIR emission and offered a first confirmation of this idea. Monnier & Millan-Gabet (2002), Monnier et al. (2005) assembled the available interferometric data to confirm that the measured sizes were well correlated with the central stars' luminosities and consistent with the dust sublimation radius. This trend was observed over more than four decades of stellar luminosity. The advent of spectrally-resolved interferometry has further revealed the presence of an additional hot component emitting from within the sublimation radius in a significant sample of objects (Malbet et al. 2007; Tatulli et al. 2007; Kraus et al. 2008b,a; Isella et al. 2008; Tannirkulam et al. 2008b; Eisner et al. 2009, 2014).

Several teams have proposed alternative explanations for the 2–7 μm excess: an extended (spherical) envelope (Hartmann et al. 1993; Vinković et al. 2006), disk wind (Vinković & Jurkić 2007; Bans & Königl 2012), magnetically lifted grains (Ke et al. 2012), and supported disk atmosphere (Turner et al. 2014).

The availability of spatially resolved observations of the inner rims has prompted research on the processes that might structure them. Isella & Natta (2005) have shown that the dependence of dust sublimation temperature on gas density causes the sublimation front to be curved. Tannirkulam et al. (2007) pointed out that the dependence on grain size of cooling efficiency and dust settling results in a broader NIR emission region. Kama et al. (2009) and Flock et al. (2016), taking into account the pressure dependence of the sublimation temperature, but not grain settling, find rim profiles similar to Tannirkulam et al. (2007), that is, a wedge pointing to the star. Vinković (2014) addressed the issue of the thickness of the rim; considering a comprehensive list of processes such as viscous heating, accretion luminosity, turbulent diffusion, dust settling, gas pressure, he concluded that the resulting inner rim thickness was too small to explain the infrared excess. The reader is referred to Dullemond & Monnier (2010) or Kraus (2015) for reviews of the structure of the inner circumstellar disks.

The goal of this article is to provide a statistical view of the milli-arcsecond morphology of the near-infrared emission around Herbig Ae/Be stars. For that purpose, we took advantage

of the improved performance offered by the visitor instrument PIONIER (sensitivity, precision and efficiency) at the Very Large Telescope Interferometer (VLTI). We established a Large Program (090C-0963) that had the following questions in mind:

1. Can we constrain the radial and vertical structure of the inner disk?
2. Can we constrain the rim dust temperature and composition?
3. Can we constrain the presence of additional emitting structures (e.g., hot inner emission, envelopes)?
4. Can we reveal deviations from axisymmetry in the emission that could be linked to radiative transfer effects?

This article is organized as follows. Section 2 introduces the sample and the immediate data reduction, that produces calibrated data. In Sect. 3, we submit the observed data to simple model fits, in a systematic and uniform way, condensing hundreds of visibilities and phase closures into a dozen or fewer parameters for each object. In Sect. 4 we use the processed data to infer some of the physical properties of the sample objects, striving to avoid possible biases. In the conclusion, we wrap up our main findings, place them into perspective with current models, and consider the outlook for follow-up work.

2. Observations

2.1. Instruments

The interferometric observations were made using the four 1.8 m auxiliary telescopes (AT) of the VLTI (see Mérand et al. 2014) at ESO's Paranal observatory, and the PIONIER instrument (Le Bouquin et al. 2011), a four-telescope recombiner operating in *H*-band (1.55–1.80 μm). The three AT configurations available at the epoch of the observations provided horizontal baselines in the range 11–140 m. The photometric observations were obtained with two telescopes at the South African Astronomical Observatory (SAAO) Sutherland Observatory: 0.50 m for *UB-VRI* bands, and 0.75 m for *JHK* bands.

2.2. Sample

Our sample is based on the lists of Malfait et al. (1998), Thé et al. (1994), and Vieira et al. (2003). One should note that a) the definition of HAeBe objects does not rest on quantitative criteria; b) our list of targets does not meet any completeness criterion. Our sample is limited at $m_H \lesssim 8$, where the fainter objects are intended to test the sensitivity limit of PIONIER/VLTI. The program objects are listed in Table 1.

Spectral types. They were obtained from the SIMBAD database and checked against the Catalog of Stellar Spectral Classifications (Skiff, 2009–2016)¹; in case of discrepancy, we used a recent measurement from the compilation of Skiff, and we quote the original reference. When available, we adopted the determination by Fairlamb et al. (2015), that also includes determinations of bolometric luminosity (the values of T_{eff} were converted to spectral types using the tables of Pecaut & Mamajek 2013). Statistics of *H* magnitude and spectral types are shown Fig. 1.

Distances. Parallaxic distances were obtained from the *Gaia* (Lindgren et al. 2016) and HIPPARCOS (Perryman et al. 1997)

¹ <http://vizier.u-strasbg.fr/viz-bin/Cat?B/mk>

Table 1. List of objects in the present survey.

Object	RA (2000)	Dec (2000)	Spectral type		Distance			HAeBe Status		nHQ	Bin
			Value	Ref.	Value	\pm	Ref.	Ref.	Group		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
HD 17081	02 44 07.35	-13 51 31.3	B7		135	16	Hi	M98	Ia	Ur	
AB AUR	04 55 45.85	+30 33 04.3	A0		153	10	Ga	M98			
HD 31648	04 58 46.27	+29 50 37.0	A5		142	7	Ga	M98	IIa	Sc	
HD 293782	05 04 29.99	-03 47 14.3	A3	F15	346	34	Ga	T94		Bb	
HD 34282	05 16 00.48	-09 48 35.4	A0	F15	325	31	Ga	M98	Ib	Bb	
CO ORI	05 27 38.34	+11 25 39.0	F7		435	93	Ga	(u)		Bb,Sc	
HD 35929	05 27 42.79	-08 19 38.4	F1	F15	385	38	Ga	M98	IIa	Ur	
MWC 758	05 30 27.53	+25 19 57.1	A5	S06	151	9	Ga	M98	Ia	Sc,Ur	
HD 244604	05 31 57.25	+11 17 41.5	A2	F15	433	64	Ga	M98	IIa	Bb	
HD 36917	05 34 46.98	-05 34 14.6	B9		495	64	Ga	M98	IIb	Ur	
T ORI	05 35 50.44	-05 28 34.9	A2	F15	750	141	F15	T94			E
HD 37258	05 36 59.25	-06 09 16.4	A0	F15	424	23	F15	M98	IIa	Bb	
HD 37357	05 37 47.08	-06 42 30.3	A0	F15	344	10	F15	M98	IIa	Bb	2FP
V 1247 ORI	05 38 05.25	-01 15 21.7	A7	F15	319	27	Ga	V03		Bb	
HD 37411	05 38 14.51	-05 25 13.3	A0	F15	358	108	F15	M98	IIb	Bb	
HD 37806	05 41 02.29	-02 43 00.7	A1	G98	420	49	Ga	M98	IIa		
HD 38087	05 43 00.57	-02 18 45.4	B3		199	75	Hi	M98			VHA
HD 39014	05 44 46.38	-65 44 07.9	A7		44	1	Hi	M98		Ur	
HD 250550	06 01 59.99	+16 30 56.7	B9	F15	637	154	Ga	T94	Ia	Bb	
HD 45677	06 28 17.42	-13 03 11.1	B2		610	123	Ga	T94			
HD 259431	06 33 05.19	+10 19 20.0	B6		610	115	Ga	T94	Ia		
MWC 158	06 51 33.40	-06 57 59.5	B8	G98	340	47	Ga	M98	IIa		
HD 53367	07 04 25.53	-10 27 15.7	B0.5	F15	247	82	Hi	T94			SB1
HD 56895	07 18 31.79	-11 11 33.9	F0		167	8	Ga	M98		Ur	
HD 58647	07 25 56.10	-14 10 43.6	B9		292	38	Ga	M98	IIa		
HD 85567	09 50 28.54	-60 58 03.0	B8	F15	907	164	F15	M98	IIa		
HD 95881	11 01 57.62	-71 30 48.4	B9.5	F15	935	227	Ga	M98	IIa		
HD 97048	11 08 03.32	-77 39 17.5	B9.5	F15	179	8	Ga	T94	Ib		
HD 98922	11 22 31.67	-53 22 11.5	B9.5	F15	649	156	Ga	M98	IIa		
HD 100453	11 33 05.58	-54 19 28.5	F0	F15	103	3	Ga	M98	Ib		
HD 100546	11 33 25.44	-70 11 41.2	A0	F15	109	4	Ga	M98	Ia		
HD 104237	12 00 05.08	-78 11 34.6	A6	F15	104	3	Ga	M98	IIa		SB2
HD 139614	15 40 46.38	-42 29 53.5	A7	F15	131	5	Ga	M98	Ia		
HD 141569	15 49 57.75	-03 55 16.3	A0	F15	111	5	Ga	M98	IIb	Sc, Ur	
HD 142666	15 56 40.02	-22 01 40.0	A8	F15	150	5	Ga	T94	IIa		
HD 142527	15 56 41.89	-42 19 23.3	F5	F15	156	6	Ga	M98	Ia		
HD 143006	15 58 36.91	-22 57 15.3	G8		166	10	Ga	M98			
HD 144432	16 06 57.95	-27 43 09.8	A8	F15	253	95	Hi	M98			
HD 144668	16 08 34.29	-39 06 18.3	A3	F15	208	38	Hi	M98	IIa		
HD 145718	16 13 11.59	-22 29 06.7	A6	F15	149	6	Ga	V03			
HD 149914	16 38 28.65	-18 13 13.7	B9.5		149	13	Ga	M98		Ur	
HD 150193	16 40 17.92	-23 53 45.2	A2	F15	145	6	Ga	M98	IIa		
AK SCO	16 54 44.85	-36 53 18.6	F7	F15	143	5	Ga	T94			SB2
HD 158643	17 31 24.95	-23 57 45.5	A0		131	15	Hi	M98			
HD 163296	17 56 21.29	-21 57 21.9	A1	F15	117	4	Ga	M98	IIa		
HD 169142	18 24 29.78	-29 46 49.4	F1	M15	145	43	V05	M98	Ib		
MWC 297	18 27 39.53	-03 49 52.1	B1.5	F15	170	34	F15	T94			
VV SER	18 28 47.87	+00 08 39.8	B6	H04; M09	330		A04	T94	IIa		
R CRA	19 01 53.66	-36 57 07.9	B5		130		A04	T94			
HD 179218	19 11 11.25	+15 47 15.6	A0		293	31	Ga	M98	Ia	Or	
HD 190073	20 03 02.51	+05 44 16.7	A2		855	351	Ga	M98	IIa		

Notes. Columns: (5) spectral type from Simbad except as noted; (9) reference establishing that object belongs to HAeBe type; (10) group following Juhász et al. (2010); (11) cause of exclusion from HQ sub-sample *Ur* unresolved (i.e. all $V^2 \geq 0.8$); *Sc*, only one baseline configuration; *Bb*, only in broadband mode; *Or*, over-resolved; (12) evidence for binarity: E, eclipsing; 2FP, double fringe packet; VHA, rapid variation of V^2 versus HA; SB1, SB2, usual meaning.

References. F15: Fairlamb et al. (2015); S06: Suárez et al. (2006); G98: Gray & Corbally (1998); H04: Hernández et al. (2004); M09: Montesinos et al. (2009); Hi (HIPPARCOS): Perryman et al. (1997); Ga (*Gaia*): Lindegren et al. (2016); V05: van Boekel et al. (2005); A04: Acke & van den Ancker (2004); M98: Malfait et al. (1998); T94: Thé et al. (1994); V03: Vieira et al. (2003); (u) uncertain, see for example, Yang et al. (2012), Calvet et al. (2004), Eiroa et al. (2002).

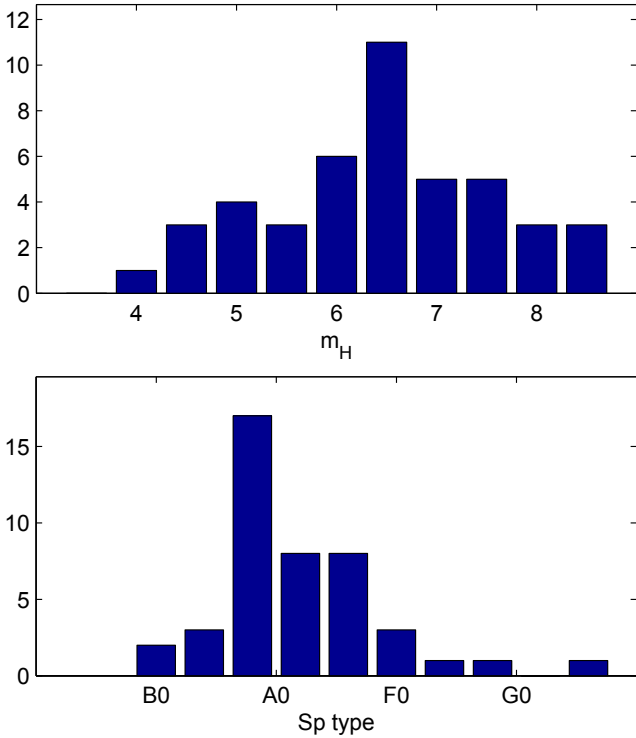


Fig. 1. Statistics of H magnitudes (*top*) of program objects and their spectral types (*bottom*).

catalogs, and, failing that, from detailed spectroscopic studies; see notes of Table 1.

Binarity. For T Ori see [Shevchenko & Vitrichenko \(1994\)](#); for HD 53367 see [Pogodin et al. \(2006\)](#); for HD 104237 see [Cowley et al. \(2013\)](#); for AK Sco see [Andersen et al. \(1989\)](#); concerning VV Ser, [Eisner et al. \(2004\)](#) mention that their data do not rule out a binary model; binarity is not supported by our (more extensive) data. HD 36917 is often quoted as SB2, referring to [Levato & Abt \(1976\)](#), who actually mention a composite spectrum, which is not confirmed by [Alecian et al. \(2013\)](#). HD 145718 is listed by Simbad as an Algol binary. However, following [Guimarães et al. \(2006\)](#) and references therein, this remains unconfirmed.

Coordinates of HD 56895. We provide the following information for the record, and to avoid others a similar mistake. We list in Table 2 the coordinates for HD 56895 or HD 56895B from various sources. It appears that the object listed by [Malfait et al. \(1998\)](#) as HD 56895B has the coordinates (within a couple of arcsec) and the V magnitude of HD 56895, while its NIR magnitudes are those of a nearby (13'') object with much redder colors. Our interferometric observations were made at the position of HD 56895, not what was intended. As a consequence, this object is not included in the data analysis.

2.3. Interferometric data

The interferometric data were acquired with the PIONIER instrument at the VLTI, during a total of 30 nights in six observing runs between December 2012 and June 2013, under Large Program 190.C-0963. The log of observations is given in Appendix C.

We used all the available configurations offered by the ATs: A1–B2–C1–D0, D0–G1–H0–I1, A1–G1–J3–K0. Most of the data were dispersed over three spectral channels across the H band, providing a spectral resolving power of $\mathcal{R} \approx 15$, while the faintest objects were observed in broad H -band ($\mathcal{R} \approx 5$).

Data were reduced and calibrated with the `pndrs` package described in [Le Bouquin et al. \(2011\)](#). Each observation block (OB) provides five consecutive files within a few minutes. Each file contains six visibilities squared V^2 and four closure phases ϕ_{cp} dispersed over the three spectral channels. Whenever possible, the five files were averaged together to reduce the final amount of data to be analyzed and to increase the signal-to-noise ratio. The statistical uncertainties typically range from 0.5° to 10° for the closure phases and from 2.5% to 20% for the visibilities squared, depending on target brightness and atmospheric conditions.

Each observation sequence of one of our targets was immediately preceded and followed by the observation of a calibration star in order to master the instrumental and atmospheric response. [Le Bouquin et al. \(2012\)](#) have shown that such calibration star(s) should be chosen close to the science object both in terms of position (within a few degrees) and magnitude (within ± 1.5 mag). We used the tool `SearchCal`² in its FAINT mode ([Bonneau et al. 2011](#)) to identify at least one suitable calibration star within a radius of 3 deg of each object of our sample.

Most of our objects are grouped into clusters in the sky. Consequently, the instrumental response could be cross-checked between various calibration stars. This allowed us to discover a few previously unknown binaries among the calibration stars. These have been reported to the bad calibrator list³. We estimated the typical calibration accuracy to be 1.5° for the phase closures and 5% for the visibilities squared. The typical accuracy of the effective wavelength of the PIONIER channels is 2%. Finally, the on-the-sky orientation of PIONIER has been checked several times and is consistent with the definition of [Pauls et al. \(2005\)](#).

2.4. Photometry

We made dedicated photometric measurements of most objects in our study, in the $UBVRIJHK$ bands, at the SAAO Sutherland 0.5 m and 0.75 m telescopes (now decommissioned); the time parallax relative to the interferometric observations is smaller (at most two years) than for photometry available in the literature. Whenever SAAO measurements could not be made, previous measurements from the literature were used with weighting following their error estimates; see Tables 3 and 4. The NOMAD catalog is not a primary source, and was used only for B and V magnitudes of MWC 297 and VV Ser from the unpublished USNO YB6 catalog. The Wise measurements are used only for plotting on SED graphs.

3. Data processing

In this section, we present steps of intermediate data processing, from reduced and calibrated data (magnitudes, visibilities, phase closures) to meaningful derived parameters. The first subsection below deals with model fits of photometric data, while the remaining subsections deal with model fitting of interferometric data.

² <http://www.jmmc.fr/searchcal>

³ <http://apps.jmmc.fr/badcal>

Table 2. Coordinates for HD 56895 (B) from various literature sources.

Catalog	Name	RA (2000)	Dec (2000)	<i>V</i>	<i>J</i>	<i>H</i>	<i>K</i>
Simbad	HD 56895	07 18 31.792	−11 11 33.92	8.42			
Simbad	MC79 2-5	07 18 30.979	−11 11 40.73	10.5			
2MASS	HD 56895	07 18 31.799	−11 11 33.90		7.632	7.526	7.427
2MASS	07183097-1111407	07 18 30.979	−11 11 40.73		6.465	5.049	4.171
Malfait+1998	HD 56895B	07 18 31.82	−11 11 34.8	8.40	6.12	4.56	3.56
This work	HD 56895	07 18 31	−11 11 33				

Notes. The coordinates from Malfait et al. (1998), originally 1950.0, have been precessed to 2000.0.

Table 3. Photometric measurements used to determine the SED of our program objects.

Reference	Bands	Key	Epoch
Monet et al. (2003) (USNO)	<i>B2 R2 I</i>	1	1974–2000
Zacharias et al. (2004) (NOMAD)	<i>BVR</i>	2	unknown
Høg et al. (2000) (TYCHO)	<i>BV</i>	3	1989–1993
Cutri et al. (2003) (2MASS)	<i>JHK</i>	4	1998–2001
Cutri et al. (2012) (WISE)	3.3, 4.6, 12, 22 μm		2010
Oudmaijer et al. (2001) (EXPORT)	<i>UBVRI</i>	5	1998–1999
Malfait et al. (1998)	<i>UBVJHKLM</i>	6	1989–1992
Mendigutía et al. (2012)	<i>JHKLM</i>	7	1992–?
Tannirkulam et al. (2008a)	<i>UBVRIJHK</i>	8	2004–2006
SAAO 0.5 m and 0.75 m telescopes	<i>UBVRIJHK</i>		2014

Notes. SAAO measurements are used by default. WISE measurements are used only for plots but not for the SED fits. The Key field is a pointer from Table 4.

3.1. Model fits of the spectral energy distribution

For each object, we performed a least squares fit of the observed fluxes (actually, the logarithms) in the eight Johnson-Cousins (Bessell et al. 1998) bands *U*, *B*, ..., *K*, according to a simple model of a stellar photosphere plus dust emission (modeled as a single temperature blackbody). The maximum of λF_λ , for $T = 1500, \dots, 1800$ K is at $\lambda \approx 2.4, \dots, 2.0$ μm in *K* band; the other, shorter λ bands used in the SED fit discriminate against cooler dust.

$$F_{\text{mod}}(\nu_k) = [F_{sV} 10^{0.4(m_V - m_k)_s} + F_{dH} B(\nu_k, T_{\text{dp}})/B(\nu_H, T_{\text{dp}})] 10^{-0.4A_V r_k}, \quad (1)$$

where

- $k = 1, \dots, 8$;
- $(m_V - m_k)_s$ are the intrinsic stellar colors derived from the published (SIMBAD) spectral type and an interpolation in the tables of Pecaut & Mamajek (2013);
- r_k is the extinction ratio A_k/A_V from the extinction law of Cardelli et al. (1989) with $R = 3$.

The fit parameters are

- F_{sV} , the absorption-free stellar flux in *V* band;
- F_{dH} , the absorption-free dust flux in *H* band;
- A_V ;
- T_{dp} , the blackbody temperature of the dust component as inferred from photometry.

Three of these (F_{sV} , F_{dH} , T_{dp}) will be used in the Discussion section; also, f_d , the fraction of the observed flux at 1.63 μm contributed by the dust component, will be used in the interpretation of interferometric data, see Sect. 3.4 below.

What value of the extinction ratio R_V should we adopt? Hernández et al. (2004), in a study of 75 HAeBe objects, provide solid evidence for a value $R_V = 5$ fitting the data better

than the standard value $R_V = 3.1$. This conclusion rests predominantly on objects with a high visual extinction $1 \lesssim A_V \lesssim 6$. On the other hand, Montesinos et al. (2009) conclude that $R_V = 3.1$ results in a better fit to the SED of VV Ser ($A_V \approx 3$) and adopt this value for other objects with lower extinction; Fairlamb et al. (2015) take a similar approach; see also Blondel & Tjin A Djie (2006), where among those 60 objects having $A_V \leq 1.0$, the preferred value of R_V is 3.1 in 50 cases. Our sample has an A_V distribution with a median value 0.36; accordingly, we decided to perform our analysis assuming $R_V = 3$.

The numerical method used for fitting the SED is described in Sect. 3.3 below, and the 1σ error bars are derived from the marginal distributions of the Markov chain. The fit results are displayed in Table B.1. A sample fit is shown in Fig. 2.

3.2. Interferometric data: at first glance

Before embarking into numerical model fitting, we should have a qualitative feel for the relationship between measurement results and object properties. We start with a plot of visibilities for the object HD 100453, see Fig. 3. Following common use, the plot is for visibility squared V^2 – a shorthand for $|V|^2$ –, but we will discuss visibilities V . Assuming that the star itself is unresolved at all observed baselines, and that we observe at a single wavelength $\lambda_0 = 1.68$ μm , the combined complex visibility of the star and circumstellar matter is:

$$V(u, v) = f_s V_s(u, v) + f_c V_c(u, v) = (1 - f_c) + f_c V_c(u, v), \quad (2)$$

where $V_c(u, v)$ is the visibility that the circumstellar component alone would have, f_c the fraction of the total flux (at λ_0 , inside the diffraction-limited field of view of one VLTI telescope) contributed by that component; likewise for f_s and V_s , with generally $V_s = 1$.

Table 4. Photometry data for the program objects.

Object	<i>U</i>	<i>B</i>	<i>V</i>	<i>R</i>	<i>I</i>	<i>J</i>	<i>H</i>	<i>K</i>	Key	Var
HD 17081		4.12	4.23	4.30	4.42	4.47	4.52	4.55	1, 3	
AB AUR	7.18	7.17	7.05	7.00	6.80	5.96	5.17	4.30	1, 3, 4, 8	
HD 31648	7.93	7.89	7.70	7.58	7.45	6.81	6.23	5.41	1, 3, 4, 5, 6, 7, 8	
HD 293782	10.30	10.04	9.76	9.62	9.45	8.86	8.00	7.12		*
HD 34282	10.22	10.07	9.88	9.79	9.65	9.15	8.48	7.80		
CO ORI	13.41	12.92	11.76	11.05	10.31	8.70	7.52	6.61		*
HD 35929	8.69	8.54	8.11	7.85	7.59	7.29	6.90	6.58		
MWC 758	8.74	8.61	8.30	8.13	7.92	7.31	6.49	5.70		
HD 244604	9.77	9.64	9.43	9.32	9.18	8.69	7.98	7.23		
HD 36917	8.22	8.17	8.00	7.86	7.66	7.33	7.10	6.66		
T ORI	10.98	10.96	10.49	10.13	10.49	8.70	7.41	6.34		*
HD 37258	9.78	9.72	9.59	9.51	9.40	8.94	8.37	7.68	4, 6	
HD 37357	9.07	9.02	8.89	8.83	8.74	8.37	7.92	7.33	4, 6	
V 1247 ORI	10.31	10.22	9.88	9.68	9.44	8.88	8.20	7.41	4	
HD 37411	10.11	10.00	9.83	9.72	9.56	9.05	8.36	7.57	4, 6	
HD 37806	7.83	7.98	7.92	7.84	7.73	7.33	6.48	5.58		
HD 38087	8.04	8.45	8.30	8.15	7.96	7.71	7.43	7.38		
HD 39014	4.68	4.55	4.32	4.19	4.05	3.90	3.77	3.72		
HD 250550	9.55	9.75	9.60	9.46	9.26	8.47	7.53	6.63	4	
HD 45677	6.81	7.43	7.39	7.21	7.11	6.87	6.09	4.48		*
HD 259431	8.57	9.05	8.73	8.39	8.07	7.42	6.71	5.71	4, 6, 8	
MWC 158	6.34	6.66	6.64	6.56	6.48	6.01	5.22	4.32		
HD 53367	6.86	7.47	7.00	6.65	6.23	5.81	5.54	5.31		*
HD 56895	8.82	8.78	8.38	8.12	7.81	6.36	4.93	3.91		
HD 58647	6.74	6.86	6.80	6.76	6.68	6.50	6.16	5.46		
HD 85567	8.17	8.69	8.54	8.33	8.09	7.60	6.69	5.75		
HD 95881	8.44	8.40	8.25	8.12	7.96	7.32	6.45	5.51		*
HD 97048	9.20	8.94	8.55	8.30	8.02	7.42	6.85	6.10		
HD 98922	6.78	6.80	6.75	6.69	6.61	6.19	5.40	4.45		
HD 100453	8.12	8.09	7.79	7.62	7.44	7.11	6.55	5.78		
HD 100546	6.59	6.68	6.67	6.65	6.66	6.51	6.18	5.69		
HD 104237	7.02	6.92	6.67	6.51	6.32	5.81	5.17	4.56		
HD 139614	8.55	8.52	8.27	8.12	7.97	7.68	7.22	6.62		
HD 141569	7.25	7.22	7.10	7.04	6.94	6.78	6.62	6.55		
HD 142666	9.39	9.17	8.67	8.34	8.00	7.49	6.68	5.92		
HD 142527	9.25	9.01	8.29	7.85	7.40	6.58	5.78	5.09		
HD 143006	11.21	10.94	10.12	9.63	9.17	8.33	7.52	6.86		
HD 144432	8.65	8.54	8.18	7.95	7.69	7.16	6.53	5.94		
HD 144668	7.76	7.53	7.16	6.90	6.63	5.82	5.12	4.37		
HD 145718	9.53	9.24	8.78	8.51	8.21	7.79	7.31	6.75		
HD 149914	7.12	7.02	6.74	6.54	6.30	5.89	5.75	5.70		
HD 150193	9.67	9.36	8.81	8.43	7.97	6.93	6.06	5.29		
AK SCO		9.81	9.17	8.72	8.38	7.67	7.03	6.38	1, 3	
HD 158643	4.79	4.82	4.80	4.77	4.72	4.63	4.56	4.28		
HD 163296	6.93	6.93	6.84	6.77	6.69	6.24	5.46	4.61		
HD 169142	8.38	8.42	8.13	7.95	7.74	7.42	7.07	6.86		
MWC 297	15.53	14.53	12.23	10.39	8.97	6.26	4.46	3.06		
VV SER	13.71	13.33	12.33	11.66	10.92	8.73	7.38	6.27		*
R CRA	13.96	13.69	12.77	11.93	10.83	7.34	5.22	3.56		
HD 179218	7.58	7.50	7.39	7.34	7.28	7.03	6.60	5.93		
HD 190073	7.91	7.95	7.83	7.75	7.62	7.25	6.60	5.77		

Notes. Unless otherwise mentioned, the data listed were acquired at the SAAO Sutherland observatory 0.5 m and 0.75 m telescopes in the scope of the present work. When such measurements are not available, we resort to published measurements as indicated by the *Key* field, that is a pointer to Table 3. The *Var* column signals with an asterisk objects with evidence for photometric variability.

To first order, and ignoring azimuthal dependency, the variation of the combined object visibility V as a function of the radius in the (u, v) plane $b = \sqrt{u^2 + v^2}$, reflects the variation of the visibility of the circumstellar component $V_c(u, v)$. The

part of the diagram where V^2 decreases with increasing b contains information on the characteristic size and even the shape of the circumstellar component, see legend sh in Fig. 3. At large enough baselines, the circumstellar component is fully resolved,

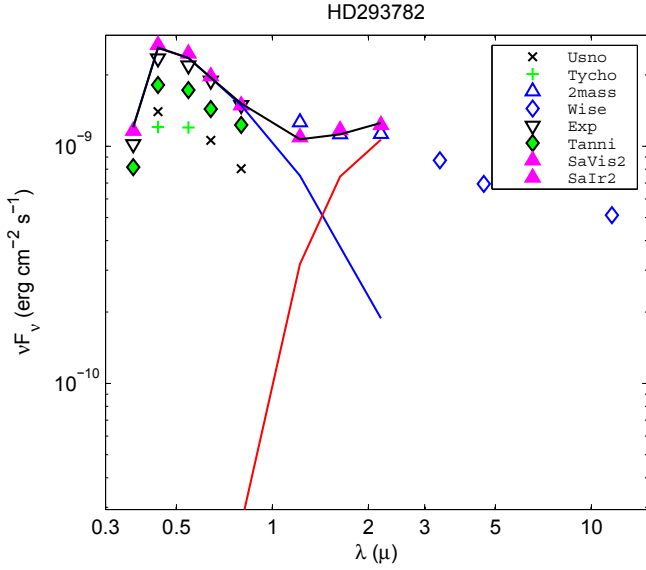


Fig. 2. Example of a fit to photometric data. Only the bands *UBVR1JHK* are used in the fit; the *Wise* data are for reference only. The three lines connect the points of the best-fit model for the star, dust, and total fluxes. The data from the recent SAAO-Sutherland photometry have been given precedence over older data. Also, this object shows strong evidence of variability.

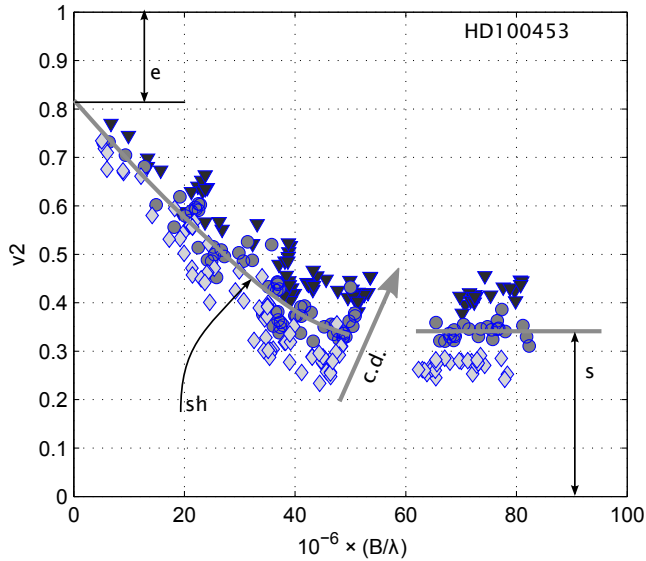


Fig. 3. Visibility squared versus B/λ . Data points from the three wavelength channels of PIONIER are identified by the shape and shading of the symbols; diamonds: $1.77 \mu\text{m}$; circles: $1.68 \mu\text{m}$; triangles: $1.59 \mu\text{m}$. Legend for annotations as follows: sh: shape of the visibility decrease; c.d.: chromatic dispersion; s: asymptotic visibility; e: deficit of visibility extrapolated to zero baseline.

the only coherent flux is from the star, diluted by the circumstellar flux: $V = (1 - f_c) = \sqrt{s}$, see Fig. 3. Conversely, if one extrapolates the curve of V^2 to zero baseline, the intercept may be at a value $V_0 = \sqrt{1 - e}$ less than one. Actually, the visibility must return to unity at zero baseline, but it does so at a baseline significantly smaller than those sampled by PIONIER/VLTI, i.e. at an angular scale larger than those analyzed by our observations. We will call this fully resolved component the “halo” without otherwise presuming a specific morphology; see also Lachaume et al. (2003, Sect. 3.4).

The visibility curve is used as an a priori criterion to define objects with high quality data “HQ”: a necessary condition being that the squared visibility drop to 80% or less of its zero-baseline intercept. This, together with binarity and other exclusion clauses, appears in the footnotes to Table 1.

Finally, we note that the three wavelength channels appear to be spread diagonally in the b - V^2 diagram. When observing with a geometrical baseline B , the three spectral channels are sampling different values of $b \equiv \sqrt{u^2 + v^2} = B/\lambda$. From that cause alone, the various points would populate a unique curve following Eq. (2). To proceed, we introduce in the visibility equation: (a) the dependence on wavelength; (b) the explicit hypothesis that the circumstellar component’s visibility can be factored into a scalar wavelength term and a wavelength-independent spatial part; and (c) we assume the star to be fully unresolved $V_s(u, v) = 1$:

$$\begin{aligned} V(u, v, \lambda) &= f_s(\lambda) + f_c(\lambda) V_c(u, v) \\ &= (1 - f_c(\lambda)) + f_c(\lambda) V_c(u, v). \end{aligned} \quad (3)$$

In the H band the stellar flux rises at shorter wavelengths, the dust flux decreases, therefore f_c decreases, and the combined visibility V increases. We refer to this as chromatic dispersion (noted c.d. in Fig. 3). We note that an anisotropic brightness distribution can also cause a spread in the b - V^2 diagram, which is different from chromatic dispersion because it manifests itself also in monochromatic data.

When the observations reach clearly into the regime where the circumstellar emission is fully resolved, as in the example we have chosen, it is possible to infer from the values of s in each channel the respective values of f_c . Returning to the other observed values of V^2 , using Eq. (2), and under the assumption that V is real positive, it is possible to isolate the visibility of the circumstellar component $V_c(u, v)$. Because these conditions are rarely all met, we cannot generally analyze a program source on the back of an envelope, and we must resort to parametric modeling.

3.3. Parametric model fitting: general methods

We use parametric models to extract morphological and statistical information from our interferometric dataset. Compared with image reconstruction, this has drawbacks, mainly that a functional form is assumed for the source spatial structure. Only a few of our objects have a dataset rich enough to allow for image reconstruction to be attempted; and image reconstruction itself is not totally free from assumptions – regularization, for example. On the other hand, parametric fitting has the advantage that within a family of models, formal error bars can be assigned to the inferred parameter values. Also, in principle, the adequacy of respective models can be gauged from the χ^2 that they achieve.

Building upon the observations of Sect. 3.2, we construct a parametric model with the following components: (1) the star, assumed unresolved at all observed baselines; (2) circumstellar emission with a model-specific and wavelength-independent spatial structure; (3) an extended halo component, defined by its spatial scale: fully resolved at all observed baselines ($\ell \geq 20$ mas), but inside the PIONIER field of view, defined by its single-mode coupling to the Auxiliary telescopes ($\ell \leq 200$ mas); in the context of this work, this presumes nothing concerning the shape of that component.

All fitting was performed in Fourier space; sky images were derived only for illustration purposes. Within the limits of the H band, analyzed by PIONIER in three spectral bands

(1.59, 1.68, and 1.76 μm), the spectral dependence of either the star or the circumstellar component is modeled as a power law, defined by the respective spectral indices k_s and k_c , where $k = \text{dlog } F_\nu / \text{dlog } \nu$. Since at large distances from the star, the H band is in the far Wien region of the grains' thermal radiation, we assume that the halo component arises from diffusion of starlight (see e.g., [Pinte et al. 2008](#)) and has the same spectral index. We verified that making the alternate assumption (same spectral index as the thermal radiation from the near circumstellar component) has a minimal impact on the fit results. Returning to Eq. (2), but now considering a range of wavelengths and including the halo component as discussed above, the visibility can be expressed as:

$$V(u, v, \lambda) = \frac{f_s (\lambda_0/\lambda)^{k_s} + V_c(u, v) f_c (\lambda_0/\lambda)^{k_c}}{(f_s + f_h) (\lambda_0/\lambda)^{k_s} + f_c (\lambda_0/\lambda)^{k_c}}, \quad (4)$$

where λ_0 is a reference wavelength (conveniently that of the central PIONIER channel, 1.68 μm) at which the flux fractions of the three components are defined: f_s , f_c , f_h for star, circumstellar, and halo respectively ($f_s + f_c + f_h = 1$), and, in contrast with Eq. (3), the wavelength dependence is explicitly parameterized. The visibility of the circumstellar component $V_c(u, v)$, is specific to each model, as concerns both the functional form (chosen) and the numerical values of the parameters (the result of the fitting procedure). Several functional forms are introduced below in Sects. 3.5–3.7.

The value of k_s is found assuming that the object's central star radiates in H band as a blackbody at T_{eff} . T_{eff} itself is derived from the spectral type, using Table 5 of [Pecaut & Mamajek \(2013\)](#).

The 1σ error estimates for the observed quantities, visibility squared and closure phase, are computed by the data reduction software, and are derived from the internal scatter during one exposure (typically on 1 min timescale).

The minimization of χ^2 proceeds in three steps. First the shuffled complex evolution (SCE) algorithm ([Duan et al. 1993](#)) performs a global search for a minimum of χ^2 . Next, the breakdown of the value of χ^2 is examined, and the contributions from V^2 and ϕ_{cp} are allocated weighting factors, such that (a) they are balanced; (b) the reduced χ^2 is close to unity. The SCE search is then restarted. Finally the Monte-Carlo Markov chain (MCMC) algorithm ([Haario et al. 2006](#)), still with rescaled χ^2 , is used to (a) derive 1σ error bars for each fit parameter from the marginal distributions of the Markov chain; (b) improve slightly the best-fit χ^2 . As in [Barnby et al. \(2009\)](#), the rescaling of χ^2 is motivated by some error bars on observables being likely underestimated, with a risk of underestimating the error bars on the fitted parameters. Moreover, some of the errors on the observables might be correlated (per-night calibration errors). An over-estimated χ^2 carries the risk of the minimum search algorithm being caught in a local minimum. The unmodified χ^2 value is listed in the results as an indication of how the model captures the complexity of the data.

3.4. Size-flux degeneracy

Our initial fits of simple models to the interferometric observations (we skip for the moment some details of the model, to be found in Sect. 3.5 below) revealed, as one might expect, that some parameter pairs are correlated. Apart from the obvious correlation arising from: $f_s + f_c + f_h = 1$, the clearest correlation was generally found to be between the characteristic size and the fractional flux of the circumstellar component. This is illustrated

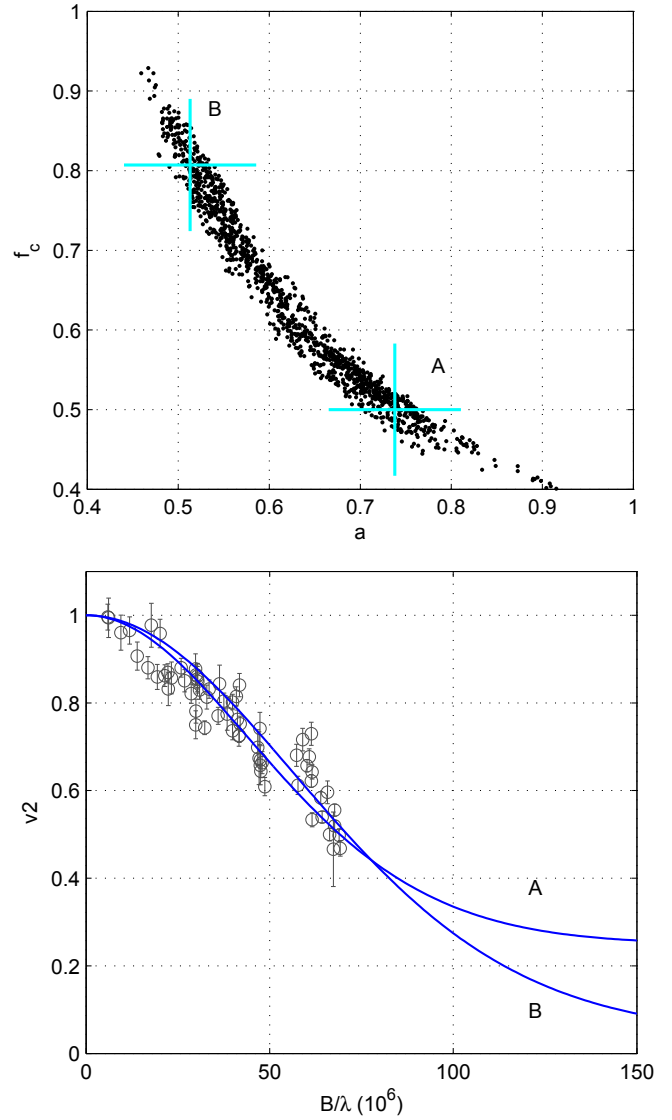


Fig. 4. Illustrating, in the case of HD 85567, the degeneracy that arises when fitting a simple model (star+circumstellar) to interferometric visibility data. *Top panel:* radius a and flux fraction f_c (in the MCMC chain) of the circumstellar component, crosses labeled A and B mark the 10% and 90% points in the respective marginal distributions. *Bottom panel:* observed data for V^2 (middle spectral channel only), and visibility profiles for (isotropic) Gaussians with the parameters at points A and B respectively.

in Fig. 4. The top panel shows the scatter plot (in the MCMC chain) for the variables a , the half-flux radius of the circumstellar component, and f_c , its fractional flux. Points A and B at 10% and 90% of the respective marginal distributions are also shown; note that the respective values differ by a factor of more than 1.5. In the bottom panel, one can see that the visibilities of two Gaussian models for parameter values at A and B are quite similar within the range of observed B/λ , and could be discriminated only by observations at longer baselines.

We see that a degeneracy between the size and the flux fraction of the circumstellar component plagues the model fitting of a partially resolved object, as already noted by [Lachaume \(2003\)](#). This begs the question: are the dust component (identified in the spectral domain) and the circumstellar component (identified by its spatial properties), related? The correlation in Fig. 5 shows that this is indeed the case. A similar plot of $f_c + f_h$

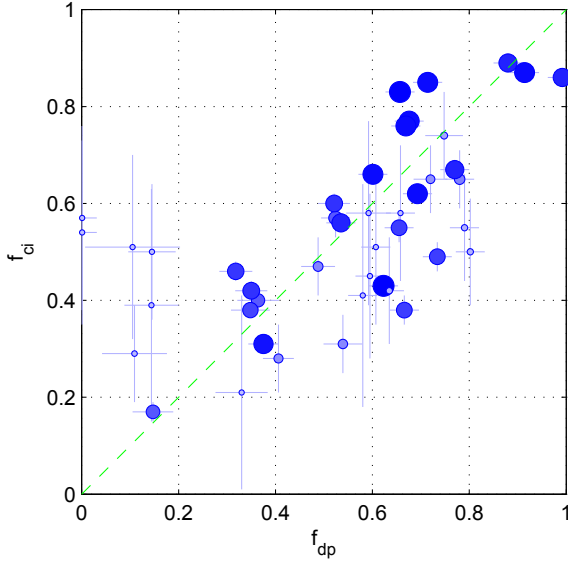


Fig. 5. Dust flux fraction f_d (H -band) from photometric fits, versus circumstellar flux fraction f_c from ellipsoid fits to the interferometric data. The size and color of each symbol reflect the combined accuracy of the f_d and f_c determinations. The error bars are 1σ

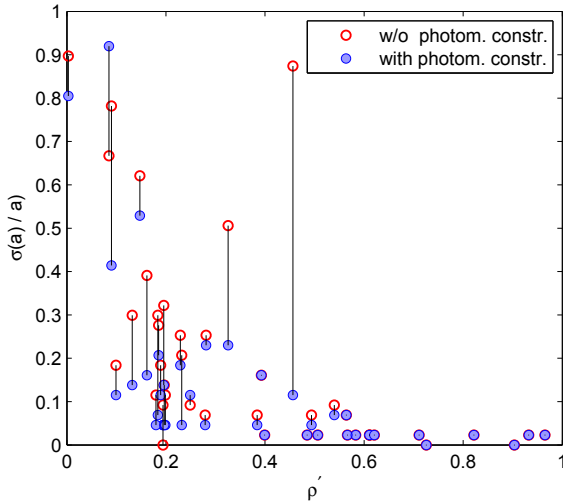


Fig. 6. Relative error estimate for the radius versus the dimensionless resolution $\rho' = (B/\lambda)_{\max} \times a$, without and with the photometric constraint in the interferometric fit. The improvement is most marked for the smaller, marginally resolved objects.

versus f_c (not shown) results in a correlation that is neither better nor worse.

Seeing that f_c deviates the most from f_d (reminder: the photometric flux fraction of the dust component at $1.68 \mu\text{m}$, defined in Sect. 3.1 above) for objects where the former is poorly constrained by interferometric data, we will assume, as a working hypothesis, that f_d and f_c measure the same (circumstellar) component of the objects. Accordingly, in order to account for this additional constraint, we introduce in the expression of χ^2 that drives the fitting of interferometric data an extra term $((f_c - f_d)/\sigma(f_d))^2$, where the value of f_d is from the photometric fit. Figure 6 shows the improvement in the size standard error when the photometric constrain is imposed in the fit of interferometric data. Such a photometric constraint is applied in all subsequent model fits.

Table 5. Hankel transform pairs for the Gaussian and pseudo-Lorentzian radial distributions.

	$\mathcal{F}(r)$	$\mathcal{V}(q)$
Gauss	$\frac{\ln(2)}{\pi a^2} \exp\left(-\left(\frac{r}{a}\right)^2 \ln(2)\right)$	$\exp\left(-\frac{(\pi a q)^2}{\ln(2)}\right)$
Lor	$\frac{a}{2\pi\sqrt{3}} \left(\frac{a^2}{3} + r^2\right)^{-3/2}$	$\exp\left(-\frac{2\pi a}{\sqrt{3}} q\right)$

Notes. Radial scaling is such that a is the half-flux radius. The distributions are scaled to unit flux, i.e. $\mathcal{V}(0) = 1$.

Table 6. Parameters for fits of ellipsoidal brightness distribution.

k_c	Spectral index of circumstellar component
f_c	Fractional flux of circumstellar component
f_h	Fractional flux of halo component
f_{Lor}	Weighting for radial profile
l_a	(log) Half flux semimajor axis
$\cos i$	Axis ratio of isophotes
θ	Position angle of major axis, east from north

Notes. l_a is shorthand for $\log_{10}(a/1 \text{ mas})$. In practice, the redundant parameter f_s , fractional flux of the star, is also included, together with a constraint $f_s + f_c + f_h = 1$.

3.5. Ellipsoids

The first and simplest model that we use for the circumstellar emission has a brightness distribution continuously decreasing outwards, with elliptic isophotes.

The Gaussian radial brightness distribution is widely used in modeling. But it is peculiar in having a strong asymptotic decay, faster than any power law or plain exponential, which might not be a good description of reality. So we also use a distribution with an opposite behavior, having an r^{-3} asymptotic decrease (the smallest integer exponent with converging flux integral). That is the pseudo-Lorentzian (Lor) distribution as shown in Table 5, which has a simple analytic Hankel (radial Fourier) transform.

Starting from a face-on model with circular symmetry, an inclined model with arbitrary axial ratio $\cos i$ and position angle θ can be derived by simple transforms in the (u, v) coordinates.

In exploratory tests, it was found that some objects “favor” (achieving a lower χ^2) the Gauss profile, while other objects favor the Lor distribution. Following that, we introduced f_{Lor} as one of the fit parameters, allowing intermediate radial distributions, such that the circumstellar component visibility in Eq. (4) is

$$V_c = (1 - f_{\text{Lor}}) \mathcal{V}_{\text{Gauss}} + f_{\text{Lor}} \mathcal{V}_{\text{Lor}}. \quad (5)$$

We proceed with the fits of the program objects. Table 6 gives the list of fit parameters; the values are listed in Table B.2.

3.6. Ring

This type of model is intended to model the emission from a bright rim, for example, the inner rim of a sublimation-bounded dust disk. We start with a “wireframe” distribution

$$\mathcal{F}_0(r) = \frac{1}{2\pi} \delta(r - a_r), \quad (6)$$

normalized to unit flux. Its complex visibility is

$$\mathcal{V}_0(q) = J_0(2\pi q a_r). \quad (7)$$

Table 7. Parameterizations of broadened elliptical ring.

Geometrical	a_r a_k	Ring angular radius ^a Kernel angular radius
Physical	$a = (a_r^2 + a_k^2)^{1/2}$ $w = a_k/a$	Half light radius ^{a,b} Kernel/half-light
Fit	$l_a = \log_{10}(a/1 \text{ mas})$ $l_{kr} = \log_{10}(a_k/a_r)$	$-1 \leq l_a \leq +1.5$ $-1 \leq l_{kr} \leq +1$

Notes. ^(a) A single notation is used for radii, whether angular (radians, milliarcseconds) or linear (AU); the context resolves ambiguities. ^(b) Actually, an approximation to the half light radius valid to 5% or better for our radial profiles.

Next we introduce azimuthal modulation:

$$\mathcal{F}(\mathbf{r}) = \mathcal{F}_0(\mathbf{r}) \times \left(1 + \sum_{j=1}^m (c_j \cos j\phi + s_j \sin j\phi) \right), \quad (8)$$

where ϕ is the polar angle, m is the order of azimuthal modulation, and the sum is absent if $m = 0$. The underlying motivation for such a modulation comes from models such as those of Dullemond et al. (2001), Isella & Natta (2005), where the inner rim of a disk is viewed inclined: the rim contour appears, to first order, as an ellipse, with the far side being more luminous from the vantage point of the observer. Leaving aside the radial structure, the angular modulation in such a model involves only sine terms of odd order. Because we want our analysis to remain model-agnostic as much as possible, we do not include such a restriction in Eq. 8.

Transforming the modulation amplitude to polar representation: $c_j + i s_j = \rho_j \exp(i\theta_j)$ and likewise for the coordinates in the (u, v) plane: $q_u + i q_v = q \exp(i\psi)$, the complex visibility for the modulated skeleton is:

$$\mathcal{V}(q) = J_0(2\pi q a_r) + \sum_{j=1}^m (-i)^j \rho_j \cos(j(\psi - \theta_j)) J_j(2\pi q a_r). \quad (9)$$

Just as for ellipsoids (Sect. 3.5), the wireframe distribution is squeezed by a factor $\cos i$ along the direction of the minor axis, and rotated by the position angle. The above-mentioned azimuthal modulation, Eq. (8), is defined with the angle origin along the major axis.

Because real ring-like images (if they exist) have a finite width, the wireframe image is convolved by an ellipsoidal kernel, with a semi-major axis a_k , the same axial ratio $\cos i$ as the wireframe, and a radial distribution that is a hybrid between a Gaussian and a pseudo-Lorentzian, as described above in Eq. (5) and Table 5.

Irrespective of the particular parameterization, this model can describe both thin rings ($a_k \ll a_r$) and, asymptotically ($a_k \gg a_r$) ellipsoids, since the convolution kernel is identical to the ellipsoid model.

The geometrical (see Table 7) parameter pair (a_r, a_k) becomes degenerate in the limit of ellipsoid-like cases where only a_k is relevant. The physical pair is more meaningful, especially when the object is marginally resolved, and the parameter w spans a finite range $0 \leq w \leq 1$. It is not, however fully suitable for the MCMC search because (by default) the method assumes a uniform prior over the allowed search interval: most of the $0 \leq w \leq 1$ interval corresponds to a distinct ring structure,

Table 8. Parameters for Ring fits.

k_c	Spectral index of circumstellar component
f_c	Fractional flux of circumstellar component
f_h	Fractional flux of halo component
f_{Lor}	Weighting for radial profile
l_a	(log) half light semi major axis
l_{kr}	(log) ratio (kernel radius)/(ring radius)
$\cos i$	Axis ratio of isophotes
θ	Position angle of major axis, east from north
c_j, s_j	Cosine and sine amplitudes for mode j

Notes. Redundant parameter f_s is also included, see Table 6.

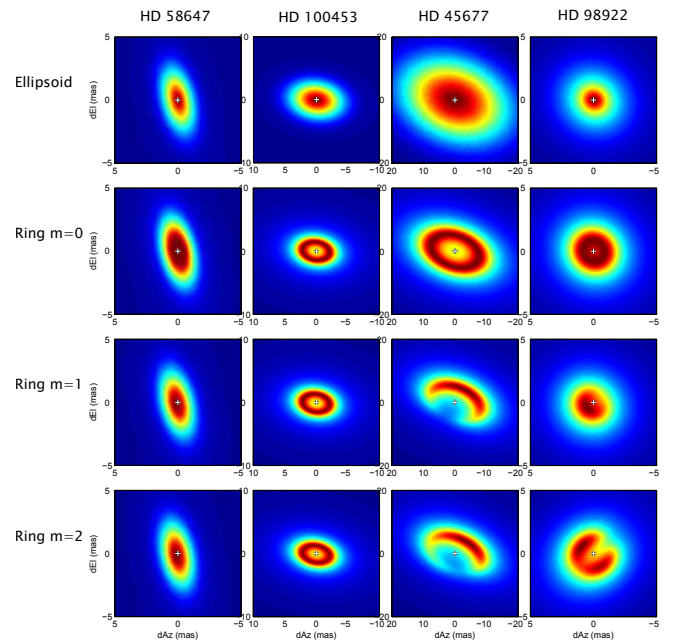


Fig. 7. Examples of model fits, showing four objects and fit results at four levels of complexity of the fit model. The symbol m is the order of azimuthal modulation; see Eq. (8).

leading to a bias towards detection of such a structure. The “fit” parameters in Table 7 cover a wide range, with a scale-free prior. The fit parameters number one more (excluding azimuthal modulation) than for the ellipsoid model; they are listed in Table 8.

Figure 7 shows examples of fits for some program objects, and shows how a given object – observed at a given resolution – requires a certain degree of complexity, but not more.

3.7. Power law with inner boundary

In some, if not all, current models for inner disk rims, one expects the brightness distribution to have a sharper cutoff inwards than outwards. Accordingly, we tested models with a radial distribution:

$$\mathcal{F}_0(r) = \begin{cases} 0 & \text{if } r < a_r \\ \frac{a_r}{2\pi} r^{-3} & \text{if } r \geq a_r, \end{cases} \quad (10)$$

and similar models with an exponent different from -3 , or an exponential decay, with or without convolution by a kernel (see Sect. 3.5 above). None of these showed a significant advantage, as measured by the χ^2 , over the already listed model types.

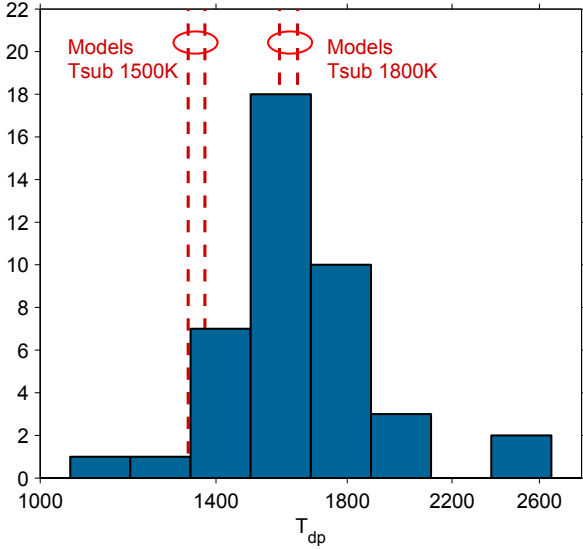


Fig. 8. Histogram of T_{dp} (log scale) derived from fits to photometric data, restricted to non-binary objects having a fractional contribution of the dust to the H -band flux $f_{\text{d}} \geq 0.1$. Dashed lines: values of T_{dp} obtained when fitting, with same procedure, models with sublimation temperature 1500 K or 1800 K; see text and Table 9.

4. Analysis and discussion

In this section we use the results of parametric fits performed in the previous section (Data processing) to address the properties of the objects themselves. Because the observations provide (at best) a 2D (interferometry) or 1D (photometry) projection of the objects, and because the parametric models are arbitrary, we attempt to reduce these shortcomings by comparisons with physical models.

We issue up front two disclaimers: firstly, our goal is not to fine-tune a physical model and declare that it represents reality; at best we can hope to support statements on some large-scale properties of the real objects. Secondly, we discuss our sample globally, and derive generic properties, which makes the best use of our limited statistics, but does not imply that real objects come from a single mold. Depending on the issue being discussed, the sample may be either the 44 non-binary objects “noBin” or the 27 so-called high-quality objects (HQ): in short, those non-binary objects that are suitably resolved, with V^2 dropping below 0.8 at the long baselines.

4.1. Dust temperatures

4.1.1. Temperatures from photometry

Figure 8 shows the histogram of fitted dust temperatures T_{dp} , subject to $f_{\text{d}} > 0.1$ to exclude objects where a fit of dust properties is not meaningful. The histogram of T_{dp} shows a few possible outliers above 2200 K or below 1200 K; to avoid any excessive influence of such outliers, we make use of the median statistic. The median value of T_{dp} is ≈ 1650 K ($\log_{10}(T_{\text{dp}}) = 3.22$). The median of the error estimates on $\log_{10}(T_{\text{dp}})$ is: 0.026, consistent with an estimate of the sample dispersion as: $\text{median} [|\log_{10}(T_{\text{dp}}) - \text{median}(\log_{10}(T_{\text{dp}}))|] = 0.030$, and with the dispersion being mostly from measurement uncertainties.

The median value for T_{dp} appears to be in the range of dust sublimation temperatures, in agreement with the current ideas regarding disks around HAeBe stars; see Dullemond & Monnier (2010) and references therein, or the disk-wind model of

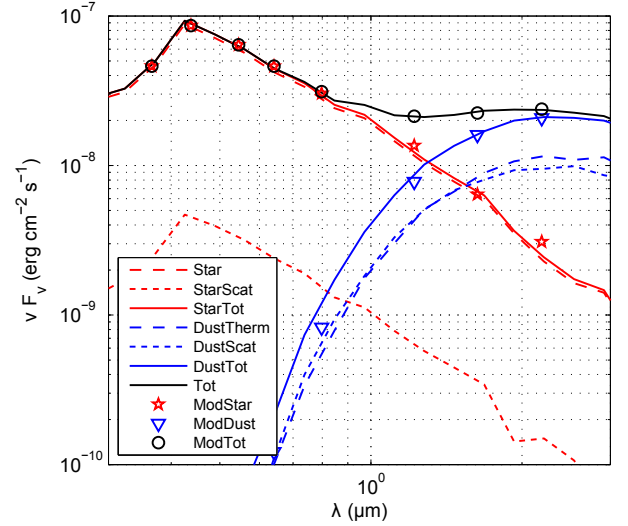


Fig. 9. Sample fit of a model SED (A1c) obtained with the MCFOST program. The lines show various contributions to the SED of the MCFOST model: direct thermal radiation (dash); diffusion (dash-dot); total (continuous) for either the stellar or the dust contributions. The symbols show the equivalent flux values in the eight photometric bands (U, \dots, K) for the fitted star+dust model. A model with a single blackbody for the dust appears to provide an acceptable fit to the near-infrared spectrum, even though the emitting dust spans a range of temperatures.

Bans & Königl (2012). However, in any such model, one expects dust to exist over a range of temperatures below the sublimation temperature; furthermore, our fitting procedure might introduce some bias. To address these two concerns, we use the MCFOST radiative transfer code (Pinte et al. 2006) to generate the SED from a few simple models of HAeBe objects combining two spectral types (for the central star) with two types of grains. The inner rim radius of each model is adjusted so that the maximum grain temperature would be (approximately) the sublimation temperature T_{sub} for the respective grain types: 1500 K for silicates, and 1800 K for carbon. These models are used only to discuss dust temperatures, and are distinct from those defined in Sect. 4.2. The values of νF_{ν} in the eight Johnson bands ($U-K$) are used as input to the same fitting procedure that is used for deriving T_{dp} from the observations. A sample fit is shown in Fig. 9. The results are summarized in Table 9; the four values of $T_{\text{d,fit}}$ are plotted in Fig. 8; the models with carbon grains appear to agree better with the observed values of T_{dp} ; in fact, the difference in $\log_{10}(T_{\text{dp}})$ between carbon and silicate models, 0.0765, is 2.7 times larger than the (median-based) sample dispersion. We conclude that: (1) the best-fit blackbody temperature for the NIR emission is close to 1650 K; (2) based on simple models, that value (1650 K) is consistent with $T_{\text{sub}} = 1800$ K (carbon?); (3) the data rule out that the grains responsible for the NIR bump have $T_{\text{sub}} = 1500$ K (silicates?).

Our finding that the sublimation-bounded inner rim of Herbig object disk is populated predominantly by grains with a high sublimation temperature can be explained by the survival of the fittest in a hostile environment. A similar conclusion has been reached by Carmona et al. (2014) in their study of HD 135344B.

4.1.2. Temperatures from interferometric data

When spectrally dispersed interferometric data has been acquired, the model fit to the interferometric data provides an estimate of the slope, across the H band, of the radiation intensity

Table 9. Properties of simple models and the respective fits to the dust temperature.

Model	T_{eff} (K)	L_{b} (L_{\odot})	R_{in} (AU)	Grains	$T_{\text{d,max}}$ (K)	$T_{\text{d,fit}}$ (K)
A1s	9250	36	0.50	silicate	1520	1370
A1c			0.36	carbon	1880	1580
B2s	20 600	2280	4.5	silicate	1460	1330
B2c			2.9	carbon	1800	1637

Notes. Common properties as follows. Viewing angle $\cos i = 0.55$ ($i \approx 56^\circ$); distance 122 pc; $R_{\text{out}} = 125$ AU; scale height 0.07 AU at $r = 1$ AU; flaring exponent 1.10; dust mass $0.65 \times 10^{-3} M_{\odot}$; grain size: $a_{\text{min}} = 0.1 \mu\text{m}$, $a_{\text{max}} = 1000 \mu\text{m}$, exponent 3.5.

from the (partly) resolved component. More precisely, the fit provides the differential slope between the extended and the unresolved (stellar) components; the latter being known from the star’s spectral type.

Define for any component the spectral index (across the H band) as:

$$k = \frac{d \log F_{\nu}}{d \log \nu}, \quad (11)$$

that can be converted easily to and from blackbody temperatures. The spectral slope of the circumstellar component, determined from interferometric data, k_{c} , can be converted to an equivalent temperature T_{ci} .

In Fig. 10 we present a scatter diagram of T_{ci} versus T_{dp} . The data are from the Ellipsoid fits to the 44 non-binary program objects, with extra restrictions: (i) dust flux fraction (H -band photometry) $f_{\text{d}} \geq 0.1$; (ii) circumstellar flux fraction (H -band interferometry) $f_{\text{c}} \geq 0.1$; (iii) object HD 56895 excluded (see Sect. 2.2 above); (iv) object must be observed in dispersed mode. A total of 35 objects meet these conditions.

First, the ranges of T_{ci} and T_{dp} are similar and not far from expected grain sublimation temperatures. Second, there is no clear correlation between these two variables. Third, the values of T_{ci} are predominantly lower than T_{dp} for the same object. We remind the reader that T_{dp} is derived by decomposing the light from a Herbig object in the spectral domain, while T_{ci} relies on a decomposition in the spatial domain, where the circumstellar component is assumed to be dominated by radiation from dust. The identity between the respective stellar and non-stellar parts in each of these decompositions is, however, an assumption.

Following our caveat above on the respective definitions of T_{ci} and T_{dp} , one possible cause for the observed discrepancy would be a non-photospheric and unresolved component of the object. For instance the inner gaseous disk that should be present inside the dust sublimation radius, at least if the star is still accreting. The determination of T_{ci} relies on the differential slope in the H band of the (partly) resolved component relative to the unresolved component. If a non-photospheric emission is present with a flux rising (towards short wavelengths) faster than the photospheric flux, then assigning the photospheric value to the slope of the unresolved component is an under-estimate, which propagates to an under-estimate of the dust temperature. The existing models for such an inner gaseous disk, for example, Muzerolle et al. (2004; their Fig. 11), or Dullemond & Monnier (2010; their Fig. 13) based on the opacities of Helling & Lucas (2009) show that at least potentially, its SED can upset the slope of the photospheric emission.

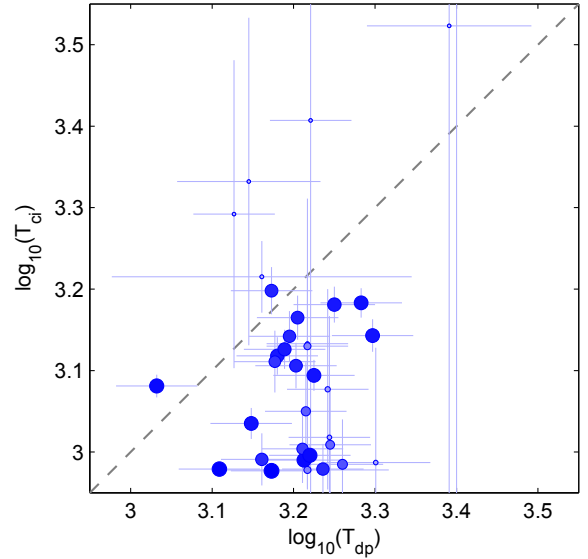


Fig. 10. Dust temperatures derived from fits to, respectively, the photometric data T_{dp} and the interferometric data T_{ci} . Values from the Ellipsoid fits to the subset of 44 non-binary objects, with some restrictions (see text). The size of the symbols reflects the combined accuracy for both variables.

4.2. Overcoming some limitations of parametric fits via substitution weighing

In the previous section, parametric fits of the observed data were used to obtain quantitative information in preparation for the discussion and statistical analysis of the present section. The values of fitted parameters can be subject to biases: either identifiable like the difference between the radius of a Ring model (mean radius) and the rim radius (innermost), or, worse, unforeseen and undetected.

To overcome as much as possible these issues, we use an approach analogous to substitution weighing (that allows accurate measurements using a balance with unbalanced or even unequal arms). We generate a small number of physical disk models, using the MCFOST code.

Each model is then “observed” at various inclinations and distances. Here, to observe means to generate visibilities squared and closure phases for a set of wavelengths and baselines typical of a program object (HD 144668). A realistic noise is added, based on the estimates derived from extensive analysis of PIONIER data; for details see Appendix A. These data are fed to the same fitting procedure as the real data. The comparison between the fit parameters from, respectively, real and model objects, helps to interpret the fit results in a way that eliminates possible systematic biases from the fitting procedure.

Our models are loosely inspired by two published models: Isella & Natta (2005, hereafter IN05), and Tannirkulam et al. (2007, hereafter THM07); we take full responsibility for the shortcomings of our imitations; our goal is mainly to sample two different morphologies. Each of IN05 and THM07 models derives a consistent solution for radiative transfer, thermal equilibrium, hydrostatic equilibrium, and dust sublimation. Furthermore, THM07 considers two grain sizes and size-dependent settling, as considered in detail by Dullemond & Dominik (2004). The smaller grains, having a lower cooling efficiency, reach the sublimation temperature at larger distances than the larger grains.

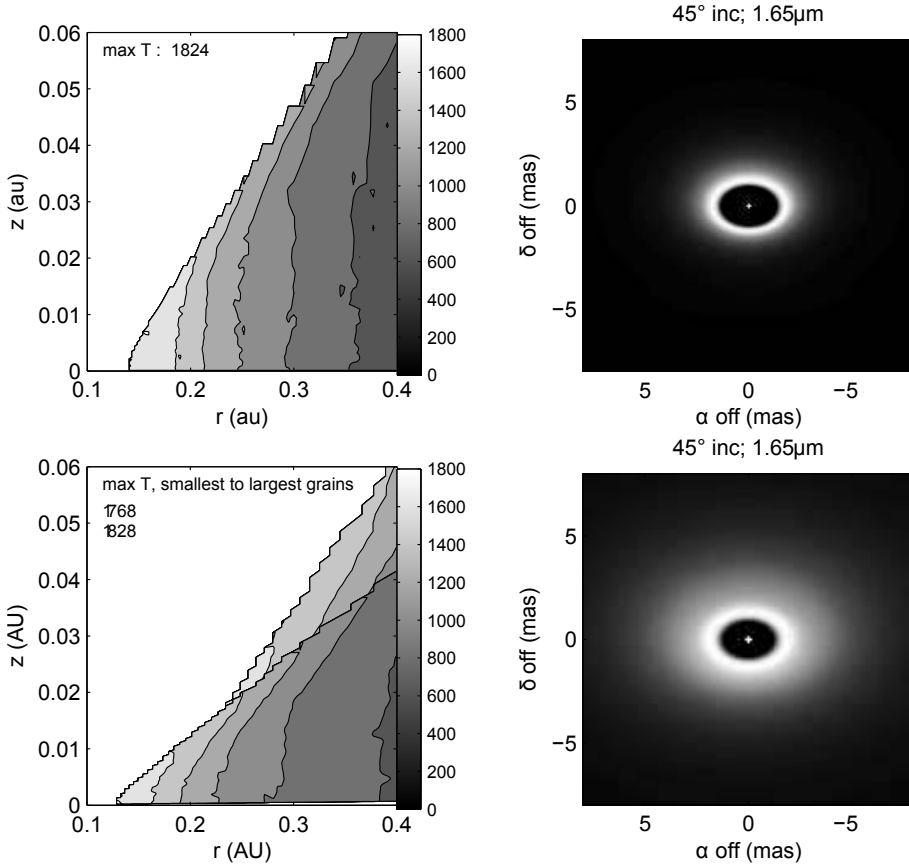


Fig. 11. Graphical summary of models IN (*above*) and THM (*below*). *Left*: temperature profiles; in the case of the THM model, the temperature distributions for large grains is overlaid onto that for small grains. *Right*: sky images at $\lambda = 1.65 \mu\text{m}$, $i = 45^\circ$; a mild enhancement of low brightness regions has been realized by a square root scaling. The angular scale is for the object located at a distance of 100 parsecs.

Our IN05-like model, IN hereinafter, has a single grain radius: $1.2 \mu\text{m}$ while our THM07-like model, THM hereinafter, has two grain radii: $0.35 \mu\text{m}$ and $1.2 \mu\text{m}$, resulting in a broader radial distribution of H -band emission. In contrast with the IN05 and THM07 originals, our models solve only for thermal equilibrium of dust and radiative transfer, given an arbitrary dust distribution with azimuthal symmetry. See Fig. 11.

Variants of each of the base models were produced for three types of central stars: A8V, A0V, and B2V. Spatial scales ℓ for each model were adjusted ($\ell \propto L_{\text{bol}}^{1/2}$ to first order) to bring the maximum grain temperature close to 1800 K, while densities were adjusted $\rho \propto \ell^{-1}$ to preserve opacities at analogous points. Anticipating the observed value of the fraction f_{rep} of stellar flux intercepted by the dusty disk (Sect. 4.7.2), we have tuned the relative thickness z/r of our models to match $f_{\text{rep}} \approx 0.2$ for the A8 and A0 variants, while we targeted $f_{\text{rep}} \approx 0.05$ for the B2 variants. More details are provided in Appendix A.

Additionally, to test the prevalence of false positives (detection of ring structure) in our fitting procedure, we generated the ELL series of images, that are ellipsoids, having the same values for the stellar flux, the circumstellar flux, and the half-light radius as the THM models; in other words, the “same”, but no ring structure. These images are generated from a prescription for their light profile, not from a radiative transfer calculation, and should not be confused with the Ellipsoid fit model introduced in 3.5.

4.3. Is there evidence for ring structure?

One possible way to answer that question is to compare the χ_r^2 values for an Ellipsoid fit and a Ring fit in its simplest form,

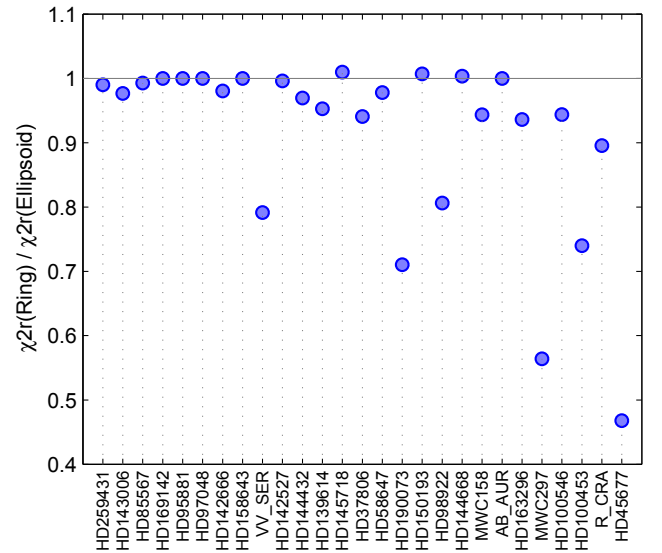


Fig. 12. Showing, for the HQ subsample, the improvement (or not) of χ_r^2 between an Ellipsoid fit and a Ring fit. The objects have been sorted by increasing size.

with no azimuthal modulation. Figure 12 shows the results, over the HQ sub-sample, sorted by size. One can see that: firstly, six objects express a preference for the ring structure: VV Ser, HD 190073, HD 98922, MWC 297, HD 100453, HD 45677; secondly, a large angular size favors, but does not guarantee that the ring structure results in a lower χ_r^2 . A natural (but not unique) interpretation of these results is that (i) a significant fraction of our program objects have a ring structure; (ii) the detection of

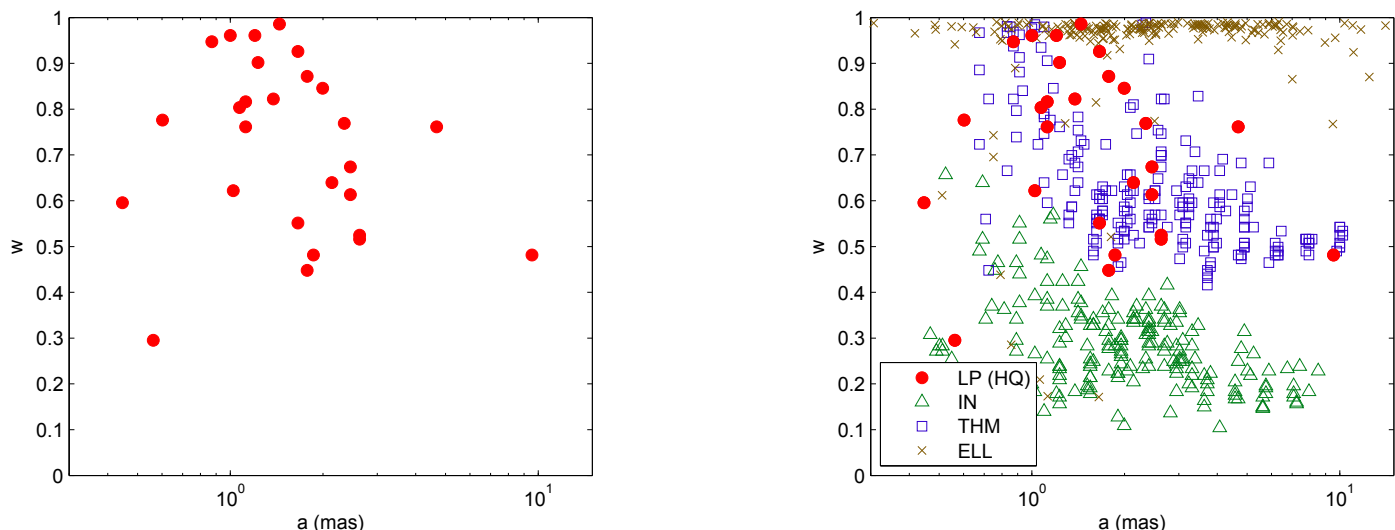


Fig. 13. *Left panel:* parametric fit results for the 27 HQ objects. Normalized ring width w versus half flux radius a . See text. *Right panel:* with fits of MCFOST models IN, THM and ELL added.

such a structure is difficult or impossible in marginally resolved objects.

The same question – whether our data show evidence for ring structures in the program objects – can be addressed in a different way. Remember that the Ring model fits comprise the Ellipsoid fits as a subset, since as $\log_{10}(a_k/a_r) \rightarrow \infty$, $w \rightarrow 1$, and the ring structure degenerates into an ellipsoid; see Tables 7 and 8. So, instead of examining the χ_r^2 of a ring fit, we examine the value of w , and, since we suspect that the ability to detect ring structures is hampered by the limited angular resolution, we plot w versus a ; see Fig. 13 (left panel). The following results emerge: (1) a negative correlation between w and a , i.e. the detection of a ring structure is less likely for small radii, as expected; (2) for a significant fraction of the objects, a ring structure is detected by the fit, but... (3) the rings seem to be wider than expected models with a rounded rim, as proposed by Isella & Natta (2005) and pictured in a number of publications. At this point, we must consider the following possibilities: (a) our parametric fit is biased, the fitted ring is wider than reality; (b) actual rings are wide (w of order 0.5); (c) there are no rings in the H -band images of HAeBe objects circumstellar matter, and the fit algorithm was biased towards finding them.

Figure 13 (right panel) shows, alongside the HQ objects, the fit results for the IN models at various inclinations and distances. Although we cannot compare one-to-one the fitted ring width with the real width (if only because of the lack of a unique definition for the latter), this plot makes it clear that the putative rings of the LP objects are wider than those of the IN model.

Also in Fig. 13, we have plotted the results of fitting THM models. This shows that at least one simple model of dust distribution and radiative transfer can result in a (a, w) diagram, if not identical, at least much closer to the observed one than the IN model.

We remind the reader that the IN model, inspired by Isella & Natta (2005), has a rim with a rounded shape, with a (relatively) large radius of curvature, and a single grain size, while the THM model, inspired by Tannirkulam et al. (2007), has a shape closer to a knife-edge and two grain sizes; its sloping surface under oblique illumination leads to a more radially extended emission.

Finally, performing fits of plain ellipsoid images ELL (defined in Sect. 4.2) we find only a small rate of false ring detection: 90% of the w values are >0.925 , and 80% are >0.975 ; while $w < 0.7$ occurs only for small angular radii $a < 1$ mas.

We conclude that, using the substitution weighing approach, we have eliminated possibilities (1) and (3) as listed above, leaving only (2): our interferometric data support the presence, in a significant fraction (at least 50%) of the HQ program objects, of a ring-like structure. Moreover, these ring structures are significantly wider than what results from a simple rounded rim as our IN model, and a fortiori for a flat vertical wall.

The THM model, however, fits the observed (a, w) diagram rather well. Some doubt concerning a sharp inner rim had already been voiced by Tannirkulam et al. (2008b); these authors interpreted the lack of a strong bounce in the visibility curve as supporting the presence of emission inside the sublimation rim. It is noteworthy that, besides THM07, Kama et al. (2009) and Flock et al. (2016) also perform a self-consistent modeling of the rim including grain sublimation, and that most of their models result in a wedge-shaped (as opposed to rounded) rim. The photospheric contours in their Figs. 6 and 7 (bottom rows) bear a striking similarity with those of our THM model (Fig. A.2, bottom row, middle panel), considering that our THM model (not physically self-consistent) was adjusted specifically to match the large value of the observed width of the H -band emission region. Dullemond & Monnier (2010, their Fig. 10 and Eq. (13)) also explicitly derive a physical model with a large radial extension of the sublimation front.

4.4. Do we see azimuthal modulation?

To answer this question, we have performed, over the HQ subsample, three types of model fits, beginning with the Ring model with no azimuthal modulation; see Table 10.

Because we keep a record of the partial χ^2 contributions, we are able a posteriori to choose to include the closure phase (ϕ_{cp}) contribution in the final value of χ^2 for the $m = 0$ model, allowing a fair comparison with the other two models.

The values of the three models listed in Table 10 are compared in Fig. 14, with the un-modulated model serving as a reference. As in Fig. 12, the objects are ordered by increasing angular

Table 10. Fits performed with or without azimuthal modulation.

Id	Number of az. modes	χ^2 driven by
Ring	$m = 0$	V^2
RingM1	$m = 1$	$V^2 + \phi_{cp}$
RingM2	$m = 2$	$V^2 + \phi_{cp}$

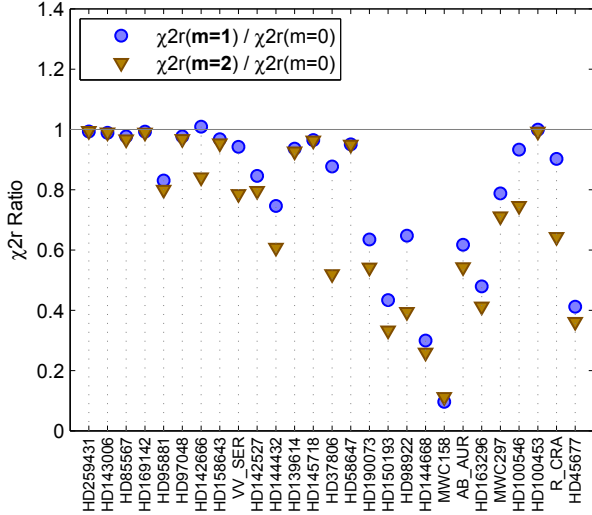


Fig. 14. Improvement of χ^2 (or lack of-) when increasing the number of azimuthal modes in the fit model, the χ^2 containing both the terms from V^2 and ϕ_{cp} . We note that, in contrast with Fig. 12, the χ^2 for the unmodulated ring model includes the closure residuals, to be comparable to the other two fit models, with azimuthal modulation. As for Fig. 12, the objects are sorted in order of increasing size.

size (value of a). One can see that most, but not all, of the better-resolved objects show an improvement of χ^2 when modulation is introduced; $m = 2$ modulation seems to provide a smaller incremental improvement than $m = 1$.

A deviation from centrosymmetry (odd m modulation) is expected when a rim is viewed at non-zero inclination. But a spatial offset between the circumstellar emission and the star has the same effect. So, we propose a slightly more stringent test in the next subsection.

4.5. Is the azimuthal modulation aligned as we expect?

In any model featuring an inner disk rim heated by the central star, one expects, at intermediate inclinations, the far side of the rim to be more luminous than the near side. Such an asymmetry involves, in Eqs. (8) and (9), only sine terms of odd order; other terms are included because the model must be unbiased.

We test the presence of such a far-side dominance using a plot based on the modulation coefficients c_1 and s_1 . We remind the reader that the modulation is defined in the rotated frame that is aligned with the apparent shape of the rim, and note that the position angle of that ellipse is (nearly) indeterminate for (near) zero inclination (pole-on). Accordingly, we represent each object at the coordinates ($x = |c_1| \sin i$, $y = |s_1| \sin i$). See Fig. 15. The asymmetry between the near and far sides of a rim image is expected to result in points aligned along the vertical axis. As a reference, the right panel shows the result of fits to *in_A0* and *thm_A0* models. The scatter diagram on the left panel of Fig. 15 show a majority of points closer to the vertical than to

the horizontal axis, similar to, but less marked than the model diagram on the right panel.

One notable exception is MWC 158 (at graph coordinates (0.85, 0)); this object has been observed with PIONIER before and during the Herbig Large Program, over a time span of ≈ 2 years, and has been shown (Kluska et al. 2016) to have a variable structure on ≈ 2 mas scale, possibly corresponding to the orbital motion of a bright condensation around the central star.

Following this special examination of MWC 158, which does not fit into the expected pattern for modulation coefficients, we must examine with equal attention the objects that do conform to the expected pattern. Two objects dominate the alignment along the vertical axis in Fig. 15: HD 45677 and HD 144668. The values of w for these two objects are:

HD 45677 0.48

HD 144668 0.85.

Figure 13 (test for false positives with ELL images) shows that a w value below 0.95 corresponds to a ring structure with a high degree of confidence. Therefore, the visual alignment pattern in Fig. 15 does arise from modulated rings, not modulated ellipsoids (in which case it would be essentially an offset).

4.6. Closure phase statistics

Closure phases provide a model-independent way to measure the degree of asymmetry of the objects. We generate plots of closure phase ϕ_{cp} versus resolution ρ' , as follows: (1) we measure the resolution by the largest of the three projected baselines of the triangle that defines each closure phase measurement; this is an arbitrary way to subsume a triangle by a scalar; (2) the resulting scatter plot is converted to an ordinary plot of closure phase versus resolution by computing percentiles in a sliding resolution window (width 0.2 in \log_{10} representation); (3) the effective resolution must take into account the angular radius of the object, and, to first order, its anisotropy. Accordingly, for an object having half-light semi-major angular diameter a at position angle θ , with an axis ratio $\cos i$, and observed over a projected baseline with coordinates $(u, v) = (b_x, b_y)/\lambda$, we define the dimensionless resolution σ' along that baseline:

$$\alpha = \pi/2 - \theta$$

$$u' = u \cos \alpha + v \sin \alpha$$

$$v' = \cos i (-u \sin \alpha + v \cos \alpha)$$

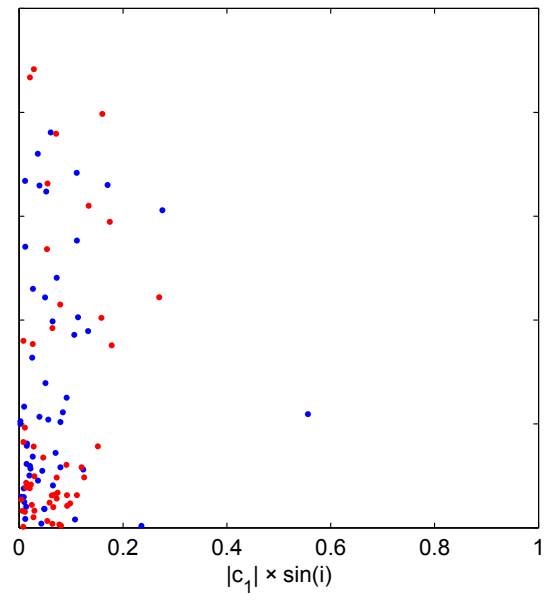
$$\sigma' = a (u'^2 + v'^2)^{(1/2)}, \quad (12)$$

and for a closure phase measured over a triangle, the value of σ' for the largest side:

$$\rho' = \max(\sigma'_k) \quad k = 1 \dots 3. \quad (13)$$

Figure 16 shows (black lines) plots of the sliding third quartile (see above) of ϕ_{cp} versus ρ' either for the totality of the 44 non-binary objects, or excluding HD 45677. Monnier et al. (2006) used similar plots, but based, at each resolution value, on the maximum closure phase, which may have a low probability of being measured in actual observations. We show two variants, with the measure of dimensionless resolution based either on the largest or the smallest side of each closure triangle.

The plot that includes HD 45677 shows higher values of ϕ_{cp} above $\rho' \approx 1$. HD 45677 is the object with the second largest angular radius (≈ 10 mas) in our sample, almost four times larger than the next largest object. Image reconstruction (Kluska et al. 2014) and parametric models up to azimuthal order $m = 5$ agree to show substructure in the sublimation rim of HD 45677; we



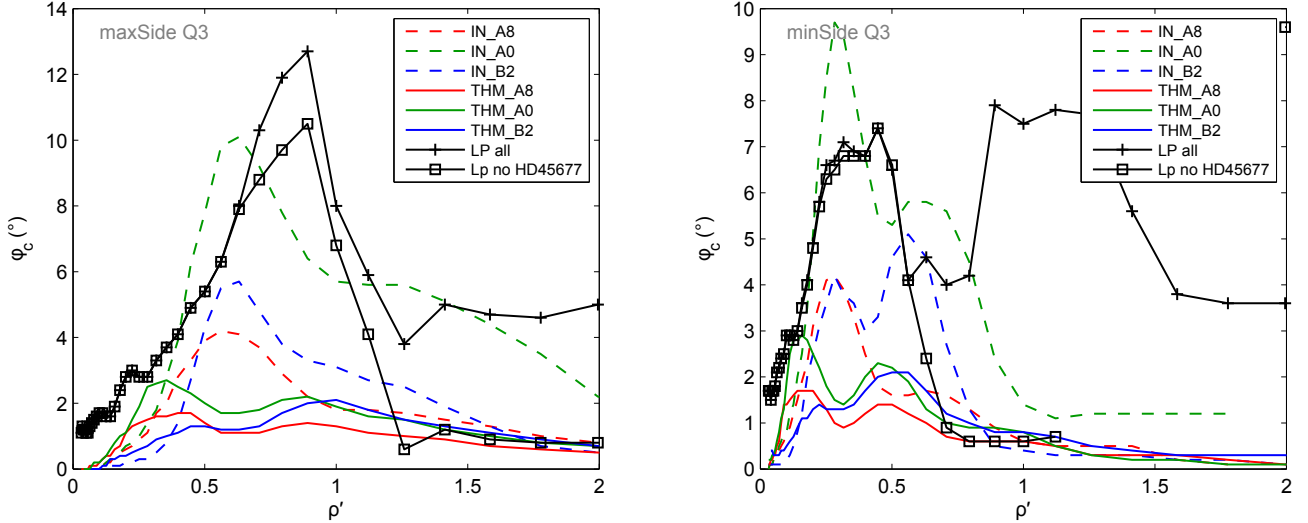


Fig. 16. Closure phase versus dimensionless resolution. *Left side*: resolution defined by largest side of triangle; *right side*: resolution measured by smallest side of triangle. Black, crosses: LP (non-binary) objects; black, squares: excluding HD 45677 (see text). Similar plots are also shown for the IN and THM MCFOST models in the three variants according to the central star.

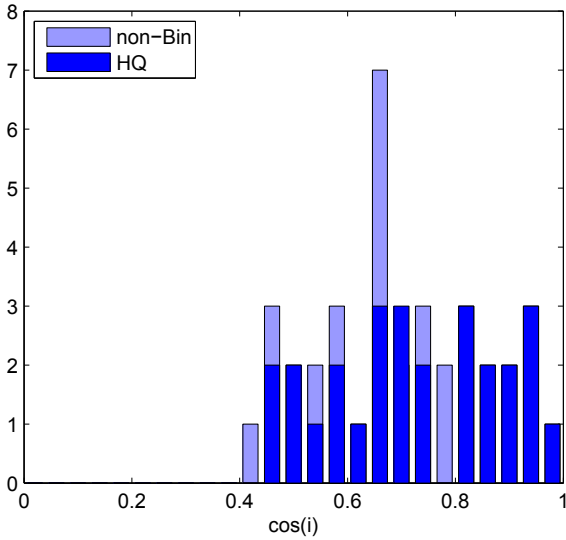


Fig. 17. Histogram of fit values for $\cos i$. The histogram for the 27 objects of the HQ sub-sample, fitted with the Ring model is superimposed over the histogram for the 44 non-binary objects, fitted with the Ellipsoid model. Parameter $\cos i$ is in fact robust: its value is not sensitive to the particular fit model used.

non-binary objects; the result is shown in Fig. 18. One can see that the histogram has a cutoff around 0.5. One object, CO Ori, is outside the limits of the histogram, at $f_{\text{rep}} = 1.64$; that object has a significant extinction $A_V \approx 1.2$ and a spectral type G5, atypical for the HAeBe class.

The value of f_{rep} would have a straightforward geometrical interpretation in the case of a disk rim fully opaque to incident stellar radiation, but optically thin for re-emitted dust radiation; in that case, its value is simply the solid angle, as seen from the star, intercepted by the rim. Because of (a) the self-occultation of the disk in the NIR; and (b) some dependence of the emergent radiation on the inclination relative to the local normal direction, one can expect the reprocessed fraction f_{rep} to depend on the inclination.

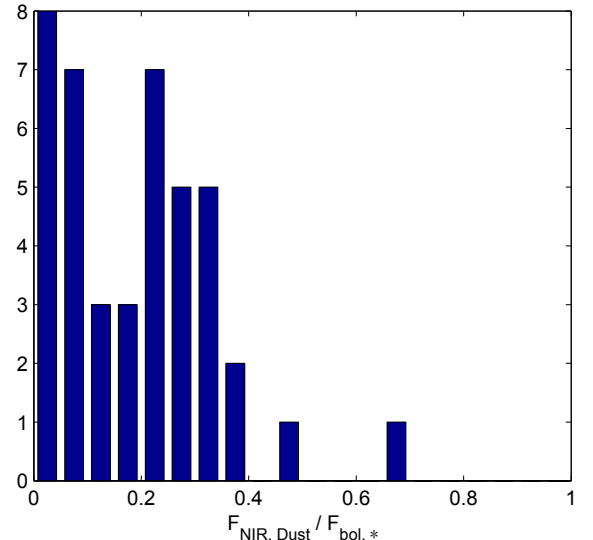


Fig. 18. Histogram of the fraction f_{rep} of stellar bolometric luminosity reprocessed to near infrared for non-binary objects.

We can, however, compare the median value of the observed sample with the similar metric for a model disk to derive a typical value. The median values of f_{rep} are: for the 44 LP non-binary objects: 0.18; for the *in_A0* MCFOST models: 0.19; for the *thm_A0* models: 0.18. The median for MCFOST models is restricted to inclinations for which the extinction of the central star $A_V < 3$. Remember (Sect. 4.2) that the thickness of the IN and THM models was adjusted to achieve such an agreement. The scatter of f_{rep} seen in Fig. 18 probably reflects the diversity of the objects included in our sample.

There is, in principle, a flaw in this procedure. In the previous subsection we argued that the flaring of the outer disk restricts the observed HAeBe disks to the inclination range $1 \geq \cos i \geq 0.45$, while we are now calibrating the observed statistics of f_{rep} against models without any outer flaring, that remain observable over a wider range of inclinations, typically

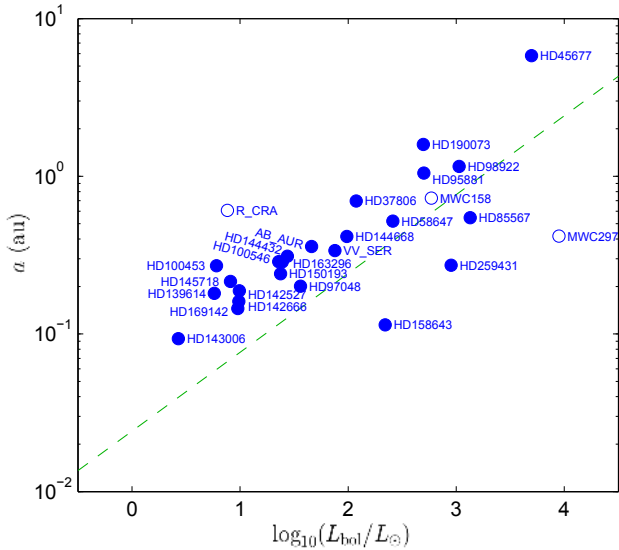


Fig. 19. Luminosity-radius plot for HQ objects. Open symbols denote three objects for which either the dust emission is dominant in H band ($f_d > 0.90$) or the extinction is large ($A_V > 5$). The dashed line shows, as a reference, the sublimation radius $a_{\text{sub},1800}$ for sublimation temperature $T_{\text{sub}} = 1800$ K, cooling efficiency $\epsilon = 1$, and backwarming factor $Q_{\text{bw}} = 1$.

$1 \geq \cos i \geq 0.2$. However, the model with the strongest dependence of f_{rep} versus inclination (a vertical-wall rim) is known, even before the present work, to be incompatible with the visibility curve. The favored THM model has only a weak dependence: $\Delta f_{\text{rep}}/\Delta \cos i \approx 0.1$. This means that selection effects on $\cos i$ do not affect significantly our determination of the thickness z/r of the inner disk.

Another question is: why should the geometrical interpretation of the reprocessed fraction be correct? After all, the albedo of the grains in our models is close to 0.5 over the range of stellar photon wavelengths. But the diffusion is strongly forward-peaked; in MCFOST, with the Mie treatment, for $a = 1.2 \mu\text{m}$ grains, and at 450 nm, the phase function drops to half the peak value within $\approx 5^\circ$ of the forward direction; so, diffusion will not hinder absorption. The situation is of course different for $1.65 \mu\text{m}$ stellar photons diffused off grains (typically $\approx 0.1 \mu\text{m}$) in the outer parts of the disk's surface.

Summarizing the results of the previous and present section, we find typical values $z/r \approx 0.2$ for the inner disk, and $z/r \approx 0.45$ for the outer disk are needed to match the statistics of f_{rep} and $\cos i$. The value $z/r \approx 0.2$ is known from previous work (see e.g., Vinković et al. 2006, Mulders & Dominik 2012 and references therein) to be larger by a factor of approximately two than predicted by hydrostatic models. See discussion in Vinković (2014). One possibility is that magnetic support increases the disk thickness over the hydrostatic value, as proposed by Turner et al. (2014).

4.8. Luminosity-radius relation

The disks of Herbig AeBe stars are thought to have an inner radius bounded by dust sublimation. This can be tested quantitatively via the luminosity-radius relation (Monnier & Millan-Gabet 2002; Monnier et al. 2005). We present in Fig. 19 the radius-luminosity diagram for the 27 objects of the HQ sub-sample. It is prepared as follows: (a) our SED fit provides a de-reddened m_V ; (b) using

Simbad spectral types (Table 1) and bolometric corrections from Pecaut & Mamajek (2013), we derive bolometric apparent magnitudes m_b ; (c) using parallaxes from HIPPARCOS (Perryman et al. 1997) we convert m_b to absolute luminosity L_b and angular to linear radius. Some of our HQ central stars have benefited from detailed spectral studies: 15 of them by Fairlamb et al. (2015), and one by Montesinos et al. (2009); see Table 1. For these objects the value of L_b derived as outlined above and the distance were superseded by the (presumably more reliable) values from these two references. Note that an error on the distance of an object moves the corresponding point in the diagram parallel to the theoretical $\log L - \log a$ line; so, accurate distances are not critical to establish a possible correlation.

On the same plot, we have drawn the (or rather a) theoretical luminosity-radius relation. Such a relation is defined by Tuthill et al. (2001); Monnier & Millan-Gabet (2002) mention and neglect backwarming, i.e. treat the equilibrium temperature of an isolated dust grain, while Kama et al. (2009) explicitly consider backwarming in the range from $C_{\text{bw}} = 1$ to $C_{\text{bw}} = 4$, the latter value being implicitly used by Dullemond et al. (2001). The rim radius can be written as:

$$\begin{aligned} R_{\text{rim}} &= \frac{1}{2} (C_{\text{bw}}/\epsilon)^{1/2} (T_*/T_{\text{sub}})^2 R_* \\ &= \frac{1}{2} (C_{\text{bw}}/\epsilon)^{1/2} (L_{\text{bol}}/4\pi\sigma T_{\text{sub}}^4)^{1/2}, \end{aligned} \quad (14)$$

where $\epsilon = Q_{\text{abs}}(T_{\text{sub}})/Q_{\text{abs}}(T_*)$, the cooling efficiency, is the ratio of Planck-averaged absorption cross-section for the considered grain species.

The line drawn in Fig. 19 expresses Eq. (14) with $T_{\text{sub}} = 1800$ K, $\epsilon = 1$ and $C_{\text{bw}} = 1$. The sublimation temperature is fixed (see Sect. 4.1.1 above). The values assigned to the other two are, however, arbitrary, and the relation as represented is best called a reference, rather than theoretical, relation.

Several factors can cause the actual objects to deviate from that reference: (1) ϵ is expected to be ≤ 1 , reaching unity for large ($a_{\text{grain}} > \lambda_{\text{NIR}}/(2\pi)$) grains. Tuthill et al. (2001) argue that the largest grains (largest ϵ) are the last survivors, but one needs to assume that grain growth indeed proceeds to $\approx 0.5 \mu\text{m}$ size; (2) the value adopted for the reference line, $C_{\text{bw}} = 1$ is the smallest possible; (3) the observed radius, with limited spatial resolution, is not the inner rim radius, but an effective radius for the H -band emitting region, that will in all cases be larger than the inner rim radius.

All three of the listed factors tend to make the measured radius larger than the reference radius (at a given luminosity). To investigate this quantitatively, we display in Fig. 20 the histogram of the ratio $r_{\text{norm}} = a_{\text{fit}}/a_{\text{sub},1800}$ of these two radii. The median value is $\text{median}(r_{\text{norm}}) = 2.0$. Note that the sublimation temperature of the grain material is not used as an adjustment variable.

Still using our procedure of substitution weighting, we process, with the same fitting procedure, images from three types of MCFOST models: (1) the IN model achieves values of r_{norm} in the range 1–2, mostly due to backwarming; (2) the THM model achieves larger values of r_{norm} than the IN model, due to the larger radial extent of the H -band emitting region; it does not, however, seem to match the observed values; (3) a third model, THMC, is similar to THM, but with smaller grain sizes and correspondingly smaller ϵ values: $0.147 \mu\text{m}$ ($\epsilon = 0.14$) and $0.235 \mu\text{m}$ ($\epsilon = 0.28$); the range of r_{norm} values is correspondingly larger.

Taken together, the three models IN, THM, and THMC can account for a spread of r_{norm} over the range 1–4. HD 100453

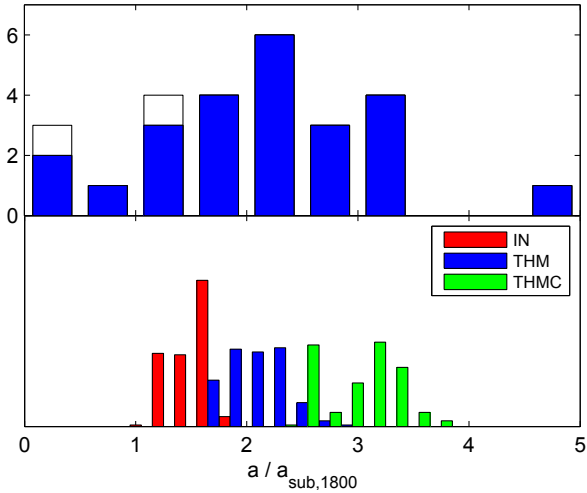


Fig. 20. *Top panel:* histogram of the ratio of the fitted half-light radius a to $a_{\text{sub},1800}$, the rim radius for a sublimation temperature of 1800 K and no backwarming. The open blocks in the bars have the same meaning as in Fig. 19. One outlier, R CrA is beyond the plot limits with $r_{\text{norm}} \approx 9$. *Bottom panel:* histograms produced from simulated observations and parametric fits to three types of MCFOST models, each for three central star types: A8, A0, and B2.

($r_{\text{norm}} = 4.5$) exceeds that range by a small amount, while the five objects with $r_{\text{norm}} < 1$ that can be identified in Fig. 19 are more problematic. The objects with the four lowest values of r_{norm} , ranging between 0.18 and 0.59, all have dust temperatures (see Sect. 3.1) below 1760 K, so that anomalous refractory grains cannot be invoked. Anticipating the results displayed in Fig. 23, we also see that an H -band emission component located inside the sublimation rim cannot plausibly explain a fit radius smaller than the reference radius.

4.9. Extended component

Our data show the presence of a fully resolved flux in a significant fraction of our sample. This is quantified by the f_h fitted parameter, which is a fraction of the total H -band flux in the instrument's field of view. This can be attributed to a spatially extended emission⁴; see for example, Fukagawa et al. (2010, their Table 5).

Based on ISO spectra Meeus et al. (2001) defined two types of Herbig Ae Be stars: group I are stars for which the mid-infrared continuum spectrum can be modeled with one power law and one additional black-body to reproduce the rising mid-IR continuum; group II objects only require the power law. In subsequent mid-IR spectroscopy studies van Boekel et al. (2005) and Juhász et al. (2010) noticed that both groups could be sorted apart in a diagram involving the near-infrared (J , H , K , L and M) to far infrared flux ratio (IRAS 12, 25 and 60 μm) and the IRAS color $m_{12} - m_{60}$ ⁵. These parameters have been considered as indicators of respectively the ratio between the flux intercepted by the inner rim and the outer disk and the degree of flaring.

We explored whether we could find a correlation between such indicators and our own estimator of extended flux (see

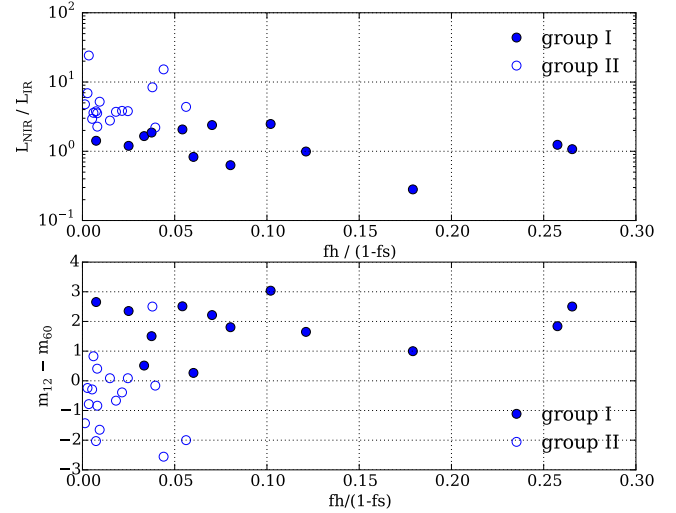


Fig. 21. Fractional flux f_h of the halo component of objects versus their infrared color.

Fig. 21). The latter was constructed as the ratio between the extended flux fraction f_h and the global excess fraction $1 - f_s$. We do find a clear indication that objects with a higher ratio of near infrared to infrared flux display small fully resolved flux while higher mid infrared color indices are correlated with higher extended flux. This fits well in the scenario where indeed group I and group II are objects with significantly different large scale near to far infrared emission.

We remind the reader of the discussions (Maaskant et al. 2013; Menu et al. 2015) concerning the exact nature of the group I/II classification and the attempts to introduce notions of disk evolution (e.g., dust settling) and planet formation (e.g., gap clearing). It has even been proposed that the near-infrared fully resolved flux might be caused partly by scattering off the inner rim of an outer disk in a transitional disk containing a large gap (Benisty et al. 2010b; Tatulli et al. 2011). We note that the f_h parameter provides a limited spatial information and do not wish to speculate more on its exact origin. In particular we recall that single-mode observations have a very restricted field of view, for PIONIER a Gaussian of roughly 200 mas field of view, which introduces a bias in the gap detection capability. But, nevertheless, it would certainly be interesting to correlate it with other planet formation evidence.

4.10. Inner gaseous disks

The possibility of an inner gaseous disk located inside the dust sublimation rim of Herbig objects has drawn some attention in recent years, from several different viewpoints. Firstly, as logically unavoidable if the dusty disk must feed accretion at or near the stellar surface (Muzerolle et al. 2004). Second, a number of authors have directly detected gas inside the dust sublimation radius of various Herbig objects via spectrally resolved interferometry in the Bry line, for example: Kraus et al. (2008a), Eisner et al. (2009), Caratti o Garatti et al. (2015), Kurosawa et al. (2016), Mendigutía et al. (2015), Ilee et al. (2014). Third, continuum (or low spectral resolution) observations, for example, Eisner et al. (2007), Isella et al. (2008), Kraus et al. (2008b), Tannirkulam et al. (2008b,a), Benisty et al. (2010a), infer the presence of an additional component inside the dust sublimation radius, that can be uniform, ring-like, or compact; note that the authors of the last paper argue in favor of

⁴ Larger than the PIONIER interferometric field of view (FOV), but smaller than its photometric FOV.

⁵ Group I sources are defined as sources with $L_{\text{NIR}}/L_{\text{IR}} \leq (m_{12} - m_{60}) + 1.5$.

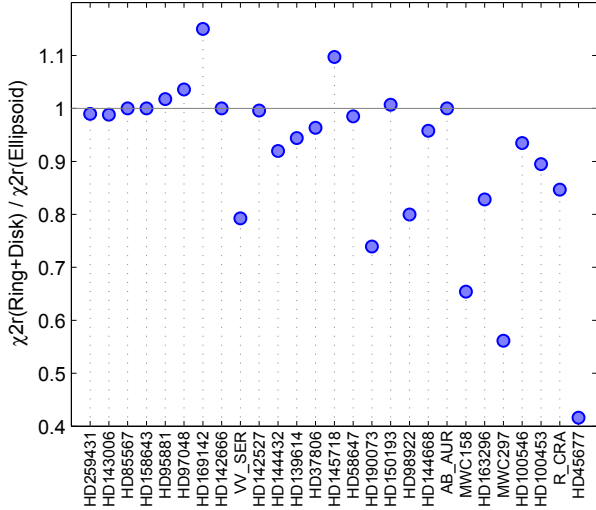


Fig. 22. Value of χ^2 achieved for the ring + inner disk models, normalized by the value for the Ellipsoid model; similar to Fig. 12. The χ^2 achieved by the ring + inner disk model is, in some cases, worse than for the Ellipsoid model; this is because in contrast with the results shown in Fig. 12, the more complex model does not comprise the simpler one as a subset.

an inner refractory dust disk. Fourth, some authors have investigated the opacities and/or the emitted spectrum from a gaseous disk as might be found inside the dust sublimation radius; see Malygin et al. (2014), Vieira et al. (2015), with the former authors concluding that the thermal equilibrium problem may be multi-valued.

In view of the diversity of spatial distributions that have been proposed for the inner disk continuum emission, and that cannot at present be tied to a physical model, we could not submit the hypothesis of dust rim plus inner gas disk to the same systematic tests as we did in the previous subsections for the dust-rim-only hypothesis. The issue is not the presence of gas inside the dust sublimation radius, for which the Bry observations provide direct evidence. But, line opacities being typically several orders of magnitude larger than continuum ones, this does not prove that an inner disk should be a significant contributor to the continuum image and visibilities.

Nevertheless, we did a simple test of a model comprising:

- a ring similar to the Ring model used above, except that an elastic constraint enforces $l_{kr} = -0.3 \pm 0.15$, corresponding to a relative width $w' \approx 0.45_{-0.11}^{+0.13}$, intervals corresponding to $\Delta(\chi^2) = 1$. Such rims are narrower than any of the fit results in Fig. 13;
- a disk with a structure like the Ellipsoid model used above, and again with an elastic constraint $\log_{10}(a_{\text{disk}}/a_{\text{ring}}) = 0 \pm 0.1$, both a values being half-light radii, and the interval given, again, for $\Delta(\chi^2) = 1$.

We show just two results of this experiment. Figure 22 shows the improvement in χ^2 from an Ellipsoid fit to a ring+disk model. Comparing with Fig. 12, one can see that the two are quite similar. Figure 23 compares the values obtained for the ring radius in the present versus the Ring model fit; again, the values are quite similar: the ratio has a mean of 0.975 and a standard deviation of 0.107.

What can we gather from this limited test of the ring+disk model? The results are quite close to those of the Ring model. With our data, we have typically just enough resolution and precision to distinguish between a sharp rim and any other structure

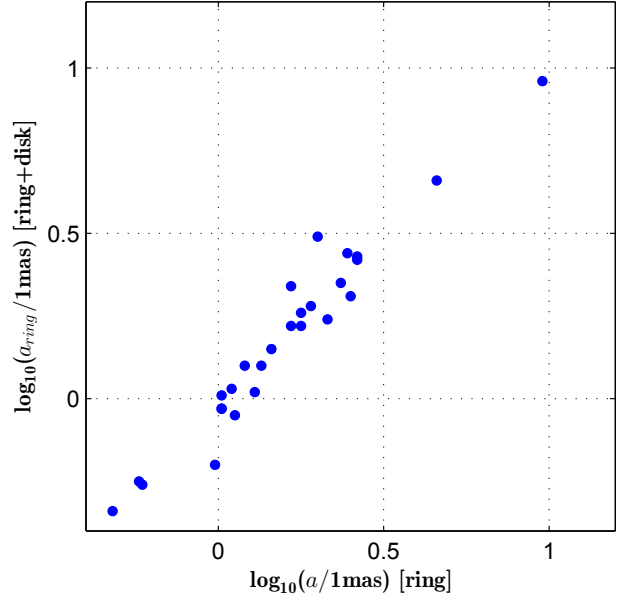


Fig. 23. Relationship between ring radii derived in the ring + disk model and the previous Ring model.

with a more damped visibility versus resolution curve, whether that is a wide rim, or a narrow one combined with an inner disk, central clump, or smaller ring.

5. Summary and conclusions

We have presented interferometric H -band observations of 51 Herbig AeBe objects, of which 44 have a non-binary star, and 27 have been classified high quality (HQ) on the basis of the resolution achieved; a dedicated and homogeneous set of photometric measurements was also acquired.

The spatial resolution achieved for a significant part of our sample allowed us to go beyond just size determinations, but, for most objects, was not sufficient to produce images. In order to make the fullest use of our data set, we examined the statistics of structural parameters obtained by fitting simple geometrical templates: ellipsoids and rings. We separately generated a small number of physical models of dust disks irradiated by the central star; they were observed with a uv coverage similar to actual sample object, and these synthetic observations were in turn fitted exactly like the real observations. This allowed us to (i) eliminate possible biases of our fitting process; (ii) make statements on physical models, and not just on structural parameters.

We have established, or confirmed, a number of properties of the dusty environment of HAeBe objects, that we summarize below under headings corresponding to the four goals spelt out in the Introduction.

5.1. Can we constrain the radial and vertical structure of the inner disk?

Radial structure. We have confirmed the presence of a ring-shaped structure (that tends to be taken for granted) in the Herbig objects of our sample, in several ways. First, for a substantial number of objects, fitting a ring structure results in a lower reduced χ^2 than fitting an ellipsoid, this being more marked for the better resolved objects. Second, performing a parametric fit that allows both an ellipsoid or a ring shape, with a continuous transition, for a number of objects, a ring shape is preferred. Also,

when a ring shape is preferred, it is a wide ring, with $w > 0.4$, where w is the ring width normalized by the global half-light radius. This excludes “fat” rim geometries with a substantial curvature radius and favors wedge-shaped rims, concurring with several recent physical models.

Luminosity-radius relation. We confirm the known luminosity-radius relation. The observed spread can be explained in part by variations in the rim geometry and in the maximum grain size, but a few objects have radii that are smaller than expected. The observed spread in sublimation temperatures can only be a minor contributor to the luminosity-radius scatter.

Vertical structure. The statistics of the reprocessed fraction (from the star’s bolometric flux to the dust’s NIR flux) allow us to infer a thickness $z/r \approx 0.2$ for the inner (meaning close and hot enough to radiate in the NIR) region of the dusty disk. The statistics of inferred inclination show a histogram populated only at $\cos i > 0.45$, that we interpret as resulting from self-obscuration by the outer parts of a flared ($z/r \approx 0.5$) disk.

5.2. Can we constrain the rim dust temperature?

We find that the dust responsible for the NIR emission of our sample objects has a sublimation temperature definitely larger than 1500 K, the favored value being 1800 K. This result is obtained by using radiative transfer models to calibrate out both the spread of temperatures in any real object, and possible biases in our fit procedure. Relating a sublimation temperature to dust properties is a difficult task, considering the range of the physical conditions and possible time-dependent effects. Accordingly, we abstain from discussing dust composition.

5.3. Can we constrain the presence of additional emitting structures?

Extended component. We find in a significant fraction of our sample a spatial component that is fully resolved at the shortest spacings ($B/\lambda \approx 5 \times 10^6$), i.e. an angular scale larger than 40 mas. We also find that the presence and relative flux of that component are correlated with the Herbig group, either the original categorical form or based on infrared colors. Diffusion of starlight off a flared disk might be the cause of such extended components, but there may be other viable mechanisms.

Inner disk. Our conclusion (above) that rims are wide results essentially from the (near-)absence of bounce in the visibility curve beyond the first minimum. A number of authors have interpreted similar observations as resulting from an extra component (hot gas, very refractory grains?) inside the dust sublimation radius. Such an alternate explanation, while viable, is loosely constrained, lacking a predictive physical model.

5.4. Can we reveal deviation from axisymmetry?

Azimuthal modulation. Fit models that include azimuthal modulation result in lower values of χ_r^2 ; such azimuthal modulation is expected from self-shadowing of an inclined rim. To probe further that agreement between observations and models, we also tested the alignment of the modulation; we find a suggestive, but not overwhelming, agreement with the expected alignment.

Phase closures. This item is closely related to the previous one, except (a) model-independent, and (b) only odd azimuthal orders contribute. Phase closures versus resolution show, as expected, a maximum near dimensionless resolution $\rho' \approx 0.5$. The value of the maximum is of order $\phi_{cp} \approx 10^\circ$; one of our physical models (IN) comes close to this value, but the other one (THM) peaks much lower, at $\phi_{cp} \approx 2^\circ$; we leave this point open for future work.

5.5. Outlook

Our understanding of the structure and physics of Herbig AeBe objects would benefit, in our opinion, from: (a) an increase in angular resolution of NIR interferometric observations by a modest factor (between two and three), that would provide a decisive improvement for all the objects that are marginally resolved with current data; (b) the continuation and extension of theoretical or numerical models of the inner disk regions, notably with the following issues in mind: the shape of the rim; its vertical structure and hydrostatic equilibrium; a comprehensive treatment of the dusty rim and the inner gaseous disk; the deviations from axisymmetry.

Acknowledgements. Based on observations made with ESO Telescopes at the La Silla Paranal Observatory under programme ID 190.C-0963. Generous time allocations by SAAO are gratefully acknowledged. We are grateful to Francois Van Wyk for diligently carrying out the infrared part of the photometry at Sutherland. J.K. acknowledges support from a Marie Skłodowska-Curie CIG grant (Ref. 618910, PI: Stefan Kraus). J.D.M. and F.B. acknowledge support from NSF-AST 1210972. Part of the research was carried out at the Jet Propulsion Laboratory, California Institute of Technology, under a contract with the National Aeronautics and Space Administration. This research has made use of: the Jean-Marie Mariotti Center Aspro2 and SearchCa1 services⁶; the SIMBAD database, operated at CDS, Strasbourg, France; and data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology. This work has made use of data from the European Space Agency (ESA) mission *Gaia* (<http://www.cosmos.esa.int/gaia>).

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⁶ Available at <http://www.jmmc.fr/aspro>

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Appendix A: MCFOST models used for double-weighting the parametric fits

Here we describe in more details the MCFOST models used in conjunction with the parametric fits. We populate the inner rim region with grains having the highest sublimation temperature, meaning carbon grains (see Sect. 4.1.1), and the lowest equilibrium temperature, meaning large grains; altogether, the grains at the inner rim are the fittest for survival. We use in the MCFOST program amorphous carbon grains, with the optical constants from Rouleau & Martin (1991). Figure A.1 shows, versus grain radius a , the cooling efficiency ϵ , the ratio of the Planck-weighted averages of the absorption cross-section at, respectively, the dust and star temperatures.

Our IN05-inspired model, labeled IN, has a curved inner rim and a single grain radius: $1.2 \mu\text{m}$. Our THM07-inspired model, labeled THM, has two grain radii: $1.2 \mu\text{m}$ and $0.35 \mu\text{m}$; the smaller grains, because of their smaller emissivity in the NIR, cannot survive quite as close to the star as the larger grains, but, where they survive, their equilibrium temperature is higher than for larger grains, which helps to achieve a radially extended H -band emission. As explained in Tannirkulam et al. (2007), the respective spatial distributions of the two grain species result naturally from differential sedimentation and differential sublimation. In the present work, however, the spatial distributions are ad hoc, subject to the condition that the maximum temperature for each species is equal to the assumed sublimation temperature $T_{\text{sub}} = 1800 \text{ K}$. Both the geometry and the range of grain sizes contribute to the THM model having a broader radial distribution of H -band emission than the IN model. The information provided in Fig. A.2 complements that already given in Fig. 11.

We simulate observations of each MCFOST model as follows: (1) we vary the inclination with values of $\cos(i)$ at the centers of 10 uniform bins; (2) we vary the distance in steps of $10^{0.1}$ subject (for each inclination) to the magnitude limits of our HQ sub-sample: $4 \leq H \leq 8$; note that we claim neither that our sample is complete within these limits, nor that the distribution of distances in our simulated sample matches the observed sample, but we believe that this serves sufficiently well our purpose: to reveal trends while avoiding possible systematic biases caused by parametric fitting; (3) for each combination of inclination and distance, the uv plane is sampled following the coverage of a typical Large Program object (HD 144668); noise is added; values of visibility squared V^2 and phase closure ϕ_{cp} are derived; (4) inclinations for which the V band extinction of the central star is in excess of three magnitudes are ignored; while the limit is somewhat arbitrary, heavily obscured central stars will not appear in lists of HAeBe objects.

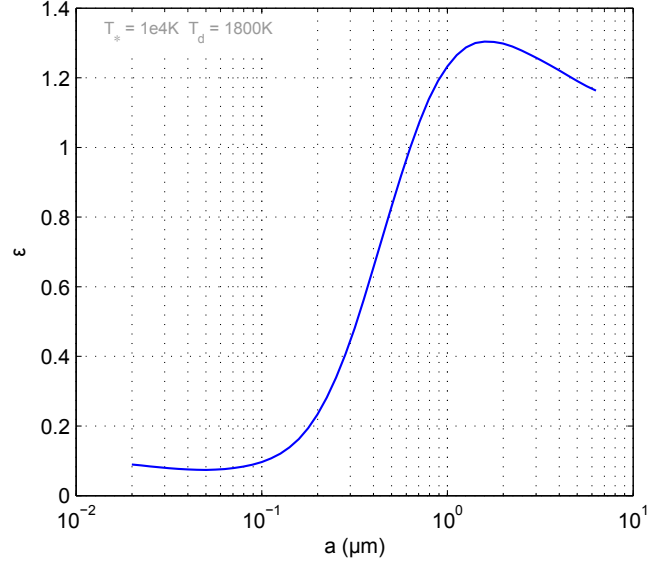


Fig. A.1. Cooling efficiency ϵ as a function of grain size, for the material adopted in our MCFOST simulations: amorphous carbon. The plot is made for $T_d = 1800 \text{ K}$ and $T_* = 10000 \text{ K}$.

Table A.1. Comparison of statistical error estimates for LP data and actual added noise for MCFOST models.

	Vis. squared V^2	Ph. closure ϕ_{cp}
LP	0.016	1.52°
Models	0.019	1.84°

Notes. We use the median metric rather than root-mean-square to avoid giving an excessive weight to a few atypically bad observations.

Simulated noise is added to the model's complex visibilities; the resulting noise for the (real) observables V^2 and ϕ_{cp} has median values slightly larger than the median values for the error estimates derived by the data reduction software for the real LP objects. We feel that matching the median error between real and simulated data is adequate for our purposes, and that a discussion of noise models for interferometric data is outside the scope of this work. We do not attempt to simulate the calibration errors or other systematic errors.

Finally, the simulated observations of the MCFOST models are subject to the same parametric model fitting as the observational data.

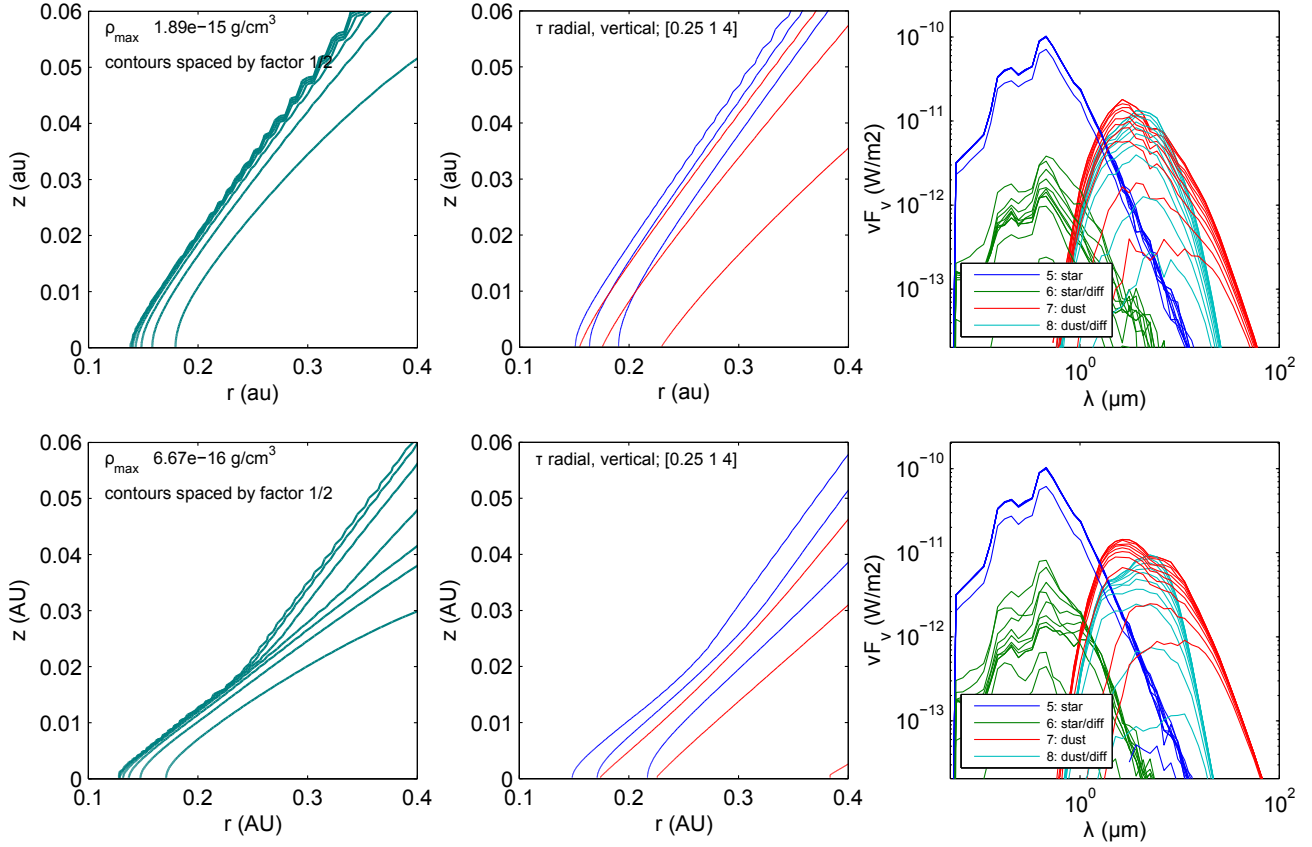


Fig. A.2. Properties of the IN and THM models, complementing those of Fig. 11. *Top row:* IN; *bottom:* THM. *Left to right:* dust mass density contours; contours of radial (blue) and vertical (red) optical depth at values $\tau = 0.25, 1.0, 4.0$; several components of the SED at each of ten inclinations; blue: stellar photosphere; green: ditto, diffused by dust; red: thermal dust emission; cyan: ditto, diffused by dust.

Appendix B: Results of photometric and interferometric fits**Table B.1.** Results of fits to the SED of program sources.

Object	χ_r^2	$\log_{10} F_{vsV}$		$A_{\text{mod},V}$		$\log_{10} F_{vdH}$		$\log_{10} T_d$		f_d	
HD 17081	0.124	-6.386	0.011	0.036	0.028	-10.841	0.848	3.134	0.280	0.001	0.002
AB AUR	1.002	-7.391	0.043	0.333	0.095	-7.864	0.017	3.260	0.017	0.780	0.021
HD 31648	1.012	-7.721	0.044	0.136	0.092	-8.442	0.049	3.221	0.041	0.592	0.046
HD 293782	0.589	-8.442	0.025	0.460	0.054	-9.082	0.023	3.192	0.018	0.666	0.021
HD 34282	0.234	-8.490	0.027	0.445	0.059	-9.314	0.030	3.244	0.024	0.607	0.028
CO ORI	1.010	-8.747	0.044	1.728	0.090	-8.727	0.023	3.244	0.021	0.790	0.021
HD 35929	0.967	-7.848	0.020	0.276	0.046	-9.330	0.159	3.145	0.088	0.145	0.049
MWC 758	0.210	-7.898	0.026	0.324	0.056	-8.496	0.023	3.217	0.020	0.658	0.023
HD 244604	0.084	-8.347	0.025	0.342	0.054	-9.110	0.027	3.224	0.023	0.623	0.025
HD 36917	0.511	-7.595	0.029	0.778	0.062	-8.987	0.083	3.301	0.067	0.330	0.054
T ORI	1.005	-8.756	0.126	0.469	0.277	-8.705	0.067	3.196	0.048	0.915	0.026
HD 37258	0.181	-8.410	0.026	0.330	0.056	-9.292	0.029	3.245	0.025	0.580	0.028
HD 37357	0.372	-8.163	0.027	0.254	0.059	-9.194	0.039	3.251	0.031	0.490	0.035
V 1247 ORI	0.355	-8.525	0.026	0.319	0.055	-9.208	0.031	3.216	0.025	0.595	0.028
HD 37411	0.035	-8.452	0.027	0.468	0.060	-9.236	0.023	3.229	0.022	0.635	0.024
HD 37806	1.136	-7.820	0.025	0.062	0.052	-8.499	0.037	3.180	0.030	0.676	0.026
HD 38087	1.250	-7.626	0.039	0.996	0.084	-9.164	0.084	3.461	0.040	0.323	0.059
HD 39014	0.344	-6.411	0.011	0.058	0.032	-10.536	1.020	3.097	0.310	0.001	0.003
HD 250550	0.616	-8.308	0.029	0.567	0.063	-8.791	0.016	3.245	0.015	0.802	0.014
HD 45677	1.001	-7.285	0.024	0.880	0.055	-8.262	0.045	3.032	0.027	0.655	0.030
HD 259431	1.002	-7.670	0.052	1.225	0.109	-8.429	0.031	3.245	0.029	0.720	0.035
MWC 158	0.257	-7.196	0.024	0.386	0.056	-7.929	0.020	3.213	0.017	0.714	0.018
HD 53367	1.308	-6.863	0.074	1.530	0.160	-8.271	0.157	3.426	0.080	0.382	0.117
HD 56895	0.617	-7.972	0.027	0.204	0.061	-7.749	0.014	3.189	0.010	0.905	0.006
HD 58647	0.091	-7.280	0.022	0.362	0.051	-8.605	0.064	3.148	0.039	0.364	0.043
HD 85567	1.008	-7.816	0.061	0.668	0.134	-8.482	0.046	3.217	0.046	0.748	0.039
HD 95881	0.094	-7.807	0.026	0.483	0.058	-8.403	0.020	3.211	0.018	0.734	0.018
HD 97048	1.008	-7.641	0.032	1.259	0.070	-8.640	0.043	3.242	0.035	0.539	0.040
HD 98922	0.130	-7.264	0.024	0.359	0.055	-8.047	0.026	3.173	0.020	0.657	0.023
HD 100453	0.288	-7.804	0.014	0.036	0.031	-8.785	0.049	3.109	0.030	0.375	0.031
HD 100546	0.904	-7.355	0.013	0.023	0.023	-8.710	0.059	3.189	0.042	0.318	0.034
HD 104237	0.197	-7.296	0.027	0.183	0.059	-8.034	0.029	3.260	0.028	0.577	0.028
HD 139614	0.370	-7.989	0.017	0.044	0.036	-9.081	0.053	3.161	0.034	0.350	0.033
HD 141569	0.583	-7.428	0.028	0.296	0.058	-9.225	0.182	3.391	0.101	0.144	0.056
HD 142666	0.632	-7.904	0.024	0.672	0.055	-8.657	0.035	3.177	0.025	0.524	0.030
HD 142527	0.681	-7.714	0.025	0.798	0.057	-8.267	0.032	3.225	0.025	0.535	0.029
HD 143006	0.304	-8.666	0.027	0.196	0.058	-9.039	0.038	3.215	0.031	0.488	0.035
HD 144432	0.183	-7.857	0.027	0.287	0.058	-8.615	0.034	3.250	0.030	0.521	0.033
HD 144668	0.281	-7.289	0.029	0.705	0.063	-7.874	0.021	3.283	0.021	0.693	0.022
HD 145718	0.197	-7.921	0.022	0.757	0.052	-9.066	0.060	3.205	0.045	0.348	0.040
HD 149914	1.600	-6.985	0.044	1.019	0.101	-8.973	0.862	3.400	0.172	0.105	0.098
HD 150193	0.214	-7.719	0.033	1.288	0.068	-8.173	0.017	3.297	0.019	0.770	0.018
AK SCO	0.293	-8.185	0.063	0.470	0.138	-8.901	0.095	3.191	0.055	0.408	0.085
HD 158643	0.236	-6.576	0.022	0.097	0.049	-8.507	0.341	3.161	0.184	0.109	0.067
HD 163296	0.215	-7.386	0.024	0.117	0.053	-8.083	0.023	3.203	0.020	0.669	0.021
HD 169142	1.371	-7.935	0.013	0.021	0.021	-9.416	0.145	3.217	0.100	0.147	0.042
MWC 297	1.001	-6.756	0.093	7.189	0.205	-7.040	0.061	3.220	0.044	0.914	0.020
VV SER	1.006	-8.211	0.033	3.052	0.069	-8.513	0.015	3.236	0.015	0.880	0.009
R CRA	1.003	-8.480	0.098	3.308	0.201	-7.568	0.051	3.127	0.025	0.992	0.002
HD 179218	0.256	-7.560	0.017	0.271	0.037	-8.749	0.048	3.173	0.034	0.406	0.032
HD 190073	1.002	-7.795	0.019	0.068	0.040	-8.584	0.031	3.195	0.026	0.601	0.024

Notes. The second value in a pair of columns is the 1σ estimate of the error derived from the scatter of the marginal distribution. A complete version of this table can be found at the CDS.

Table B.2. Values for the eight parameters of the fit of an Ellipsoid model.

Object	$\chi^2 r$	k_c	f_s	f_h	$\cos i$	θ (rad)	f_{Lor}	l_a	f_c
HD 17081	0.17	1.66	0.96	0.00	0.76	-0.20	0.00	-0.13	0.04
AB AUR	0.40	-5.85	0.19	0.03	0.98	2.14	0.27	0.32	0.78
HD 31648	0.45	-0.48	0.42	0.01	0.78	2.23	0.16	0.28	0.57
HD 293782	3.33	-	0.33	0.00	0.87	1.54	0.66	-0.10	0.67
HD 34282	2.13	-	0.30	0.08	0.41	2.29	0.33	-0.08	0.62
CO ORI	1.06	-5.22	0.22	0.00	0.66	0.67	0.42	-0.23	0.78
HD 35929	0.59	-1.06	0.86	0.00	0.85	0.27	0.00	-0.25	0.14
MWC 758	0.11	-3.32	0.33	0.02	0.66	1.74	0.05	0.13	0.65
HD 244604	0.00	-	0.38	0.00	0.58	0.35	0.64	-0.24	0.62
HD 36917	1.19	-5.82	0.69	0.03	0.01	1.67	0.50	-0.58	0.29
HD 37258	1.51	-	0.42	0.00	0.41	2.48	0.01	-1.63	0.58
V 1247 ORI	0.99	-	0.38	0.03	0.89	3.08	0.14	-0.36	0.59
HD 37411	0.29	-	0.36	0.00	0.45	2.00	0.46	-0.18	0.64
HD 37806	3.87	-3.54	0.23	0.01	0.77	0.75	0.37	0.16	0.76
HD 39014	1.85	1.97	0.91	0.01	0.59	0.65	0.03	0.07	0.08
HD 250550	0.36	-	0.17	0.03	0.62	2.31	0.17	-0.13	0.79
HD 45677	13.77	-4.11	0.40	0.00	0.73	1.22	0.00	0.99	0.60
HD 259431	0.99	-5.39	0.25	0.02	0.91	0.66	0.59	-0.34	0.73
MWC 158	7.77	-5.75	0.14	0.02	0.56	1.20	0.98	0.31	0.84
HD 58647	1.36	-4.90	0.59	0.02	0.48	0.23	0.24	0.19	0.39
HD 85567	1.37	-3.36	0.23	0.00	0.76	2.02	0.30	-0.27	0.77
HD 95881	1.13	-5.50	0.27	0.04	0.65	2.74	0.75	-0.00	0.69
HD 97048	0.84	-4.18	0.47	0.04	0.53	2.90	0.71	0.03	0.49
HD 98922	6.81	-6.00	0.17	0.01	0.92	0.98	0.78	0.25	0.82
HD 100453	2.00	-5.97	0.58	0.11	0.67	1.42	0.09	0.39	0.31
HD 100546	4.44	-3.42	0.48	0.11	0.66	2.58	0.57	0.37	0.42
HD 139614	1.06	-5.74	0.54	0.06	0.83	0.18	0.89	0.11	0.41
HD 141569	0.61	0.22	0.86	0.00	0.21	1.92	0.80	-0.53	0.13
HD 142666	1.53	-3.64	0.44	0.02	0.50	2.82	0.41	0.03	0.54
HD 142527	2.52	-3.90	0.41	0.03	0.83	0.12	0.43	0.06	0.56
HD 143006	0.85	-4.64	0.48	0.03	0.89	0.01	0.19	-0.30	0.49
HD 144432	1.63	-2.66	0.43	0.00	0.90	1.38	0.86	0.09	0.57
HD 144668	2.84	-2.64	0.38	0.00	0.59	2.18	0.25	0.27	0.62
HD 145718	1.02	-2.88	0.59	0.03	0.45	0.03	1.00	0.15	0.38
HD 149914	0.51	1.76	0.88	0.00	0.87	0.85	0.05	-0.46	0.12
HD 150193	1.43	-3.18	0.30	0.00	0.82	2.12	0.77	0.21	0.70
HD 158643	0.57	-2.25	0.83	0.01	0.65	2.13	0.88	0.03	0.16
HD 163296	1.56	-3.72	0.24	0.00	0.68	2.24	0.41	0.34	0.76
HD 169142	1.00	-5.99	0.76	0.08	0.93	1.81	0.88	-0.01	0.17
MWC 297	9.84	-5.64	0.11	0.01	0.89	1.65	0.00	0.36	0.87
VV SER	2.35	-5.97	0.08	0.02	0.52	0.02	0.50	0.03	0.90
R CRA	4.88	-1.42	0.04	0.06	0.69	0.12	0.52	0.63	0.90
HD 179218	2.55	-2.46	0.58	0.02	0.66	0.50	0.03	1.38	0.40
HD 190073	1.83	-3.19	0.34	0.00	0.93	2.88	0.00	0.19	0.66

Notes. This fit was performed on the 44 non-binary program objects. See Table 6 for symbol details. No value is given for the spectral index k_c of the circumstellar component for those objects where 50% or more of the observations were made in non-dispersed mode. Error bars are not shown because of page width limitation; a complete version of this table can be found at the CDS.

Table B.3. Values for the eleven parameters of the fit of a Ring model with first order azimuthal modulation.

Object	$\chi^2 r$	k_c	f_s	f_h	$\cos i$	θ (rad)	f_{Lor}	l_a	f_r	l_{kr}	c_1	s_1
AB AUR	0.79	-5.75	0.24	0.03	0.91	1.40	0.31	0.37	0.73	0.08	0.97	0.18
HD 37806	2.61	-1.73	0.34	0.00	0.75	0.79	0.94	0.22	0.66	-0.18	0.08	-0.13
HD 45677	5.59	-4.12	0.42	0.03	0.63	1.20	1.00	0.98	0.55	-0.26	-0.18	0.98
HD 259431	1.43	-5.18	0.27	0.02	0.98	0.82	0.99	-0.35	0.71	-0.13	0.05	-1.00
MWC 158	21.53	-3.25	0.24	0.12	0.53	1.26	1.00	0.33	0.63	-0.08	1.00	-0.02
HD 58647	1.41	-3.98	0.65	0.02	0.47	0.23	0.66	0.25	0.33	-0.30	-0.07	-0.26
HD 85567	1.15	-2.04	0.29	0.00	0.79	2.10	0.38	-0.22	0.70	0.09	0.28	-0.96
HD 95881	1.41	-4.44	0.32	0.05	0.62	2.73	0.85	0.05	0.64	0.15	-0.99	-0.15
HD 97048	0.81	-3.84	0.48	0.04	0.56	2.89	0.85	0.05	0.48	0.07	0.60	0.78
HD 98922	5.83	-5.85	0.21	0.03	0.94	1.20	0.90	0.25	0.76	0.25	0.42	-0.66
HD 100453	1.29	-5.31	0.61	0.09	0.66	1.41	0.83	0.42	0.30	-0.21	0.01	0.03
HD 100546	3.96	-2.43	0.55	0.11	0.69	2.66	1.00	0.42	0.34	-0.22	0.17	-0.17
HD 139614	1.02	-5.56	0.57	0.06	0.85	0.25	1.00	0.14	0.37	0.16	0.16	-0.59
HD 142666	1.36	-4.18	0.45	0.02	0.50	2.84	0.58	0.03	0.53	0.13	-0.04	0.00
HD 142527	2.27	-3.67	0.42	0.03	0.84	0.09	0.42	0.08	0.55	0.54	-0.60	-0.57
HD 143006	0.86	-4.26	0.50	0.03	0.88	2.94	0.66	-0.25	0.47	-0.51	0.61	0.20
HD 144432	1.75	-2.41	0.45	0.00	0.91	1.35	0.99	0.09	0.55	0.32	-0.18	0.81
HD 144668	3.27	-2.48	0.40	0.00	0.61	2.22	0.21	0.30	0.60	0.20	-0.39	0.92
HD 145718	1.11	-2.82	0.60	0.03	0.47	0.03	1.00	0.16	0.37	0.77	0.18	-0.86
HD 150193	1.84	-2.69	0.33	0.00	0.85	2.13	0.82	0.22	0.67	0.39	0.24	-0.97
HD 158643	0.64	-2.38	0.81	0.01	0.66	2.15	0.98	-0.06	0.18	0.47	-0.82	-0.51
HD 163296	2.18	-2.64	0.32	0.00	0.67	2.20	0.63	0.39	0.68	-0.04	-0.54	-0.35
HD 169142	0.96	-6.00	0.76	0.08	0.92	2.18	0.86	0.00	0.16	0.54	0.45	-0.60
MWC 297	9.34	-3.39	0.15	0.00	0.88	1.82	0.40	0.39	0.85	-0.11	0.08	-0.11
VV SER	1.98	-4.36	0.12	0.00	0.60	0.08	0.99	0.01	0.88	-0.10	0.09	-0.99
R CRA	4.79	1.17	0.08	0.00	0.72	0.26	0.91	0.67	0.91	0.07	-0.69	0.72
HD 190073	1.21	-2.15	0.42	0.00	0.86	2.78	0.00	0.27	0.58	-0.26	-0.16	0.10

Notes. This fit was performed on the HQ subsample. See Tables 8 and 7 for symbol details. Error bars are not shown because of page width limitation; a complete version of this table can be found at the CDS.

Appendix C: Log of observations**Table C.1.** Log of observations for the program objects.

Target	Obs. date	Configuration	MJD	nV^2	nCP
AB AUR	2012-12-22	A1-B2-C1-D0	56 283.1	18	12
AB AUR	2012-12-20	A1-B2-C1-D0	56 281.2	18	12
AK SCO	2013-06-17	D0-G1-H0-I1	56 460.2	15	12
AK SCO	2013-07-03	A1-B2-C1-D0	56 476.1	18	12
AK SCO	2013-06-06	A1-G1-J3-K0	56 449.3	18	12
AK SCO	2013-06-10	A1-G1-J3-K0	56 453.3	18	12
CO ORI	2013-01-28	A1-G1-J3-K0	56 320.1	6	4
CO ORI	2012-12-22	A1-C1-D0	56 283.1	9	3
CO ORI	2012-12-21	A1-B2-C1-D0	56 282.2	15	9
HD 100453	2013-01-29	A1-G1-J3-K0	56 321.3	18	12
HD 100453	2013-01-28	A1-G1-J3-K0	56 320.4	18	12
HD 100453	2012-12-22	A1-B2-C1-D0	56 283.3	18	12
HD 100453	2013-01-27	A1-G1-J3-K0	56 319.3	27	12
HD 100453	2012-12-19	A1-B2-C1-D0	56 280.3	36	24
HD 100453	2013-01-30	A1-G1-J3-K0	56 322.3	12	3
HD 100453	2013-01-31	A1-G1-J3-K0	56 323.2	18	12
HD 100453	2013-02-17	D0-G1-H0-I1	56 340.3	36	24
HD 100453	2013-02-20	D0-G1-H0-I1	56 343.2	36	24
HD 100453	2013-02-18	D0-G1-H0-I1	56 341.3	72	45
HD 100453	2013-02-01	A1-G1-J3-K0	56 324.3	78	36
HD 100546	2013-01-29	A1-J3-K0	56 321.3	18	6
HD 100546	2012-12-22	A1-B2-C1-D0	56 283.3	18	12
HD 100546	2012-12-20	A1-B2-C1-D0	56 281.4	18	12
HD 100546	2013-02-20	D0-G1-H0-I1	56 343.3	18	12
HD 100546	2013-01-30	A1-J3-K0	56322.3	18	6
HD 100546	2013-01-31	A1-K0	56323.3	3	0
HD 100546	2013-02-17	D0-G1-H0-I1	56 340.4	18	12
HD 100546	2013-02-19	D0-G1-H0-I1	56 342.3	72	48
HD 100546	2013-02-18	D0-G1-H0-I1	56 341.3	18	12
HD 100546	2013-02-01	A1-G1-J3-K0	56 324.3	36	24
HD 104237	2013-04-11	D0-G1-H0-I1	56 393.2	378	252
HD 104237	2013-02-19	D0-G1-H0-I1	56 342.2	36	24
HD 104237	2013-02-18	D0-G1-H0-I1	56 341.4	18	12
HD 104237	2012-12-22	A1-B2-C1-D0	56 283.3	18	12
HD 104237	2012-12-21	A1-B2-C1-D0	56 282.4	18	12
HD 139614	2013-07-03	A1-B2-C1-D0	56 477.0	18	12
HD 139614	2013-06-16	D0-G1-H0-I1	56 460.0	36	21
HD 139614	2013-06-06	A1-G1-J3-K0	56 449.1	18	12
HD 141569	2013-06-06	A1-G1-J3-K0	56 449.2	18	12
HD 142527	2013-06-17	D0-G1-H0-I1	56 460.2	15	12
HD 142527	2013-06-16	D0-G1-H0-I1	56 459.6	36	24
HD 142527	2013-06-15	D0-G1-H0-I1	56 458.4	54	36
HD 142527	2013-06-04	A1-G1-J3-K0	56 447.2	18	12
HD 142527	2013-05-13	A1-B2-C1-D0	56 425.2	5	4
HD 142527	2013-06-06	A1-G1-J3-K0	56 449.1	18	12
HD 142527	2013-06-07	A1-G1-J3-K0	56 450.1	36	24
HD 142527	2013-07-03	A1-B2-C1-D0	56 476.1	18	12
HD 142527	2013-06-10	A1-G1-J3-K0	56 453.0	18	12
HD 142527	2013-07-04	A1-B2-C1-D0	56 477.1	18	12
HD 142527	2013-02-20	D0-G1-H0-I1	56 343.3	18	12
HD 142527	2013-06-05	A1-G1-J3-K0	56 448.2	54	36
HD 142666	2013-06-17	D0-G1-H0-I1	56 460.0	18	12
HD 142666	2013-07-03	A1-B2-C1-D0	56 476.1	18	12
HD 142666	2013-06-06	A1-G1-J3-K0	56 449.2	18	12
HD 143006	2013-06-17	D0-G1-H0-I1	56 460.1	18	12
HD 143006	2013-06-06	A1-G1-J3-K0	56 449.2	18	12
HD 143006	2013-07-04	A1-B2-C1-D0	56 477.0	18	12

Table C.1. continued.

Target	Obs. date	Configuration	MJD	nV^2	nCP
HD 144432	2013-06-17	D0-G1-H0-I1	56 460.1	18	12
HD 144432	2013-06-16	D0-H0	56459.3	3	0
HD 144432	2013-06-04	A1-G1-J3-K0	56 447.2	18	12
HD 144432	2013-06-10	A1-G1-J3-K0	56 453.3	18	12
HD 144432	2013-07-03	A1-B2-C1-D0	56 476.2	18	12
HD 144432	2013-06-07	A1-G1-J3-K0	56 450.2	36	24
HD 144668	2013-06-15	D0-G1-H0-I1	56 458.2	36	24
HD 144668	2013-06-04	A1-G1-J3-K0	56 447.3	18	12
HD 144668	2013-06-05	A1-G1-J3-K0	56 448.2	54	36
HD 144668	2013-06-10	A1-G1-J3-K0	56 453.1	36	24
HD 144668	2013-07-03	A1-B2-C1-D0	56 476.1	18	12
HD 144668	2013-06-07	A1-G1-J3-K0	56 450.3	18	12
HD 144668	2013-07-04	A1-B2-C1-D0	56 477.1	15	12
HD 145718	2013-06-17	D0-G1-H0-I1	56 460.0	18	12
HD 145718	2013-07-03	A1-B2-C1-D0	56 476.2	18	12
HD 145718	2013-06-06	A1-G1-J3-K0	56 449.3	18	12
HD 145718	2013-06-10	A1-G1-J3-K0	56 453.2	18	12
HD 149914	2013-06-15	D0-G1-H0-I1	56 458.2	18	12
HD 149914	2013-06-04	A1-G1-J3-K0	56 447.3	18	12
HD 149914	2013-06-06	A1-G1-J3-K0	56 449.1	18	12
HD 149914	2013-06-10	A1-G1-J3-K0	56 453.2	18	12
HD 150193	2013-06-17	D0-G1-H0-I1	56 460.2	18	12
HD 150193	2013-07-04	A1-B2-C1-D0	56 477.2	18	12
HD 150193	2013-06-06	A1-G1-J3-K0	56 449.3	18	12
HD 150193	2013-06-10	A1-G1-J3-K0	56 453.2	18	12
HD 158643	2013-06-15	D0-G1-H0-I1	56 458.1	36	24
HD 158643	2013-06-04	A1-G1-J3-K0	56 447.3	18	12
HD 158643	2013-06-06	A1-G1-J3-K0	56 449.4	18	12
HD 158643	2013-06-07	A1-G1-J3-K0	56 450.2	36	24
HD 158643	2013-07-03	A1-B2-C1-D0	56 476.6	36	24
HD 158643	2013-07-06	A1-B2-C1-D0	56 479.0	18	12
HD 158643	2013-07-04	A1-B2-C1-D0	56 477.2	36	24
HD 163296	2013-07-03	A1-B2-C1-D0	56 476.2	18	12
HD 163296	2013-06-15	D0-G1-H0-I1	56 458.2	54	36
HD 169142	2013-06-17	D0-G1-H0-I1	56 460.2	15	12
HD 169142	2013-06-09	A1-G1-J3-K0	56 452.2	18	12
HD 169142	2013-07-03	A1-B2-C1-D0	56 476.3	18	12
HD 169142	2013-06-04	A1-G1-J3-K0	56 447.3	18	12
HD 17081	2013-01-21	A1-G1-J3-K0	56 313.1	18	12
HD 17081	2013-01-26	A1-G1-J3-K0	56 318.0	18	12
HD 17081	2012-12-19	A1-B2-C1-D0	56 280.1	18	12
HD 179218	2013-06-06	A1-G1-J3-K0	56 449.4	18	12
HD 179218	2013-07-04	A1-B2-C1-D0	56 477.2	48	33
HD 190073	2013-06-06	A1-G1-J3-K0	56 449.4	18	12
HD 190073	2013-07-04	A1-B2-C1-D0	56 477.3	33	24
HD 244604	2013-01-28	A1-G1-J3-K0	56 320.2	4	1
HD 250550	2013-01-28	A1-G1-J3-K0	56 320.2	5	4
HD 259431	2013-01-30	A1-G1-J3-K0	56 322.2	18	12
HD 259431	2012-12-20	A1-B2-C1-D0	56 281.2	18	12
HD 293782	2013-02-20	D0-G1-H0-I1	56 343.1	6	4
HD 293782	2013-01-29	G1-J3-K0	56 321.1	2	0
HD 293782	2012-12-22	A1-B2-C1-D0	56 283.2	5	4
HD 293782	2013-02-19	H0-I1	56 342.1	1	0
HD 293782	2012-12-21	A1-B2-C1-D0	56 282.3	6	4
HD 31648	2012-12-21	A1-B2-C1-D0	56 282.1	18	12
HD 34282	2013-02-20	D0-G1-H0-I1	56 343.0	6	4
HD 34282	2013-02-19	D0-H0	56 342.1	1	0
HD 34282	2013-02-01	A1-G1-J3-K0	56 324.1	6	4
HD 35929	2013-01-26	A1-G1-J3-K0	56 318.1	18	12

Table C.1. continued.

Target	Obs. date	Configuration	MJD	nV^2	nCP
HD 35929	2012-12-19	A1-B2-C1-D0	56 280.1	18	12
HD 35929	2012-12-21	A1-B2-C1-D0	56 282.2	18	12
HD 36917	2013-01-27	A1-G1-J3-K0	56 319.1	15	12
HD 36917	2012-12-19	A1-B2-C1-D0	56 280.1	18	12
HD 37258	2012-12-21	A1-B2-C1-D0	56 282.3	4	4
HD 37357	2012-12-22	A1-B2-C1-D0	56 283.2	6	4
HD 37357	2013-01-31	A1-G1-J3-K0	56 323.2	6	2
HD 37357	2012-12-21	A1-B2-C1-D0	56 282.3	11	8
HD 37411	2013-02-01	A1-G1-J3-K0	56 324.1	5	3
HD 37411	2012-12-21	A1-B2-C1-D0	56 282.3	5	4
HD 37806	2012-12-22	A1-B2-C1-D0	56 283.0	18	12
HD 37806	2013-01-27	G1-K0	56 319.1	3	0
HD 37806	2013-01-26	A1-G1-J3-K0	56 318.2	54	36
HD 37806	2012-12-21	A1-B2-C1-D0	56 282.0	18	12
HD 37806	2013-01-31	A1-G1-J3-K0	56 323.1	18	9
HD 37806	2013-02-18	D0-G1-H0-I1	56 341.1	18	12
HD 38087	2013-01-26	A1-G1-J3-K0	56 318.2	90	60
HD 38087	2012-12-19	A1-B2-C1-D0	56 280.2	18	12
HD 39014	2013-01-29	A1-G1-J3-K0	56 321.1	33	24
HD 39014	2013-01-28	A1-G1-J3-K0	56 320.0	18	12
HD 39014	2013-01-22	A1-G1-J3-K0	56 314.0	36	24
HD 39014	2013-01-27	A1-G1-J3-K0	56 319.0	36	24
HD 39014	2013-01-26	A1-G1-J3-K0	56 318.0	18	12
HD 39014	2013-01-25	A1-J3-K0	56 317.1	9	3
HD 39014	2012-12-21	A1-B2-C1-D0	56 282.1	18	12
HD 39014	2013-01-30	A1-G1-J3-K0	56 322.0	18	12
HD 39014	2013-01-31	A1-G1-J3-K0	56 323.0	18	12
HD 45677	2013-01-29	A1-G1-J3-K0	56 321.2	27	15
HD 45677	2012-12-22	A1-B2-C1-D0	56 283.2	18	12
HD 45677	2013-01-27	A1-G1-J3-K0	56 319.2	30	15
HD 45677	2013-01-26	A1-G1-J3-K0	56 318.3	18	12
HD 45677	2012-12-20	A1-B2-C1-D0	56 281.2	54	36
HD 45677	2013-02-20	D0-G1-H0-I1	56 343.1	18	12
HD 45677	2013-01-30	A1-G1-J3-K0	56 322.1	36	21
HD 45677	2013-01-31	A1-G1-J3-K0	56 323.1	18	12
HD 45677	2013-02-22	D0-G1-H0-I1	56 345.2	18	12
HD 45677	2013-02-17	D0-G1-H0-I1	56 340.0	15	6
HD 45677	2013-02-19	D0-G1-H0-I1	56 342.1	18	12
HD 45677	2013-02-18	D0-G1-H0-I1	56 341.1	36	24
HD 45677	2013-02-01	A1-G1-J3-K0	56 324.1	18	9
HD 53367	2013-01-27	A1-G1-J3-K0	56 319.1	18	12
HD 53367	2013-02-20	D0-G1-H0-I1	56 343.2	18	12
HD 53367	2012-12-22	A1-B2-C1-D0	56 283.2	18	12
HD 53367	2012-12-19	A1-B2-C1-D0	56 280.3	18	12
HD 58647	2012-12-22	A1-B2-C1-D0	56 283.1	18	12
HD 58647	2013-01-27	A1-G1-J3-K0	56 319.2	18	12
HD 58647	2012-12-19	A1-B2-C1-D0	56 280.2	18	12
HD 58647	2013-02-17	D0-G1-H0-I1	56 340.2	18	12
HD 58647	2013-02-19	D0-G1-H0-I1	56 342.2	18	12
HD 58647	2013-02-18	D0-G1-H0-I1	56 341.1	18	12
HD 85567	2013-06-04	A1-G1-J3-K0	56 448.0	18	12
HD 85567	2013-06-05	A1-G1-J3-K0	56 448.0	18	12
HD 85567	2013-06-06	A1-G1-J3-K0	56 449.5	36	24
HD 85567	2013-06-09	A1-G1-J3-K0	56 453.0	18	12
HD 85567	2013-01-26	A1-G1-J3-K0	56 318.3	15	12
HD 85567	2012-12-19	A1-B2-C1-D0	56 280.3	18	12
HD 85567	2013-02-17	D0-G1-H0-I1	56 340.2	18	12
HD 85567	2013-02-20	D0-G1-H0-I1	56 343.3	18	12
HD 85567	2013-02-18	D0-G1-H0-I1	56 341.4	18	12
HD 85567	2013-02-19	D0-G1-H0-I1	56 342.0	18	12

Table C.1. continued.

Target	Obs. date	Configuration	MJD	nV^2	nCP
HD 95881	2012-12-22	A1-B2-C1-D0	56 283.3	18	12
HD 95881	2012-12-19	A1-B2-C1-D0	56 280.4	18	12
HD 95881	2013-01-30	A1-J3-K0	56 322.3	9	3
HD 95881	2013-02-17	D0-G1-H0-I1	56 340.3	36	24
HD 95881	2013-02-19	D0-G1-H0-I1	56 342.3	18	12
HD 95881	2013-02-20	D0-G1-H0-I1	56 343.2	18	12
HD 97048	2013-02-17	D0-G1-H0-I1	56 340.3	18	12
HD 97048	2012-12-22	A1-B2-C1-D0	56 283.4	18	12
HD 97048	2012-12-20	A1-B2-C1-D0	56 281.3	18	12
HD 98922	2013-01-28	A1-G1-J3-K0	56 320.4	54	36
HD 98922	2012-12-22	A1-B2-C1-D0	56 283.4	18	12
HD 98922	2013-01-27	A1-G1-J3-K0	56 319.3	51	30
HD 98922	2013-01-26	A1-G1-J3-K0	56 318.4	18	12
HD 98922	2012-12-20	A1-B2-C1-D0	56 281.3	36	24
HD 98922	2013-02-20	D0-G1-H0-I1	56 343.2	36	24
HD 98922	2013-01-30	A1-G1-J3-K0	56 322.3	24	12
HD 98922	2013-01-31	A1-G1-J3-K0	56 323.2	36	24
HD 98922	2013-02-17	D0-G1-H0-I1	56 340.2	54	36
HD 98922	2013-02-19	D0-G1-H0-I1	56 342.3	18	12
HD 98922	2013-02-18	D0-G1-H0-I1	56 341.3	72	48
HD 98922	2013-02-01	A1-G1-J3-K0	56 324.2	54	36
MWC158	2013-01-28	A1-G1-J3-K0	56 320.3	18	12
MWC158	2013-01-27	A1-G1-J3-K0	56 319.2	54	36
MWC158	2013-01-26	A1-G1-J3-K0	56 318.3	18	12
MWC158	2012-12-20	A1-B2-C1-D0	56 281.1	18	12
MWC158	2013-01-30	A1-G1-J3-K0	56 322.1	18	12
MWC158	2012-12-19	A1-B2-C1-D0	56 280.2	36	24
MWC158	2013-02-17	D0-G1-H0-I1	56 340.1	18	12
MWC158	2013-02-20	D0-G1-H0-I1	56 343.2	18	12
MWC158	2013-02-18	D0-G1-H0-I1	56 341.2	18	12
MWC158	2013-02-01	A1-G1-J3-K0	56 324.1	36	24
MWC158	2013-01-31	A1-G1-J3-K0	56 323.1	18	12
MWC297	2013-06-17	D0-G1-H0-I1	56 460.3	18	12
MWC297	2013-06-15	D0-G1-H0-I1	56 458.3	18	12
MWC297	2013-06-04	A1-G1-J3-K0	56 447.4	18	12
MWC297	2013-06-10	A1-G1-J3-K0	56 453.4	18	12
MWC297	2013-07-03	A1-B2-C1-D0	56 476.3	18	12
MWC297	2013-06-09	A1-G1-J3-K0	56 452.3	18	12
MWC297	2013-06-07	A1-G1-J3-K0	56 450.4	90	60
MWC297	2013-07-05	A1-B2-C1-D0	56 479.0	18	12
MWC297	2013-07-04	A1-B2-C1-D0	56 477.3	18	12
MWC758	2012-12-20	A1-B2-C1-D0	56 281.2	18	12
R CRA	2013-06-07	G1-K0	56 450.4	3	0
R CRA	2013-06-15	D0-G1-H0	56 458.2	6	0
R CRA	2013-06-17	D0-G1-H0-I1	56 460.4	9	6
R CRA	2013-07-03	A1-B2-C1-D0	56 476.4	54	36
R CRA	2013-07-04	A1-B2-C1-D0	56 477.4	36	24
R CRA	2013-07-06	A1-B2-C1-D0	56 479.1	36	24
T ORI	2013-01-31	A1-K0	56 323.1	3	0
T ORI	2013-02-18	D0-G1-H0-I1	56 341.1	18	12
T ORI	2013-01-26	A1-G1-J3-K0	56 318.1	18	12
T ORI	2012-12-19	A1-B2-C1-D0	56 280.2	18	12
T ORI	2012-12-21	A1-B2-C1-D0	56 282.2	18	12
V 1247 ORI	2013-01-31	A1-G1-J3-K0	56 323.2	5	3
V 1247 ORI	2012-12-21	A1-B2-C1-D0	56 282.3	12	8
VV SER	2013-07-03	A1-B2-C1-D0	56 476.3	18	12
VV SER	2013-06-04	A1-G1-J3-K0	56 447.4	24	15
VV SER	2013-06-20	U1-U2-U3-U4	56 463.1	18	12
VV SER	2013-06-07	A1-G1-J3-K0	56 450.3	18	12

Appendix D: Summary plots for program objects

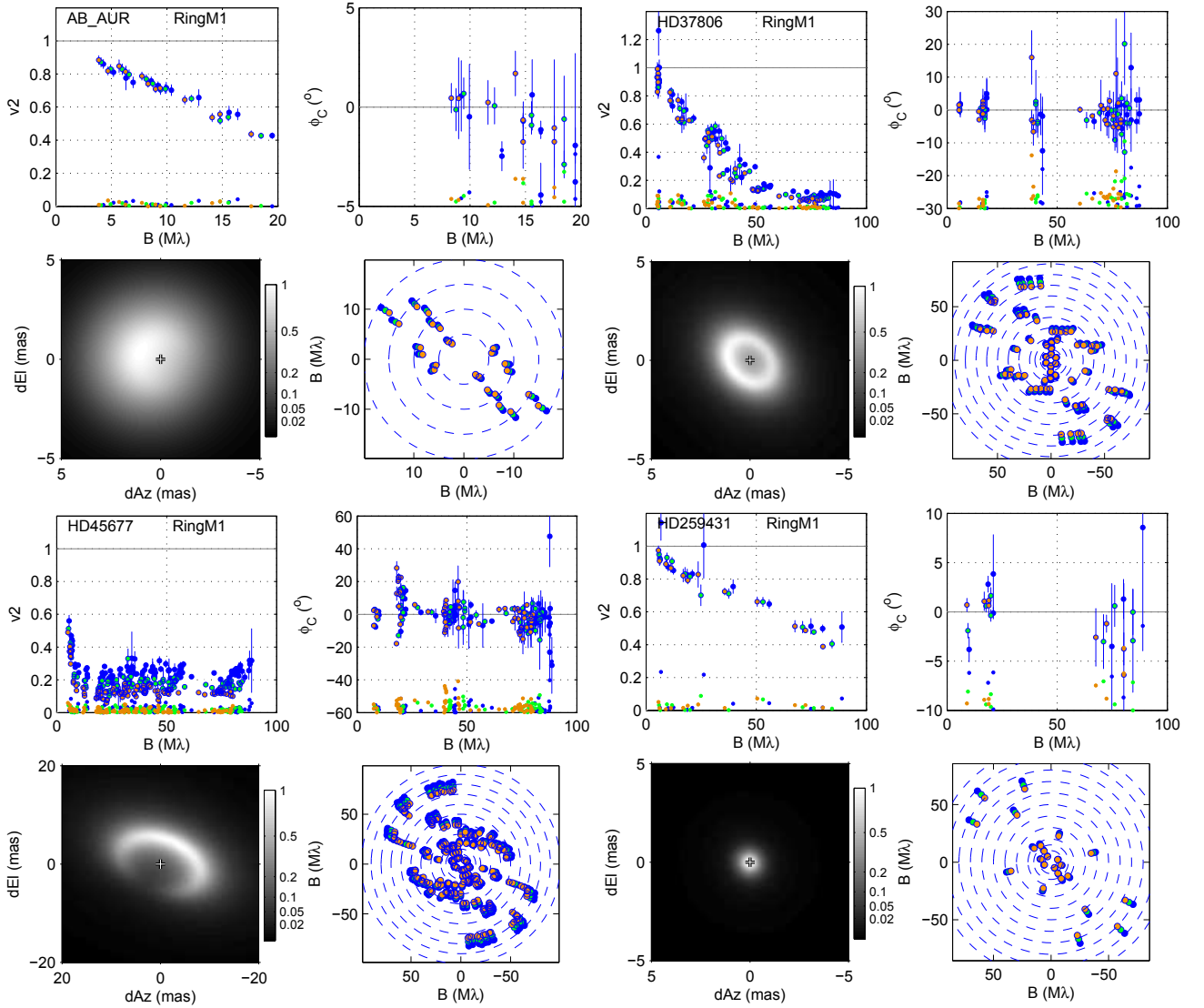


Fig. D.1. Summary plots for the HQ objects. Four panels are shown for each object: (1) visibility squared V^2 versus projected baseline in units of $10^6\lambda$; (2) phase closure ϕ_{cp} versus the largest projected baseline of each triangle; (3) a half-tone image of the circumstellar component resulting from a Ring fit with $m = 1$ azimuthal modulation, the star's position is shown by a cross symbol; (4) the (uv) plane coverage. For spectrally dispersed observations, the red, green, blue colors represent wavelengths from longest to shortest. For the V^2 and ϕ_{cp} plots, the absolute value of the fit residuals is shown by the dots at the bottom of the plot.

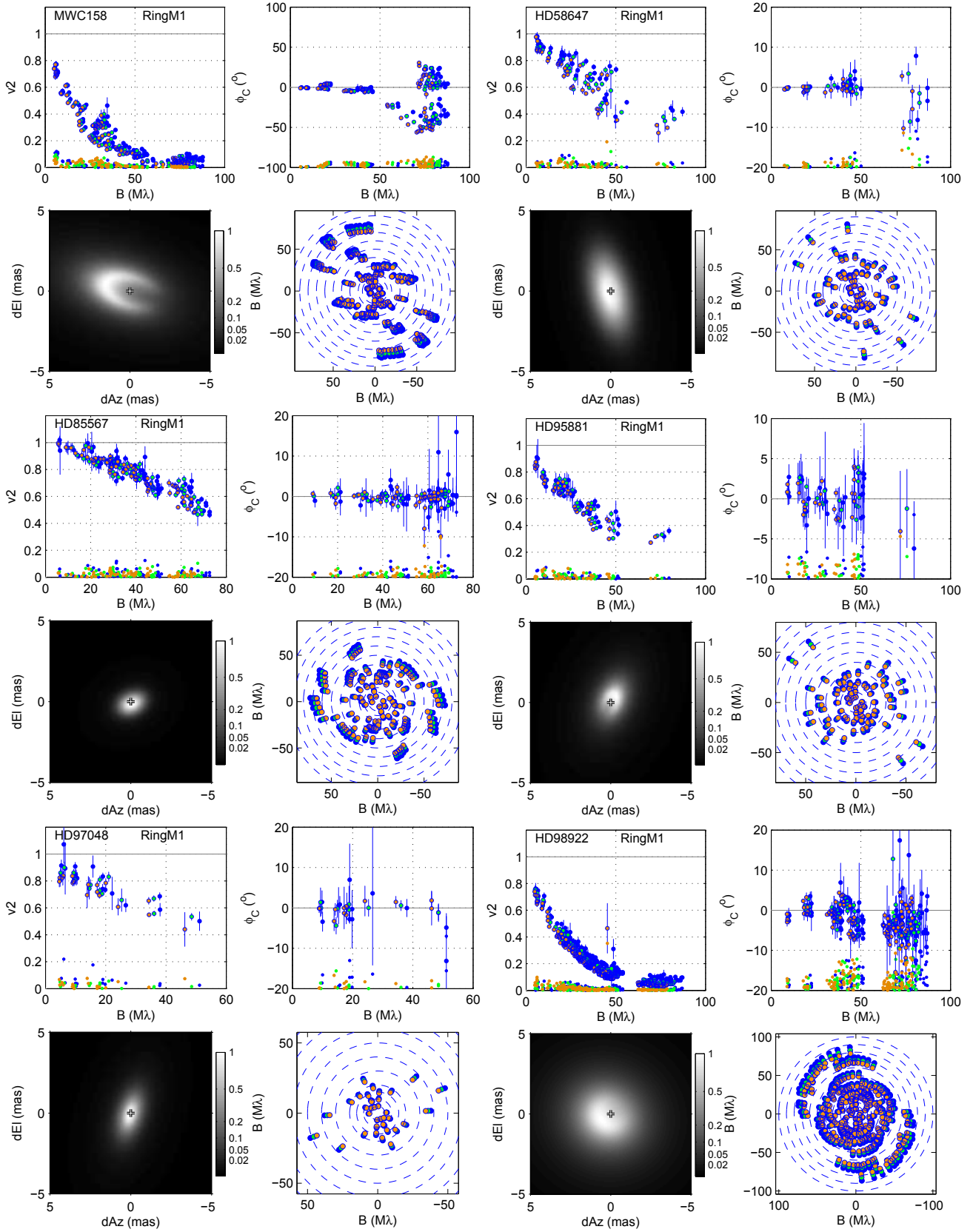


Fig. D.1. continued.

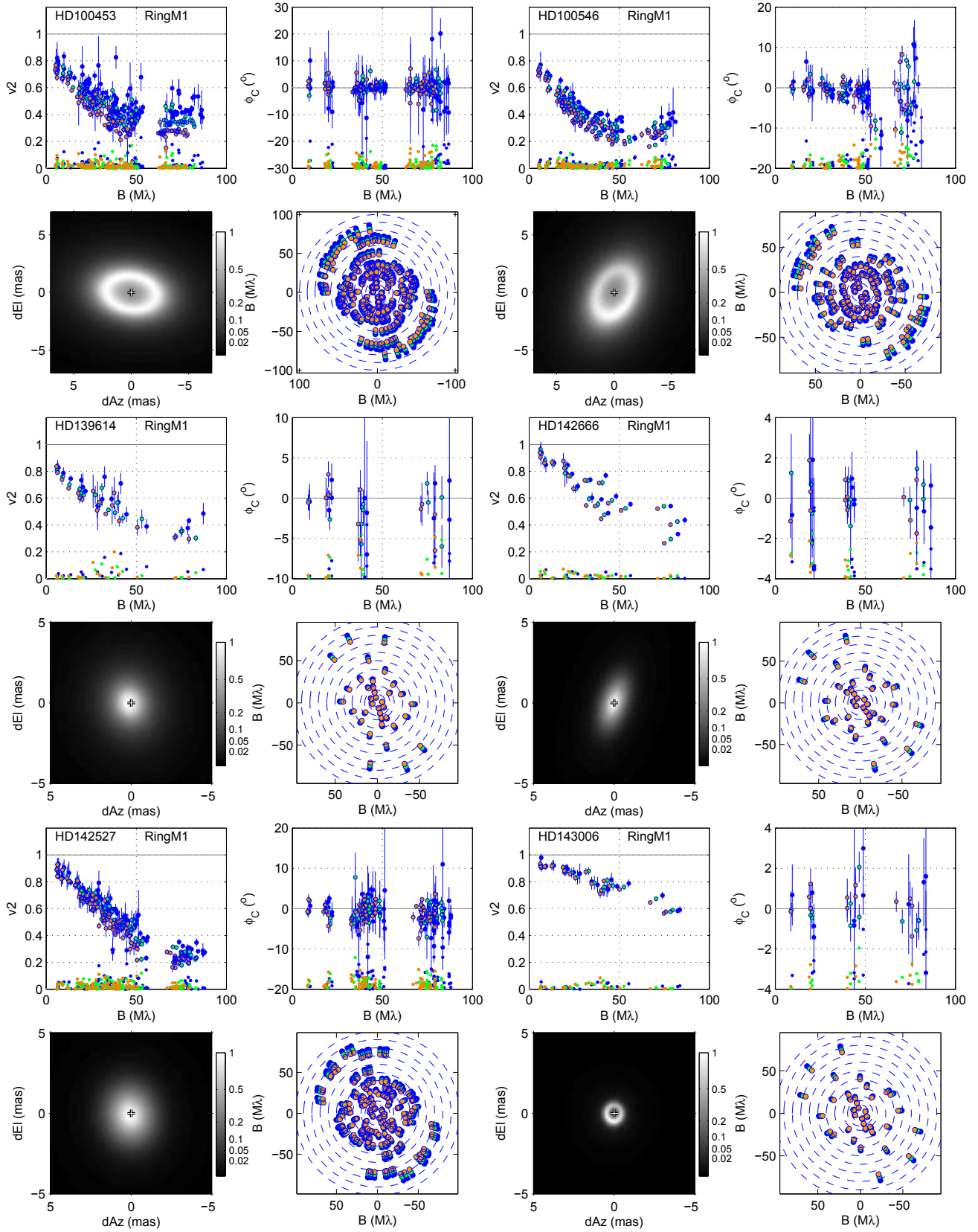


Fig. D.1. continued.

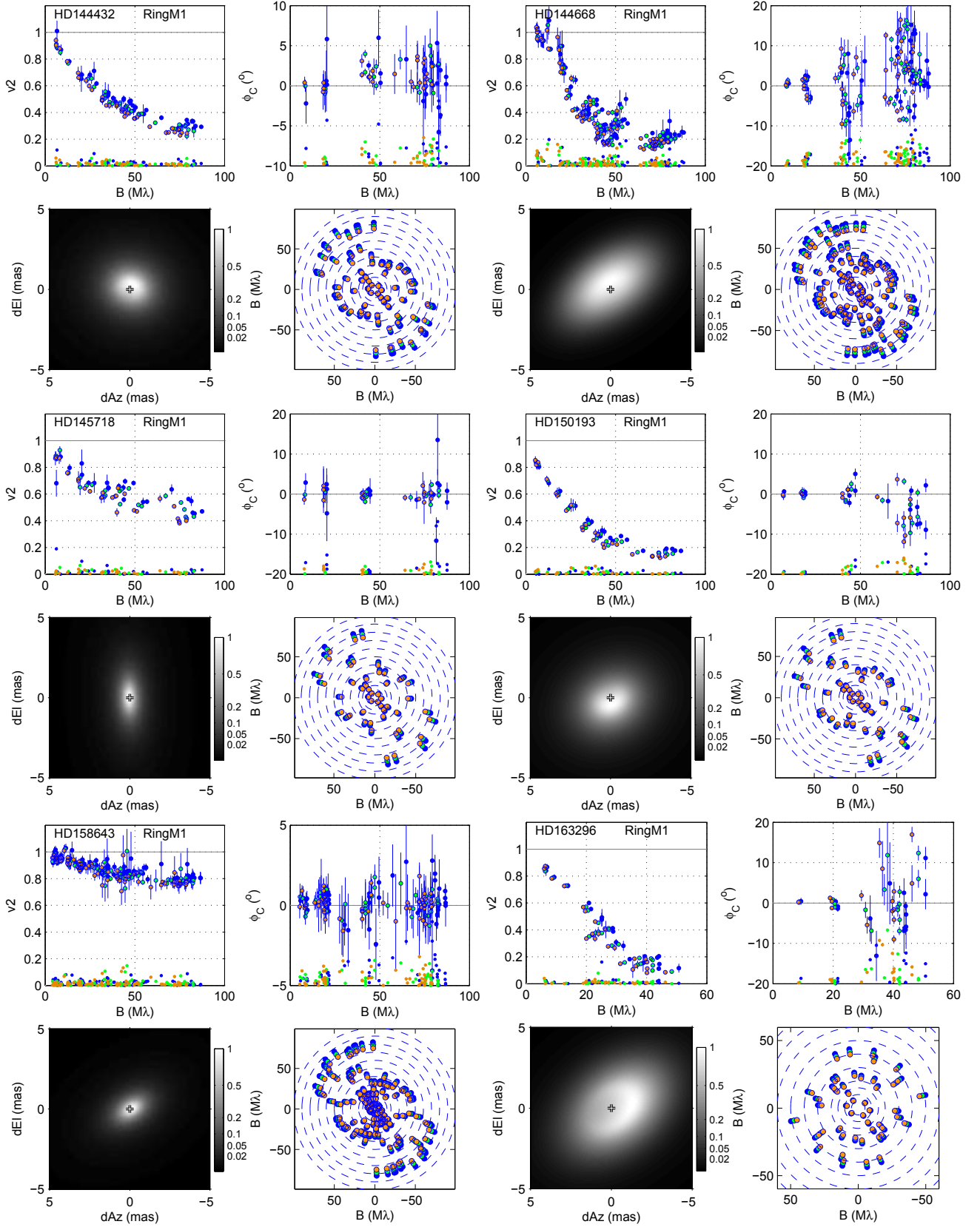


Fig. D.1. continued.

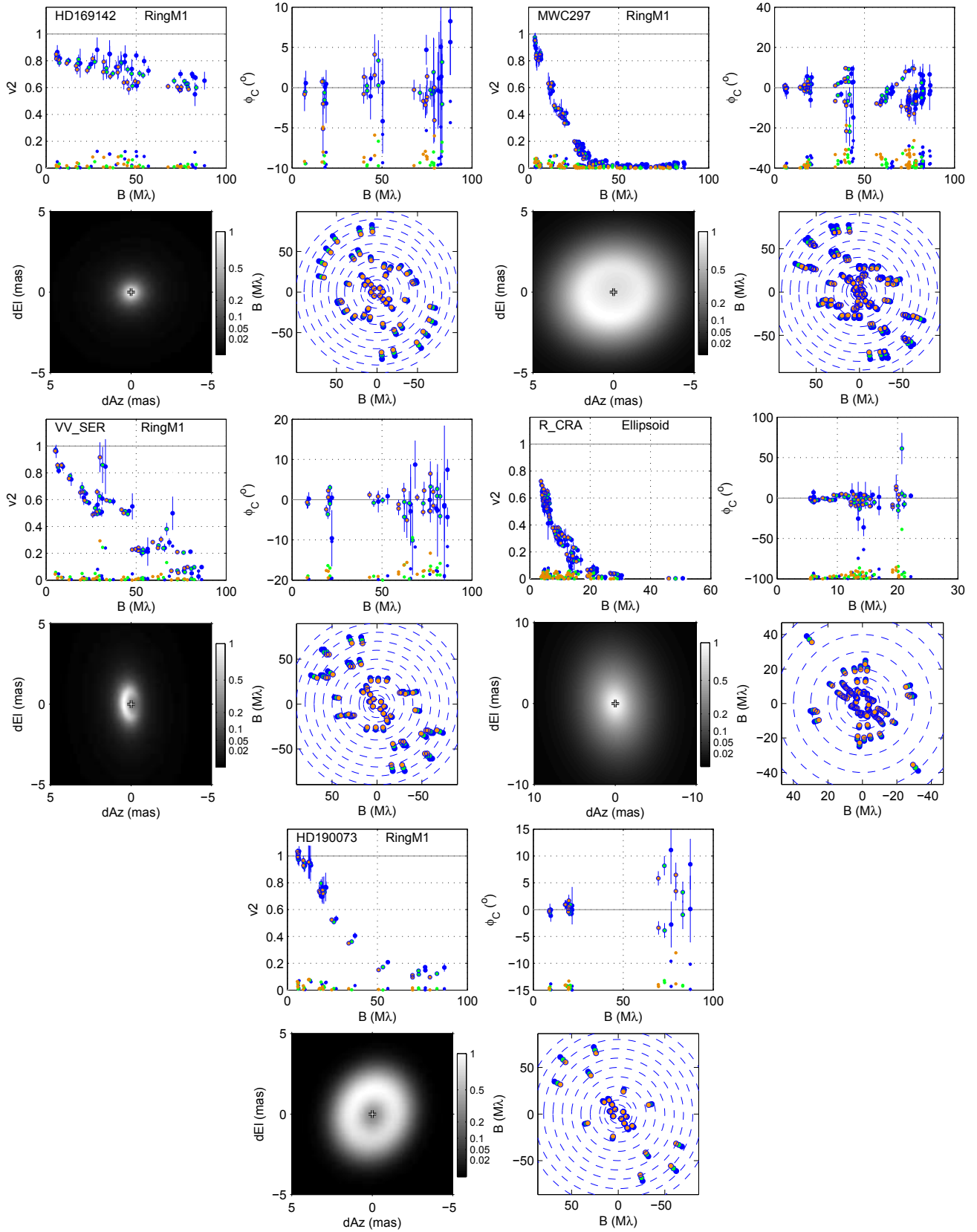


Fig. D.1. continued.

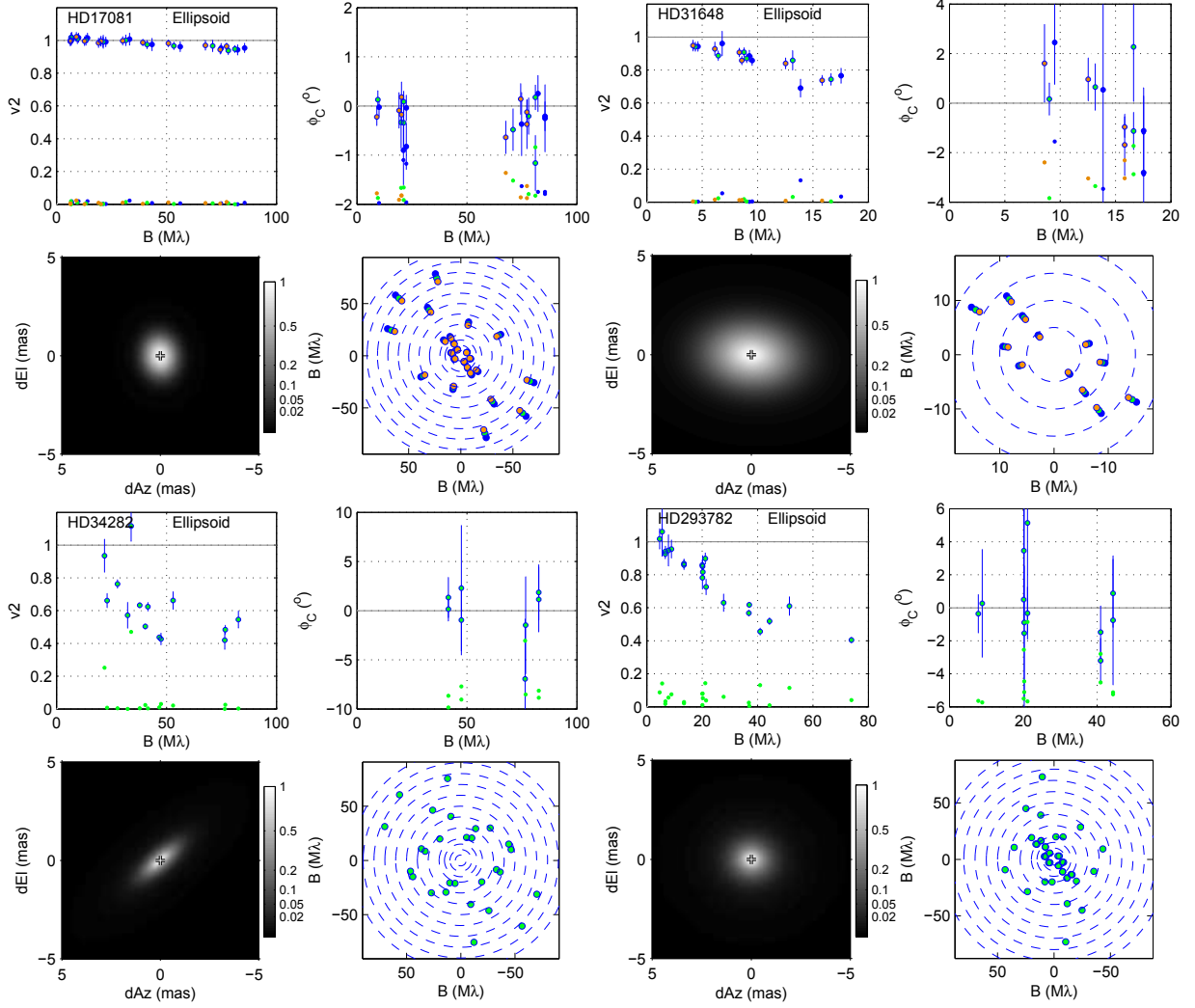


Fig. D.2. Summary plots for the non-HQ objects. Similar plots to those in Fig. D.1 above, for the rest of the sample. For these objects, because of the limited resolution achieved or other limitations, a simpler *Ellipsoid* fit was made. For objects tagged as binary, no fit was attempted, and the image sub-panel is absent.

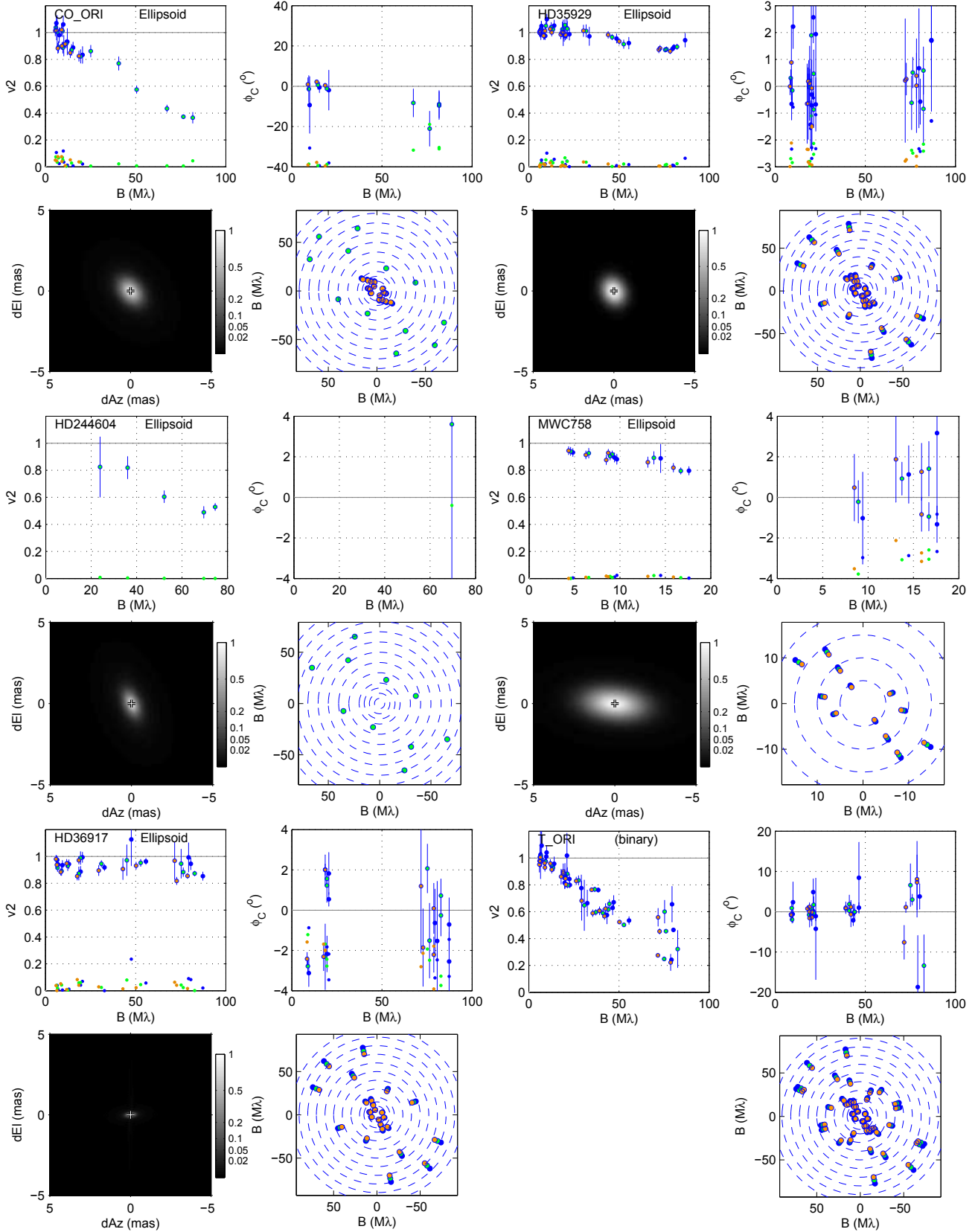


Fig. D.2. continued.

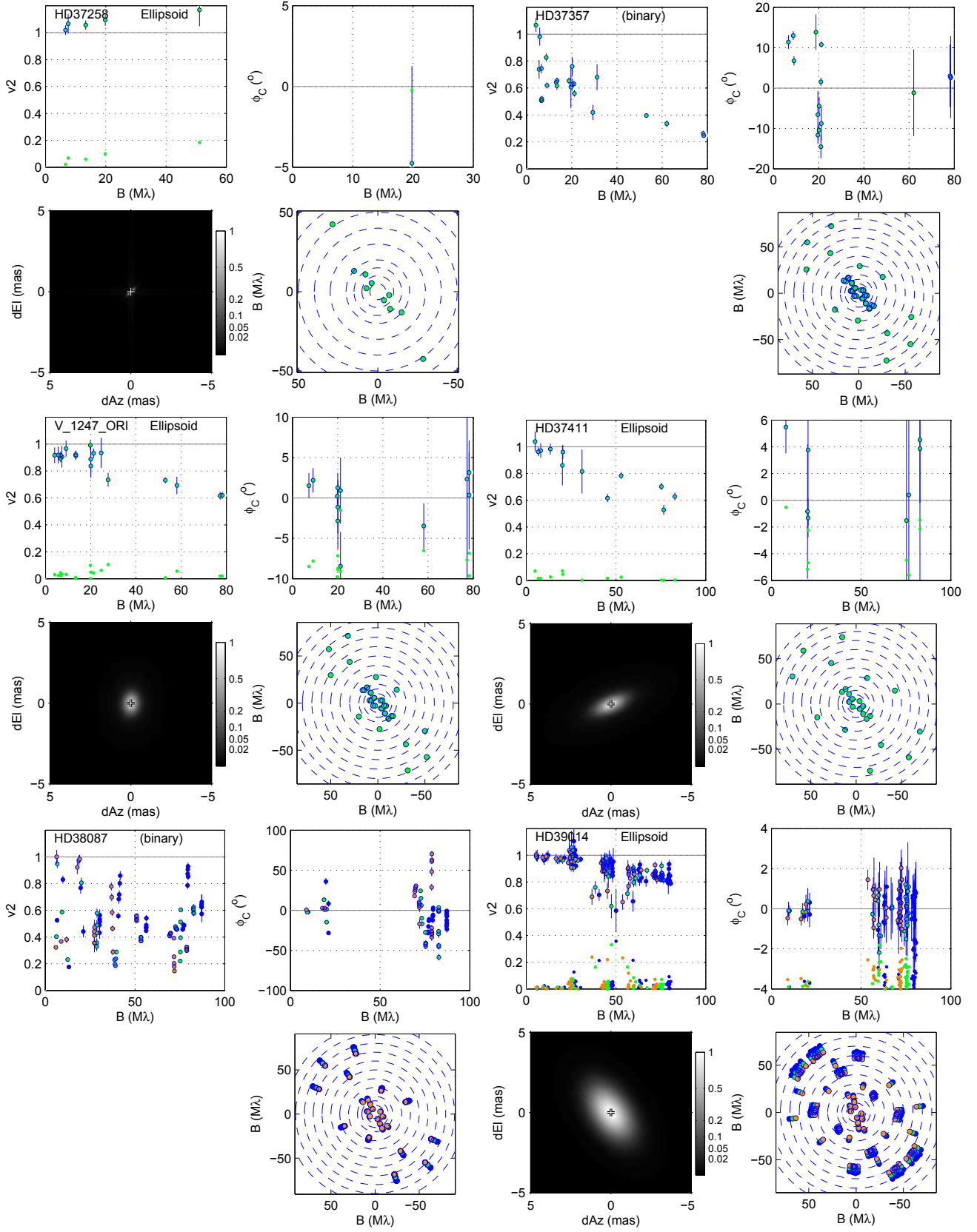


Fig. D.2. continued.

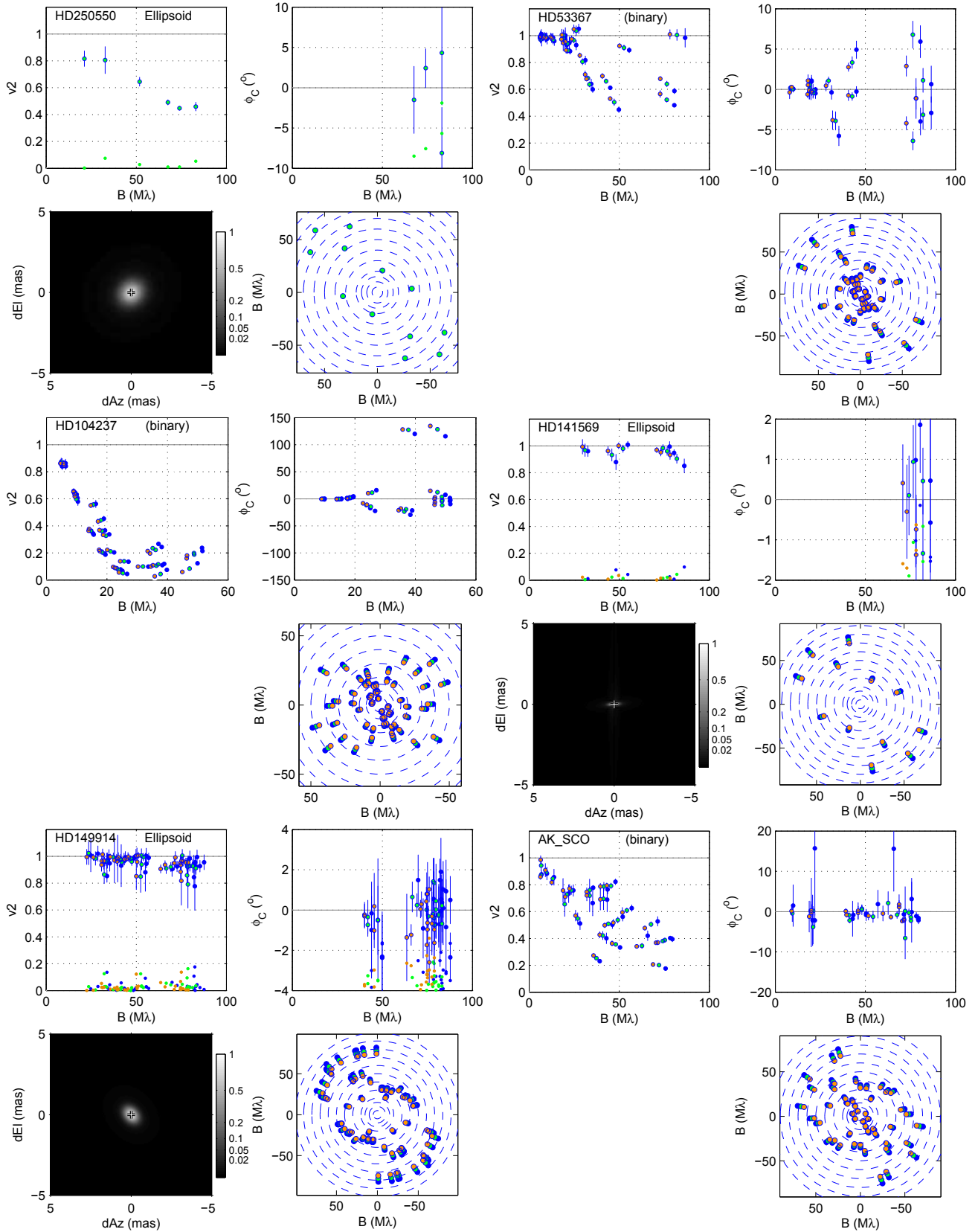


Fig. D.2. continued.

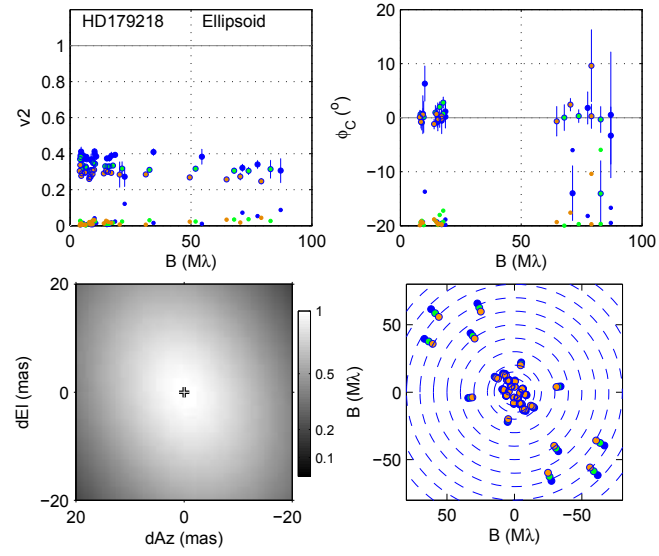


Fig. D.2. continued.