# Study of $\boldsymbol{B} \rightarrow \boldsymbol{X} \boldsymbol{\gamma}$ Decays and Determination of $\left|\boldsymbol{V}_{\boldsymbol{t d}} / \boldsymbol{V}_{\boldsymbol{t s}}\right|$ 

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Using a sample of 471 million $B \bar{B}$ events collected with the $B A B A R$ detector, we study the sum of seven exclusive final states $B \rightarrow X_{s(d)} \gamma$, where $X_{s(d)}$ is a strange (non-strange) hadronic system with a mass of up to $2.0 \mathrm{GeV} / c^{2}$. After correcting for unobserved decay modes, we obtain a branching fraction for $b \rightarrow d \gamma$ of $(9.2 \pm 2.0($ stat. $) \pm 2.3$ (syst.) $) \times 10^{-6}$ in this mass range, and a branching fraction for $b \rightarrow s \gamma$ of $(23.0 \pm 0.8($ stat. $) \pm 3.0($ syst. $)) \times 10^{-5}$ in the same mass range. We find $\frac{\mathcal{B}(b \rightarrow d \gamma)}{\mathcal{B}(b \rightarrow s \gamma)}=$ $0.040 \pm 0.009$ (stat.) $\pm 0.010$ (syst.), from which we determine $\left|V_{t d} / V_{t s}\right|=0.199 \pm 0.022$ (stat.) $\pm$ 0.024 (syst.) $\pm 0.002$ (th.).

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The decays $b \rightarrow d \gamma$ and $b \rightarrow s \gamma$ are flavor-changing neutral current processes forbidden at tree level in the

[^0]Standard Model (SM). The leading-order processes are one-loop electroweak penguin diagrams, for which the top quark is the dominant virtual particle. In theories beyond the SM, new virtual particles may appear in the loop, which could lead to measurable effects on experimental observables such as branching fractions and $C P$ asymmetries [1]. In the SM the inclusive rate for $b \rightarrow d \gamma$ is suppressed relative to $b \rightarrow s \gamma$ by a factor $\left|V_{t d} / V_{t s}\right|^{2}$, where $V_{t d}$ and $V_{t s}$ are Cabibbo-Kobayashi-Maskawa matrix elements. Measurements of $\left|V_{t d} / V_{t s}\right|$ using the exclusive modes $B \rightarrow(\rho, \omega) \gamma$ and $B \rightarrow K^{*} \gamma$ [4, [5] are now wellestablished, with theoretical uncertainties of $7 \%$ from

TABLE I: The reconstructed decay modes. Charge conjugate states are implied throughout this paper.

| $B \rightarrow X_{d} \gamma$ | $B \rightarrow X_{s} \gamma$ |
| :--- | :--- |
| $B^{0} \rightarrow \pi^{+} \pi^{-} \gamma$ | $B^{0} \rightarrow K^{+} \pi^{-} \gamma$ |
| $B^{+} \rightarrow \pi^{+} \pi^{0} \gamma$ | $B^{+} \rightarrow K^{+} \pi^{0} \gamma$ |
| $B^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+} \gamma$ | $B^{+} \rightarrow K^{+} \pi^{+} \pi^{-} \gamma$ |
| $B^{0} \rightarrow \pi^{+} \pi^{-} \pi^{0} \gamma$ | $B^{0} \rightarrow K^{+} \pi^{-} \pi^{0} \gamma$ |
| $B^{0} \rightarrow \pi^{+} \pi^{-} \pi^{+} \pi^{-} \gamma$ | $B^{0} \rightarrow K^{+} \pi^{-} \pi^{+} \pi^{-} \gamma$ |
| $B^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+} \pi^{0} \gamma$ | $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+} \pi^{0} \gamma$ |
| $B^{+} \rightarrow \pi^{+} \eta \gamma$ | $B^{+} \rightarrow K^{+} \eta \gamma$ |

weak annihilation and hadronic form factors [2]. This ratio can also be obtained from the $B_{d}$ and $B_{s}$ mixing frequencies [3]. It is important to confirm the consistency of the two methods of determining $\left|V_{t d} / V_{t s}\right|$, since new physics effects would enter in different ways in mixing and radiative decays. A measurement of the branching fractions of inclusive $b \rightarrow d \gamma$ relative to $b \rightarrow s \gamma$ would determine $\left|V_{t d} / V_{t s}\right|$ with reduced theoretical uncertainties compared to that from exclusive modes [6].

This letter supersedes of [8], and presents the first significant observation of the $b \rightarrow d \gamma$ transition in the hadronic mass range $M\left(X_{d}\right)>1.0 \mathrm{GeV} / c^{2}$, resulting in a significant improvement in the determination of $\left|V_{t d} / V_{t s}\right|$ via the ratio of inclusive widths. Inclusive $b \rightarrow s \gamma$ and $b \rightarrow d \gamma$ rates are extrapolated from the measurements of the partial decay rates to seven exclusive final states (see Table (I) in the hadronic mass ranges $0.5<M\left(X_{d}\right)<1.0 \mathrm{GeV} / c^{2}$ (low mass, containing the previously measured $K^{*}, \rho$ and $\omega$ resonances) and $1.0<M\left(X_{d}\right)<2.0 \mathrm{GeV} / c^{2}$ (high mass). We combine these measurements and make a model-dependent extrapolation to higher hadronic mass to obtain an inclusive branching fraction $(\mathcal{B})$ for $b \rightarrow(s, d) \gamma$. These measurements use the full dataset of $471 \times 10^{6} B \bar{B}$ pairs collected at the $\Upsilon(4 S)$ resonance at the PEP-II B factory with the BABAR detector [7].

High energy photons are reconstructed from an isolated energy cluster in the barrel of the calorimeter, with shape consistent with a single photon, and energy $1.15<$ $E_{\gamma}^{*}<3.50 \mathrm{GeV}$, where * denotes the center-of-mass (CM) frame. We remove photons that can form a $\pi^{0}(\eta)$ candidate in association with another photon of energy greater than $30(250) \mathrm{MeV}$ if the two-photon invariant mass is in the range $110<m_{\gamma \gamma}<160\left(520<m_{\gamma \gamma}<560\right) \mathrm{MeV} / c^{2}$ for the low mass region and $95<m_{\gamma \gamma}<155$ (530 $<$ $\left.m_{\gamma \gamma}<565\right) \mathrm{MeV} / c^{2}$ for the high mass region.

Charged pion and kaon candidates are selected from well-reconstructed tracks. We use a pion selection algorithm to differentiate pions from kaons, with a typical selection efficiency of $95 \%$ and kaon mis-identification rate of $4 \%$. Kaons are identified as tracks failing the pion selection criteria. We reconstruct $\pi^{0}(\eta)$ candidates from pairs of photons of minimum energy 20 MeV with an invariant mass $115<m_{\gamma \gamma}<150\left(470<m_{\gamma \gamma}<\right.$ 620) $\mathrm{MeV} / c^{2}$. We require all pion, $\eta$ and kaon candidates
to have a momentum in the laboratory frame greater than $600(425) \mathrm{MeV} / c$ in the low (high) mass region.
The selected pion, $\eta$, kaon and high-energy photon candidates are combined to form $B$ meson candidates consistent with one of the seven decay modes. The charged particles are combined to form a common vertex with a $\chi^{2}$ probability greater than $1 \%$. We use the kinematic variables $\Delta E=E_{B}^{*}-E_{\text {beam }}^{*}$, where $E_{B}^{*}$ is the energy of the $B$ meson candidate and $E_{\text {beam }}^{*}$ is the beam energy, and $m_{\mathrm{ES}}=\sqrt{E_{\text {beam }}^{* 2}-\vec{p}_{B}^{* 2}}$, where $\vec{p}_{B}^{*}$ is the momentum of the $B$ candidate. We consider candidates in the range $-0.3<\Delta E<0.2 \mathrm{GeV}$ and $m_{\mathrm{ES}}>5.22 \mathrm{GeV} / c^{2}$.
Contributions from continuum processes $\left(e^{+} e^{-} \rightarrow q \bar{q}\right.$, with $q=u, d, s, c$ ) are reduced by considering only events for which the ratio $R_{2}$ of second-to-zeroth order FoxWolfram moments [9] is less than 0.98. To further discriminate between the jet-like continuum background and the more spherically symmetric signal events, we compute the angle $\theta_{T}^{*}$ between the photon momentum and the thrust axis of the rest of the event (ROE) and require $\left|\cos \left(\theta_{T}^{*}\right)\right|<0.8$. The ROE is defined as all charged tracks and neutral energy deposits that are not used to reconstruct the $B$ candidate.
Ten other event shape variables that distinguish between signal and continuum events are combined in a neural network (NN). These include the ratio $R_{2}^{\prime}$, which is $R_{2}$ is calculated in the frame recoiling against the photon momentum, the $B$ meson production angle with respect to the beam axis in the CM frame, $\theta_{B}^{*}$, and the L-moments [10] of the ROE with respect to either the thrust axis of the ROE or the direction of the high energy photon. Differences in lepton, pion and kaon production between background and $B$ decays are exploited by including several flavor-tagging variables applied to the ROE [11]. Using the NN output, we reject $99 \%$ of continuum background while preserving $25 \%$ of signal decays

After all selections are applied, there remain events with more than one $B$ candidate. In these events the candidate with the reconstructed $\pi^{0}$ or $\eta$ mass closest to nominal is retained. Where there is no $\pi^{0}$ or $\eta$ we retain the candidate with the highest vertex $\chi^{2}$ probability.

The signal yields in the data for the sum of the seven decay modes are determined from two-dimensional extended maximum likelihood fits to the $\Delta E$ and $m_{\mathrm{ES}}$ distributions. We consider the following contributions: signal, combinatorial backgrounds from continuum processes, backgrounds from other $B$ decays, and cross-feed from mis-reconstructed $B \rightarrow X \gamma$ decays. The fits to $B \rightarrow X_{d} \gamma$ events contain components from misidentified $b \rightarrow s \gamma$ decays, and we neglect the small $b \rightarrow d \gamma$ background in the fits to $B \rightarrow X_{s} \gamma$ events.

Each contribution is modeled by a probability density function (PDF) that is determined from Monte Carlo (MC) simulated events unless otherwise specified. For the misidentified signal cross-feed components, we use a binned two-dimensional PDF to account for correlations. All the other PDFs are products of one-dimensional func-
tions of $\Delta E$ and $m_{\mathrm{ES}}$. For signal, the $m_{\mathrm{ES}}$ spectrum is described by a Crystal Ball function [12], and $\Delta E$ by a Cruijff function [13]. The parameters of these functions are determined from the fit to the high-statistics $B \rightarrow X_{s} \gamma$ data sample. We use these fitted values to fix the signal shape in the fits to $B \rightarrow X_{d} \gamma$ events.

The remaining $B$ backgrounds contain a small component that peaks in $m_{\mathrm{ES}}$ but not $\Delta E$, which is modeled by a Gaussian distribution in $m_{\text {ES }}$. Continuum and other non-peaking backgrounds are described by an ARGUS shape [14] in $m_{\text {ES }}$ and a second-order polynomial in $\Delta E$.

We perform separate fits for $B \rightarrow X_{d} \gamma$ and $B \rightarrow X_{s} \gamma$ in each of the hadronic mass ranges $0.5-1.0 \mathrm{GeV} / c^{2}$ and $1.0-2.0 \mathrm{GeV} / c^{2}$. For each of the four fits, we combine the component PDFs and fit for the signal, generic $B$ and continuum yields, the ARGUS and two polynomial shape parameters. We scale the cross-feed contributions proportionally to the fitted signal yield, re-fit and iterate until the procedure converges. Projections of $m_{\mathrm{ES}}$ and $\Delta E$ from fits to data for $B \rightarrow X_{s} \gamma$ and $B \rightarrow X_{d} \gamma$ are shown in the high mass regions in Figure 1. Table II gives the signal yields, efficiencies (after corrections for systematic effects) and partial branching fractions $(\mathcal{P B})$. We calculate $\mathcal{P B}$ using $\mathcal{P B}(B \rightarrow X \gamma)=N_{S} /\left(2 \epsilon N_{B \bar{B}}\right)$, where $N_{B \bar{B}}$ is the number of $B \bar{B}$ pairs in the data sample.


FIG. 1: Projections of $\Delta E$ with $5.275<m_{\mathrm{ES}}<5.286 \mathrm{GeV} / c^{2}$ for (a) $B \rightarrow X_{s} \gamma$ and (b) $B \rightarrow X_{d} \gamma$, and of $m_{\mathrm{ES}}$ with $-0.1<\Delta E<0.05 \mathrm{GeV}$ for (c) $B \rightarrow X_{s} \gamma$ and (d) $B \rightarrow X_{d} \gamma$ in the mass range $1.0-2.0 \mathrm{GeV} / c^{2}$. Data points are compared with the sum of all the fit contributions (solid line). The jagged line is an artifact of the fit projection over the sum of several binned histograms. The dashed line shows the signal component.

We have investigated a number of sources of systematic uncertainty in the measurement of the partial branching
fractions, some of which are common to both $B \rightarrow X_{d} \gamma$ and $B \rightarrow X_{s} \gamma$ and cancel in the ratio of branching fractions (see Table III those that do not cancel in the ratio are marked by an asterisk). Uncertainties in tracking efficiency, particle identification, $\gamma$ and $\pi^{0}$ reconstruction, and the $\pi^{0} / \eta$ veto have been evaluated using independent control samples of data and MC simulated events, and incorporated into our analysis. Uncertainty due to the NN selection has been evaluated by comparing the efficiency of the selection in data and MC for the $B \rightarrow X_{s} \gamma$ events, which are relatively free of background, assuming that potential discrepancies between data and MC are the same for the $B \rightarrow X_{d} \gamma$ sample. The means and widths of the signal PDF are varied within the range allowed by the fit to the $B \rightarrow X_{s} \gamma$ data, accounting for correlations. Other PDF parameters are also varied within the $1 \sigma$ limits determined from the fit to MC. We vary the $b \rightarrow s \gamma$ background in the fit to $B \rightarrow X_{d} \gamma$ by the statistical uncertainty on our measurement of those decays. The signal cross-feed originating from our measured channels is varied by the statistical uncertainty on our measurement; other signal cross-feed backgrounds by $\pm 50 \%$. An additional uncertainty on the efficiency arises from the fragmentation of the hadronic system among the measured final states. For $B \rightarrow X_{s} \gamma$ the uncertainty is constrained by the errors on the measured data; for $B \rightarrow X_{d} \gamma$ an estimate is obtained from the difference between the default phase-space fragmentation (see below) and a re-weighting using the measured data/MC differences in $B \rightarrow X_{s} \gamma$.

To obtain inclusive $\mathcal{B}(b \rightarrow s \gamma)$ and $\mathcal{B}(b \rightarrow d \gamma)$ we need to correct the partial $\mathcal{B}$ values in Table 【I for the fractions of missing final states. After correcting for the $50 \%$ of missing decay modes with neutral kaons, the low mass $B \rightarrow X_{s} \gamma$ measurement is found to be consistent with previous measurements of the rate for $B \rightarrow K^{*} \gamma$ [15]. For the low mass $B \rightarrow X_{d} \gamma$ region, we correct for the small amount of non-reconstructed $\omega$ final states (for example, $\omega \rightarrow \pi^{0} \gamma$ ), and find a partial branching fraction consistent with previous measurements of $\mathcal{B}(B \rightarrow(\rho, \omega) \gamma)$ [15]. We assume that non-resonant decays do not contribute in this region.

In the high mass region, the missing fractions depend on the fragmentation of the hadronic system and are expected to be different for $X_{d}$ and $X_{s}$. In our signal MC, fragmentation is modeled by selecting an array of finalstate particles and resonances according to the phasespace probability of the final state, as implemented by JETSET [16]. We further constrain the distribution of $X_{s}$ final states to that observed for our seven decay modes as well as the distributions of a number of other states measured in [17]. According to this MC model we reconstruct $43 \%$ of the total width in $b \rightarrow d \gamma$, and $36 \%$ in $b \rightarrow s \gamma$. A further $37 \%$ of the width of $b \rightarrow s \gamma$ is constrained by the isospin relation between charged and neutral kaon decays. We explore the uncertainty in the correction for missing modes by considering several alternative models: replacing $50 \%$ of $b \rightarrow s \gamma$ and $b \rightarrow d \gamma$

TABLE II: Signal yields $\left(N_{S}\right)$, efficiencies $(\epsilon)$, partial branching fractions $(\mathcal{P B})$, inclusive branching fractions $(\mathcal{B})$ and the ratio of inclusive branching fractions for the measured decay modes. The first error is statistical and second is systematic (including an error from extrapolation to missing decay modes, for the inclusive $\mathcal{B}$ ).

|  | $M\left(X_{s}\right) 0.5-1.0$ | $M\left(X_{d}\right) 0.5-1.0$ | $M\left(X_{s}\right) 1.0-2.0$ | $M\left(X_{d}\right) 1.0-2.0$ | $M\left(X_{s}\right) 0.5-2.0$ | $M\left(X_{d}\right) 0.5-2.0$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $N_{S}$ | $804 \pm 33$ | $35 \pm 9$ | $990 \pm 42$ | $56 \pm 14$ | - | - |
| $\epsilon$ | $4.5 \%$ | $3.1 \%$ | $1.6 \%$ | $1.9 \%$ | - | - |
| $\mathcal{P B}\left(\times 10^{-6}\right)$ | $19 \pm 1 \pm 1$ | $1.2 \pm 0.3 \pm 0.1$ | $66 \pm 3 \pm 6$ | $3.2 \pm 0.8 \pm 0.5$ | - | - |
| $\mathcal{B}\left(\times 10^{-6}\right)$ | $38 \pm 2 \pm 2$ | $1.3 \pm 0.3 \pm 0.1$ | $192 \pm 8 \pm 29$ | $7.9 \pm 2.0 \pm 2.2$ | $230 \pm 8 \pm 30$ | $9.2 \pm 2.0 \pm 2.3$ |
| $\frac{\mathcal{B}(b \rightarrow d \gamma)}{\mathcal{B}(b \rightarrow s \gamma)}$ | $0.033 \pm 0.009 \pm 0.003$ | - | $0.040 \pm 0.009 \pm 0.010$ |  |  |  |

TABLE III: Systematic errors on the measured partial and inclusive branching fractions $\mathcal{B}$. Systematic errors that do not cancel in the ratio of rates are marked with (*).

| Systematic | $M\left(X_{s}\right)$ |  |  | $M\left(X_{d}\right)$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Error Source | $0.5-1.0$ | $1.0-2.0$ | $0.5-1.0$ | $1.0-2.0$ |  |
| Track selection | $0.3 \%$ | $0.4 \%$ | $0.3 \%$ | $0.4 \%$ |  |
| Photon reconstruction | $1.8 \%$ | $1.8 \%$ | $1.8 \%$ | $1.8 \%$ |  |
| $\pi^{0} / \eta$ reconstruction | $0.9 \%$ | $1.1 \%$ | $1.4 \%$ | $1.6 \%$ |  |
| Neural network | $1.1 \%$ | $4.9 \%$ | $1.1 \%$ | $4.9 \%$ |  |
| $B$ counting | $0.6 \%$ | $0.6 \%$ | $0.6 \%$ | $0.6 \%$ |  |
| PID $\left(^{*}\right)$ | $2.0 \%$ | $2.0 \%$ | $2.0 \%$ | $2.0 \%$ |  |
| Fit bias $\left(^{*}\right)$ | $0.1 \%$ | $0.9 \%$ | $4.9 \%$ | $6.5 \%$ |  |
| PDF shapes $\left(^{*}\right)$ | $2.3 \%$ | $0.6 \%$ | $3.7 \%$ | $3.4 \%$ |  |
| Histogram binning $\left(^{*}\right)$ | $0.8 \%$ | $0.2 \%$ | $1.8 \%$ | $1.8 \%$ |  |
| Background $\left(^{*}\right)$ | $0.8 \%$ | $1.2 \%$ | $5.9 \%$ | $7.0 \%$ |  |
| Fragmentation $\left(^{*}\right)$ | - | $3.3 \%$ | - | $5.1 \%$ |  |
| Signal model | - | $5.8 \%$ | - | $6.0 \%$ |  |
| Error on partial $\mathcal{B}$ | $4.0 \%$ | $9.0 \%$ | $9.3 \%$ | $14.2 \%$ |  |
| Missing $\geq 5$ body |  | $9.6 \%$ |  | $18.2 \%$ |  |
| Other missing states |  | $7.5 \%$ |  | $15.3 \%$ |  |
| Spectrum Model |  | $1.8 \%$ |  | $1.6 \%$ |  |
| Error on inclusive $\mathcal{B}$ | $4.0 \%$ | $15.2 \%$ | $9.3 \%$ | $27.7 \%$ |  |

hadronic final states with a mix of resonances; varying $b \rightarrow s \gamma$ fragmentation constraints within their statistical uncertainties; and setting the $b \rightarrow d \gamma$ fragmentation rates to those of their corresponding $b \rightarrow s \gamma$ states. The resulting missing fractions vary by up to $50(40) \%$ relative to the nominal model in $B \rightarrow X_{s} \gamma\left(B \rightarrow X_{d} \gamma\right)$. We therefore independently vary final states with $\geq 5$ stable hadrons, or with $\geq 2 \pi^{0}$ or $\eta$ mesons, by $\pm 50(40) \%$.

Results for the corrected $\mathcal{B}$ values are shown in Table II Adding the two mass regions, taking into account a partial cancellation of the missing fraction uncertainties in the ratio of $b \rightarrow d \gamma$ to $b \rightarrow s \gamma$, we find $\mathcal{B}(b \rightarrow$ $d \gamma) / \mathcal{B}(b \rightarrow s \gamma)=0.040 \pm 0.009$ (stat.) $\pm 0.010$ (syst.) in the mass range $M(X)<2.0 \mathrm{GeV} / c^{2}$.

We correct for the unmeasured region $M(X)>$ $2.0 \mathrm{GeV} / c^{2}$ using the spectral shape from KaganNeubert [18] with the kinetic parameters $\left(m_{b}, \mu_{\pi}^{2}\right)=$
(4.65 $\pm 0.05,-0.52 \pm 0.08)$ extracted from fits of $b \rightarrow s \gamma$ and $b \rightarrow c \ell \nu$ data [19], yielding corrections of $1.66 \pm 0.03$; the spectra for $b \rightarrow s \gamma$ and $b \rightarrow d \gamma$ are expected to be almost identical.

Conversion of the ratio of inclusive branching fractions to the ratio $\left|V_{t d} / V_{t s}\right|$ is done according to [6], which requires the Wolfenstein parameters $\bar{\rho}$ and $\bar{\eta}$ as input. However, since the world average of these quantities relies on previous measurements of $\left|V_{t d} / V_{t s}\right|$ we instead re-express $\bar{\rho}$ and $\bar{\eta}$ in terms of the world average of the independent CKM angle $\beta$ [15]. This procedure yields a value of $\left|V_{t d} / V_{t s}\right|=0.199 \pm 0.022$ (stat.) $\pm 0.024$ (syst.) $\pm 0.002$ (th.), compatible and competitive with more model-dependent determinations from the measurement of the exclusive modes $B \rightarrow(\rho, \omega) \gamma$ and $B \rightarrow K^{*} \gamma[4, ~ 5]$.

In summary, we have measured the inclusive $b \rightarrow s \gamma$ and $b \rightarrow d \gamma$ transition rates using a sum of seven final states in the hadronic mass range up to $2.0 \mathrm{GeV} / c^{2}$, making the first significant observation of the $b \rightarrow d \gamma$ transition in the region above $1.0 \mathrm{GeV} / c^{2}$. The value of $\left|V_{t d} / V_{t s}\right|$ derived from these measurements has an experimental uncertainty approaching that from the measurement of exclusive decays $B \rightarrow(\rho, \omega) \gamma$ and $B \rightarrow K^{*} \gamma$, but a significantly smaller theoretical uncertainty.

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