

Subfemtotesla Scalar Atomic Magnetometry Using Multipass Cells

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Scalar atomic magnetometers have many attractive features but their sensitivity has been relatively poor. We describe a Rb scalar gradiometer using two multipass optical cells. We use a pump-probe measurement scheme to suppress spin-exchange relaxation and two probe pulses to find the spin precession zero crossing times with a resolution of 1 psec. We realize a magnetic field sensitivity of 0.54 fT/Hz^{1/2}, which improves by an order of magnitude the best scalar magnetometer sensitivity and exceeds, for example, the quantum limit set by the spin-exchange collisions for a scalar magnetometer with the same measurement volume operating in a continuous regime.

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Alkali-metal magnetometers can surpass superconducting quantum interference devices as the most sensitive detectors of a magnetic field, reaching a sensitivity below 1 fT/Hz^{1/2} [1,2], but only if they are operated near zero magnetic field to eliminate spin relaxation due to spin-exchange collisions [3,4]. Many magnetometer applications, such as searches for permanent electric dipole moments [5], detection of nuclear magnetic resonance signals [6], and low-field magnetic resonance imaging [7], require sensitive magnetic measurements in a finite magnetic field. In addition, scalar magnetometers measuring the Zeeman frequency are unique among magnetic sensors in being insensitive to the direction of the field, making them particularly suitable for geomagnetic mapping [8] and field measurements in space [9,10]. The sensitivity of scalar magnetometers has been relatively poor, as summarized recently in Ref. [11]. The best directly measured scalar magnetometer sensitivity is equal to 7 fT/Hz^{1/2} with a measurement volume of 1.5 cm³ [12], while estimates of fundamental sensitivity per unit measurement volume for various types of scalar alkali-metal magnetometers range from several fT cm^{3/2}/Hz^{1/2} [13,14] to about 1 fT cm^{3/2}/Hz^{1/2} [12]. Here we describe a new type of scalar atomic magnetometer using multipass vapor cells [15,16] and operating in a pulsed pump-probe mode [17] to achieve magnetic field sensitivity of 0.54 ± 0.03 fT/Hz^{1/2} with a measurement time of 0.8 msec and measurement volume of 0.66 cm³ in each multipass cell. The magnetometer sensitivity approaches, for the first time, the fundamental limit set by Rb-Rb collisions. We also develop here a quantitative method to analyze significant effects of atomic diffusion on the spectrum of the spin-projection noise in vapor cells with buffer gas using a spin time-correlation function.

The sensitivity of an atomic magnetometer, as any other frequency measurement, is fundamentally limited by spin projection noise and spin relaxation. For N spin-1/2 atoms with coherence time T_2 the sensitivity after a long measurement time $t \gg T_2$ is given by [18] $\delta B = \sqrt{2e/NT_2}t/\gamma$,

where γ is the gyromagnetic ratio. Spin squeezing techniques can reduce this uncertainty by a factor of \sqrt{e} but do not change the scaling with N [18–20]. The number of atoms can be increased until collisions between them start to limit T_2 . Writing $T_2^{-1} = n\sigma\bar{v}$, where n is the density of atoms, σ is the spin relaxation cross section, and \bar{v} is the average collisional velocity, and taking $t = 0.5$ s to calculate the magnetic field spectral noise density B_n in T/Hz^{1/2}, we obtain

$$B_n = (2/\gamma)\sqrt{e\sigma\bar{v}/V}. \quad (1)$$

Thus the magnetic field spectral noise density per measurement volume V is fundamentally limited by the spin-relaxation cross section. It also sets the limit on the minimum energy resolution per unit bandwidth $\varepsilon = B_n^2 V / 2\mu_0$ of atomic magnetometers, which can, in certain cases, approach \hbar [2]. In hot alkali-metal vapor magnetometers operating in a finite magnetic field, the relaxation is dominated by the spin-exchange cross section $\sigma_{SE} = 1.9 \times 10^{-14}$ cm². Taking into account ⁸⁷Rb nuclear spin $I = 3/2$, which reduces the spin projection noise by a factor of 2 and the relaxation rate due to spin-exchange collisions by a factor of 5 [12], we get from Eq. (1) a limit of 0.49 fT cm^{3/2}/Hz^{1/2}.

However, alkali-metal spin exchange is a nonlinear process with a relaxation rate that changes in time, which modifies the fundamental sensitivity given by Eq. (1). The spin-exchange relaxation can be reduced by optical pumping of atoms into a stretched spin state [21], but fundamental sensitivity for a scalar magnetometer still remains limited by spin exchange if it is operated in a continuous optical pumping regime [12]. The limit calculated in Ref. [12] for a quantum-nondemolition (QND) measurement of the ⁸⁷Rb spin is 0.51 fT cm^{3/2}/Hz^{1/2}. On the other hand, if the magnetometer is operated in a pulsed pump-probe regime and uses QND measurements, the sensitivity can be asymptotically limited by the spin-destruction cross section, which is as low as $\sigma_{SD} = 10^{-18}$ cm² for K atoms,

leading to a potential improvement by 2 orders of magnitude [22]. Thus, it is particularly interesting to study spin projection noise in scalar alkali-metal magnetometers, both because it presents a real limit to their practical sensitivity and because of large improvement possible from spin-squeezing techniques.

A key parameter for QND measurements of spin-projection noise is the optical depth on resonance $OD = \sigma_0 n l$, where σ_0 is the probe laser absorption cross section on resonance and l is the path length of the probe beam through the atomic vapor [23]. We have developed multipass optical cells with mirrors internal to the alkali-metal vapor cell to increase l by 2 orders of magnitude [16]. Compared to optical cavities, multipass cells have a much larger interaction volume and allow direct recording of large optical rotations. We use two 42-pass cells placed in the same vapor cell as a gradiometer with a baseline equal to the 1.5 cm distance between the cells; see Fig. 1(a). The cells have cylindrical mirrors with a 10 cm radius of curvature separated by 30 mm. One of the mirrors in each cell has a 2.5 mm diameter hole for entrance and exit of the probe beam focused to a waist diameter of 1.9 mm. The glass vapor cell contains a drop of enriched ^{87}Rb and 70 torr N_2 gas. A boron-nitride oven is used to heat the vapor cell using ac currents at 600 kHz to 120 °C, giving an $OD \sim 5000$. The cell is placed in a bias magnetic field of 72.9 mG in the \hat{z} direction generated by an ultrastable

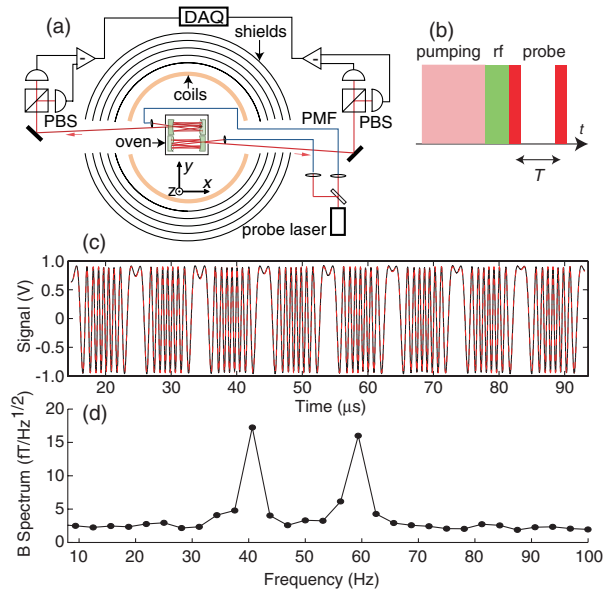


FIG. 1 (color online). (a) Experiment setup. PBS: polarization beam splitter; PMF: polarization maintaining fiber; DAQ: data acquisition card. (b) The timing of the pulsed operation. (c) Optical rotation (black line) recorded for one probe pulse at atom density of $0.8 \times 10^{13}/\text{cm}^3$ together with a fitted curve (red dashed line). (d) Magnetic field noise spectrum obtained in the gradiometer in the presence of a calibrating magnetic field gradient at 40 Hz. The peak at 60 Hz is due to ac line noise.

custom current source and is enclosed in a five-layer magnetic shield.

We measure the atom density n from the transverse relaxation T_2 at low polarization, which is dominated by spin-exchange collisions with a known cross section [16]. The number of atoms participating in the measurement at any given time $N = nV_b$ is determined from the area of Faraday rotation power spectral density for unpolarized atoms [24]. We make measurements of the noise peak at two different magnetic fields and take their difference to remove the background dominated by photon shot noise. Figure 2(a) shows one example of unpolarized power spectral density obtained using this method, which gives $V_b = 0.35(2) \text{ cm}^3$ for each cell.

While diffusion does not affect the area under the spin noise peak, it causes the line shape of the noise spectrum to deviate from a simple Lorentzian. To analyze it quantitatively, we consider the time autocovariance function of the Faraday rotation signal $\phi(t)$, which is given by the Fourier transform of the power spectrum. One can show that

$$\langle \phi(t) \phi(t + \tau) \rangle = \sum_i \left(\frac{c r_e f D_i}{(2I + 1) \int I(\mathbf{r}) dy dz} \right)^2 \times n \langle F_i^2 \rangle \times \int I(\mathbf{r}_1) G(\mathbf{r}_1 - \mathbf{r}_2, \tau) I(\mathbf{r}_2) d^3 \mathbf{r}_1 d^3 \mathbf{r}_2, \quad (2)$$

where the sum is taken over the two alkali-metal hyperfine states, $F_a = I + 1/2$ and $F_b = I - 1/2$, and $\langle F_i^2 \rangle = F_i(F_i + 1)(2F_i + 1)/6(2I + 1)$. The dispersion factor is $D_i = 1/(\nu_i - \nu)$ for far detuning of the probe frequency

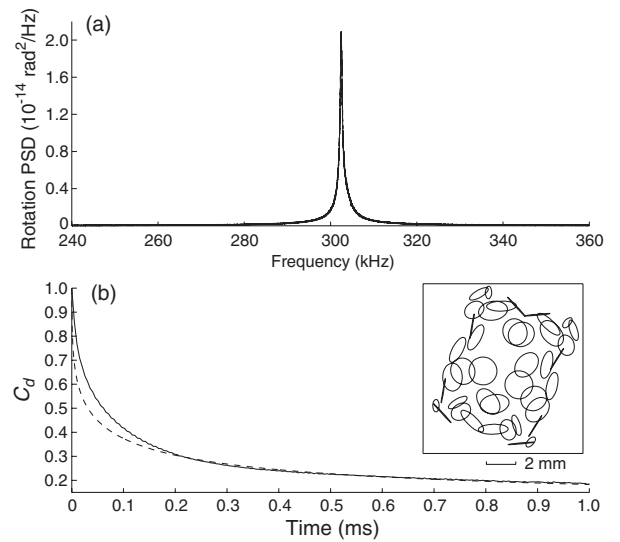


FIG. 2. (a) Unpolarized atom spin noise spectrum taken at 0.42 G with atom density of $1.2 \times 10^{13}/\text{cm}^3$ after subtraction of the photon shot noise background from a spin noise measurement at low magnetic field. (b) Spin correlation function due to the diffusion of the atoms out of the probe beam. Solid line (dashed line) is the experimental (calculated) result with atom density of $1.2 \times 10^{13}/\text{cm}^3$. The inset shows the calculated beam pattern at the center of the cavity.

ν from the hyperfine resonances ν_i . Here $I(\mathbf{r})$ is the total probe laser intensity at position \mathbf{r} , including all beam passes inside the cavity, and $G(r, \tau)$ is the Green's function for spin evolution with a diffusion coefficient D and a transverse relaxation time T_2 , $G(r, \tau) = e^{-r^2/4D\tau - \tau/T_2} / (4\pi D\tau)^{3/2}$. The intensity profile of the probe laser in the cell is determined by measuring the input Gaussian beam size and calculating the astigmatic Gaussian beam propagation in the multipass cell [25]. An example of the calculated intensity profile in the middle of the cell is shown in the inset of Fig. 2. The effective number of atoms participating in the measurement is defined as the number of atoms that would generate the same spin noise area $\langle \phi(t)^2 \rangle$ if interrogated with a uniform probe intensity. We obtain a generalization of a result given in Ref. [24] that works for laser beams with varying focusing and overlap,

$$N = n l^2 \frac{[\int I(\mathbf{r}) dy dz]^2}{\int I(\mathbf{r})^2 dV}, \quad (3)$$

where l is the total probe laser path in the multipass cell. Based on the calculated intensity profile, we obtain $V_b = 0.36 \text{ cm}^3$, in good agreement with direct experimental measurements. In Fig. 2(b) we compare the diffusion component of the calculated spin time-correlation function $C_d(\tau) = \langle \phi(t)\phi(t+\tau) \rangle e^{\tau/T_2} / \langle \phi(t)^2 \rangle$ with the experimental measurement obtained by taking the Fourier transform of the spin noise peak after centering it at zero frequency and correcting for the transverse spin relaxation time $C_d(\tau) = C(\tau)e^{\tau/T_2}$. They agree well except at early times due to deviations from a perfect Gaussian of tightly focused beams within the cell, indicating that Green's function method can quantitatively describe the line shape of the spin noise spectrum in the presence of diffusion with multiple overlapping laser beams.

Figure 1(b) shows the timing for magnetic field measurements. For an optical pumping pulse, which lasts 14 msec, we use two circular polarized beams on resonance with the $D1$ transitions from both ground hyperfine states. Then we apply a $\pi/2$ rf pulse lasting three periods of the Zeeman resonance frequency. We apply the first probe light pulse shortly after the rf excitation and the second probe pulse with a delay time T from the first one. The probe laser is tuned to 794.780 nm and the power of the light exiting from each multipass cell is about 0.5 mW. We turn on and off the probe light slowly compared with the Larmor period using an acousto-optic modulator to suppress transient spin excitation. The pump-probe cycle is repeated every 16.6 msec, synchronized with 60 Hz to reduce its influence.

Figure 1(c) shows a typical record of the optical rotation signal during one of the probe pulses. We fit the data using the equation [16]

$$V = V_0 \sin \left[2\phi \left(1 - \frac{t-t_c}{T_2} \right) \sin[\omega(t-t_c)] + \psi \right] + B. \quad (4)$$

We find the time of zero crossings t_{c1}, t_{c2} of the first and second pulses and calculate $T_c = t_{c2} - t_{c1}$, which gives a measure of the magnetic field $B = 2\pi m / \gamma T_c$, where m is the integer number of spin precession cycles between the measured zero crossings. If the measurements are repeated with overall duty cycle d , then the magnetic field sensitivity per $\text{Hz}^{1/2}$ is given by

$$B_n = B \delta T_c \sqrt{2/dT_c}, \quad (5)$$

where δT_c is the standard deviation of repeated measurements of T_c .

The two multipass cells work as a gradiometer to measure $\partial B_z / \partial y$ with a noise level that is $\sqrt{2}$ larger than given by Eq. (5) while canceling common magnetic noise. The calibration of a scalar magnetometer is given by fundamental constants, but we check its response to gradients by applying a calibrated magnetic field gradient $\partial B_z / \partial y$ with rms amplitude of 21.6 fT/cm oscillating at 40 Hz. For this measurement the atomic density is $1.4 \times 10^{13} / \text{cm}^3$, with the probe pulse length of four Larmor periods, the separation between two probe pulses $T = 823 \mu\text{s}$, and the cycle period is 5 ms. Figure 1(d) shows the Fourier spectrum of the magnetic field difference between the two cells in the presence of the gradient. Integration of the 40 Hz peak in the spectrum gives an rms signal of 33 fT, in good agreement with the expected 32.4 fT field difference between the centers of the two cells created by the gradient field.

The limiting fundamental noise sources include atomic spin projection noise (ASN) and photon shot noise (PSN), while technical sources include magnetic shield noise and time jitter of the data acquisition. One important feature of our arrangement is backaction evasion of quantum fluctuations of the probe beam circular polarization due to zero spin polarization of atoms in the \hat{z} direction following the $\pi/2$ pulse [24]. Figure 3 shows the dependence of the noise on the rf excitation amplitude when it deviates from the $\pi/2$ amplitude. We compare it to the noise in T_c when

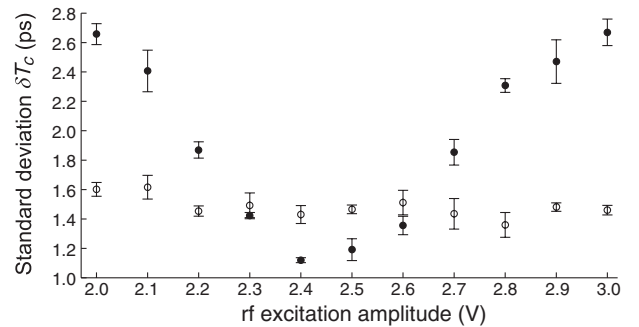


FIG. 3. The dependence of the standard deviation δT_c on the rf pulse amplitude. Empty (solid) circles denote the backaction evasion with stroboscopic modulation (normal modulation) of probe light. Here the probe pulse length and T are equal to four Larmor periods.

using a stroboscopic probe modulation backaction evasion scheme [22], where the probe beam is modulated at twice the Larmor frequency with a 20% duty cycle. The results confirm that the magnetometer works in a backaction-free regime. The magnetic shield gradient noise is due to thermal Johnson currents and is calculated based on known electrical conductivity of the inner μ -metal shield, giving $0.40(5)$ fT/Hz $^{1/2}$ [26]. The time jitter noise is determined by recording the signals from the same multipass cell with two acquisition channels and ranges from 0.3 to 0.5 ps depending on the length of the probe pulse.

Figure 4 shows the magnetic field sensitivity for a range of parameters. The experimental duty cycle is limited to 10% by available pump laser power, but we use $d = 1$ in Eq. (5) to find the fundamental sensitivity from the measured uncertainty δT_c . Figure 4(a) shows the nonlinear relaxation of transverse spin polarization due to spin exchange at four different densities, from which we find that the initial transverse polarization is equal to $0.96(1)$. We plot the sensitivity as a function of the probe pulse length t_p in Fig. 4(b). The variance in T_c due to PSN and data acquisition noise decreases as $1/t_p$ and the variance due to ASN

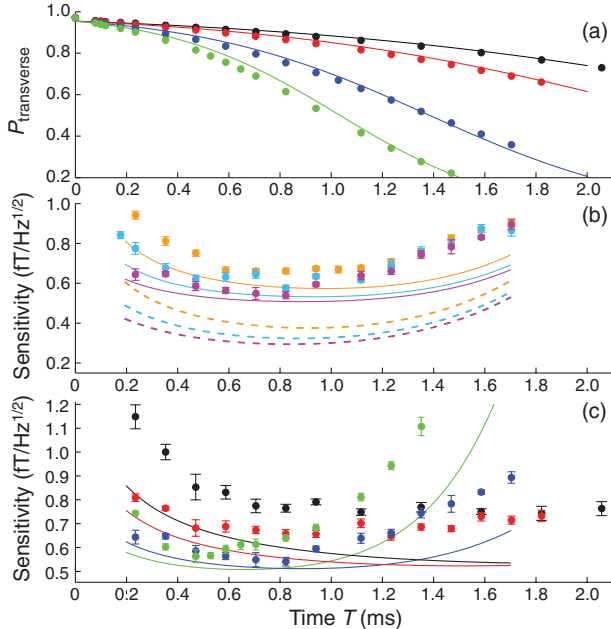


FIG. 4 (color). (a) Relaxation of transverse polarization P_t (points) for $n = 1.9$ (green), 1.4 (blue), 0.8 (red), and $0.6(\text{black}) \times 10^{13}/\text{cm}^3$ together with theoretical prediction (lines). (b) The points are the experimental results of magnetic field sensitivity at $n = 1.4 \times 10^{13}/\text{cm}^3$, with probe pulse length of 4 (orange), 8 (cyan), and 12 (purple) Larmor periods. Solid (dashed) lines are the theoretically calculated sensitivity based on measured parameters with (without) magnetic shield noise and time jitter noise. (c) Experiment results (points) of magnetic field sensitivity with probe length of 12 Larmor periods at different atom densities, with the same color notation as plot (a), together with theoretical predictions (lines).

also decreases because atom diffusion effectively involves more atoms into the measurement. The effective number of atoms N_m participating in the measurement after a pulse time t_p can be found using the diffusion correlation function $N_m = nV_b t_p / [2 \int_0^{t_p} (1 - t/t_p) C_d(t) dt]$. For the longest pulse length of $230 \mu\text{sec}$ we obtain $V_m = 1.9V_b$, corresponding to an effective interaction volume of 0.66 cm^3 . We also show a theoretical estimate of the sensitivity including ASN, PSN, magnetic gradient noise, and time jitter noise in Fig. 4(b) with solid lines and only ASN and PSN with broken lines; these are derived in the Supplemental Material [27] in the limit of high spin polarization. Figure 4(c) shows similar results at other densities. When the atom density increases, the optimal T decreases because of faster spin relaxation, indicating that the magnetometer works in a Rb collision-limited regime. For the longest probe pulse length and atom density of $1.4 \times 10^{13}/\text{cm}^3$, the experimental data show a best sensitivity of 0.54 ± 0.03 fT/Hz $^{1/2}$, which is 10% above the predicted value. In the absence of magnetic shield noise the intrinsic sensitivity is projected to be 0.3 fT/Hz $^{1/2}$, dominated by ASN. For comparison, the quantum limit for the best previously considered scalar magnetometer using QND measurements with continuous pumping is equal to 0.63 fT/Hz $^{1/2}$ for the same measurement volume [12].

In conclusion, we described a scalar magnetometer based on multipass atomic vapor cells. It uses a pulsed mode with a high initial polarization and reaches the spin-exchange collision limited regime where the sensitivity is largely independent of atom density. The best sensitivity obtained is 0.54 fT/Hz $^{1/2}$ with an effective interaction volume of 0.66 cm^3 , which is an order of magnitude improvement over the previous best sensitivity for a scalar magnetometer. We also developed a quantitative method for analyzing the effect of diffusion on quantum spin noise using spin time-correlation function. By relying on precision timing measurements with a very wide dynamic range and fractional sensitivity of $7 \times 10^{-11}/\text{Hz}^{1/2}$ this magnetometer opens the possibility of fundamentally new applications, for example unshielded detection of magnetoencephalography signals [28]. The sensitivity per unit volume can be further improved in this system by reducing the decay of the spin time-correlation function due to atomic diffusion, which will allow suppression of ASN due to spin squeezing between two probe pulses. The spin correlation decay is dominated by a few tightly focused beam spots in the multipass cell and can be reduced by modifying multipass cell parameters to avoid tight beam focusing. The magnetic shield noise can also be reduced by using a ferrite shield [29].

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