

## Subwavelength imaging at optical frequencies using a transmission device formed by a periodic layered metal-dielectric structure operating in the canalization regime

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Imaging with subwavelength resolution using a periodic metal-dielectric layered structure is demonstrated. The structure operates in canalization regime as a transmission device and it does not involve negative refraction and amplification of evanescent modes. The thickness of the structure has to be an integer number of half-wavelengths and can be made as large as required for certain applications, in contrast to the solid metallic slabs operating with subwavelength resolution which have to be much thinner than the wavelength. Resolution of  $\lambda/20$  at 600 nm wavelength is confirmed by numerical simulation for a 300 nm thick structure formed by a periodic stack of 10 nm layers of glass with  $\epsilon=2$  and 5 nm layers of metal-dielectric composite with  $\epsilon=-1$ . Resolution of  $\lambda/60$  is predicted for a structure with same thickness, period and operating frequency, but formed by 7.76 nm layers of silicon with  $\epsilon=15$  and 7.24 nm layers of silver with  $\epsilon=-14$ .

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The possibility of imaging with subwavelength resolution was first reported by Pendry in 2000.<sup>1</sup> It was shown that the slab of left-handed material,<sup>2</sup> a medium with both negative permittivity and permeability, can create images with nearly unlimited resolution. This idea impeached validity of classical restriction on resolution of imaging systems, diffraction limit, and became a starting point for creation of new research area of metamaterials,<sup>3</sup> artificial media possessing extraordinary electromagnetic properties usually not available in the natural materials. The idea of Pendry's perfect lens is based on such exotic phenomena observable in left-handed media as backward waves, negative refraction and amplification of evanescent waves. The far-field of a source is focused due to effects of backward waves and negative refraction. The near field of the source, which contains subwavelength details, is recovered in the image plane because of the amplification of evanescent modes in the slab. Currently, the samples of left-handed materials are created only in microwave region.<sup>4</sup> The creation of left-handed materials at THz frequencies and in optical range meets with problems related to the difficulty in getting required magnetic properties<sup>5,6</sup> which have to be created artificially. In the absence of magnetic properties the lenses formed by materials with negative permittivity only (for example, silver at optical frequencies) are still capable to create images with subwavelength resolution, but the operation is restricted to *p*-polarization only and the lens has to be thin as compared to the wavelength.<sup>1</sup> This idea was confirmed by recent experimental results<sup>7,8</sup> which demonstrated the reality of subwavelength imaging using silver slabs in optical frequency range. The resolution of such lenses is restricted by losses in the silver, but this problem can be alleviated by cutting the slab into the multiple thin layers<sup>9,10</sup> and introduction of active materials.<sup>11</sup> Unfortunately, at the moment there is no recipe how to increase the thickness of such lenses other than the introduction of artificial magnetism.

Competitive alternatives of left-handed media at optical frequencies are photonic crystals.<sup>12,13</sup> The negative refraction effect in photonic crystals at the frequencies close to the

band-gap edges was reported by Notomi in Ref. 14, and the subwavelength imaging using flat lenses formed by photonic crystals was demonstrated both theoretically<sup>15-18</sup> and experimentally.<sup>19,20</sup> Unfortunately, the resolution of such lenses is strictly limited by period of the crystal. This fundamental restriction was formulated and proven in Ref. 21. It means that it is impossible to get very good subwavelength resolution using lenses formed by photonic crystals since they operate in the regime when the wavelength in the crystal is comparable with lattice period, but this wavelength can not be shortened too much due to the lack of naturally available high-contrast materials.

During studies of negative refraction and imaging in photonic crystals it was noted that in the certain cases subwavelength imaging happens due to the other principle than that in left-handed materials. The evidence of non-negative refraction was reported by numerous authors<sup>22-26</sup> for the crystals operating in the first frequency band. The subwavelength lenses formed by such crystals indeed operate in the regime which does not involve negative refraction and amplification of evanescent waves. This regime was called in Ref. 26 as *canalization*. The slab of photonic crystal in the canalization regime operates not like usual lens which focus radiation into a focal point. It effectively works as a transmission device which delivers subwavelength images from front interface of the structure to the back one. The implementation of such a regime becomes possible if the crystal has a flat iso-frequency contour and the thickness of the slab fulfils Fabry-Perot condition (an integer number of half-wavelengths).<sup>26</sup> The flat iso-frequency contour allows to transform all spatial harmonics produced by the source, including evanescent modes, into propagating eigenmodes of the crystal. This preserves subwavelength details of the source which usually disappear with distance due to rapid spatial decay of evanescent harmonics. These propagating eigenmodes transmit image across the slab from the front interface to the back one. The possible reflections from the interfaces are eliminated with the help of Fabry-Perot resonance for transmission which in this case holds for all incidence angles due to flatness of iso-frequency contour.

The transmission devices operating in the canalization regime have same restrictions on the resolution provided by periodicity as those working in the left-handed regime: In order to get subwavelength resolution it is required to have period of the structure to be much smaller than the wavelength. In microwave region the canalization regime with  $\lambda/6$  resolution for *s*-polarization<sup>26</sup> was implemented using an electromagnetic crystal formed by a lattice of wires periodically loaded by capacitances.<sup>27</sup> Such a crystal has a resonant band-gap at very low frequencies (with wavelength/period ratio  $\lambda/a=14$ ) and does not contain high-contrast materials. The theoretical and numerical estimations<sup>26</sup> were confirmed by experimental verification<sup>28</sup> and  $\lambda/10$  resolution was demonstrated. The higher resolution can be achieved using loading by larger capacitances, but the real implementations of these ideas meet with such problems as strong losses and very narrow band-width of operation.

An excellent possibility to realize the canalization regime for *p*-polarization is provided by a wire medium, a material formed by a lattice of parallel conducting wires.<sup>29–32</sup> This material supports very special type of eigenmodes, so-called transmission line modes,<sup>32</sup> which transfer energy strictly along wires with the speed of light and can have arbitrary transverse wave vector components. It means that such modes correspond to completely flat isofrequency contour which is the main requirement for implementing the canalization regime. The detailed analytical, numerical, and experimental studies<sup>33</sup> show that flat slabs formed by the wire medium are capable to transmit subwavelength images with a resolution equal to double period of the structure which can be made as small as required. Effectively, such devices work as multi-conductor transmission lines (telegraph) or bundle of subwavelength waveguides, which perform pixel-to-pixel imaging. It is important that such structures are matched to free space and do not experience parasitic reflections from the interfaces. The subwavelength imaging with  $\lambda/15$  resolution at 1 GHz was demonstrated in the work.<sup>33</sup> The measured bandwidth of operation is 18%. Moreover, the structure is nearly not sensitive to the losses. Thus, the device can be made as thick as required. The only restriction is that the thickness should be an integer number of half-wavelengths (in order to fulfil Fabry-Perot condition).

The slab of wire medium is an unique subwavelength imaging device for microwave frequencies where metals are ideally conducting. At the higher frequencies including visible range such a device will not operate properly since the metals at these frequencies have plasma-like behavior. In the present paper we propose a different structure which can operate in the canalization regime at optical frequency range. This is a subwavelength optical telegraph which operates completely in the same principle as the slab of wire medium at microwaves. It is known that the wire medium<sup>32</sup> can be described by spatially dispersive permittivity tensor of the form

$$\bar{\bar{\epsilon}} = \mathbf{xx} + \mathbf{yy} + \epsilon \mathbf{zz}, \quad \epsilon(\omega, q_z) = 1 - \frac{k_0^2}{k^2 - q_z^2}, \quad (1)$$

where *z*-axis is oriented along wires,  $k = \omega/c$  is wave number of the host medium,  $k_0 = \omega_0/c$  is wave number corresponding

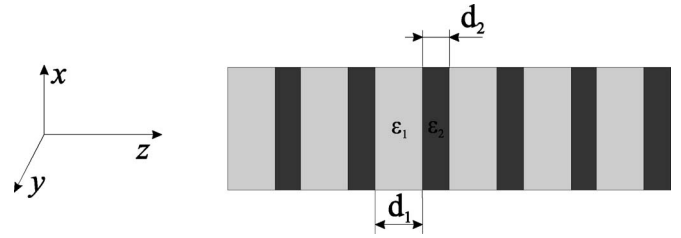


FIG. 1. Geometry of layered metal-dielectric metamaterial.

to the plasma frequency  $\omega_0$  which depends on the lattice period and radius of wires,  $q_z$  is *z*-component of wave vector  $\mathbf{q}$ ,  $c$  is the speed of light. For the transmission line mode  $q_z = k$  and effective permittivity  $\epsilon$  becomes infinite. Thus, transmission line modes effectively propagate in the medium with permittivity tensor of the form

$$\bar{\bar{\epsilon}} = \mathbf{xx} + \mathbf{yy} + \infty \mathbf{zz}. \quad (2)$$

In order to achieve in optical range the same properties as the wire medium has at microwave frequencies it is required to find some uniaxial optical material which has permittivity of the form (2). Usually, it is assumed that in optical range it is impossible to get very high values of permittivity. It is true for natural materials, but for metamaterials, especially uniaxial, it is not so. The high permittivity can be achieved in layered metal-dielectric structures.<sup>34</sup> Let us consider a layered structure presented in Fig. 1.

Such a metamaterial can be described using permittivity tensor of the form:

$$\bar{\bar{\epsilon}} = \epsilon_{\parallel}(\mathbf{xx} + \mathbf{yy}) + \epsilon_{\perp} \mathbf{zz}, \quad (3)$$

where

$$\epsilon_{\parallel} = \frac{\epsilon_1 d_1 + \epsilon_2 d_2}{d_1 + d_2}, \quad \epsilon_{\perp} = \left[ \frac{\epsilon_1^{-1} d_1 + \epsilon_2^{-1} d_2}{d_1 + d_2} \right]^{-1}.$$

In order to get  $\epsilon_{\parallel} = 1$  and  $\epsilon_{\perp} = \infty$ , and obtain a material with permittivity tensor of the form (2), required for implementation of the canalization regime, it is necessary to choose parameters of the layered material so that  $\epsilon_1/\epsilon_2 = -d_1/d_2$  and  $\epsilon_1 + \epsilon_2 = 1$ . From the first equation it is clear that one of the layers should have negative permittivity and thus, the structure has to be formed by one dielectric layer and one metallic layer. For example, one can choose  $\epsilon_1 = 2$ ,  $\epsilon_2 = -1$ , and  $d_1/d_2 = 2$ , or  $\epsilon_1 = 15$ ,  $\epsilon_2 = -14$ , and  $d_1/d_2 = 15/14$ .

Note, that no layered structure required for canalization regime can be formed using equally thick layers  $d_1 = d_2$ . The layered metal-dielectric structures considered in Refs. 9–11 have completely different properties as compared to the structures considered in the present paper. As it is noted in Ref. 11, the structures with  $d_1 = d_2$  and  $\epsilon_1 = -\epsilon_2$  (as in Refs. 9–11) correspond to  $\epsilon_{\perp} = 0$  and  $\epsilon_{\parallel} = \infty$ , and operate as an array of wires embedded into the medium with zero permittivity. Such a structure can be considered as unmatched uniaxial analogue of so-called material with zero-index of refraction.<sup>35</sup> The absence of matching ( $\mu = 1$ , but not 0, as it is required) causes strong reflections and restricts slab thickness to be thin. In contrast to this case, in the canalization regime the reflections from the slab are absent due to the

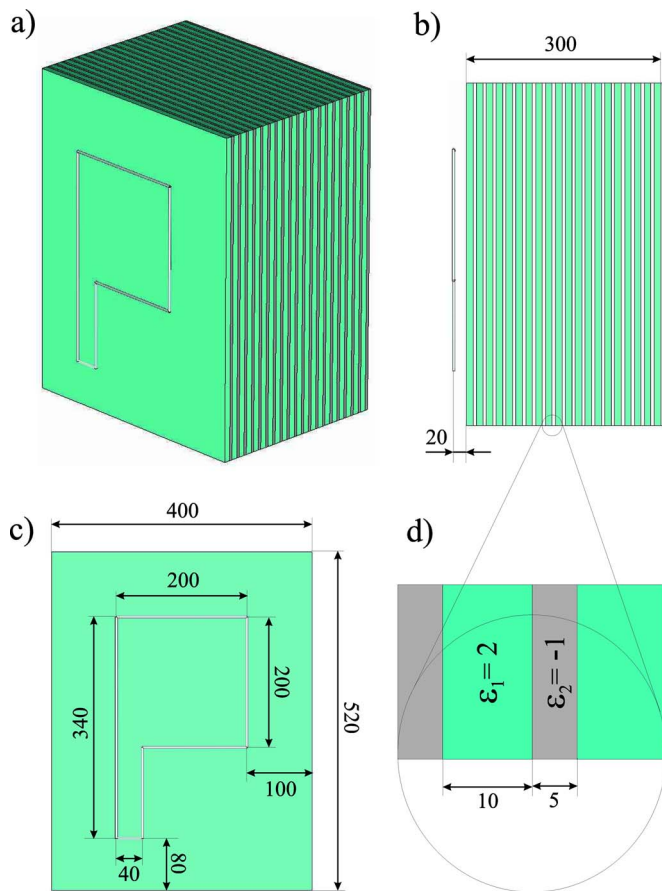


FIG. 2. (Color online) Geometry of transmission device formed by a layered metal-dielectric metamaterial: (a) Perspective view, (b) side view, (c) front view, (d) small details. All dimensions are in nm.

Fabry-Perot condition which holds for all angles of incidence.

In order to demonstrate how canalization regime can be implemented using the suggested metal-dielectric layered structure, we present results of numerical simulation using CST Microwave Studio package. A subwavelength source (a loop of the current in the form of P-letter) is placed at 20 nm distance from a 300 nm thick multi-layer slab composed of 10 and 5 nm thick layers with  $\epsilon_1=2$  and  $\epsilon_2=-1$ , respectively. The detailed geometry of the structure is presented in Fig. 2. The wavelength of operation  $\lambda$  is 600 nm. The field distributions in the planes parallel to the interface of the structure plotted in Fig. 3 clearly demonstrate imaging with 30 nm resolution ( $\lambda/20$ ). Figures 3(a) and 3(b) show the field produced by the source in free space at 20 nm distance. It is practically identical to the field observed at the front interface of the structure, Figs. 3(c) and 3(d). It confirms that the reflections from the front interface are negligibly small. Actually, the main contribution into reflected field comes from diffraction at corners and wedges of the device. Figures 3(e) and 3(f) show the field at the back interface of the structure. The image is clearly visible, but it is a little bit distorted by plasmon-polariton modes excited at the back interface. Being diffracted into the free space this distribution forms an image without distortions produced by plasmon-polariton modes,

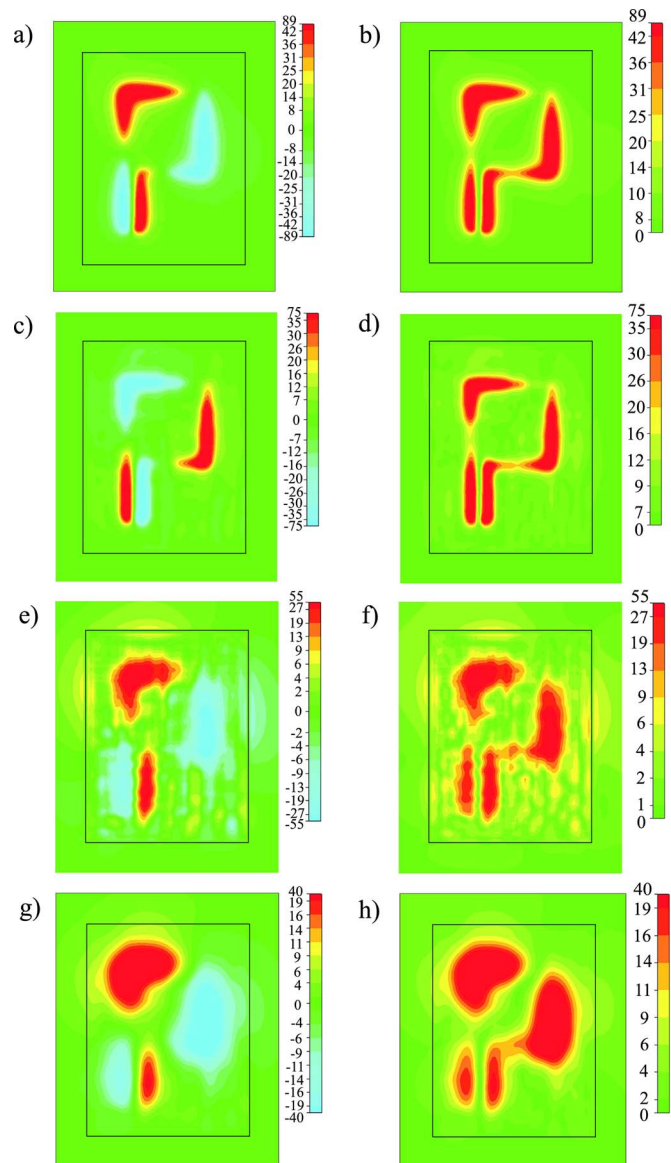


FIG. 3. (Color online) Distributions of normal to the interface component of electrical field (arbitrary units): (a) In free space, 20 nm from source, (c) at the front interface, (e) at the back interface, (g) in free space, 20 nm from back interface; and their absolute values, (b), (d), (f), (h), respectively.

see Figs. 3(g) and 3(h) presenting field distribution at 20 nm distance from the back interface.

The resolution of the proposed layered structure is restricted by its period  $d=d_1+d_2$ . The model of uniaxial dielectric (3) is valid only for restricted range of wave-vector components. In order to illustrate this we calculated isofrequency contour for the layered structure under consideration treating it as 1D photonic crystal and using an analytical dispersion equation available in Ref. 36. The result is presented in Fig. 4. While  $|q_x d/\pi| < 0.5$  the isofrequency contour is flat, the homogenized model (3) is valid and the structure operates in the canalization regime. The spatial harmonics which have  $|q_x d/\pi| > 0.5$  will be lost by the device and this defines  $d/0.5 \approx \lambda/20$  resolution. The calculation of isofrequency contour for the case of  $\epsilon_1=15$ ,  $\epsilon_2=-14$ ,  $d_1=7.76$  nm, and  $d_2=7.24$  nm for the same wavelength of 600 nm revealed its

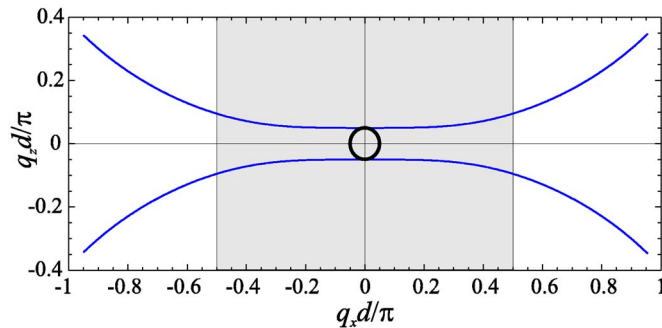


FIG. 4. (Color online) Isofrequency contour of layered metal-dielectric structure with  $\epsilon_1=2$ ,  $\epsilon_2=-1$ ,  $d_1=10$  nm,  $d_2=5$  nm,  $d=d_1+d_2=15$  nm for  $\lambda=600$  nm. The region where the dispersion curve is flat ( $|q_x d / \pi| < 0.5$ ) is shadowed. The circle in the center represents isofrequency contour of the free space.

flatness for  $|q_x d / \pi| > 1.5$ . This allows us to predict  $d/1.5 \approx \lambda/60$  resolution for this case. Note, that the similar restrictions on resolution by the periodicity are applicable for the layered structures considered in Refs. 10 and 11 in spite of the authors' claims that resolution of such structures is mainly limited by losses. The general study of limitations on homogenization of periodic layered structures will be published elsewhere.

In conclusion, we have demonstrated possibility of the imaging with subwavelength resolution using a layered metal-dielectric structure. The structure operates in canalization regime as a transmission device and does not involve negative refraction and amplification of evanescent modes. The simulation was done for 300 nm thick structure comprising of 10 nm dielectric layers with  $\epsilon=2$  and 5 nm metal layers with  $\epsilon=-1$  at wavelength of 600 nm and resolution of  $\lambda/20=30$  nm was shown. The metal with  $\epsilon=-1$  at 600 nm wavelength can be created by doping some lossless dielectric by small concentration of silver which has  $\epsilon=-15$  at such frequencies, in the similar manner to the ideas of works Refs. 37 and 38. Even more promising resolution of  $\lambda/60=10$  nm was predicted for the layered structure comprising of 7.76 nm layers of dielectric with  $\epsilon=15$  and 7.24 nm layers of metal with  $\epsilon=-14$ . The last structure can be constructed using silicon as dielectric and silver as metal, but very accurate fabrication with error no more than 0.05 nm will be required in order to get proper result. The losses in silver in both cases are already reduced by operating at rather long wavelength of 600 nm, but in accordance with our estimations they are still high enough to destroy quality of the subwavelength resolution. This problem can be solved by using of active materials, for example, doped silicon.<sup>11,37</sup>

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