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Super-Efficient Cross-Correlation (SEC-C): a fast matched filtering code suitable for desktop computers

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Abstract

We present a new method to accelerate the process of matched filtering (template matching) of seismic waveforms by efficient calculation of (cross-) correlation coefficients. The cross-correlation method is commonly used for analyzing seismic data, e.g. to detect repeating or similar seismic waveform signals, earthquake swarms, foreshocks, aftershocks, low-frequency earthquakes and non-volcanic tremor. Recent growth in the density and coverage of seismic instrumentation demands fast and accurate methods to analyze the corresponding large volumes of data generated. Historically there are two approaches used to perform matched filtering; one using the time domain and the other the frequency domain. Recent studies reveal that time domain matched filtering is memory efficient and frequency domain matched filtering is time efficient, assuming the same amount of computational resources.

We show that our Super Efficient Cross-Correlation (SEC-C) method – a frequency domain method that optimizes computations using the overlap-add method, vectorization and fast normalization – is not only more time efficient than existing frequency domain methods when run on the same number of CPU threads, but is also more memory efficient than time domain methods. For example, using 30 channels of data with a sample rate of 50 Hz and 30 templates, each with durations of 8 seconds, SEC-C uses only 2.3 GB of memory while other frequency domain codes use three times more and parallelized time domain codes use ~30% more. We have implemented a precise, fully-normalized version of SEC-C that removes the mean of the data in each sliding window, and thus does not require any preprocessing of the seismic data. Another strength of the SEC-C method is that it can be used to search for repeating seismic events in a concatenated stack of individual event waveforms. In this use case our method is more than one order of magnitude faster than conventional methods. The SEC-C method does not require specialized hardware to achieve its computation speed; instead it exploits algorithmic ideas that are both time- and memory-efficient and are thus suitable for use on off-the-shelf desktop machines.

Introduction

Matched filtering, also known as template matching, similarity search, or “query-by-content”, is a commonly used method in seismology. The matched portions of a continuous data with a template can be identified by calculating normalized correlation coefficients, usually referred to by seismologists as zero-lag cross-correlation coefficients (CCCs). By choosing appropriate thresholds for these CCC values, we can detect similar or repeating patterns in those continuous

data. Template matching is often used for detecting seismic events with low signal-to-noise waveforms within large volumes of continuous data. A high detection capability along with applicability to a wide variety of seismic source types makes template matching a powerful tool for seismologists. For example, template matching can be used to detect seismic events such as foreshocks, aftershocks, icequakes, repeating earthquakes (REs), volcanic earthquakes, geothermal seismic activity, swarms, low frequency earthquakes (LFEs) and non-volcanic tremor, to monitor nuclear explosions, and to identify seismic triggering (e.g. Nadeau et al., 1995; Gibbons and Ringdal, 2006; Shelly et al., 2007; Peng and Zhao, 2009; Meng and Peng, 2014; Allstadt and Malone, 2014; Skoumal et al., 2015; Kato et al., 2016; Frank et al., 2017).

Beside the event detection applications explained above, cross-correlation analysis has become an important part of determining event locations and relocations in the last two decades (e.g. Waldhauser and Ellsworth; 2000; Schaff and Waldhauser, 2005; Hauksson and Shearer, 2005). The relative arrival time of seismic phases to seismic stations for each event in a group of nearby events is the main input information for relocation algorithms (e.g. Waldhauser and Ellsworth; 2000, Hauksson and Shearer, 2005) and traditionally is estimated by comparing the picked phase arrival times from earthquake catalogs. The picked phase arrival times usually contain errors due to station noise and uncertainty in the phase picking algorithm or human error. On the other hand, CCC methods can precisely calculate the relative time shift between individual waveforms as the CCC between them is maximized when two waveforms are aligned. These methods can also be used to precisely detect temporal velocity changes in the Earth's crust (e.g. Poupinet et al., 1984; Schaff and Beroza, 2004; Thomas et al., 2012) or even the Earth's inner core (Tkalčić et al., 2013). Precise information about relative phase arrival times also plays an important role

in seismic tomography (e.g. Zhang and Thurber, 2003). A fast method for performing template matching in continuous data and for pairwise cross-correlations of individual waveforms could potentially lead to computation time improvements in many branches of seismology, therefore.

For most earthquake detection and (re)location applications (e.g. aftershocks, foreshocks, swarms, event relocations), choosing a waveform template can be straightforward, e.g. selecting a well-recorded event within an area of interest (e.g. Shelly et al., 2007; Schaff and Waldhauser, 2010; Meng and Peng, 2014). However, in cases where it is known that a specific type of event repeats over time (e.g. REs or LFEs), but cannot be identified a priori, seismologists have used different techniques such as array processing (e.g. Frank et al, 2014), pairwise similarity search (also known as “autocorrelation”; e.g. Brown et al., 2008), or careful visualization of seismic data (e.g. Shelly et al, 2009) to identify templates.

The duration of continuous data available for investigation by template matching is of the order of decades (e.g. Shelly et al., 2017). If, for example, we could reduce the run time of a template matching analysis from 300 seconds to 100 seconds for each day of seismic data, this would add up to ~8 days of computation time savings for one decade of seismic data. In other words, given the power law increase in the volume of waveform data archived in seismic data repositories (e.g. IRIS DMC; Hutko, et al., 2017), there is a high demand for fast, precise, and user-friendly seismic analysis methods.

For a single waveform of continuous seismic data with n samples and a single template with a length of m samples, the time complexity of template matching in the time domain is $O((n-m)m)$,

or approximately $O(nm)$ when $n \gg m$. In the frequency domain, the time complexity is $O(n \log n)$ (Lewis, 1995). The normalization of computed CCCs adds an additional delay to the computational run time. The relative computational time complexity between these two methods then can be determined by comparing the size of $\log(n)$ with m .

In this paper, whenever we talk about time complexity comparisons between the time- and frequency-domain methods, we assume that these two methods are written in a common programming language and use the same computational resources (e.g. a single thread of a CPU). For seismological applications, a template waveform usually contains several seconds of seismic data (i.e. $m \approx 10\text{--}1000$ samples) and the data set to be compared to is typically weeks, months or years of seismic data that are usually stored as daily continuous seismic data files (i.e. $n \approx 10^6\text{--}10^7$ samples per day). This implies that the frequency domain method should be the faster method unless a template with a short length (e.g. less than a second, for one day of data with 50 Hz sample rate) is used. On the other hand, frequency domain methods, which typically involve the template being padded with zeros at least to the length of the comparison data, require much more memory (e.g. Lewis, 1995; Chamberlain et al, 2018). Despite not being time efficient with respect to frequency domain methods, time domain template matching is often considered suitable for CPU and graphics processing unit (GPU) parallelization as the implementation is straightforward and it is memory efficient (e.g. Meng et al., 2012; Beauce et al., 2018; Mu et al, 2017). Here we demonstrate, using several algorithmic improvements, a single CPU frequency domain method that we call Super Efficient Cross-Correlation (SEC-C) that is equivalent in speed to modern CPU-parallelized codes running on more than 10 processor cores, and only a few times slower than GPU parallelized codes. Such a code, running on a

regular desktop computer with a few processor cores, can be a powerful tool for template matching that in some cases (e.g. long duration of templates, 100 Hz sample rates) is as powerful as GPU parallelized codes without requiring extensive memory or additional hardware.

SEC-C is fast, memory efficient, and, for a minimal increase in computation time, can be precise to machine precision. A ‘fully-normalized’ version of the algorithm removes the mean of the data for each sliding window internally and therefore can be used for template matching of raw seismic data (Figure S1). Several of the parallelized methods mentioned above require prior operations on the data, or specific conditions or assumptions (e.g. removing the mean from the data, low variability on the amplitude or using single-precision floating points; Beauce et al., 2018; Chamberlain et al., 2018; Mu et al., 2017; respectively). Chamberlain et al., (2018) reported that using single-precision floating points for normalization calculations can introduce errors in the CCC results of up to 20 percent for a large earthquake within low-amplitude noise. Beauce et al. (2018) tested the removal of the mean from the data from a M 7.8 earthquake and showed that the CCC error is 1.2 percent. SEC-C is capable of outputting both the CCC sum as well as the individual CCC for each channel without introducing extra runtime. The latter case is useful when the moveout of P-wave arrivals is not precisely known and/or the stations are far from each other (i.e. the moveout is very large), so that matched filtering at individual stations is a better option.

Our aim in this study is to calculate fast, memory efficient and precise CCCs for template matching applications in seismology. SEC-C employs a combination of several speed-up techniques such as the Fast Fourier Transform (FFT), the overlap-add method (Rabiner and

Gold, 1975), vectorization tricks and a fast normalization method inspired by Mueen's Algorithm for Similarity Search (MASS; Mueen et al, 2015). This method can be coded in any array programming computer language (e.g. MATLAB, Fortran 90, R, the NumPy extension to Python). It does not require any special libraries except for the FFT. The SEC-C Matlab code is provided in the supplementary materials that accompany this article. The MATLAB code along with a Python version also are available in a GitHub repository (https://github.com/Naderss/SEC_C).

The algorithm

The traditional time domain sliding window cross-correlation method

Assume that we have a seismic template waveform X with a length of m samples and a continuous time series Y with a length of n samples. A traditional brute force way of performing template matching is to calculate the CCC of X with a sub-window of Y that has the same length (i.e. of m samples) and repeat this procedure with a sliding sub-window shifted by one sample or some small interval (e.g. 0.02 sec; Shelly et al., 2009). Assume that Y^i is the i th sub window of Y , then the CCC for any sub-window is defined as below:

$$CCC_i = \frac{(x-\bar{x}).(Y^i-\bar{Y}^i)}{\sqrt{((x-\bar{x}).(x-\bar{x})).((Y^i-\bar{Y}^i).(Y^i-\bar{Y}^i))}} \quad (1)$$

Here, the bar symbol above X and Y^i refers to the mean values for each. For example, \bar{X} is referring to a vector with a length of m in which each component is the mean of X . If we assume that the local mean is already removed from the data and templates this can be reduced to the equation below:

$$CCC_i = \frac{\bar{X} \cdot Y^i}{\sqrt{(\bar{X} \cdot \bar{X})(Y^i \cdot Y^i)}} \quad (2)$$

This procedure typically requires looping of this calculation over many sub-windows of Y . For most real seismological applications, this needs to be repeated for multiple stations with multiple components and several templates. This becomes time consuming for a long continuous waveform and with the sample rates required for most seismic applications (e.g. usually greater than 20 Hz). For example, calculating CCCs for one day of continuous waveform with a 100 Hz sample rate and sliding for a 0.02 sec interval for 10 stations, 3 components and for 20 templates, requires the evaluation of equation (1) 24 (hours) \times 60 (minutes) \times 60 (seconds) \times 50 (CC evaluations per second) \times 10 (stations) \times 3 (components) \times 20 (templates) = $\sim 2.6 \times 10^9$ times.

For one year of data, the number of calculations increases to $\sim 10^{12}$. The time complexity of (1) has a linear relationship with template length (m) and as m increases the total computational time increases proportionately. In order to tackle the runtime problem of computing many nested loops, recent time domain-based methods have focused on parallelization either using CPU clusters or GPU architecture that can compute this calculation using hundreds to thousands of threads simultaneously (e.g. Meng et al, 2012, Beauce, et al, 2018; Mu et al, 2017). However,

performing a real-world case of template matching using a regular desktop machine in the time domain is yet a challenge and out of reach.

The alternative way of performing template matching is to use the frequency domain to calculate the numerator of eq (2) without looping over sliding windows. Here we briefly give an introduction to frequency domain template matching, using the CCC metric.

The traditional frequency domain cross-correlation method

We first define two vectors with the same length, extended to the next highest power of two:

- i) X' = reverse X and append $(n+l - m)$ zeros to the end
- ii) Y' = append Y with l zeros at the end

Here l is the number of zeros that needs to be added to the Y to make the length of Y a power of two. In the past the FFT algorithm performed optimally when the length of the data was a power of two. New FFT libraries however can calculate the FFT efficiently if the prime factors are small (e.g. FFTW; Frigo and Johnson, 2005). Therefore, depending on the FFT libraries and n , l can be chosen to be 0 or any number that can make $n+l$ a power of two. Then the convolution of X' and Y' would produce all the possible numerators of (1) (Lewis, 1995):

$$(X' * Y')_i = X \cdot Y^i \quad (2)$$

As mentioned above, subscript i here is referred to the i th sub window. We call this vector the sliding dot product of X and Y , $sdp(X, Y)$. We can calculate this sliding dot product using the fast Fourier transform (FFT) method as below (Lewis, 1995; Smith, 1997):

$$\text{iii) } sdp(XY) := (X' * Y') = FFT^{-1}(FFT(X') \cdot FFT(Y'))$$

The three procedures above allow us to calculate the numerator of (1).

Algorithms for calculating the denominator of eq (2) (i.e. the normalization part) may vary from method to method. As the time complexity of the FFT is $O(n \log n)$, if we assume a normalization with a linear time complexity, then the overall time complexity of the frequency domain method is $O(n \log n)$. If we compare this to the time domain time complexity (i.e. $O(nm)$), when m is greater than $\log n$, the frequency domain approach becomes a better choice of method. For a single day of seismic data, depending on the sample rate (e.g. from 20 to 100 Hz), $\log n$ varies between ~ 14 and 16 . This means that the frequency domain approach is more efficient if $m > 16$ – corresponding to a template length of 0.32 seconds when a sample rate of 50 Hz is assumed. The exact template length, m , at which the frequency domain becomes more time efficient depends on the hardware and the FFT libraries (Smith, 1997). For most seismic applications, however, template lengths of more than several seconds of data are required, implying that methods that make use of the frequency domain are more time efficient. (Note as we mentioned above our assumption is that both methods use the same amount of CPU resources, e.g. one CPU thread.)

On the other hand, frequency domain methods are not typically memory efficient. During the procedure (i), the template length increases at least to the length of the data (i.e. n if l is assumed to be zero). Our tests (see ‘Memory Efficiency’, below) show that these types of frequency domain methods (e.g. EQcorrscan; Chamberlain et al., 2018) can almost exceed the memory of a desktop computer with 16 GB of RAM in some use cases (e.g. using 40 templates for 10 stations with 3 components with a sample rate of 50 Hz and template length of 8 seconds). Even if a test case includes a small number of channels of data (not 30 channels as above), having a memory efficient method allows the user to perform matching for more templates at the same time and therefore at a reduced run-time overall. The frequency method memory limitations can be circumvented using algorithmic improvements, however – below, we describe how our ‘Super Efficient’ algorithm is efficient both in terms of computation time and memory.

The Super Efficient Cross-Correlation (SEC-C) algorithm

Here we use several methodological ‘tricks’ to reduce both the run time and memory usage when calculating CCCs for the multi-station and multi-template case of matched filtering of seismic data using a frequency domain-based method. First, in order to reduce the run time and memory overhead required, we use a “block convolution” procedure (also called “sectioned convolution”; e.g. Rabiner and Gold, 1975) using the “overlap-add” method (e.g. Rabiner and Gold, 1975) to calculate the sliding dot product using the FFT method (i.e. iii). This method is used in signal processing techniques to perform the convolution of a long signal with a finite impulse response filter (e.g. Rabiner and Gold, 1975; Smith, 1997). The main idea is to divide a long signal into small pieces and then perform the FFT convolution for each piece. In order to ensure accurate

calculation of the sliding dot product at the border of two neighboring pieces there should be an overlap of $m-1$ samples between neighboring pieces. If we assume that the length of each piece is k and if we ignore the recomputation in areas of overlap, the time complexity for a single trace of the data then becomes $O((n/k)(k \log k)) = O(n \log k)$ as we need to compute (iii) for n/k pieces. Here k becomes a tunable parameter that should be carefully chosen for optimal performance. If $k \ll n$ (e.g. comparable in size with m), performing many repetitions (loops) will slow down the process. If k is large and comparable in size with n then calculating the FFT for each piece will be time consuming. The optimal value for k can be determined by trial and error, and mainly depends on hardware aspects (e.g. CPU cache size and clock speed). Using a trial and error procedure that we performed using two different desktop machines, we recommend assigning a power of two for k (e.g. 2^{12} for one day of 20 Hz data or 2^{13} for one day of 50–100 Hz data) for efficient performance. However, in all cases we advise running some test cases to find values of k to optimize the run time.

One other feature of the overlap-add method is that the template is not required to be padded by zero to the length of the data, which for large n can require hundreds of MB of memory space. Using the shorter waveform pieces of the overlap-add method reduces this requirement to padding until the length of k (equivalent to tens of KB of memory usage if $k = 2^{13}$). This can result in a large memory savings when multiple stations and templates are used. The k value can also be chosen to be very small in order to minimize memory usage, although this will come at the expense of increased run times.

The second ‘trick’ to speed up the template matching is to use vectorized calculations of sliding dot product for all overlap-add pieces instead of looping over these pieces. For example, MATLAB has options for vectorized FFT, dot product and inverse FFT and therefore the whole procedure of (iii) can be vectorized. For the case of multi-template matched filtering, the FFTs of the templates can also be calculated in a vectorized basis as well.

A third optimization ‘trick’ is that we apply a very efficient normalization (i.e. denominator of eq (1)) inspired by the MASS algorithm (Mueen et al, 2015), that we describe below. Note that X is a constant and can be precalculated. For calculating $Y^i \cdot Y^i$ we use the following procedures:

i) Calculate the cumulative sum of Y squared and prepend a zero to it as below:

$$C_{k+1} = \begin{cases} \sum_{j=1}^k Y_j Y_j, & (1 \leq k \leq n) \\ 0, & (k = 0) \end{cases}$$

ii) Then, $Y^i \cdot Y^i$ can be calculated as below:

$$Y^i \cdot Y^i = C_{i+m} - C_i.$$

These will give us the denominator of eq (2) with the time complexity of $O(n)$. Note that recent versions of MATLAB (2017a and later) include a built-in function, *movsum*, that performs this procedure with a similar time complexity and runtime. *movsum* returns the sliding m -points sums of a vector. We use this function for simplicity in the current version of SEC-C. For other

programming languages and older versions of MATLAB the procedure explained above can be used.

The output of the algorithm we describe above is the sliding CCC for the template X and a the continuous waveform Y with the time complexity of $O(n \log k)$. We then loop over the stations, components and templates in order to calculate the various CCCs required in the multi-channel and multi-template cases. Along with these required loops, some of the operations, such as zero padding, reversing and calculating FFTs of templates, are performed in a vectorized basis. SEC-C can output either the CCC for each channel individually for each template or produce weighted CCC sums of all channels. For the second option, weightings should be provided by the user. For more details of the algorithm we refer to the MATLAB code provided in supplementary materials.

SEC-C is a single CPU code that is optimized for seismic data sets with lengths of ~one day that can handle hundreds of channels of data and templates in an efficient run time. If faster run times are needed, the user can simply parallelize the problem by running SEC-C in parallel for different day of data on each single CPU core of a multi-core desktop machine. A toy example of running SEC-C using the MATLAB parallelized for-loop, *parfor*, is provided in the SEC-C GitHub repository (https://github.com/Naderss/SEC_C).

The full-normalized version of the Super Efficient Cross-Correlation (SEC-C) algorithm

The algorithm explained above is based on eq (2) that includes the assumption that the local mean is removed from the data and templates. This can be acceptable for most cases of seismological applications, but in some cases, e.g. where there are sudden large fluctuations in the data, such as instrument spikes or nearby large earthquakes, can be problematic. Most current approaches based on the assumption that the mean and any spikes are removed from data (e.g. Beauce et al., 2018; Chamberlain et al., 2018). Beauce et al, (2018) indicate that this assumption can affect the results of CCC calculations for the M_w 7.8, 2016 Kaikoura earthquake by as much as 1.2%; however, this is an extreme cases where there are large deviations from the mean in the data. Our experiment on Mt St Helens seismicity (i.e. a more ‘normal’ test case) shows the differences between CCCs calculated by eq (1), and the SEC-C method with the zero-mean assumption (eq 2), for single channel of data are of the order of 10^{-4} (Figure 1e).

As SEC-C is a versatile algorithm we can make some simple changes that calculate CCCs based on eq (1) without the need for simplifying assumptions. Here we briefly discuss this implementation.

First, the mean of the templates can be precalculated and removed. Equation (1) in this case becomes:

$$CCC_i = \frac{x.(Y^i - \bar{Y}^i)}{\sqrt{(x.x)((Y^i - \bar{Y}^i).(Y^i - \bar{Y}^i))}} = \frac{(x.Y^i) - (x.\bar{Y}^i)}{\sqrt{(x.x)(Y^i.Y^i - (2Y^i.\bar{Y}^i - \bar{Y}^i.\bar{Y}^i))}} \quad (3)$$

There are two extra terms in this equation with respect to eq (2), $X \cdot \bar{Y}^i$ in the numerator and $(2Y^i \cdot \bar{Y}^i - \bar{Y}^i \cdot \bar{Y}^i)$ in the denominator. Before calculating these two terms, we define S^i as a local sum of Y :

$$S^i = \sum_{j=i}^{i+m} Y_j \quad (4)$$

The term $X \cdot \bar{Y}^i$ vanishes as the mean of X is removed. In other words:

$$X \cdot \bar{Y}^i = \text{mean}(Y^i)(\text{sum}(X)) = ((S^i)/m) (\text{sum}(X)) = ((S^i)) (\text{sum}(X)/m) = (S^i)(\text{mean}(X)) = 0$$

And the extra term in the denominator of eq (3) can be calculated as below:

$$2Y^i \cdot \bar{Y}^i - \bar{Y}^i \cdot \bar{Y}^i = 2(S^i) (S^i / m) - m(S^i/m) (S^i / m) = (S^i)^2/m$$

Note that the mean of Y^i is simply S^i / m . S^i can be calculated with a similar algorithm as that described above for $Y^i \cdot Y^i$, or by using the *movsum* function in MATLAB, with a linear time complexity.

By applying these implementations, the runtime of SEC-C only increased by less than 1.1% of that of the regular SEC-C algorithm and in our heaviest test case the run time is almost the same (Figure 2). This is because the cost of computing the mean of the data is only borne once; once the mean is computed, as many templates as desired can be run at no additional cost. As this

‘fully-normalized’ version of SEC-C removes the sliding mean from the data, it can be used for raw data (e.g. Figure S1).

Comparisons with other approaches

We compare here SEC-C with other contemporary methods in terms of accuracy, speed and memory efficiency, the main characteristics of any matched filter method. For the accuracy test we compare SEC-C with *xcorr*, a built-in MATLAB function for calculating CCCs. In order to test SEC-C in term of speed and memory usage we compare it with two current, recently-published methods; EQcorrscan (Chamberlain et al., 2018), a frequency domain-based matched filter method and Fast Matched Filter (FMF; Beauce et al., 2018), a time domain-based method.

SEC-C accuracy and precision, and the impact of the zero-mean assumption

To test the accuracy and precision of this method, we applied the SEC-C algorithm to the seismicity at Mt St Helens volcano. We select a template waveform from repeating volcanic earthquake swarms that occurred on December 3, 2005, recorded in the vertical channel of the seismic station YEL (Figure 1a). The high seismicity rates on this day are related to the dome-building eruption in 2004–2005 at Mt St Helens. So-called “drumbeat” earthquakes, repeating events that occur at regular, short intervals, occurred every 30-300 seconds during this eruptive episode (Iverson et al., 2006; Figure 1b). We calculate the CCC between our template and a 24 hour-long continuous waveform (the whole of December 3) using both SEC-C and a sliding

xcorr function over each window calculated with zero lag (Figure 1c, d). We removed the sliding mean of the data for each sliding window prior to calling *xcorr* for that window. This is a ‘brute force’ and therefore very slow method, but it is effective as a reference method for calculating CCCs precisely and accurately. A comparison between the CCC values output by this precise, traditional method and the SEC-C method on this identical dataset show that the differences of the results are on the order of 10^{-4} and 10^{-15} for the regular and fully-normalized versions of SEC-C, respectively (Figure 1e), implying that the fully-normalized version of our method is precise to machine precision and can reproduce the results of traditional methods on the order of machine precision. SEC-C uses double precision for its calculations, and this, along with the option of removing the mean for each sliding window, underpins its capacity for accurate and precise CCC computations.

SEC-C speed

We compare SEC-C with two contemporary codes: one that computes CCCs in the frequency domain; EQcorrscan version 0.2.7; and one that uses the time domain; FMF (accessed June 2018); in terms of run time and memory usage. Both the EQcorrscan and FMF methods use routines compiled in C for calculating CCCs, accompanied with multithreaded routines and OpenMP (Dagum and Menon, 1998) loops for parallelization. Both packages have a wrapper for use in Python; FMF also has a wrapper in MATLAB. We use the fastest version of the correlation backend of EQcorrscan that uses the FFTW library (Frigo and Johnson, 2005) for the Fourier transform procedure. We use synthetic data for the comparison test generated by test codes accompanying both software packages. We also use the same synthetic data generated by

the FMF test code to test SEC-C. Our tests are run on a desktop machine with an Intel Core i7-4790k CPU processor that includes 4 cores (8 threads) and 16 GB of memory. Note that this is the intended platform (i.e. a ‘desktop computer’) for the current version of the SEC-C method. In contrast, EQcorrscan can take advantage of CPU clusters with large memory capacity, and FMF is designed to take advantage of GPU hardware where available. Therefore, the comparisons stated below do not reflect the capabilities of these methods for their intended cases, rather they show performance of the methods when computational/memory resources are limited.

From now on we demonstrate the matched filter test cases with a vector with six numbers indicating the number of days of seismic data, number of stations, number of components, sample rate in Hz, template length in seconds and number of templates, respectively. In this case our test case vector was (1, 10, 3, 50, 8, x). We tried different values of x, by varying the number of templates from 1 to 40. We cannot test a greater number of templates as the EQcorrscan code exceeds the available memory on our test machine with more than 40 templates.

To make a clearer comparison between the speed of SEC-C and the speeds of the other codes, we run SEC-C using three different strategies: (i) forcing MATLAB to only use one CPU thread for the computations (hereafter referred to as the ‘single thread case of SEC-C’); (ii) allowing MATLAB to use multithreading (i.e. the use of multiple CPU threads) for some built-in functions that are optimized for it (the ‘regular case of SEC-C’); and (iii) running multiple single thread instances of SEC-C independently and simultaneously in parallel (the ‘parallelized case of SEC-C’). For strategy (iii), if the number of stations is sufficiently small, one day of data can be

run per CPU thread; if not, and if memory limitations become an issue, each day of data can be divided by the number of threads, into equally-sized smaller subsets.

Fig 2 demonstrates the results for our speed test. We find that SEC-C's performance is on average ~2, 4 and 6 times faster than FMF for the three SEC-C strategies explained above, respectively. As FMF makes use of multithreading to gain computation speed, a second test on a machine with an Intel Core i5 processor (4 cores, 4 threads) was ~8 times slower than the regular case of SEC-C for the same test vector (Figure S2). Overall, assuming limited computational resources such as a desktop computer, the strength of the SEC-C algorithm with respect to FMF is when the template length is large (e.g. > 5 sec), the number of stations and components is also large (e.g. > 30 channels), and when higher sample rates (e.g. > 50 Hz) are needed. If the use case involves templates with short lengths (e.g. a few seconds) and uses data with lower sample rates (e.g. 20 Hz), then FMF becomes more effective with respect to SEC-C. Also, if the data do not involve higher frequency content, the step feature in FMF, which calculates CCCs at regular sample steps, rather than for every sample, can be used to speed up the computation. However, this comes at the expense of potentially degraded matching performance and/or lower peak CCC values, especially when the step size is bigger than the lowest period used. As mentioned above, SEC-C can be effectively parallelized by running multiple instances on different CPU threads for enhanced performance, whereas FMF makes use of all CPU resources for a single run.

Although the memory efficiency tweaks that we have made in SEC-C tradeoff with computation speed, our run test mentioned above shows that SEC-C runs approximately twice as fast with respect to EQcorrscan when both are using a single thread (Fig 2). Memory issues with

EQcorrscan did not allow us to perform our test case using the parallelized version of EQcorrscan, however our tests with fewer templates (less than 5) show that the run time of the parallelized version of EQcorrscan is slightly longer compared to the parallelized version of SEC-C (i.e. strategy (iii) mentioned above). Overall, as the number of processes increases (e.g. increasing sample rate, number of stations, number of templates), the speed of SEC-C with respect to EQcorrscan increases.

Here we give two more examples that show the relative efficiency of SEC-C with respect to other contemporary codes in terms of speed. Beauce et al. (2018) reported the run time for a matched filter with the test vector (1, 12, 3, 50, 8, 20) while running the test using 24 CPU cores for EQcorrscan and FMF with 1 sample step (i.e. on all samples). EQcorrscan finished this test in 15.8 seconds, compared with 55.5 seconds for FMF. We run the same test using SEC-C on a single CPU thread on the desktop PC mentioned above, completing it in 88 seconds. This indicates that the single thread case of SEC-C has run times on the order of EQcorrscan and FMF running on multiple threads. The run time of the regular case of SEC-C (i.e. strategy ii from above) is 49 seconds for this test. In another study, Mu et al. (2017) reported a test case vector of (1, 1, 1, 100, 2.56, 18) that finished in 2.97 seconds using the most CPU efficient and parallelized version of their matched filter code (the ‘C2 method’) running on 18 processor cores. SEC-C can complete this test case, again using one CPU thread on the same desktop machine mentioned above, in 5.45 seconds. Note that both FMF and the method of Mu et al, (2017) are GPU-optimized and their GPU implementations can run much faster than their reported runtimes for CPU clusters. However, the examples and tests above highlight the

efficiency of SEC-C when the computational resources are limited (e.g. few CPU cores and no available GPU, such as a desktop computer or laptop).

SEC-C memory efficiency

The strength of the SEC-C method compared to time domain CPU codes is the run time speed. However, compared to other frequency domain methods (e.g. EQcorrscan), its strength is its memory efficiency. Here we test the memory usage of SEC-C with respect to FMF and EQcorrscan while running a test with the case vector of (1, 10, 3, 50, 8, 30). We monitor the memory usage of these three methods using the *htop* (<http://hisham.hm/htop/>) command. We compare the peak of memory usage before and during the runs. We find that the peak memory usage of EQcorrscan was 6.9 GB, compared with 2.95 GB for FMF and only 2.31 GB for SEC-C. Note that the memory usage corresponding to the input and output data in this test case adds up to ~2GB. This show that our memory-based implementation made SEC-C even more efficient than time domain methods (e.g. in this case FMF uses ~0.64 GB more memory than SEC-C).

One more example that can demonstrate the strength of the SEC-C method with respect to the other methods is when applying a matched filter to a large array of seismic stations, e.g. with a test vector of (1, 60, 3, 50, 10, 10). Using a regular desktop or even a small cluster it is not possible to achieve this efficiently using a time domain method (e.g. FMF). In order to use a regular frequency domain method (e.g. EQcorrscan), to avoid memory problems the user must divide the data into smaller subsets with smaller n and loop over those subsets. The additional disk read/write operations when loading data subsets and saving the results could potentially be

more time consuming compared to a case where the matched filtering can be completed in one process. SEC-C can complete the example above, with the test case mentioned above in ~two minutes on our test machine. SEC-C can perform matched filtering of up to a test case of (1, 110, 3, 50, 10, 1) without a memory problem and in a similarly efficient time (i.e. less than a minute) using the same desktop machine.

Example applications of the SEC-C algorithm

SEC-C is a versatile method that can be used for speeding up detection of any similar seismic events, e.g. REs, LFEs, triggered earthquakes, swarms of nonvolcanic or volcanic earthquakes, foreshocks and aftershock sequences. Here we show two examples of these applications.

1) Detection of low frequency earthquakes: Here we present an example to show how this method can help us in the rapid detection of LFEs. We searched for LFEs in waveform data from a tremor burst that occurred on October 6, 2007 on the San Andreas Fault near Parkfield, CA (Figure 3a), in which many LFEs were detected by template matching (Shelly et al., 2009). We select an LFE template waveform for each station (Figure 3b) by stacking matrix profiles (a measure of waveform self-similarity) from 24 hours of data spanning the tremor burst from three borehole stations of the HRSN (High Resolution Seismic Network) in the Parkfield area. (For full details of this procedure and of the matrix profile method, see Zhu et al., 2016, 2018.)

We then use the SEC-C method to calculate CCC functions for 5 HRSN stations and sum these CCC functions, aligning them by accounting for the differential arrival time (i.e. moveouts) for the

template at each station (i.e. using the S wave envelope peak). We then used the threshold of 8 times of median absolute deviation (MAD, e.g. Shelly et al., 2007, 2009). Figure 3c shows the sum of CCC functions for 5 stations and the threshold. In general, the temporal pattern of detected event origin times (Figure 3d) is consistent with the results of Shelly et al., (2009; Figure 2); any differences in detail can be attributed to the different network configurations used, and the recursive matched filter process used in the earlier study.

In this example the test case vector is (1, 5, 1, 20, 5, 1) and regular case of running SEC-C can complete it in 0.21 seconds. For the 50Hz and 100 Hz cases, run time increases to 0.54 and 1.38 seconds respectively. Assuming that this computation time would scale linearly with the number of days of data searched, performing the same procedure for one year of continuous data would take between ~77 and 504 seconds depending on the sample rate. To test this hypothesis, we use the parallelized case of SEC-C on 365 days of data, with each of eight CPU threads on our test machine running a single thread instance of SEC-C on one day of data at a time, simultaneously. The run time for this case, including loading data, running SEC-C and saving the output for the 20 and 100 Hz cases took 81 and 423 secs, respectively, using our desktop test machine. This shows how this method could greatly expedite searches for repeating seismic events in continuous waveform data if suitable event templates are known.

2) Detection of repeating earthquakes from individual detected catalog events: Along with the acceleration of template matching in continuous seismic data, one main strength of the SEC-C method is it can be applied to template matching among individual waveforms from previously detected events. Here we show one example: searching for repeating earthquakes (REs) in

Central California near Parkfield. For this purpose, we compared the performance of SEC-C with that of the *xcorr* function as the latter in this case is an efficient way of calculating CCC functions (i.e. CCC as function of lag-time) for the individual event waveforms. The maximum lag (in terms of number of samples) that the CCC function needs to be calculated over depends on the errors in the seismogram phase information (e.g. P arrival pick), that are typically of the order of 1–2 seconds, multiplied by the sample rate. In this section we use a ‘brute force’ traditional method using the MATLAB cross-correlation routine *xcorr*, in which individual waveforms are compared to each other one-by-one, via two nested loops, as a comparison to the SEC-C method.

Our runtime tests show that the SEC-C method can accelerate the search for REs by up to a factor of 15.5 faster than the traditional method, depending on the number of individual candidate events we start with.

In order to make use of the SEC-C method to search for REs in a set of individual event waveforms, we must first concatenate these event waveforms together to form one continuous waveform. The SEC-C method can then be used to compute cross-correlations between this continuous waveform and a template waveform as described above. Although SEC-C is fast at computing CCCs, as we demonstrate above, many of the CCCs calculated in this case are not necessary for the detection process. The unnecessary CCC calculations result from our concatenated waveform effectively having a large number of ‘artificial waveforms’ (or ‘waveform chimeras’) composed of parts of pairs of neighboring waveforms. For example, if we have two event waveforms, A and B, and concatenate them, the SEC-C method would calculate

the CCC between the template and a waveform window containing the second half of event A and the first half of event B (Figure 4a). The resulting calculated value would be a scientifically meaningless quantity, and in the traditional method we would not compute it. A great many of the CCCs computed using SEC-C in this setup would be of this unnecessary type. Since we would not expend computing resources to compute these meaningless cross-correlations under the traditional method, preferring instead to search for a small range of plausible time shifts within the target waveform, the differential in computation time between the two methods is greatly reduced for this application compared with scanning a continuous waveform, but still, we obtain faster run times using SEC-C, as we document below.

Our experiments in searching for REs near Parkfield (Figure 3a, Figure 4a, b) show that the search for REs using the SEC-C algorithm is more than one order of magnitude faster than the traditional method. We use for this demonstration triggered event data from the Northern California Seismic Network station PGH (Figure 3a), that has historically high signal-to-noise ratios and also a long period of operation (1987-present). We retrieve event waveforms from this station, targeting events whose catalog locations are within a small area in Parkfield where the occurrence of REs is expected (e.g. Lengliné and Marsan, 2009; Nadeau, 2014). In total we perform 14399661 pairwise CCC calculations for 5366 waveforms that are bandpass filtered between 1 and 15 Hz, with 100 Hz sample rate and with 10 seconds' duration. We found 284 candidate RE families, each having more than 3 events in a family with CCCs greater than or equal to 0.95 between their pairs. The family with the largest number of repeats has 49 events in total. Figure 3b shows an example of a RE family with 18 recurrences since 1987 detected by SEC-C. The first five sequences of this family reoccurred regularly before the M_w 6.0 2004

Parkfield earthquake with a recurrence of 3.5 ± 0.3 years. The sequences triggered by the 2004 event had recurrence intervals that were shortened to hours in its immediate aftermath and eventually, following a typical Omori-Utsu law, recovered to their original recurrence intervals from before the 2004 mainshock in a period of ~ 7 years.

The new method improves the computation time for searching for REs from around one-and-a-half hours under the traditional approach to less than seven minutes using SEC-C, using our desktop test machine. To compare the run times between the two methods, we run multiple tests on each using a series of differently-sized random subsets of these waveforms. On average, we find the SEC-C method is 12.1 times faster than the traditional, looped CCC method (see figure 4a). The speed-up factor stays above ~ 11 for all the subset sizes we test. We have started to apply the SEC-C code to large scale seismic applications, such as mining a large seismic data set (i.e. including 40,000+ events, 300+ stations, 600,000+ event waveforms) to search for REs in Northern California (Shakibay Senobari and Funning, manuscript in preparation; Funning et al., 2017). Although a discussion of the results of that work is beyond the scope of this study, we found that the entire process, including data downloading and pre-processing, computation of the waveform comparisons and clustering of the results, could be completed in one week using the same desktop machine.

Conclusions

We use a combination of different algorithm improvements such as FFT convolution, the overlap-add method, vectorization and fast normalization to produce an accurate sliding cross-

correlation coefficient (CCC) algorithm with zero-lag that is inexpensive to compute for large seismic data sets. This method, which we call SEC-C, is usable for many time series applications that require efficient computation of cross-correlations, including various seismological applications such as detecting repeating earthquakes, foreshocks, aftershocks, LFEs, etc. SEC-C is a seismic cross-correlation package that can leverage a regular desktop machine and make it as a powerful tool that can handle demanding matched filter projects. The MATLAB code is available in the Supplementary Materials accompanying the article and also it is available, along with a Python version, from our GitHub repository. An example of performing template matching that includes, retrieving, preprocessing, performing template matching using SEC-C and postprocessing results is also included in the GitHub repository, for new users with low computational resources. We test this method on several different seismic data sets at a range of sample rates and compare it with other CPU-based contemporary methods. Our tests reveal that SEC-C is not only accurate to machine precision (i.e. double precision) but also it is the most efficient in terms of speed and memory usage. SEC-C can efficiently calculate the CCC sum and can also save the individual CCCs for each channel without introducing extra cost in term of speed. Despite calculating many unnecessary CCCs, searching for repeating seismic events in a set of individual event waveforms using the SEC-C method shows a speed improvement of more than one order of magnitude on average for sets of hundreds to thousands of waveforms with respect to regular pairwise CCC calculations. This will reduce the run time requires for performing pairwise cross-correlation of several thousands of events from hours to minutes using a regular desktop machine

Our development of the SEC-C method is part of an ongoing effort for speeding up seismic cross-correlation analysis. We plan to continue our time and memory optimization for SEC-C in future, e.g. through producing versions in lower-level programming languages (e.g. C++) and exploring the possibility of parallelization, both for CPUs and GPUs.

DATA AND RESOURCES

We retrieved the seismic data for stations near Mt St Helens and Parkfield from the Incorporated Research Institutions for Seismology Data Management Center (IRIS-DMC) using the IRISFETCH MATLAB software that can be downloaded from <http://ds.iris.edu/ds/nodes/dmc/software/downloads/irisFetch.m> (last accessed July 2018). We managed the seismic data (e.g. filtering, merging, visualizing, etc) data using the MATLAB Signal Processing Toolbox and Seismic Analysis Code (SAC; last accessed March 2018). Some figures were made using the Generic Mapping Tools (GMT; Wessel et al., 2013; last accessed March 2018). We used EQcorrscan version 0.2.7 (<https://eqcorrscan.readthedocs.io/en/latest/>; last accessed July 2018) and Fast Matched Filter (FMF; https://github.com/beridel/fast_matched_filter; last accessed July 2018) for our speed and memory comparison tests.

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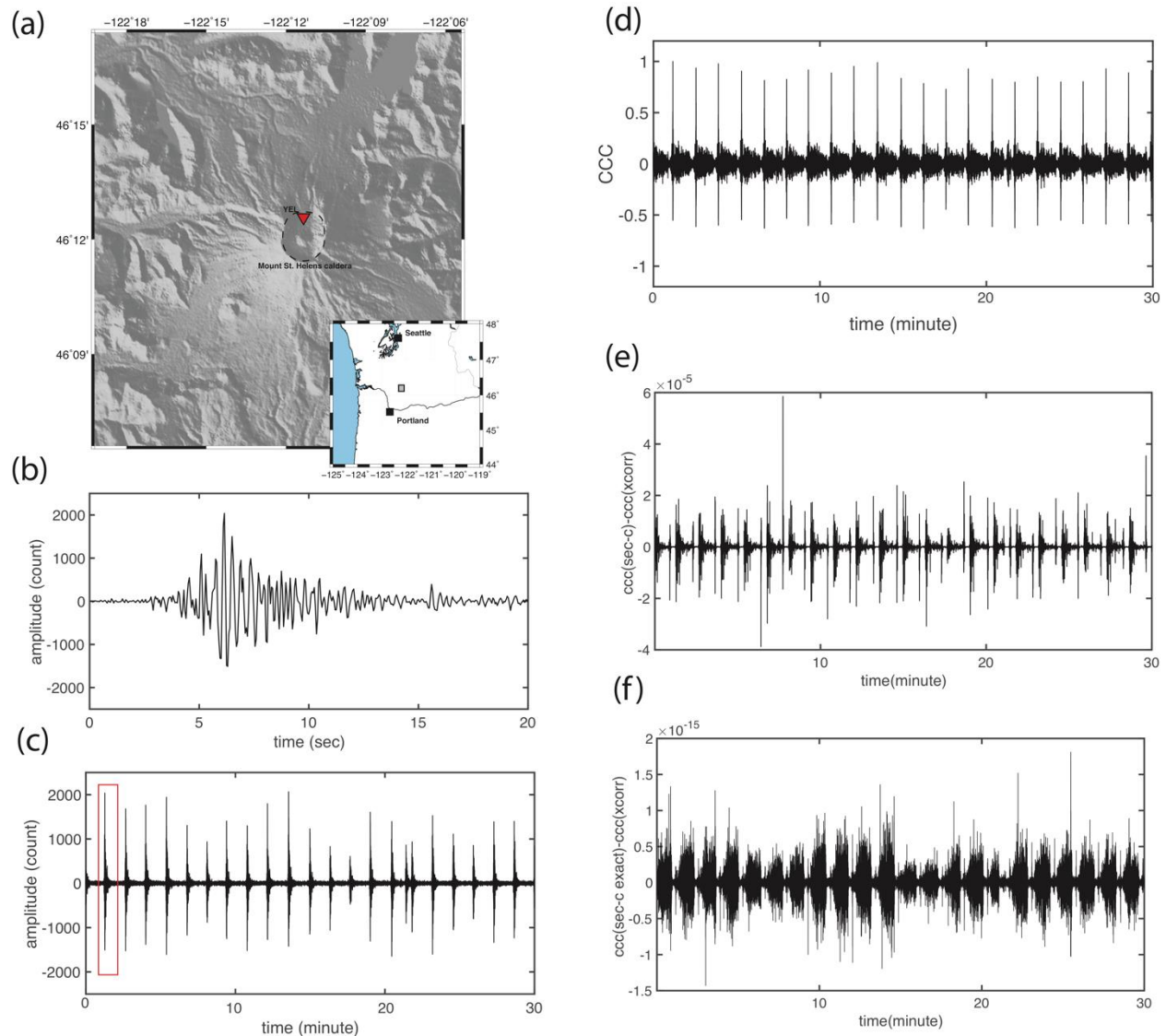


Figure 1: (a) A topographic map of the Mt St Helens volcano area. Triangle shows the location of seismic station YEL. Dashed line delimits the caldera, the source of drumbeat seismicity. (b) A “drumbeat” earthquake template waveform recorded on the vertical component channel of station YEL. (c) 30 minutes of seismic data recorded at the same station on December 3, 2004. Box indicates the template event shown in (b). (d) Cross-correlation coefficient (CCC) function calculated using the traditional sliding window method using the *xcorr* function in MATLAB (with the mean of the sliding window removed) for one day of data, note that in this and

subsequent plots we only show a 30-minute subset of this CCC function. (e) Difference of CCC calculated with the regular SEC-C method (sliding window mean not removed) with the CCC from (d). (f) same as (e) but for the full-normalized version of SEC-C where the mean is removed from each sliding window. The amplitude of (f) shows that the difference between CCC results are approximately on the order of machine precision (i.e. double precision), indicating the precision of the full-normalized version of the SEC-C method.

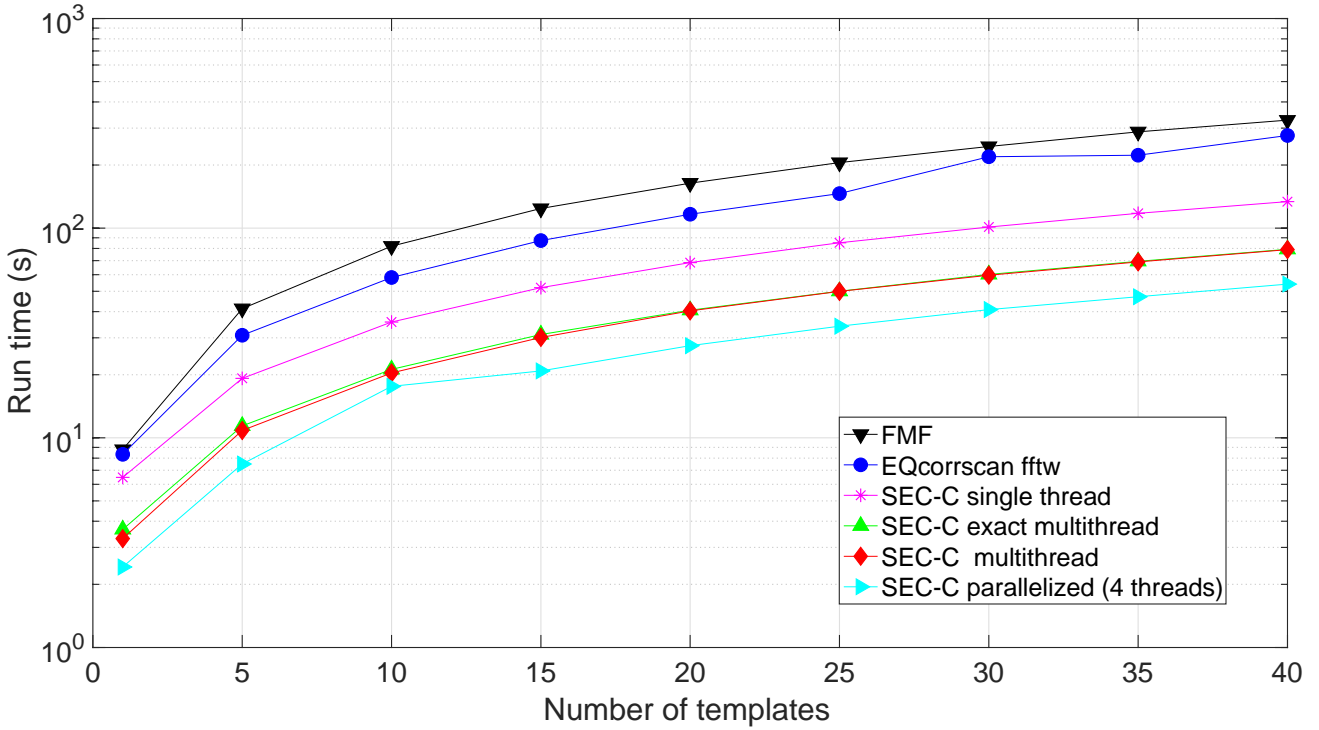


Figure 2: Matched filter run time comparison between SEC-C, the full-normalized version of SEC-C, EQcorrscan and FMF, performed on a desktop machine with a quad-core (Intel i7-4790) processor. SEC-C run time is reported for three different computation strategies: SEC-C single thread (all computations run on a single CPU thread), SEC-C multithread (a single instance of SEC-C, but with some MATLAB functions using multithreading in the background) and a parallelized case of SEC-C, where 4 single thread instances are run on a quarter of the data set each at the same time. The test case data set includes one day of data for 10 stations, each with 3 components, with a 50 Hz sample rate and a template length of 8 seconds. The run time is plotted on a log scale versus the number of templates on a linear scale. Note that we only consider the CCC sum procedure for the comparison and therefore runtime does not include the loading of data or pre-processing, such as median absolute deviation (MAD) calculation or detection. The comparison shows that SEC-C would be the best choice to run the matched filter procedure on a desktop computer as it is 2-6 times faster than other contemporary methods, depending on the

computational resources used. Note that the speed of the full-normalized version of SEC-C is almost equal to that of regular SEC-C for higher numbers of templates, indicating that in such cases, SEC-C full-normalized would be the better choice as it does not significantly increase the runtime.

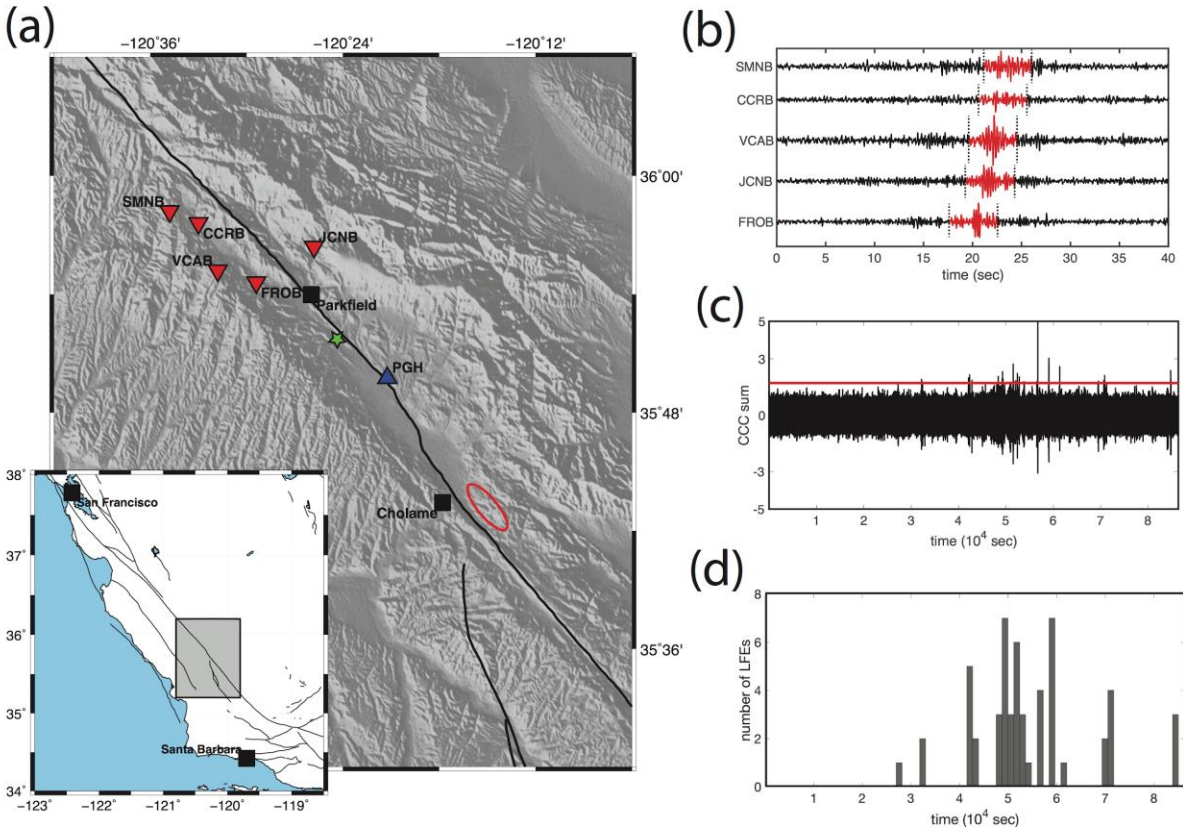


Figure 3: (a) A map of the San Andreas fault area near Parkfield, CA. Inverted triangles are the locations of Parkfield High-Resolution Seismic Network (HRSN) stations that are used in this study to search for low frequency earthquakes (LFEs), regular triangle is station PGH from the Northern California Seismic Network (NCSN) used to search for repeating earthquakes (REs), Star is the location of a family of REs (see Figure 3c), and ellipse shows the approximate locations of the LFEs detected by Shelly et al., (2009). (b) Waveforms from HRSN seismic stations showing our LFE template (indicated by dashed lines). Note that the waveforms are arranged from top to bottom based on their stations' approximate distance to the source (i.e. most to least distant, respectively). (c) Sum of the CCC functions from the 5 HRSN stations calculated using the template shown in (b) and the SEC-C method, for waveforms from October 6, 2007

(UTC). The horizontal line is the detection threshold we use, 8 times the median absolute deviation (MAD), based on Shelly et al. (2007). (d) A histogram of LFEs detected using the SEC-C method and our template. Note that although we used a different method, our results (i.e. detection times and number of detections) broadly agree with those of Shelly et al., (2009; Figure 2).

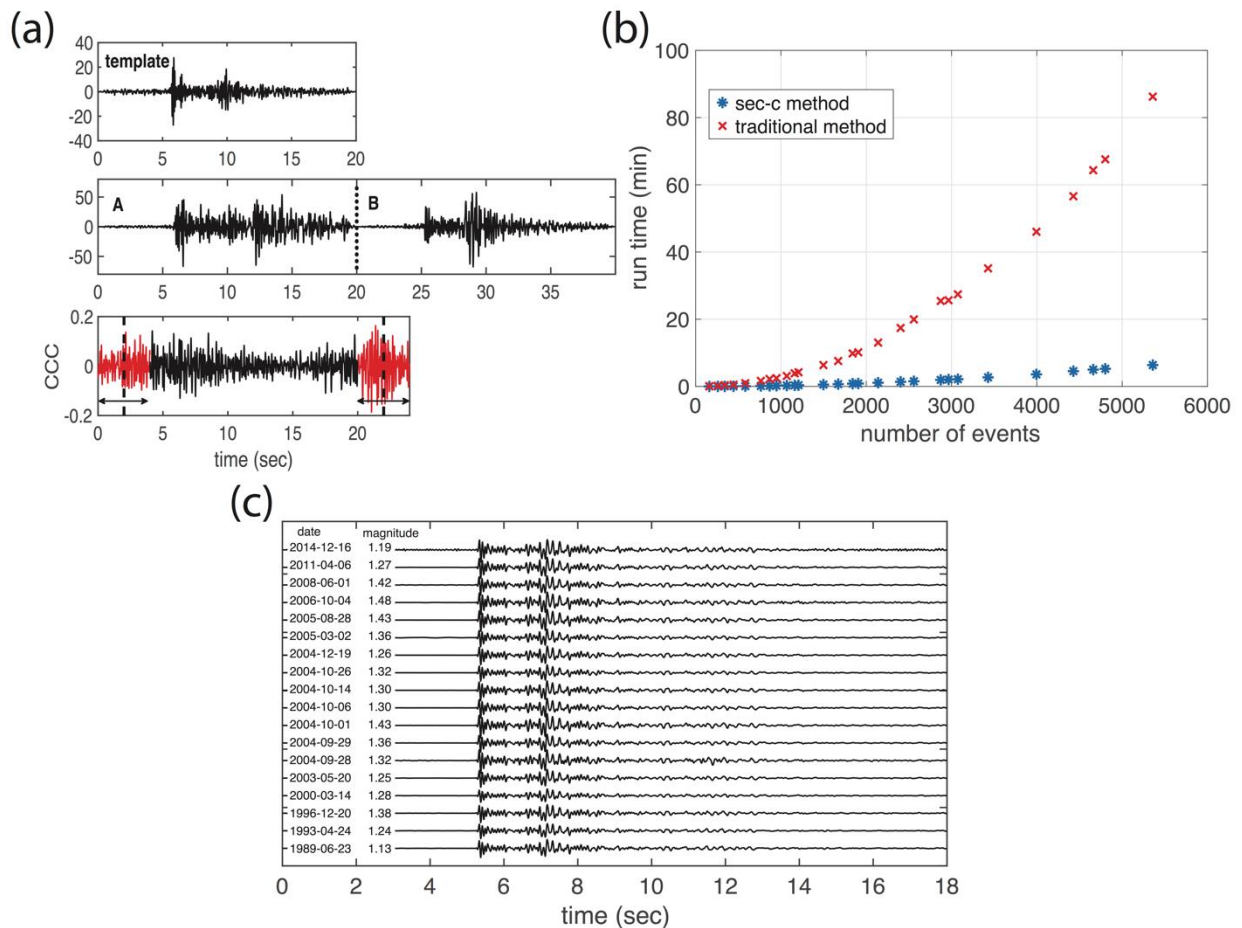


Figure 4: (a) An example shows how we use the SEC-C method to calculate cross-correlation coefficients (CCCs) for individual event waveforms. From top to bottom: a template, concatenated waveforms A and B, and CCC between the template and the concatenated waveform. Portions of the CCC function indicated by double-headed arrows are the scientifically useful calculated CCCs and the remainder the ‘unnecessary’ CCCs calculated in this process. Dashed lines indicate the CCC when the template is aligned with A and B based on P arrival phase information. The majority of CCC calculations are unnecessary (more than 83 percent). (b) Computational time comparison between SEC-C method and the traditional method of searching for REs in different data sets containing different numbers of events. Note that both

of these methods show computation time proportional to the square of the number of events, n (i.e $O(n^2)$). This comparison shows that the SEC-C method is 10.8 to 15.5 times faster for data sets ranging from hundreds to thousands of events and has a mean improvement of 12.1 times faster in general. (c) One example of a RE family detected by the SEC-C method using waveform data from seismic station PGH (see Figure 3a for locations of the RE family and PGH).