# SWITCHED-CAPACITOR DC-DC CONVERTERS FOR LOW-POWER ON-CHIP APPLICATIONS 

Dragan Maksimović and Sandeep Dhar<br>Colorado Power Electronics Center<br>Department of Electrical and Computer Engineering<br>University of Colorado, Boulder, CO 80309-0425<br>http://ece-www.colorado.edu/~pwrelect

Phone: (303)492-4863, Fax: (303)492-2758, maksimov@colorado.edu, dhar@copec.colorado.edu


#### Abstract

The paper describes switched-capacitor dc-dc converters (charge pumps) suitable for on-chip, low-power applications. The proposed configurations are based on connecting two identical but opposite-phase SC converters in parallel, thus eliminating the need for separate bootstrap gate drivers. We focus on emerging very low-power VLSI applications such as batterypowered or self-powered signal processors where high power conversion efficiency is important and where power levels are in the milliwatt range. Conduction and switching losses are considered to allow design optimization in terms of switching frequency and component sizes. Open-loop and closed-loop operation of an experimental, fully integrated, 10 MHz voltage doubler is described. The doubler has 2 V or 3 V input and generates 3.3 V or 5 V output at up to 5 mW load. The converter circuit fabricated in a standard $1.2 \mu$ CMOS technology takes $0.7 \mathrm{~mm}^{2}$ of the chip area.


## 1 Introduction

Switched-capacitor (SC) dc-dc converters (also called "charge pumps") are power converters that consist of switches and energytransfer capacitors in the power stage. The switches are periodically turned on and off so that the converter cycles through a number of switched networks. Possible low and medium-power applications of SC converters have been examined in a number of publications ([1][9], and others). In this paper, we focus on very low-power, on-chip applications [1, 2, 3], where there is a need to generate various DC voltage levels from a given external DC supply $V_{D D}$. Such applications include EEPROM and Flash memories, auxiliary supplies for analog portions of low-voltage, mixed-signal VLSI, and implementation of emerging adaptive voltage-scaling power management techniques [10] in energy-limited systems. The output power in these applications is often in the milliwatt range, but converter efficiency and area taken by the converter can be very important.

The purpose of this paper is to introduce design objectives and constraints in the relatively new and expanding power electronics area of on-chip power conversion. A general approach to construct SC converter configurations well suited for on-chip implementation in standard CMOS technologies is discussed in Section 2, together with analysis of conduction and switching losses. An experimental, fully

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Figure 1: Ideal switched-capacitor voltage doubler. Switches "1" are on during one phase of the clock, switches " 2 " are on during the opposite phase.
integrated voltage doubler is described in Section 3.

## 2 On-Chip Implementation of SC Converters in Standard CMOS Technology

In two-phase SC converters, an example of which is shown in Fig. 1, the number of switched networks is two. When an ideal SC converter is unloaded, the DC voltage conversion ratio $M=V_{O} / V_{D D}$ assumes a value $M=M_{i}$, which is uniquely determined by the converter topology. For example, the basic voltage doubler shown in Fig. 1 has the ideal step-up conversion ratio $M_{i}=V_{O} / V_{D D}=2$.

In this section we examine issues related to design and implementation of fully integrated switched-capacitor power converters in standard CMOS technology. First, it is of interest to compare some of the traditional discrete-component power converter design constraints to integrated-circuit (IC) realizations. In discrete-component realizations, minimizing the power-stage component count and circuit complexity are the usual cost constraints, whereas in IC realizations the required chip area is important. Much more flexibility is available to the designer in sizing components (switches and capacitors), but the component characteristics are subject to the technology limitations, some of which are pointed out in this section.

### 2.1 On-chip capacitors

In a standard CMOS process, there are a number of ways to construct capacitors. For example, Fig. 2 shows a capacitor constructed as a parallel-plate capacitor using two polysillicone layers in a double-poly CMOS process. The circuit model for the capacitor


Figure 2: Double-poly capacitor.


Figure 3: A general implementation block diagram using two opposite-phase SC converters connected in parallel.
$C$ also includes parasitic capacitances: $C_{B P}$ from the bottom plate of $C$ to substrate (ground), and $C_{T P}$ from the top plate to substrate. The top-plate capacitance is due to the interconnect metal wires, and is usually very small compared to the capacitance $C$. However, the bottom-plate capacitor has area at least equal to the area of the capacitor $C$, and so it can have very significant value and effects on the circuit operation. The bottom-plate capacitance can be expressed as $C_{B P}=\alpha C$, where can be up to $10 \%$ for the double-poly capacitor.

### 2.2 Switched-capacitor circuit configurations

The switches in an on-chip SC converter can be realized using NMOS or PMOS device, or their parallel or series combinations. For step-up voltage-conversion applications, such as the basic voltage doubler shown in Fig. 1, appropriate gate-drive signals for the switches must include voltage levels above the available supply voltage $V_{D D}$.

One approach to constructing step-up SC configurations together with appropriate gate drive signals is illustrated in Fig. 3. The idea is to combine two identical SC converters in parallel and operate the converters with opposite-phase clock signals [1]. Fig. 3 shows the two-phase clock signals $p_{1}, p_{2}$, at constant switching frequency $f$, generated from the input $V_{D D}$ supply. The two converters have the same but opposite-phase pulsating voltages at the internal nodes. The


Figure 4: Realization of the voltage doubler based on the block diagram of Fig. 3.
pulsating voltages from one converter are used as gate-drive signals in the other converter.
Fig. 4 shows implementation of the basic voltage doubler of Fig. 1 based on the block diagram of Fig. 3 [2]. One SC converter consists of the switches $M_{1}, M_{3}, M_{5}, M_{7}$, and the capacitor $C_{1}$. The other SC converter consists of the switches $M_{2}, M_{4}, M_{6}, M_{8}$ and the capacitor $C_{2}$. The two converters share the same input voltage $V_{D D}$, and the same output filter capacitor $C_{\text {out }}$. The gates of $M_{5}, M_{6}$ and $M_{7}$, $M_{8}$ are cross-coupled. Operation of the cross-coupled converter can be described as follows: when $p_{1}$ clock is equal to $+V_{D D}$ (i.e. high) and $p_{2}$ clock is 0 (i.e. low), $M_{1}$ is on, and node $a_{1}$ is at approximately zero volts. Device $M_{4}$ is on so that node $a_{2}$ is at $V_{D D}$, bringing node $b_{2}$ up to approximately $2 V_{D D}$ since $C_{2}$ was charged up to $+V_{D D}$ in the previous half cycle. As a result, the NMOS device $M_{5}$, with the gate tied to the node $b_{2}$, is turned on, node $b_{1}$ is at approximately $V_{D D}$, and the capacitor $C_{1}$ is charged to $+V_{D D}$ through $M_{5}$ and $M_{1}$. At the same time, since the node $b_{2}$ is at $+2 V_{D D}$ and $b_{1}$ is at $+V_{D D}$, the PMOS device $M_{8}$ turns on and the output is charged to $+2 V_{D D}$ through $M_{4}$ and $M_{8}$, while the device $M_{7}$ is off. In the opposite phase, $C_{2}$ is recharged to $+V_{D D}$ through $M_{6}$ and $M_{2}$, while the output is charged to $2 V_{D D}$ through $M_{3}, C_{1}$, and $M_{7}$.

The parallel, opposite-phase, cross-coupled converter connection eliminates the need for separate bootstrap gate drivers. Also, the effective switching frequency for the output filter capacitor is $2 f$, where $f$ is the clock frequency. Each switch is driven with a gate-to-source on-voltage equal to at least $V_{D D}$, so that the on-voltage drop can be reduced to a small drop across the device on resistance. There are no constant (threshold) voltage drops as in some other low-efficiency implementations.

The cross-coupled converter connection can be used to construct other SC converter configurations. Fig. 5 shows two SC converters with ideal unloaded step-up conversion ratio $V_{O} / V_{D D}=3$. Possible on-chip realizations of these two converters following the block diagram of Fig. 3 are shown in Fig. 6.

### 2.3 Losses and efficiency

Conduction losses originate from charging and discharging of energy-transfer capacitors. The power is dissipated on the switch onresistances. A switched-capacitor converter model that can predict DC conversion ratio $M=V_{O} / V_{D D}$ and conduction losses consists of an ideal transformer with turns ratio $M_{i}=V_{O} / V_{D D}$ equal to the ideal, no-load conversion ratio of the SC converter, and a series output


Figure 5: Two switched-capacitor voltage tripler examples.
resistance $R_{o}(f)$ which is a function of clock frequency $f[8,9]$.
In the low-frequency limit, the output resistance is inversely proportional to the energy-transfer capacitance values, and the clock frequency [8],

$$
\begin{equation*}
R_{o}(f)=\frac{K}{C f} \tag{1}
\end{equation*}
$$

At high switching frequencies, the output resistance reaches a minimum value $R_{\text {omin }}$, which depends on the switch on resistances, and which can be found using state-space averaging. An analytical approximation for $R_{o}(f)$ over wide range of frequencies was proposed in [9]:

$$
\begin{equation*}
R_{o}(f) \approx R_{o \min } \sqrt{1+\left(f_{c} / f_{s}\right)^{2}} \tag{2}
\end{equation*}
$$

where the "corner" frequency $f_{c}$ is the frequency where the lowfrequency asymptote and the high frequency asymptote have the same value,

$$
\begin{equation*}
f_{c}=\frac{K}{C R_{o m i n}} \tag{3}
\end{equation*}
$$

For a given load current $I_{O}$, the conduction loss $P_{c}$ can be found as

$$
\begin{equation*}
P_{c}=R_{o}(f) I_{O}^{2} \tag{4}
\end{equation*}
$$

In an on-chip implementation, the switching losses can be estimated by finding the total parasitic capacitances at various nodes and the voltage swing across the capacitances. If the capacitance from node $a$ to ground is $C_{a}$, and if the voltage at the node $a$ is pulsating between $V_{1}=m_{1} V_{D D}$ and $V_{2}=m_{2} V_{D D}$, the switching power loss due to this capacitance is

$$
\begin{equation*}
P_{a}=C_{a}\left(V_{2}-V_{1}\right)^{2} f=\left(m_{2}-m_{1}\right)^{2} C_{a} V_{D D}^{2} f \tag{5}
\end{equation*}
$$

The total switching loss is found by summation of switching losses over all nodes in the SC converter:

$$
\begin{equation*}
P_{s w}=\sum_{\text {nodes }} P_{\text {node }} \tag{6}
\end{equation*}
$$

For example, in the voltage tripler of Fig. 6(a), we get:

$$
\begin{equation*}
P_{s w}(a) \approx 2 f V_{D D}^{2}\left(C_{a}+2 C_{b}+4 C_{c}+6 C_{d}\right), \tag{7}
\end{equation*}
$$

where, $C_{a}$ is the total parasitic capacitance from node $a_{1}$ (or $a_{2}$ ) to ground.


Figure 6: Implementation of the converter examples from Fig. 5 based on the block diagram of Fig. 3.

In the converter of Fig. 6(b), we get:

$$
\begin{equation*}
P_{s w}(b) \approx 2 f V_{D D}^{2}\left(C_{a}+2 C_{b}+3 C_{c}\right) \tag{8}
\end{equation*}
$$

From the results above, one can observe that the converter (b) has an advantage over the converter (a) because the internal voltage node swings are smaller, thus resulting in lower switching losses.

With on-chip capacitors, the bottom-plate parasitic capacitances dominate the nodal capacitances. In the converter (a), we have $C_{a} \approx$ $C_{B P}$, and $C_{c} \approx C_{B P}$, so that this portion of the power loss becomes:

$$
\begin{equation*}
P_{B P}(a) \approx 10 f V_{D D}^{2} C_{B P}=10 f V_{D D}^{2} \alpha C . \tag{9}
\end{equation*}
$$

In the converter (b), $C_{a} \approx 2 C_{B P}$, so that:

$$
\begin{equation*}
P_{P B}(b) \approx 4 f V_{D D}^{2} C_{B P}=4 f V_{D D}^{2} \alpha C . \tag{10}
\end{equation*}
$$

Notice that the power loss due to the bottom-plate capacitance in the converter (b) is about 2.5 times smaller than in the converter (a).

From the discussion above, the total switching loss in the converter can be written as

$$
\begin{equation*}
P_{s w}=C_{s w} V_{D D}^{2} f, \tag{11}
\end{equation*}
$$

where $C_{s w}$ is the equivalent switching-loss capacitance of the converter. For a given converter configuration, optimum clock frequency $f$ can be found where the sum of conduction and switching losses $P_{c}+P_{s w}$ is minimum [9].

## 3 Voltage doubler implementation and experimental results

To illustrate on-chip SC converter design issues, we consider implementation of a voltage doubler based on the cross-coupled configu-


Figure 7: Detailed circuit diagram of the voltage doubler of Fig. 4. Drive transistors $M_{1}, M_{2}, M_{3}, M_{4}$ are not shown.
ration of Fig. 4. The technology used for fabrication is AMI $1.2 \mu$ double-poly n -well technology available through MOSIS [11].

Detailed circuit diagram of the basic voltage doubler is shown in Fig. 7. Substrate connections for all devices are indicated in the figure: NMOS device share the common substrate, which is connected to ground, while PMOS devices are constructed in a common n-well, which is biased at voltage $V_{B}$. Two opposite-phase clock signals ( $p_{1}$ and $p_{2}$ shown in Fig. 3), are used to drive CMOS inverters $M_{1}, M_{3}$ and $M_{2}, M_{4}$ shown in Fig. 4, in order to produce two pump drive signals at nodes $a_{1}$ and $a_{2}$ as shown in Fig. 7. The drive signals at nodes $a_{1}$ and $a_{2}$ are shown as non-overlapping opposite-phase signals: there are short time intervals when both $a_{1}$ and $a_{2}$ are at zero volts. NMOS pump devices $M_{5}, M_{6}$ have cross-coupled gates (nodes $b_{1}, b_{2}$ ), that swing between $V_{D D}$ and $2 V_{D D}$. Since the drive signals at nodes $a_{1}, a_{2}$ are nonoverlapping, $M_{5}$ and $M_{6}$ are never on at the same time. The energy-transfer pump capacitors $C_{1}, C_{2}$ are charged through $M_{5}, M_{6}$ to $+V_{D D}$ in opposite phases of the clock signals. Series PMOS switches $M_{7}, M_{8}$ also have cross-coupled gates and are used to pass $2 V_{D D}$ to the output filter capacitor $C_{\text {out }}$. In addition, auxiliary PMOS devices $M_{7 a}, M_{8 a}$, and capacitor $C_{b}$ are used to bias the n-well of the PMOS devices at voltage $V_{B} \approx 2 V_{D D}$ [2]. Since $C_{b}$ is unloaded, $V_{B}$ is always greater than or equal to $V_{\text {out }}$, which ensures that the source and drain to $n$-well junctions of the PMOS devices are always reverse biased. This is important because forward bias of these junctions may cause lossy discharge of the output or latch-up condition through the p-substrate of the chip [2].

A problem with the circuit shown in Fig. 7 is that during the intervals when both $a_{1}$ and $a_{2}$ are close to ground, both $b_{1}$ and $b_{2}$ are close to $V_{D D}$, and therefore both PMOS switches $M_{7}, M_{8}$ are turned on at the same time. As a result, undesirable lossy discharge of the output filter capacitor $C_{\text {out }}$ occurs. One may attempt to reduce the time intervals when $a_{1}$ and $a_{2}$ are simultaneously low, or even to slightly overlap the two drive signals. However, this contradicts the desirable timing of the drive waveforms for the NMOS pump devices $M_{5}$ and


Figure 8: Circuit diagram of the experimental voltage doubler.
$M_{6}$, and may lead to the case when both $M_{5}$ and $M_{6}$ are turned on at the same time. This would result in lossy discharge of $C_{1}, C_{2}$ back to $V_{D D}$. The problem with exact timing of the drive signals $a_{1}, a_{2}$ is particularly important at high clock frequencies (in the MHz range and above), because the losses incurred due to the undesirable conduction of the cross-coupled device effectively increase the switching losses in the converter.

In order to alleviate the problem observed in the circuit of Fig. 7, we investigated the circuit shown in Fig. 8. Another cross-coupled pump is added. The second cross-coupled pump is driven by overlapping drive signals at nodes $a_{3}, a_{4}$. The two pumps are coupled so that NMOS devices in both pumps are driven by non-overlapping signals, while PMOS devices in both pumps are driven by overlapping signals as shown in Fig. 9. As a result of this arrangement, possible lossy simultaneous conduction of the pairs $\left(M_{3}, M_{4}\right),\left(M_{13}, M_{14}\right),\left(M_{7}\right.$, $M_{8}$ ), and ( $M_{17}, M_{18}$ ) are eliminated. However, it is still important that the transitions of $a_{1}$ and $a_{3}$, as well as of $a_{2}$ and $a_{4}$ occur at the same time, and that these transitions have short rise and fall times, in order to avoid parasitic discharge of the output filter capacitor $C_{\text {out }}$ through one of the PMOS series switches.

The circuit of Fig. 8, together with an oscillator, and a clock generator to produce the waveforms shown in Fig. 9, have been fabricated in $1.2 \mu$ double-poly CMOS technology. All capacitors are doublepoly capacitors described in Section 2.1. The device and capacitor


Figure 9: Drive waveforms for the voltage doubler in Fig. 8.


Figure 10: Experimental drive waveforms in the doubler of Fig. 8 operating at $f=10 \mathrm{MHz}$.
sizes were selected so that the voltage doubler can produce $V_{O}=5 \mathrm{~V}$ output from $V_{D D}=3 \mathrm{~V}$ input at the maximum output power of 5 mW . The energy-transfer capacitors are 30 pF each, the output filter capacitor is 60 pF . The doubler occupies $0.7 \mathrm{~mm}^{2}$ of the chip area, not including i/o and supply/ground pads.

Experimental pump drive signals $a_{1}, a_{2}, a_{3}, a_{4}$ observed through four output pads are shown in Fig. 10 for $f=10 \mathrm{MHz}$ clock frequency.

The plot of output voltage as a function of frequency is shown in Fig. 11 for $V_{D D}=2 \mathrm{~V}$ and $V_{D D}=3 \mathrm{~V}$ for a frequency range of 5 MHz to 20 MHz at no load, $R=10 k \Omega$ and $R=4.7 k \Omega$ load. The fact that the no-load output voltage is slightly lower than the ideal $2 V_{D D}$ indicates that the SC voltage doubler still has some undesirable discharge of the output filter capacitor through the PMOS switches.

The voltage doubler of Fig. 9 consists of four basic doublers connected in parallel. The low-frequency asymptote of the output resistance as a function of frequency is: $R_{o}(f)=\frac{1}{4 C f}$, while the highfrequency asymptote is: $R_{o m i n}=\left(R_{n 1}+R_{n 2}+R_{p 1}+R_{p 2}\right) / 2$, which depends on the on-resistance $R_{n 1}$ of the NMOS driver transistor $M_{1}, R_{n 2}$ of the NMOS pump transistor $M_{3}, R_{p 1}$ of the PMOS driver $M_{3}$, and $R_{p 2}$ of the PMOS switch $M_{7}$. For $V_{D D}=3 \mathrm{~V}$, and the selected device sizes, we have $R_{\text {omin }}=196 \Omega+148 \Omega+279 \Omega+$ $279 \Omega=450 \Omega$. Each of the four energy-transfer, 30 pF pump capacitors has $C_{B P}=2.3 \mathrm{pF}$ bottom-plate capacitance. If all other switching losses are neglected, the equivalent switching loss capacitance is $C_{s w} \approx 4 C_{B P}=9.2 \mathrm{pF}$. Experimental power-loss measurements at


Figure 11: Output DC voltage $V_{O}$ as a function of clock frequency $f$ for various loads and input supply voltages.


Figure 12: Measured (lines with points) and theoretical power efficiency of the voltage doubler of Fig. 8 as functions of clock frequency $f$ for two different loads.
no load for various $V_{D D}$ and for a range of clock frequencies, indicate that the switching loss indeed follows the theoretical expression $P_{s w}=C_{s w} V_{D D}^{2} f$, but the value of the equivalent switching-loss capacitance estimated from the measurement is $C_{s w}=20 \mathrm{pF}$. Additional switching loss can be attributed to other nodal capacitances, losses in the waveform generator circuit, and parasitic discharge of the output through the PMOS switches.

Fig. 12 shows theoretical and measured power efficiency for $f=$ $10 \mathrm{MHz}, V_{D D}=3 \mathrm{~V}$, and two different loads, $R=10 k \Omega$ and $R=$ $4.7 k \Omega$. For $R=4.7 k \Omega$, which is the maximum load the doubler was designed for, the efficiency peaks at about $68 \%$ for $f$ around 10 MHz . Good agreement between the theoretical and the measured results can be observed.

The voltage doubler can be operated as a closed-loop voltage regulator using a simple "bang-bang" feedback circuit shown in Fig. 13 [9]. The on-chip oscillator has a clock-enable input $\overline{C E}$. When $\overline{C E}$ is low, the oscillator is enabled and generates the clock signal for the voltage doubler. When $\overline{C E}$ is high, the oscillator is disabled and no clock signal is produced. A voltage comparator with hysteresis is used to generate the clock-enable signal. Closed-loop operation was tested for: $V_{D D}=2 \mathrm{~V}, V_{\text {ref }}=3.3 \mathrm{~V}$, and the hysteresis loop of $\pm 0.1 \mathrm{~V}$ around the 3.3 V reference, and for $V_{D D}=3 \mathrm{~V}, V_{\text {ref }}=5 \mathrm{~V}$, and $\pm 0.1 \mathrm{~V}$ hysteresis loop around the 5 V reference. Waveforms of Fig. 14 illustrate how the converter maintains the output voltage within the limits specified by the hysteresis loop when subject to a step change in load.


Figure 13: Voltage doubler operated as a closed-loop voltage regulator.


Figure 14: Waveforms illustrating closed-loop operation of the voltage doubler.


Figure 15: Efficiency of the closed-loop doubler voltage regulator operating at $f=10 \mathrm{MHz}$ as a function of load current, for two different operating conditions: $V_{D D}=2 \mathrm{~V}, V_{O}=3.3 \mathrm{~V}$, and $V_{D D}=3 \mathrm{~V}$, $V_{O}=5 \mathrm{~V}$.

In addition to good output voltage regulation, another advantage of the closed-loop control scheme is that both switching and conduction losses scale with load. At no load, the oscillator is almost always turned off and no-load power losses are very small, $5 \mu \mathrm{~W}$ for $V_{D D}=$ 3V in our experimental circuit. Fig. 15 shows efficiency measured for fixed $f=10 \mathrm{MHz}$ frequency over a range of loads and the output
closed-loop regulated at 3.3 V (with $V_{D D}=2 \mathrm{~V}$ ), and at 5 V (with $V_{D D}=3 \mathrm{~V}$ ). It can be observed that almost constant efficiency is maintained for a wide range of loads.

## 4 Conclusions

The paper describes switched-capacitor dc-dc converters (charge pumps) suitable for on-chip, low-power applications. We focus on emerging energy-limited very low-power VLSI applications (such as battery-powered or self-powered signal processors) where high power conversion efficiency is important and where power levels are in the milliwatts range. In fully integrated realizations with on-chip capacitors, the design is not limited by the number of components or the circuit complexity. Also, compared to discrete-circuit designs, there is much more flexibility in sizing switches and capacitors. However, on-chip capacitors exhibit large parasitic (bottom-plate) capacitances that increase switching losses in the converter and ultimately limit the achievable power efficiency.

Converter configurations suitable for on-chip realization are described. The proposed configurations are based on connecting two (or more) identical but opposite-phase SC converters in parallel, thus eliminating the need for separate bootstrap gate drivers. Conduction and switching losses are considered to allow design optimization in terms of switching frequency and component sizes. Open-loop and closed-loop operation of an experimental, fully integrated, 10 MHz voltage doubler is described. The doubler has 2 V or 3 V input and generates 3.3 V or 5 V output at up to 5 mW load. The converter circuit fabricated in a standard $1.2 \mu$ CMOS technology takes $0.7 \mathrm{~mm}^{2}$ of the chip area.

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