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Synchrotron X-ray study of the electron density in α -Al₂O₃

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Material for deposit

Lists of structure factors for all of 5 data sets and figures of deformation density sections in (01T0) plane through O and two Al atoms for data sets 1,3,4,5 and 3 scaled on data set 2 with the extinction corrections evaluated by minimizing differences between equivalent reflection intensities and with the extinction parameter included in the structure refinement.

Synchrotron X-ray Study of the Electron Density in α -Al₂O₃

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Abstract

Structure factors for corundum α -Al₂O₃, have been measured using 0.7 Å and 0.9 Å synchrotron radiation as well as Mo K α ($\lambda = 0.71069$ Å) radiation. The stronger structure factors from two sets of synchrotron data and three sets of Mo K α tube data for two small crystals are remarkably consistent. In analysing those data, extinction corrections evaluated by minimizing differences between equivalent reflection intensities were compared with those from the more common procedure of least squares determination of the extinction parameters as a part of the structure refinement. Difference electron densities evaluated with extinction corrections from equivalent reflection intensities are more consistent than those which optimize $|F_o|$ v $|F_c|$ agreement. Approximate symmetry in the concordant densities is related more closely to the Al-Al geometry than to nearest neighbour Al-O interactions. Space group $R\bar{3}c$, hexagonal, $M_r = 101.96$, $a = 4.7540$ (5) Å, $c = 12.9820$ (6) Å, $V = 254.09$ (6) Å³, $Z = 6$, $D_x = 3.997$ Mg m⁻³, $\mu_{0.9} = 2.361$, $\mu_{0.7} = 1.097$, $\mu_{\text{Mo } K\alpha} = 1.139$ mm⁻¹, $F(000) = 300$, $T = 293$ K, $R = 0.024$, $wR = 0.030$, $S = 4.84$ for the unique 0.7 Å synchrotron reflection data.

71271

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Data set 1					
h	k	l	Fo	$\sigma(Fo)$	
0	-2	2	13.742	.300	-1 -1 6 95.588 .516
0	-4	4	37.861	.371	-1 -2 7 12.822 .267
0	-6	6	9.272	.784	-1 -3 8 34.144 .269
-1	9	-7	14.000	.509	-1 -4 9 21.354 .333
-1	8	-6	24.064	.424	-1 -5 10 29.132 .361
-1	6	-4	44.012	.324	-2 8 -1 13.111 .495
-1	5	-3	24.414	.291	-2 7 0 28.019 .360
-1	4	-2	32.177	.239	-2 6 1 12.706 .369
-1	3	-1	18.787	.215	-2 5 2 7.111 .396
-1	2	0	58.448	.218	-2 4 3 36.081 .234
-1	0	2	48.667	.184	-2 -1 8 26.992 .240
-1	-1	3	77.718	.176	-2 -2 9 27.579 .282
-1	-2	4	76.093	.208	-2 -3 10 37.467 .310
-1	-3	5	7.051	.418	-2 -4 11 9.639 .515
-1	-4	6	52.600	.291	-2 -6 13 11.053 .600
-1	-5	7	14.709	.393	-3 9 0 34.653 .406
-1	-6	8	18.915	.423	-3 7 2 25.860 .358
-1	-7	9	9.599	.623	-3 5 4 61.133 .270
-2	8	-4	32.122	.397	-3 -1 10 61.485 .281
-2	7	-3	14.302	.436	-3 -2 11 9.476 .426
-2	6	-2	12.400	.389	-3 -3 12 24.503 .373
-2	5	-1	12.162	.321	-3 -5 14 26.642 .423
-2	4	0	54.437	.321	-4 8 3 12.559 .503
-2	0	4	89.439	.293	-4 7 4 17.398 .397
-2	-1	5	15.403	.244	-4 6 5 11.274 .407
-2	-2	6	70.808	.247	-4 -2 13 9.914 .534
-2	-3	7	10.630	.373	-4 -3 14 13.933 .491
-2	-4	8	16.148	.382	-4 -4 15 10.282 .608
-2	-5	9	13.128	.485	-5 9 4 25.565 .424
-2	-6	10	15.958	.479	-5 7 6 35.249 .364
-3	6	0	72.235	.419	-5 -1 14 34.034 .376
-3	0	6	14.643	.359	-5 -2 15 11.597 .520
-3	-1	7	8.350	.357	-5 -3 16 20.659 .447
-3	-2	8	12.731	.347	-6 8 7 13.239 .502
-3	-4	10	44.253	.370	-6 -1 16 9.357 .635
-3	-5	11	9.737	1.501	0 6 0 58.092 .469
-3	-6	12	12.251	.497	0 4 2 38.969 .357
-4	10	-2	15.513	.479	0 0 6 18.665 .441
-4	9	-1	13.342	.484	0 -2 8 25.221 .313
-4	8	0	25.666	.558	0 -4 10 63.674 .419
-4	0	8	38.716	.402	0 -6 12 20.446 .576
-4	-1	9	21.522	.342	-1 9 -1 13.818 .517
-4	-2	10	37.766	.341	-1 8 0 22.008 .426
-4	-5	13	10.738	.560	-1 5 3 24.719 .286
-5	10	0	15.388	.638	-1 4 4 50.177 .243
-5	0	10	31.493	.485	-1 0 8 44.239 .277
-5	-1	11	14.022	.415	-1 -1 9 43.673 .222
-6	0	12	19.756	.583	-1 -2 10 61.541 .254
-6	-2	14	27.029	.420	-1 -5 13 13.173 .479
0	7	-4	8.387	.816	-1 -6 14 16.750 .481
0	3	0	127.477	.436	-2 7 3 13.771 .430
0	-1	4	79.547	.236	-2 6 4 40.363 .312
0	-3	6	33.685	.382	-2 5 5 10.754 .378
0	-5	8	10.204	.634	-2 0 10 62.125 .336
0	-7	10	40.534	.566	-2 -1 11 9.477 .358
-1	9	-4	24.707	.436	-2 -2 12 7.908 .434
-1	8	-3	10.717	.557	-2 -4 14 29.420 .382
-1	7	-2	16.522	.427	-2 -5 15 10.893 .578
-1	6	-1	15.584	.371	-2 -6 16 20.894 .430
-1	5	0	45.122	.277	-3 8 4 33.810 .383
-1	4	1	9.081	.326	-3 6 6 12.715 .381
-1	3	2	20.867	.209	-3 0 12 38.872 .406
					-3 -1 13 7.098 .476
					-3 -2 14 41.632 .345

-4	9	5	12.981	.528
-4	8	6	26.858	.400
-4	0	14	25.778	.498
-4	-1	15	16.483	.437
-4	-2	16	19.264	.439
-5	10	6	20.614	.445
-5	9	7	11.081	.585
-5	0	16	27.571	.570
-5	-1	17	11.153	.546
-6	0	18	25.631	.601
0	7	2	25.796	.562
0	5	4	52.770	.421
0	-1	10	79.558	.315
0	-3	12	38.672	.406
0	-5	14	36.919	.512
-1	8	3	10.560	.593
-1	7	4	21.222	.405
-1	6	5	14.746	.381
-1	5	6	52.493	.292
-1	-1	12	9.756	.353
-1	-2	13	9.412	.388
-1	-3	14	33.344	.330
-1	-4	15	17.664	.417
-1	-5	16	24.572	.409
-2	9	4	19.305	.478
-2	8	5	13.434	.501
-2	7	6	36.061	.359
-2	6	7	12.390	.408
-2	-1	14	47.402	.298
-2	-2	15	21.138	.357
-2	-3	16	29.189	.372
-3	9	6	8.955	.598
-3	7	8	27.865	.375
-3	-1	16	18.752	.381
-3	-3	18	29.969	.396
-4	8	9	12.206	.514
-4	-3	20	28.176	.428
-5	9	10	17.384	.452
-5	-1	20	15.687	.493
0	8	4	24.769	.615
0	6	6	11.178	.648
0	0	12	53.556	.587
0	-2	14	53.445	.402
0	-4	16	12.503	.593
0	-6	18	24.627	.602
-1	9	5	14.316	.469
-1	8	6	23.847	.422
-1	6	8	8.561	.548
-1	0	14	49.876	.380
-1	-1	15	26.689	.303
-1	-2	16	30.934	.332
-1	-5	19	10.063	.640
-2	7	9	12.416	.489
-2	0	16	37.226	.427
-2	-4	20	21.587	.426
-3	8	10	17.545	.475
-3	0	18	40.280	.509
-3	-2	20	19.611	.428
-4	9	11	12.021	.509
-4	0	20	35.383	.563
-4	-1	21	14.544	.471
0	7	8	28.089	.568
0	-1	16	30.007	.430
0	-3	18	41.470	.501

0	-5	20	17.838	.617
-1	8	9	9.029	.673
-1	7	10	34.745	.382
-1	-1	18	9.565	.432
-1	-3	20	32.382	.392
-1	-4	21	14.185	.496
-2	9	10	19.689	.440
-2	8	11	11.584	.587
-2	-1	20	28.513	.382
-2	-2	21	16.111	.485
-3	9	12	12.382	.517
-4	-1	24	25.509	.415
0	8	10	15.232	.635
0	0	18	50.769	.768
0	-2	20	28.243	.543
-1	0	20	37.214	.482
-1	-1	21	20.106	.415
-1	-4	24	24.941	.417
-2	-2	24	30.550	.399
-1	-1	24	34.209	.395
-2	-1	26	12.798	.517
0	-2	26	15.937	.673
-1	0	26	10.551	.874
-1	-1	27	15.679	.463

Data set 2

h	k	l	Fo	$\sigma(Fo)$
0	-2	2	13.841	.140
0	-4	4	38.162	.196
0	-6	6	11.085	.229
-1	8	-6	24.520	.172
-1	7	-5	5.818	.168
-1	6	-4	44.600	.158
-1	5	-3	25.255	.145
-1	4	-2	32.209	.130
-1	3	-1	18.859	.111
-1	2	0	56.753	.522
-1	0	2	46.544	.116
-1	-1	3	74.698	.419
-1	-2	4	74.991	.325
-1	-3	5	7.679	.133
-1	-4	6	53.322	.150
-1	-5	7	14.623	.160
-1	-6	8	18.738	.169
-1	-7	9	9.828	.173
-2	8	-4	32.946	.170
-2	7	-3	14.111	.162
-2	6	-2	13.291	.153
-2	5	-1	12.004	.140
-2	4	0	54.411	.182
-2	0	4	87.272	.195
-2	-1	5	15.603	.119
-2	-2	6	70.773	.139
-2	-3	7	10.904	.323
-2	-4	8	16.635	.159
-2	-5	9	13.078	.167
-2	-6	10	16.412	.172
-3	9	-3	2.221	.184
-3	8	-2	1.189	.195
-3	7	-1	2.850	.165
-3	6	0	72.750	.219
-3	0	6	14.397	.178
-3	-1	7	7.989	.137
-3	-2	8	12.704	.148

-3	-3	9	.985	.218	-5	9	4	25.920	.171
-3	-4	10	44.863	.168	-5	8	5	7.828	.168
-3	-5	11	6.913	.172	-5	7	6	35.970	.165
-4	9	-1	12.801	.170	-5	-1	14	33.454	.168
-4	8	0	26.336	.236	-5	-2	15	11.337	.170
-4	0	8	39.139	.206	-6	9	6	8.000	.172
-4	-1	9	21.676	.153	-6	8	7	13.072	.171
-4	-2	10	37.743	.162	-6	-1	16	9.716	.171
-4	-3	11	1.671	.190	0	0	8	-.069	.622
-4	-4	12	.927	.242	0	0	6	0	.229
-5	0	10	31.929	.224	0	0	4	37.991	.193
-5	-1	11	13.313	.164	0	0	6	18.433	.230
-5	-2	12	4.579	.169	0	-2	8	25.324	.172
-5	-3	13	6.658	.172	0	-4	10	63.861	.217
-6	0	12	20.533	.237	0	-6	12	20.504	.237
-6	-1	13	5.640	.171	-1	8	0	21.750	.170
-7	0	14	6.291	.242	-1	7	1	5.961	.164
0	0	7	8.537	.237	-1	6	2	4.677	.156
0	5	-2	5.055	.213	-1	5	3	25.334	.144
0	3	0	123.056	.446	-1	4	4	50.603	.134
0	-1	4	73.352	.810	-1	0	8	43.526	.159
0	-3	6	13.818	.179	-1	-1	9	43.767	.124
0	-5	8	9.493	.220	-1	-2	10	61.612	.139
0	-7	10	42.087	.244	-1	-3	11	5.436	.148
-1	8	-3	10.387	.171	-1	-4	12	4.643	.156
-1	7	-2	16.584	.164	-1	-5	13	13.003	.166
-1	6	-1	16.300	.155	-1	-6	14	17.525	.171
-1	5	0	46.161	.144	-2	9	1	7.659	.172
-1	4	1	8.827	.129	-2	8	2	1.092	.231
-1	3	2	21.050	.112	-2	7	3	14.200	.162
-1	-1	6	92.811	.559	-2	6	4	40.131	.155
-1	-2	7	12.330	.125	-2	5	5	11.680	.143
-1	-3	8	34.441	.141	-2	0	10	62.510	.189
-1	-4	9	21.434	.153	-2	-1	11	9.774	.139
-1	-5	10	29.339	.164	-2	-2	12	6.835	.150
-1	-6	11	4.539	.171	-2	-3	13	8.273	.158
-2	9	-2	5.950	.172	-2	-4	14	29.585	.167
-2	8	-1	13.311	.168	-2	-5	15	11.523	.171
-2	7	0	28.237	.161	-3	9	3	2.388	.174
-2	6	1	12.265	.151	-3	8	4	33.933	.168
-2	5	2	6.637	.140	-3	7	5	2.546	.164
-2	4	3	36.530	.129	-3	6	6	12.665	.155
-2	-1	8	27.648	.128	-3	0	12	39.478	.206
-2	-2	9	28.370	.141	-3	-1	13	5.941	.153
-2	-3	10	38.331	.153	-3	-2	14	41.355	.162
-2	-4	11	9.896	.162	-3	-3	15	1.229	.209
-2	-5	12	4.366	.171	-3	-4	16	5.027	.172
-3	9	0	34.545	.172	-4	9	5	12.164	.171
-3	8	1	7.887	.167	-4	8	6	27.517	.169
-3	7	2	25.722	.160	-4	7	7	2.798	.170
-3	6	3	1.316	.181	-4	0	14	25.255	.224
-3	5	4	60.891	.146	-4	-1	15	17.512	.164
-3	-1	10	62.001	.148	-4	-2	16	18.984	.169
-3	-2	11	9.154	.154	-4	-3	17	1.345	.216
-3	-3	12	24.449	.163	-5	8	8	4.226	.170
-3	-4	13	2.491	.176	-5	0	16	27.849	.236
-3	-5	14	27.087	.172	-5	-1	17	11.162	.169
-4	9	2	1.799	.172	-6	0	18	24.749	.241
-4	8	3	13.066	.167	0	7	2	26.439	.235
-4	7	4	17.753	.161	0	5	4	52.926	.214
-4	6	5	11.915	.154	0	-1	10	78.836	.183
-4	-1	12	4.571	.160	0	-3	12	39.334	.205
-4	-2	13	10.248	.165	0	-5	14	37.263	.232
-4	-3	14	12.918	.170					

-1	8	3	10.320	.169
-1	7	4	21.840	.164
-1	6	5	14.937	.156
-1	5	6	53.270	.149
-1	-1	12	9.534	.135
-1	-2	13	8.768	.145
-1	-3	14	33.481	.156
-1	-4	15	17.647	.163
-1	-5	16	23.725	.169
-2	9	4	19.832	.170
-2	8	5	13.330	.168
-2	7	6	35.885	.164
-2	6	7	11.651	.156
-2	-1	14	47.726	.149
-2	-2	15	21.079	.156
-2	-3	16	29.505	.164
-2	-4	17	8.133	.168
-3	9	6	8.197	.170
-3	8	7	7.535	.168
-3	7	8	28.013	.164
-3	-1	16	18.778	.159
-3	-2	17	7.354	.165
-3	-3	18	29.267	.170
-4	9	8	4.468	.172
-4	8	9	12.137	.169
-4	-1	18	6.995	.167
-4	-2	19	8.552	.170
0	8	4	26.231	.241
0	6	6	10.122	.228
0	0	12	53.349	.322
0	-2	14	54.410	.208
0	-4	16	12.013	.228
0	-6	18	25.737	.242
-1	8	6	24.167	.170
-1	7	7	6.193	.166
-1	6	8	9.125	.160
-1	0	14	49.657	.200
-1	-1	15	26.885	.147
-1	-2	16	30.951	.155
-1	-3	17	4.150	.162
-1	-4	18	6.210	.168
-1	-5	19	10.527	.171
-2	8	8	2.436	.183
-2	7	9	12.679	.166
-2	0	16	35.830	.215
-2	-1	17	6.842	.157
-2	-2	18	7.020	.163
-2	-3	19	7.040	.168
-2	-4	20	21.393	.171
-3	8	10	17.641	.171
-3	0	18	42.208	.230
-3	-1	19	4.434	.168
-3	-2	20	19.302	.170
-4	0	20	35.519	.239
-4	-1	21	14.361	.171
0	7	8	28.111	.240
0	-1	16	30.461	.209
0	-3	18	41.584	.230
0	-5	20	16.748	.240
-1	8	9	9.263	.171
-1	7	10	34.861	.169
-1	-1	18	8.517	.156
-1	-2	19	6.664	.163
-1	-3	20	32.171	.168

-1	-4	21	14.060	.170
-2	8	11	12.736	.171
-2	-1	20	28.621	.165
-2	-2	21	16.491	.169
-2	-3	22	6.178	.170
-3	-1	22	5.446	.169
0	0	18	50.561	.381
0	-2	20	28.891	.231
0	-4	22	9.454	.240
-1	0	20	36.629	.229
-1	-1	21	19.743	.165
-1	-2	22	1.344	.222
-1	-3	23	2.858	.179
-2	0	22	4.315	.237
-2	-1	23	5.039	.171
-3	0	24	4.307	.243
0	-1	22	3.144	.240
0	-3	24	3.963	.240
-1	-1	24	34.396	.170
0	0	24	4.900	.399

Data set 3				
h	k	l	Fo	$\sigma(Fo)$
0	-2	2	13.641	.035
0	-4	4	37.285	.245
0	-6	6	10.463	.052
-1	8	-6	23.945	.036
-1	7	-5	5.551	.037
-1	6	-4	43.020	.182
-1	5	-3	24.783	.098
-1	4	-2	31.378	.162
-1	3	-1	18.252	.077
-1	2	0	54.510	.884
-1	0	2	44.703	.152
-1	-1	3	70.719	.591
-1	-2	4	71.503	.455
-1	-3	5	7.671	.032
-1	-4	6	51.667	.444
-1	-5	7	14.602	.081
-1	-6	8	18.332	.038
-1	-7	9	9.754	.034
-2	8	-4	32.401	.038
-2	7	-3	14.013	.036
-2	6	-2	12.928	.036
-2	5	-1	11.758	.071
-2	4	0	52.700	.250
-2	0	4	80.893	.215
-2	-1	5	15.384	.029
-2	-2	6	67.142	.507
-2	-3	7	10.373	.035
-2	-4	8	16.348	.037
-2	-5	9	13.002	.036
-2	-6	10	16.250	.035
-3	9	-3	2.310	.041
-3	8	-2	3.185	.054
-3	7	-1	3.185	.286
-3	6	0	68.459	.939
-3	0	6	14.016	.044
-3	-1	7	7.697	.033
-3	-2	8	12.442	.035
-3	-3	9	1.183	.043
-3	-4	10	43.730	.121
-3	-5	11	6.986	.036
-4	9	-1	12.489	.037

-4	8	0	26.082	.052	-5	-2	15	11.375	.036
-4	0	8	37.364	.234	-6	9	6	8.127	.036
-4	-1	9	21.130	.083	-6	8	7	12.960	.037
-4	-2	10	37.100	.150	-6	-1	16	9.614	.037
-4	-3	11	1.952	.039	0	8	-2	.740	.064
-4	-4	12	.987	.047	0	6	0	56.535	.299
-5	0	10	31.016	.053	0	4	2	37.106	.243
-5	-1	11	12.985	.037	0	0	6	17.348	.059
-5	-2	12	4.388	.129	0	-2	8	24.370	.174
-5	-3	13	6.536	.036	0	-4	10	60.944	.290
-6	0	12	19.974	.056	0	-6	12	20.113	.056
-6	-1	13	5.535	.038	-1	8	0	21.835	.037
-7	0	14	6.098	.055	-1	7	1	5.934	.037
0	7	-4	8.062	.051	-1	6	2	4.963	.036
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0	3	0	112.546	.951	-1	4	4	48.889	.184
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0	-3	6	13.687	.044	-1	-1	9	42.391	.173
0	-5	8	9.620	.051	-1	-2	10	59.338	.190
0	-7	10	40.673	.055	-1	-3	11	5.482	.035
-1	8	-3	10.283	.036	-1	-4	12	4.820	.110
-1	7	-2	16.284	.081	-1	-5	13	12.733	.036
-1	6	-1	15.466	.036	-1	-6	14	17.140	.035
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-1	3	2	20.633	.095	-2	7	3	13.905	.037
-1	-1	6	86.480	.749	-2	6	4	39.258	.158
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-1	-4	9	21.381	.090	-2	-1	11	10.289	.341
-1	-5	10	28.745	.106	-2	-2	12	6.807	.035
-1	-6	11	4.802	.037	-2	-3	13	8.437	.037
-2	9	-2	5.902	.035	-2	-4	14	29.297	.087
-2	8	-1	13.669	.039	-2	-5	15	11.512	.036
-2	7	0	27.594	.037	-3	9	3	2.263	.041
-2	6	1	12.321	.035	-3	8	4	33.033	.097
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-2	4	3	35.317	.359	-3	6	6	12.643	.036
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-2	-2	9	27.817	.131	-3	-1	13	5.744	.036
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-2	-4	11	9.945	.037	-3	-3	15	1.093	.046
-2	-5	12	4.223	.038	-3	-4	16	5.108	.125
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-3	5	4	58.110	.197	-4	-1	15	17.321	.037
-3	-1	10	59.053	.201	-4	-2	16	19.102	.038
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-2	6	7	11.597	.036
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-3	-1	16	18.815	.037
-3	-2	17	7.294	.037
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-4	8	9	12.100	.037
-4	-1	18	6.615	.038
-4	-2	19	8.711	.035
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-1	-3	20	32.367	.098
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-2	-1	20	28.687	.037
-2	-2	21	16.674	.036

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0	-2	20	28.521	.053
0	-4	22	9.422	.048
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-1	-1	21	19.830	.037
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-2	-1	23	5.218	.035
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0	0	24	4.159	.087

Data set 4

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-1	4	-2	32.057	.201
-1	3	-1	18.980	.173
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-1	0	2	48.013	.555
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-1	-3	5	7.775	.306
-1	-4	6	53.325	.243
-1	-5	7	14.460	.333
-1	-6	8	18.798	.351
-1	-7	9	9.464	.512
-2	8	-4	32.922	.326
-2	7	-3	14.393	.332
-2	6	-2	12.818	.306
-2	5	-1	12.384	.248
-2	4	0	54.583	.267
-2	0	4	87.247	1.664
-2	-1	5	15.608	.195
-2	-2	6	71.019	.211
-2	-3	7	10.561	.302
-2	-4	8	18.560	.307
-2	-5	9	13.304	.371
-2	-6	10	16.715	.375
-3	7	-1	4.581	.620
-3	6	0	72.711	.354
-3	0	6	14.193	.302
-3	-1	7	8.112	.287
-3	-2	8	12.306	.292
-3	-4	10	44.759	.307
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-4	8	0	27.518	.440
-4	0	8	38.462	.335
-4	-1	9	21.748	.274
-4	-2	10	37.856	.287
-5	0	10	31.075	.403
-5	-1	11	13.445	.360
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-6	-1	13	6.334	.605

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-1	7	-2	16.412	.332	-2	-4	14	29.012	.322
-1	6	-1	15.863	.300	-2	-5	15	11.579	.538
-1	5	0	45.560	.230	-3	8	4	33.848	.319
-1	4	1	9.216	.243	-3	6	6	12.207	.324
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-1	-2	7	12.723	.224	-3	-2	14	41.695	.291
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-1	-4	9	21.830	.280	-4	8	6	27.630	.329
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-4	8	3	13.538	.375	-1	-4	15	17.866	.324
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-5	7	6	35.943	.302	-2	-3	16	29.744	.311
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Data set 5

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-1	-3	5	7.864	.274
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-1	-5	7	14.418	.330
-1	-6	8	18.772	.340
-1	-7	9	9.405	.480
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-2	-2	6	69.885	.439
-2	-3	7	10.600	.294
-2	-4	8	16.184	.310
-2	-5	9	12.888	.372
-2	-6	10	15.952	.388

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-3	-4	10	44.367	.302
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-4	0	8	38.438	.328
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-1	5	3	24.849	.235	0	0	12	53.450	.492
-1	4	4	49.864	.200	0	-2	14	54.179	.332
-1	0	8	44.510	.231	0	-4	16	12.747	.519
-1	-1	9	44.089	.185	-1	8	6	23.626	.338
-1	-2	10	61.987	.212	-1	7	7	6.708	.617
-1	-3	11	5.220	.444	-1	6	8	9.571	.375
-1	-4	12	5.545	.489	-1	0	14	50.211	.320
-1	-5	13	12.905	.361	-1	-1	15	27.181	.253
-1	-6	14	18.308	.587	-1	-2	16	31.329	.271
-2	9	1	7.920	.556	-1	-4	18	6.560	.944
-2	7	3	13.889	.336	-1	-5	19	11.390	.746
-2	6	4	39.734	.257	-2	7	9	13.139	.380
-2	5	5	11.635	.273	-2	0	16	36.444	.367
-2	0	10	62.668	.285	-2	-1	17	6.806	.454
-2	-1	11	9.766	.275	-2	-2	18	7.453	.455
-2	-2	12	6.146	.425	-2	-3	19	8.177	.787
-2	-3	13	8.775	.377	-3	8	10	18.618	.357
-2	-4	14	29.810	.313	-3	0	18	40.651	.418
-2	-5	15	12.094	.686	-3	-2	20	19.322	.593
-3	8	4	33.281	.317	-4	0	20	35.013	.471
-3	6	6	12.540	.308	-4	-1	21	14.263	.690
-3	0	12	38.575	.336	0	7	8	27.528	.464
-3	-1	13	6.040	.440	0	-1	16	30.067	.354
-3	-2	14	40.562	.287	0	-3	18	41.864	.414
-4	9	5	12.053	.440	0	-5	20	16.711	.967
-4	8	6	27.489	.318	-1	8	9	9.669	.472
-4	0	14	25.090	.398	-1	7	10	34.537	.318
-4	-1	15	16.976	.343	-1	-1	18	8.694	.402
-4	-2	16	19.324	.341	-1	-2	19	6.768	.512
-5	9	7	12.518	.411	-1	-3	20	32.618	.559
-5	0	16	27.964	.452	-1	-4	21	15.464	.653
-5	-1	17	10.279	.479	-2	8	11	12.009	.446
0	7	2	27.294	.434	-2	-1	20	29.070	.311
0	5	4	52.201	.347	-2	-2	21	16.760	.626
0	-1	10	80.930	.296	0	0	18	50.789	.654
0	-3	12	38.596	.340	0	-2	20	29.410	.418
0	-5	14	36.801	.428	0	-4	22	8.987	1.255
-1	8	3	9.981	.447	-1	0	20	36.634	.416
-1	7	4	21.506	.320	-1	-1	21	19.537	.339
-1	6	5	14.739	.306	0	-1	22	5.561	.681
-1	5	6	52.409	.238	0	-3	24	5.259	1.442
-1	-1	12	9.169	.293	-1	-1	24	33.608	.583
-1	-2	13	8.914	.316	0	0	24	7.638	1.038
-1	-3	14	33.066	.271					
-1	-4	15	17.689	.331					
-1	-5	16	23.192	.609					
-2	8	5	13.255	.385					
-2	7	6	36.039	.291					
-2	6	7	12.183	.316					
-2	-1	14	48.158	.245					
-2	-2	15	20.964	.298					
-2	-3	16	29.237	.310					
-2	-4	17	8.344	.884					
-3	9	6	7.678	.566					
-3	8	7	7.527	.527					
-3	7	8	28.015	.303					

Figure legends

Fig. 1. Δr for $\alpha\text{-Al}_2\text{O}_3$ in the (01 $\bar{1}$ 0) plane through two Al and three O atoms with two O atoms deviating from the plane by 0.11 Å shown in italics. Extinction corrections were evaluated by minimizing differences between equivalent reflection intensities. (a) data set 1, (b) data set 3, (c) data set 4, (d) data set 5. Map borders 5.1 by 5.9 Å. Contour interval 0.1 eÅ⁻³, positive, negative contours - solid, short dashes respectively.

Fig. 2. Δr for $\alpha\text{-Al}_2\text{O}_3$ in the plane as Fig. 1. Extinction corrections were determined as part of the least squares structure refinement. (a) data set 1, (b) data set 3, (c) data set 4, (d) data set 5. Map borders and contour interval as for Fig. 1.

Fig 3. Δr for $\alpha\text{-Al}_2\text{O}_3$ in the (01 $\bar{1}$ 0) plane for data set 3 scaled on data set 2. Map borders 5.1 by 5.1 Å. Map borders and contour interval as for Fig. 1.

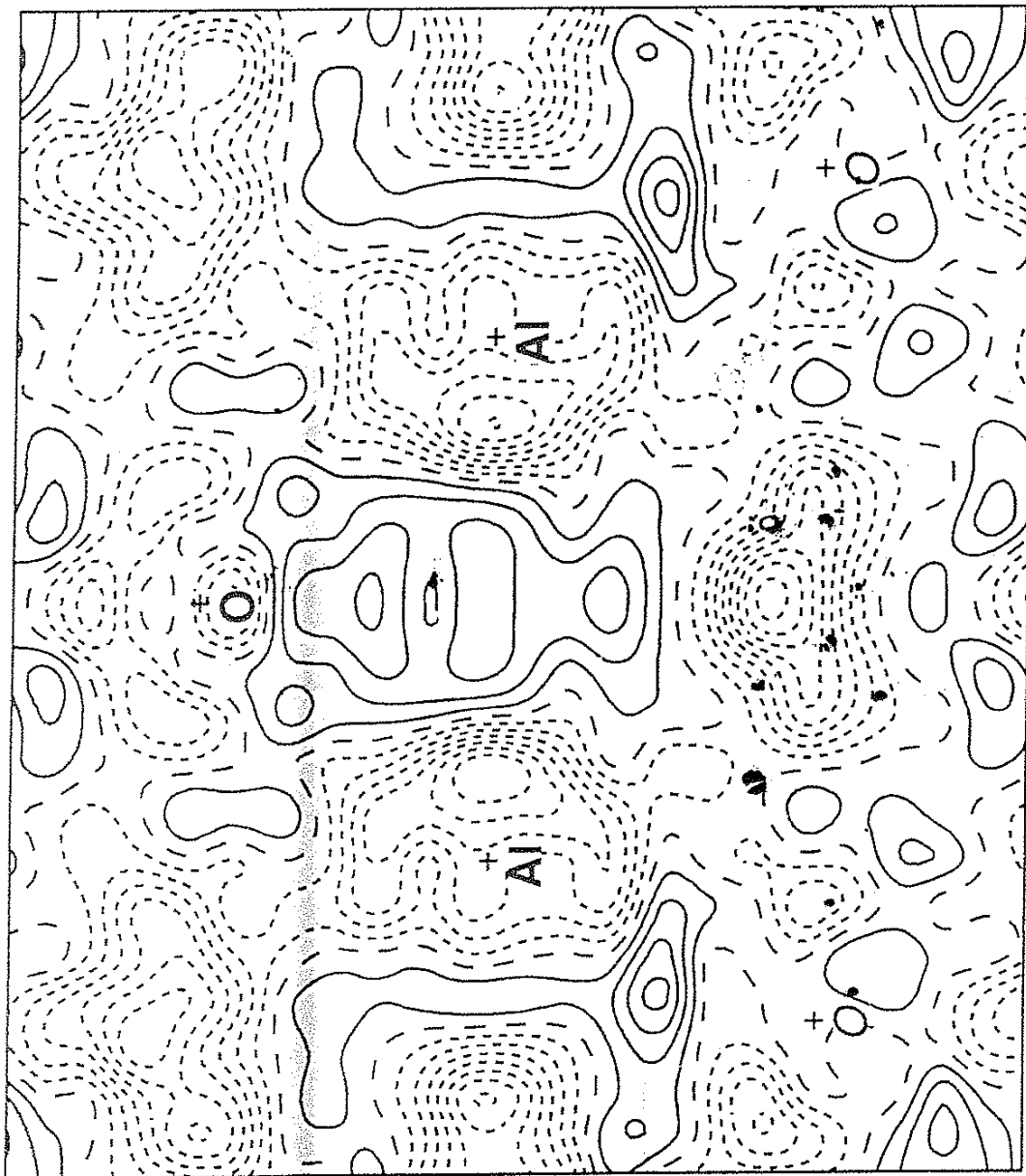


Fig. 1(a)

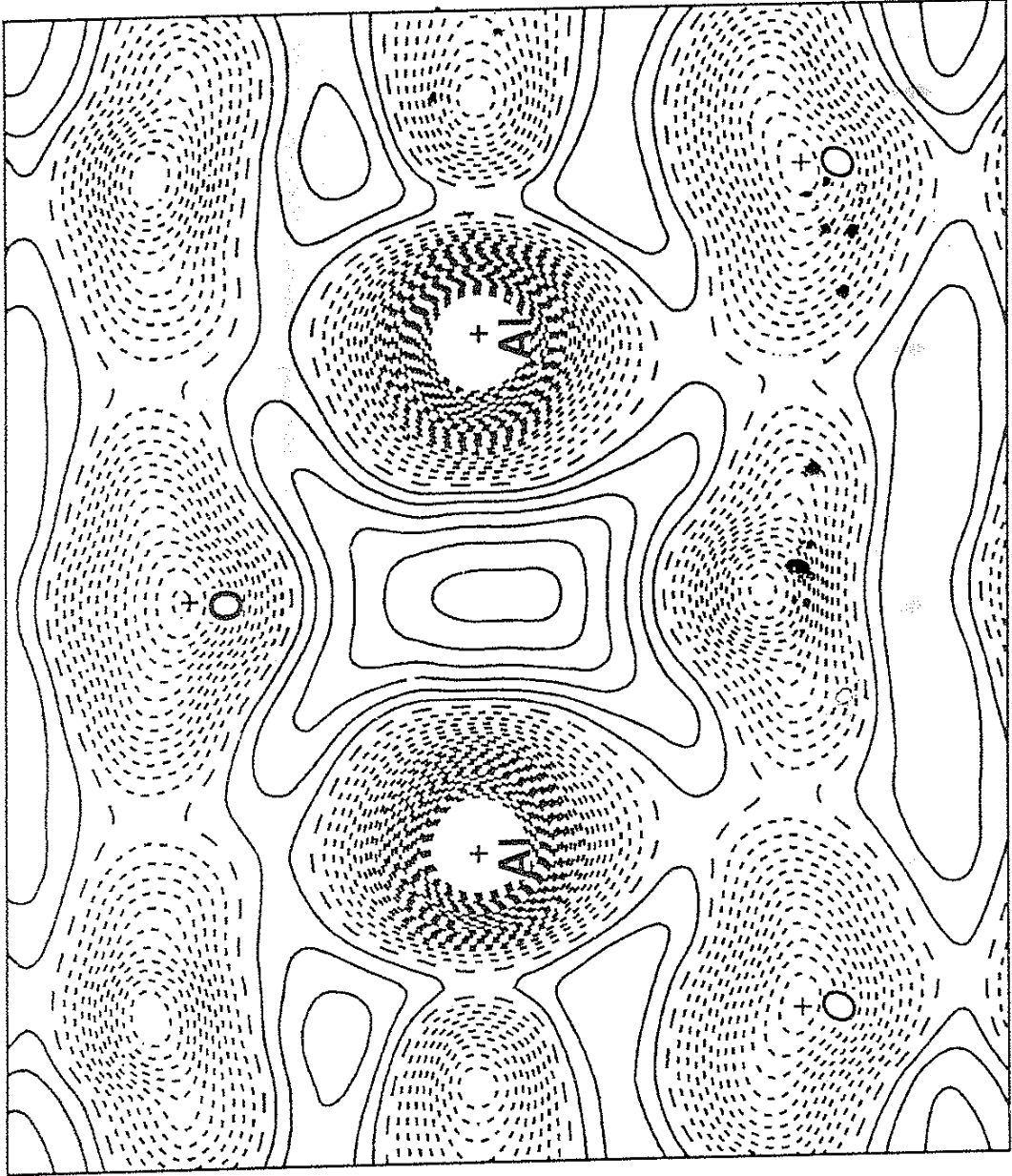


Fig. 1(b)

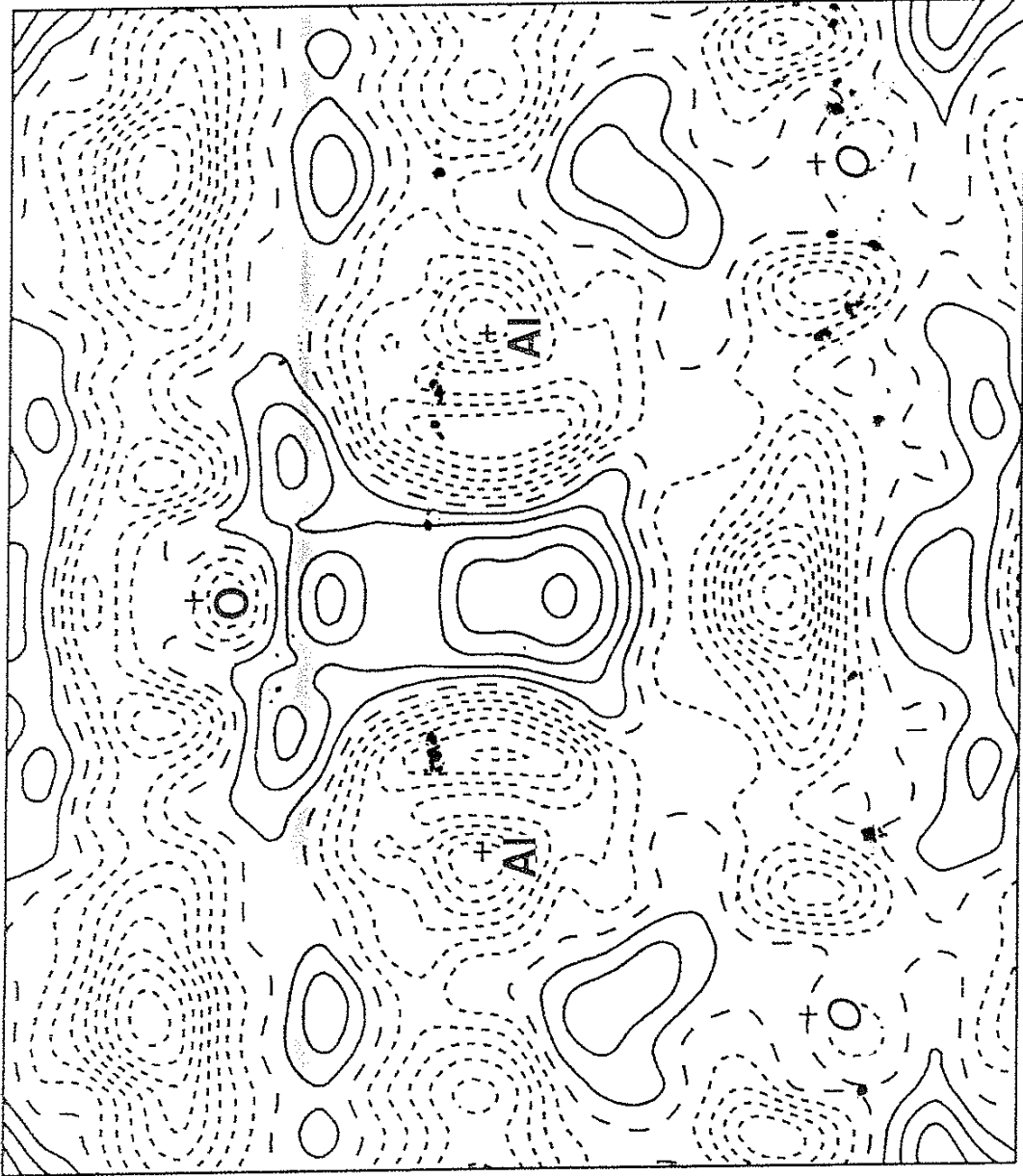


Fig. 1(c)

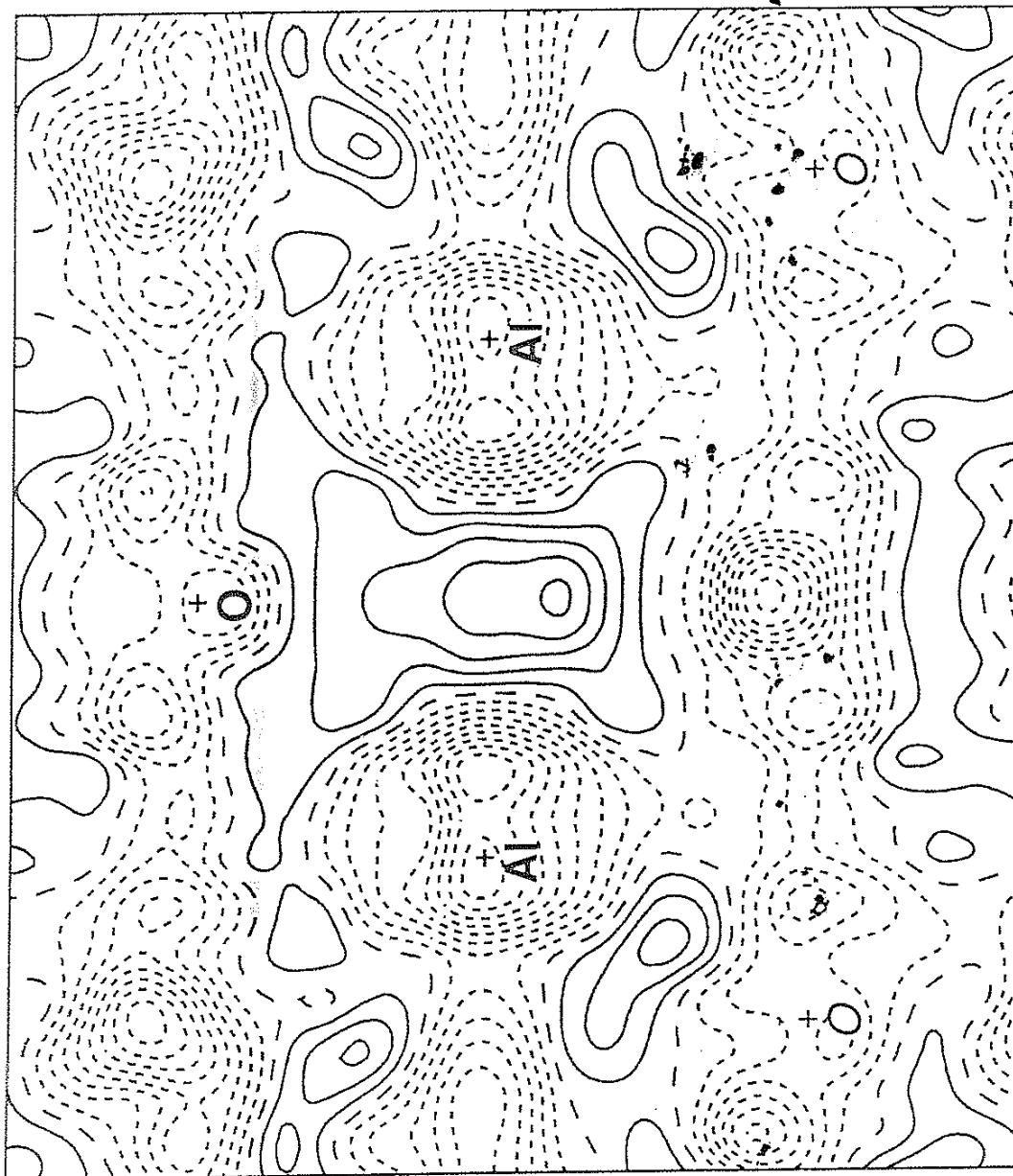


Fig. 1(d)

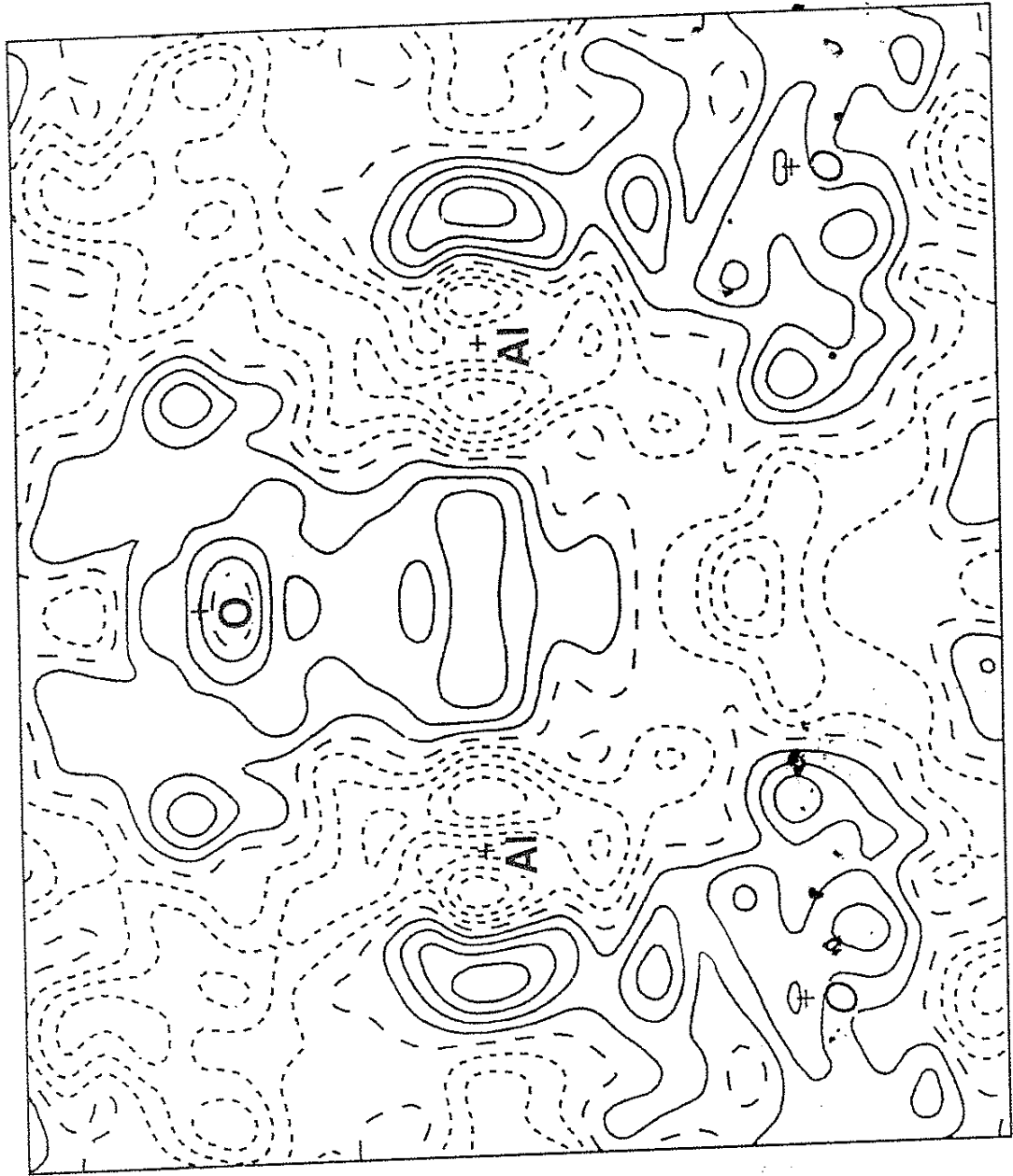


Fig. 2(a)

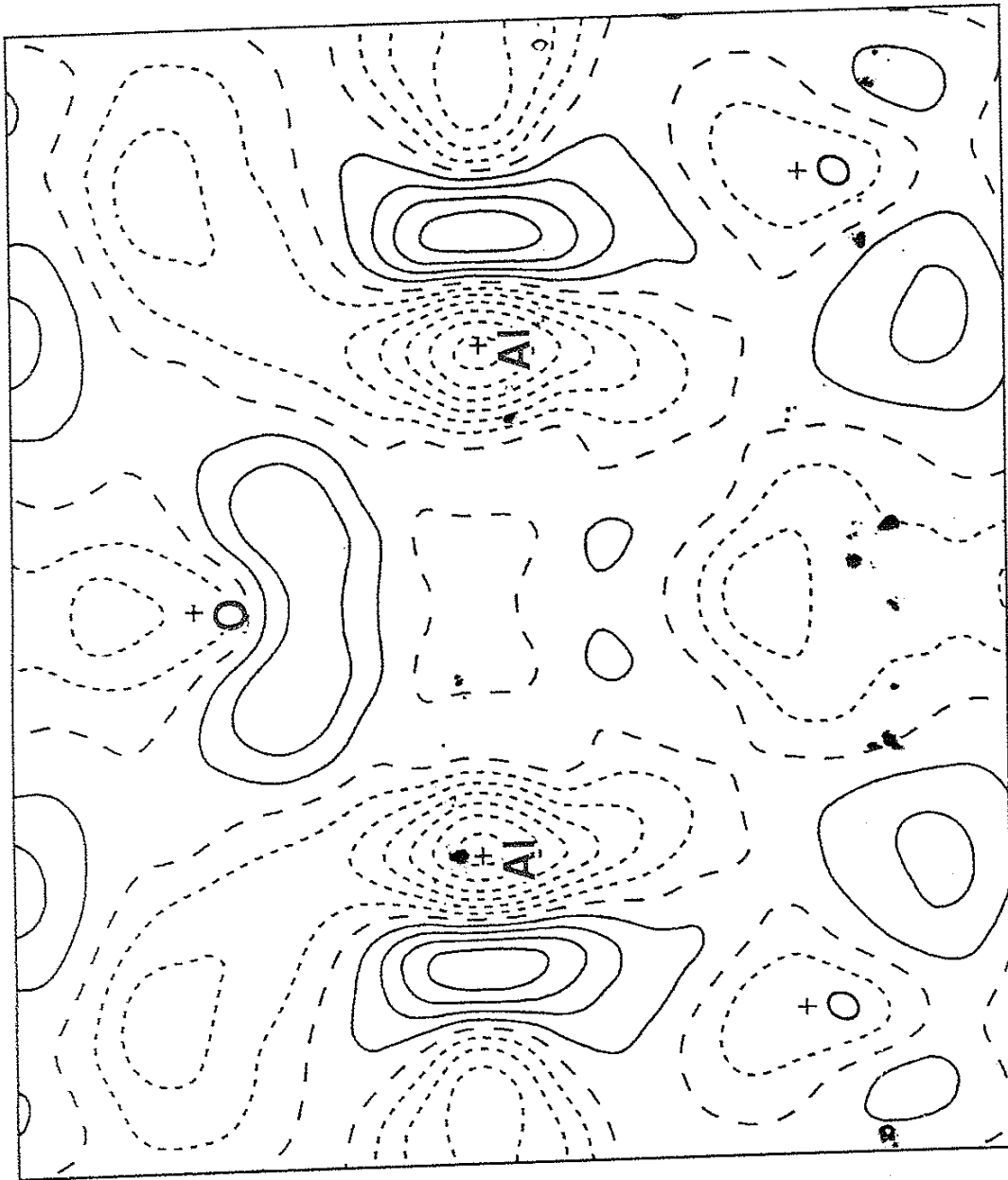


Fig. 2(b)

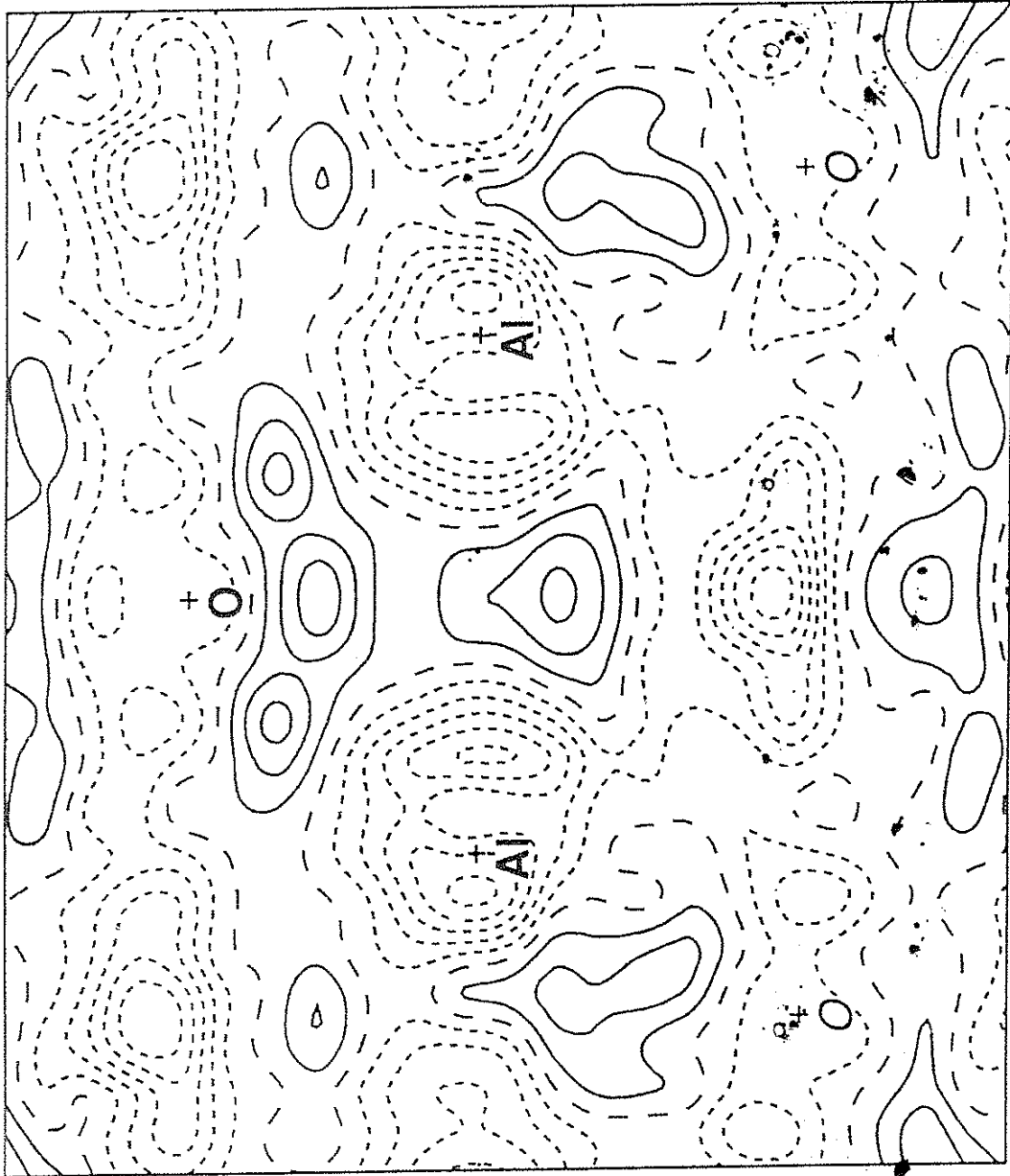


Fig. 2(c)

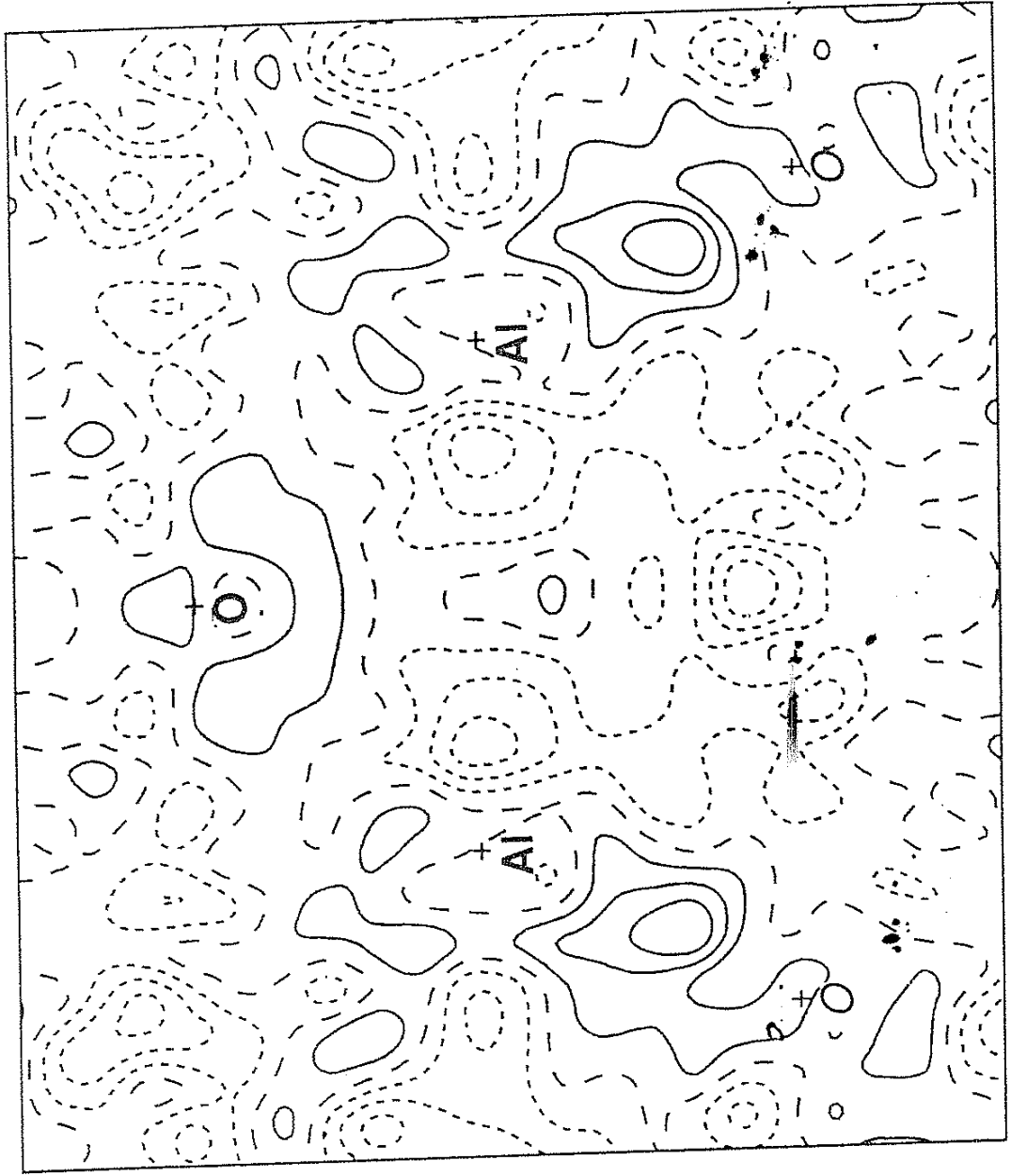


Fig. 2(d)

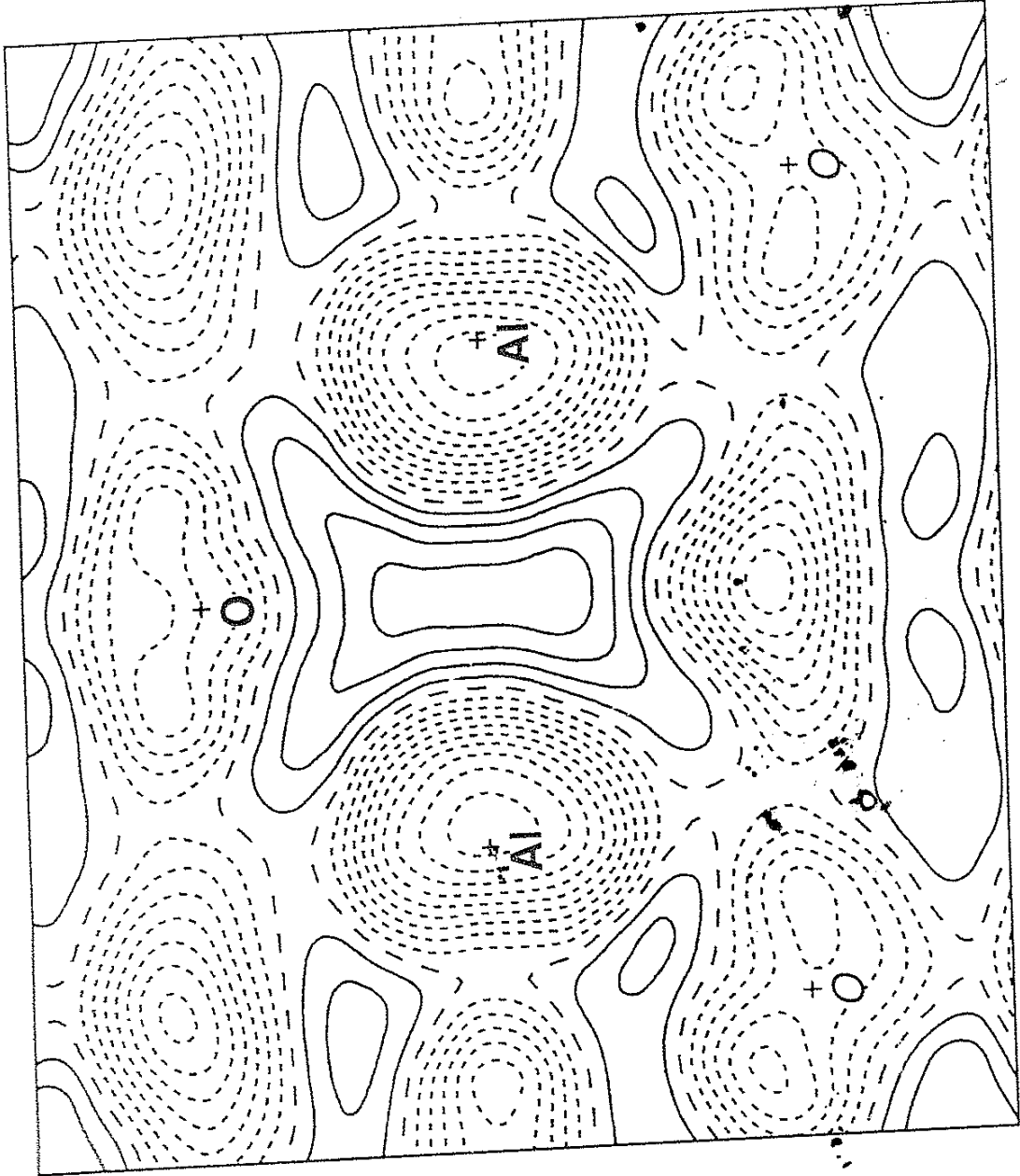


Fig. 3