

V

Taylor Series Approximation to Solve Neutrosophic Multi-objective Programming Problem

Ibrahim M. Hezam¹ • Mohamed Abdel-Baset^{2*} • Florentin Smarandache³

¹ Department of computer, Faculty of Education, Ibb University, Ibb city, Yemen.
E-mail: Ibrahim.math@gmail.com

² Department of Operations Research, Faculty of Computers and Informatics, Zagazig University, Sharqiyah,
Egypt. E-mail: analyst_mohamed@yahoo.com

³ Math & Science Department, University of New Mexico, Gallup, NM 87301, USA.
E-mail: smarand@unm.edu

Abstract

In this chapter, Taylor series is used to solve neutrosophic multi-objective programming problem (NMOPP). In the proposed approach, the truth membership, indeterminacy membership, falsity membership functions associated with each objective of multi-objective programming problems are transformed into a single objective linear programming problem by using a first order Taylor polynomial series. Finally, to illustrate the efficiency of the proposed method, a numerical experiment for supplier selection is given as an application of Taylor series method for solving neutrosophic multi-objective programming problem.

Keywords

Taylor series; Neutrosophic optimization; Multi-objective programming problem.

1 Introduction

In 1995, Smarandache [13], starting from philosophy (when [8] fretted to distinguish between absolute truth and relative truth or between absolute falsehood and relative falsehood in logics, and respectively between absolute membership and relative membership or absolute non-membership and relative non-membership in set theory) [12], began to use the non-standard analysis. Also, inspired from the sport games (winning, defeating, or tie scores), from votes (pro, contra, null/black votes), from positive/negative/zero numbers, from yes/no/NA,

from decision making and control theory (making a decision, not making one, or hesitating), from accepted/rejected/pending, etc., and guided by the fact that the law of excluded middle did not work any longer in the modern logics [12], Smarandache combined the non-standard analysis with a tri-component logic/set/probability theory and with philosophy. How to deal with all of them at once, is it possible to unify them? [12].

Netrosophic theory means Neutrosophy applied in many fields in order to solve problems related to indeterminacy. Neutrosophy is a new branch of philosophy that studies the origin, nature, and scope of neutralities, as well as their interactions with different ideational spectra. This theory considers every entity $\langle A \rangle$ together with its opposite or negation $\langle \text{anti}A \rangle$ and with their spectrum of neutralities $\langle \text{neut}A \rangle$ in between them (i.e. entities supporting neither $\langle A \rangle$ nor $\langle \text{anti}A \rangle$). The $\langle \text{neut}A \rangle$ and $\langle \text{anti}A \rangle$ ideas together are referred to as $\langle \text{non}A \rangle$.

Neutrosophy is a generalization of Hegel's dialectics (the last one is based on $\langle A \rangle$ and $\langle \text{anti}A \rangle$ only). According to this theory every entity $\langle A \rangle$ tends to be neutralized and balanced by $\langle \text{anti}A \rangle$ and $\langle \text{non}A \rangle$ entities - as a state of equilibrium. In a classical way $\langle A \rangle$, $\langle \text{neut}A \rangle$, $\langle \text{anti}A \rangle$ are disjoint two by two. But, since in many cases the borders between notions are vague, imprecise, Sorites, it is possible that $\langle A \rangle$, $\langle \text{neut}A \rangle$, $\langle \text{anti}A \rangle$ (and $\langle \text{non}A \rangle$ of course) have common parts two by two, or even all three of them as well. Hence, in one hand, the Neutrosophic Theory is based on the triad $\langle A \rangle$, $\langle \text{neut}A \rangle$, and $\langle \text{anti}A \rangle$. In the other hand, Neutrosophic Theory studies the indeterminacy, labeled as I , with $I_n = I$ for $n \geq 1$, and $mI + nI = (m+n)I$, in neutrosophic structures developed in algebra, geometry, topology etc.

The most developed fields of Netrosophic theory are Neutrosophic Set, Neutrosophic Logic, Neutrosophic Probability, and Neutrosophic Statistics - that started in 1995, and recently Neutrosophic Precalculus and Neutrosophic Calculus, together with their applications in practice. Neutrosophic Set and Neutrosophic Logic are generalizations of the fuzzy set and respectively fuzzy logic (especially of intuitionistic fuzzy set and respectively intuitionistic fuzzy logic). In neutrosophic logic a proposition has a degree of truth (T), a degree of indeterminacy (I), and a degree of falsity (F), where T, I, F are standard or non-standard subsets of $]0, 1^+[$.

Multi-objective linear programming problem (MOLPP) a prominent tool for solving many real decision-making problems like game theory, inventory problems, agriculture based management systems, financial and corporate planning, production planning, marketing and media selection, university planning and student admission, health care and hospital planning, air force maintenance units, bank branches etc.

Our objective in this chapter is to propose an algorithm to the solution of neutrosophic multi-objective programming problem (NMOPP) with the help of the first order Taylor's theorem. Thus, neutrosophic multi-objective linear programming problem is reduced to an equivalent multi-objective linear programming problem. An algorithm is proposed to determine a global optimum to the problem in a finite number of steps. The feasible region is a bounded set. In the proposed approach, we have attempted to reduce computational complexity in the solution of (NMOPP). The proposed algorithm is applied to supplier selection problem.

The rest of this chapter is organized as follows. Section 2 gives brief some preliminaries. Section 3 describes the formation of the problem. Section 4 presents the implementation and validation of the algorithm with practical application. Finally, section 6 presents the conclusion and proposals for future work.

2 Some preliminaries

Definition 1. [1] A triangular fuzzy number \tilde{J} is a continuous fuzzy subset from the real line R whose triangular membership function $\mu_{\tilde{J}}(J)$ is defined by a continuous mapping from R to the closed interval $[0,1]$, where

- (6) $\mu_{\tilde{J}}(J) = 0$ for all $J \in (-\infty, a_1]$,
- (7) $\mu_{\tilde{J}}(J)$ is strictly increasing on $J \in [a_1, m]$,
- (8) $\mu_{\tilde{J}}(J) = 1$ for $J = m$,
- (9) $\mu_{\tilde{J}}(J)$ is strictly decreasing on $J \in [m, a_2]$,
- (10) $\mu_{\tilde{J}}(J) = 0$ for all $J \in [a_2, +\infty)$.

This will be elicited by:

$$\mu_{\tilde{J}}(J) = \begin{cases} \frac{J - a_1}{m - a_1}, & a_1 \leq J \leq m, \\ \frac{a_2 - J}{a_2 - m}, & m \leq J \leq a_2, \\ 0, & otherwise. \end{cases} \quad (18)$$

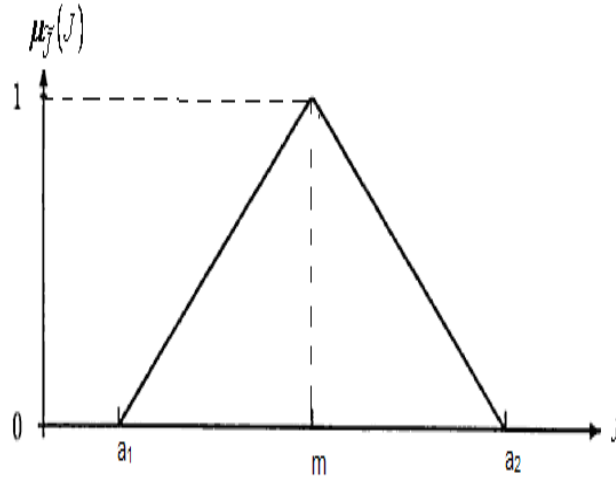


Fig. 3: Membership Function of Fuzzy Number J .

where m is a given value a_1 & a_2 denoting the lower and upper bounds. Sometimes, it is more convenient to use the notation explicitly highlighting the membership function parameters. In this case, we obtain

$$\mu(J; a_1, m, a_2) = \text{Max} \left\{ \text{Min} \left[\frac{J - a_1}{m - a_1}, \frac{a_2 - J}{a_2 - m} \right], 0 \right\} \quad (19)$$

In what follows, the definition of the α -level set or α -cut of the fuzzy number \tilde{J} is introduced.

Definition 2. [1] Let $X = \{x_1, x_2, \dots, x_n\}$ be a fixed non-empty universe. An intuitionistic fuzzy set IFS A in X is defined as

$$A = \left\{ \langle x, \mu_A(x), \nu_A(x) \rangle \mid x \in X \right\} \quad (20)$$

which is characterized by a membership function $\mu_A : X \rightarrow [0,1]$ and a non-membership function $\nu_A : X \rightarrow [0,1]$ with the condition $0 \leq \mu_A(x) + \nu_A(x) \leq 1$ for all $x \in X$ where μ_A and ν_A represent, respectively, the degree of membership and non-membership of the element x to the set A . In addition, for each IFS A in X , $\pi_A(x) = 1 - \mu_A(x) - \nu_A(x)$ for all $x \in X$ is called the degree of hesitation of the element x to the set A . Especially, if $\pi_A(x) = 0$, then the IFS A is degraded to a fuzzy set.

Definition 3. [4] The α -level set of the fuzzy parameters \tilde{J} in problem (1) is defined as the ordinary set $L_\alpha(\tilde{J})$ for which the degree of membership function exceeds the level, α , $\alpha \in [0,1]$, where:

$$L_\alpha(\tilde{J}) = \{J \in R \mid \mu_{\tilde{J}}(J) \geq \alpha\} \quad (21)$$

For certain values α_j^* to be in the unit interval.

Definition 4. [10] Let X be a space of points (objects) and $x \in X$. A neutrosophic set A in X is defined by a truth-membership function $\mu_A(x)$, an indeterminacy-membership function $\sigma_A(x)$ and a falsity-membership function $\nu_A(x)$. It has been shown in figure 2. $\mu_A(x)$, $\sigma_A(x)$ and $\nu_A(x)$ are real standard or real nonstandard subsets of $]0-, 1+[$. That is $T_A(x): X \rightarrow]0-, 1+[$, $I_A(x): X \rightarrow]0-, 1+[$ and $F_A(x): X \rightarrow]0-, 1+[$. There is not restriction on the sum of $\mu_A(x)$, $\sigma_A(x)$ and $\nu_A(x)$, so $0- \leq \sup T_A(x) \leq \sup I_A(x) \leq \sup F_A(x) \leq 3+$.

In the following, we adopt the notations $\mu(x)$, $\sigma_A(x)$ and $\nu_A(x)$ instead of $T_A(x)$, $I_A(x)$ and $F_A(x)$, respectively. Also, we write SVN numbers instead of single valued neutrosophic numbers.

Definition 5. [10] Let X be a universe of discourse. A single valued neutrosophic set A over X is an object having the form

$$A = \{ \langle x, \mu_A(x), \sigma_A(x), \nu_A(x) \rangle : x \in X \},$$

where $\mu_A(x): X \rightarrow [0,1]$, $\sigma_A(x): X \rightarrow [0,1]$ and $\nu_A(x): X \rightarrow [0,1]$ with $0 \leq \mu_A(x) + \sigma_A(x) + \nu_A(x) \leq 3$ for all $x \in X$. The intervals $\mu(x)$, $\sigma_A(x)$ and $\nu_A(x)$ denote the truth-membership degree, the indeterminacy-membership degree and the falsity membership degree of x to A , respectively.

For convenience, a SVN number is denoted by $A = (a, b, c)$, where $a, b, c \in [0,1]$ and $a + b + c \leq 3$.

Definition 6 Let \tilde{J} be a neutrosophic triangular number in the set of real numbers R , then its truth-membership function is defined as

$$T_{\tilde{J}}(J) = \begin{cases} \frac{J - a_1}{a_2 - a_1}, & a_1 \leq J \leq a_2, \\ \frac{a_2 - J}{a_3 - a_2}, & a_2 \leq J \leq a_3, \\ 0, & \text{otherwise.} \end{cases} \quad (22)$$

its indeterminacy-membership function is defined as

$$I_{\tilde{j}}(J) = \begin{cases} \frac{J-b_1}{b_2-b_1}, & b_1 \leq J \leq b_2, \\ \frac{b_2-J}{b_3-b_2}, & b_2 \leq J \leq b_3, \\ 0, & \text{otherwise.} \end{cases} \quad (23)$$

and its falsity-membership function is defined as

$$F_{\tilde{j}}(J) = \begin{cases} \frac{J-c_1}{c_2-c_1}, & c_1 \leq J \leq c_2, \\ \frac{c_2-J}{c_3-c_2}, & c_2 \leq J \leq c_3, \\ 1, & \text{otherwise.} \end{cases} \quad (24)$$

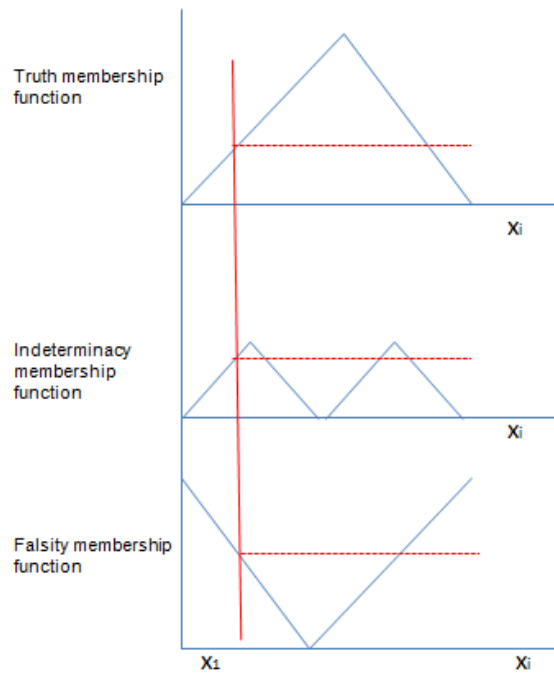


Fig. 4: Neutrosophication process [11]

3 Formation of The Problem

The multi-objective linear programming problem and the multi- objective neutrosophic linear programming problem are described in this section.

A. Multi-objective Programming Problem (MOPP)

In this chapter, the general mathematical model of the MOPP is as follows [6]:

$$\min/\max \left[z_1(x_1, \dots, x_n), z_2(x_1, \dots, x_n), \dots, z_p(x_1, \dots, x_n) \right] \quad (8)$$

subject to $x \in S, x \geq 0$

$$S = \left\{ x \in R^n \left| AX \begin{pmatrix} \leq \\ = \\ \geq \end{pmatrix} b, X \geq 0. \right. \right\} \quad (25)$$

B. Neutrosophic Multi-objective Programming Problem (NMOPP)

If an imprecise aspiration level is introduced to each of the objectives of MOPP, then these neutrosophic objectives are termed as neutrosophic goals.

Let $z_i \in [z_i^L, z_i^U]$ denote the imprecise lower and upper bounds respectively for the i^{th} neutrosophic objective function.

For maximizing objective function, the truth membership, indeterminacy membership, falsity membership functions can be expressed as follows:

$$\mu_i^I(z_i) = \begin{cases} 1, & \text{if } z_i \geq z_i^U, \\ \frac{z_i - z_i^L}{z_i^U - z_i^L}, & \text{if } z_i^L \leq z_i \leq z_i^U, \\ 0, & \text{if } z_i \leq z_i^L \end{cases} \quad (26)$$

$$\sigma_i^I(z_i) = \begin{cases} 1, & \text{if } z_i \geq z_i^U, \\ \frac{z_i - z_i^L}{z_i^U - z_i^L}, & \text{if } z_i^L \leq z_i \leq z_i^U, \\ 0, & \text{if } z_i \leq z_i^L \end{cases} \quad (27)$$

$$\nu_i^I(z_i) = \begin{cases} 0, & \text{if } z_i \geq z_i^U, \\ \frac{z_i - z_i^L}{z_i^U - z_i^L}, & \text{if } z_i^L \leq z_i \leq z_i^U, \\ 1, & \text{if } z_i \leq z_i^L \end{cases} \quad (28)$$

For minimizing objective function, the truth membership, indeterminacy membership, falsity membership functions can be expressed as follows:

$$\mu_i^I(z_i) = \begin{cases} 1, & \text{if } z_i \leq z_i^L, \\ \frac{z_i^U - z_i}{z_i^U - z_i^L}, & \text{if } z_i^L \leq z_i \leq z_i^U, \\ 0, & \text{if } z_i \geq z_i^U \end{cases} \quad (29)$$

$$\sigma_i^I(z_i) = \begin{cases} 1, & \text{if } z_i \leq z_i^L, \\ \frac{z_i^U - z_i}{z_i^U - z_i^L}, & \text{if } z_i^L \leq z_i \leq z_i^U, \\ 0, & \text{if } z_i \geq z_i^U \end{cases} \quad (30)$$

$$\nu_i^I(z_i) = \begin{cases} 0, & \text{if } z_i \leq z_i^L, \\ \frac{z_i^U - z_i}{z_i^U - z_i^L}, & \text{if } z_i^L \leq z_i \leq z_i^U, \\ 1, & \text{if } z_i \geq z_i^U \end{cases} \quad (31)$$

4 Algorithm for Neutrosophic Multi-Objective Programming Problem

The computational procedure and proposed algorithm of presented model is given as follows:

Step 1. Determine $x_i^* = (x_{i1}^*, x_{i2}^*, \dots, x_{in}^*)$ that is used to maximize or minimize the i^{th} truth membership function $\mu_i^I(X)$, the indeterminacy membership $\sigma_i^I(X)$, and the falsity membership functions $\nu_i^I(X)$. $i=1,2,\dots,p$ and n is the number of variables.

Step 2. Transform the truth membership, indeterminacy membership, falsity membership functions by using first-order Taylor polynomial series

$$\mu_i^I(x) \cong \mu_i^I(x_i^*) + \sum_{j=1}^n (x_j - x_{ij}^*) \frac{\partial \mu_i^I(x_i^*)}{\partial x_j} \quad (32)$$

$$\sigma_i^I(x) \cong \sigma_i^I(x_i^*) + \sum_{j=1}^n (x_j - x_{ij}^*) \frac{\partial \sigma_i^I(x_i^*)}{\partial x_j}$$

(33)

$$v_i^I(x) \equiv v_i^I(x_i^*) + \sum_{j=1}^n (x_j - x_{ij}^*) \frac{\partial v_i^I(x_i^*)}{\partial x_j} \quad (34)$$

Step 3. Find satisfactory $x_i^* = (x_{i1}^*, x_{i2}^*, \dots, x_{in}^*)$ by solving the reduced problem to a single objective for the truth membership, indeterminacy membership, falsity membership functions respectively.

$$\begin{aligned} p(x) &= \sum_{i=1}^p \left[\mu_i^I(x_i^*) + \sum_{j=1}^n (x_j - x_{ij}^*) \frac{\partial \mu_i^I(x_i^*)}{\partial x_j} \right] \\ q(x) &= \sum_{i=1}^p \left[\sigma_i^I(x_i^*) + \sum_{j=1}^n (x_j - x_{ij}^*) \frac{\partial \sigma_i^I(x_i^*)}{\partial x_j} \right] \\ h(x) &= \sum_{i=1}^p \left[v_i^I(x_i^*) + \sum_{j=1}^n (x_j - x_{ij}^*) \frac{\partial v_i^I(x_i^*)}{\partial x_j} \right] \end{aligned} \quad (35)$$

Thus neutrosophic multiobjective linear programming problem is converted into a new mathematical model and is given below:

Maximize or Minimize $p(x)$

Maximize or Minimize $q(x)$

Maximize or Minimize $h(x)$,

where $\mu_i^I(X)$, $\sigma_i^I(X)$ and $v_i^I(X)$ calculate using equations (10), (11), and (12) or equations (13), (14), and (15) according to type functions maximum or minimum respectively.

4.1 Illustrative Example

A multi-criteria supplier selection is selected from [2]. For supplying a new product to a market assume that three suppliers should be managed. The purchasing criteria are net price, quality and service. The capacity constraints of suppliers are also considered.

It is assumed that the input data from suppliers' performance on these criteria are not known precisely. The neutrosophic values of their cost, quality and service level are presented in Table 1.

The multi-objective linear formulation of numerical example is presented as $\min z_1, \max z_2, z_3$:

$$\begin{aligned}
 \min z_1 &= 5x_1 + 7x_2 + 4x_3, \\
 \max z_2 &= 0.80x_1 + 0.90x_2 + 0.85x_3, \\
 \max z_3 &= 0.90x_1 + 0.80x_2 + 0.85x_3, \\
 s.t.: \\
 x_1 + x_2 + x_3 &= 800, \\
 x_1 &\leq 400, \\
 x_2 &\leq 450, \\
 x_3 &\leq 450, \\
 x_i &\geq 0, \quad i = 1, 2, 3.
 \end{aligned}$$

Table 1: Suppliers quantitative information

	Z1 Cost	Z2Quality (%)	Z3 Service (%)	Capacity
Supplier 1	5	0.80	0.90	400
Supplier 2	7	0.90	0.80	450
Supplier 3	4	0.85	0.85	450

The truth membership, indeterminacy membership, falsity membership functions were considered to be neutrosophic triangular. When they depend on three scalar parameters (a1, m, a2). z_1 depends on neutrosophic aspiration levels (3550,4225,4900), when z_2 depends on neutrosophic aspiration levels (660,681.5,702.5), and z_3 depends on neutrosophic aspiration levels (657.5,678.75,700).

The truth membership functions of the goals are obtained as follows:

$$\mu_1^I(z_1) = \begin{cases} 0, & \text{if } z_1 \leq 3550, \\ \frac{4225 - z_1}{4225 - 3550}, & \text{if } 3550 \leq z_1 \leq 4225, \\ \frac{4900 - z_1}{4900 - 4225}, & \text{if } 4225 \leq z_1 \leq 4900, \\ 0, & \text{if } z_1 \geq 4900 \end{cases}$$

$$\mu_2^I(z_2) = \begin{cases} 0, & \text{if } z_2 \geq 702.5, \\ \frac{z_2 - 681.5}{702.5 - 681.5}, & \text{if } 681.5 \leq z_2 \leq 702.5, \\ \frac{z_2 - 660}{681.5 - 660}, & \text{if } 660 \leq z_2 \leq 681.5, \\ 0, & \text{if } z_2 \leq 660. \end{cases}$$

$$\mu_3^I(z_3) = \begin{cases} 0, & \text{if } z_3 \geq 700, \\ \frac{z_3 - 678.75}{700 - 678.75}, & \text{if } 678.75 \leq z_3 \leq 700, \\ \frac{z_3 - 657.5}{678.75 - 657.5}, & \text{if } 657.5 \leq z_3 \leq 678.75, \\ 0, & \text{if } z_3 \leq 657.5. \end{cases}$$

$$\text{If } \mu_1^I(z_1) = \max\left(\min\left(\frac{4225 - (5x_1 + 7x_2 + 4x_3)}{675}, \frac{4900 - (5x_1 + 7x_2 + 4x_3)}{675}, 0\right)\right)$$

$$\mu_2^I(z_2) = \min\left(\max\left(\frac{(0.8x_1 + 0.9x_2 + 0.85x_3) - 681.5}{21}, \frac{(0.8x_1 + 0.9x_2 + 0.85x_3) - 660}{21}, 1\right)\right)$$

$$\mu_3^I(z_3) = \min\left(\max\left(\frac{(0.9x_1 + 0.8x_2 + 0.85x_3) - 678.75}{21.25}, \frac{(0.9x_1 + 0.8x_2 + 0.85x_3) - 657.5}{21.25}, 1\right)\right)$$

$$\text{Then } \mu_1^{I*}(350, 0, 450), \mu_2^{I*}(0, 450, 350), \mu_3^{I*}(400, 0, 400)$$

The truth membership functions are transformed by using first-order Taylor polynomial series

$$\begin{aligned} \hat{\mu}_1^I(x) &= \mu_1^I(350, 0, 450) + \left[(x_1 - 350) \frac{\partial \mu_1^I(350, 0, 450)}{\partial x_1} \right] \\ &+ \left[(x_2 - 0) \frac{\partial \mu_1^I(350, 0, 450)}{\partial x_2} \right] + \left[(x_3 - 450) \frac{\partial \mu_1^I(350, 0, 450)}{\partial x_3} \right] \end{aligned}$$

$$\hat{\mu}_1^I(x) = -0.00741x_1 - 0.0104x_2 - 0.00593x_3 + 5.2611$$

In the similar way, we get

$$\hat{\mu}_2^I(x) = 0.0381x_1 + 0.0429x_2 + 0.0405x_3 - 33.405$$

$$\hat{\mu}_3^I(x) = 0.042x_1 + 0.037x_2 + 0.0395x_3 - 32.512$$

The $p(x)$ is

$$p(x) = \hat{\mu}_1^I(x) + \hat{\mu}_2^I(x) + \hat{\mu}_3^I(x)$$

$$P(x) = 0.07259x_1 + 0.0695x_2 + 0.0741x_3 - 60.6559$$

s.t.:

$$x_1 + x_2 + x_3 = 800,$$

$$x_1 \leq 400,$$

$$x_2 \leq 450,$$

$$x_3 \leq 450,$$

$$x_i \geq 0, i = 1, 2, 3.$$

The linear programming software LINGO 15.0 is used to solve this problem. The problem is solved and the optimal solution for the truth membership model is obtained is as follows: $(x_1, x_2, x_3) = (350, 0, 450)$ $z_1=3550$, $z_2=662.5$, $z_3=697.5$.

The truth membership values are $\mu_1 = 1$, $\mu_2 = 0.1163$, $\mu_3 = 0.894$. The truth membership function values show that both goals z_1 , z_3 and z_2 are satisfied with 100%, 11.63% and 89.4% respectively for the obtained solution which is $x_1=350$; $x_2=0$, $x_3=450$.

In the similar way, we get $\sigma_i^I(X)$, $q(x)$. Consequently, we get the optimal solution for the indeterminacy membership model is obtained is as follows: $(x_1, x_2, x_3) = (350, 0, 450)$ $z_1=3550$, $z_2=662.5$, $z_3=697.5$ and the indeterminacy membership values are $\mu_1 = 1$, $\mu_2 = 0.1163$, $\mu_3 = 0.894$. The indeterminacy membership function values show that both goals z_1 , z_3 and z_2 are satisfied with 100%, 11.63% and 89.4% respectively for the obtained solution which is $x_1=350$; $x_2=0$, $x_3=450$.

In the similar way, we get $v_i^I(X)$ and $h(x)$ Consequently, we get the optimal solution for the falsity membership model is obtained is as follows: $(x_1, x_2, x_3) = (350, 0, 450)$ $z_1=3550$, $z_2=662.5$, $z_3=697.5$ and the falsity membership values are $\mu_1 = 0$, $\mu_2 = 0.8837$, $\mu_3 = 0.106$. The falsity membership function values show that both goals z_1 , z_3 and z_2 are satisfied with 0%, 88.37% and 10.6% respectively for the obtained solution which is $x_1=350$; $x_2=0$, $x_3=450$.

5 Conclusions and Future Work

In this chapter, we have proposed a solution to Neutrosophic Multiobjective Programming Problem (NMOPP). The truth membership, indeterminacy membership, falsity membership functions associated with each objective of the problem are transformed by using the first order Taylor polynomial series. The neutrosophic multi-objective programming problem is

reduced to an equivalent multiobjective programming problem by the proposed method. The solution obtained from this method is very near to the solution of MOPP. Hence this method gives a more accurate solution as compared with other methods. Therefore, the complexity in solving NMOPP has reduced to easy computation. In the future studies, the proposed algorithm can be solved by metaheuristic algorithms.

Acknowledgement

The authors would like to thank the anonymous referees for their constructive comments and suggestions that have helped a lot to come up with this improved form of the chapter.

References

- [1] El-Hefenawy, N., Metwally, M. A., Ahmed, Z. M., & El-Henawy, I. M. A Review on the Applications of Neutrosophic Sets. *Journal of Computational and Theoretical Nanoscience*, 13(1), (2016), pp. 936-944.
- [2] X. Xu, Y. Lei, and W. Dai. Intuitionistic fuzzy integer programming based on improved particle swarm optimization. In: *Journal of Computer Applications*, vol. 9, 2008, p. 062.
- [3] A. Yücel, and Ali Fuat Güneri. A weighted additive fuzzy programming approach for multi-criteria supplier selection. In: *Expert Systems with Applications*, 38, no. 5 (2011): 6281-6286.
- [4] Mohamed, Mai, et al. "Neutrosophic Integer Programming Problem." *Neutrosophic Sets & Systems* 15 (2017).
- [5] L. Yi, L. Wei-min, and X. Xiao-lai. Intuitionistic Fuzzy Bilevel Programming by Particle Swarm Optimization. In: *Computational Intelligence and Industrial Application*, 2008. PACIIA'08. Pacific-Asia Workshop on, IEEE, 2008, pp. 95–99.
- [6] Abdel-Baset, Mohamed, and Ibrahim M. Hezam. An Improved Flower Pollination Algorithm for Ratios Optimization Problems. In: *Applied Mathematics & Information Sciences Letters An International Journal* , 3, no. 2 (2015): 83-91.
- [7] R. Irene Hepzibah, R and Vidhya. Intuitionistic Fuzzy Multi-Objective Linear Programming Problem(IFMOLPP) using Taylor Series. In: *International Journal of Scientific and Engineering Research (IJSER)*, Vol. 3, Issue 6, June 2014.
- [8] A. Amid, S. H. Ghodsypour, and Ch O'Brien. Fuzzy multiobjective linear model for supplier selection in a supply chain. In: *International Journal of Production Economics* 104, no. 2 (2006): 394-407.
- [9] D. Pintu, Tapan K. R. Multi-objective non-linear programming problem based on Neutrosophic Optimization Technique and its application in Riser Design Problem. In: *Neutrosophic Sets and Systems*, Vol. 9, 2015: 88-95.
- [10] Abdel-Basset, M., Mohamed, M. & Sangaiah, A.K. *J Ambient Intell Human Comput* (2017). DOI: <https://doi.org/10.1007/s12652-017-0548-7>
- [11] S. Aggarwal, Ranjit B., and A. Q. Ansari. Neutrosophic modeling and control. In: *Computer and Communication Technology (ICCCT)*, 2010 International Conference on, pp. 718-723. IEEE, 2010.
- [12] Abdel-Baset, M., Hezam, I. M., & Smarandache, F. Neutrosophic Goal Programming. In: *Neutrosophic Sets & Systems*, vol. 11 (2016).

Editors: *Prof. Florentin Smarandache*
Dr. Mohamed Abdel-Basset
Dr. Yongquan Zhou

[13] Smarandache, F. A Unifying Field in Logics: Neutrosophic Logic. Neutrosophy, Neutrosophic Set, Neutrosophic Probability: Neutrosophic Logic. Neutrosophy, Neutrosophic Set, Neutrosophic Probability. Infinite Study, 2005.