

NIH Public Access

Author Manuscript

J Aging Health. Author manuscript; available in PMC 2009 September 29.

Published in final edited form as:

J Aging Health. 2008 March ; 20(2): 183–197. doi:10.1177/0898264307310448.

Testing Measurement Reliability in Older Populations: Methods for Informed Discrimination in Instrument Selection and

Application

Peter H. Van Ness, PhD, MPH^{1,2}, Virginia R. Towle, M.Phil.¹, and Manisha Juthani-Mehta, MD¹

¹ Department of Internal Medicine, Yale University School of Medicine

² Department of Epidemiology and Public Health, Yale University School of Medicine

Abstract

Objectives—We recommend confidence intervals as measures of precision for reliability coefficients, regression modeling as supplements for such omnibus reliability statistics, and unreliability detection as a goal of reliability testing distinct from reliability inference.

Methods—Illustrative reliability analyses are conducted of measures selected from a study of clinical features associated with urinary tract infection in older nursing home residents.

Results—Standard methods for reliability testing, e.g., kappa coefficients, are often inappropriate for small samples and exact methods or descriptive reliability statistics are viable alternatives.

Discussion—Supplementation of omnibus statistics by loglinear regression modeling is especially appropriate for aging research because it facilitates tests of marginal homogeneity and comparisons of reliability results for relatively young and old subgroups. Latent class regression analysis is useful for older samples because multifactorial health conditions are often measured in multiple ways and assessment of their reliability can be integrated, granting certain assumptions, with validity assessment.

Keywords

reliability testing; confidence intervals; loglinear models; latent class analysis; aging

Introduction

Reliability testing in clinical aging research includes comparisons of results of measurements given on separate occasions test—retest reliability—and measurements obtained by different raters—inter-rater reliability. Such testing seeks to determine whether results obtained by measurement instruments will likely be replicated. Cohen's kappa coefficient is most often used for categorical measurements and the intraclass correlation coefficient for continuous measurement scales (Cohen, 1960; Fisher, 1925). The objectives of this article are three-fold: to recommend that confidence intervals as measures of precision accompany reliability coefficients, to indicate that regression modeling can overcome some limitations of these omnibus reliability statistics, and to distinguish between reliability inference and unreliability

Address Correspondence to: Peter H. Van Ness, Yale University School of Medicine, Department of Internal Medicine, Program On Aging, 300 George Street, Suite 775, New Haven, CT 06511, Phone: (203) 737-1958; Fax: (203) 785-4823, Email: peter.vanness@yale.edu.

detection as goals of reliability testing. Clarity about these three points will allow us to address practical problems that arise in testing reliability in an illustrative study of clinical features associated with urinary tract infection in older nursing home residents.

Confidence Intervals Recommended

Even conscientiously conducted reliability studies that compare results to some minimally acceptable level of reliability often fail to include measures of precision with kappa or intraclass correlation coefficients (Gregson et al., 2000; Wolinsky, Miller, Andresen, Malmstrom, & Miller, 2005). A kappa coefficient of 0.45 alone does not provide sufficient evidence to infer that the tested measurement instrument satisfies the often-cited Landis and Koch level of >0.40 for "moderate" reliability (Landis & Koch, 1977:165). Also required is a 90% confidence interval whose lower bound is greater than 0.4, thereby documenting that a null hypothesis is rejected for a one-sided significance level of 0.05. If a measurement instrument has a kappa value of 0.45 but a confidence interval whose lower bound extends considerably below 0.40, then the next study participant randomly drawn from the same population might be measured with less than moderate reliability.

Minimum acceptable values of an intraclass correlation coefficient have been discussed. Fleiss describes values from 0.40 to 0.75 as "fair to good" (Fleiss, 1986:7); Streiner and Norman recommend values > 0.75 for continuous scales used in health research (Streiner & Norman, 1995). (These criterial levels should be used with care and common sense; a recent article described them as "hopelessly arbitrary." (de Mast, 2007:152)) Flack and colleagues and Walter and colleagues have provided sample size formulae for the kappa and intraclass correlation coefficients, respectively, so that reliability studies can be correctly powered (Flack, Afifi, Lachenbruch, & Schouten, 1988; Walter, Eliasziw, & Donner, 1998) (Table 1).

The practice of not reporting measures of precision for reliability test results originates, perhaps, from the irrelevance of p-values from hypothesis tests whose null values are zero, e.g., reliability assumed to be only marginally greater than chance is hardly worth the effort to assess. Measures of precision, such as confidence intervals, are not required for Cronbach's alpha coefficient because it is mathematically already the lower bound of a reliability coefficient (Cronbach, 1951). Its reporting may have set an historical precedent for reporting kappa coefficients and intraclass correlation coefficients. Whatever the origin of the practice might be, when these kappa and intraclass correlation coefficients are used for statistical inference they should be accompanied by confidence intervals.

Omnibus Statistics

Kappa and intraclass correlation coefficients can be described as "omnibus quantities" because they summarize several dimensions of relevant data in a single number, and, thus, this same number can represent a plurality of dimensional configurations (van Belle, 2002:6–7:). (Compare Tables 2a and 2b.) This omnibus status makes them easy to calculate and to interpret; however, it also has limitations. Reliability studies often present results for several measurement instruments and at least implicitly claim to indicate which of the tested instruments are most reliable. Even when accompanied by suitable measures of precision, kappa coefficients, and intraclass correlation coefficients for ordinal data (which are approximately equivalent to kappa values when quadratically weighted (Fleiss & Cohen, 1973)), cannot adequately discriminate between the reliability of two instruments unless an unrealistic presupposition is met. This presupposition posits that the distributions of what is being measured are approximately the same for the two tables (Thompson & Walter, 1988). Even for a single table, if marginal totals (summations across specific rows or columns in a contingency table representing agreement data) vary from one rater to another, the kappa

coefficient may take on different values even though the total proportion of agreement remains the same (Feinstein & Cicchetti, 1990).

In discussing the ambiguities introduced by kappa coefficients with unbalanced distributions, i.e., the prevalence of the condition of interest differs for two ratings summarized in the same table, Cicchetti and Feinstein recommend supplementing reports of the coefficient with the proportion of agreement for each level of the measurement variable (Cicchetti & Feinstein, 1990). (Proportions of positive and negative agreement discriminate between Tables 2a and 2b for which the kappa coefficients are the same; also, they suggest that the kappa value from Table 2c is more readily comparable to the kappa value for Table 2b than for Table 2a.) Although proportions of agreement are convenient and valuable, supplementing omnibus reliability statistics with relevant regression modeling techniques is a more informative and more general approach.

Reliability and Regression Modeling

In the case of the intraclass correlation coefficient, the advent of linear mixed effect models allows for its calculation from a single regression model. It can be obtained as an item in the model's correlation matrix (SAS/STAT User's Guide, Version 9.1.3, 2005). It provides the flexibility of calculating different versions of the intraclass correlation coefficient, ones for only randomly selected study participant samples, ones with only randomly selected raters, and ones with random terms for both study participants and raters. Confidence intervals and subgroup analyses can easily be calculated. Two other regression modeling techniques are especially helpful for evaluating reliability for nominal and ordinal scales.

Loglinear Regression Models

Loglinear regression models have been used to analyze rater agreement since the mid 1980's (Tanner & Young, 1985a, , 1985b). Loglinear models are used instead of standard linear models because agreement data occur as discrete counts rather than on continuous scales. Counts can be treated as independent observations from a Poisson distribution. Loglinear models lend themselves to modeling agreement beyond chance because their simplest form—the independence model—assumes that the mean values of cells in a 2×2 table, m_{ij} , can be estimated by the product of the table sample size, n, and the probabilities of counts occurring in a specified row, π_{i+} , and column, π_{+j} . The natural logarithm of the mean number of counts is used because this transformation makes the above multiplicative relationship additive, i.e., linear in the parameters. Modifications of this model attempt to capture patterns of agreement beyond chance.

Results from loglinear agreement models overcome the shortcomings of the kappa omnibus reliability statistic in several ways. Its primary measure of association, the agreement odds ratio, is more discriminating, e.g., it is less liable to give the same numerical value for different data configurations. (Note the distinct odds ratios in Tables 2a-2c; Table 2d shows odds ratios to be invariant under transposition of both rows and columns.) The agreement odds ratio for two raters can be defined in an analogous way to an odds ratio used in cohort studies. Assuming for pairs of subjects that each rater classifies them in one of two categories, *i* and *j*:

Like the kappa and intraclass correlation coefficients, larger values of the agreement odds ratio indicates that observers are more likely to agree for the given pair of categories (Agresti,

 $AOR = \frac{odds}{odd} of rater 2 classifying subjects in$ *i*when rater 1 classifies them in*i*

 $AOR = \frac{1}{\text{odds of rater 2 classifying subjects in } i$ when rater 1 classifies them in j= $\frac{1}{\text{odds of concordance in category classification among raters}}$

odds of discordance in category classification among raters

2002). (Although the agreement odds ratio is interpretable in a way analogous to traditional odds ratios it is actually calculated differently.) When there are only two response categories, the agreement odds ratio is calculated from a parameter δ that represents the extent of exact agreement beyond chance. For models with ordinal response categories a second parameter (β) can be estimated that represents beyond chance agreement due to a linear association between ratings obtained from two raters. Thus, in these models agreement can not only be decomposed into agreement due to chance and beyond chance agreement, but beyond chance agreement is further decomposed into parts attributable to exact agreement and linear association (Velema, Blettner, Restrepo, & Munoz, 1991).

Table 3a shows an agreement table relevant to reliability testing of a measure of ease of distraction administered to an older nursing home population. It is one of several variables designed to measure changes in mental status that are thought to be clinical features of urinary tract infections in this population. The weighted (quadratic) kappa coefficient for this table is 0.34 (90% CI 0.12, 0.57). This is not an acceptable level of reliability and one might be interested in the nature and sources of the unreliability. One might assess the marginal homogeneity of the agreement table, i.e., whether the probability of falling in any category of the row classification is equal to the probability of falling in any category of the left-to-right table diagonal—occur in a differential pattern that might be amenable to correction by further training, or in a more random way that might simply reflect a limitation of the measurement instrument.

Two-by-two tables can be tested for marginal homogeneity using a McNemar test for symmetry (McNemar, 1947). Rejection of the null hypothesis of symmetry in this case implies rejection of a null hypothesis of marginal homogeneity and this indicates that differential disagreement occurs to an extent statistically significant at some specified level, usually 0.05. This approach to testing marginal homogeneity is applicable to 2×2 tables but not for larger square tables. Loglinear regression techniques provide a more general way to test for marginal homogeneity. A loglinear model can be fit that assumes that counts occurring off of the main diagonal of a square contingency table are symmetrically distributed. A likelihood ratio chi-square statistic measures model goodness of fit. With only a slight modification a second loglinear model can be fit that relaxes the symmetry assumption to allow for marginal heterogeneity (Darroch & McCloud, 1986). Comparison of the likelihood ratio chi-square from this quasi-symmetry model and the above symmetry model allows for a statistical test of a null hypothesis of marginal homogeneity. Rejection of this null hypothesis indicates that differential disagreement between raters occurs in a way that is statistically significant. For Table 3a the symmetry model yields a likelihood ratio chi-square statistic of 4.53 with 3 degrees of freedom (df), and the quasi-symmetry model yields values of 0.19 with 1 df. Hence, upon subtracting the latter values from the former, a chi-square test of 4.34 for 2 df has a p-value of 0.114. In some cases, especially for small sample sizes, results will be questionable due to poor fitting models; this topic will be addressed subsequently.

A second issue that a clinical researcher might want to investigate for the ease of distraction measure is whether the reliability of this instrument differs for two subgroups. Often of interest are possible differences in reliability when the younger versus the older portions of the cohort are compared. Tables 3b1 and 3b2 represent agreement data for two age-related subgroups. The weighted kappa for the younger half (65–86) is 0.27 (90% CI 0.00, 0.53) and it is 0.47 (90% CI 0.17, 0.77) for the older half (87+). A test for the equality of the two kappa coefficients fails to reject the null hypothesis of equality ($\chi^2 = 0.68$, df=1, p=0.411). Two factors require that this test for equality be interpreted with caution. First, the marginal distributions of the two age-related agreement tables are different and so comparison of the two coefficients is problematic. Second, the small sample size makes the test underpowered. Geriatric researchers

are also often interested in knowing whether reliability differs for proxy responses versus older study participant responses. A similar subgroup analysis would be insightful for investigating this issue.

An advantage of the loglinear regression approach is that it can incorporate a binary covariate into the model that allows for statistical inferences as to whether the reliability of an instrument differs for two groups (Graham & Jackson, 2000). It allows for the calculation of agreement odds ratios for pairs of levels in the measurement scale and thereby avoids some of the ambiguity in comparing kappa coefficients of differently distributed agreement tables.

Latent Class Regression Models

The dependence of the kappa coefficient to imbalances in marginal distributions of agreement data motivates its supplementation with additional information that can be provided effectively by loglinear regression models. A second consideration motivates supplementation of omnibus reliability statistics with latent class regression models. Testing a measurement instrument for reliability pragmatically implicates that it successfully measures what it is intended to measure; it implicates validity understood as diagnostic accuracy. An instrument that consistently misses its mark is little redeemed by the consistency of its errors. Validity is difficult to test statistically. Latent class models provide some insight.

Latent variable regression models (also describable as finite mixture models) differ from traditional regression models by containing parameters that describe unobserved variables. When modeling rater agreement, they model the joint distribution of ratings as a mixture of distributions for levels of a latent variable. They effectively relax the traditional assumption that the same probability model holds for the entirety of the data set being analyzed. In clinical reliability analyses, the latent variable might be disease severity such that the rating scale posits certain disease thresholds that correspond to rating levels. These thresholds might be understood to mark points on continuum of disease severity (latent trait models) or to specify transitions between homogenous stages of disease progression (latent class models). The simplest case of a latent class model posits two classes of a health condition—its presence and absence (John S. Uebersax, 1992; J. S. Uebersax & Grove, 1990).

Measurement error in this context is relative and its assessment is based on an important assumption and a key data requirement. It is assumed that if two ratings disagree one is correct and the other incorrect, and that if a plurality of ratings gives the same result that this result is correct. These assumptions allow some assessment of validity in the absence of a definitive criterion, but obviously require that there be data from at least three, and preferably more, raters. Some latent variable models permit inferences about rating sensitivity, specificity, and the area under a Receiver Operating Characteristic (ROC) curve. These model results have the advantage of being easily interpretable in a clinical context and readily comparable to other relevant information.

A useful application of latent class modeling addresses the multifactorial nature of many health conditions among older persons. For instance, ease of distraction is not the only dimension of a change in mental status that might be relevant to diagnosing a urinary tract infection. Others are measures of altered perception, disorganized speech, restlessness, lethargy, and daily mental variability. The latent classes of change and no change in mental status are identified as a function of the covariances among the six variables (Lanza, 2007) (Table 4). The lethargy and daily mental variability variables are least sensitive, with the lethargy variable also having the worst specificity. (Confidence intervals should likewise accompany measures of sensitivity and specificity (Ely et al., 2001).) This suggests that the lethargy variable is poorly measuring the change in mental status that one intends to measure with the other variables and might best be deleted from the group in study analyses. Note that the ease of distraction has fairly strong

sensitivity and specificity results despite its apparently limited inter-rater reliability. Using regression techniques like latent class analysis provides additional perspectives on measurement instruments and makes possible informed discrimination in instrument selection and/or correction.

Reliability Inference and Unreliability Detection

In formal reliability studies in which inferences are drawn, statistics like the kappa and intraclass correlation coefficients should be accompanied by confidence intervals. Evaluation of measurement reliability, however, is often undertaken for more practical purposes such as detecting unreliability in instrument administration that might be corrected by further training or scale modification. In clinical aging research small sample sizes are often used for such practical purposes, rendering statistically significant results unlikely. What is especially important in these circumstances is to avoid bias introduced by small sample sizes. Exact versions of kappa coefficients are available as are exact tests of marginal homogeneity (*StatXact User's Guide, Version 7*, 2006). (For data in Table 3a exact methods yield substantively similar analytic results as reported above.) Unbalanced distributions can be especially pronounced in small agreement tables and thereby generate kappa coefficients that are hard to interpret. Alternatives to the kappa might be sought that are less influenced by such imbalances and so more easily interpreted (Brennan & Prediger, 1981); (Munoz & Bangdiwala, 1997).

Finally, descriptive reliability statistics might have to suffice for small samples. Using the percentage of overall agreement Byrt and colleagues propose for 2-by-2 tables a "prevalence-adjusted and bias-adjusted kappa" (PABAK) that is equal to two times the overall percentage of agreement minus one (Byrt et al., 1993). They also propose a bias index for such tables that provides insight comparable to a test for marginal homogeneity and a prevalence index that integrates information from percentages of positive and negative agreement. These descriptive statistics sometimes yield results that concur with the kappa coefficient (Table 5a) and in other cases suggest different reliability results (Table 5b.) Use of such simple descriptive statistics is preferable to inferential methods in circumstances for which the latter are not applicable. This point emphasizes that the goal of reliability testing, being the effective selection and application of measurement instruments, should be pursued by different methods as circumstances require.

Acknowledgments

This study was supported by Claude D. Pepper OAIC at Yale University School of Medicine (#P30AG21342). The authors thank Heather G. Allore for her assistance.

References

Agresti, A. Categorical Data Analysis. Vol. 2. Hoboken, NJ: John Wiley & Sons; 2002.

- Brennan RL, Prediger DJ. Coefficient kappa: Some uses, misuses, and alternatives. Educational and Psychological Measurement 1981;41:687–699.
- Byrt T, Bishop J, Carlin JB. Bias, prevalence, and kappa. Journal of Clinical Epidemiology 1993;46:423– 429. [PubMed: 8501467]
- Cicchetti DV, Feinstein AR. High agreement but low kappa: II. Resolving the paradoxes. Journal of Clinical Epidemiology 1990;43:551–558. [PubMed: 2189948]
- Cohen J. A coefficient of agreement for nominal scales. Educational and Psychological Measurement 1960;20:37–46.
- Cronbach LJ. Coefficient alpha and the internal structure of tests. Psychometrika 1951;16:297-334.
- Darroch JN, McCloud PI. Category distinguishability and observer agreement. Australian Journal of Statistics 1986;28:371–388.

- Ely EW, Inouye SK, Bernard GR, Gordon S, Francis J, May L, et al. Delirium in mechanically ventilated patients: Validity and reliability of the Confusion Assessment Method for the Intensive Care Unit (CAM-ICU). JAMA 2001;286:2703–2710. [PubMed: 11730446]
- Feinstein AR, Cicchetti DV. High agreement but low kappa: I. The problems of two paradoxes. Journal of Clinical Epidemiology 1990;43:543–549. [PubMed: 2348207]
- Fisher, RA. Statistical Methods for Research Workers. Edinburgh: Oliver and Boyd; 1925.
- Flack VF, Afifi AA, Lachenbruch PA, Schouten HJA. Sample size determinations for the two rater kappa statistic. Psychometrika 1988;53:321–325.
- Fleiss, JL. The Design and Analysis of Clinical Experiments. New York: John Wiley & Sons; 1986.
- Fleiss JL, Cohen J. The equivalence of weighted kappa and the intraclass correlation coefficient as measures of reliability. Educational and Psychological Measurement 1973;33:613–619.
- Graham P, Jackson R. A comparison of primary and proxy respondent reports of habitual physical activity, using kappa statistics and log-linear models. Journal of Epidemiology and Biostatistics 2000;5:255– 265. [PubMed: 11055276]
- Gregson JM, Leathley MJ, Moore AP, Smith TL, Sharma AK, Watkins CL. Reliability of measurements of muscle tone and muscle power in stroke patients. Age and Ageing 2000;29:223–228. [PubMed: 10855904]
- Hinze, JL. PASS 2005 User's Guide. Kaysville, UT: Number Cruncher Statistical Systems; 2004.
- Landis JR, Koch GG. The measurement of observer agreement for categorical data. Biometrics 1977;33:159–174. [PubMed: 843571]
- Lanza, ST.; Lemmon, D.; Schafer, JL.; Collins, LM. PROC LCA & PROC LTA User's Guide Version 1.1.3. University Park, PA: Methodology Center, Pennsylvania State University; 2007.
- McNemar Q. Note on the sampling error of the difference between correlated proportions or percentages. Psychometrika 1947;12:153–157.
- Munoz SR, Bangdiwala SI. Interpretation of Kappa and B statistics measures of agreement. Journal of Applied Statistics 1997;24:105–111.
- Nee, JC. EasyStat 3.04 User's Guide. New York: New York Psychiatric Institute; 1998.
- SAS/STAT User's Guide, Version 9.1.3. Cary, N.C: SAS Institute; 2005.
- StatXact User's Guide, Version 7. Cambridge, MA: Cytel Statistical Software & Services; 2006.
- Streiner, DL.; Norman, GR. Health Measurement Scales: A Practical Guide to their Development and Use. Vol. 2. New York: Oxford University Press; 1995.
- Tanner MA, Young MA. Modeling agreement among raters. Journal of the American Statistical Association 1985a;80:175–180.
- Tanner MA, Young MA. Modeling ordinal scale disagreement. Psychological Bulletin 1985b;98:408– 415. [PubMed: 3901069]
- Thompson WD, Walter SD. A reappraisal of the kappa coefficient. Journal of Clinical Epidemiology 1988;41:949–958. [PubMed: 3057117]
- Uebersax JS. Modeling approaches for the analysis of observer agreement. Investigative Radiology 1992;27:738–743. [PubMed: 1399458]
- Uebersax JS, Grove WM. Latent class analysis of diagnostic agreement. Statistics in Medicine 1990;9:559–572. [PubMed: 2190288]
- van Belle, G. Statistical Rules of Thumb. Hoboken, NJ: John Wiley & Sons; 2002.
- Velema JP, Blettner M, Restrepo M, Munoz N. The evaluation of agreement by means of log-linear models: Proxy interviews on reproductive history among floriculture workers in Columbia. Epidemiology 1991;2:107–115. [PubMed: 1932307]
- Walter SD, Eliasziw M, Donner A. Sample size and optimal designs for reliability studies. Statistics in Medicine 1998;17:101–110. [PubMed: 9463853]
- Wolinsky FD, Miller DK, Andresen EM, Malmstrom TK, Miller JP. Reproducibility of physical performance and physiologic assessments. Journal of Aging and Health 2005;17:111–124. [PubMed: 15750047]

Table 1Power Tables for the Kappa Coefficient (κ) and the Intraclass Correlation Coefficient (ICC)

Power Table for Kappa Coefficier	nts with Two Observations per 0.05 and w	Subject for a Binary Variable with a $\kappa = 0.40$ Null Hypothesis	with .40 Prevalence Using a C	One-Sided Test at Alpha =
		Obser	ved ĸ	
Sample Size	.60	.70	.80	.90
20	.22	.40	.66	.94
30	.30	.56	.86	.99
50	.44	.79	.98	.99
100	.72	.98	.99	.99

Power Table for Intraclass Correlation Coefficients with Two Observations per Subject Using a One-Sided Test at Alpha = 0.05 and with a ICC = 0.75 Null Hypothesis[#]

		Observe	ed ICC	
Sample Size	.80	.85	.90	.95
20	.13	.34	.70	.98
30	.16	.45	.85	.99
50	.22	.63	.97	.99
100	.35	.88	.99	.99

*(Nee, 1998)

#(Hinze, 2004)

Rater 1 8 Auer 1 8 Auer 1 8 5 8 5 8 5 9 7 9 7	•	••		-
Rater 1 35 15 50 15 35 50 50 50 $\kappa = 0.40 (90\% C1^{*} 0.25, 0.55)$ OR = 5.44 proportion - agreed = $0.70 = 2a([N + (a - d)]^{\#}$ proportion - agreed = $0.70 = 2a([N - (a - d)]^{\#}$ Table 2b 45 5 5 50 50 70 30 $\kappa = 0.40 (90\% C1 0.26, 0.54)$ OR = 9.00 proportion - agreed = 0.75 proportion - agreed = 0.625 Table 2c Table	Table 2a			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			Rater 2	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Rater 1	35	15	50
$ \begin{array}{c} \mbox{$$x$ = 0.40 (90\% C1 ^{9} 0.25, 0.55)$} \\ OR = 5.44 \\ \mbox{$$proportion + agreed = 0.70 = 2a/[N + (a - d)]^{4'$} \\ \mbox{$$proportion - agreed = 0.70 = 2d/[N - (a - d)]^{4'$} \\ \mbox{$$proportion - agreed = 0.70 = 2d/[N - (a - d)]^{4'$} \\ \mbox{$$Table 2b$} \\ \begin{array}{c} \mbox{$$45$ & 5 & 50 \\ \mbox{$$25$ & 25 & 50 \\ \mbox{$$70$ & 30 & x = 0.40 (90\% C1 0.26, 0.54)$ \\ OR = 9.00 \\ \mbox{$$proportion + agreed = 0.75$ \\ $proportion - agreed = 0.625$ & 40 \\ \mbox{$$0$ & 15 & 25 & 40 \\ \mbox{$$0$ & 15 & 25 & 40 \\ \mbox{$$0$ & 60 & 40 & x = 0.375 (90\% C1 ^{9} 0.22, 0.53)$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.75$ \\ $proportion + agreed = 0.75$ \\ $proportion - agreed = 0.625$ & 40 & 60 \\ \mbox{$$x$ = 0.375$ (90\% C1 ^{9} 0.22, 0.53)$ \\ OR = 5.00 \\ $$proportion + agreed = 0.625$ & 40 & 60 \\ \mbox{$$40$ & 60 & 40 & 60 \\ \mbox{$$x$ = 0.375$ (90\% C1 0.22, 0.53)$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.625$ & $\mathsf{15$ & 40 & 60 \\ \mbox{$$40$ $$60$ & 60 & 70 & $\mathsf{22$ 0.53)$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.625$ & $\mathsf{15$ & 40 & 60 \\ \mbox{$$40$ $$60$ & 60 & 70 & $\mathsf{22$ 0.53)$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.625$ & $\mathsf{15$ & 40 & 60 \\ \mbox{$$40$ $$60$ & 60 & 70 & $\mathsf{22$ 0.53)$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.625$ & $\mathsf{10$ & 20 & 20 & 10 & 22 0.53)$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.625$ & $\mathsf{10$ & 10 & 22 0.53$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.625$ & $\mathsf{10$ & 10 & 22 0.53$ \\ OR = 5.00 \\ \mbox{$$proportion + agreed = 0.625$ & $\mathsf{10$ & 10 & $\mathsf{$		15	35	50
$\begin{array}{c} & \begin{array}{c} & & & & & & & & & & & & & & & & & & &$		50	50	
$ \begin{array}{c} \label{eq:proportion + agreed = 0.70 = 2a' [N + (a - d)]^{\#} \\ \mbox{proportion - agreed = 0.70 = 2d' [N - (a - d)]^{\#} \\ \hline \\ \mbox{Table 2b} \\ \mbox{45} & 5 & 50 \\ \mbox{25} & 25 & 50 \\ \mbox{70} & 30 \\ \mbox{$\kappa = 0.40$ (00% CI 0.26, 0.54)$ } \\ \mbox{$OR = 9.00$ } \\ \mbox{$proportion + agreed = 0.75$ } \\ \mbox{$proportion + agreed = 0.625$ } \\ \hline \\ \mbox{Table 2c} \\ \mbox{45} & 15 & 60 \\ \mbox{60 & 40$ } \\ \mbox{$\kappa = 0.375$ (90\% CI^{+} 0.22, 0.53)$ } \\ \mbox{$OR = 5.00$ } \\ \mbox{$proportion + agreed = 0.75$ } \\ \mbox{$Proportion + agreed = 0.625$ } \\ \hline \\ \mbox{$Table 2c$ } \\ \mbox{$Table 2c$ } \\ \mbox{$Table 2c$ } \\ \mbox{$Proportion + agreed = 0.75$ } \\ \mbox{$Proportion + agreed = 0.625$ } \\ $Proportion + agreed = 0.625$		$\kappa = 0.40 \ (90\% \ \text{CI}^* \ 0.25, \ 0.55)$		
$\begin{tabular}{ c c c c } & & & & & & & & & & & & & & & & & & &$		OR = 5.44		
Table 2b 45 5 50 25 25 50 70 30 50 $\kappa = 0.40 (90\% CI 0.26, 0.54)$ 90 900 proportion + agreed = 0.75 90 900 proportion - agreed = 0.625 90 900 Table 2c 45 15 45 15 60 15 25 40 60 40 90 $\kappa = 0.375 (90\% CI * 0.22, 0.53)$ 90 90 proportion + agreed = 0.75 90 90 proportion + agreed = 0.75 90 90 Proportion + agreed = 0.75 proportion + agreed = 0.75 90 90 Proportion + agreed = 0.75 Proportion + agreed = 0.625		proportion + agreed = $0.70 = 2a/[N + agreed = 0.70]$	$(a - d)]^{\#}$	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		proportion – agreed = $0.70 = 2d/[N - d/(N - d)]$	$(a - d)]^{\#}$	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Table 2b		_	-
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				
$ \begin{array}{c} \kappa = 0.40 \ (90\% \ CI \ 0.26, 0.54) \\ OR = 9.00 \\ proportion + agreed = 0.75 \\ proportion - agreed = 0.625 \end{array} \\ \hline \\ \hline \\ Table 2c \\ 45 \\ 15 \\ 5 \\ 60 \\ 60 \\ 60 \\ \kappa = 0.375 \ (90\% \ CI \ 0.22, 0.53) \\ OR = 5.00 \\ proportion + agreed = 0.625 \end{array} \\ \hline \\ \hline \\ Table 2d \\ \hline \\ \hline \\ Table 2d \\ \hline \\ Table 2d \\ \hline \\ \hline \\ Table 2d \\ \hline \\ \hline \\ \hline \\ Table 2d \\ \hline \\ $				50
$\begin{array}{c} & \mbox{OR} = 9.00 \\ & \mbox{proportion} + \mbox{agreed} = 0.625 \end{array} \\ \hline \\ \hline \\ \hline \\ \hline \\ Table 2c \\ & \mbox{45} & 15 & 60 \\ & 15 & 25 & 40 \\ & 60 & 40 \\ & \mbox{κ = 0.375$ (90\% CI ^* 0.22, 0.53) \\ & \mbox{OR} = 5.00 \\ & \mbox{proportion} + \mbox{agreed} = 0.625 \end{array} \\ \hline \\ \hline \\ \hline \\ \hline \\ Table 2d \\ \hline \\ \hline \\ \hline \\ Table 2d \\ \hline \\ $			30	
proportion + agreed = 0.75 proportion = agreed = 0.625 Table 2c 45 15 60 40 60 40 $\kappa = 0.375 (90\% CI^* 0.22, 0.53)$ $0R = 5.00$ proportion = agreed = 0.625 15 40 Table 2d 25 15 40 15 40 15 40 15 40 15 40 15 40 15 40 15 40 15 40 15 40 15 40 15 40 15 40 15 160				
proportion – agreed = 0.625 Table 2c 45 15 60 15 25 40 60 40 60 $\kappa = 0.375 (90\% Cl^* 0.22, 0.53)$ 0R = 5.00 9000000000000000000000000000000000000				
Table 2c 45 15 60 15 25 40 60 40 60 $\kappa = 0.375 (90\% CI^* 0.22, 0.53)$ 7 7 OR = 5.00 proportion + agreed = 0.75 7 proportion - agreed = 0.625 40 60 40 Table 2d 25 15 40 40 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 60 60 $\kappa = 0.375 (90\% CI 0.22, 0.53)$ 7 7				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		proportion agreed = 0.025		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Table 2c			
60 40 $\kappa = 0.375 (90\% \text{ CI}^* 0.22, 0.53)$ 0R = 5.00 proportion + agreed = 0.75 proportion - agreed = 0.625 Table 2d Table 2d 25 15 40 60 40 60 $\kappa = 0.375 (90\% \text{ CI } 0.22, 0.53)$ 60 0R = 5.00 0R = 5.00 proportion + agreed = 0.625 15		45	15	60
$\kappa = 0.375 (90\% \text{ CI}^* 0.22, 0.53)$ $OR = 5.00$ proportion + agreed = 0.75 proportion - agreed = 0.625 Table 2d $25 15 40$ $15 45 60$ $40 60$ $\kappa = 0.375 (90\% \text{ CI } 0.22, 0.53)$ $OR = 5.00$ proportion + agreed = 0.625		15	25	40
$OR = 5.00$ proportion + agreed = 0.75 proportion - agreed = 0.625 Table 2d $25 15 40$ $15 45 60$ $40 60$ $\kappa = 0.375 (90\% CI 0.22, 0.53)$ $OR = 5.00$ proportion + agreed = 0.625		60	40	
proportion + agreed = 0.75 proportion - agreed = 0.625 Table 2d 25 15 40 40 60 40 60 $\kappa = 0.375$ (90% CI 0.22, 0.53) OR = 5.00 proportion + agreed = 0.625		$\kappa = 0.375 (90\% \text{ CI}^* 0.22, 0.53)$		
proportion - agreed = 0.625 Table 2d $25 15 40 60 60 60 60 60 60 60$		OR = 5.00		
Table 2d 25 15 40 15 45 60 40 60 60 $\kappa = 0.375$ (90% CI 0.22, 0.53) 0R = 5.00 0R = 5.00 proportion + agreed = 0.625		proportion $+$ agreed $= 0.75$		
$\begin{array}{cccccccc} 25 & 15 & 40 \\ 15 & 45 & 60 \\ 40 & 60 \\ \kappa &= 0.375 \ (90\% \ CI \ 0.22, \ 0.53) \\ OR &= 5.00 \\ proportion + agreed &= 0.625 \end{array}$		proportion $-$ agreed $= 0.625$		
$\begin{array}{cccccccc} 25 & 15 & 40 \\ 15 & 45 & 60 \\ 40 & 60 \\ \kappa &= 0.375 \ (90\% \ CI \ 0.22, \ 0.53) \\ OR &= 5.00 \\ proportion + agreed &= 0.625 \end{array}$	Table 2d			
15 45 60 40 60 $\kappa = 0.375$ (90% CI 0.22, 0.53) 60 $OR = 5.00$ $7000000000000000000000000000000000000$	14010 20	25	15	40
40 60 $\kappa = 0.375 (90\% \text{ CI } 0.22, 0.53)$ OR = 5.00 proportion + agreed = 0.625				
$\kappa = 0.375 (90\% \text{ CI } 0.22, 0.53)$ OR = 5.00 proportion + agreed = 0.625				
OR = 5.00 proportion + agreed = 0.625				
proportion $+$ agreed $= 0.625$				
		proportion – agreed = 0.75		

*CI = Confidence Interval

[#](Cicchetti & Feinstein, 1990) Agreement tables are lettered consecutively by rows, from left to right and top to bottom.

Table 3 Subgroup Decomposition by Age of a 3 × 3 Agreement Table for a Measure of Ease of Distraction (N=30)

Table 3a				
		Rater 2		
Rater 1	8	6	1	
	2	9	3	
	0	1	0	
Table 3b1: Age ≤ 86				
	3	4	1	
	0	4	2	
	0	1	0	
Table 3b2: Age > 86				
1401e 502. Age > 60	5	2	0	
	2	5	1	
	0	0	0	

Table 4

Results of a Latent Class Analysis of Six Change of Mental Status Variables (N = 62)

	Latent Class Prevalence Estimates ¹	
% No Chan	ge	% Change
0.65		0.35
	Diagnostic Accuracy Estimates ¹	
Variable	Sensitivity	Specificity
	(95% Confidence Interval)	(95% Confidence Interval)
Ease of Distraction	0.78 (0.61, 0.95)	0.87 (0.77, 0.97)
Altered Perception	0.73 (0.55, 0.92)	0.87 (0.77, 0.97)
Disorganized Speech	0.88 (0.75, 1.00)	0.98 (0.94, 1.00)
Restlessness	0.71 (0.52, 0.90)	0.86 (0.75, 0.97)
Lethargy	0.63 (0.43, 0.83)	0.77 (0.64, 0.90)
Daily Mental Variability	0.64 (0.44, 0.84)	0.88 (0.78, 0.98)

I Likelihood ratio chi-square statistic = 57.73 with 50 degrees of freedom and a p-value of 0.211, so there is a failure to reject the null hypothesis of goodness of fit.

Table 5Descriptive Reliability Statistics for Two Urine-Related Measures (N = 20)

Table 5a: Change in Odor		
5	1	
1	13	
$PABAK = 0.80 = [(2*(a+d)/N)-1]^{\#}$		
Bias Index = $0.00 = (b - c)/N^{\#}$		
Prevalence Index = $-0.40 = (a - d)/N^{\text{#}}$		
Kappa = 0.76 (90% CI [*] 0.50, 1.00)		
$Kappa = 0.70 (90\% C1^{-} 0.50, 1.00)$		
Table 5b: Change in Incontinence		
-		
0	2	
1	17	
PABAK = 0.70		
Bias Index = 0.05		
Prevalence Index $= -0.85$		

Kappa = - 0.07 (90% CI - 0.16, 0.01)

[#](Byrt, Bishop, & Carlin, 1993) Agreement tables are lettered consecutively by rows, from left to right and top to bottom.

*CI = Confidence Interval