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The 6dF Galaxy Survey: baryon acoustic oscillations and the local Hubble constant

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ABSTRACT

We analyse the large-scale correlation function of the 6dF Galaxy Survey (6dFGS) and detect a baryon acoustic oscillation (BAO) signal at $105 \, h^{-1}$ Mpc. The 6dFGS BAO detection allows us to constrain the distance–redshift relation at $z_{\rm eff} = 0.106$. We achieve a distance measure of $D_V(z_{\rm eff}) = 457 \pm 27$ Mpc and a measurement of the distance ratio, $r_{\rm s}(z_{\rm d})/D_V(z_{\rm eff}) = 0.336 \pm 0.015$ (4.5 per cent precision), where $r_{\rm s}(z_{\rm d})$ is the sound horizon at the drag epoch $z_{\rm d}$. The low-effective redshift of 6dFGS makes it a competitive and independent alternative to Cepheids and low-z supernovae in constraining the Hubble constant. We find a Hubble constant of $H_0 = 67 \pm 3.2 \, {\rm km \, s^{-1} \, Mpc^{-1}}$ (4.8 per cent precision) that depends only on the *Wilkinson Microwave Anisotropy Probe-7* (*WMAP-7*) calibration of the sound horizon and on the galaxy clustering in 6dFGS. Compared to earlier BAO studies at higher redshift, our analysis is less dependent on other cosmological parameters. The sensitivity to H_0 can be used to break the degeneracy between the dark energy equation of state parameter w and w in the cosmic microwave background data. We determine that $w = -0.97 \pm 0.13$, using only *WMAP-7* and BAO data from both 6dFGS and Percival et al. (2010).

We also discuss predictions for the large-scale correlation function of two future wide-angle surveys: the Wide field ASKAP L-band Legacy All-sky Blind surveY (WALLABY) blind H I survey (with the Australian Square Kilometre Array Pathfinder, ASKAP) and the proposed Transforming Astronomical Imaging surveys through Polychromatic Analysis of Nebulae (TAIPAN) all-southern-sky optical galaxy survey with the UK Schmidt Telescope. We find that both surveys are very likely to yield detections of the BAO peak, making WALLABY the first radio galaxy survey to do so. We also predict that TAIPAN has the potential to constrain the Hubble constant with 3 per cent precision.

Key words: surveys – cosmology: observations – dark energy – distance scale – large-scale structure of Universe.

1 INTRODUCTION

The current standard cosmological model, Λ cold dark matter (Λ CDM), assumes that the initial fluctuations in the distribution of matter were seeded by quantum fluctuations pushed to cosmological scales by inflation. Directly after inflation, the Universe is radiation-dominated and the baryonic matter is ionized and coupled

to radiation through Thomson scattering. The radiation pressure drives sound waves originating from overdensities in the matter distribution (Peebles & Yu 1970; Sunyaev & Zeldovich 1970; Bond & Efstathiou 1987). At the time of recombination ($z_* \approx 1090$), the photons decouple from the baryons and shortly after that (at the baryon drag epoch $z_{\rm d} \approx 1020$) the sound wave stalls. Through this process, each overdensity of the original density perturbation field has evolved to become a centrally peaked perturbation surrounded by a spherical shell (Bashinsky & Bertschinger 2001, 2002; Eisenstein, Seo & White 2007a). The radius of these shells is called

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the sound horizon $r_{\rm s}$. Both overdense regions attract baryons and dark matter and will be preferred regions of galaxy formation. This process can equivalently be described in Fourier space, where during the photon–baryon coupling phase, the amplitude of the baryon perturbations cannot grow and instead undergo harmonic motion leading to an oscillation pattern in the power spectrum.

After the time of recombination, the mean free path of photons increases and becomes larger than the Hubble distance. Hence from now on the radiation remains almost undisturbed, eventually becoming the cosmic microwave background (CMB).

The CMB is a powerful probe of cosmology due to the good theoretical understanding of the physical processes described above. The size of the sound horizon depends (to first order) only on the sound speed in the early Universe and the age of the Universe at recombination, both set by the physical matter and baryon densities, $\Omega_{\rm m}\,h^2$ and $\Omega_{\rm b}\,h^2$ (Eisenstein & Hu 1998). Hence, measuring the sound horizon in the CMB gives extremely accurate constraints on these quantities (Komatsu et al. 2011). Measurements of other cosmological parameters often show degeneracies in the CMB data alone (Efstathiou & Bond 1999), especially in models with extra parameters beyond flat Λ CDM. Combining low-redshift data with the CMB can break these degeneracies.

Within galaxy redshift surveys, we can use the correlation function, ξ , to quantify the clustering on different scales. The sound horizon marks a preferred separation of galaxies and hence predicts a peak in the correlation function at the corresponding scale. The expected enhancement at $s=r_s$ is only $\Delta \xi \approx 10^{-3}b^2(1+2\beta/3+\beta^2/5)$ in the galaxy correlation function, where b is the galaxy bias compared to the matter correlation function, and β accounts for linear redshift-space distortions. Since the signal appears at very large scales, it is necessary to probe a large volume of the Universe to decrease sample variance, which dominates the error on these scales (Tegmark 1997; Eisenstein, Hu & Tegmark 1998; Goldberg & Strauss 1998).

Very interesting for cosmology is the idea of using the sound horizon scale as a standard ruler (Eisenstein et al. 1998; Cooray et al. 2001; Blake & Glazebrook 2003; Seo & Eisenstein 2003). A standard ruler is a feature whose absolute size is known. By measuring its apparent size, one can determine its distance from the observer. The baryon acoustic oscillation (BAO) signal can be measured in the matter distribution at low redshift, with the CMB calibrating the absolute size, and hence the distance—redshift relation can be mapped (see e.g. Bassett & Hlozek 2009, for a summary).

The Sloan Digital Sky Survey (SDSS; York et al. 2000) and the 2dF Galaxy Redshift Survey (2dFGRS; Colless et al. 2001) were the first redshift surveys which have directly detected the BAO signal. Recently, the WiggleZ Dark Energy Survey has reported a BAO measurement at redshift z = 0.6 (Blake et al. 2011).

Eisenstein et al. (2005) were able to constrain the distance-redshift relation to 5 per cent accuracy at an effective redshift of $z_{\rm eff}=0.35$ using an early data release of the SDSS luminous red galaxy (LRG) sample containing \approx 47 000 galaxies. Subsequent studies using the final SDSS-LRG sample and combining it with the SDSS-main and the 2dFGRS sample were able to improve on this measurement and constrain the distance-redshift relation at $z_{\rm eff}=0.2$ and 0.35 with 3 per cent accuracy (Percival et al. 2010). Other studies of the same data found similar results using the correlation function $\xi(s)$ (Gaztanaga, Cabre & Hui 2009; Labini et al. 2009; Martinez et al. 2009; Sanchez et al. 2009; Kazin et al. 2010a), the power spectrum P(k) (Cole et al. 2005; Huetsi 2006; Tegmark et al. 2006; Reid et al. 2010), the projected correlation function $w(r_{\rm p})$

of photometric redshift samples (Blake et al. 2007; Padmanabhan et al. 2007) and a cluster sample based on the SDSS photometric data (Huetsi 2009). Several years earlier, a study by Miller, Nichol & Batuski (2001) found first hints of the BAO feature in a combination of smaller data sets.

Low-redshift distance measurements can directly measure the Hubble constant H_0 with a relatively weak dependence on other cosmological parameters such as the dark energy equation of state parameter w. The 6dF Galaxy Survey (6dFGS) is the biggest galaxy survey in the local Universe, covering almost half the sky. If 6dFGS could be used to constrain the redshift–distance relation through BAOs, such a measurement could directly determine the Hubble constant, depending only on the calibration of the sound horizon through the matter and baryon density. The objective of the present paper is to measure the two-point correlation function on large scales for the 6dFGS and extract the BAO signal.

Many cosmological parameter studies add a prior on H_0 to help break degeneracies. The 6dFGS derivation of H_0 can provide an alternative source of that prior. The 6dFGS H_0 -measurement can also be used as a consistency check of other low-redshift distance calibrators such as Cepheid variables and Type Ia supernovae (through the so-called distance ladder technique; see e.g. Freedman et al. 2001; Riess et al. 2011). Compared to these more classical probes of the Hubble constant, the BAO analysis has an advantage of simplicity, depending only on $\Omega_{\rm m} \, h^2$ and $\Omega_{\rm b} \, h^2$ from the CMB and the sound horizon measurement in the correlation function, with small systematic uncertainties.

Another motivation for our study is that the SDSS data after data release 3 (DR3) show more correlation on large scales than expected by Λ CDM, and have no sign of a crossover to negative ξ up to $200 \, h^{-1}$ Mpc (the Λ CDM prediction is $140 \, h^{-1}$ Mpc) (Kazin et al. 2010a). It could be that the LRG sample is a rather unusual realization, and the additional power just reflects sample variance. It is interesting to test the location of the crossover scale in another red galaxy sample at a different redshift.

This paper is organized as follows. In Section 2 we introduce the 6dFGS survey and the K band selected subsample used in this analysis. In Section 3 we explain the technique we apply to derive the correlation function and summarize our error estimate, which is based on lognormal realizations. In Section 4 we discuss the need for wide-angle corrections and several linear and non-linear effects which influence our measurement. Based on this discussion, we introduce our correlation function model. In Section 5 we fit the data and derive the distance estimate $D_V(z_{\rm eff})$. In Section 6 we derive the Hubble constant and constraints on dark energy. In Section 7 we discuss the significance of the BAO detection of 6dFGS. In Section 8 we give a short overview of future all-sky surveys and their power to measure the Hubble constant. We conclude and summarize our results in Section 9.

Throughout the paper, we use r to denote real space separations and s to denote separations in redshift space. Our fiducial model assumes a flat universe with $\Omega_{\rm m}^{\rm fid}=0.27,\,w^{\rm fid}=-1$ and $\Omega_{k}^{\rm fid}=0.$ The Hubble constant is set to $H_0=100h\,{\rm km~s^{-1}\,Mpc^{-1}},$ with our fiducial model using $h^{\rm fid}=0.7.$

2 THE 6DF GALAXY SURVEY

2.1 Targets and selection function

The galaxies used in this analysis were selected to $K \le 12.9$ from the Two Micron All Sky Survey Extended Source Catalogue (2MASS XSC; Jarrett et al. 2000) and combined with redshift data from

the 6dFGS (Jones et al. 2009). The 6dFGS is a combined redshift and peculiar velocity survey covering nearly the entire southern sky with $|b| < 10^{\circ}$. It was undertaken with the Six-Degree Field (6dF) multifibre instrument on the UK Schmidt Telescope from 2001 to 2006. The median redshift of the survey is z = 0.052 and the 25: 50: 75 per cent percentile completeness values are 0.61: 0.79: 0.92. Papers by Jones et al. (2004, 2006, 2009) describe 6dFGS in full detail, including comparisons between 6dFGS, 2dFGRS and SDSS.

Galaxies were excluded from our sample if they resided in sky regions with completeness lower than 60 per cent. After applying these cuts, our sample contains 75 117 galaxies. The selection function was derived by scaling the survey completeness as a function of magnitude to match the integrated on-sky completeness, using mean galaxy counts. This method is the same adopted by Colless et al. (2001) for 2dFGRS and is explained in Jones et al. (2006) in detail. The redshift of each object was checked visually and care was taken to exclude foreground Galactic sources. The derived completeness function was used in the real galaxy catalogue to weight each galaxy by its inverse completeness. The completeness function was also applied to the mock galaxy catalogues to mimic the selection characteristics of the survey. Jones et al. (in preparation) describe the derivation of the 6dFGS selection function, and interested readers are referred to this paper for a more comprehensive treatment.

2.2 Survey volume

We calculated the effective volume of the survey using the estimate of Tegmark (1997):

$$V_{\text{eff}} = \int d^3 x \left[\frac{n(x) P_0}{1 + n(x) P_0} \right]^2, \tag{1}$$

where n(x) is the mean galaxy density at position x, determined from the data, and P_0 is the characteristic power spectrum amplitude of the BAO signal. The parameter P_0 is crucial for the weighting scheme introduced later. We find that the value of $P_0 = 40\,000\,h^{-3}\,\mathrm{Mpc^3}$ (corresponding to the value of the galaxy power spectrum at $k \approx 0.06\,h\,\mathrm{Mpc^{-1}}$ in 6dFGS) minimizes the error of the correlation function near the BAO peak.

Using $P_0 = 40\,000\,h^{-3}\,\mathrm{Mpc^3}$ yields an effective volume of $0.08\,h^{-3}\,\mathrm{Gpc^3}$, while using instead $P_0 = 10\,000\,h^{-3}\,\mathrm{Mpc^3}$ (corresponding to $k \approx 0.15h\,\mathrm{Mpc^{-1}}$) gives an effective volume of $0.045\,h^{-3}\,\mathrm{Gpc^3}$.

The volume of the 6dFGS is approximately as large as the volume covered by the 2dFGRS, with a sample density similar to SDSS-DR7 (Abazajian et al. 2009). Percival et al. (2010) reported successful BAO detections in several samples obtained from a combination of SDSS DR7, SDSS-LRG and 2dFGRS with effective volumes in the range $0.15-0.45\ h^{-3}\ {\rm Gpc}^3$ (using $P_0=10\ 000\ h^{-3}\ {\rm Mpc}^3$), while the original detection by Eisenstein et al. (2005) used a sample with $V_{\rm eff}=0.38\ h^{-3}\ {\rm Gpc}^3$ (using $P_0=40\ 000\ h^{-3}\ {\rm Mpc}^3$).

3 CLUSTERING MEASUREMENT

We focus our analysis on the two-point correlation function. In the following subsections we introduce the technique used to estimate the correlation function and outline the method of lognormal realizations, which we employed to derive a covariance matrix for our measurement.

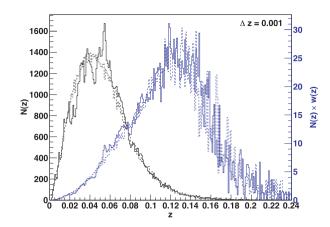


Figure 1. Redshift distribution of the data (black solid line) and the random catalogue (black dashed line). The weighted distribution (using weights from equation 6) is shifted to higher redshift and has increased shot noise, but a smaller error due to sample variance (blue solid and dashed lines).

3.1 Random catalogues

To calculate the correlation function, we need a random sample of galaxies which follows the same angular and redshift selection function as the 6dFGS sample. We base our random catalogue generation on the 6dFGS luminosity function of Jones et al. (in preparation), where we use random numbers to pick volume-weighted redshifts and luminosity-function-weighted absolute magnitudes. We then test whether the redshift-magnitude combination falls within the 6dFGS K-band faint and bright apparent magnitude limits (8.75 $\leq K < 12.9$).

Fig. 1 shows the redshift distribution of the 6dFGS *K*-selected sample (black solid line) compared to a random catalogue with the same number of galaxies (black dashed line). The random catalogue is a good description of the 6dFGS redshift distribution in both the weighted and unweighted case.

3.2 The correlation function

We turn the measured redshift into comoving distance via

$$D_C(z) = \frac{c}{H_0} \int_0^z \frac{dz'}{E(z')}$$
 (2)

with

$$E(z) = \left[\Omega_{\rm m}^{\rm fid}(1+z)^3 + \Omega_{k}^{\rm fid}(1+z)^2 + \Omega_{k}^{\rm fid}(1+z)^{3(1+w^{\rm fid})}\right]^{1/2},\tag{3}$$

where the curvature $\Omega_k^{\rm fid}$ is set to zero, the dark energy density is given by $\Omega_{\rm A}^{\rm fid}=1-\Omega_{\rm m}^{\rm fid}$ and the equation of state for dark energy is $w^{\rm fid}=-1$. Because of the very low redshift of 6dFGS, our data are not very sensitive to Ω_k , w or any other higher dimensional parameter which influences the expansion history of the Universe. We will discuss this further in Section 5.3.

Now we measure the separation between all galaxy pairs in our survey and count the number of such pairs in each separation bin. We do this for the 6dFGS data catalogue, a random catalogue with the same selection function and a combination of data–random pairs. We call the pair-separation distributions obtained from this analysis DD(s), RR(s) and DR(s), respectively. The binning is chosen to be from $10 \, h^{-1}$ Mpc up to $190 \, h^{-1}$ Mpc, in $10 \, h^{-1}$ Mpc steps. In the analysis, we used 30 random catalogues with the same size as the

data catalogue. The redshift correlation function itself is given by Landy & Szalay (1993):

$$\xi^{\text{data}}(s) = 1 + \frac{\text{DD}(s)}{\text{RR}(s)} \left(\frac{n_{\text{r}}}{n_{\text{d}}}\right)^{2} - 2\frac{\text{DR}(s)}{\text{RR}(s)} \left(\frac{n_{\text{r}}}{n_{\text{d}}}\right),\tag{4}$$

where the ratio n_r/n_d is given by

$$\frac{n_{\rm r}}{n_{\rm d}} = \frac{\sum_{i}^{N_{\rm r}} w_i(\mathbf{x})}{\sum_{j}^{N_{\rm d}} w_j(\mathbf{x})},\tag{5}$$

and the sums go over all random (N_r) and data (N_d) galaxies. We use the inverse density weighting of Feldman, Kaiser & Peacock (1994):

$$w_i(x) = \frac{C_i}{1 + n(x)P_0},\tag{6}$$

with $P_0 = 40\,000\,h^3\,{\rm Mpc^{-3}}$ and C_i being the inverse completeness weighting for 6dFGS (see Section 2.1 and Jones et al., in preparation). This weighting is designed to minimize the error on the BAO measurement, and since our sample is strongly limited by sample variance on large scales, this weighting results in a significant improvement to the analysis. The effect of the weighting on the redshift distribution is illustrated in Fig. 1.

Other authors have used the so-called J_3 -weighting which optimizes the error over all scales by weighting each scale differently (e.g. Efstathiou 1988; Loveday et al. 1995). In a magnitude limited sample, there is a correlation between luminosity and redshift, which establishes a correlation between bias and redshift (Zehavi et al. 2005). A scale-dependent weighting would imply a different effective redshift for each scale, causing a scale-dependent bias.

Finally, we considered a luminosity-dependent weighting as suggested by Percival, Verde & Peacock (2004). However, the same authors found that explicitly accounting for the luminosity-redshift relation has a negligible effect for 2dFGRS. We found that the effect to the 6dFGS correlation function is $\ll 1\sigma$ for all bins. Hence the static weighting of equation (6) is sufficient for our data set.

We also include an integral constraint correction in the form of

$$\xi^{\text{final}}(s) = \xi^{\text{data}}(s) + ic, \tag{7}$$

where ic is defined as

$$ic = \frac{\sum_{s} RR(s)\xi(s)}{\sum_{s} RR(s)}.$$
 (8)

The function RR(s) is calculated from our mock catalogue, and $\xi(s)$ is a correlation function model. Since ic depends on the model of the correlation function, we have to recalculate it at each step during the fitting procedure. However, we note that ic has no significant impact to the final result.

Fig. 2 shows the correlation function of 6dFGS at large scales. The BAO peak at $105 \, h^{-1}$ Mpc is clearly visible. The plot includes model predictions of different cosmological parameter sets. We will discuss these models in Section 5.2.

3.3 Lognormal error estimate

To obtain reliable error bars for the correlation function, we use lognormal realizations (Coles & Jones 1991; Cole et al. 2005; Kitaura, Jasche & Metcalf 2009). In what follows, we summarize the main steps, but refer the interested reader to Appendix A in which we give a detailed explanation of how we generate the lognormal mock catalogues. In Appendix B, we compare the lognormal errors with jackknife estimates.

Lognormal realizations of a galaxy survey are usually obtained by deriving a density field from a model power spectrum, P(k),

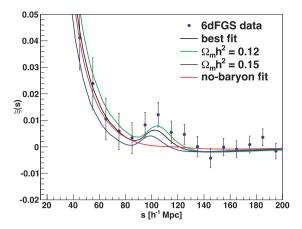


Figure 2. The large-scale correlation function of 6dFGS. The best-fitting model is shown by the black line with the best-fitting value of $\Omega_{\rm m}\,h^2=0.135\pm0.020$. Models with different $\Omega_{\rm m}\,h^2$ are shown by the green line $(\Omega_{\rm m}\,h^2=0.12)$ and the blue line $(\Omega_{\rm m}\,h^2=0.15)$. The red line is a linear CDM model with $\Omega_{\rm b}\,h^2=0$ (and $\Omega_{\rm m}\,h^2=0.1$), while all other models use the WMAP-7 best-fitting value of $\Omega_{\rm b}\,h^2=0.022\,27$ (Komatsu et al. 2011). The significance of the BAO detection in the black line relative to the red one is 2.4σ (see Section 7). The error bars at the data points are the diagonal elements of the covariance matrix derived using lognormal mock catalogues.

assuming Gaussian fluctuations. This density field is then Poisson sampled, taking into account the window function and the total number of galaxies. The assumption that the input power spectrum has Gaussian fluctuations can only be used in a model for a density field with overdensities $\ll 1$. As soon as we start to deal with finite rms fluctuations, the Gaussian model assigns a non-zero probability to regions of negative density. A lognormal random field LN(x), can avoid this unphysical behaviour. It is obtained from a Gaussian field G(x) by

$$LN(x) = \exp[G(x)] \tag{9}$$

which is positive-definite but approaches 1 + G(x) whenever the perturbations are small (e.g. at large scales). Calculating the power spectrum of a Poisson sampled density field with such a distribution will reproduce the input power spectrum convolved with the window function. As an input power spectrum for the lognormal field, we use

$$P_{\rm nl}(k) = A P_{\rm lin}(k) \exp[-(k/k_*)^2]$$
(10)

where $A = b^2(1 + 2\beta/3 + \beta^2/5)$ accounts for the linear bias and the linear redshift-space distortions. $P_{\text{lin}}(k)$ is a linear model power spectrum in real space obtained from CAMB (Lewis, Challinor & Lasenby 2000) and $P_{\text{nl}}(k)$ is the non-linear power spectrum in redshift space. Comparing the model above with the 6dFGS data gives A = 4. The damping parameter k_* is set to $k_* = 0.33h\,\text{Mpc}^{-1}$, as found in 6dFGS (see fitting results later). How well this input model matches the 6dFGS data can be seen in Fig. 9.

We produce 200 such realizations and calculate the correlation function for each of them, deriving a covariance matrix

$$C_{ij} = \sum_{n=1}^{N} \frac{[\xi_n(s_i) - \overline{\xi}(s_i)][\xi_n(s_j) - \overline{\xi}(s_j)]}{N - 1}.$$
 (11)

Here, $\xi_n(s_i)$ is the correlation function estimate at separation s_i and the sum goes over all N lognormal realizations. The mean value is

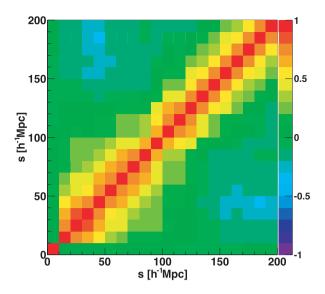


Figure 3. Correlation matrix derived from a covariance matrix calculated from 200 lognormal realizations.

defined as

$$\overline{\xi}(s_i) = \frac{1}{N} \sum_{n=1}^{N} \xi_n(s_i).$$
 (12)

The case i = j gives the error (ignoring correlations between bins, $\sigma_i^2 = C_{ii}$). In the following, we will use this uncertainty in all diagrams, while the fitting procedures use the full covariance matrix.

The distribution of recovered correlation functions includes the effects of sample variance and shot noise. Non-linearities are also approximately included since the distribution of overdensities is skewed.

In Fig. 3 we show the lognormal correlation matrix r_{ij} calculated from the covariance matrix. The correlation matrix is defined as

$$r_{ij} = \frac{C_{ij}}{\sqrt{C_{ii}C_{jj}}},\tag{13}$$

where C is the covariance matrix (for a comparison to jackknife errors, see appendix B).

4 MODELLING THE BAO SIGNAL

In this section we will discuss wide-angle effects and non-linearities. We also introduce a model for the large-scale correlation function, which we later use to fit our data.

4.1 Wide-angle formalism

The model of linear redshift-space distortions introduced by Kaiser (1987) is based on the plane-parallel approximation. Earlier surveys such as SDSS and 2dFGRS are at sufficiently high redshift that the maximum opening angle between a galaxy pair remains small enough to ensure the plane-parallel approximation is valid. However, the 6dFGS has a maximum opening angle of 180° and a lower mean redshift of $z\approx 0.1$ (for our weighted sample) and so it is necessary to test the validity of the plane-parallel approximation. The wide-angle description of redshift-space distortions has been laid out in several papers (Szalay, Matsubara & Landy 1997; Matsubara 2004; Szapudi 2004; Papai & Szapudi 2008; Raccanelli, Samushia & Percival 2010), which we summarize in Appendix C.

We find that the wide-angle corrections have only a very minor effect on our sample. For our fiducial model, we found a correction of $\Delta\xi=4\times10^{-4}$ in amplitude at $100\,h^{-1}\,\mathrm{Mpc}$ and $\Delta\xi=4.5\times10^{-4}$ at $200\,h^{-1}\,\mathrm{Mpc}$, (Fig. C2 in the appendix). This is much smaller than the error bars on these scales. Despite the small size of the effect, we nevertheless include all first-order correction terms in our correlation function model. It is important to note that wide-angle corrections affect the correlation function amplitude only and do not cause any shift in the BAO scale. The effect of the wide-angle correction on the unweighted sample is much greater and is already noticeable on scales of $20\,h^{-1}\,\mathrm{Mpc}$. Weighting to higher redshifts mitigates the effect because it reduces the average opening angle between galaxy pairs, by giving less weight to wide-angle pairs (on average).

4.2 Non-linear effects

There are a number of non-linear effects which can potentially influence a measurement of the BAO signal. These include scale-dependent bias, the non-linear growth of structure on smaller scales, and redshift-space distortions. We discuss each of these in the context of our 6dFGS sample.

As the Universe evolves, the acoustic signature in the correlation function is broadened by non-linear gravitational structure formation. Equivalently, we can say that the higher harmonics in the power spectrum, which represent smaller scales, are erased (Eisenstein et al. 2007a).

The early Universe physics, which we discussed briefly in the introduction, is well understood and several authors have produced software packages (e.g. CMBFAST and CAMB) and published fitting functions (e.g. Eisenstein & Hu 1998) to make predictions for the correlation function and power spectrum using thermodynamical models of the early Universe. These models already include the basic linear physics most relevant for the BAO peak. In our analysis, we use the CAMB software package (Lewis et al. 2000). The non-linear evolution of the power spectrum in CAMB is calculated using the HALOFIT code (Smith et al. 2003). This code is calibrated by N-body simulations and can describe non-linear effects in the shape of the matter power spectrum for pure CDM models to an accuracy of around 5-10 per cent (Heitmann et al. 2010). However, it has previously been shown that this non-linear model is a poor description of the non-linear effects around the BAO peak (Crocce & Scoccimarro 2008). We therefore decided to use the linear model output from CAMB and incorporate the non-linear effects separately.

All non-linear effects influencing the correlation function can be approximated by a convolution with a Gaussian damping factor $\exp[-(rk_*/2)^2]$ (Eisenstein et al. 2007b,a), where k_* is the damping scale. We will use this factor in our correlation function model introduced in the next section. The convolution with a Gaussian causes a shift of the peak position to larger scales, since the correlation function is not symmetric around the peak. However this shift is usually very small.

All of the non-linear processes discussed so far are not at the fundamental scale of $105 \, h^{-1} \, \text{Mpc}$, but are instead at the cluster-formation scale of up to $10 \, h^{-1} \, \text{Mpc}$. The scale of $105 \, h^{-1} \, \text{Mpc}$ is far larger than any known non-linear effect in cosmology. This has led some authors to the conclusion that the peak will not be shifted significantly, but rather only blurred out. For example, Eisenstein et al. (2007a) have argued that any systematic shift of the acoustic scale in real space must be small ($\leq 0.5 \, \text{per cent}$), even at z = 0.

However, several authors report possible shifts of up to 1 per cent (Guzik & Bernstein 2007; Smith, Scoccimarro & Sheth 2007, 2008; Angulo et al. 2008). Crocce & Scoccimarro (2008) used renormalized perturbation theory and found per cent level shifts in the BAO peak. In addition to non-linear evolution, they found that mode coupling generates additional oscillations in the power spectrum, which are out of phase with the BAO oscillations predicted by linear theory. This leads to shifts in the scale of oscillation nodes with respect to a smooth spectrum. In real space, this corresponds to a peak shift towards smaller scales. Based on their results, Crocce & Scoccimarro (2008) propose a model to be used for the correlation function analysis at large scales. We will introduce this model in the next section.

4.3 Large-scale correlation function

To model the correlation function on large scales, we follow Crocce & Scoccimarro (2008) and Sanchez, Baugh & Angulo (2008), and adopt the following parametrization:¹

$$\xi^{\text{model}}(s) = B(s)b^2 \left[\xi(s) * G(r) + \xi_1^1(r)\xi'(s) \right]. \tag{14}$$

Here, we decouple the scale dependency of the bias B(s) and the linear bias b. G(r) is a Gaussian damping term, accounting for non-linear suppression of the BAO signal. $\xi(s)$ is the linear correlation function (including wide-angle description of redshift-space distortions; equation (C4) in the appendix). The second term in equation (14) accounts for the mode coupling of different Fourier modes. It contains $\xi'(s)$, which is the first derivative of the redshift-space correlation function, and $\xi^1_+(r)$, which is defined as

$$\xi_1^1(r) = \frac{1}{2\pi^2} \int_0^\infty dk \, k P_{\text{lin}}(k) j_1(rk), \tag{15}$$

with $j_1(x)$ being the spherical Bessel function of order 1. Sanchez et al. (2008) used an additional parameter $A_{\rm MC}$ which multiplies the mode-coupling term in equation (14). We found that our data are not good enough to constrain this parameter, and hence adopted $A_{\rm MC}=1$ as in the original model by Crocce & Scoccimarro (2008).

In practice, we generate linear model power spectra $P_{\text{lin}}(k)$ from CAMB and convert them into a correlation function using a Hankel transform:

$$\xi(r) = \frac{1}{2\pi^2} \int_0^\infty dk \, k^2 P_{\text{lin}}(k) j_0(rk), \tag{16}$$

where $j_0(x) = \sin(x)/x$ is the spherical Bessel function of order 0.

The '*' symbol in equation (14) is only equivalent to a convolution in the case of a 3D correlation function, where we have the Fourier theorem relating the 3D power spectrum to the correlation function. In case of the spherically averaged quantities, this is not true. Hence, the '*' symbol in our equation stands for the multiplication of the power spectrum with $\tilde{G}(k)$ before transforming it into a correlation function. $\tilde{G}(k)$ is defined as

$$\tilde{G}(k) = \exp[-(k/k_*)^2],$$
(17)

with the property

$$\tilde{G}(k) \to 0 \text{ as } k \to \infty.$$
 (18)

The damping scale k_* can be calculated from linear theory (Crocce & Scoccimarro 2006; Matsubara 2008) by

$$k_* = \left[\frac{1}{6\pi^2} \int_0^\infty dk \, P_{\text{lin}}(k) \right]^{-1/2},\tag{19}$$

where $P_{\rm lin}(k)$ is again the linear power spectrum. $\Lambda {\rm CDM}$ predicts a value of $k_* \simeq 0.17 \, h \, {\rm Mpc}^{-1}$. However, we will include k_* as a free fitting parameter.

The scale dependence of the 6dFGS bias, B(s), is derived from the GiggleZ simulation (Poole et al., in preparation); a dark matter simulation containing 2160³ particles in a 1 h^{-1} Gpc box. We rank-order the haloes of this simulation by $V_{\rm max}$ and choose a contiguous set of 250 000 of them, selected to have the same clustering amplitude of 6dFGS as quantified by the separation scale r_0 , where $\xi(r_0) = 1$. In the case of 6dFGS, we found $r_0 = 9.3 h^{-1}$ Mpc. Using the redshift-space correlation function of these haloes and of a randomly subsampled set of $\sim 10^6$ dark matter particles, we obtain

$$B(s) = 1 + (s/0.474 \, h^{-1} \text{Mpc})^{-1.332}, \tag{20}$$

which describes a 1.7 per cent correction of the correlation function amplitude at separation scales of $10\,h^{-1}$ Mpc. To derive this function, the GiggleZ correlation function (snapshot z=0) has been fitted down to $6\,h^{-1}$ Mpc, well below the smallest scales we are interested in.

5 EXTRACTING THE BAO SIGNAL

In this section, we fit the model correlation function developed in the previous section to our data. Such a fit can be used to derive the distance scale $D_V(z_{\rm eff})$ at the effective redshift of the survey.

5.1 Fitting preparation

The effective redshift of our sample is determined by

$$z_{\text{eff}} = \sum_{i}^{N_{b}} \sum_{i}^{N_{b}} \frac{w_{i} w_{j}}{2N_{b}^{2}} (z_{i} + z_{j}), \tag{21}$$

where $N_{\rm b}$ is the number of galaxies in a particular separation bin and w_i and w_j are the weights for those galaxies from equation (6). We choose $z_{\rm eff}$ from bin 10 which has the limits $100\,h^{-1}$ Mpc and $110\,h^{-1}$ Mpc and which gave $z_{\rm eff}=0.106$. Other bins show values very similar to this, with a standard deviation of ± 0.001 . The final result does not depend on a very precise determination of $z_{\rm eff}$, since we are not constraining a distance to the mean redshift, but a distance ratio [see equation (24), later]. In fact, if the fiducial model is correct, the result is completely independent of $z_{\rm eff}$. Only if there is a z-dependent deviation from the fiducial model do we need $z_{\rm eff}$ to quantify this deviation at a specific redshift.

Along the line of sight, the BAO signal directly constrains the Hubble constant H(z) at redshift z. When measured in a redshift shell, it constrains the angular diameter distance $D_A(z)$ (Matsubara 2004). In order to separately measure $D_A(z)$ and H(z), we require a BAO detection in the 2D correlation function, where it will appear as a ring at around $105 h^{-1}$ Mpc. Extremely large volumes are necessary for such a measurement. While there are studies that report a successful (but very low signal-to-noise ratio) detection in the 2D correlation function using the SDSS-LRG data (e.g. Gaztanaga et al. 2009; Chuang & Wang 2011, but see also Kazin et al. 2010b), our sample does not allow this kind of analysis. Hence we restrict ourselves to the 1D correlation function, where we measure a combination of $D_A(z)$ and H(z). What we actually measure is a superposition of two angular measurements (RA and Dec.) and one line-of-sight measurement (redshift). To account for this mixture of measurements, it is common to report the BAO distance constraints

¹ Note that r = s, the different letters just specify whether the function is evaluated in redshift space or real space.

as (Eisenstein et al. 2005; Padmanabhan & White 2008)

$$D_V(z) = \left[(1+z)^2 D_A^2(z) \frac{cz}{H_0 E(z)} \right]^{1/3}, \tag{22}$$

where D_A is the angular distance, which in the case of $\Omega_k = 0$ is given by $D_A(z) = D_C(z)/(1+z)$.

To derive model power spectra from CAMB, we have to specify a complete cosmological model, which in the case of the simplest Λ CDM model ($\Omega_k = 0, w = -1$) is specified by six parameters: $\omega_c, \omega_b, n_s, \tau, A_s$ and h. These parameters are the physical cold dark matter and baryon density ($\omega_c = \Omega_c h^2, \omega_b = \Omega_b h^2$), the scalar spectral index (n_s), the optical depth at recombination (τ), the scalar amplitude of the CMB temperature fluctuation (A_s) and the Hubble constant in units of $100 \, \mathrm{km \, s^{-1} \, Mpc^{-1}}$ (h).

Our fit uses the parameter values from WMAP-7 (Komatsu et al. 2011): $\Omega_b h^2 = 0.022\,27$, $\tau = 0.085$ and $n_s = 0.966$ (maximum likelihood values). The scalar amplitude A_s is set so that it results in $\sigma_8 = 0.8$, which depends on $\Omega_{\rm m}\,h^2$. However, σ_8 is degenerated with the bias parameter b which is a free parameter in our fit. Furthermore, h is set to 0.7 in the fiducial model, but can vary freely in our fit through a scale-distortion parameter α , which enters the model as

$$\xi^{\text{final}}(s) = \xi^{\text{model}}(\alpha s). \tag{23}$$

This parameter accounts for deviations from the fiducial cosmological model, which we use to derive distances from the measured redshift. It is defined as (Eisenstein et al. 2005; Padmanabhan & White 2008)

$$\alpha = \frac{D_V(z_{\text{eff}})}{D_V^{\text{fid}}(z_{\text{eff}})}.$$
 (24)

The parameter α enables us to fit the correlation function derived with the fiducial model, without the need to recalculate the correlation function for every new cosmological parameter set.

At low redshift we can approximate $H(z) \approx H_0$, which results in

$$\alpha \approx \frac{H_0^{\text{fid}}}{H_0}.\tag{25}$$

Compared to the correct equation (24) this approximation has an error of about 3 per cent at redshift z = 0.1 for our fiducial model. Since this is a significant systematic bias, we do not use this approximation at any point in our analysis.

5.2 Extracting $D_V(z_{eff})$ and $r_s(z_d)/D_V(z_{eff})$

Using the model introduced above we performed fits to 18 data points between 10 and $190\,h^{-1}\,\mathrm{Mpc}$. We excluded the data below $10\,h^{-1}\,\mathrm{Mpc}$, since our model for non-linearities is not good enough to capture the effects on such scales. The upper limit is chosen to be well above the BAO scale, although the constraining contribution of the bins above $130\,h^{-1}\,\mathrm{Mpc}$ is very small. Our final model has four free parameters: $\Omega_{\mathrm{m}}\,h^2$, b, α and k_* .

The best fit corresponds to a minimum χ^2 of 15.7 with 14 degrees of freedom (d.o.f.) (18 data points and four free parameters). The best-fitting model is included in Fig. 2 (black line). The parameter values are $\Omega_{\rm m} h^2 = 0.135 \pm 0.020$, $b = 1.65 \pm 0.10$ and $\alpha = 1.039 \pm 0.062$, where the errors are derived for each parameter by marginalizing over all other parameters. For k_* , we can give a lower limit of $k_* = 0.19h$ Mpc⁻¹ (with 95 per cent confidence level).

We can use equation (24) to turn the measurement of α into a measurement of the distance to the effective redshift $D_V(z_{\rm eff}) = \alpha D_V^{\rm fid}(z_{\rm eff}) = 457 \pm 27 \, {\rm Mpc}$, with a precision of 5.9 per cent. Our

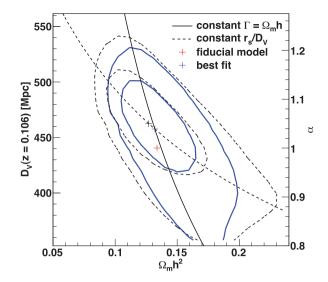


Figure 4. Likelihood contours of the distance $D_V(z_{\rm eff})$ against $\Omega_{\rm m} h^2$. The corresponding values of α are given on the right-hand axis. The contours show 1σ and 2σ errors for both a full fit (blue solid contours) and a fit over $20-190 \, h^{-1}$ Mpc (black dashed contours) excluding the first data point. The black cross marks the best-fitting values corresponding to the dashed black contours with $(D_V, \Omega_{\rm m} h^2) = (462, 0.127)$, while the blue cross marks the best-fitting values for the blue contours. The black solid curve corresponds to a constant $\Omega_{\rm m} h^2 D_V(z_{\rm eff})$ $(D_V \sim h^{-1})$, while the dashed line corresponds to a constant angular size of the sound horizon, as described in the text.

fiducial model gives $D_V^{\rm fid}(z_{\rm eff}) = 440.5$ Mpc, where we have followed the distance definitions of Wright (2006) throughout. For each fit we derive the parameter $\beta = \Omega_{\rm m}(z)^{0.545}/b$, which we need to calculate the wide-angle corrections for the correlation function.

The maximum likelihood distribution of k_* seems to prefer smaller values than predicted by Λ CDM, although we are not able to constrain this parameter very well. This is connected to the high significance of the BAO peak in the 6dFGS data (see Section 7). A smaller value of k_* damps the BAO peak and weakens the distance constraint. For comparison, we also performed a fit fixing k_* to the Λ CDM prediction of $k_* \simeq 0.17 \, h\, {\rm Mpc}^{-1}$. We found that the error on the distance $D_V(z_{\rm eff})$ increases from 5.9 to 8 per cent. However, since the data do not seem to support such a small value of k_* , we prefer to marginalize over this parameter.

The contours of $D_V(z_{\text{eff}}) - \Omega_{\text{m}} h^2$ are shown in Fig. 4, together with two degeneracy predictions (Eisenstein et al. 2005). The solid line is that of constant $\Omega_{\rm m} h^2 D_V(z_{\rm eff})$, which gives the direction of degeneracy for a pure CDM model, where only the shape of the correlation function contributes to the fit, without a BAO peak. The dashed line corresponds to a constant $r_s(z_d)/D_V(z_{eff})$, which is the degeneracy if only the position of the acoustic scale contributes to the fit. The dashed contours exclude the first data point, fitting from 20 to 190 h^{-1} Mpc only, with the best-fitting values $\alpha = 1.050 \pm 1.050$ 0.075 [corresponding to $D_V(z_{\text{eff}}) = 462 \pm 33 \,\text{Mpc}$], $\Omega_{\text{m}} h^2 = 0.127$ \pm 0.025 and $b = 1.59 \pm 0.15$. The contours of this fit are tilted towards the dashed line, which means that the fit is now driven by the BAO peak, while the general fit (solid contours) seems to have some contribution from the shape of the correlation function. Excluding the first data point increases the error on the distance constraint only slightly from 5.9 to 7.1 per cent. The value of $\Omega_{\rm m} h^2$ tends to be smaller, but agrees within 1σ with the former value.

Going back to the complete fit from 10 to $190 h^{-1}$ Mpc, we can include an external prior on $\Omega_{\rm m} h^2$ from WMAP-7, which carries an error of only 4 per cent (compared to the ≈ 15 per cent we

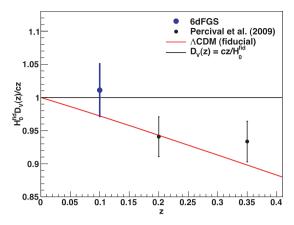


Figure 5. The distance measurement $D_V(z)$ relative to a low-redshift approximation. The points show 6dFGS data and those of Percival et al. (2010).

obtain by fitting our data). Marginalizing over $\Omega_{\rm m} h^2$ now gives $D_V(z_{\rm eff}) = 459 \pm 18$ Mpc, which reduces the error from 5.9 to 3.9 per cent. The uncertainty in $\Omega_{\rm m} h^2$ from WMAP-7 contributes only about 5 per cent of the error in D_V [assuming no error in the WMAP-7 value of $\Omega_{\rm m} h^2$ results in $D_V(z_{\rm eff}) = 459 \pm 17$ Mpc].

In Fig. 5 we plot the ratio $D_V(z)/D_V^{\text{low}-z}(z)$ as a function of redshift, where $D_V^{\text{low}-z}(z) = cz/H_0$. At sufficiently low redshift, the approximation $H(z) \approx H_0$ is valid and the measurement is independent of any cosmological parameter except the Hubble constant. This figure also contains the results from Percival et al. (2010).

Rather than including the WMAP-7 prior on $\Omega_{\rm m} h^2$ to break the degeneracy between $\Omega_{\rm m} h^2$ and the distance constraint, we can fit the ratio $r_{\rm s}(z_{\rm d})/D_V(z_{\rm eff})$, where $r_{\rm s}(z_{\rm d})$ is the sound horizon at the baryon drag epoch $z_{\rm d}$. In principle, this is rotating Fig. 4 so that the dashed black line is parallel to the x-axis and hence breaks the degeneracy if the fit is driven by the BAO peak; it will be less efficient if the fit is driven by the shape of the correlation function. During the fit, we calculate $r_{\rm s}(z_{\rm d})$ using the fitting formula of Eisenstein & Hu (1998).

The best fit results in $r_{\rm s}(z_{\rm d})/D_V(z_{\rm eff})=0.336\pm0.015$, which has an error of 4.5 per cent, smaller than the 5.9 per cent found for D_V but larger than the error in D_V when adding the WMAP-7 prior on $\Omega_{\rm m} h^2$. This is caused by the small disagreement in the $D_V - \Omega_{\rm m} h^2$ degeneracy and the line of constant sound horizon in Fig. 4. The χ^2 is 15.7, similar to the previous fit with the same number of degrees of freedom.

5.3 Extracting $A(z_{eff})$ and $R(z_{eff})$

We can also fit for the ratio of the distance between the effective redshift, $z_{\rm eff}$, and the redshift of decoupling ($z_* = 1091$; Eisenstein et al. 2005):

$$R(z_{\text{eff}}) = \frac{D_V(z_{\text{eff}})}{(1 + z_*)D_A(z_*)},\tag{26}$$

with $(1+z_*)D_A(z_*)=D_C(z_*)^2$ being the CMB angular distance. Besides the fact that the Hubble constant H_0 cancels out in the determination of R, this ratio is also more robust against effects caused by possible extra relativistic species (Eisenstein & White 2004). We calculate $D_A(z_*)$ for each $\Omega_{\rm m}\,h^2$ during the fit and then marginalize over $\Omega_{\rm m}\,h^2$. The best fit results in $R=0.0324\pm0.0015$, with $\chi^2=15.7$ and the same 14 d.o.f.

Focusing on the path from z=0 to $z_{\rm eff}=0.106$, our data set can give interesting constraints on $\Omega_{\rm m}$. We derive the parameter (Eisenstein et al. 2005)

$$A(z_{\text{eff}}) = 100 D_V(z_{\text{eff}}) \frac{\sqrt{\Omega_{\text{m}} h^2}}{cz_{\text{eff}}},$$
(27)

which has no dependence on the Hubble constant since $D_V \propto h^{-1}$. We obtain $A(z_{\rm eff}) = 0.526 \pm 0.028$ with $\chi^2/{\rm d.o.f.} = 15.7/14$. The value of A would be identical to $\sqrt{\Omega_{\rm m}}$ if measured at redshift z=0. At redshift z=0.106, we obtain a deviation from this approximation of 6 per cent for our fiducial model, which is small but systematic. We can express A, including the curvature term Ω_k and the dark energy equation of state parameter w, as

$$A(z) = \frac{\sqrt{\Omega_{\rm m}}}{E(z)^{1/3}} \begin{cases} \left[\frac{\sinh\left(\sqrt{\Omega_k}\chi(z)\right)}{\sqrt{\Omega_k}z} \right]^{2/3} & \Omega_k > 0 \\ \left[\frac{\chi(z)}{z} \right]^{2/3} & \Omega_k = 0 \\ \left[\frac{\sin\left(\sqrt{|\Omega_k|}\chi(z)\right)}{\sqrt{|\Omega_k|}z} \right]^{2/3} & \Omega_k < 0 \end{cases}$$
 (28)

with

$$\chi(z) = D_C(z) \frac{H_0}{c} = \int_0^z \frac{dz'}{E(z')}$$
 (29)

and

$$E(z) = \left[\Omega_{\rm m}(1+z)^3 + \Omega_k(1+z)^2 + \Omega_{\Lambda}(1+z)^{3(1+w)}\right]^{1/2}.$$
(30)

Using this equation, we now linearize our result for $\Omega_{\rm m}$ in Ω_k and w, and get

$$\Omega_{\rm m} = 0.287 + 0.039(1+w) + 0.039\Omega_k \pm 0.027. \tag{31}$$

For comparison, Eisenstein et al. (2005) found

$$\Omega_{\rm m} = 0.273 + 0.123(1+w) + 0.137\Omega_k \pm 0.025 \tag{32}$$

based on the SDSS-LRG DR3 sample. This result shows the reduced sensitivity of the 6dFGS measurement to w and Ω_k .

6 COSMOLOGICAL IMPLICATIONS

In this section we compare our results to other studies and discuss the implications for constraints on cosmological parameters. We first note that we do not see any excess correlation on large scales as found in the SDSS-LRG sample. Our correlation function is in agreement with a crossover to negative scales at $140 \, h^{-1} \, \mathrm{Mpc}$, as predicted from $\Lambda \, \mathrm{CDM}$.

6.1 Constraining the Hubble constant, H_0

We now use the 6dFGS data to derive an estimate of the Hubble constant. We use the 6dFGS measurement of $r_{\rm s}(z_{\rm d})/D_V(0.106) = 0.336 \pm 0.015$ and fit directly for the Hubble constant and $\Omega_{\rm m}$. We combine our measurement with a prior on $\Omega_{\rm m}\,h^2$ coming from the WMAP-7 Markov Chain results (Komatsu et al. 2011). Combining the clustering measurement with $\Omega_{\rm m}\,h^2$ from the CMB corresponds to the calibration of the standard ruler.

We obtain values of $H_0 = 67 \pm 3.2 \, \mathrm{km \ s^{-1} \ Mpc^{-1}}$ (which has an uncertainty of only 4.8 per cent) and $\Omega_{\mathrm{m}} = 0.296 \pm 0.028$. Table 1 and Fig. 6 summarize the results. The value of Ω_{m} agrees with the value we derived earlier (Section 5.3).

² In case of $\Omega_k = 0$.

Table 1. All parameter constraints from 6dFGS obtained in this paper. The priors used to derive these parameters are listed in square brackets. All parameters assume $\Omega_b h^2 = 0.02227$, and in cases where a prior on $\Omega_{\rm m}\,h^2$ is used, we adopt the WMAP-7 Markov Chain probability distribution (Komatsu et al. 2011). $A(z_{\text{eff}})$ is the acoustic parameter defined by Eisenstein et al. (2005) [see equation (27) in the text] and $R(z_{\text{eff}})$ is the distance ratio of the 6dFGS BAO measurement to the last-scattering surface. The most sensible value for cosmological parameter constraints is $r_s(z_d)/D_V(z_{eff})$, since this measurement is uncorrelated with $\Omega_{\rm m} h^2$. The effective redshift of 6dFGS is $z_{\text{eff}} = 0.106$, and the fitting range is from 10 to 190 h^{-1} Mpc.

Summary of	f parameter	constraints	from	6dFGS
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$ \frac{\Omega_{\rm m} h^2}{D_V(z_{\rm eff})} \\ D_V(z_{\rm eff}) \\ P_V(z_{\rm eff}) \\ r_{\rm s}(z_{\rm d})/D_V(z_{\rm eff}) \\ R(z_{\rm eff}) $	0.135 ± 0.020 (14.8 per cent) 457 ± 27 Mpc (5.9 per cent) 459 ± 18 Mpc (3.9 per cent) 0.336 ± 0.015 (4.5 per cent) 0.0324 ± 0.0015 (4.6 per cent)	$[\Omega_{ m m}h^2$ prior]
$A(z_{ m eff})$ $\Omega_{ m m}$ H_0	0.526 ± 0.028 (5.3 per cent) 0.296 ± 0.028 (9.5 per cent) 67 ± 3.2 (4.8%)	$[\Omega_{\rm m} h^2 \text{ prior}]$ $[\Omega_{\rm m} \mathbf{h^2} \text{ prior}]$

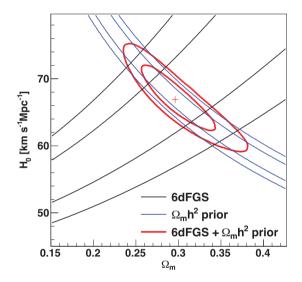


Figure 6. The blue contours show the WMAP-7 $\Omega_{\rm m} h^2$ prior (Komatsu et al. 2011). The black contour shows constraints from 6dFGS derived by fitting to the measurement of $r_s(z_d)/D_V(z_{eff})$. The solid red contours show the combined constraints resulting in $H_0 = 67 \pm 3.2 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ and $\Omega_{\rm m} = 0.296 \pm 0.028$. Combining the clustering measurement with $\Omega_{\rm m} h^2$ from the CMB corresponds to the calibration of the standard ruler.

To combine our measurement with the latest CMB data, we use the WMAP-7 distance priors, namely the acoustic scale

$$\ell_A = (1 + z_*) \frac{\pi D_A(z_*)}{r_s(z_*)},\tag{33}$$

the shift parameter

$$R = 100 \frac{\sqrt{\Omega_{\rm m} h^2}}{c} (1 + z_*) D_A(z_*)$$
 (34)

and the redshift of decoupling z_* (tables 9 and 10 in Komatsu et al. 2011). This combined analysis reduces the error further and yields $H_0 = 68.7 \pm 1.5 \, {\rm km \ s^{-1} \, Mpc^{-1}}$ (2.2 per cent) and $\Omega_{\rm m} = 0.29 \pm 1.5 \, {\rm km \ s^{-1} \, Mpc^{-1}}$ 0.022 (7.6 per cent).

Percival et al. (2010) determine a value $H_0 = 68.6 \pm 2.2 \,\mathrm{km}$ s⁻¹ Mpc⁻¹ using SDSS-DR7, SDSS-LRG and 2dFGRS, while Reid et al. (2010) found $69.4 \pm 1.6 \,\mathrm{km}\,\mathrm{s}^{-1}\,\mathrm{Mpc}^{-1}$ using the SDSS-LRG sample and WMAP-5. In contrast to these results, 6dFGS is less affected by parameters like Ω_k and w because of its lower redshift. In any case, our result of the Hubble constant agrees very well with earlier BAO analyses. Furthermore, our result agrees with the latest CMB measurement of $H_0 = 70.3 \pm 2.5 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$ (Komatsu et al. 2011).

The SH0ES programme (Riess et al. 2011) determined the Hubble constant using the distance ladder method. They used about 600 near-IR observations of Cepheids in eight galaxies to improve the calibration of 240 low-redshift (z < 0.1) Type Ia supernova, and calibrated the Cepheid distances using the geometric distance to the maser galaxy NGC 4258. They found $H_0 = 73.8 \pm 10^{-2}$ 2.4 km s⁻¹ Mpc⁻¹, a value consistent with the initial results of the Hubble Key project ($H_0 = 72 \pm 8 \,\mathrm{km}\,\mathrm{s}^{-1}\,\mathrm{Mpc}^{-1}$; Freedman et al. 2001), but 1.7σ higher than our value (and 1.8σ higher when we combine our data set with WMAP-7). While this could point towards unaccounted or underestimated systematic errors in either one of the methods, the likelihood of such a deviation by chance is about 10 per cent and hence is not enough to represent a significant discrepancy. Possible systematic errors affecting the BAO measurements are the modelling of non-linearities, bias and redshift-space distortions, although these systematics are not expected to be significant at the large scales relevant to our analysis.

To summarize the finding of this section, we can state that our measurement of the Hubble constant is competitive with the latest result of the distance ladder method. The different techniques employed to derive these results have very different potential systematic errors. Furthermore, we found that BAO studies provide the most accurate measurement of H_0 that exists, when combined with the CMB distance priors.

6.2 Constraining dark energy

One key problem driving current cosmology is the determination of the dark energy equation of state parameter, w. When adding additional parameters like w to Λ CDM, we find large degeneracies in the WMAP-7-only data. One example is shown in Fig. 7. WMAP-7

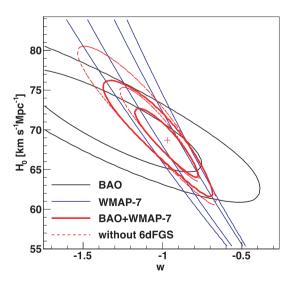


Figure 7. The blue contours shows the WMAP-7 degeneracy in H_0 and w (Komatsu et al. 2011), highlighting the need for a second data set to break the degeneracy. The black contours show constraints from BAO data incorporating the $r_s(z_d)/D_V(z_{eff})$ measurements of Percival et al. (2010) and 6dFGS. The solid red contours show the combined constraints resulting in $w = -0.97 \pm 0.13$. Excluding the 6dFGS data point widens the constraints to the dashed red line with $w = -1.01 \pm 0.17$.

Table 2. *w*CDM constraints from different data sets. Comparing the two columns shows the influence of the 6dFGS data point. The 6dFGS data point reduces the error on *w* by 24 per cent compared to *WMAP-7+LRG* which contains only the BAO data points of Percival et al. (2010). We assume flat priors of $0.11 < \Omega_{\rm m} \, h^2 < 0.16$ and marginalize over $\Omega_{\rm m} \, h^2$. The asterisks denote the free parameters in each fit.

Parameter	WMAP-7+LRG	WMAP-7+LRG+6dFGS
H_0 $\Omega_{ m m}$ Ω_{Λ} w	$69.9 \pm 3.8(*)$ 0.283 ± 0.033 0.717 ± 0.033 $-1.01 \pm 0.17(*)$	$68.7 \pm 2.8(*)$ 0.293 ± 0.027 0.707 ± 0.027 $-0.97 \pm 0.13(*)$

alone cannot constrain H_0 or w within sensible physical boundaries (e.g. w < -1/3). As we are sensitive to H_0 , we can break the degeneracy between w and H_0 inherent in the CMB-only data. Our assumption of a fiducial cosmology with w = -1 does not introduce a bias, since our data are not sensitive to this parameter and any deviation from this assumption is modelled within the shift parameter α .

We again use the WMAP-7 distance priors introduced in the last section. In addition to our value of $r_s(z_d)/D_V(0.106)=0.336\pm0.015$, we use the results of Percival et al. (2010), who found $r_s(z_d)/D_V(0.2)=0.1905\pm0.0061$ and $r_s(z_d)/D_V(0.35)=0.1097\pm0.0036$. To account for the correlation between the two latter data points, we employ the covariance matrix reported in their paper. Our fit has three free parameters: $\Omega_{\rm m} h^2$, H_0 and w.

The best fit gives $w=-0.97\pm0.13$, $H_0=68.7\pm2.8\,\mathrm{km\,s^{-1}\,Mpc^{-1}}$ and $\Omega_\mathrm{m}\,h^2=0.1380\pm0.0055$, with a $\chi^2/\mathrm{d.o.f.}=1.3/3$. Table 2 and Fig. 7 summarize the results. To illustrate the importance of the 6dFGS result to the overall fit, we also show how the results change if 6dFGS is omitted. The 6dFGS data improve the constraint on w by 24 per cent.

Finally we show the best-fitting cosmological parameters for different cosmological models using *WMAP-7* and BAO results in Table 3.

7 SIGNIFICANCE OF THE BAO DETECTION

To test the significance of our detection of the BAO signature, we follow Eisenstein et al. (2005) and perform a fit with a fixed $\Omega_b=0$, which corresponds to a pure CDM model without a BAO signature. The best fit has $\chi^2=21.4$ with 14 d.o.f. and is shown as the red line in Fig. 2. The parameter values of this fit depend on the parameter priors, which we set to $0.7<\alpha<1.3$ and $0.1<\Omega_m$ $h^2<0.2$. Values of α much further away from 1 are problematic since equation (24) is only valid for α close to 1. Comparing the

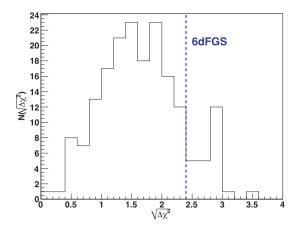


Figure 8. The number of lognormal realizations found with a certain $\sqrt{\Delta\chi^2}$, where the $\Delta\chi^2$ is obtained by comparing a fit using a ΛCDM correlation function model with a no-baryon model. The blue line indicates the 6dFGS result.

best pure CDM model with our previous fit, we estimate that the BAO signal is detected with a significance of 2.4σ (corresponding to $\Delta \chi^2 = 5.6$). As a more qualitative argument for the detection of the BAO signal we would like to refer again to Fig. 4 where the direction of the degeneracy clearly indicates the sensitivity to the BAO peak.

We can also use the lognormal realizations to determine how likely it is to find a BAO detection in a survey like 6dFGS. To do this, we produced 200 lognormal mock catalogues and calculated the correlation function for each of them. We can now fit our correlation function model to these realizations. Furthermore, we fit a no-baryon model to the correlation function and calculate $\Delta\chi^2$, the distribution of which is shown in Fig. 8. We find that 26 per cent of all realizations have *at least* a 2σ BAO detection, and that 12 per cent have a detection >2.4 σ . The lognormal realizations show a mean significance of the BAO detection of $1.7 \pm 0.7\sigma$, where the error describes the variance around the mean.

Fig. 9 shows the 6dFGS data points together with all 200 lognormal realizations (grey). The red data points indicate the mean for each bin, and the black line is the input model derived as explained in Section 3.3. This comparison shows that the 6dFGS data contain a BAO peak slightly larger than expected in ΛCDM.

The amplitude of the acoustic feature relative to the overall normalization of the galaxy correlation function is quite sensitive to the baryon fraction, $f_b = \Omega_b/\Omega_m$ (Matsubara 2004). A higher BAO peak could hence point towards a larger baryon fraction in the local universe. However, since the correlation function model seems to agree very well with the data (with a reduced χ^2 of 1.12) and is within the range spanned by our lognormal realizations, we

Table 3. Parameter constraints from WMAP7+BAO for (i) a flat Λ CDM model, (ii) an open Λ CDM (o Λ CDM), (iii) a flat model with w= constant (wCDM) and (iv) an open model with w= constant (owCDM). We assume flat priors of $0.11<\Omega_{\rm m}$ $h^2<0.16$ and marginalize over $\Omega_{\rm m}$ h^2 . The asterisks denote the free parameters in each fit.

Parameter	ΛCDM	oΛCDM	wCDM	owCDM
H_0 $\Omega_{ m m}$	$69.2 \pm 1.1(*)$ 0.288 ± 0.011	$68.3 \pm 1.7(*)$ 0.290 ± 0.019	$68.7 \pm 2.8(*)$ 0.293 ± 0.027	$70.4 \pm 4.3(*)$ 0.274 ± 0.035
$egin{array}{l} \Omega_k \ \Omega_{\Lambda} \ w \end{array}$	(0) 0.712 ± 0.011 (-1)	$-0.0036 \pm 0.0060(*)$ 0.714 ± 0.020 (-1)	$(0) \\ 0.707 \pm 0.027 \\ -0.97 \pm 0.13(*)$	$-0.013 \pm 0.010(*)$ 0.726 ± 0.036 $-1.24 \pm 0.39(*)$

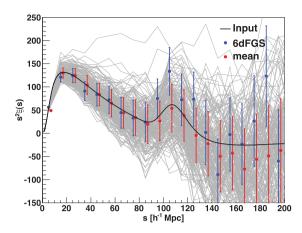


Figure 9. The different lognormal realizations used to calculate the covariance matrix (shown in grey). The red points indicate the mean values, while the blue points show actual 6dFGS data (the data point at $5 h^{-1}$ Mpc is not included in the fit). The red data points are shifted by $2 h^{-1}$ Mpc to the right for clarity.

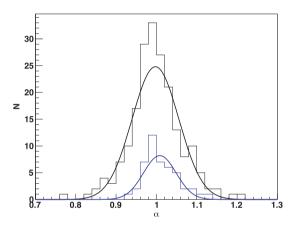


Figure 10. This plot shows the distribution of the parameter α derived from the 200 lognormal realizations (black). The distribution is well fitted by a Gaussian with a mean of $\mu=0.998\pm0.004$ and a width of $\sigma=0.057\pm0.005$. In blue we show the same distribution selecting only the lognormal realizations with a strong BAO peak (>2 σ). The Gaussian distribution in this case gives a mean of 1.007 \pm 0.007 and $\sigma=0.041\pm0.008$.

cannot claim any discrepancy with Λ CDM. Therefore, the most likely explanation for the excess correlation in the BAO peak is sample variance.

In Fig. 10 we show the distribution of the parameter α obtained from the 200 lognormal realizations. The distribution is well described by a Gaussian with $\chi^2/\text{d.o.f.} = 14.2/20$, where we employed Poisson errors for each bin. This confirms that α has Gaussian distributed errors in the approximation that the 6dFGS sample is well described by lognormal realizations of an underlying Λ CDM power spectrum. This result increases our confidence that the application of Gaussian errors for the cosmological parameter fits is correct. The mean of the Gaussian distribution is at 0.998 \pm 0.004, in agreement with unity, which shows that we are able to recover the input model. The width of the distribution shows the mean expected error in α in a Λ CDM universe for a 6dFGS-like survey. We found $\sigma = 0.057 \pm 0.005$, which is in agreement with our error in α of 5.9 per cent. Fig. 10 also contains the distribution of α , selecting only the lognormal realizations with a strong (>2 σ) BAO peak (blue data).

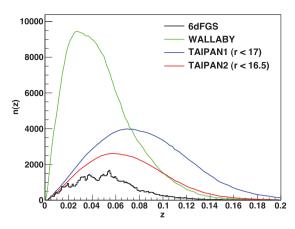


Figure 11. Redshift distribution of 6dFGS, WALLABY and two different versions of the proposed TAIPAN survey. See text for details.

We included this selection to show that a stronger BAO peak does not bias the estimate of α in any direction. The Gaussian fit gives χ^2 /d.o.f. = 5/11, with a mean of 1.007 \pm 0.007. The distribution of α shows a smaller spread with $\sigma = 0.041 \pm 0.008$, about 2σ below our error on α . This result shows that a survey like 6dFGS is able to constrain α (and hence D_V and H_0) to the precision we report in this paper.

8 FUTURE ALL SKY SURVEYS

A major new wide-sky survey of the local Universe will be the Wide field ASKAP L-band Legacy All-sky Blind surveY (WALLABY).³ This is a blind H I survey planned for the Australian Square Kilometre Array Pathfinder telescope (ASKAP), currently under construction at the Murchison Radio-astronomy Observatory in Western Australia.

The survey will cover at least 75 per cent of the sky with the potential to cover 4π of sky if the Westerbork Radio Telescope delivers complementary northern coverage. Compared to 6dFGS, WALLABY will more than double the sky coverage including the Galactic plane. WALLABY will contain $\sim\!500\,000\text{-}600\,000$ galaxies with a mean redshift of around 0.04, giving it around four times greater galaxy density compared to 6dFGS. In the calculations that follow, we assume for WALLABY a 4π survey without any exclusion around the Galactic plane. The effective volume in this case turns out to be $0.12\,h^{-3}\,\mathrm{Gpc}^3$.

The TAIPAN⁴ survey, proposed for the UK Schmidt Telescope at Siding Spring Observatory, will cover a comparable area of sky, and will extend 6dFGS in both depth and redshift ($z \simeq 0.08$).

The redshift distribution of both surveys is shown in Fig. 11, alongside 6dFGS. Since the TAIPAN survey is still in the early planning stage, we consider two realizations: TAIPAN1 (406 000 galaxies to a faint magnitude limit of r=17) and the shallower TAIPAN2 (221 000 galaxies to r=16.5). We have adopted the same survey window as was used for 6dFGS, meaning that it covers the whole southern sky excluding a 10° strip around the Galactic plane. The effective volumes of TAIPAN1 and TAIPAN2 are 0.23 and $0.13\,h^{-3}\,\mathrm{Gpc^3}$, respectively.

³ http://www.atnf.csiro.au/research/WALLABY

⁴ TAIPAN: Transforming Astronomical Imaging surveys through Polychromatic Analysis of Nebulae.

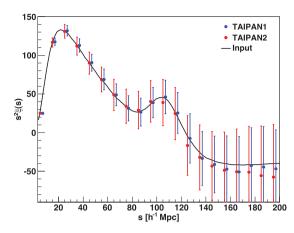


Figure 12. Predictions for two versions of the proposed TAIPAN survey. Both predictions assume a 2π -steradian southern sky-coverage, excluding the Galactic plane (i.e. $|b| > 10^{\circ}$). TAIPAN1 contains 406 000 galaxies while TAIPAN2 contains 221 000 (see Fig. 11). The blue points are shifted by $2\,h^{-1}$ Mpc to the right for clarity. The black line is the input model, which is a Λ CDM model with a bias of 1.6, $\beta=0.3$ and $k_*=0.17h\,\mathrm{Mpc}^{-1}$. For a large number of realizations, the difference between the input model and the mean (the data points) is only the convolution with the window function.

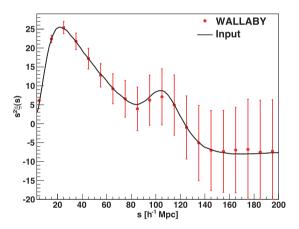


Figure 13. Prediction for the WALLABY survey. We have assumed a 4π -steradian survey with 602 000 galaxies, b=0.7, $\beta=0.7$ and $k_*=0.17h\,\mathrm{Mpc}^{-1}$.

To predict the ability of these surveys to measure the large-scale correlation function, we produced 100 lognormal realizations for TAIPAN1 and WALLABY, and 200 lognormal realizations for TAIPAN2. Figs 12 and 13 show the results in each case. The data points are the mean of the different realizations, and the error bars are the diagonal of the covariance matrix. The black line represents the input model which is a Λ CDM prediction convolved with a Gaussian damping term using $k_* = 0.17h\,\mathrm{Mpc^{-1}}$ (see equation 17). We used a bias parameter of 1.6 for TAIPAN (similar to that found in 6dFGS) and following our fiducial model we get $\beta = 0.3$, resulting in $A = b^2(1 + 2\beta/3 + \beta^2/5) = 3.1$. For WALLABY, we used a bias of 0.7 (based on the results found in the HIPASS survey; Basilakos et al. 2007). This results in $\beta = 0.7$ and A = 0.76. To calculate the correlation function, we used $P_0 = 40\,000\,h^3\,\mathrm{Mpc}^3$ for TAIPAN and $P_0 = 5\,000h^3\,\mathrm{Mpc}^3$ for WALLABY.

The error bar for TAIPAN1 is smaller by roughly a factor of 1.7 relative to 6dFGS, which is consistent with scaling by $\sqrt{V_{\rm eff}}$ and is comparable to the SDSS-LRG sample. We calculate the significance

of the BAO detection for each lognormal realization by performing fits to the correlation function using ΛCDM parameters and Ω_b = 0, in exactly the same manner as the 6dFGS analysis described earlier. We find a 3.5 \pm 0.8 σ significance for the BAO detection for TAIPAN1, 2.1 \pm 0.7 σ for TAIPAN2 and 2.1 \pm 0.7 σ for WALLABY, where the error again describes the variance around the mean.

We then fit a correlation function model to the mean values of the lognormal realizations for each survey, using the covariance matrix derived from these lognormal realizations. We evaluated the correlation function of WALLABY, TAIPAN2 and TAIPAN1 at the effective redshifts of 0.1, 0.12 and 0.14, respectively. With these in hand, we are able to derive distance constraints to respective precisions of 7, 6 and 3 per cent. The predicted value for WALLABY is not significantly better than that from 6dFGS. This is due to the significance of the 6dFGS BAO peak in the data, allowing us to place tight constraints on the distance. As an alternative figure of merit, we derive the constraints on the Hubble constant. All surveys recover the input parameter of $H_0 = 70 \,\mathrm{km \, s^{-1} \, Mpc^{-1}}$, with absolute uncertainties of 3.7, 3 and 2.2 km s⁻¹ Mpc⁻¹ for WALLABY, TAIPAN2 and TAIPAN1, respectively. Hence, TAIPAN1 is able to constrain the Hubble constant to 3 per cent precision. These constraints might improve when combined with Planck constraints on $\Omega_{\rm b}h^2$ and $\Omega_{\rm m}h^2$ which will be available when these surveys come along.

Since there is significant overlap between the survey volume of 6dFGS, TAIPAN and WALLABY, it might be interesting to test whether the BAO analysis of the local Universe can make use of a multiple tracer analysis, as suggested recently by Arnalte-Mur et al. (2011). These authors claim that by employing two different tracers of the matter density field – one with high bias to trace the central overdensities and one with low bias to trace the small density fluctuations - one can improve the detection and measurement of the BAO signal. Arnalte-Mur et al. (2011) test this approach using the SDSS-LRG sample (with a very large bias) and the SDSSmain sample (with a low bias). Although the volume is limited by the amount of sample overlap, they detect the BAO peak at 4.1σ . Likewise, we expect that the contrasting high bias of 6dFGS and TAIPAN, when used in conjunction with the low bias of WALLABY, would furnish a combined sample that would be ideal for such an analysis.

Neither TAIPAN nor WALLABY is designed as BAO surveys, with their primary goals relating to galaxy formation and the local Universe. However, we have found that TAIPAN1 would be able to improve the measurement of the local Hubble constant by about 30 per cent compared to 6dFGS going to only slightly higher redshift. WALLABY could make some interesting contributions in the form of a multiple tracer analysis.

9 CONCLUSION

We have calculated the large-scale correlation function of the 6dFGS and detected a BAO peak with a significance of 2.4σ . Although 6dFGS was never designed as a BAO survey, the peak is detectable because the survey contains a large number of very bright, highly biased galaxies, within a sufficiently large effective volume of $0.08 \, h^{-3} \, \mathrm{Gpc^3}$. We draw the following conclusions from our work.

(i) The 6dFGS BAO detection confirms the finding by SDSS and 2dFGRS of a peak in the correlation function at around $105\ h^{-1}$ Mpc, consistent with Λ CDM. This is important because 6dFGS is an independent sample, with a different target selection, redshift distribution and bias compared to previous studies. The 6dFGS

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BAO measurement is the lowest redshift BAO measurement ever made

- (ii) We do not see any excess correlation at large scales as seen in the SDSS-LRG sample. Our correlation function is consistent with a crossover to negative values at $140 h^{-1}$ Mpc, as expected from ΛCDM models.
- (iii) We derive the distance to the effective redshift as $D_V(z_{\rm eff}) = 457 \pm 27 \,{\rm Mpc}$ (5.9 per cent precision). Alternatively, we can derive $r_s(z_d)/D_V(z_{\rm eff}) = 0.336 \pm 0.015$ (4.5 per cent precision). All parameter constraints are summarized in Table 1.
- (iv) Using a prior on $\Omega_{\rm m} h^2$ from WMAP-7, we find $\Omega_{\rm m} =$ 0.296 ± 0.028 . Independent of WMAP-7, and taking into account curvature and the dark energy equation of state, we derive Ω_{m} $= 0.287 + 0.039(1 + w) + 0.039\Omega_k \pm 0.027$. This agrees very well with the first value, and shows the very small dependence on cosmology for parameter derivations from 6dFGS given its low redshift.
- (v) We are able to measure the Hubble constant, $H_0 = 67 \pm$ 3.2 km s⁻¹ Mpc⁻¹, to 4.8 per cent precision, using only the standard ruler calibration by the CMB (in form of $\Omega_{\rm m} h^2$ and $\Omega_{\rm b} h^2$). Compared to previous BAO measurements, 6dFGS is almost completely independent of cosmological parameters (e.g. Ω_k and w), similar to Cepheid and low-z supernovae methods. However, in contrast to these methods, the BAO derivation of the Hubble constant depends on very basic early Universe physics and avoids possible systematic errors coming from the build-up of a distance ladder.
- (vi) By combining the 6dFGS BAO measurement with those of WMAP-7 and previous redshift samples (from SDSS-DR7, SDDS-LRG and 2dFGRS; Percival et al. 2010), we can further improve the constraints on the dark energy equation of state, w, by breaking the H_0 -w degeneracy in the CMB data. Doing this, we find w = -0.97 ± 0.13 , which is an improvement of 24 per cent compared to previous combinations of BAO and WMAP-7 data.
- (vii) We have made detailed predictions for two next-generation low-redshift surveys, WALLABY and TAIPAN, Using our 6dFGS result, we predict that both surveys will detect the BAO signal, and that WALLABY may be the first radio galaxy survey to do so. Furthermore, we predict that TAIPAN has the potential to constrain the Hubble constant to a precision of 3 per cent improving the 6dFGS measurement by 30 per cent.

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APPENDIX A: GENERATING LOGNORMAL MOCK CATALOGUES

Here we explain in detail the different steps used to derive a lognormal mock catalogue, as a useful guide for researchers in the field. We start with an input power spectrum (which is determined as explained in Section 3.3) in units of h^{-3} Mpc³. We set up a 3D grid with the dimensions $L_x \times L_y \times L_z = 1000 \times 1000 \times 1000 \ h^{-1}$ Mpc with 200^3 subcells. We then distribute the quantity $P(\mathbf{k})/V$ over this grid, where V is the volume of the grid and $\mathbf{k} = \sqrt{k_x^2 + k_y^2 + k_z^2}$ with $k_x = n_x 2\pi/L_x$ and n_x being an integer value specifying the x-coordinates of the grid cells.

Performing a complex-to-real Fourier transform (FT) of this grid will produce a 3D correlation function. Since the power spectrum has the property $P(-k) = P(k)^*$, the result will be real.

The next step is to replace the correlation function $\xi(r)$ at each point in the 3D grid by $\ln[1 + \xi(r)]$, where \ln is the natural logarithm. This step prepares the input model for the inverse step, which we later use to produce the lognormal density field.

Using a real-to-complex FT we can revert to k-space where we now have a modified power spectrum, $P_{ln}(\mathbf{k})$. At this point, we divide by the number of subcells N_c . The precise normalization depends on the definition of the discrete FT. We use the FFTW library (Frigo & Johnson 2005), where the discrete FT is defined as

$$Y_i = \sum_{j=0}^{N_c - 1} X_j \exp[\pm 2\pi i j \sqrt{-1}/N_c]. \tag{A1}$$

The modified power spectrum $P_{ln}(k)$ is not guaranteed to be neither positive defined nor a real function, which contradicts the definition of a power spectrum. Weinberg & Cole (1992) suggested to construct a well-defined power spectrum from $P_{ln}(k)$ by

$$P'_{ln}(\mathbf{k}) = \max[0, \text{Re}[P_{ln}(\mathbf{k})]].$$
 (A2)

We now generate a real and an imaginary Fourier amplitude $\delta(\mathbf{k})$ for each point on the grid by randomly sampling from a Gaussian distribution with rms $\sqrt{P_{\text{ln}}'(\mathbf{k})/2}$. However, to ensure that the final overdensity field is real, we have to manipulate the grid, so that all subcells follow the condition $\delta(-\mathbf{k}) = \delta(\mathbf{k})^*$.

Performing another FT results in an overdensity field $\delta(x)$ from which we calculate the variance σ_G^2 . The mean of $\delta(x)$ should be

zero. The lognormal density field is then given by

$$\mu_L(\mathbf{x}) = \exp\left[\delta(\mathbf{x}) - \sigma_G^2/2\right],\tag{A3}$$

which is now a quantity defined on $[0, \infty[$ only, while $\delta(x)$ is defined on $]-\infty, \infty[$.

Since we want to calculate a mock catalogue for a particular survey, we have to incorporate the survey selection function. If W(x) is the selection function with the normalization $\sum W(x) = 1$, we calculate the mean number of galaxies in each grid cell as

$$n_{\mathfrak{g}}(\mathbf{x}) = N W(\mathbf{x}) \,\mu_L(\mathbf{x}),\tag{A4}$$

where N is the total number of galaxies in our sample. The galaxy catalogue itself is than generated by Poisson sampling $n_g(x)$.

The galaxy position is not defined within the subcell, and we place the galaxy in a random position within the box. This means that the correlation function calculated from such a distribution is smooth at scales smaller than the subcell. It is therefore important to make sure that the grid cells are smaller than the size of the bins in the correlation function calculation. In the 6dFGS calculations presented in this paper, the grid cells have a size of $5 h^{-1}$ Mpc, while the correlation function bins are $10 h^{-1}$ Mpc in size.

APPENDIX B: COMPARISON OF LOGNORMAL AND JACKKNIFE ERROR ESTIMATES

We have also estimated jackknife errors for the correlation function, by way of comparison. We divided the survey into 18 regions and calculated the correlation function by excluding one region at a time. We found that the size of the error bars around the BAO peak varies by around 20 per cent in some bins, when we increase the number of jackknife regions from 18 to 32. Furthermore, the covariance matrix derived from jackknife resampling is very noisy and hard to invert

We show the jackknife errors in Fig. B1. The jackknife error shows more noise and is larger in most bins compared to the log-normal error. The error shown in Fig. B1 is only the diagonal term of the covariance matrix and does not include any correlation between bins.

The full error matrix is shown in Fig. B2, where we plot the correlation matrix of the jackknife error estimate compared to

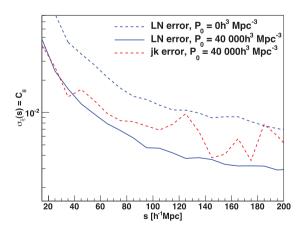


Figure B1. Correlation function error for different values of P_0 . The weighting with $P_0 = 40\,000\,h^3\,\mathrm{Mpc}^{-3}$ reduces the error at the BAO scale by almost a factor of 4 compared to the case without weighting. The red dashed line indicates the jackknife error.

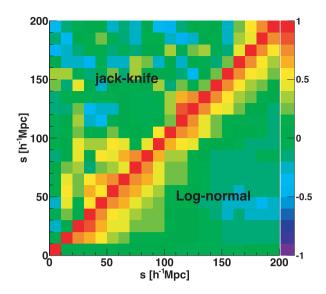


Figure B2. Correlation matrix of the jackknife errors (upper-left triangle) and lognormal errors (lower-right triangle).

the lognormal error. The jackknife correlation matrix looks much more noisy and seems to have less correlation in neighbouring bins.

The number of jackknife regions cannot be chosen arbitrarily. Each jackknife region must be at least as big as the maximum scale under investigation. Since we want to test scales up to almost $200 \, h^{-1}$ Mpc, our jackknife regions must be very large. On the other hand, we need at least as many jackknife regions as we have bins in our correlation function, otherwise the covariance matrix is singular. These requirements can contradict each other, especially if large scales are analysed. Furthermore, the small number of jackknife regions is the main source of noise (for a more detailed study of jackknife errors, see e.g. Norberg et al. 2008).

Given these limitations in the jackknife error approach, correlation function studies on large scales usually employ simulations or lognormal realizations to derive the covariance matrix. We decided to use the lognormal error in our analysis. We showed that the jack-knife errors tend to be larger than the lognormal error at larger scales and carry less correlation. These differences might be connected to the much higher noise level in the jackknife errors, which is clearly visible in all our data. It could be, however, that our jackknife regions are too small to deliver reliable errors on large scales. We use the minimum number of jackknife regions to make the covariance matrix non-singular (the correlation function is measured in 18 bins). The mean distance of the jackknife regions to each other is about $200 \, h^{-1}$ Mpc at the mean redshift of the survey, but smaller at low redshift.

APPENDIX C: WIDE-ANGLE FORMALISM

The general redshift-space correlation function (ignoring the planeparallel approximation) depends on ϕ , θ and s. Here, s is the separation between the galaxy pair, θ is the half opening angle, and ϕ is the angle of s to the line of sight (see fig. 1 in Raccanelli et al. 2010). For the following calculations, it must be considered that in this parametrization, ϕ and θ are not independent. The total correlation function model, including $O(\theta^2)$ correction terms, is then given by Papai & Szapudi (2008):

$$\xi(\phi, \theta, s) = a_{00} + 2a_{02}\cos(2\phi) + a_{22}\cos(2\phi) + b_{22}\sin^{2}(2\phi)$$

$$+ [-4a_{02}\cos(2\phi) - 4a_{22} - 4b_{22} - 4a_{10}\cot^{2}(\phi)$$

$$+ 4a_{11}\cot^{2}(\phi) - 4a_{12}\cot^{2}(\phi)\cos(2\phi) + 4b_{11}$$

$$- 8b_{12}\cos^{2}(\phi)]\theta^{2} + O(\theta^{4})$$
(C1)

This equation reduces to the plane-parallel approximation if $\theta = 0$. The factors a_{xy} and b_{xy} in this equation are given by

$$a_{00} = \left[1 + \frac{2\beta}{3} + \frac{2\beta^{2}}{15}\right] \xi_{0}^{2}(r)$$

$$-\left[\frac{\beta}{3} + \frac{2\beta^{2}}{21}\right] \xi_{2}^{2}(r) + \frac{3\beta^{2}}{140} \xi_{4}^{2}(r)$$

$$a_{02} = -\left[\frac{\beta}{2} + \frac{3\beta^{2}}{14}\right] \xi_{2}^{2}(r) + \frac{\beta^{2}}{28} \xi_{4}^{2}(r)$$

$$a_{22} = \frac{\beta^{2}}{15} \xi_{0}^{2}(r) - \frac{\beta^{2}}{21} \xi_{2}^{2}(r) + \frac{19\beta^{2}}{140} \xi_{4}^{2}(r)$$

$$b_{22} = \frac{\beta^{2}}{15} \xi_{0}^{2}(r) - \frac{\beta^{2}}{21} \xi_{2}^{2}(r) - \frac{4\beta^{2}}{35} \xi_{4}^{2}(r)$$

$$a_{10} = \left[2\beta + \frac{4\beta^{2}}{5}\right] \frac{1}{r} \xi_{1}^{1}(r) - \frac{\beta^{2}}{5r} \xi_{3}^{1}(r)$$

$$a_{11} = \frac{4\beta^{2}}{3r^{2}} \left[\xi_{0}^{0}(r) - 2\xi_{2}^{0}(r)\right]$$

$$a_{21} = \frac{\beta^{2}}{5r} \left[3\xi_{3}^{1}(r) - 2\xi_{1}^{1}(r)\right]$$

$$b_{11} = \frac{4\beta^{2}}{3r^{2}} \left[\xi_{0}^{0}(r) + \xi_{2}^{0}(r)\right]$$

$$b_{12} = \frac{2\beta^{2}}{5r} \left[\xi_{1}^{1}(r) + \xi_{3}^{1}(r)\right], \tag{C2}$$

where $\beta = \Omega_{\rm m}(z)^{0.545}/b$, with *b* being the linear bias. The correlation function moments are given by

$$\xi_l^m(r) = \frac{1}{2\pi^2} \int_0^\infty dk \, k^m P_{\text{lin}}(k) j_l(rk), \tag{C3}$$

with $j_l(x)$ being the spherical Bessel function of order l.

The final spherically averaged correlation function is given by

$$\xi(s) = \int_0^{\pi} \int_0^{\pi/2} \xi(\phi, \theta, s) N(\phi, \theta, s) \, d\theta \, d\phi, \tag{C4}$$

where the function $N(\phi, \theta, s)$ is obtained from the data. $N(\phi, \theta, s)$ counts the number of galaxy pairs at different ϕ , θ and s, and includes the areal weighting $\sin(\phi)$ which usually has to be included in an integral over ϕ . It is normalized such that

$$\int_0^{\pi} \int_0^{\pi/2} N(\phi, \theta, s) \, \mathrm{d}\theta \, \mathrm{d}\phi = 1. \tag{C5}$$

If the angle θ is of order 1 rad, higher order terms become dominant and equation (C1) is no longer sufficient. Our weighted sample has only small values of θ , but growing with s (see Fig. C1). In our case, the correction terms contribute only mildly at the BAO scale (red line in Fig. C2). However, these corrections behave like a scale-dependent bias and hence can introduce systematic errors if not modelled correctly.

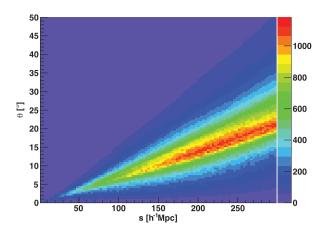


Figure C1. The half-opening angle θ as a function of separation s of the 6dFGS weighted catalogue. The plane-parallel approximation assumes $\theta=0$. The mean half-opening angle at the BAO scale is $\lesssim 10^{\circ}$. The colour bar gives the number of pairs in each bin.

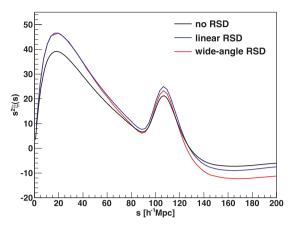


Figure C2. The black line represents the plain correlation function without redshift-space distortions (RSDs), $\xi(r)$, obtained by a Hankel transform of our fiducial Λ CDM power spectrum. The blue line includes the linear model for RSDs (linear Kaiser factor) using $\beta=0.27$. The red line uses the same value of β but includes all correction terms outlined in equation (C1) using the $N(\phi, \theta, s)$ distribution of the weighted 6dFGS sample employed in this analysis.

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