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## THE ACUTE INFLAMMATORY RESPONSE IN DIVERSE SHOCK STATES

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**ABSTRACT**—A poorly controlled acute inflammatory response can lead to organ dysfunction and death. Severe systemic inflammation can be induced and perpetuated by diverse insults such as the administration of toxic bacterial products (e.g., endotoxin), traumatic injury, and hemorrhage. Here, we probe whether these varied shock states can be explained by a universal inflammatory system that is initiated through different means and, once initiated, follows a course specified by the cellular and molecular mechanisms of the immune and endocrine systems. To examine this question, we developed a mathematical model incorporating major elements of the acute inflammatory response in C57Bl/6 mice, using input from experimental data. We found that a single model with different initiators including the autonomic system could describe the response to various insults. This model was able to predict a dose range of endotoxin at which mice would die despite having been calibrated only in nonlethal inflammatory paradigms. These results show that the complex biology of inflammation can be modeled and supports the hypothesis that shock states induced by a range of physiologic challenges could arise from a universal response that is differently initiated and modulated.

**KEYWORDS**—Mathematical modeling, inflammation, shock, organ dysfunction, hemorrhage

### INTRODUCTION

Acute systemic inflammation is triggered by both infection and trauma. This response involves a cascade of events mediated by a network of cells and molecules. The process localizes and identifies an insult, strives to eliminate offending agents, and initiates a repair process. If the system functions properly, inflammation eventually abates, and the body returns to equilibrium. However, the inflammatory response can also compromise healthy tissue, further exacerbating inflammation (1, 2) and possibly culminating in organ failure or death (3).

Shock and organ dysfunction are major healthcare problems that afflict victims of both trauma and sepsis. In 1999, a quarter of a million deaths were associated with sepsis in the United States alone (4, 5).

The initial progression of systemic inflammation can have different manifestations depending on how it is triggered, i.e., infection or trauma. However, as it progresses, the resulting shock states and organ dysfunction converge. Thus, in developing treatments and predicting outcome, it is important to ascertain which elements of inflammation are universal and which are specific to the initial insult.

Much has been learned regarding the cellular and molecular mechanisms of the acute inflammatory response. However, except for recombinant human activated protein C (Drotrecogin Alfa [activated]) (6) and low-dose corticosteroids in patients with relative adrenal insufficiency (7), this knowledge has not led to effective therapies for inflammation-induced shock. Many attempted antiinflammatory strategies have failed to improve outcome in large, randomized trials, despite showing promise in animal and early-phase human studies (8).

One reason for this failure may be that inflammation-induced shock is a complex process. The full consequences of modulating single pathways or mediators are difficult to predict from the knowledge of those pathways or mediators in isolation. Additionally, the correct therapy may depend on the exact stage and trajectory of the disease. We suggest that the complexity and diversity of shock states arises from the time-dependent interactions of a unified inflammatory response that is highly sensitive to specific modes of initiation and modulation. We further propose that this complexity might be effectively captured in a mathematical model that incorporates the dynamic interactions of a few key elements of the acute inflammatory response. A mathematical model might likewise provide new insights into the global consequences of manipulating individual components of inflammation. Mathematical modeling is increasingly being used to address biological complexity, in some cases leading to novel predictions (9–13).

We have previously described two mathematical models of inflammation of increasing complexity. The simpler model, consisting solely of a pathogen, a single population of inflammatory cells, and a measure of global tissue damage/dysfunction, could describe both recoverable infection and septic shock (14).

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A more complex model was used to create simulated populations of septic patients and to simulate a clinical trial of anti-TNF therapy (15). In this paper, we report a further enhancement to our mathematical model of acute inflammation and shock, based on some known underlying cellular and molecular mechanisms of inflammation. Our model represents the simultaneous interactions of several different pathways. Specifically, we show that it can account for the temporal changes in the concentrations of three selected cytokines and nitric oxide by-products in mice, for disparate initial insults involving bacterial lipopolysaccharide (LPS, endotoxin), surgical trauma, and hemorrhage.

## MATERIALS AND METHODS

### Experimental procedures

**Mice**—All animal experiments were approved by the Institutional Animal Care and Use Committee of the University of Pittsburgh. The experiments were performed in adherence to the National Institutes of Health Guidelines on the Use of Laboratory Animals. All studies were carried out in C57Bl/6 mice (6–10 weeks old; Charles River Laboratories, Charles River, ME).

**Endotoxemia protocol**—Mice received either LPS (from *E. coli* O111:B4, 3, 6, or 12 mg/kg intraperitoneally; Sigma Chemical Co., St. Louis, MO) or saline control. At various time points following this injection, the mice (four to eight separate mice per time point) were euthanized, and their sera were obtained for measurement of various analytes (see below). All of the mice survived this high dose of LPS until the final time point (24 h following injection of LPS).

**Surgical trauma and hemorrhagic shock protocols**—For surgical trauma and hemorrhagic shock treatment, mice were anesthetized, and both femoral arteries were surgically prepared and cannulated. For hemorrhagic shock, the mice were then subjected to withdrawal of blood with a mean arterial pressure (MAP) maintained at 25 mmHg for 2.5 h with continuous monitoring of blood pressure as described previously (16). The normal MAP in mice is approximately 100 mmHg. In the resuscitated hemorrhage groups, the mice were resuscitated over 10 min with their remaining shed blood plus two times the maximal shed blood amount in lactated Ringer solution via the arterial catheter. For trauma, only the surgical preparation was conducted. In some cases, LPS was administered intraperitoneally to mice undergoing hemorrhagic shock. Animals were euthanized by exsanguination, and their serum analyzed as described below.

**Analysis of cytokines and  $\text{NO}_2^-/\text{NO}_3^-$** —The following cytokines were measured using commercially available ELISA kits (R&D Systems, Minneapolis, MN): TNF, IL-10, and IL-6. Nitric oxide was measured as  $\text{NO}_2^-/\text{NO}_3^-$  by the nitrate reductase method using a commercially available kit (Cayman Chemical, Ann Arbor, MI) (17). Aspartate aminotransferase (AST) was measured using a commercially available kit (Vitros Chemistry™; Ortho-Clinical Diagnostics, Raritan, NJ) according to manufacturer's instructions.

### Mathematical model of acute inflammation

We constructed a mathematical model of acute inflammation that incorporates key cellular and molecular components of the acute inflammatory response (see Results, Table 1, and Appendix). The mathematical model consists of a system of 15 ordinary differential equations that describe the time course of these components. Included in the model equations are two systemic variables that represent mean arterial blood pressure and global tissue dysfunction and damage. "Global tissue damage/dysfunction" describes the overall health of the organism because the hallmark of the pathology accompanying sepsis and hemorrhagic shock is the eventual, sequential failure of multiple organs. Given the complexity of simulating individual organs, we approximated this process by treating it as a gradual, ongoing process occurring in the whole body and driven by inflammation. Thus, unrecoverable tissue damage/dysfunction served as a surrogate for death, whereas damage/dysfunction that tended to return to baseline over a several-day period was a proxy for survival. In the model, pathogen-derived products, trauma, and hemorrhage are initiators of inflammation. (We note that hemorrhage is caused by injury that disrupts the integrity of blood vessels, and thus the two processes must be included in an accurate simulation).

Each equation was constructed from known interactions among model components as documented in the existing scientific literature. In deriving the mathematical model, we balanced biological realism with simplicity. Our goal was to find a fixed set of parameters that would qualitatively reproduce many known scenarios of inflammation found in the literature, correctly describe our data, and serve as a platform for eventually testing novel predictions experimentally.

The model and parameters were specified in three stages. In the preliminary stage, the model was constructed so it could reproduce qualitatively several different scenarios reported in the literature. In this stage, direct values of parameters such as cytokine half-lives were used when available. In the second stage, the model was matched to our experimental data by adjusting some of the parameters using our knowledge of the biological mechanisms together with the dynamics of the model to attain desired time course shapes. In the third stage, the parameters were optimized using a stochastic gradient descent algorithm that was implemented in software of Immunetrics, Inc. (Pittsburgh, PA).

The units of all the quantities in the model were specified so that for the experimental protocols tested they ranged from zero to one. This was done for computational convenience and has no implications for the underlying biology.

TABLE 1. Dynamic variables of the mathematical model

Model component	Comment
Lipopolysaccharide (endotoxin, LPS)	Immunostimulant derived from gram-negative bacteria or administered exogenously
Resting neutrophils ( $N_R$ )	Renewable pool of local and circulating neutrophils susceptible to activation
Activated neutrophils ( $N_A$ )	Pool of local and circulating activated triggered by LPS, TNF, IL-6, and tissue dysfunction
Resting macrophage ( $M_R$ )	Circulating monocyte or local macrophages that act as a cellular pool for activated macrophages. The total count of resting monocyte/macrophages can increase in proportion to the total inflammatory activity
Activated macrophages ( $M_A$ )	Activation triggered by LPS, TNF, IL-6, tissue trauma, and tissue dysfunction. Activation is down-regulated by antiinflammatory cytokines
Constitutive nitric oxide synthase (eNOS)	Normally participates in blood pressure homeostasis. Activity is increased by antiinflammatory cytokines and decreased by LPS, TNF, and trauma
Inducible nitric oxide synthase (iNOSd, iNOS)	Increased by LPS and TNF in activated neutrophils and macrophages. Decreased by antiinflammatory cytokines (iNOSd is a precursor to iNOS)
$\text{NO}_2^-/\text{NO}_3^-$ ( $\text{NO}_3^-$ )	Stable reaction products of nitric oxide; related to the intensity of the local production of nitric oxide by iNOS and eNOS
TNF	A major early proinflammatory cytokine secreted mainly by activated macrophages but also by activated neutrophils
IL-10	An early antiinflammatory cytokine whose synthesis is triggered by proinflammatory stimuli, antagonizes TNF and iNOS via TNF-dependent and TNF-independent pathways
IL-6	A proinflammatory cytokine with additional antiinflammatory effects
Adrenergic inhibitory activity (CA)	Represents inhibitory activity of the adrenergic system on the production of TNF and IL-6
IL-12	Secreted by activated macrophages in the presence of TNF or IL-6, this cytokine limits the activity of IL-10
Blood pressure (BP)	Homeostasis depends on iNOS and eNOS activity. Blood pressure can be artificially manipulated
Tissue damage (D)	Can be caused by direct trauma, hypotension, or the action of proinflammatory cytokines. Nitric oxide is tissue-protective

However, to compare with experimental data, it was necessary to rescale the model outputs to experimental units by selecting optimal rescaling factors when comparing to data. These factors are specified for only the four quantities for which experimental data were available and convert the arbitrary units into true units. The final parameter set in the Appendix is expressed in arbitrary units for the concentrations and in hours for time.

### Comparison to experimental data

The model was calibrated to experimental data sets from five scenarios of inflammation: LPS intraperitoneal injection at 3 mg/kg, 6 mg/kg, and 12 mg/kg; surgical trauma consisting of the insertion of cannulae without further intervention; surgical trauma plus hemorrhage, with procedures as described above. Four analytes—TNF, IL-10, IL-6, and stable reaction products of NO ( $\text{NO}_2^-/\text{NO}_3^-$ )—were measured in all scenarios. These analytes were chosen because they represent a diverse selection of the main responders of the early inflammatory response and are produced on a rapid (TNF, IL-10), intermediate (IL-6), and slow ( $\text{NO}_2^-/\text{NO}_3^-$ ) time scale. As we will show, even with this limited data set, the relevant biological mechanisms and the mathematical model are constrained (18, 19). The statistical analysis was performed with the S-Plus statistical and programming package (Statistical Sciences, Inc., Seattle, WA).

### Model prediction

We wished to evaluate whether the model could predict a behavior not contained in the training data. We therefore assessed the prediction to a range of endotoxin boluses up to 30 mg/kg, which, from existing literature data, should be lethal (18, 20, 21).

## RESULTS

### Differences in the kinetics of cytokine and NO production in mouse endotoxemia, trauma, and hemorrhage

Trauma and hemorrhagic shock cause many of the same qualitative inflammatory consequences as endotoxemia, though with different kinetics and magnitude (22). Normal, non-manipulated mice had low levels of cytokines in their serum (data not shown). Surgical trauma alone resulted in elevated circulating levels of the measured cytokines (Fig. 1). In trauma (Fig. 1D), hemorrhagic shock (Fig. 2D), and endotoxemia (Figs. 3D, 4D, and 5D),  $\text{NO}_2^-/\text{NO}_3^-$  levels first decrease and then rise (though the levels of  $\text{NO}_2^-/\text{NO}_3^-$  rise to a much higher peak in endotoxemia). We also note that there is a delay of approximately 2 h before the cytokines respond. The absolute and relative peak levels differ significantly between trauma (Fig. 1) and endotoxemia. Compared with endotoxemia at 3 mg/kg, TNF peak level in trauma is approximately 20 to 40 times lower, IL-6 is approximately 7 times lower, and IL-10 levels are slightly higher. TNF also has a secondary peak at 24 h

in trauma. When surgery is followed by hemorrhage, animals had higher peak levels of TNF (Fig. 4A) and IL-6 (Fig. 4C), but similar or slightly higher levels of IL-10 (Fig. 4B) as compared with trauma alone.  $\text{NO}_2^-/\text{NO}_3^-$  has approximately the same form (Fig. 4D). We note that the experimental spread in the data is very large near the peaks. Although the data exhibit large variability at these points, the timing of these peaks is quite predictable.

### Generation of a mathematical model of acute inflammation

The dynamics of the measured analytes for these three experimental paradigms exhibit significant differences, although they also share qualitative similarity (2). We propose that the observed differences in the inflammatory responses are caused by differences in the initiating insult: pathogen-derived products versus tissue trauma and/or blood loss. We further propose that, once set in motion, the inflammatory response will follow a path determined by universal physiological mechanisms. For example, it has been recently appreciated that “alarm/danger” molecules such as HMGB1 or HSP-70, thought initially to participate only in the response to pathogens (23), are also important in the process of inflammation induced by sterile means (e.g., trauma) (24). This new paradigm suggests that the host is more concerned with damage or change in the *status quo* than with “foreignness.” This response also appears to share receptors: recent articles have implicated TLR4 in the response to sterile inflammation induced by endogenous ligands presumably released from damaged/dysfunctional tissue (for example, in the setting of ischemia/reperfusion injury) (25).

To support our hypotheses, we constructed a mathematical model that incorporates known physiological interactions between the various elements of the immune system. The model structure and parameters are given in the Appendix, and the output of this model in the settings of endotoxemia and trauma/hemorrhage are depicted as solid lines overlying the actual data in the figures. We discuss the statistical analysis of how well the model accounts for the data in the following section.

In the model, neutrophils and macrophages are activated directly by bacterial LPS or indirectly by various stimuli elicited systemically on trauma and hemorrhage. Although not included explicitly in our model, early effects such as mast cell degranulation and complement activation (1) are incorporated

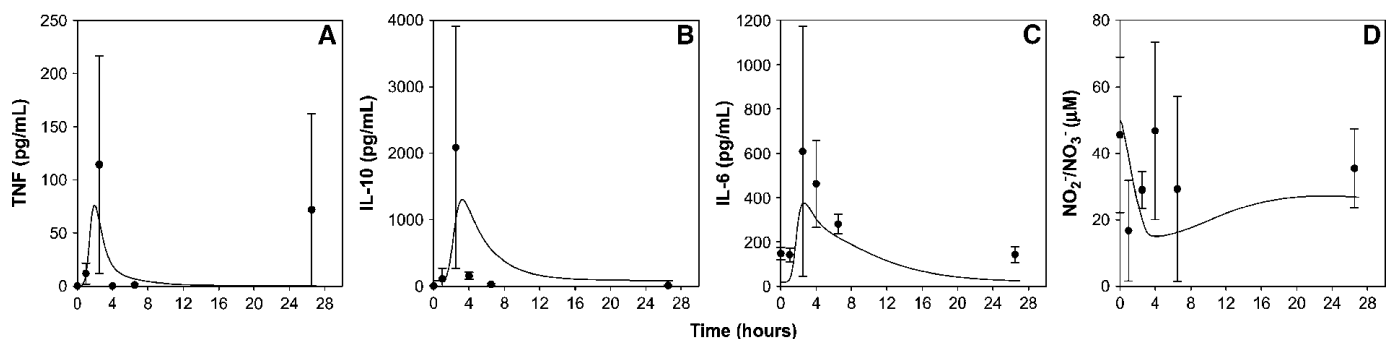


FIG. 1. **Experimental data and model predictions for surgery-induced inflammation.** Mice (3–6 separate mice per time point) were subjected to surgical trauma alone. Animals were euthanized by exsanguination 0, 1.5, or 4 h after surgery. At various time points following this treatment, the mice (3–6 separate mice per time point) were euthanized, and their plasma obtained for analysis of cytokines: TNF (A), IL-10 (B), IL-6 (C), and  $\text{NO}_2^-/\text{NO}_3^-$  (D). Symbols represent values from individual mice; solid lines represent model predictions.

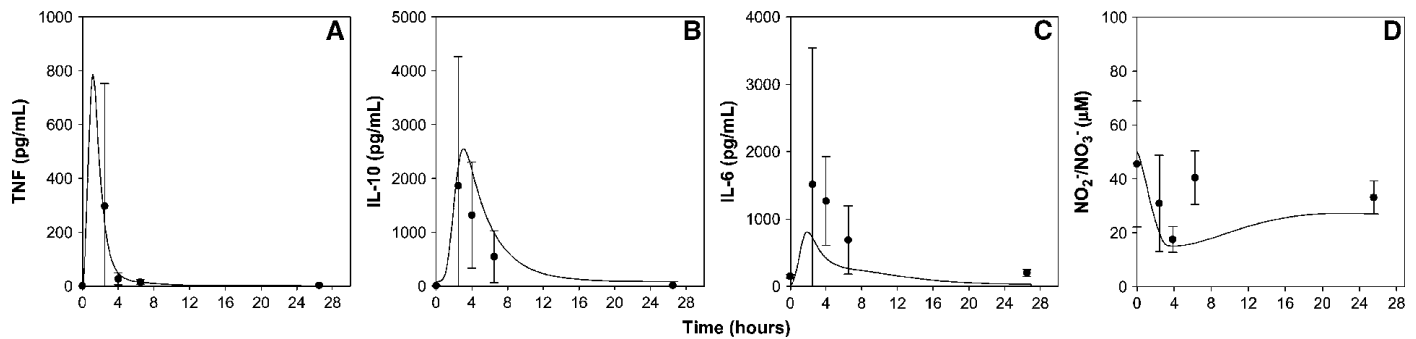


FIG. 2. **Experimental data and model predictions for surgery/hemorrhage-induced inflammation.** Mice (3–6 separate mice per time point) were subjected to combined surgical trauma and hemorrhagic shock. Animals were euthanized by exsanguination 0, 1.5, or 4 h after resuscitation. All analytes were measured as described in Figure 1. Symbols represent values from individual mice; solid lines represent model predictions.

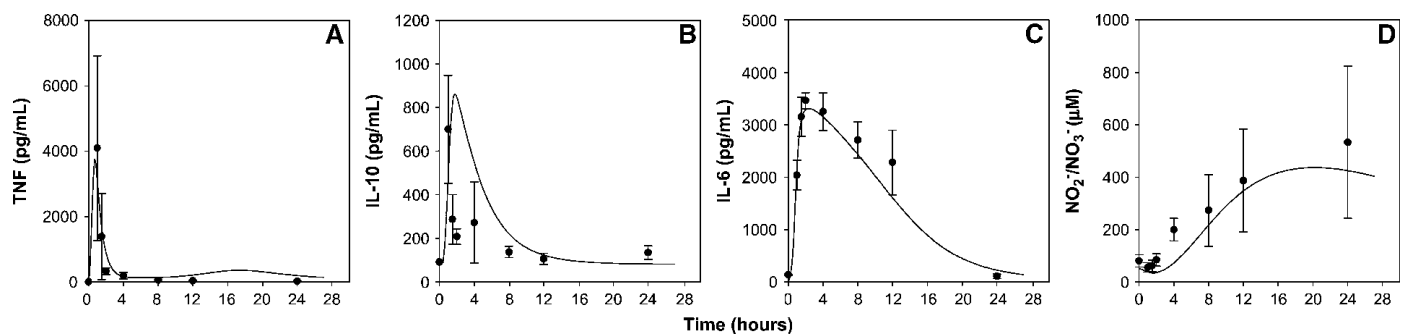


FIG. 3. **Experimental data and model predictions for endotoxemia (3 mg/kg LPS)-induced inflammation.** Mice received either 3 mg/kg LPS or saline control. At various time points following this injection, all analytes were measured as described in Figure 1. Symbols represent values from individual mice; solid lines represent model predictions.

implicitly in the dynamics of our LPS and cytokine variables. These stimuli, including LPS, enter the systemic circulation quickly and activate circulating monocytes and neutrophils (18). Activated neutrophils also reach compromised tissue by migrating along a chemoattractant gradient (26).

Once activated, macrophages and neutrophils produce and secrete effectors that activate these same cells and also other cells, such as endothelial cells. Proinflammatory cytokines—tumor necrosis factor (TNF), interleukin (IL)-6, and IL-12 in our mathematical model—promote immune cell activation and proinflammatory cytokine production (27). The concurrent production of antiinflammatory cytokines counterbalances the actions of proinflammatory cytokines. In an ideal situation, these antiinflammatory agents serve to restore homeostasis. However, when overproduced, they may lead to detrimental immunosuppression (28–30).

Our model includes a fast-acting antiinflammatory cytokine, IL-10, and a slower-acting antiinflammatory activity encompassing active transforming growth factor- $\beta$ 1 (TGF- $\beta$ 1), soluble receptors for proinflammatory cytokines, and cortisol. We note that although activated TGF- $\beta$ 1 has a lifetime of only a few minutes, latent TGF- $\beta$ 1 is ubiquitous (31) and can be activated either directly or indirectly by other slower agents such as IL-6 or NO (32–34).

Proinflammatory cytokines also induce macrophages and neutrophils to produce free radicals. In our model, inducible

NO synthase (iNOS)-derived NO is directly toxic to bacteria and indirectly to host tissue (35–37). Although the actions of superoxide ( $O_2^-$ ) and other oxidative mechanisms (37) do not appear explicitly in the model, their activity is accounted for implicitly through the proinflammatory agents. In the model, the actions of these products that can cause direct tissue dysfunction or damage are subsumed by the action of each cytokine directly. The induced damage can incite more inflammation by activating macrophages and neutrophils (38). However, NO can also protect tissue from damage induced by shock (39–41) even though overproduction of this free radical causes hypotension (36). Proinflammatory cytokines also reduce the expression of endothelial nitric oxide synthase (eNOS), thereby increasing tissue dysfunction (42).

In endotoxemia, the model assumes that LPS enters the bloodstream and incites a system-wide response (43). Lipopolysaccharide is cleared in approximately 1 h (44, 45). Circulating neutrophils are activated directly and produce TNF (46) and IL-10 (47–49). The newly produced TNF combines with LPS to activate macrophages that then secrete TNF, IL-6, IL-12, and IL-10 (50). Activated neutrophils, macrophages, and endothelial cells produce NO through iNOS (51). The model assumes that locally produced NO is eventually detected as the measured serum end products  $NO_2^-/NO_3^-$ , and this process depends on the differential induction of eNOS and iNOS in various organs over time (52, 53). In order for TNF to rise and

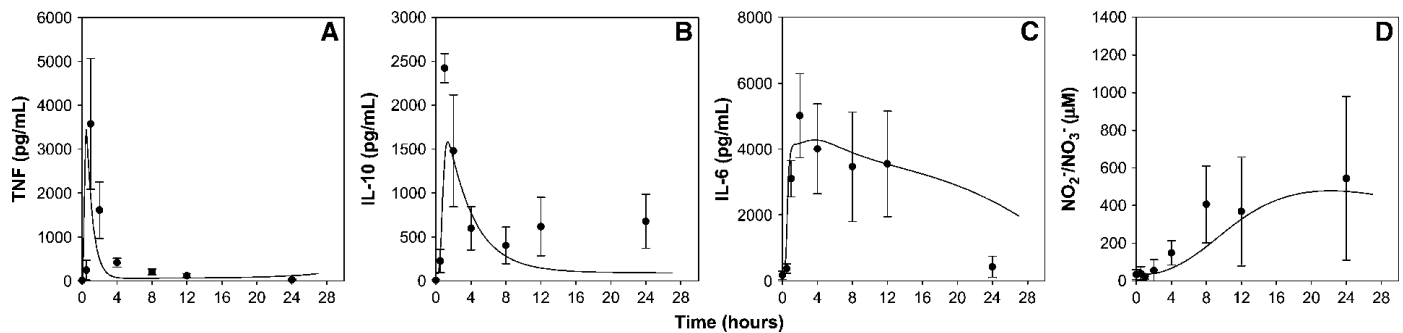


FIG. 4. **Experimental data and model predictions for endotoxemia (6 mg/kg LPS)-induced inflammation.** Mice received either 6 mg/kg LPS or saline control. At various time points following this injection, the mice (3–8 separate mice per time point) were euthanized, and their plasma obtained for analysis of cytokines as in Figure 1. Symbols represent values from individual mice; solid lines represent model predictions.

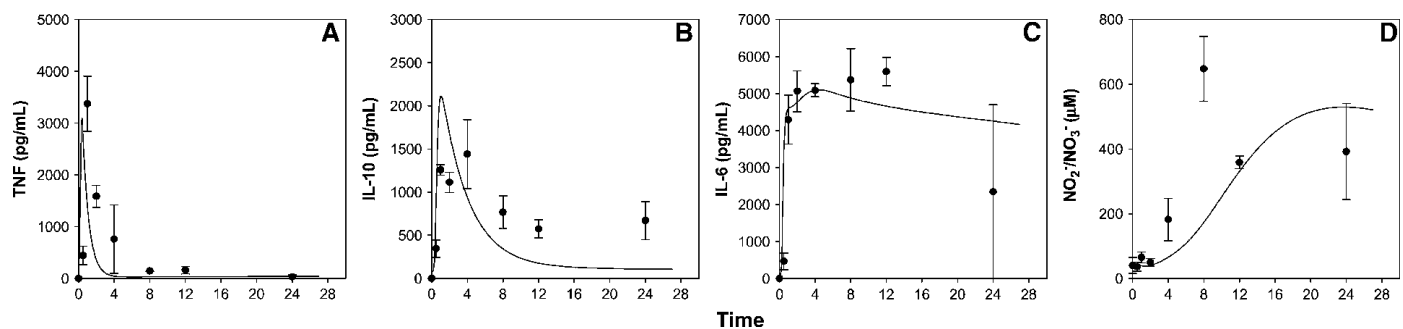


FIG. 5. **Experimental data and model predictions for endotoxemia (12 mg/kg LPS)-induced inflammation.** Mice received either 6 mg/kg LPS or saline control. At various time points following this injection, the mice (3–8 separate mice per time point) were euthanized, and their plasma obtained for analysis of cytokines as in Figure 1. Symbols represent values from individual mice; solid lines represent model predictions.

fall within a few hours as it does in Figure 1, the model required an inhibitory agent to suppress TNF production; this was accounted for by IL-10 (54, 55) and other slow antiinflammatory cytokines including IL-6 (56). Previous work has indicated that IL-6 may exert both pro- and antiinflammatory properties (57). We believe this antiinflammatory action could be mediated by inducing or activating TGF- $\beta$ 1 (32) on the surface of neutrophils and macrophages, as has been shown for cytokines such as interferon- $\gamma$  (58). To account for the saturation of IL-6 for LPS levels beyond 6 mg/kg (Fig. 2; see also Fig. 5) in the model, we suggest that IL-6 also can act as an antiinflammatory cytokine and inhibit production of itself (59). IL-10 is inhibited by IL-12 (55) and stimulated by TGF- $\beta$ 1 (60), which can come from various sources.

The response to trauma (Fig. 1) exhibits a different time course from endotoxemia (Figs. 3, 4, and 5). To account for these differences in the model, we assume that localized trauma first induces platelets to release TGF- $\beta$ 1 (31), which then chemoattracts circulating neutrophils to the site of injury (61–63). Simultaneously, elements associated with trauma and dysfunctional and/or damaged tissue, possibly HMG-B1 (64), are released and activate the neutrophils when they arrive. The trauma-induced products combine with TNF to activate local macrophages to produce IL-6 and IL-10. To achieve the massive release of IL-10 in comparison to IL-6 and TNF in the model, we assume that catecholamine release by the autonomic

nervous system (65) induces production of IL-10 by macrophages (66, 67). Catecholamines also down-regulate production of TNF and IL-6 (68, 69). We also assumed that trauma causes a severe drop in eNOS (or eNOS-derived NO, e.g., by the rapid reduction in availability of L-arginine) (70) to account for the dip in  $\text{NO}_2^-/\text{NO}_3^-$ ; it is known that trauma patients exhibit reduced systemic  $\text{NO}_2^-/\text{NO}_3^-$  as compared with uninjured controls (71, 72). A similar drop in eNOS activity or expression also occurs in endotoxemia (73–76).

The model assumes that blood loss in hemorrhage causes some tissue damage as well as directly contributing to neutrophil and macrophage activation (22). This causes a greater release of TNF, which in turn induces higher IL-10 and IL-6 release. The model output suggests that an increase in TNF and IL-6 will be accompanied by an increase in IL-10, though the spread in the data is too large to corroborate this prediction.

#### **Statistical assessment of the model in comparison to the data**

Across all scenarios, using all the data points, we obtain a correlation coefficient of 0.81 between the data and the model. Because the scatter of the data is large, trimming outliers seems reasonable. Eliminating 1% of outliers raises the correlation coefficient to 0.86, and a correlation coefficient of 0.90 is obtained by trimming 3% of the outliers. A formal test that the correlation coefficient is zero, versus the alternative that it is

greater than zero, yields a  $P$  value  $<0.0001$ , with an associated  $z$ -value of 38.1, indicating a strong positive dependence between the data and the model.

The correlation coefficients for the four separate data curves in the five scenarios as shown in Figures 1–5 are presented in the Appendix. This analysis indicates that although the model seems to capture the entire data set well, it does not capture the behavior of individual analytes uniformly well in all five scenarios.

### Qualitative assessment of the model

We sought to examine the qualitative behavior of our model, in reference to published studies of inflammation in the setting of endotoxemia and/or trauma. We used this process as a form of quality control in the quantitative fitting process of a given iteration of the model, requiring that a given iteration of the model exhibit qualitatively correct behavior across all the scenarios depicted in Table 2. We chose these scenarios as the qualitative test set because those published studies contained information of relevance to the analytes whose time courses are the core of our model.

### Prediction of lethal endotoxemia

When subjected to simulated endotoxin loads exceeding 9 mg/kg, the model predicts persistent high levels of IL-6 and high levels of damage (Fig. 6). In fact, the model predicts that cumulative damage will grow rapidly and fail to resolve within the first 24 h with doses exceeding 12 mg/kg. It appears that predicted cytokine levels have reached a plateau at about that dose, with limited increment with higher doses. The small differences in peak cytokine levels we observed between 6 mg/kg and 12 mg/kg support this observation (saturation at or around 15 mg/kg was not built in the model). We would therefore predict that levels as low as 9 mg/kg could be lethal in many animals if not euthanized at 24 h. Indeed, several animals are quite sick at the time of euthanasia. This concurs with the report by Wakatana of an LD<sub>10</sub> of 10 mg/kg and LD<sub>90</sub> of 30 mg/kg at 24 h (20). Of note, others reported significantly lower LD<sub>100</sub> doses in C57/BL6 mice (21). Our own data yielded a LD<sub>80</sub> of 17 mg/kg (unpublished results).

## DISCUSSION

The acute inflammatory response to infection and trauma is highly complex, with many levels of feedback. As a result, the manipulation of a single pathway may lead to unpredictable results. We suggest it is necessary to examine the global response

of all the participating cytokines and immune cells simultaneously over several hours or days. Only then can successful therapies be developed systematically (11, 77–80).

Mathematical modeling can provide such a global framework (1, 77, 79, 81). Our model is based on differential equations that represent the dynamics of the mean value of cytokines and cell levels along with variables for blood pressure and global tissue damage/dysfunction. The equations are derivable from physiological interactions using standard principles of mass-action kinetics (82), and the simulated levels can be compared directly to data. This contrasts with our prior work, which presented simpler models of the innate response to an infectious agent without calibration to prospective data (14, 15). The present manuscript describes a continuation of this effort, with the attempt to calibrate the model to actual data; we hope in the future to integrate several more components of the inflammation response. The current model is a very incomplete representation of all the processes of inflammation. However, we believe that it captures many of the main features of acute inflammation and can give new insights into the complex interactions of the process. Moreover, we note that although we used very different modeling strategies and underlying assumptions and elements as compared with other investigators who are simulating acute inflammation (83, 84), our models have often concurred (79).

Though a single mathematical model was able to encompass the dynamics of acute inflammation induced by diverse insults (represented as different starting conditions for our simulations), we found several inconsistencies between the output of the model and our experimental data. For example, we were unable to satisfactorily account for the rise in TNF at 24 h in our model in surgical trauma. Interestingly, we do not see a rise in TNF at 24 h in the trauma/hemorrhage data as we did in trauma alone. This discrepancy probably signifies that the model fails to account for a biological mechanism that is of particular relevance in the interaction of shock and hemorrhage. For example, a possible explanation for this observed discrepancy is that the increase in TNF and IL-6 induces a larger, delayed antiinflammatory response that suppresses TNF later. Therefore, such discrepancies stimulate additional data acquisition to support the existence of mechanisms, either by refining the search for existing data or by guiding the collection of new data. Integration of these mechanisms, in turn, will lead to more accurate models. The process of modeling complex systems, where not all fundamental behaviors and interactions are well understood, is therefore inherently iterative.

TABLE 2. Qualitative scenarios used in calibration of the mathematical model of inflammation

Animal	Model	Expected results	References
Mice	Intraperitoneal endotoxin challenge	Increased levels of TNF, IL-6, NO, cardiovascular collapse	(91)
Rats	Intraperitoneal endotoxin challenge (5-100 ug/kg)	Circulatory endotoxin within 15 minutes, 30-90 minutes to IL-6	(92)
Mice	Endotoxin challenge in TNF deficiency	Resistance to endotoxin induced inflammation, increase levels of IL-6.	(93–97)
Mice	Endotoxin challenge in IL-6 deficiency	TNF- $\alpha$ expression is much higher than in wild type animals. In localized tissue damage TGF- $\beta$ 1 and IL-10 are increased.	(98–106)
Mice	Endotoxin challenge and hemorrhagic shock in Nitric Oxide Synthase deficiency.	Decreased hypotension initially, more organ dysfunction, no change in prognosis with endotoxin, decrease cellular recruitment. Lower inflammation in hemorrhagic shock.	(16,107–115)

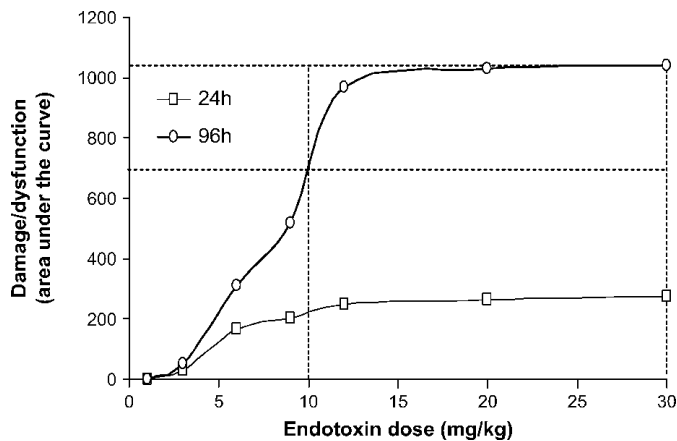


FIG. 6. Prediction of late damage and mortality following LPS administration. The model predicted a large increase of total damage/dysfunction at 24 and 96 h at doses of LPS exceeding 9 mg/kg. Open circles and squares represent doses at which the simulations were conducted. The proportion of damage/dysfunction sustained after 24 h is particularly noticeable at higher doses. This suggests that mortality could be associated with the persistence of damage/dysfunction. LD<sub>10</sub> and LD<sub>90</sub> doses as reported by Wakahara et al. are projected on the x-axis as dotted lines (20). Total damage seems to plateau at doses exceeding 15 mg/kg. A similar response is seen in the area under the IL-6 curve (data not shown).

We note that agent-based models of systemic inflammation have also been developed (79, 83). In these methods, discrete “agents” representing cells and cytokines interact through a set of fixed rules on a spatial grid, with various probabilities of a given interaction taking place. These methods are useful when the participating elements have large amounts of heterogeneity and when they have many internal states that affect their interactions with other elements. Equation-based models like the one we have created are more applicable in settings where the overall behavior of a given variable is sought (i.e., the concentration of a given cytokine in the blood, or the cumulative behavior of neutrophils). We feel that both approaches have merits, and methods incorporating both approaches may be useful in the future (79).

We hypothesize that the acute inflammatory response to diverse insults such as endotoxemia, trauma, and hemorrhagic shock are different manifestations of a universal system. We have attempted to demonstrate this possibility with mathematical modeling. Additionally, our hypothesis is supported by large epidemiologic studies, which indicate that physiological changes, organ failure rates, and survival are similar among patients with infectious and noninfectious causes of acute inflammation (85, 86).

Our model is a biologically based, dynamical simulation. As such, it differs from statistical models based on studies in large patient populations, which seek correlations among various factors (e.g., vital signs and laboratory values) and outcomes (87). Statistical models have demonstrated conclusively that circulating levels of cytokines such as IL-6 correlate with outcome in septic patients (88) and have been successful in understanding average population outcomes. However, these statistical models are mostly descriptive, making limited use of biological mechanisms. Consequently they are unable to provide causal inference and are unreliable to predict outcome of individuals (89).

In conclusion, we have developed this mathematical model with a goal of assisting the rational design of therapies directed against the inflammatory consequences of infection and trauma, the current treatment of which is largely supportive (antibiotics, vasopressors, or mechanical ventilation) (90). Despite suffering from several limitations (a limited subset of inflammatory interactions, the use of mass action kinetics, calibration to circulating but not local levels of cytokines, limited data, and lack of serial measurements in single animals), the model can simulate certain disease scenarios qualitatively as well as simulating the time course of cytokine levels in three distinct paradigms of inflammation in mice. We are in the process of addressing these limitations in various ways. For example, though we did not measure Po<sub>2</sub> and lactate in the studies described in this manuscript, we have initiated animal studies and inflammation-modeling efforts in the setting of irreversible hemorrhagic shock. In the course of those studies, we are obtaining Po<sub>2</sub>, Pco<sub>2</sub>, and other measurements and attempting to incorporate these measurements into our damage/dysfunction equation. Extending this mathematical model, with validation in humans, may lead to the *in silico* development of novel therapeutic approaches and real-time diagnostics.

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## APPENDIX

Below are the ordinary differential equations of the model. The equations represent the dynamics of circulating or systemic levels of immune cells, cytokines, and molecules. Equations were derived from “influence diagrams” constructed from literature reports. We provide an example of such a diagram in Figure A1. Every arrow is linked to specific literature references hosted in a citation manager supporting the existence and occasionally providing quantitative information regarding the

process represented by this particular arrow. In addition, are two systemic variables representing blood pressure and tissue damage/dysfunction. The effect of trauma is expressed as an exponential decay of influence after an initial insult. It represents possible released cellular material that can trigger inflammation. The function  $f_B(B)$  is phenomenological and represents the stimulatory effect of a decrease in blood pressure on triggering a stress response. This occurs in a variety of ways, and we are currently examining how to model it more exactly as part of ongoing projects in larger animals. Small deviations from normality probably are of little consequence, whereas larger deviations are proportionally more harmful (and rapidly so) as the ability of the organism to compensate decreases. This is what explains the phenomenological fourth-power exponent. For numerical ease, the variables of the equations are defined in abstract units of concentration. The actual units are restored with a linear scaling factor when compared to experimental data. The time unit is fixed at hours. The differential equations were solved numerically using the XPPAUT freeware written by Dr. G. B. Ermentrout (University of Pittsburgh, Department of Mathematics; [www.math.pitt.edu/~phase](http://www.math.pitt.edu/~phase)) as well as proprietary software of Immunetrics, Inc. The fitting process included quantitative data, but the overall behavior of the model had also to be compatible with various qualitative scenarios extracted from the literature. These scenarios are listed in Table 2. Failure to comply with any of those qualitative behaviors resulted in discarding a given model.

**Equations**

$$M'_R = \left[ \left( k_{MLPS} \frac{LPS(t)^2}{1+(LPS(t)/x_{MLPS})^2} + k_{MD} \frac{D^4}{x_{MD}^4 + D^4} \right) \times \left( \frac{TNF^2}{x_{MTNF}^2 + TNF^2} + k_{M6} \frac{IL6^2}{x_{M6}^2 + IL6^2} \right) + k_{MTR} TR(t) + k_{MB} f_B(B) \right] \times \frac{1}{1+((IL10+CA)/x_{M10})^2} M_R - k_{MA} M_A$$

$$N'_R = - \left( k_{NLPS} \frac{LPS(t)}{1+LPS(t)/x_{NLPS}} + k_{NTNF} \frac{TNF}{1+TNF/x_{NTNF}} + k_{N6} \frac{IL6^2}{1+(IL6/x_{N6})^2} + k_{ND} \frac{D^2}{1+(D/x_{ND})^2} + k_{NB} f_B(B) + k_{NTR} TR(t) \right) \times \frac{1}{1+((IL10+CA)/x_{N10})^2} N_R - k_{NA} N_A$$

$$M'_R = - \left[ \left( k_{MLPS} \frac{LPS(t)^2}{1+(LPS(t)/x_{MLPS})^2} + k_{MD} \frac{D^4}{x_{MD}^4 + D^4} \right) \times \left( \frac{TNF^2}{x_{MTNF}^2 + TNF^2} + k_{M6} \frac{IL6^2}{x_{M6}^2 + IL6^2} \right) + k_{MTR} TR(t) + k_{MB} f_B(B) \right] \times \frac{1}{1+((IL10+CA)/x_{M10})^2} M_R - k_{MR} (M_R - S_M)$$

$$N'_A = \left( k_{NLPS} \frac{LPS(t)}{1+LPS(t)/x_{NLPS}} + k_{NTNF} \frac{TNF}{1+TNF/x_{NTNF}} + k_{N6} \frac{IL6^2}{1+(IL6/x_{N6})^2} + k_{ND} \frac{D^2}{1+(D/x_{ND})^2} + k_{NB} f_B(B) + k_{NTR} TR(t) \right) \times \frac{1}{1+((IL10+CA)/x_{N10})^2} N_R - k_{NA} N_A$$

$$iNOSd' = (k_{INOSN} N_A + k_{INOSM} M_A + k_{INOSEC} \left( \frac{TNF^2}{1+(TNF/x_{INOSTNF})^2} + k_{INOS6} \frac{IL6^2}{1+(IL6/x_{INOS6})^2} \right)) \times \frac{1}{1+(IL10/x_{INOS10})^2} \frac{1}{1+(NO/x_{INOSNO})^4} - k_{INOSd} iNOSd$$

$$iNOS' = k_{INOS} (iNOSd - iNOS),$$

$$eNOS' = k_{ENOSEC} \frac{1}{1+TNF/x_{ENOSTNF}} \frac{1}{1+LPS(t)/x_{ENOSLPS}} \frac{1}{1+(TR(t)/x_{ENOSTR})^4} - k_{ENOSE} eNOS$$

$$NO'_3 = k_{NO3} (NO - NO_3)$$

$$TNF' = (k_{TNFN} N_A + k_{TNFM} M_A) \frac{1}{1+((IL10+CA)/x_{TNF10})^2} \frac{IL6}{1+(IL6/x_{TNF6})^3} - k_{TNF} TNF$$

$$IL6' = (k_{6N} N_A + M_A) \left( k_{6M} + k_{6TNF} \frac{TNF^2}{x_{6TNF}^2 + TNF^2} + k_{6NO} \frac{NO^2}{x_{6NO}^2 + NO^2} \right) \frac{1}{1+((CA+IL10)/x_{610})^2} + k_6 (S_6 - IL6)$$

$$IL12' = k_{12M} M_A \frac{1}{1+(IL10/x_{1210})^2} - k_{12} IL12$$

$$CA' = k_{CATRA}(t) - k_{CA} CA$$

$$IL10' = (k_{10N} N_A + M_A (1 + k_{10A}(t)))$$

$$\left( k_{10MR} + k_{10TNF} \frac{TNF^4}{x_{10TNF}^4 + TNF^4} + k_{106} \frac{IL6^4}{x_{106}^4 + IL6^4} \right)$$

$$\left( (1 - k_{10R}) \frac{1}{1+(IL12/x_{1012})^4} + k_{10R} \right) - k_{10} (IL10 - S_{10})$$

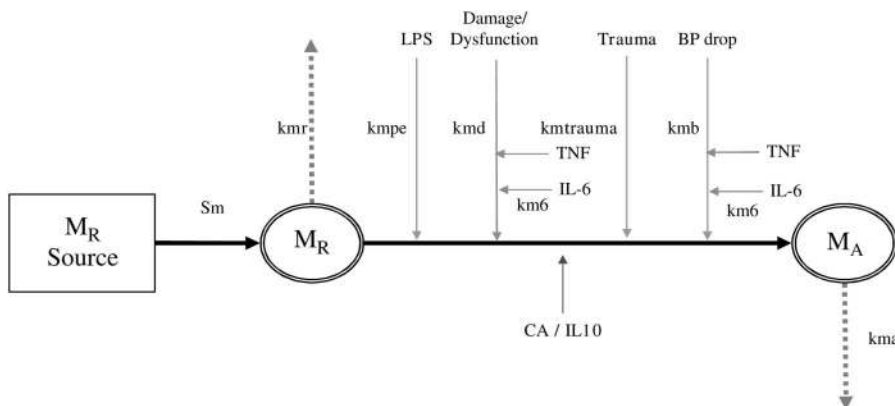


FIG. A1. **A simplified version of macrophage dynamics.** In the model used herein, resting macrophages ( $M_R$ ) are activated by a number of physiologic processes, including endotoxin (PE), damage/dysfunction, trauma and hypotension (blood pressure [BP] drop). This recruitment process can be up-regulated (green lines) in the presence of tumor necrosis factor TNF and interleukin (IL)-6, whereas IL-10 and other antiinflammatory (CA) molecules down-regulate (red line) these activating influences. Both resting and activated macrophages ( $M_A$ ) “die” at their respective rates (gray dotted line). Each process is supported by a literature search.

$$B' = k_B \left( \frac{B_0 - Hem(t)}{1 + k_{BNO}(NO - x_{BNO})} - B \right)$$

$$D' = \left( k_{DBfB}(B) + k_{D6} \frac{IL6^4}{x_{D6}^4 + IL6^4} + k_{DTR} TR(t) \right) \frac{1}{x_{DNO}^2 + NO^2} - k_D D$$

where

$$NO = iNOS(1 + k_{NOMN}(M_A + N_A)) + eNOS$$

$$LPS(t) = LPS(0) \exp(-k_{LPS}t),$$

$$TR(t) = TR_{ON} \exp(-(t - t_{TR})^2/x_{TR}^2),$$

$$A(t) = A_{ON} \exp(-(t - t_A)^2/x_A^2)$$

$$f_B(B) = H(B_0 - B)(B_0 - B)^4,$$

$$Hem(t) = (B_0 - B(0))H(t_{HRES} - t),$$

$$H(x) = \begin{cases} 1, & x > 0. \\ 0, & x < 0 \end{cases}$$

**Model Parameters**

Model parameters are divided into several categories: initial conditions, source terms, rate constants, and saturation constants (Table A1). The initial conditions determine different experimental paradigms. For endotoxemia:  $LPS(0) = 3, 6, \text{ or } 12, TR_{ON} = 0, A_{ON}(0) = 0, B(0) = 1$ ; for trauma:  $LPS(0) = 0, TR_{ON} = 1, A_{ON} = 1, B(0) = 1$ ; for hemorrhage:  $LPS(0) = 0, TR_{ON} = 1, A_{ON} = 1, B(0) = 0.25$ .

**Units**

The time unit is fixed at hours. The variables are all in relative units. To match the data we use conversion factors of 35,000, 17,000, 8,000, and 1,000, respectively, to convert the arbitrary units of TNF, IL-6, IL-10, and  $NO_3$  into true concentrations (pg/L). The variable A is a simple representation of autonomic outflow. Epinephrine and other biogenic amines released at the time of acute stressor such as hemorrhage are well known to briefly stimulate IL-10 and to a lesser degree IL-6, IL-12, and other modulators of immunity (67, 116–119). The exponential decay was inserted to mimic the empirical observation of a similar decay in circulating catecholamines and to reflect the brevity of their biological action on immune cells.

**Statistical Complement**

Examination of the data shows high heteroskedasticity for observations obtained in different animals. A closer study of the scatter shows a power law relationship between the standard deviation and the mean of the analyte response, closely approximating  $\sigma = 1.57\mu^{0.76}$ , where  $\sigma$  is the standard deviation and  $\mu$  is the mean. A consequence of this relationship is that, in addition to assessing the model by using the individual data points directly, we can also compare the model to the mean responses, keeping in mind the fact that the observed error in response is proportional to the mean response itself to a power of approximately three-quarters.

A detailed analysis of fit yields the following correlation coefficients (four analytes—IL-10, IL-6, NO, and TNF—in four scenarios—LPS doses at 3 mg/kg, 6 mg/kg, and 12 mg/kg, shock, and surgical trauma): IL10, 0.69 0.57 0.85 0.58 0.48; IL6, 0.78 0.98 0.82 0.54 0.72; NO, 0.70 0.84 0.71 0.35 0.17; TNF, 0.38 0.87 0.34 0.48 0.49. Therefore, although the fit overall is good,  $P < 0.0001$ , some curves are not described as well by the model.

TABLE A1. Model parameters

Initial conditions and source terms					
$S_M = 1.0$	$t_{HRES} = 2.5$	$M_R(0) = 1$	$iNOS(0) = 0$	$TNF(0) = 0$	$B_0 = 1.0$
$S_N = 1.0$	$t_{TR} = 1.86$	$M_A(0) = 0$	$iNOS3(0) = 0$	$IL6(0) = 0.001$	$IL12(0) = 0$
$S_6 = 0.001$	$x_{TR} = 0.6785$	$N_R(0) = 1$	$eNOS(0) = .05$	$IL10(0) = 0.01$	$x_A = 1.1636$
$S_{10} = 0.01$	$t_A = 2.0138$	$N_A(0) = 0$	$NO_3(0) = 0$	$CA(0) = 0$	$D(0) = 0$
Rate constants					
$k_{LPS} = 1.0$	$k_{NTNF} = 0.2$	$k_{INOSN} = 1.5$	$k_{NO3} = 0.46$	$k_6 = 0.7$	$k_{CA} = 0.1$
$k_{MLPS} = 1.01$	$k_{N6} = 0.557$	$k_{INOSM} = 0.1$	$k_{NOMA} = 2.0$	$k_{6N} = 0.2$	$k_{CATR} = 0.16$
$k_{MTR} = 0.04$	$k_{NB} = 0.1$	$k_{INOSec} = 0.1$	$k_{TNFN} = 2.97$	$k_{10MA} = 0.1$	$k_{12M} = 0.303$
$k_{M6} = 0.1$	$k_{ND} = 0.05$	$k_{INOS6} = 2.0$	$k_{TNFM} = 0.1$	$k_{10N} = 0.1$	$k_{12} = 0.05$
$k_{MB} = 0.0495$	$k_{NTR} = 0.02$	$k_{INOSd} = 0.05$	$k_{TNF} = 1.4$	$k_{10A} = 62.87$	$k_B = 4$
$k_{MR} = 0.05$	$k_{NTGF} = 0.1$	$k_{INOS} = 0.101$	$k_{6M} = 3.03$	$k_{10TNF} = 1.485$	$k_{BNO} = 0.2$
$k_{MA} = 0.2$	$k_{NR} = 0.05$	$k_{ENOS} = 4.0$	$k_{6TNF} = 1.0$	$k_{106} = 0.051$	$k_{DB} = 0.02$
$k_{MANO} = 0.2$	$k_{NNO} = 0.4$	$k_{ENOSEC} = 0.05$	$k_{62} = 3.4$	$k_{10} = 0.35$	$k_{D6} = 0.3$
$k_{NLPS} = 0.15$	$k_{NA} = 0.5$	$k_N = 0.5$	$k_{6NO} = 2.97$	$k_{10R} = 0.1$	$k_D = 0.05$
					$k_{DTR} = 0.05$
Saturation constants					
$x_{MLPS} = 10$	$x_{NLPS} = 15.0$	$x_{INOS10} = 0.1$	$x_{ENOSTR} = 0.1$	$x_{6NO} = 0.4$	$x_{1210} = 0.2525$
$x_{MD} = 1.0$	$x_{NTNF} = 2.0$	$x_{INOSTNF} = 0.05$	$x_{TNF6} = 0.059$	$x_{10TNF} = 0.05$	$x_{BNO} = 0.05$
$x_{MTNF} = 0.4$	$x_{N6} = 1.0$	$x_{INOS6} = 0.1$	$x_{TNF10} = 0.079$	$x_{1012} = 0.049$	$x_{D6} = 0.25$
$x_{M6} = 1.0$	$x_{ND} = 0.4$	$x_{INOSNO} = 0.3$	$x_{610} = 0.1782$	$x_{106} = 0.08$	$x_{DNO} = 0.4$
$x_{M10} = 0.297$	$x_{N10} = 0.2$	$x_{ENOSTNF} = 0.4$	$x_{6TNF} = 0.1$	$x_{12TNF} = 0.2$	
$x_{MCA} = 0.9$	$x_{NNO} = 0.5$	$x_{ENOSLPS} = 1.015$	$x_{66} = 0.2277$	$x_{126} = 0.2$	