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**Permalink** https://escholarship.org/uc/item/5n4879gj

**Journal** Nature, 398(6726)

**ISSN** 0028-0836

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Publication Date 1999-04-01

## DOI

10.1038/18821

Peer reviewed

# The afterglow, the redshift, and the extreme energetics of the $\gamma$ -ray burst 990123

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This manuscript was submitted to Nature on 11 February 1999 and resubmitted on 27 February 1999 with revisions in response to comments from the referees. We are making this m.s. available on astroph given the intense interest in GRB 990123. You are free to refer to this paper in your own paper. However, we do place restrictions on any dissemination in the popular media. The article is under embargo until it is published. For further enquiries, please contact Shri Kulkarni (srk@astro.caltech.edu) or Fiona Harrison (fiona@srl.caltech.edu).

A companion paper to this by Bloom et al. can also be found on astroph. (astr-ph/9902182) with links to HST images of the host of GRB 990123.

Afterglow, or long-lived emission, has now been detected from about a dozen well-positioned gamma-ray bursts. Distance determinations made by measuring optical emission lines from the host galaxy, or absorption lines in the afterglow spectrum, place the burst sources at significant cosmological distances, with redshifts ranging from  $\sim 1-3$ . The energy required to produce the bright gamma-ray flashes is enormous: up to  $\sim 10^{53}$  erg or 10% of the rest mass energy of a neutron star, if the emission is isotropic. Here we present the discovery of the optical afterglow and the redshift of GRB 990123, the brightest well-localized GRB to date. With our measured redshift of  $\geq 1.6$ , the inferred isotropic energy release exceeds the rest mass of a neutron star thereby challenging current theoretical models for the origin of GRBs. We argue that the optical and IR afterglow measurements reported here may provide the first observational evidence of beaming in a GRB, thereby reducing the required energetics to a level where stellar death models are still tenable.

Almost thirty years after their discovery<sup>1</sup>, the distance scale to gamma-ray bursts (GRBs) was finally unambiguously determined just two years ago<sup>2</sup>. Thanks to precise and prompt GRB localizations by the Italian-Dutch satellite, BeppoSAX<sup>3</sup> and the All Sky Monitor<sup>4</sup> aboard the Rossi X-ray Timing Explorer, afterglow emission spanning the wavelength range from X-ray to radio has now been detected in about a dozen events<sup>5,6,7</sup>. This has provided redshift measurements for four bursts: one through the detection of optical absorption lines<sup>2</sup> and three by identifying emission features in the host galaxies<sup>8,9,10</sup>. It is now assumed that a substantial fraction of all GRBs occur at significant cosmological distances ( $z \sim 1-3$ ).

The large inferred distances imply staggering energetics. In particular, our measured redshift of z = 3.14 for GRB 971214 (ref. 8) led us to an inferred isotropic energy loss of  $3 \times 10^{53}$  erg, or  $0.1 M_{\odot} c^2$ . At that time, this result was seen to challenge most proposed GRB models. The energy estimate can be reduced by invoking non-spherical emitting surface geometry, e.g. jets. However, to date, there is no firm observational evidence for jets in GRBs. Indeed, on statistical grounds, Grindlay<sup>11</sup> and Greiner et al.<sup>12</sup> constrain the "beaming factor" (the reduction in inferred energy release relative to that for the spherical case) to be less than 0.1.

BeppoSAX ushered in 1999 with the discovery of GRB 990123<sup>13</sup>, the brightest GRB seen by BeppoSAX to date. It is in the top 0.3% of all bursts, if ranked by the observed fluence<sup>14</sup>. If the inferred energetics of GRB 971214 strained theoretical models, GRB 990123, with a minimum redshift of 1.6 and an inferred isotropic energy release of  $1.9M_{\odot}c^2$ , takes them to the breaking point. In this paper, we present optical and infrared observations of GRB 990123, which both establish the distance to this luminous event, and through the observed break in the decay may provide the first observational evidence yet of beaming in a GRB.

#### The optical and the infrared afterglow

Much of our information about the parameters of GRB explosions (energy, ambient gas density, dynamics) has been obtained from radio and optical afterglow studies. These returns have motivated observers to carry out long-term multi-wavelength studies of the afterglow.

We initiated an optical and IR follow-up program for GRB 990123 on 23.577 January 1999 UT, 3.7 hr after the event, in response to the BeppoSAX preliminary localization<sup>15</sup>. We used a charge coupled device (CCD) at the Palomar 60-inch telescope to image the field of the BeppoSAX localization. We identified a new source by comparing the first CCD image with an image of the field obtained from the Digital Palomar Observatory Sky Survey II (DPOSS), and concluded that this was the optical afterglow of GRB 990123. We promptly reported the discovery to the GRB Coordinates Network<sup>16</sup> (GCN) and the Central Bureau of Astronomical Telegrams. The optical source lies within the tighter BeppoSAX localization<sup>13</sup> obtained a few hours later (see Figure 1).

Continued observations at Palomar, Keck and other observatories showed that the source exhibited the characteristic fading behavior seen in other GRB optical afterglows. The association of the optical transient (OT) with GRB 990123 is therefore secure. Table 1 summarizes the photometric observations of the OT. Included in the table is a single observation<sup>17</sup> obtained from the Hubble Space Telescope (HST); the analysis of the HST data are reported elsewhere<sup>18</sup>. Figure 2 shows the OT light curve in various bands (primarily Gunn r and K) using the photometric data shown in Table 1.

A considerable body of literature<sup>19,20,21,22</sup> has been developed to explain the afterglow phenomenon. Briefly, afterglow can be understood as arising from synchrotron emission from particles shocked by the explosive debris sweeping up ambient medium. Assuming that the electrons behind the shock are accelerated to a power-law differential energy distribution with index -p, the simplest afterglow model (e.g. ref. 23) predicts that the afterglow flux,  $f_{\nu}(t) \propto t^{\alpha}\nu^{\beta}$  where  $f_{\nu}(t)$  is the flux at frequency  $\nu$  and t is the time measured with respect to the epoch of the GRB. Interpretation of the afterglow data in the framework of these models can, in principle, yield many interesting parameters of the GRB explosion (e.g. ref. 24,25).

As the OT faded, the K band image of January 28 showed that the host galaxy was only a fraction of an arcsecond displaced with respect to the OT. A proper analysis of the decay of the OT thus requires that we correctly assess the contribution of the host galaxy to the flux of the OT. The adopted values are  $K_{\text{host}} = 0.9 \pm 0.3 \,\mu\text{Jy}$  and  $r_{\text{host}} = 0.58 \pm 0.04 \,\mu\text{Jy}$ ; see legend to Figure 2 for additional details. A discussion of the host galaxy can be found in Bloom et al.<sup>18</sup>.

In Figure 2 we present the light curve of the OT after subtracting the contribution from the host galaxy and correcting for Galactic extinction. No single power law can fit the *r*-band curve. We fit two power laws with a break at epoch  $t_{\text{break}}$  (see Figure 2). The best fit parameters are  $\alpha_{1r} = -1.10 \pm 0.03$ ,  $t_{\text{break}} = 2.04 \pm 0.46$  d and  $\alpha_{2r} = -1.65 \pm 0.06$ . In contrast, the K band data are well fitted by a single power law,  $\alpha_K = -1.10 \pm 0.11$ . We now discuss the behaviour of the afterglow in the first few days.

The value of  $\alpha_{1r}$  and  $\alpha_K$  are similar to those measured in other afterglows (e.g. refs. 26,27,8). In the 2–10 keV band the afterglow was observed by a variety of instruments

aboard BeppoSAX starting 6 hr after the burst<sup>13</sup>. From the analysis of these data,  $\alpha_X = -1.44 \pm 0.07$ . In the framework of the afterglow models, the power law decay index  $\alpha = 3(1-p)/4$  or  $\alpha = (2-3p)/4$ , depending on whether the electrons are cooling on a timescale that is slower or faster than the age of the shock. A value of p = 2.44 is consistent with  $\alpha_{1r}$ ,  $\alpha_K$  and  $\alpha_X$ ; this would require that the X-ray emitting electrons are in the fast cooling regime whereas the electrons emitting photons in the r and the K bands are in the slow cooling regime.

As briefly summarized above, afterglow models predict that the spectrum of the OT should also be a power law and with the spectral index  $\beta$  having a specific relation to  $\alpha$ . After correcting for Galactic extinction, one day after the burst we find that  $\beta_{rK} =$  $-0.8 \pm 0.1$ . This value is what is expected when the electrons emitting optical and IR photons are in the slow cooling regime. In contrast, comparing the X-ray flux six hours after the burst<sup>13</sup> with the interpolated *r*-band flux (from Figure 2) we find  $\beta_{rX} = -0.54$ . Such a large value for  $\beta$  is inconsistent with the simple afterglow model. (Supporting this flat spectrum is the observation that the *B*-band fluxes, although limited, are comparable to the *r*-band fluxes; see Figure 2.) Selective extinction by intervening dust in the host galaxy is an unlikely explanation given the strong detection of the afterglow in the *B* band (Table 1) and in the *U* band<sup>28</sup>.

We draw attention to the fact that such a discrepancy between X-ray and optical fluxes is not uncommon and, in our opinion, a similiar discrepancy exists for GRB 971214 and GRB 980703 as well. This topic is worthy of further study since it is indicative of a fundamental violation of at least one basic assumption of the simple afterglow model (spherical geometry, impulsive energy release and only one dominant emission mechanism – synchrotron emission) Indeed, later in this article, we show that the later behaviour of the afterglow is also not consistent with the simplest afterglow model.

#### Determining the redshift

We obtained spectra of the optical transient source with the Low Resolution Imaging  $Spectrograph^{29}$  on the Keck II telescope on the night of January 23, 1999. These observations consisted of three spectra, each of about 600-s duration. A quick analysis showed absorption features, indicating that the OT must be at or beyond a redshift of 1.61. A subsequent detailed data reduction yielded the spectrum displayed in Figure 3.

The OT spectrum is marked by prominent absorption lines whose suggested identifications are listed in Table 2, and marked in Figure 3. Similar lines are routinely seen in quasar spectra, and are thought to arise from absorption in intergalactic clouds. Accepting the identifications, we note that all the absorption features can be attributed to a single intergalactic cloud at a redshift  $z_{abs} = 1.6004 \pm 0.0008$ . The uncertainty in the redshift has approximately equal contributions from random and systematic errors. The absorption is relatively strong, suggesting the absorbing system has a high column density of gas. This is only the second time that an absorption redshift has been determined for a GRB OT (the other case being GRB 970508 [ref. 2], and possibly also GRB 980703 [ref. 9]), thus placing the OT unambiguously at a cosmological distance. Although the redshift,  $z_{abs} = 1.6$ , is a lower limit, it seems likely that the absorption originates in the GRB host galaxy. From the absence of the Ly $\alpha$  forest in our spectrum, we can place a firm upper limit to the redshift of z < 2.9. The absence of the reported Ly $\alpha$  forest in the spectrum<sup>30</sup> obtained from the Nordic Optical Telescope (NOT)<sup>30</sup> would further lower this limit to  $z \leq 2.2$ . These limits are further supported by the relatively strong continuum detections of the OT in the *B* band (see Table 1) and in the *U* band<sup>28</sup>, which suggest little or no absorption by the intergalactic gas.

No other convincing absorption features (aside from the normal telluric absorption) are detected in our spectrum in the wavelength range  $\lambda \sim 4700 - 9000$  Å. There are no obvious strong emission lines out to  $\lambda \sim 9600$  Å. The absence of other absorption systems in the OT spectrum is not surprising: in this redshift range there is about one metallic line absorber per unit redshift interval<sup>31</sup>.

Our slit also included the bright galaxy ~ 10 arcsecond to the West of the OT. We determine a redshift of  $z = 0.2783 \pm 0.0005$  for this galaxy, in agreement with the NOT measurement<sup>32</sup>. From our IR observations we note that the K band magnitude of this galaxy is  $K = 16.39 \pm 0.03$ . At this redshift, this corresponds to a normal,  $L \sim L_*$  galaxy.

#### The energetics of the burst

The combination of a high fluence and a redshift,  $z \ge 1.6$ , imply that this burst is extremely energetic. For this discussion, we assume a standard Friedmann model cosmology with  $H_0 = 65$  km s<sup>-1</sup> Mpc<sup>-1</sup>,  $\Omega_0 = 0.2$ , and  $\Lambda_0 = 0$  (if  $\Lambda_0 > 0$  then the inferred distance would increase, further aggravating the energetics of the burst). At the redshift z = 1.6004, the derived luminosity distance is  $D_L = 3.7 \times 10^{28}$  cm, corresponding to the distance modulus (m - M) = 45.39, and 1 arcsec in projection corresponds to 8.6 proper kpc, or 22.5 comoving kpc.

From the observed fluence<sup>14</sup> (energy > 20 keV) of  $5.1 \times 10^{-4}$  erg cm<sup>-2</sup> and the inferred  $D_L$ , we estimate the  $\gamma$ -ray energy release, assuming the emission was isotropic, to be  $3.4 \times 10^{54}$  erg  $\approx 1.9 M_{\odot} c^2$ , more than the rest mass energy of a neutron star. The prompt optical flash detected by ROTSE<sup>33</sup> had a V magnitude of 8.9, implying a peak luminosity in the UV band (restframe) of  $\sim 3.3 \times 10^{16} L_{\odot}$ . This is about a million times the luminosity of a normal galaxy, and about a thousand times the luminosity of the brightest quasars known! The prompt optical emission is attributed to emission from the reverse shock<sup>20,34</sup>; in contrast, the late-time afterglow which is the focus of this paper arises from the forward shock.

The above energetics and the peak luminosities are truly staggering. Popular models suggest that GRBs are associated with stellar deaths, and not with quasars (or the nuclei of galaxies). Perhaps the strongest observational evidence in favor of this presumption is that some GRBs are found offset from their host galaxy, and are therefore not positionally consistent with an active nucleus. An isotropic energy release of  $1.9M_{\odot}c^2$  is, however, essentially incompatible with the popular stellar death models (coalescence of neutron stars and the currently popular model of the death of massive stars). This large energy release is barely consistent with exotic models such as that of baryon decay<sup>35</sup>; in such models essentially the entire rest mass energy of the neutron star is released. There are two ways to reduce the estimated energy release. The first possibility is that the burst is amplified by gravitational lensing. Indeed, on the basis of early reports<sup>36</sup> of a possible foreground galaxy near the line of sight to the OT, we proposed that GRB 990123 was lensed. This hypothesis received a boost when the NOT team reported<sup>30</sup> possible intervening systems at redshifts of 0.286 and 0.201 which could be potential candidates for lensing. Our own subsequent, deeper imaging observations have failed to confirm any foreground galaxy and, as discussed above, there is little spectroscopic evidence for the 0.286 and 0.201 absorption systems. There is therefore no direct evidence for lensing at this time.

Furthermore, the lensing probability is  $\propto A^{-2}$  where A is the amplification provided by the lens. Even with  $A \sim 2$ , the expected probability for lensing at a redshift of 1.6 is  $10^{-3}$  (ref. 37). This probability is consistent with the observation that roughly 1 in 500 cosmic radio sources, which likely have a similar redshift distribution to GRBs, are lensed. Thus it is not very likely<sup>38</sup> that one out of the 15 bursts observed by BeppoSAX so far would be highly magnified.

We now consider the second possibility: the emitting surface in GRB 990123 is not spherical. Indeed, almost all energetic sources in astrophysics (e.g. quasars and accreting stellar black holes, pulsars) are not spherically emitting sources but display jet-like geometry. Not surprisingly there is an extensive literature on jets in the GRB context (e.g. refs. 39,40,41,42,43) as well as for the afterglow emission<sup>44</sup>.

Should the emitting surface be a jet with an opening angle of radius  $\theta_0$  then the inferred energy is reduced from the isotropic value by the beaming factor,  $f_b \sim \theta_0^2/2$ . Here we make the reasonable assumption based on other astrophysical sources that the jet is two sided. Thus if  $\theta_0 \sim 0.3$  then  $f_b \sim 5 \times 10^{-2}$ , and the  $\gamma$ -ray energy released is  $\sim 10^{53}$  erg, a value within reach of current models for the origin of GRBs.

As discussed below, a marked steepening of the afterglow emission is the clearest and simplest signature of a jet-like geometry. The three well studied GRBs (970228, 970508, 980703)<sup>26,45,46,47,48,49</sup> exhibit, at late times (epochs longer than few days) a single power law decay and with indicies that are reasonable for spherical expansion,  $\alpha \sim -1.2$ . (The complicated early time variations seen in afterglows of many GRBs are not relevant to the discussion here.) The radio afterglow of GRB 970508 has been used to argue<sup>50</sup> for beaming in this source but this result is model dependent. It is against this backdrop that we now proceed to see if there is evidence for non-spherical geometry in GRB 990123.

#### The shape of the burst: beaming?

Our knowledge of the shape of the emitting region in GRBs is limited because, due to relativistic beaming, only a small portion (angular size ~  $\Gamma^{-1}$ , where  $\Gamma$  is the Lorentz factor of the bulk motion of the emitting material) is visible to the observer. Thus the observer is unable to distinguish a sphere from a jet as long as  $\Gamma > \theta_0^{-1}$ . However, as the source continues its radial expansion,  $\Gamma$  will decrease, and when  $\Gamma < \theta_0^{-1}$  there will be a marked decrease in the observed flux. Even if the jet continues to evolve as a cone with a constant opening angle, the observer will see the flux reduced by the ratio of the solid angle of the emitting surface  $(\propto \theta_0^2)$  to that expected for a spherical expansion  $(\propto \gamma^{-2})$ . Thus the light curve will steepen by  $\gamma^2 \theta_0^2 \propto t^{-3/4}$ . This is a purely geometric effect.

Rhoads<sup>51</sup> makes the important point that unless the jet is confined by some mechanism (as advocated in ref. 43) the jet will also expand sideways at the sound speed of shocked relativistic material,  $c_s = c/\sqrt{3}$ . Thus as the jet evolves, the solid angle of the emitting region increases as  $\pi(\theta_0 + c_s t_{co}/ct)^2$ , where t is the time since the burst in the GRB frame, and  $t_{co} = t/\Gamma$  is the elapsed time in the frame moving with the jet. When  $\Gamma$  falls below  $\theta_0^{-1}$  the jet spreads in the lateral direction. Consequently, in this regime,  $\Gamma$  decreases exponentially with radius r instead of as a power law. We can therefore take r to be essentially constant during this spreading phase. Since  $t_E \approx r/2\Gamma^2 c$ , we find  $\Gamma \propto t_E^{-1/2}$  during the spreading phase; here,  $t_E$  is the elapsed time in the frame of the observer at Earth. With this scaling the typical synchrotron frequency,  $\nu_m$ , decreases as  $t_E^{-2}$  and the flux at this frequency drops as  $t_E^{-1}$ . The flux at a fixed frequency above  $\nu_m$  drops as  $F_{\nu} = F_{\nu,m}(\nu/\nu_m)^{-(p-1)/2} \propto t_E^{-p}$ , where  $p \sim 2.5$  is the electron energy power-law index. This is more than one power of t steeper than that for a spherical afterglow,  $t_E^{-3(p-1)/4} \propto t_E^{-1.1}$ .

In contrast to this discussion, we expect another kind of break and that is when the electrons responsible for the photons in the band of interest enter the cooling regime. In this case,  $\alpha$  decreases by 1/4 (e.g. ref. 23). However, unlike the break due to jet geometry (discussed above) this break is not broad-band. Regardless, in both cases, electron cooling or jets,  $\alpha$  is expected to evolve over a timescale of  $t_{\text{break}}$ . Thus the expected change in  $\alpha$ ,  $\Delta \alpha \equiv \alpha_1 - \alpha_2$  is 3/4 (constant  $\theta_0$ ),  $1 - \alpha_1/3$  (spreading jet) or 1/4 (electron cooling) should be considered to be *upper limits*; see also ref. 52.

As can be seen from Figure 2 we do indeed see a break in the *r*-band flux with  $\Delta \alpha_r = 0.55 \pm 0.07$ ; the 95% confidence interval, taking into account of covariance with the epoch of the break, is 0.4–0.7 (see Figure 2). On statistical grounds, we can rule out  $\Delta \alpha = 1/4$ . The prediction of  $\Delta \alpha = 1/4$  for cooling electron cooling arises from basic synchrotron theory and is therefore a robust prediction. Therefore, we firmly conclude that the observed break is not due to electron cooling.

The measured value of  $\Delta \alpha$  support the hypothesis of a jet in GRB 990123. However, the lack of a break in the K-band light curve is an issue of considerable concern. As explained in the legend to Figure 2, a single power-law model provides a good fit to the Kband data. Within statistical errors we can state that the r-band model does not conform to the K-band light curve. Unfortunately, the quality and quantity of the K-band data and the uncertainty in the adopted flux of the host galaxy do not permit us to derive parameters for a broken power law model independent of those derived from the r-band light curve. [Future K-band observations when the OT has essentially disappeared would help us resolve at least the latter uncertainty.]

We cautiously advance the hypothesis that we are seeing evidence for a jet (perhaps with no sideways expansion). If so,  $\theta_0 \sim \Gamma(t_{\text{break}})^{-1}$  and for typical parameters  $\theta_0 \sim 0.2$  in which case  $f_b \sim 0.02$ . Thus the energy released in  $\gamma$ -rays alone is  $6 \times 10^{52}$  erg. Including the X-ray afterglow<sup>13</sup> raises the total energy release to  $10^{53}$  erg. GRB 990123 was indeed a very energetic GRB. Following the discovery of the afterglow phenomenon<sup>5,6,7</sup>, it was thought that afterglow observations would provide only global parameters of the GRB explosion (e.g. energy released, ambient density), but it now appears that afterglow observations may give us insight into the geometry of the explosion as well.

Acknowledgment. We are indebted to G. Neugebauer for obtaining IR data on 29 January 1999. We thank A. Filippenko, L. Hillenbrand and J. Carpenter for kindly agreeing to exchange telescope time thereby enabling us to follow up this very interesting GRB and B. Oppenheimer for help with observations on February 7 and 8. Some of the observations reported here were obtained at the W. M. Keck Observatory, which is operated by the California Association for Research in Astronomy, a scientific partnership among California Institute of Technology, the University of California and the National Aeronautics and Space Administration. It was made possible by the generous financial support of the W. M. Keck Foundation. SRK's research is supported by the National Science Foundation and NASA. SGD acknowledges a partial support from the Bressler Foundation.

Date	Telescope	Band	Magnitude	Reference/
$(\mathrm{UT})$			-	Observers
Jan 23.577	P60	r	$18.65\pm0.04$	SCO
Jan $23.578$	P200	В	$18.93\pm0.04$	LML, JSM
Jan 23.958	UPSO	r	$20.00\pm0.05$	ref. 53
Jan 24.005	UPSO	В	$20.16\pm0.15$	ref. 53
Jan 24.18	BAO	r	$20.39\pm0.15^a$	ref. 54
Jan 24.194	BAO	В	$20.64\pm0.07$	ref. 54
Jan 24.547	WO	r	$20.93\pm0.2^a$	ref. 55
Jan 24.636	KI	Κ	$18.29\pm0.04$	Koerner & Kirkpatrick
Jan 24.934	UPSO	r	$21.22\pm0.08^a$	ref. 53
Jan $24.978$	UPSO	В	$22.06\pm0.20$	ref. 53
Jan 25.14	BAO	r	$21.37\pm0.15^a$	ref. 54
Jan 25.940	UPSO	r	$21.73\pm0.12^a$	ref. 53
Jan 26.154	BAO	r	$22.09\pm0.10^a$	ref. 54
Jan $27.652$	KI	Κ	$19.73\pm0.07$	MAM, ISM, HIT
Jan 29.677	KI	Κ	$20.40\pm0.08$	G. Neugebauer & LA
Jan $30.52$	MDM	r	$23.28\pm0.18^a$	JH, IAY
Feb $3.54$	MDM	r	$23.88\pm0.24^a$	JH, IAY
Feb 6.6	KI	Κ	$20.84\pm0.13$	NK
Feb 7.610	KI	Κ	$21.00\pm0.09$	SRK
Feb 8.6	KI	Κ	$20.83 \pm 0.11$	SRK
Feb $9.052$	$\operatorname{HST}$	r	$24.12\pm0.10$	ref. 18
Feb 9.6	KI	Κ	$20.97\pm0.10$	L. Hillenbrand
Feb 10.6	KI	Κ	$21.21\pm0.11$	L. Hillenbrand
Feb $9.654$	KII	r	$23.91\pm0.07^a$	A. Filippenko
Feb 14.50	MDM	r	$24.10\pm0.10^a$	JH, IAY

 Table 1. Photometric observations of GRB 990123

#### Notes:

(1) Telescope Acronyms. P60, Palomar 60-inch telescope. P200, Palomar 200-inch Hale telescope. UPSO, U. P. State Observatory 104-cm telescope. BAO, Bologna Astronomical Observatory 1.5-m telescope. WO, Fred L. Whipple Observatory 1.2-m telescope. KI, Keck-I 10-m telescope. MDM, 2.4-m Hiltner Telescope. KII, Keck-II 10-m telescope. HST, Hubble Space Telescope.

(2) Photometric zeropoint. The night of 23 January UT was photometric at Palomar. Absolute zero-points for the Gunn-r and B-band data were obtained using the observations of standard star-fields<sup>56,57,58</sup>. The absolute zero-point for the K-band observations was obtained using Keck-I data from the night of 24 January UT. Each bandpass zero-point was confirmed independently by at least two members of our group. All subsequent imaging by our group were reduced in the standard manner and photometry was propagated using a set of secondary stars in the GRB field. Photometry derived from data taken in the Cousins R-band were recalibrated to Gunn-r; the quoted uncertainties include the

estimated zeropoint and statistical uncertainties. In this table, we include all of our photometric data obtained to date and also data drawn from the literature which we could reliably place in our B, Gunn-r, and K-band system. Magnitudes marked with the superscript a are  $R_c$  magnitudes corrected to Gunn r-band using secondary reference stars reported in ref. 59,36.

Line ID	$\lambda_{obs,air}$	$\lambda_{rest,vac}$	z	$W_{\lambda,obs}$	, ±
	(A)	(A)		$(\mathbf{A})$	(Å)
Al III 1862	4843.74	1862.78	1.6010	1.23	0.07
Zn II 2026	5267.29	2026.14	1.6004	2.08	0.17
Cr II 2062	5361.77	2062.23	1.6007	1.26	0.10
Zn II 2062	5361.77	2062.66	1.6002	1.26	0.10
Fe II $2260$	5877.17	2260.78	1.6003	0.91	0.07
Fe II $2344$	6096.14	2344.21	1.6012	3.04	0.28
Fe II $2374$	6173.87	2373.73	1.6016	3.07	0.28
Fe II $2382$	6195.29	2382.76	1.6008	3.60	0.40
Fe II $2586$	6725.75	2586.64	1.6009	2.84	0.37
Fe II $2600$	6759.94	2600.18	1.6005	3.48	0.14
${ m Mg}$ II 2796	7269.47	2796.35	1.6003	4.59	0.30
${\rm Mg~II~2803}$	7289.49	2803.53	1.6008	4.80	0.52
${\rm Mg~I~2852}$	7416.97	2852.97	1.6005	2.87	0.18

Table 2. Absorption Lines Detected in the Spectrum of the OT

Notes:

(1)  $W_{\lambda,obs}$  is the observed line equivalent width; for the restframe values, divide by (1+z).

(2) The observed absorption line at 5362 Å is a blend of two lines, Cr II 2062 and Zn II 2062, and thus it appears twice.

Figure 1. Discovery image of the optical counterpart of GRB 990123. (Left) A 4 arcmin × 4 arcmin portion centered on the OT and extracted from the Digital Palomar Observatory Sky Survey II (DPOSS); the DPOSS is the digitized version of the second Palomar Observatory Sky Survey. (Right) A CCD image in the Gunn-*r* band obtained at the Palomar 60-inch. The new source, the presumed optical afterglow of GRB 990123, is marked. The circle is the 50-arcsecond localization of the X-ray afterglow<sup>13</sup> as obtained from the Narrow Field Instrument aboard BeppoSAX. Absolute astrometry on the Palomar 60-inch discovery image was obtained by comparison of 34 objects near the optical transient with the USNO-A2.0 V2.0 Catalogue<sup>60</sup>. The r.m.s. uncertainties of the astrometry are 0.28''(R.A.) and 0.26''(declination). We find the position of the optical transient to be,  $\alpha = 15^{h}25^{m}30^{s}.34$ ,  $\delta = +44^{d}45'59''.11$  (J2000).

Figure 2. Optical and infrared light curves of the transient afterglow of GRB 990123 from 4 hours to 23 days after the burst. The observed magnitudes from Table 1 have been corrected for Galactic extinction and converted to flux (see below).

(*Top*) The light curve of the transient + host galaxy. From ref. 61 we estimate the Galactic extinction in the direction of the optical transient  $(l, b = 73.12^{\circ}, 54.64^{\circ})$  to be E(B-V) = 0.01597. Thus, assuming the average Galactic extinction curve  $(R_V = 3.1)$ , the extinction measure is  $A_B = 0.069$ ,  $A_r = 0.041$ , and  $A_K = 0.006$  mag.

(*Bottom*) The inferred light curve of the transient. The contribution of the host flux has been subtracted from the Gunn-r and K-band fluxes at each epoch. The adopted host galaxy fluxes are  $K = 22.1 \pm 0.3$  magnitude corresponding to  $0.9 \pm 0.3 \,\mu$ Jy and  $0.58 \pm 0.04 \,\mu$ Jy (Gunn r); see below for details. The error bars include photometric error as well as the uncertainties in the estimated host galaxy flux.

r-band curve. A single power law decay model is inconsistent with the r-band data  $(\chi^2_{\min}/d.o.f \simeq 10)$ . We then fit the r-band points to a broken power law model:  $F_{\nu} = F_*(t/t_{\text{break}})^{\alpha_{1r}}$  for  $t \leq t_{\text{break}}$  and  $F_{\nu} = F_*(t/t_{\text{break}})^{\alpha_{2r}}$  for  $t \geq t_{\text{break}}$ ; here, t is the time in days since the GRB and  $t_{\text{break}}$  is epoch of the break. Using a Levenberg-Marquardt  $\chi^2$  minimization<sup>62</sup>, we find the r-band data are adequately fit by this broken power-law model  $(\chi^2 = 12.1 \text{ for } 9 \text{ d.o.f.})$  with the following parameters  $F_* = 7.0 \pm 1.9 \,\mu$ Jy,  $t_{\text{break}} = 2.04 \pm 0.46$  d,  $\alpha_{1r} = -1.10 \pm 0.03$ , and  $\alpha_{2r} = -1.65 \pm 0.06$ . The errors quoted are  $1-\sigma$  confidence intervals for each respective parameter. Our value of  $\alpha_{1r}$  agrees very well with the Sagar et al.'s<sup>53</sup> determination ( $\alpha = -1.10 \pm 0.06$ ), based on B and R observations obtained over the first two nights. There is some covariance between  $\alpha_2$  and  $t_{\text{break}}$  so that the confidence level on a subset of parameters may extend beyond the above quoted errors. For instance, concurrent values of ( $t_{\text{break}} = 1$  d,  $\alpha_{2r} = -1.5$ ) are allowed at the 2- $\sigma$  level as are ( $t_{\text{break}} = 3$  d,  $\alpha_{2r} = -1.8$ ).

*K*-band curve. In contrast, the *K*-band data can be modelled with a single power law index:  $\alpha_K = -1.12 \pm 0.11$  ( $\chi^2 = 8.8$  for 6 d.o.f.). This is an acceptable fit (probability of 35%). The *K*-band data cannot be statistically reconciled to the best fit *r*-band model (i.e. assuming  $\alpha_{1r}$ ,  $\alpha_{2r}$  and  $t_{\text{break}}$  to be fixed) with  $\chi^2$  ranging from 28 to 66 (7 d.o.f.), depending on the value assumed for the flux of the host galaxy.

The flux of the host galaxy was estimated as follows. For the *r*-band observations, we used the HST/STIS imaging where the host galaxy is clearly resolved and thus the flux of the OT and the host can be measured quite accurately. In ref. 18 we discuss in great detail the tie between Gunn-*r* photometry and the STIS photometry (done with CLEAR filter which corresponds approximately to the V band) as well as *R*-band photometry. The photometric ties are robust so that the flux of the host in *r* band is well determined,  $0.58 \pm 0.04 \,\mu$ Jy.

We determined the flux of the host galaxy in K-band as follows. We used the deepest exposures with the best seeing images (February 9 and February 10). In these images the OT is clearly resolved from the host galaxy. Sets of pixels dominated by the OT or by the galaxy were masked, and total fluxes with such censored data were evaluated in photometric apertures of varying radii. Total fluxes of the OT+galaxy were also measured in the same apertures using the uncensored data. We also varied the aperture radii, and the

position and the size of the sky measurement annulus. On February 9 (February 10) UT we find the OT contributes 65 (57) percent (±10 percent) of the total OT+galaxy light. The estimated errors of the fractional contributions of the OT to the total light reflect the scatter obtained from variations in the parameters of these image decompositions. In both epochs the fractional contribution of the host implies a flux of the host galaxy is  $0.9 \pm 0.3 \,\mu$ Jy ( $K_{\text{host}} = 22.1 \pm 0.3 \,\text{mag}$ ). As a further test, we fit the K-band light curve assuming the flux is given as the sum of a power-law (OT) plus a constant flux (host galaxy). This fit yields  $K_{\text{host}} = 21.55 \pm 0.20 \,\text{magnitude}$ , in agreement with the magnitude derived from direct imaging. However, we note that the fit is barely acceptable ( $\chi^2 = 11.9$ , 5 d.o.f.).

Figure 3. The spectrum of the optical transient of GRB 990123. Prominent absorption features are marked; all of these can be attributed to various absorption lines at a redshift,  $z_{abs} = 1.6004$ ; the two features labeled as "atm" are telluric absorption features (A and B bands) of the Earth's atmosphere.

Three 600-s integrations were taken, though the last one was terminated after 563 s due to the onset of fog; the integrations commenced at UT 15:38, UT 15:49 and UT 16:01, respectively. The last spectrum also suffered from a higher sky background from the brightening dawn sky. The sky conditions appeared to be good during the first two integrations, with seeing about 1 arcsecond. We used the 300 line/mm grating and the resulting wavelength coverage was 4700 Å to 9000 Å with an effective resolution of about 11.6Å, (full width at half maximum). Spectra were taken with the 1.0 arcsecond wide longslit oriented at position angle (PA) 90° (i.e. East-West) and centered on the OT; the slit also included the prominent galaxy that is about 10 arcsecond West of the OT (see Figure 1).

The usual calibration observations were not obtained given the urgency of the observations. The calibration of the wavelength was obtained using a dispersion curve measured with the same grating and slit, but a somewhat different tilt, ten days earlier. Wavelengths of the unblended night sky emission lines were then used to adjust the zero-point of the wavelength solution fit; this procedure also compensated flexure of the instrument between the exposures. An approximate flux calibration was accomplished by using the instrument response curve also measured 10 days earlier; the instrument response is stable enough for this approach. The slit losses due to the seeing and the difference of the actual slit PA from the optimal (parallactic) angle at the time of observations make the net flux calibration and the overall the shape of the spectrum somewhat uncertain. Nonetheless, we note that our spectroscopic flux measurement is in excellent agreement with photometry from interpolation of the r-band light curve. In any case, this is not important for the redshift measurements discussed in the text.

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