The Capital Asset Pricing Model in the 21st Century

Analytical, Empirical, and Behavioral Perspectives

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