The Crust and Upper Mantle of Central Mexico

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Summary

Six strain and inertial seismographs at Queen Creek, Arizona (QC-AZ), recorded six modes of surface waves from a suite of 18 earthquakes near Chiapas, Mexico. The six group-velocity dispersion curves were used in a least-squares inversion to estimate the shear velocity structure of the upper 380 km of crust and mantle in central Mexico. Multiple filter analysis of 108 seismograms produced group velocity dispersion curves slower than average continental paths. The range of the average deviation from the mean dispersion curve for the fundamental modes was 0.025 to 0.160 km s^{-1} for Rayleigh waves and $0.025-0.281 \text{ km s}^{-1}$ for Love waves. The inversion models have low velocities that correspond with a representative geotherm and petrologic P-T diagrams to indicate partial melting. The 4-layer crust is 30 km thick with a high-temperature gradient LVZ in the granitic layer and with a LVZ in the lower 8 km of a basaltic layer resulting from a high geothermal gradient or from partial melting of water saturated rock. The mantle has a 4-8 km thick solid lid and a shallow low velocity zone. The lowest velocities correspond to 10-20 per cent partial melting. A sharp velocity gradient at 70-80 km probably results from both the phase change to garnet pyrolite and the lower extreme of partial water pressure with the disappearance of amphiboles from the host pyrolite. Based on the velocities, 5 per cent anhydrous melting extends to 260 km. From 300 to 380 km temperature gradients and crystal lattice instabilities prior to the olivine-spinel phase change produce another LVZ. A hypothesis is presented that the large volume of low density magma produces a regional vertical force that creates high flat plateaus as found in central Mexico and the Colorado Plateau. The inversion models have a 7.5 s S-wave residual relative to the Canadian Shield model CANSD in agreement with observed US station anomalies.

Introduction

The properties of the whole Earth are becoming well known through the inversion of combinations of body wave travel times and of various sets of the free oscillation frequencies in conjunction with the mass of the Earth and the moment of inertia of the Earth. As the gross properties of an average earth are better established, the variations from this average become more apparent and convincing.

This paper looks at the structure of the upper 380 km of the Earth in a region of major variation from the average. The shear-wave structure of the crust and upper

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Hypocentral data for earthquakes near the coast of Chiapas, Mexico, from Preliminary Determination of Epicentres and International Seismological Centre

							Azimuth station			
Svent	Date	Time GCT	N. latitude	W. longitude	Depth (km)	$m_{\rm b}$	to cpicentre	Dist deg	tance km	Data source
1	1970 April 29	1122:36-4	14.618	92.690	41	5-6	132-5	25.2	2307-6	PDE
		1122:35-8±0-71	$14 \cdot 55 \pm 0 \cdot 043$	$92 \cdot 75 \pm 0 \cdot 038$	36 ± 6.3	5.4	132.8	25.3	2809.5	ISC
2	1970 April 29	1207:30-7	14.231	92.811	33	5.1	133-3	25.5	2832.8	PDE
		$1207:27 \pm 5 \cdot 1$	$14 \cdot 2 \pm 0 \cdot 12$	92.69 ± 0.064	7 ± 28	5.0	133-2	25.6	2843 • 5	ISC
ę	1970 April 29	1229:19.3	14.527	92.645	33	4.5	132-6	25.3	2818-4	PDE
		$1229:41 \pm 1.0$	$14 \cdot 93 \pm 0 \cdot 080$	92.83 ± 0.053	218 ± 7.3	4.3	132-3	24-9	2771-6	ISC
4	1970 April 29	1252:52.6	14-457	92.778	33	4.5	132-9	25-3	2815-2	PDE
		$1252:52 \pm 2.2$	$14 \cdot 1 \pm 0 \cdot 17$	92.93 ± 0.074	43 ± 11	4.5	133.7	25.5	2835-9	ISC
ŝ	1970 April 29	1929:52.3	14.671	93-499	29	5-2	133-9	24.7	2748•4	PDE
	,	$1929:54 \cdot 8 \pm 0 \cdot 60$	$14 \cdot 83 \pm 0 \cdot 045$	93.48 ± 0.039	$40 \pm 5 \cdot 2$	5.2	133-6	24.6	2735.8	ISC
9	1970 April 29	1938:32.3	14-561	93.552	33	4.9	134-2	24.8	2754.3	PDE
	•	$1938:33 \pm 1.1$	14.56 ± 0.086	93.63 ± 0.050	37 ± 6.8	4.8	134-3	24-7	2749.1	ISC
7	1970 April 29	2033:39-9	14.317	92.686	33	4.9	133.0	25.5	2833 · 5	PDE
	F	$2033:42 \cdot 5 \pm 0 \cdot 45$	$14 \cdot 40 \pm 0 \cdot 035$	$92 \cdot 69 \pm 0 \cdot 030$	$50 \pm 4 \cdot 1$	4.9	132-9	25.4	2826-4	ISC
œ	1970 April 29	2047:47·3	14 • 446	92.866	33	4.6	133-1	25-3	2810-1	PDE
		$2047:50 \pm 1.6$	14.5±0.14	92·91±0·051	49 ± 8.0	4.6	133-1	25.2	2802 · 8	ISC
6	1970 April 30	0043	not listed							PDE
		$0043:26\pm 2.9$	14・7±0・10	92·71±0·074	25 ± 20	4.1	132.5	25.2	2799-4	ISC

10	1970 April 30	0054:13.6	14.457	93.050	57	4.9	133-4	25.2	2796-7	PDE
		$0054:14 \cdot 6 \pm 0 \cdot 80$	$14 \cdot 51 \pm 0 \cdot 063$	$93 \cdot 09 \pm 0 \cdot 053$	61 ± 7.4	4.8 8	133・4	25.1	2789-7	ISC
11	1970 April 30	0358:24 · 3	14.506	93-170	33	4.5	133.6	25.0	2784.3	PDE
	4	$0358:28 \cdot 8 \pm 0 \cdot 85$	$14:65 \pm 0.087$	$93 \cdot 07 \pm 0 \cdot 055$	70 ± 6.5	4.3	133.2	25-0	2779-1	ISC
12	1970 April 30	0359:50-2	14.662	93·044	33	5.1	133.1	25.0	2780-0	PDE
		$0359:54 \cdot 6 \pm 0 \cdot 86$	$14 \cdot 67 \pm 0 \cdot 049$	$93 \cdot 03 \pm 0 \cdot 052$	71±7·9	4.9	133 · 1	25.0	2780·1	ISC
13	1970 April 30	0546:22-0	14-431	93·330	33	4.9	134.0	25.0	2780-4	PDE
		$0546:24 \cdot 7 \pm 0 \cdot 60$	14.56 ± 0.044	$93 \cdot 31 \pm 0 \cdot 038$	$48\pm5\cdot2$	4.9	133.7	24.9	2770-6	ISC
14	1970 April 30	0832:59-1	14.698	93.192	19	5.6	133.3	24-9	2766-5	PDE
	I	$0833:01 \cdot 1 \pm 0 \cdot 69$	$14 \cdot 61 \pm 0 \cdot 034$	$93 \cdot 29 \pm 0 \cdot 031$	37 ± 6.1	5.8	133-6	24.9	2767・6	ISC
15	1970 April 30	0859:07 · 6	14.531	93.400	33	5.2	133-9	24.9	2767•1	PDE
		$0859:08 \pm 1 \cdot 1$	14.56 ± 0.060	$93 \cdot 24 \pm 0 \cdot 068$	$35 \pm 9 \cdot 1$	5.1	133-6	25.0	2775-3	ISC
16	1970 April 30	1251:36.3	14 • 447	93-430	24	5.3	134-1	24-9	2772-0	PDE
		$1251:37\pm 1\cdot 2$	$14 \cdot 50 \pm 0 \cdot 048$	93.36 ± 0.038	$24\pm 8\cdot 8$	5.4	133.9	24.9	2772-4	ISC
17	1970 April 30	1321:03 2	14-476	93-498	22	5.4	134.2	24.9	2764-9	PDE
		$1321:04 \pm 1.2$	$14 \cdot 65 \pm 0 \cdot 047$	$93 \cdot 40 \pm 0 \cdot 037$	17 ± 8.3	5.3	133.8	24.8	2756.7	ISC
18	1970 April 30	1545:12.4	13-955	92-873	33	4.5	133.8	25.6	2851 · 8	PDE
	,	$1545:09 \pm 5.4$	13・7±0・24	$92 \cdot 89 \pm 0 \cdot 087$	26 ± 27	4.5	134.2	25.8	2873-2	ISC
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Table 1 (continued)

Note

PDE depths given as 33 were listed as N and were constrained to 33 in the solution.

mantle of a path along the centre of Mexico from about 14 to 33 degrees north latitude is established by inversion of Rayleigh-wave and Love-wave group velocities for the fundamental modes, the first higher modes, and the second higher modes from 108 earthquake-instrument pairs.

Data

The data used in this study were surface waves from a suite of 18 closely-grouped earthquakes near the coast of Chiapas, Mexico, that were recorded at the Queen Creek Seismological Station (QC-AZ). QC-AZ is about 50 km south-east of Phoenix, Arizona. The instrumentation at QC-AZ consisted of 3-component highsensitivity inertial and strain seismographs recorded in several passbands (Fix & Sherwin 1970). The surface waves recorded in the long-period (LP) passband on the three strain and three inertial seismographs were used in this study providing a possible 108 earthquake-instrument pairs.

The hypocentral data from the Preliminary Determination of Epicenters (PDE) lists of the National Ocean Survey (NOS) (the organizational name at that time) and from the International Seismological Center (ISC) lists are given in Table 1 along with calculated epicentral distances and azimuths from the station to the epicentres. The epicentral distances based on the two lists are in agreement within 0.1-20.7 km for all the earthquakes except number 3 for which the ISC solution had a depth of 218 km. This slight variation in epicentral locations is within the normal tolerance expected for routine locations. The differences in epicentral distances for each earthquake are all less than 1 per cent of the total distance and will result in less than a 1 per cent variation in observed group velocities based either on the PDE epicentre or on the ISC epicentre. The PDE data were the only set available at the beginning of the study and were used for the calculations leading to the observed group velocities.

The epicentral region, the location of QC-AZ, and the path between them are shown in Fig. 1.

The geologic structure of Mexico is a continuation of the general structure of the western United States (WUS). The structure parallels the Gulf of California–Pacific Ocean coast line. The Sierra Madre Occidental is a high mountain chain near the west coast. To the east of the Sierra Madre Occidental is a high plateau, the Mesa Central, that has an uplift and valley structure that resembles the Basin and Range. The Sierra Madre Oriental contains many folded belts on the east that grade into the Gulf of Mexico coastal plain. Between north latitudes of about 18–20 deg a line of volcanoes and recent volcanic activity extends from the Pacific Ocean to the Gulf of Mexico. To the south of the line of volcanoes is an extensive metamorphosed region (King 1969; de Cserna 1961).

The 3-component inertial seismograms from event 16 are illustrated in Fig. 2. (The LP seismometers have a natural period of 17.3 s. The galvanometers have a natural period of 110 s; and the system amplitude response peaks at 25 s.) These recordings are typical of the signals from all 18 earthquakes. The horizontal seismographs were oriented in azimuths of 325 deg and 55 deg to take advantage of the QC-AZ mine configuration. All 18 earthquakes were at azimuths of 132.3-134.2 deg from QZ-AZ. These azimuths are about 12 deg off the back azimuth of the 325 deg instruments providing essentially a radial and a transverse orientation of the horizontal seismographs. Because of this orientation and the separation of wave types on the seismograms, the group velocities were calculated from the seismograms as recorded. The *P*-wave arrival is seen on the PZLL vertical seismogram and on the radial P325LL horizontal seismogram, but not on the transverse P55LL horizontal seismogram. (Nomenclature: P = pendulum, Z = vertical, 325, 55 = azimuth for up on recording, first L = LP response, second L = low gain channel). The SH arrival







is very distinct on the P55LL transverse trace and the SV arrival about 10 s later is distinct on the PZLL. The S arrival on the P325LL trace appears to be a mixture of SH and SV motion. The Love-wave fundamental mode and higher modes are recorded on the P55LL seismogram. The Rayleigh-wave fundamental mode and higher modes are recorded on the PZLL and P325LL seismograms. A small amount of Love-wave energy can be seen in the P325LL seismogram. Both the Rayleigh-wave train and the Love-wave train contain a beat at a group velocity of about 2.5 km s⁻¹. This beat and the following signals are interpreted as a multipath effect from a lateral refraction. A few of the peaks are clipped on each of the seismograms where the signal exceeded the maximum amplitude on the magnetic tape recorder low gain channels.

Method

The method used to obtain the shear wave velocity structure is similar to that of other investigators. The observed group velocities were obtained. A starting model was established. Partial derivatives of group velocity relative to shear wave velocity were calculated for the various layers of the model. Then, a least squares inversion was performed to obtain the shear wave velocity structure. Each of the aspects of the method is discussed in the following paragraphs.

The observed group velocities were obtained by the 'multiple filter technique' (Dziewonski, Bloch & Landisman 1969). In the multiple filter technique, the digitized seismic signals are transformed to the frequency domain with the Fast Fourier Transform (FFT), the frequency coefficients are passed through a group of narrow-band Gaussian filters centred at selected frequencies, a quadrature spectrum is formed, filtered in-phase and quadrature spectra are transformed with the FFT to the time domain to form the envelope of the filtered traces at the selected frequencies (Bracewell 1965), the instantaneous amplitude and phase are established at the specified group velocities, the amplitudes are normalized to a maximum value of 99 based on both a linear normalization and a decibel (dB) normalization, and the results are printed as a function of group velocity and logarithm of the period. The amplitudes are manually contoured to aid in selection of the maxima which define the dispersion curves. Herrmann (1973) has shown that with the Gaussian filter, if the spectral amplitude of the signal is not a function of frequency within the narrow-band limits of the filter, the instantaneous amplitude is a maximum at a time $t = r/U_0$ where r is the epicentral distance and U_0 is the group velocity at angular frequency ω_0 . He has also shown that the Gaussian filter suppresses the dependence of the amplitude estimate upon the epicentral distance and the shape of the group velocity curve. Herrmann defined a time duration t_d for the Gaussian time domain envelope to decay from the peak value to an amplitude of exp $(-\pi)$. In terms of the period of the signal T_0 and α , a parameter of the filter

$$t_{\rm d} = T_0 \sqrt{\frac{\alpha}{\pi}}.$$
 (1)

He concluded that if two maxima are separated by a time greater than $2t_d$, then two modes are not interfering and group velocities can be unambiguously established. In the Gaussian filters used in this work, α equals 36.9. This value was selected for α for a time-bandwidth product that provided a compromise between resolution in the time domain and in the frequency domain (Dziewonski *et al.* 1969; Papoulis 1962). The resulting time durations t_d are $3.4 T_0$.

The multiple filter technique was applied to the 108 seismograms over the two decade period range from 2.90 to 290.7 s with 83 periods and over the group velocity window from 5.00 to 1.00 km s^{-1} at 0.02 km s^{-1} intervals. The printed amplitudes

The crust and upper mantle of central Mexico

EVENT - NEAR COAST OF CHIAPAS STATION - QC-AZ INSTRUMENT - PZLL



FIG. 3. Multiple filter analysis of surface waves from an earthquake near the coast of Chiapas, Mexico, 1970 April 30, 1251:36.3 origin time, recorded on vertical inertial seismograph PZLL.

were contoured and the dispersion curves were drawn for each of the earthquakeinstrument pairs. Examples of the multiple filter analysis technique applied to event number 16, 1970 April 30, 1251 : 36.3 origin time, are given in Fig. 3 for the vertical inertial seismograph PZLL, in Fig. 4 for the radial horizontal seismograph P325LL, and in Fig. 5 for the transverse horizontal seismograph P55LL. The curves plotted in

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EVENT -- NEAR COAST OF CHIAPAS STATION -- QC-AZ INSTRUMENT -- P325LL 6 7 8 9 10 15



FIG. 4. Multiple filter analysis of surface waves from an earthquake near the coast of Chiapas, Mexico, 1970 April 30, 1251:36.3 origin time, recorded on radial inertial seismograph P325LL.

the figures are the smoothed mean group-velocity dispersion curves; they will be discussed later. Despite the fact that the horizontal seismographs are only 12 deg off radial and transverse orientation, some signals from the non-wanted mode appear in the analysis. These signals are not evident in the seismograms (Fig. 2). The fundamental Rayleigh-wave (LR_0) dispersion curve and the fundamental Love-wave

EVENT -- NEAR COAST OF CHIAPAS STATION -- QC-AZ INSTRUMENT -- P55LL



FIG. 5. Multiple filter analysis of surface waves from an earthquake near the coast of Chiapas, Mexico, 1970 April 30, 1251:36·3 origin time, recorded on transverse inertial seismograph P55LL.

 (LQ_0) dispersion curve approach each other at periods between 35 and 40 s. However, with the multiple filter analysis, the dispersion curve is well established on both sides of this region and can be satisfactorily continued through it. The group velocities of the amplitude maxima were tabulated for the periods of the analysis. The sample mean, median, standard deviation (second moment), and average deviation from the

mean (first moment) were calculated from the data set for each mode. The sample mean group velocities were smoothed with a seven-point least squares smoothing function (Lanczos 1956). The smoothed sample means were used in the inversion process.

The initial phase and geometric orientation of a source of Rayleigh waves can affect the apparent group velocity. Knopoff & Schwab (1968) derived an expression for the group velocity U of

$$U = \frac{r}{t - (d\Psi/d\omega)}$$
(2)

where r is epicentral distance, t is time, Ψ is a phase angle determined from the source parameters, and ω is angular frequency. Empirically, they found that for a point source dipping 45 deg away from the detector and for two structure models (2) could be approximated by

$$\frac{1}{U} = \frac{1}{\overline{U}} - \frac{2.073}{r}$$
(3)

where \overline{U} is the group velocity for a vertical or horizontal source. One structure model was a simple layered crust over a semi-infinite half-space and the other structure model was derived for the crust and upper mantle north of the Alpine crest and contained an S-wave low-velocity channel. Equation (3) implies a shift in origin time of 2.073 s for the models and source considered by Knopoff & Schwab (1968). The earthquakes used in this study were at epicentral distances of about 2800 km (Table 1). It was assumed that the effect of the initial phase of the source was comparable to or less than that of the Alpine model of Knopoff & Schwab. Since 2.8 s is 0.1 per cent of the total travel time, the effect of the initial phase was neglected in this study.

The initial model for the inversion process was established from the models of previous investigators. The P-wave velocity models considered were from a central Mexico non-reversed refraction profile of the Carnegie Institute of Terrestrial Magnetism (Steinhart & Meyer 1961; Press 1966), an extensive refraction survey in the vicinity of the Tonto Forest Observatory (TFO) by Warren (1969), an inversion of the ray parameter $p = dT/d\Delta$ determined from an extended TFO array by Johnson (1967), and Basin and Range P-wave travel-time inversions by Green & Hales (1968), Archambeau, Flinn & Lambert (1969), Massé (1971), Massé, Landisman & Jenkins (1972), and Wiggins & Helmberger (1973). The S-wave velocity models considered (see Fig. 6) were from trial and error fits to Love-wave phase velocities between Dugway and Tucson by Wickens & Pec (1968) and to Basin and Range Rayleigh-wave phase velocities by Pilant (1967), S-wave travel-time inversions by Lehmann (1955; Dorman, Ewing & Oliver 1960), Ibrahim & Nuttli (1967), Nuttli (1969), and Hales & Roberts (1970), and an inversion of S-wave $dT/d\Delta$ from the TFO extended array by Kovach & Robinson (1969). The initial model FBR1 was taken from (a) two upper crustal layer P velocities from Warren (1969), (b) top layer, lower crust, and mantle P velocities from Massé (1971; Massé et al. 1972), (c) S velocities for the mantle and the third crustal layer from Kovach & Robinson (1969), (d) the S velocity of the top layer was obtained from Massé's P velocity and an assumed Poisson ratio of 0.33, (e) the S velocity of the second layer was obtained from Warren's P velocity and the Poisson ratio of 0.321 determined by Fix for QC-AZ (Fix & Sherwin 1972), (f) the depth of the interfaces and the division of the model into discrete layers was a minor compromise between the models of Massé and Kovach and Robinson with a requirement that both P-wave and S-wave interfaces be at the same depths, and (g) the densities were taken from the Nafe and Drake (Talwani, Sutton & Worzel 1959; Press 1966) empirical relation between P-wave velocity and density. Theoretical dispersion curves were calculated for the initial model, but they did not resemble the



FIG. 6. Shear-wave velocity models from the literature.

finer points of the observed dispersion curves. Therefore, three other models were constructed using seismic velocities calculated by Birch (1969) for spherical partial melt nodules in olivine plus a basaltic melt along the solidus. One model had the original *P*-velocity structure and an *S*-wave structure with no lid and 5 per cent melt.

The other two models had *P*-wave and *S*-wave structures representing 10 per cent melt; one model had a lid and the other model did not. The model with a 16 km thick lid and 10 per cent melt was adopted as the starting model FBR3 because the group velocities had a maximum at about 45 s and a minimum at about 90 s. The starting model FBR3 is given in Table 2 and the shear-wave velocities are plotted with the inversion models. During the course of the study, some instabilities were experienced with inversions using the relatively thin layers of model FBR3. An abbreviated form of the model (FBR3A) was created with fewer, thicker layers. Model FBR3A, given in Table 3, has essentially the same structure as model FBR3.

Table 2

Starting model FBR3

	Depth (at bettern	C	Compressional	Shear	
Laver	of laver)	Thickness	velocity	velocity	Density
No	(km)	(km)	$(km s^{-1})$	$(km s^{-1})$	$(g \text{ cm}^{-3})$
110.	(Mill)	(Mill)	(kiii b)	(um s)	(gein)
1	1	1	3.000	1.500	2.32
2	2	1	5.590	$2 \cdot 87$	2.62
3	4	2	5.590	2.87	2.62
4	6	2	6·12	3.58	2.90
5	10	4	6.12	3.58	2.90
6	14	4	6.12	3.58	2.90
7	18	4	6.12	3.58	2.90
8	22	4	6.91	3.80	3.09
9	26	4	6.91	3.80	3.09
10	30	4	6.91	3.80	3.09
11	34	4	7.49	4.50	3.26
12	38	4	7.49	4.50	3.26
13	42	4	7.80	4.50	3.32
14	46	4	7.80	4.50	3.32
15	50	4	7.75	4.47	3.31
16	60	10	7.60	4.33	3.30
17	70	10	7.37	4.12	3.30
18	80	10	7.38	4.12	3.30
19	100	20	7.40	4.13	3.30
20	120	20	7.42	4.14	3.30
21	140	20	7.49	4.16	3.30
22	150	10	7.45	4.17	3.39
23	160	10	7.76	4.28	3.45
24	180	20	8.350	4.489	3.50
25	200	20	8.350	4.504	3.50
26	220	20	8.380	4.609	3.51
27	240	20	8.380	4.609	3.51
28	260	20	8.380	4.609	3.51
29	280	20	8.380	4.609	3.51
30	300	20	8.600	4.609	3.55
31	320	20	8.800	4.706	3.62
32	340	20	8.80	4.740	3.62
33	360	20	9.01	4.82	3.69
34	380	20	9.25	4.89	3.75
35	400	20	9.25	5.07	3.90
36	420	20	9.625	5.250	4.01
37	460	40	9.650	5.320	4.06
38	500	40	9.67	5.38	4.11
39	550	50	9.70	5.44	4.15
40	600	50	9.80	5.51	4.23
41	625	25	9.90	5.57	4.26
42	645	20	10.85	5.90	4.51
43	/00	55	10.95	6.14	4.69
44	$\frac{1}{2}$ space	c 0	10.32	6.14	4.69

Table	3
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Starting model FBR3A

Layer No.	Depth (at bottom of layer) km	Thickness km	Compressional wave velocity km s ⁻¹	Shear wave velocity km s ⁻¹	Density g cm ⁻³
1 2 3 4 5 6 7 8 9 10 11 12 13	1 4 18 30 38 50 80 120 160 200 260 300 340	1 3 14 12 8 12 30 40 40 40 40 60 40 40	3.00 5.59 6.12 6.91 7.49 7.80 7.37 7.42 7.45 8.35 8.35 8.38 8.60 8.80	$1 \cdot 50 \\ 2 \cdot 87 \\ 3 \cdot 58 \\ 3 \cdot 80 \\ 4 \cdot 50 \\ 4 \cdot 50 \\ 4 \cdot 12 \\ 4 \cdot 14 \\ 4 \cdot 17 \\ 4 \cdot 50 \\ 4 \cdot 609 \\ 4 \cdot 609 \\ 4 \cdot 72 \\ 1 - 10 \\$	$2 \cdot 32$ $2 \cdot 62$ $2 \cdot 90$ $3 \cdot 09$ $3 \cdot 26$ $3 \cdot 32$ $3 \cdot 30$ $3 \cdot 30$ $3 \cdot 30$ $3 \cdot 50$ $3 \cdot 51$ $3 \cdot 55$ $3 \cdot 62$
14 15 16 17 18	380 420 460 500 1 2 space	40 40 40 40 ∞	9 • 25 9 • 625 9 • 65 9 • 67 9 • 70	4 · 89 5 · 07 5 · 32 5 · 38 5 · 44	3·75 3·90 4·06 4·11 4·15

Theoretical phase velocity and group velocity dispersion curves were calculated for the fundamental and the first five higher modes of Rayleigh waves and Love waves. The theoretical calculations were made with a computer program originally written by Dorman (Dorman et al. 1960) modified by Robert P. Massé and again modified by the present author. The program uses the Thompson-Haskell matrix method (Thompson 1950; Haskell 1953; Harkrider 1964) with matrix factoring for Rayleigh waves as suggested by Dunkin (1965) to minimize numerical problems at the shorter wave lengths. The program contains an option to correct the flat earth model to equivalent spherical earth properties. The Rayleigh-wave correction is only an approximation (Alterman, Jarosch & Pekeris 1961). The Love-wave correction is exact (Biswas & Knopoff 1970) and involves a change in the flat earth layer thicknesses, S velocities, and densities. Partial derivatives of group velocity with respect to layer shear velocity were calculated for each layer of models FBR3 and FBR3A for the several modes over a range of periods. The partial derivatives were calculated with a program written by the present author. This program perturbs the layer shear velocity by a small increment and calculates the partial derivative from the original group velocity, the perturbed group velocity, and the shear velocity increment. Harkrider (1968) has developed equations for Love-wave group velocity partial derivatives in terms of energy integrals based on variational principles. Since a computer program was not available to calculate the Love-wave partial derivatives from the energy integrals, and since Rayleigh-wave partial derivatives would have to be calculated numerically, all of the partial derivatives were obtained numerically by the same program. The partial derivatives of group velocity with respect to layer shear-wave velocity for the fundamental Rayleigh-wave mode and the fundamental Love-wave mode for model FBR3 are plotted in Figs 7 and 8 and for model FBR3A in Figs 9 and 10. There are several features of the partial derivatives that are significant to this study. For most mode-layer combinations, the partial derivatives are positive for some periods (generally the longer periods) and negative for other periods (generally the shorter periods). Thus, for any given mode and layer, information at one period can be cancelled, reinforced, or changed by information at another period.



FIG. 7. Partial derivatives of fundamental Rayleigh-wave group velocity with respect to layer shear velocity for model FBR3.



FIG. 8. Partial derivatives of fundamental Love-wave group velocity with respect to layer shear velocity for model FBR3.



FIG. 9. Partial derivatives of fundamental Rayleigh-wave group velocity with respect to layer shear velocity for model FBR3A.

For most mode-period combinations, the partial derivatives for some layers are positive and for other layers, are negative. Thus, for any given mode and period, information relating to one layer can be cancelled, reinforced, or changed by the relationship among layers. In this manner, the partial derivative curves contain information relating to the resolution capability of an inversion process. The curves can be read as plotted to determine what periods most affect a given layer; or they can be read vertically to determine what layers are most affected at a given period.

Model FBR3 has thinner layers than model FBR3A and the partial derivatives have sharper peaks and overlap each other considerably more than the partial derivatives corresponding to the same depths for model FBR3A. The sharper peaks indicate better resolution, but the increased overlap presents problems of inversion instability and probably decreases the linear independence of information at adjacent periods. The majority of higher mode curves have large partial derivatives where the theoretical group-velocity dispersion curve changes rapidly between 3.5 and 4.0s and between 6 and 8 s. These period ranges were avoided in the inversions. The Love-wave partial



FIG. 10. Partial derivatives of fundamental mode Love-wave group velocity with respect to layer shear velocity for model FBR3A.

derivatives have broader peaks than the Rayleigh-wave partial derivatives. The Love-waves are more sensitive to the shallower structure and, at a given period, the Rayleigh-wave sensitivity extends to deeper depths than the Love-wave sensitivity. The partial derivatives for the layers in the low velocity zone (LVZ) are larger than the partial derivatives for the adjacent layers.

The inversion method used in this study is a least squares technique patterned after that developed and used by Bloch (1969; Bloch, Hales & Landisman 1969) and used by James (1971b). Bloch used phase velocities and group velocities for several modes to obtain the shear-wave velocity structure in southern Africa. James used trial and error inversion with phase velocities and Bloch's method of inversion with group velocities to obtain the shear-wave velocity structure in the Andes. To improve stability, the least squares process is applied to the shear velocity in one layer at a time proceeding through the set of layers included in the solution in a specified order. The process is then repeated for a selected number of iterations. The least-squares numerical inversion of seismic surface wave phase velocity dispersion data to obtain properties of the crust and mantle was first utilized by Dorman & Ewing (1962) in the New York-Pennsylvania area. Brune & Dorman (1963) applied this method to phase velocities of surface waves propagated across the Canadian Shield. McEvilly (1964) used this technique to invert phase velocities to obtain a model of the crust and upper mantle in the central United States.

If a set of group velocities $U_{0_{mi}}$ are observed for given modes m at a set of periods T_{mi} , and if a set of theoretical group velocities $U_{T_{mi}}$ are calculated for the same modes and periods from a model, the least squares problem is to minimize the sum of the squares of the residuals R_{mi}

where

$$R_{mi} = U_{0_{mi}} - U_{T_{mi}} \qquad m = 1, 2, ..., \text{NM} \qquad i = 1, 2, ..., \text{IP}_{m}$$
(4)

and NM is the number of modes and IP_m is the number of periods for mode m. Thus, we want to minimize

$$\sum_{m=1}^{\text{NM}} \sum_{i=1}^{\text{IP}_m} \mathbf{R}_{mi}^2.$$
 (5)

Assuming small changes and that there is a linear dependence between layer shear velocity and theoretical group velocity, and using the partial derivative of group velocity for mode m and period i with respect to shear-wave velocity β in layer k = j, we can write a set of equations

n

$$\frac{\partial U_{mi}}{\partial \beta_k} d\beta_j = \mathbf{R}_{mi} \tag{6}$$

or in matrix notation

$$\mathbf{P}\mathbf{D} = \mathbf{R} \tag{7}$$

where P is a row vector of partial derivatives; D is a single element column vector of the change in shear velocity needed in layer k = i, and **R** is a column vector of residuals. If both sides are multiplied by the transpose of **P**,

$$\mathbf{P}^T \, \mathbf{P} \mathbf{D} = \mathbf{P}^T \, \mathbf{R}. \tag{8}$$

These equations are solved for D which is the least squares solution of (7) for the change in shear velocity $\Delta\beta$ of layer k = j. The theoretical group velocity is then revised by the set of equations

$$\Delta U_{T_{mi}} = \frac{\partial U_{mi}}{\partial \beta_k} \, \Delta \beta_j \tag{9}$$

R is revised by

$$\mathbf{R}_{mi}(\text{new}) = \mathbf{R}_{mi}(\text{old}) - \Delta U_{T_{mi}}.$$
(10)

The succeeding layers are each then treated in the same manner, until the change in all layers to be used in the solution has been calculated. The overall solution is then improved by repeating the entire process for several iterations.

The preceding discussion considered only group velocities and layer shear velocities. Other independent parameters such as phase velocities and Rayleigh-wave ellipticity (Boore & Toksöz 1969) could have been used separately or in combination with the other two parameters. Also other properties of the layers such as compressional wave velocity and density could be used, again separately or in combination. Dorman & Ewing (1962), Brune & Dorman (1963) and McEvilly (1964) used only phase velocities in their inversions. Bloch (1969; Bloch et al. 1969) used both phase velocities and group velocities. He came to the conclusion that the inversion of the group-velocity dispersion curve should produce a more detailed earth model than the inversion of the phase-velocity dispersion curve. This conclusion is based on the fact that the group velocity is a derivative of the phase velocity and will have large variations for a corresponding small variation in the phase velocity. Knopoff (1972) and Pilant & Knopoff (1970) reason that inversion of phase velocities eliminates one degree of non-uniqueness present in the inversion of group velocities, because a single group velocity curve could fit several phase velocity curves that were displaced from each other by constants. I agree with Bloch that the derivative function, group velocity, is the more sensitive function and should produce more resolution in the inversion process. The experimental phase velocities were determined with assumptions of a constant initial phase with frequency and of a specific number of radian circles that pertain to the source-station pair. A similar assumption is not required in the group velocity determination. Since ample group-velocity dispersion curves, this study was confined to inversion of the group-velocity dispersion curves.

Brune & Dorman (1963), McEvilly (1964) and Der & Landisman (1972) illustrate partial derivatives of Rayleigh-wave phase velocity with respect to layer shear-wave velocity, layer compressional-wave velocity, and layer density and of Love-wave phase velocity with respect to layer shear-wave velocity and layer density. The partial derivatives with respect to shear-wave velocities, are larger than the partial derivatives with respect to the other two parameters. Thus, the inversion process has considerably more resolution with shear-wave velocities than with compressional-wave velocities or densities. Both Brune & Dorman (1963) and McEvilly (1964) experienced instability when both shear-wave velocity and density were allowed to vary in a solution and both only reported on shear-wave solutions. Bloch (1969; Bloch *et al.* 1969) and James (1971b) only used shear-wave partial derivatives in their inversions. Der, Massé & Landisman (1970) found that the resolution of phase velocities was inferior to the resolution with group velocities having the same magnitude of errors.

In recent years several authors have presented theoretical discussions concerning the non-uniqueness of inversion of seismic data and concerning the resolving power of various data sets. Backus & Gilbert (1967, 1968, 1970), Backus (1970a, b, c), Jackson (1972) and Parker (1972) have treated the general problem of determining the average properties of the Earth from sets of gross earth data selected from appropriate earth functionals. Der et al. (1970) and Der & Landisman (1972) independently developed similar concepts, primarily for the application of inversion of surfacewave dispersion data to determine the properties of the crust and upper mantle. All of these papers develop various methods for evaluating the trade-off between resolution, stability, and errors in the data. The methods considered by these authors involve the simultaneous inversion of all parameters in the solution at one time. The method used by Bloch (1969; Bloch et al. 1969), James (1971b), and in this study has not been specifically treated theoretically, but the inversion for each layer is a simplified case of the larger inversion problem. The trade-offs in this study between resolution, stability, and variation of the results were made empirically based on the concepts in these papers. Resolution was achieved with many thin layers in the model FBR3 (layers are generally 4 km thick in the crust, 10 km thick in the upper mantle, and 20 km thick in the lower mantle). This high resolution sacrificed stability in that only the fundamental mode Rayleigh-wave and Love-wave dispersion curves could be used in the solution. The solutions with the higher modes had the same characteristics of high velocities or low velocities in the same layers as the fundamental mode solutions, but the layer shear-velocity values were exaggerated, i.e. unreasonably too high or too low. Also, as will be seen later, the solution starting with the top layer and proceeding down, varied in the low-velocity regions from the solution starting with the bottom layer and proceeding up. Very satisfactory stability was achieved by thickening the layers in the starting model FBR3A while maintaining the same structure. The thicker layers produced the same solution from the top as from the bottom with six modes $(LR_0, LR_1, LR_2, LQ_0, LQ_1 and LQ_2)$ in the solution. Stability also was achieved in the inversion process by dropping out layers for certain modes when the sum of the partial derivatives squared was smaller than an empirically selected number. In the solution of equation (8), the product $\mathbf{P}^T \mathbf{P}$ is in the denominator. This product is the sum of the partial derivatives squared for layer k. If this product is small, the solution can become too large. Originally solutions were made with no restraints, values of the sum of the partial derivatives squared were determined for layers that had unreasonable solutions, a minimum value for $\mathbf{P}^T \mathbf{P}$ was established, and new solutions were made with the program omitting layers in which $\mathbf{P}^T \mathbf{P}$ was less than the minimum value.

Each residual \mathbf{R}_{mi} (equation (4)) contains some information that is allocated to the solution of D in equation (8). Since layers are treated individually in the method used in this study, there is a possibility of distributing a disproportionate share of this information to the layers treated in the beginning of the solution. This fact became evident when an attempt was made to establish the crust shear velocities with fundamental Rayleigh-wave and Love-wave data; and then restraining the crust to these values, to use only the same Rayleigh-wave data to establish the upper mantle shear velocities. All the information was applied in the solution for the crust and the following solution for the mantle produced meaningless results. As a consequence of this experiment, the inversion computer program was modified to allow omission of specified layers for any mode and/or to restrain any selected layer at an arbitrary value of shear-wave velocity. In general, proper use of the deletion of layers for some modes improved the solutions and conversely, almost any restraint, including the top layer, degraded the solution. Here 'improved' and 'degraded' are interpreted in terms of reasonableness of relative velocities in the various layers and in terms of the root-mean-square (rms) values of final residuals (equation (10)) for each mode individually and all modes collectively. To accommodate a reasonable allocation of the information in the residuals \mathbf{R}_{mi} to the layers treated early in the solution, it was found necessary to weight the solution of these layers. A weighting factor of less than 1.0 calculated by the index of the layer encountered in the solution times the iteration number divided by 10 was applied for the first seven iterations. Thus, the first layer used in the solution was weighted from 0.1 to 0.7 for seven iterations, respectively, the second layer was weighted for four iterations, the third layer for three, the fourth layer for two, and the fifth through the ninth layers were weighted only for the first iteration. This weighting produced stability in the first three layers encountered in the solution that was not possible without the weighting.

Results

The results of this study are (1) a set of observed group-velocity dispersion curves for six surface-wave modes for a path across Central Mexico determined from a seismograph station with ultra-high sensitivity three-component inertial seismographs and strain seismographs, (2) statistical properties on the measurement variations from 108 earthquake-instrument pairs for the fundamental mode Rayleigh-wave and Love-wave group velocity dispersion curves; and (3) four similar models of the shear-wave velocities in the crust and upper mantle of Central Mexico.

The group-velocity dispersion curve for the fundamental mode Rayleigh-wave is plotted in Fig. 11; and the group-velocity dispersion curve for the fundamental Love-wave is plotted in Fig. 12. The central curves are the mean of the group velocities obtained from the multiple filter analysis. The other two curves in each figure are the mean plus and minus the average deviation from the mean (first moment). Statistical properties of the observations of group velocities are given in Table 4 for the fundamental Rayleigh-wave and in Table 5 for the fundamental Love-wave. The values of the sample mean in the fourth columns were smoothed with a seven point least squares



FIG. 11. Observed group-velocity dispersion curve with average deviation from the mean for fundamental mode Rayleigh wave.



FIG. 12. Observed group-velocity dispersion curve with average deviation from the mean for fundamental mode Love wave.

	Index	-	7	ę	4	ŝ	9	7	×	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33
ge	Min	2·7000	2.7000	2.7000	2.7000	2.7000	2.6800	2.6800	2.6800	$2 \cdot 7000$	2.7000	2.7000	2.7000	2.7000	2.7000	2.6600	2.6600	2.6500	2.6300	2.6400	2.6500	2.6400	2.6400	2.5700	2.5600	2.5600	2.5600	2.5600	2.5100	2.5200	2.6100	2.5800	2.5700	2.5400
Ran	Max	2.8400	2.8600	2.8600	$2 \cdot 8500$	2.8400	2.8400	2.8400	2.8500	2.8400	2.8600	2.8600	2.8500	2.8500	2.8600	2.8700	2.8700	2.8600	2.8600	2.8500	$2 \cdot 8600$	2.8600	2.8600	$2 \cdot 8700$	2.9000	2.9200	2.9100	$2 \cdot 8500$	2.8600	2.8600	2.8500	2.8400	2.8200	2.8200
No.	samples	47	47	48	48	48	50	50	50	51	51	52	53	57	57	59	58	59	61	60	60	59	57	57	58	99	99	99	2	65	2	63	65	62
Ave 1st	moment	0.0328	0.0345	0.0327	0.0304	0.0325	0.0328	0.0334	0.0348	0.0320	0.0314	0.0313	0.0281	0.0286	0.0296	0.0337	0.0390	0.0400	0.0389	0.0385	0.0367	0.0415	0.0433	0.0560	0.0569	0.0602	0.0586	0.0606	0.0556	0.0506	0.0375	0.0298	0.0271	0.0274
	Median	2·7800	2·7800	$2 \cdot 7700$	2.7650	2.7600	2.7600	2.7600	2.7600	2.7600	2.7600	2.7600	2.7600	2.7600	2·7600	2.7600	2.7600	2.7600	2.7500	2.7500	2.7600	2.7600	2.7600	2.7300	2.7200	2-7250	2.7400	2·7450	2·7400	2.7300	2.7100	2-7300	2.7400	2.7500
Std	dev.	0-0391	0.0406	0.0399	0.0375	0.0388	0.0394	0.0409	0.0424	0.0403	0.0387	0.0384	0.0370	0.0368	0.0376	0.0432	0.0473	0.0482	0.0481	0.0471	0.0458	0.0528	0.0529	0.0691	0.0717	0.0767	0.0747	0.0745	0.0705	0.0628	0.0471	0.0407	0.0379	0.0404
	Mean	2·7721	2·7743	2.7706	2·7683	2.7671	2·7656	2.7630	2·7624	2·7606	2·7612	2.7625	2.7636	2·7602	2·7591	2·7571	2.7528	2.7500	2·7482	2·7488	2.7513	2.7551	2.7519	2·7419	2.7383	2.7386	2.7386	2·7321	2·7272	2.7211	2·7209	2·7284	2·7431	2.7558
Smooth	mean	2.7729	2.7725	$2 \cdot 7713$	2·7692	2.7667	2·7652	2·7635	2.7619	2.7611	2.7618	2·7622	2·7622	2.7614	2.7591	2.7561	2·7531	2.7501	2·7485	2·7498	2·7524	2·7526	2.7495	2.7446	2.7404	2.7379	2.7364	2·7324	2·7264	2.7216	2·7228	2·7286	2.7412	2·7569
	Period	2.90680	3-07472	3.25233	3-44021	3.63895	3.84916	4·07152	4.30672	4.55551	4.81867	5.09703	5.39147	5.70292	6.03237	6 · 38084	6·74945	7-13935	7-55177	7-98802	8 • 44947	8-93757	9.45387	10.00000	10-57768	11.18872	11-83507	12.51875	13·24193	$14 \cdot 00688$	14.81603	15-67191	16.57724	17-53487
	Index	1	7	ŝ	4	5	6	7	×	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33

Statistics on observed group velocities Rayleigh-wave mode LR_0

Table 4

474

2.5400	2.5500	2.5700	2·7400	2.7500	2.9000	2.9100	2.9600	3.0300	3.0700	3.1200	$3 \cdot 1300$	3.2700	3.2800	3.2200	$3 \cdot 2400$	3.4600	3.4800	$3 \cdot 2800$	$3 \cdot 3600$	3.4600	3.3500	3.3200	3.3200	3.1500	3.3200	3.2100	3.3200	3-3200	3.2300	$3 \cdot 1600$	3.1500	$3 \cdot 1100$	3.0400	2.9500	$2 \cdot 8700$	2.7500	2.6900
2.8700	2.8900	2.9300	3.0100	$3 \cdot 1200$	$3 \cdot 2000$	3.2900	3.3500	$3 \cdot 4000$	3.4100	$3 \cdot 4700$	3.6800	$3 \cdot 6700$	3.6800	3 · 7200	3 · 7000	3.6800	3.7400	$3 \cdot 8200$	$3 \cdot 8900$	$4 \cdot 1600$	$4 \cdot 2400$	4.3000	$4 \cdot 2800$	$4 \cdot 0700$	3.8400	3-8500	3.5500	3.5600	3.6300	$3 \cdot 6000$	$3 \cdot 6300$	$3 \cdot 6600$	3.6000	3.0900	3.0500	3.0400	3 · 0200
62	8	57	51	51	45	35	28	27	26	20	21	20	20	21	19	19	18	17	17	16	16	13	12	13	10	6	7	7	9	Ś	4	4	÷	2	7	7	7
0.0331	0.0350	0.0389	0.0373	0.0422	0.0380	0.0480	0.0518	0.0574	0.0669	0.0705	0.1057	0.0860	0.0765	0.0833	0.0653	0.0532	0.0706	0.1047	0.1135	0.1194	0.1306	0.1585	0.1608	0.1331	0.0820	0.0933	0.0586	0.0800	0.0983	0.1280	0.1450	0.1975	0.2333	0.0700	0.0900	0.1450	0.1650
2.7700	2.800	2.8400	2.9000	2.9500	2.9900	$3 \cdot 0200$	$3 \cdot 0750$	3.1100	$3 \cdot 2000$	$3 \cdot 3150$	3.4100	3 • 5000	3 · 5450	3 · 5600	3 · 5500	3.5600	3.5600	3.5800	3.6000	3.6200	3.6550	3.5800	3.5950	3.5700	3.5250	3.4800	3.4200	3 • 4300	3.4500	3 • 4200	3.3600	3.2900	$3 \cdot 1100$	3.0200	2.9600	2.8950	2.8550
0-0478	0.0514	0.0566	0.0501	0.0592	0.0558	0.0711	0.0756	0.0795	0.0839	0.0924	0.1392	0.1080	0.0998	$0 \cdot 1133$	0.1004	0.0627	0.0810	0.1349	0.1365	0.1679	0.1947	0.2389	0.2463	0.2064	0.1357	0.1650	0.0776	0.0988	0.1408	0.1760	0.2009	0.2510	0.3051	0660.0	0.1273	0.2051	0.2333
2.7789	2.7993	2.8349	2.9024	2.9510	2.9889	3.0273	3.0832	3 · 1241	3.2054	3.3005	3.3852	$3 \cdot 4850$	3 · 5215	3.5333	3.5511	3.5716	3 · 5961	3.6165	3.6518	3.6769	3.6869	3.6500	3-6525	3.5977	3.5300	3 • 4944	3-4314	3.4329	3.4583	3.4260	3.3750	3.3375	3.2500	3.0200	2.9600	2.8950	2.8550
1477.0	2-8031	2.8455	2.8945	2.9441	2.9919	3-0302	3.0748	3.1350	3.2079	3.2983	3.3941	3.4678	3.5155	3.5417	3 • 5541	3.5708	3 • 5947	3.6225	3.6537	3.6701	3.6788	3 • 6689	3.6363	3 · 5941	3 · 5404	3.4809	3.4524	3.4438	3 • 4341	3 · 4252	3.4012	3.3149	3 · 2028	3.0780	2.9586	2.8812	2.8662
18.54781	19-61927	20-75263	21-95146	23 · 21954	24.56088	25.97970	27·48048	29-06796	30-74715	32.52334	34-40213	36.38946	38-49159	40.71515	43.06717	46.55506	$48 \cdot 18666$	50-97029	53.91471	57.02924	60.32368	63 · 80843	67 • 49448	71 · 39348	75.51770	79.88018	84-49466	89.37571	94.53873	100.00000	105-77675	111 - 88722	118-35067	125.18750	132-41928	140.06882	148 • 16025
74	5.5	36	37	38	39	40	41	42	43	4	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	8	61	62	63	2	65	99	67	68	69	70	11

Table 4 (continued)

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ŝ	
Table	1

Statistics on observed group velocities Love-wave mode LQ₀

	Index	1	7	m	4	ŝ	9	7	∞	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32
ge	Min	2.8600	2.8600	2.8600	2.8600	2.8400	2.8400	$2 \cdot 8200$	2.8200	$2 \cdot 8200$	2.8300	2.8300	2.8200	$2 \cdot 8200$	2.8200	$2 \cdot 8100$	2.8000	$2 \cdot 8000$	2.7900	2.7800	2.7900	2.8100	2.8000	2.8600	2.7600	2.8600	2.8700	2.8700	2.8100	2.7900	2.7800	2.9400	2.9500
Ran	Max	3.0000	2.9800	2.9800	2.9600	2.9600	2.9800	2.9800	2.9800	2.9800	2.9800	2.9600	2.9600	2.9700	2.9800	2.9800	2.9800	3.0200	3-0200	3.0700	3.0300	3.0200	3.0200	3.0300	3.0300	3.0600	3.0600	3.0500	3.0500	3.0700	3.2500	3.3200	3.3500
No.	samples	24	24	25	26	27	27	27	27	29	29	29	29	31	32	31	30	31	31	29	29	28	28	27	27	25	24	25	23	26	28	29	30
Ave 1st	moment	0.0267	0.0271	0.0288	0.0285	0.0263	0.0259	0.0270	0.0300	0.0314	0.0338	0.0286	0.0286	0.0297	0.0300	0-0355	0.0410	0.0416	0.0387	0.0386	0-0383	0.0407	0.0464	0.0456	0-0578	0.0432	0.0413	0.0392	0.0443	0.0377	0.0429	0.0393	0-0353
	Median	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9400	2.9300	2.9400	2.9200	2.9200	2.9200	2.9200	2.9500	2.9800	2 · 9900	2.9900	3.0100	3 · 0250	3.0350	3.0600	3 · 0950
Std	dev.	0.0350	0.0322	0.0343	0.0336	0.0330	0.0332	0-0365	0-0383	0.0395	0.0406	0.0367	0.0388	0.0399	0.0406	0.0460	0.0496	0.0516	0.0485	0.0553	0.0500	0.0499	0.0552	0.0517	0.0680	0.0540	0.0534	0.0500	0.0597	0.0575	0.0726	0.0630	0-0620
	Mean	2-9350	2-9346	2.9348	2.9308	2.9304	2.9307	2.9274	2.9259	2.9317	2.9272	2.9276	2.9276	2.9261	2.9287	2.9219	2.9190	2.9210	2·9213	2.9314	2.9297	2.9286	2.9236	2.9311	2.9285	2.9676	2.9779	2.9784	2.9909	3·0092	3.0329	3.0652	3.0987
Smooth	mean	2.9351	2.9347	2.9337	2.9323	2.9308	2.9285	2-9287	2.9283	2.9281	2.9286	2.9279	2-9274	2.9275	2.9253	2.9230	2.9203	2.9206	2.9242	2.9280	2.9285	2.9289	2.9238	2.9287	2.9420	2.9577	2.9714	2.9843	2.9918	3.0088	3-0347	3.0659	3.0973
	Period	2.90680	3.07472	3·25233	3.44021	3.63895	3.84916	4·07152	4.30672	4.55551	$4 \cdot 81867$	5.09703	5.39147	5.70292	6.03237	6.38084	6·74945	7.13935	7.55177	7.98802	8·44947	8-93757	9.45387	10.00000	10.57768	11.18872	11-83507	12-51875	13.24193	$14 \cdot 00688$	14.81603	15.67191	16.57724
	Index	1	7	ę	4	5	9	7	ø	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32

33	34	35	36	37	38	39	40	41	42	43	4	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	2	65
2.9800	2.9900	3.0300	3-0300	2.9400	3.1900	3·2000	3 · 2800	3.2700	3.2700	3.2700	3.2600	3.3000	3.4000	3-4300	3.4000	3 · 3400	3.2700	3.2100	$3 \cdot 1600$	3.6800	3.6100	3-4200	3.3200	$3 \cdot 2500$	$3 \cdot 3400$	3 · 2200	$3 \cdot 2400$	3.0800	2.9900	3.0400	3 • 5400	3-4400
3.3500	3-3500	$3 \cdot 3400$	3-3300	3.3300	3.3600	3.3900	3.4300	3.4500	3 · 7000	3.7400	3.7700	$3 \cdot 7800$	3.7600	$3 \cdot 7900$	3.9800	$4 \cdot 1300$	$4 \cdot 4000$	$4 \cdot 5300$	4.6400	$4 \cdot 1400$	$4 \cdot 1900$	$4 \cdot 1500$	$4 \cdot 2100$	$4 \cdot 3400$	4.4300	$4 \cdot 4800$	$4 \cdot 4800$	$3 \cdot 8200$	3.9000	$4 \cdot 0100$	$4 \cdot 1500$	$4 \cdot 2200$
31	31	30	31	35	36	37	36	36	40	36	36	35	30	31	29	28	26	25	23	20	21	19	16	17	16	15	13	6	6	8	9	ę
0.0381	0.0529	0.0513	0.0568	0.0449	0.0289	0.0292	0.0239	0.0292	0.0365	0.0433	0.0478	0.0580	0.0593	0.0790	0.0983	0.1064	0·1258	0.1288	0.1387	0.0970	0.1229	0.1505	0.2081	0.2453	0.2806	0.2767	0.2300	0.1889	0.2244	0.2588	0.1883	0.2667
3.1200	$3 \cdot 1400$	3.1650	$3 \cdot 2000$	3.2400	$3 \cdot 2800$	3.3100	$3 \cdot 3400$	3.3450	$3 \cdot 3700$	3.3950	$3 \cdot 4300$	3.4600	3 • 5050	3.5500	$3 \cdot 6200$	$3 \cdot 6750$	$3 \cdot 7200$	3.7600	$3 \cdot 8200$	3.8100	3.8300	$3 \cdot 8400$	3.8750	$3 \cdot 8600$	3 · 8250	3.7100	3-5900	3.4300	3.4900	3.6350	$3 \cdot 8400$	3.8000
0.0599	0.0712	0.0662	0.0726	0.0693	0.0384	0.0394	0.0319	0.0361	0.0640	0.0733	0.0789	0.0859	0.0853	0.0984	0.1282	0.1535	0.1954	0.2147	0.2469	0.1273	0.1528	0.1937	0.2666	0.3075	0.3342	0.3549	0.3206	0.2395	0.2913	0.3257	0.2452	0.3904
3 · 1294	3 · 1474	3 · 1687	3.1900	3 · 2351	3.2822	3.3051	3-3356	3.3514	3.3750	3.4011	3-4317	3 • 4774	3.5207	3.5771	3.6510	3.7064	3.7573	3 · 7908	3.8222	3.8485	3-8548	3 · 8289	3.8250	3.8359	3-8556	3-7433	3.6785	3 • 4978	3 • 5400	3.6088	3.8183	3.8200
3.1256	3 · 1469	3 · 1684	3 · 1987	3.2350	3 • 2740	3 · 3082	3.3327	3-3530	3.3751	3.4010	3 • 4344	3.4733	3 • 5240	3 • 5830	3.6455	3 · 7054	3.7549	3.7936	3 · 8265	3 · 8427	3.8446	3.8371	3·8434	3.8374	3 · 8248	3 · 7466	3.6425	3 • 5478	3.5611	3.6432	3 · 7461	3.8078
17-53487	18·54781	19-61927	20.75263	21-95146	23 • 21954	24 • 56088	25.97970	27 · 48048	29.06796	30-74715	32.52334	34-40213	36.38946	38-49159	40-71515	43.06717	45.55506	$48 \cdot 18666$	50-97029	53-91471	57-02924	60-32368	63 · 80843	67-49448	71 · 39348	75-51770	$79 \cdot 88018$	84 • 49466	89.37571	94.53873	100.00000	105 · 77675
33	34	35	36	37	38	3 6	40	41	42	43	4	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	09	61	62	63	2	65

Table 5 (continued)

smoothing (Lanczos 1956) to obtain the values in the third columns. The smoothed sample mean values were used in the inversions.

The smoothed values are essentially within 0.01 km s^{-1} or less from the mean values and are considered to be the better set of experimental group velocities. The sample standard deviations are given in the fifth column. In an attempt to improve the data set by removing outliers, the data were truncated at plus and minus one standard deviation in a manner similar to that used with body-wave data (Freedman 1966, 1968; Tucker, Herrin & Freedman 1968). When the standard deviation of the whole population was estimated from the standard deviation of the truncated sample and the p(k) factor for a normal distribution (Freeman 1966), larger estimates of the standard deviation were obtained than given in the table. Since 60 or more samples are available at many of the periods, the sample population should be a good representation of the whole population. Two conclusions are apparent: truncation of the data set is not valid and should not be used (that is, there are no samples that can be statistically deemed as outliers) and the distribution of samples is tighter than a normal distribution. The sample data set used in this study has not been truncated. The tight statistical distribution is the result of the resolution of the multiple filter analysis and of the diligence used in the data processing.

Claerbout & Muir (1973) have proposed the use of the sample median instead of the sample mean and the absolute value of the sample variation from the median instead of the square of the difference between a sample and the arithmetic mean. The sample median and the average sample variation from the mean are given in Tables 4 and 5. For these data, the medians are almost identical to the means. This identity is the result of a symmetrical two-sided distribution with no skewness to either early or late times. The errors in the observed group velocities quantized by the sample standard deviation and the average deviation from the mean include errors from (1) origin time, (2) hypocentre location, (3) initial phase of the source, (4) station timing errors, (5) non-great circle propagation paths, (6) interference from lateral refractions, (7) incomplete separation of modes, (8) incorrect digitizing start times and/or sampling rates, (9) mistakes in entering parameters into computer programs, (10) unknown bugs in computer programs, (11) incorrect picks of maxima on the multiple filter analysis output, (12) bias in the interpretation of the dispersion curve. Despite these sources of errors, the average deviation from the mean was between about 0.025 and 0.060 km s⁻¹ for both Rayleigh waves and Love waves for periods up to 35 s. At longer periods, the average deviation was about 0.060 to 0.160 km s⁻¹ for Rayleigh waves and between about 0.060 and 0.281 km s⁻¹ for Love waves. At the shorter periods, the Love-wave deviations are smaller than the Rayleigh-wave deviations, but at the longer periods, the situation is reversed. By inspection of the seismogram in Fig. 2, it can be seen that, at this epicentral distance, the fundamental Love wave begins about 40s after the S-wave arrival and among the higher mode Love-wave arrivals. Apparently, this mixture of modes has confused the analysis with the resulting large deviations from the mean among the 15-20 samples at each period from 45 to 75 s. Similar but more serious mixture of Love modes was observed by James (1971a) in South America and by Thatcher & Brune (1973) in Baja California.

Only limited data on surface-wave dispersion in Mexico are available in the literature. These data, all for fundamental Rayleigh waves, from Papazachos (1964), Santo (1965), Tarr (1969) and Thatcher & Brune (1973), are plotted as data points in Fig. 13 along with the LR₀ curve from this study. Agreement among the data points is exceptional for all paths except the Gulf of California–TUC and Baja California paths of Thatcher & Brune (1973).

Several group-velocity dispersion curves for the first higher mode Rayleigh wave LR_1 and the second higher mode Rayleigh wave LR_2 are plotted in Fig. 14. Several group-velocity dispersion curves for the first higher mode Love wave LQ_1 and the



FIG. 13. Observed group-velocity dispersion curve for fundamental mode Rayleigh wave from the literature.

second higher mode Love wave LQ_2 are plotted in Fig. 15. The scatter in groupvelocity of the higher modes is greater than for the fundamental modes. In the steep portions of the curves, it is better to consider the variation as taking place in period rather than in group velocity. Some energy from the higher modes can be seen, but is not contoured, in the multiple filter analyses illustrated in Figs 3, 4 and 5 which are plotted in terms of normalized linear amplitudes. The curves in Figs 14 and 15 were derived from the plots of normalized decibel amplitudes that show more detail for the smaller amplitudes. Because of the bias that the large slopes might introduce into numerical averages and because of lack of success with erroneously determined higher mode dispersion curves, I decided to use a set of typical dispersion curves for the higher modes that were actual observations from the real world and not average numbers that could have been masticated by numerical manipulation. The selected curves are shown with bolder lines in Figs 14 and 15. They were chosen as medians by visual inspection. The curves in Figs 14 and 15 were determined from the data by picking amplitude maxima in the multiple filter analysis in the general shape of theoretical dispersion curves calculated from preliminary solutions using the fundamental modes of Rayleigh wave and Love wave. Information on additional higher modes is contained in the data, but no satisfactory method was discovered of establishing the correct mode for the several prominent energy packets. This statement is especially applicable in the vicinity of the group velocity of 4.50 km s^{-1} . As can be seen in Fig. 2, this is the arrival time of the S wave. Tolstoy & Usdin (1953) and Satô, Usami & Landisman (1968) provide an understanding of the method by which normal modes can be summed to generate body waves. Theoretical group-velocity dispersion curves for the first five higher modes calculated for model FBR3 had a well-defined flat region between group velocities of 4.00 and 4.20 km s⁻¹ and another less well-defined flat region between group velocities of 3.25 and 3.50 km s⁻¹. Using



FIG. 14. Observed group-velocity dispersion curves for first higher and for second higher Rayleigh wave.

ray theory, the first flat region corresponds to the S-wave arrival. Similarly in the multiple filter analyses of this study, energy is detected over a large period range in the vicinity of 4.5 km s^{-1} . The velocity of the faster flat region in the theoretical curves is controlled by the 4.50 km s^{-1} shear-wave velocity in the lid of the mantle. The second flat in the theoretical curves corresponds to the Lg and Rg arrivals and is controlled by the 3.80 km s^{-1} shear-wave velocity in the bottom layer of the crust. Based on a qualitative comparison with Figs 14 and 15, the lid of the mantle should



FIG. 15. Observed group-velocity dispersion curves for first higher and for second higher Love wave.

have a shear-wave velocity greater than 4.5 km s^{-1} and the bottom layer in the crust should have a shear-wave velocity greater than 3.6 km s^{-1} .

A considerable number of inversions were made with various combinations of modes and with various combinations of data sets. The majority of the models from the solutions had the same general shape with low velocity zones in the same layers and with fast velocities in the same layers. Four preferred models are presented below. Two models (numbers 1 and 2) were generated from solutions with the high resolution

Table 6

Modes,	period	ranges	and	number	• of	`layers	used	in	the	inversion	for	models	1,	2,	A1
						and .	A2								

		Mod	lel		
Mode	1 and 2 Period range	No. of layers	Mode	A1 and A2 Period range	No. of layers
LR ₀ LQ ₀	10·0-71·4 10·0-71·4	28 28	LR0 LR1 LR2 LQ0 LQ1 LQ2	$10 \cdot 0 - 71 \cdot 4$ $15 \cdot 7 - 30 \cdot 7$ $9 \cdot 45 - 40 \cdot 7$ $10 \cdot 0 - 71 \cdot 4$ $14 \cdot 8 - 34 \cdot 4$ $8 \cdot 4 - 40 \cdot 7$	14 14 14 14 14

starting model FBR3 and the other two models (numbers A1 and A2) were generated from solutions with the starting model FBR3A that produced more stable results. Solutions for models 1 and A1 begin the inversion with the top layer; solutions for models 2 and A2 begin the inversion with the bottom layer. The modes, period ranges, and the number of layers used in these inversions are given in Table 6. The shear-wave velocities for models 1 and 2 along with those for model FBR3 are given in Table 7 for the upper 100 km of crust and upper mantle. These velocities are plotted in Fig. 16. The partial derivatives are small for layers 20–28 for the fundamental modes (see Figs 7 and 8) and the model 1 and 2 velocities are unrealistic for depths greater than 100 km and have not been presented. The shear-wave velocities for models A1 and A2 and model FBR3A are given in Table 8. The upper 100 km of crust and upper mantle 8. The upper 100 km of crust and upper mantle 8. The upper 100 km of crust and upper mantle 8. The upper 100 km of crust and upper mantle 8. The upper 100 km of crust and upper mantle 8. The upper 100 km of crust and upper mantle 8. The upper 100 km of crust and upper mantle are plotted in Fig. 17. The entire models are plotted in Fig. 18.

The Rayleigh-wave group velocity dispersion curves calculated from the four models are plotted in Fig. 19 with the observed smoothed mean plus and minus the average deviation from the mean for the fundamental mode and with the observed first and second higher mode 'median' dispersion curves. Similar curves are plotted in Fig. 20 for the Love-wave modes. The group velocities from the high resolution models 1 and 2 and for the fundamental Love wave for models A1 and A2 all lie well within the variation band of the observed fundamental modes. A comparison of Figs 19 and 20 with Figs 14 and 15 provides similar data for the higher modes. The second higher modes were fitted very well by the inversions and generally lie within the band of observations. The first higher modes were not fitted as well. Some of the variations from the high modes propagated into the residuals for the fundamental modes, especially the Rayleigh. The use of all six modes has provided a sharpening of the resolution kernel (Der *et al.* 1970; Jackson 1972), but the inclusion of the higher mode data with a larger variance has increased the residuals (Jackson 1972).

Discussion of results

The shear-wave velocity structures of the four inversion models in Figs 16-18 represent the lowest shear-wave velocities of any area of the world studied to date. These velocities are probably representative of other similar regions with high heat flow and high uplifted plateaus. In the following paragraphs, the physical properties of the velocities will be presented and then will be interpreted in terms of the generalized petrology, a representative geotherm, partial melting, and phase changes within the materials. Differences between S-wave travel times through the models are compared with S-wave station residuals.



FIG. 16. Upper 100 km shear-wave structure from inversion of fundamental mode Rayleigh-wave and Love-wave group velocities with starting model FBR3.

The inversion models 1 and 2 (Table 7, Fig. 16) have a four-layer 30 km thick crust with velocities corresponding to: a low-velocity sedimentary layer, a sedimentary rock layer, a granitic layer with a low velocity zone, and a basaltic layer with a low velocity zone. The mantle has a thin 4 km lid with a normal shear-wave velocity. Immediately below the lid partial melting occurs. (Partial melting percentages given in this part of the paper for the mantle are based on the shear velocities calculated by Birch (1969) based on spherical nodules of basalt melting along the solidus in a host



FIG. 17. Upper 100 km shear-wave velocity structure from inversion of fundamental mode, first higher mode, and second higher mode Rayleigh-wave and Love-wave group velocities with starting model FBR3A.

of olivine. Actual partial melting probably occurs in a planar structure along grain boundaries and the actual percentage of melt for the same shear-wave velocity may be significantly less than with the Birch spherical melt model.) Model 1 drops to a very low shear-wave velocity at a depth of 34 km implying an 18 per cent partial melting that gradually decreases to 5 per cent melt at the 100 km depth. Model 2 grades into



FIG. 18. Shear-wave velocity structure from inversion of fundamental mode, first higher mode, and second higher mode Rayleigh-wave and Love-wave group velocities with starting model FBR3A.

the lowest velocity that corresponds to 20 per cent partial melting at depths of 46-50 km. Model 2 decreases to about the same velocity and the same 5 per cent melt as model 1 at the 100 km depth. At depths below 100 km, models 1 and 2 have unrealistic shear-wave velocities. The partial derivatives of group velocity with respect to layer shear-wave velocity are small for the fundamental modes for the layers

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FIG. 19. Rayleigh-wave group-velocity dispersion curves: calculated from model 1,
2, A1 and A2, observed fundamental mode smoothed mean±average deviation from the mean, and observed 'median' higher modes.



FIG. 20. Love-wave group-velocity dispersion curves: calculated from model 1, 2, A1 and A2, observed fundamental mode smoothed mean±average deviation from the mean, and observed ' median' higher modes.

Table 7

Shear-wave velocities for starting model FBR3 and inversion models 1 and 2

			Shear-	Shear-wave velocity (km s ⁻¹)		
Layer No.	Depth at bottom (km)	Thickness (km)	Starting model FBR3	Model 1	Model 2	
1	1	1	1 - 50	0.896	0.980	
2	2	1	2.87	2.817	2.630	
3	4	2	2.87	2.974	2.709	
4	6	2	3.58	3.646	3.645	
5	10	4	3.58	3.296	3 • 503	
6	14	4	3.58	3.269	3.359	
7	18	4	3.58	3.377	3.177	
8	22	4	3.80	3.799	3.542	
9	26	4	3.80	3.487	3 • 577	
10	30	· 4	3.80	3.394	3.442	
11	34	4	4·50	4.428	4.263	
12	38	4	4.50	3.698	4.137	
13	42	4	4.50	3.823	4.039	
14	46	4	4·50	3.902	3.968	
15	50	4	4.47	4.016	3.555	
16	60	10	4.33	4.147	3.874	
17	70	10	4.12	4·102	3.920	
18	80	10	4.12	4.270	4.112	
19	100	20	4·13	4.283	4.372	

Table 8

Shear-wave velocities for starting model FBR3A and inversion models A1 and A2

		Shear-wave velocity (km s ⁻¹)			
Layer No.	Depth at bottom (km)	Thickness (km)	Starting model FBR3A	Model A1	Model A2
1	1	1	1 · 50	0.643	0
2	4	3	2.87	3 · 107	3.139
3	18	14	3.58	3.368	3.427
4	30	12	3.80	3.544	3 · 458
5	38	8	4.50	4.783	4.646
6	50	12	4.50	3.601	3-923
7	80	30	4·12	3.929	3.828
8	120	40	4 ·14	4.349	4.374
9	160	40	4·17	4.521	4.517
10	200	40	4.50	4.539	4 · 542
11	260	60	4.609	4.267	4.275
12	300	40	4.609	4.750	4.624
13	340	40	4.72	4.092	4.305
14	380	40	4.89	3.962	3.780

20-28 that are at depths greater than 100 km (see Figs 7 and 8). These solutions lost resolution for the thin layers of these models at depths greater than 100 km, and the results have not been presented.

Inversion models A1 and A2 (Table 8, Figs 17 and 18) have similar features to models 1 and 2. The crust has four layers, but the thicker layers eliminate the possibility of low velocity zones. However, the velocities are low for the granitic and basaltic layers, and are representative of the velocities in the middle of the LVZ's of

models 1 and 2, lending support to their existence. The mantle has as thin a lid as the model will allow-8 km. This lid in both models has the high velocities that were expected based on the 4.5 km s^{-1} flat region for the higher modes (Figs 14 and 15). Immediately below the lid the models have low velocity zones. Model A1, similar to model 1 that also started with the top layer, decreases to a velocity corresponding to 20 per cent partial melt between depths of 38 and 50 km, then grades up to a velocity indicating 5 per cent partial melt at depths of 80-120 km. Model A2, similar to model 2 that also started with the bottom layer, grades into a 16 per cent partial melt at depths between 50 and 80 km and then the velocity increases to that related to 5 per cent melt at depths of 80 to 120 km. Models A1 and A2 differ by only 0.003 to 0.025 km s^{-1} at depths between 80 and 260 km and follow each other closely to the bottom of the models at the 380 km depth. Models A1 and A2 have a low velocity zone at depths between 200 and 260 km. Also, there is no sharp velocity increase at the 160 km depth. Below the 300 km depth models A1 and A2 enter still another LVZ. The Ibrahim & Nuttli (1967, also Nuttli 1969) model has a LVZ at depths between 341 and 391 km with a minimum of 4.40 km s^{-1} at 371 km. One of the Hales & Roberts (1970) models (SLUTD1) retained the Ibrahim and Nuttli depths, but it required a minimum velocity of $4 \cdot 10 \text{ km s}^{-1}$. The other Hales and Roberts model (SLUTD2) did not have this LVZ, but required an exceptionally sharp increase in velocity at the depth of 391 km. All the other models given in the literature and shown in Fig. 6 have large velocity gradients near the 400 km depth.

These physical velocity features of the four inversion models now will be interpreted in terms of a representative geotherm and of the melting temperatures of representative rocks combined with a solid-solid phase change below 380 km depth. Herrin (1972) was able to create models of the Canadian Shield and the Basin and Range that had consistent mineralogy between the two provinces, but that differed only in the temperatures between the surface and a depth of about 400 km. Similarly, the majority of the velocity structure of the inversion models can be explained by the geotherm. A heat flow model was established and temperatures were calculated for several depths. The heat flow along this path is high and a surface heat flow of about 2.4×10^{-6} cal cm⁻² s is probably representative (D. D. Blackwell 1974, private communication). The heat flow model is based on a surface layer of constant heat generating material and a constant mantle heat flow (Birch, Roy & Decker 1968). The parameters assumed for calculation of the central Mexico geotherm are given in Table 9 and the temperatures are given in Table 10. For comparison, the Basin and Range model of Blackwell (1971) with the highest temperatures is also given in Tables 9 and 10. With the higher heat flow and similar conductivities, the central Mexico geotherm model is seen to be higher than the Basin and Range geotherm. The central Mexico geotherm is plotted in Fig. 21 on a part of the diagram of pressure and temperature fields for the petrologic model of a mantle of Pyrolite III composition taken from Green & Ringwood (1970). The oceanic and pre-Cambrian shield geotherms from Clark & Ringwood (1964) are included for comparison. The central Mexico geotherm and the Pyrolite III models substantiate: (1) the need for a thin, solid lid to the mantle, and (2) the requirement for partial melting in the uppermost portions of the mantle. The actual geotherm will follow the solidus from the beginning of melt to a depth at which the geotherm is lower than the solidus. The models of Table 9 and the temperatures given in Table 10 do not reflect melting and are not representative of the thermal regime below depths of about 35 km. To represent a central Mexico geotherm without melting, a line has been sketched in the figure using the general shape of the other two geotherms and approaching the same temperatures at about a 400 km depth. This sketched line is seen to cross the Pyrolite III solidus in the vicinity of the 180 km depth. However, both the geothermal model and the mineralogical model are subject to large unknowns at these pressures and temperatures. The depth of 260 km from models A1 and A2 has a larger velocity discontinuity

Depth to Depth to Thet layer 2 mantle 10 ⁻³ . (km) layer 1	18 30 6-5	10 30 6-5
Heat I generation 10 ⁻¹³ cal cm ³ s	5.0	5.3
Depth of heat generating layer (km)	10	10
Mantle heat flow μcal $cm^2 s$	1.9	1.37
Surface heat flow $\frac{\mu cal}{cm^2 s}$	2.4	1.90
Model	Central Mexico	Basin anu Range 1 (Blackwell 1971)

Table 9

Models for temperature-deptin calculations

Table 10

Depth	Temperature (°C)		
(km)	Central Mexico	Basin and Range 1	
0	0	0	
5	175	136	
10	331	252	
15	477	389	
20	641	526	
25	831	663	
30	1021	800	
35	1116	937	
40	1211	1074	
45	1306	1211	
50	1401	1348	

Temperature versus depth for models of Table 9

that probably represents the bottom of the melt layer. Based on Fig. 21, the discontinuities at the 70 and 80 km depths in models 1 and 2 and at the 80 km depth in models A1 and A2 may represent the phase change from pyroxene pyrolite with a spinel and pyroxene mixture to garnet pyrolite with a garnet and olivine mixture. If this interpretation is correct, it suggests at least a 6 per cent alumina content in a pyrolite mantle. An alternate interpretation in terms of water content is presented in the next paragraph.



PRESSURE (kb)

FIG. 21. Central Mexico geotherm model diagrammed with pressure, temperature, and petrologic model of mantle of Pyrolite III composition after Green & Ringwood (1970), with oceanic and Precambrian shield geotherms after Clark & Ringwood (1964).

The sharp discontinuity, the extreme low velocities, and the apparent high percentages of partial melting (based on Birch's velocities) just under the mantle lid can be explained fully in terms of the geotherm. However, fluid (water) pressure may be a significant contributor to the extent of the decrease in velocities. Anderson & Sammis (1970) have reasoned that the upper boundary of melting is also at the region of instability of the hydrous mineral phases and of the first appearance of free water with depth. A small amount of water (0.1 per cent) can lower the melting temperature by as much as 200 °C (Ringwood 1969; Anderson & Sammis 1970). However, as more host rock melts, the small amount of free water becomes a lower concentration within the melt and the melting temperature rises, approaching the anhydrous melting temperature. Consequently, for the mantle to have 5 per cent or more partial melting in the presence of 0.1 per cent water, the temperatures must be very near the anhydrous solidus (Ringwood 1969). Ringwood (1969), Green (1970), Green & Ringwood (1970) and Lambert & Wyllie (1970) suggest that the water can be supplied from the source rock by amphibole as hornblende or perhaps phlogopite. Hornblende is not stable above 1000–1100 °C (Yoder & Tilley 1962; Lambert & Wyllie 1970; Green & Ringwood 1970) and on decomposition will release water to the melt phase. In the source pyrolite, at pressures greater than about 27 kbar (Green & Ringwood 1970), hornblende will not be present and the possibilities for free water from the host rock would cease. In the models of this study the hydrostatic pressure is 27 kbar near a depth of 85 km. Therefore, the seismic discontinuities at depths 70 and 80 km in models 1 and 2 and 80 km in models A1 and A2 could be an indication of the lower extreme of the amphibole and free water region rather than the pyroxene pyrolite to garnet pyrolite phase change suggested in the previous paragraph.

The above hypothesis of the presence of a small amount of water in the melted zone immediately below a thin, hot, solid lid requires a hypothesis to explain why the lid does not melt also. In fact, this contradiction can be used as an argument against water content in the mantle. However, if heat was introduced at a significant depth into the mantle within recent geologic time, the heat transport may have not yet reached to the top of the mantle. This heat could have been introduced by anomalously large motions at the friction contact between the lithosphere and the athenosphere, or it could have been introduced by a palaeosubduction zone that is an extension of the zone at the Central American Trench.

In contrast to the model of spherical melt inclusions of Birch (1969), Walsh (1969) derived equations for elastic properties of a two-phase material composed of a solid isotropic matrix with randomly oriented thin elliptical inclusions of melt. The elastic properties of the mixture are a function of the elastic properties of the two phases, the melt concentration, and the aspect ratio of the melt zones. The cube of the aspect ratio appears in the equations for the elastic properties; whereas, the melt concentration appears only to the first power. Thin elliptical melt zones along grain boundaries are a more reasonable model for partial melting than the spherical geometry. Using the Walsh (1969) theory, Anderson et al. (1972) have plotted seismic velocities against melt concentration for several aspect ratios for a solid olivine matrix with basalt melt. The minimum LVZ velocity of 3.601 km s^{-1} from model A1 can be achieved with an aspect ratio of 1 and 20 per cent melting (Birch's model) or aspect ratios and per cent melting ratios, respectively, of about 5×10^{-2} and 10 per cent or 5×10^{-3} and 1 per cent. With elliptical melt zones 200 times as long as they are high, the LVZ of the four models can be interpreted as resulting from less than 10 per cent melting. Exact estimates of partial melting must wait for experimental evidence on the geometry of melt inclusions at mantle pressures and temperatures. Spetzler & Anderson (1968) have observed seismic velocities and attenuation in a NaCl, brine, ice system that showed a sudden decrease in velocity and increase in attenuation for minute concentrations of melt at the eutectic temperature. These sudden changes are in agreement with the Walsh theory.

Another factor that could create the asymmetric concentration of low velocities immediately below the lid as indicated by the inversion models 1 and A1 is the upward migration of both free water and low melting temperature minerals. In other words, this velocity structure is the consequence of differentiation of basaltic magma within the mantle. Ringwood (1969) estimates that 5 per cent partial melting is about the lower bound for the melt to become unstable and to rise forming magma chambers. Since Mexico does have current volcanic activity, the active generation of magma in the mantle is a realistic possibility.

At this point, a new hypothesis is presented on the uplift of high flat plateaus. As melting occurs, the density and the viscosity decrease and the molten material becomes more mobile and rises. When it reaches the bottom of the solid lid, it is blocked from further upward migration within the material. As melting increases, the gravity differential increases and a large uniform upward force is exerted throughout the region. Woollard (1972) gives the Bouguer gravity anomaly in the central Mexico highlands as an almost constant -200 mgal with a few small contours of -220 mgal. The Pratt-Hayford isostatic anomaly is about -20 mgal for a compensation depth of 113.7 km. These gravity anomalies substantiate the existence of a large vertical regional force. This large force acts to raise the region as a flat entity and the high plateau is formed. This hypothesis can be applied to the central highlands of Mexico by the seismic low velocities found in this study. It is possible that similar forces have created the Colorado Plateau. Very few heat flow determinations have been made in this province (Roy, Blackwell & Decker 1972). However, the Sn velocity across the Colorado Plateau from Rangely, Colorado, to OC-AZ is about 10 per cent slower than the Sn velocity from the Nevada Test Site (NTS) to QC-AZ (Fix & Sherwin 1972). This significantly slower shear-wave velocity suggests that the Colorado Plateau may have a mantle similar to central Mexico. Woollard (1972) shows a Bouguer gravity anomaly of about -200 to -280 mgal in the Colorado Plateau that is very similar to the Bouguer anomaly of -200 to -220 mgal in the central Mexico highlands. The physical processes causing the Colorado Plateau to rise may also be contributing to the east-west tensional forces within the Basin and Range Province to the west.

A low-velocity zone begins at a depth of 300 km and extends to the bottom of the models A1 and A2 at a depth of 380 km. This LVZ corresponds to similar LVZ's in the shear-wave models of Ibrahim & Nuttli (1967) and Hales & Roberts (1970). Two possible mechanisms could cause the LVZ at these depths. This depth is the region of the transition from olivine to spinel. Spinel has a low critical thermal gradient for shear-wave velocity. For a temperature gradient greater than $0.69 \,^{\circ}C \,\mathrm{km^{-1}}$ in spinel the shear-wave velocity will decrease with depth (Liebermann & Schreiber 1969; Anderson & Sammis 1970). The second possible mechanism is the decrease of the shear modulus from instability in the crystal lattices prior to the olivine-spinel solid-solid phase change (Anderson & Julian 1969; Ahrens 1972). The extreme low velocities of models A1 and A2 and the high temperature gradients in the upper mantle, suggest that both mechanisms are probably in effect in central Mexico.

The central Mexico geotherm is plotted in Fig. 22 on a diagram of the pressure and temperature fields for crustal rocks. The solidus curve for water saturated granite and the solidus and liquidus curve for water saturated olivine tholeiite in Fig. 22 are taken from Yoder & Tilley (1962). The depths for model FBR3 are given at the corresponding hydrostatic pressures and the low-velocity regions of models 1 and 2 are indicated. The olivine tholeiite was selected as a typical basalt, but other basaltic compositions have similar solidus and liquidus curves (Yoder & Tilley 1962). The central Mexico geotherm intersects the basalt solidus exactly at the beginning of the LVZ. These data imply that the base of the crust very probably is a partially molten zone. Anderson & Sammis (1970) reached the similar conclusion that in the Basin and Range province partial melting is implied at the base of the crust. Accord-



FIG. 22. Central Mexico geotherm model diagrammed with pressure and temperature curves for water saturated granite and olivine tholeiite after Yoder & Tilley (1962).

ing to the thermal models in Tables 9 and 10 the temperatures at the 30 km depth in central Mexico are about 220 °C higher than in the Basin and Range. Another explanation of the LVZ in the basaltic layer is the thermal gradient of 38 °C km⁻¹. This gradient is well in excess of the 2–3 °C km⁻¹ critical gradient for common minerals (Liebermann & Schreiber 1969). Thus, this LVZ can be explained only in terms of the high thermal gradient and it is not necessary to insist on a water saturated rock or even on partial melting.

The central Mexico geotherm does not hit the water saturated granite solidus until depths below the granitic layer implying that the granitic layer does not have partial melting. In the granitic layer the gradient of the geotherm is $29 \,^{\circ}\text{C}\,\text{km}^{-1}$. This gradient is also well in excess of the critical gradient for common minerals and explains the LVZ.

The extreme low velocities found in the inversion models are capable of explaining the large S-wave station residuals. Doyle & Hales (1967) and Hales & Herrin (1972) report S residuals for stations within the US that range from -4.5 s (early) in the midwest to +3.3 s (late) in the Basin and Range Province. Previous shear-wave models have not provided sufficient time delays to explain this maximum 7.8 s time difference. The time for shear waves to travel vertically through several models from a 400 km depth is given in Table 11 relative to the 88.40 s required to travel through the CANSD model of Brune & Dorman (1963). The CANSD model is taken as representative of the stable pre-Cambrian shields with the fastest times of any tectonic province. From the table, it can be seen that all previous models, including the several that were based only on seismic waves that traversed the Basin and Range province.

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Table 11

Shear-wave travel times from a depth of 400 km to the surface for several models

Model	Time through model minus time through model CANSD (sec)	Reference
CANSD	0*	Brune & Dorman (1963)
DUG-TUC	0.22	Wickens & Pec (1968)
Lehman	0.43	Dorman et al. (1960)
(NE America)		
STAN 3	1.16	Kovach & Robinson (1969)
(TFO array)		
Ibrahim & Nuttli	1.29	Ibrahim & Nuttli (1967)
(US and NTS)		Nuttli (1969)
SLUTD1	1.44	Hales & Roberts (1970)
(US)		
FBR3A	2.54	This study
(Basin and Range)		-
B&R III	4.60	Pilant (1967)
Model A1	7.46	This study
Model A2	7.59	This study
Model 1	8.14	This study
Model 2	12.28	This study

* Absolute time through CANSD is 88.40 s

cannot explain the 7.8-s travel-time difference. Models A1 and A2 of this study provide 7.46 and 7.59 s delays and almost exactly explain the variations in station residuals that have been observed. Model 1 exceeds the travel time slightly, but model 2 is too slow. These times are the result of the low velocities at depths below 120 km in models 1 and 2 that are unrealistic and that are below the depth of accurate velocities for the high resolution model. The models from this study can explain the S-wave station residuals because the path through central Mexico has the low velocity structure over a sufficient distance that it can be accurately sampled with surface waves. The areas in the Basin and Range Province with the highest S-wave station residuals are smaller. Unless carefully planned, surface-wave studies in these areas will average the regions of lowest velocities with regions of higher velocities to obtain intermediate models that cannot explain the S-wave residuals. Refraction P-wave studies have a similar sampling problem and the lowest velocities are averaged with higher velocities along the path. Inversion of body wave travel time and $dT/d\Delta$ curves does not provide a unique solution (Gerver & Markushevich 1966; Wiggins, McMechan & Toksöz 1973) in the low velocity zone and investigators to date have not found it necessary to try models with low velocities as extensive as found in this surface-wave study.

Summary

Group velocity dispersion curves have been determined by multiple filter analysis for a path across central Mexico for the fundamental mode, first higher mode, and second higher mode for Rayleigh waves and for Love waves. The fundamental mode curves have slower velocities than average continental paths. Both the Rayleigh-wave and the Love-wave curves peak at a period of about 60 s and decrease toward longer periods.

Eighteen closely-grouped earthquakes and ultra-high-sensitivity three-component

inertial LP seismographs and three-component strain LP seismographs provided 108 earthquake-instrument pairs. This quantity of data provided a basis for investigating errors in group velocity determinations. The average deviation from the mean was between about 0.025 and 0.060 km s⁻¹ for Rayleigh waves and Love waves at periods shorter than 35 s. At longer periods the average deviation was between about 0.060 km s⁻¹ for Rayleigh waves and between about 0.060 and 0.160 km s⁻¹ for Rayleigh waves and between about 0.060 and 0.281 km s⁻¹ for Love waves.

The inversion technique of Bloch has been extended so that many options can be exercised in the inversion program. An important addition has been a layer-iteration weighting that provides stability for the first layers encountered in a solution.

The central Mexico group velocity dispersion curves have been inverted with a least squares layer by layer technique. Two high resolution models and two more stable inversion models are presented.

These models contribute valuable insight into the composition and thermal state of the crust and mantle. All four inversion models have a 30 km thick crust with four layers: a low-velocity sedimentary layer, a sedimentary rock layer, a granitic layer with a low velocity zone resulting from a high geothermal gradient but without melting, and a basaltic layer with a low velocity zone at depths between 22 and 30 km resulting from either the high geothermal gradient or partial melting of a wet basalt or a combination of these two factors. The mantle has a thin lid that is 4-8 km thick and may have a higher than normal mantle shear-velocity. Partial melting occurs immediately below the lid. The velocities correspond to partial melting of 20 per cent according to Birch's (1969) theory of partial melting and are probably greater than 10 per cent according to Walsh's (1969) theory. The sharpness and depth of the LVZindicate mass transport of magma to the underside of the solid lid. The low velocities and their change of partial melt with depth can be explained by an anhydrous Pyrolite III model. However, the data also suggest the need for partial water pressure in the mantle. The water comes from amphiboles that do not remain stable at pressures corresponding to a depth of about 70 km. The sharp velocity increase at this depth is possibly a combination of the bottom of the water zone and phase change from pyroxene pyrolite to olivine pyrolite. The partial melt zone continues to a depth of 260 km in the anhydrous condition with smaller percentages of melt. At a depth of 300 km, another low velocity zone begins probably under the combined effect of instabilities in the crystal lattices just prior to the olivine-spinel solid-solid phase change and of the geothermal gradient exceeding the $0.69 \,^{\circ}\text{C km}^{-1}$ critical shear-wave gradient of spinel. The instabilities in the crystal structure result in a negative pressure derivative for the shear modulus. Supplementary correlation is obtained for the partial melting and the low velocities by large negative Bouguer gravity anomalies and by a representative calculated geotherm and the melting temperatures of crust and mantle rock species.

The shear-wave velocities of the four inversion models are the first published that can explain the 7.8-s S station residual variation in North America.

A new hypothesis is presented concerning high flat plateaus. As melting occurs, density decreases providing a buoyancy force and viscosity decreases aiding mobility of the molten mass. The melting and mobility are aided by partial water pressure available from melted amphiboles. The light hot magma rises to the base of the lid where further movement is blocked. However, the ligher material exerts a regionally uniform vertical force that is capable of lifting the central Mexico highlands normal to the local gravity vector. It is suggested that the Colorado Plateau may be the result of a similar regional uplift.

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