

THE DEMAND FOR BEER, WINE AND SPIRITS:

A SYSTEM-WIDE ANALYSIS

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A SYSTEM-WIDE ANALYSIS\*

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## 1. INTRODUCTION

The system-wide approach to the analysis of consumer demand considers the multivariate structure of the problem in which the consumer allocates his income to all goods simultaneously. This approach combines the theory of the consumer with empirical analysis and has enjoyed much popularity over the past decade. For surveys of these developments, see Barten (1977), Brown and Deaton (1972), Philips (1974), Powell (1974), Theil (1975/76, 1980) and Theil and Clements (1980).

Most previous applications of the system-wide approach have used national accounts commodity groups (food, clothing, housing and so on). For many business and government policy purposes, however, these groups are much too broad. For example, to analyse the effects on consumption of all but the simplest changes in indirect taxes, we would need considerably more disaggregation. Similarly, market researchers need to analyse demand at the individual product level for purposes of forecasting and formulating pricing and other policies. The objective of this paper is to use the consumption of beer, wine and spirits to illustrate how the approach can be applied to give insights into the structure of demand for more narrowly defined commodity groups. When the consumer's utility function is appropriately separable in alcoholic beverages and all other goods, it is possible to confine our attention to the three beverages and ignore all other goods. In Section 2 of the paper we set out the so-called differential version of the system-wide approach. In Section 3 we use the alcohol data to estimate demand equations for beer, wine and spirits. We then use the demand model in Sections 4 and 5 to (i) explain the rapid growth of wine consumption and (ii) measure the welfare cost of alcohol taxes. Section 6 contains concluding comments. In a subsequent paper we will use the demand equations to formulate optimal tax packages for the alcoholic beverages.

## 2. DIFFERENTIAL DEMAND EQUATIONS

In this section we first formulate the consumer's demand equations for all  $n$  goods in terms of differentials. These are unconditional demand equations as they depend on all prices and total expenditure. The coefficients of these equations are not necessarily taken to be constant, so the model is general. We then block the  $n$  goods such that they form groups which are separable in the consumer's utility function. This leads to a composite demand equation for each group, as well as conditional demand equations within each group. The variables of the conditional equation are exclusively concerned with the group to which the good belongs, allowing us to focus attention on demand within the group. Finally, for estimation we set out a Rotterdam parametrization. This section is based on Theil (1975/76, 1980).

### Unconditional Demand Equations

We write  $p_i, q_i$  for the price and quantity demanded for good  $i$  ( $i=1, \dots, n$ ),  $M = \sum_{i=1}^n p_i q_i$  for total expenditure ("income" for short), and  $w_i = p_i q_i / M$  for the  $i^{\text{th}}$  budget share. Under general conditions, the demand for good  $i$  can be written as (see Appendix)

$$(1) \quad w_i d(\log q_i) = \theta_i d(\log Q) + \sum_{j=1}^n v_{ij} d\left(\log \frac{p_j}{P'}\right),$$

where  $\theta_i = \partial(p_i q_i) / \partial M$  is the  $i^{\text{th}}$  marginal share;  $d(\log Q) = \sum_{i=1}^n w_i d(\log q_i)$  is the Divisia volume index of the change in the consumer's real income;  $d(\log p_j / P')$  is to be interpreted as the change in the deflated price of  $j$   $d(\log p_j) - d(\log P')$ , where  $d(\log P') = \sum_{i=1}^n \theta_i d(\log p_i)$  is the Frisch price index; and

$$(2) \quad v_{ij} = \lambda p_i u^{ij} p_j / M$$

is the  $(i, j)^{\text{th}}$  price coefficient, where  $\lambda$  is the marginal utility of income

and  $u^{ij}$  is the  $(i,j)^{th}$  element of the inverse of the Hessian of the utility function  $[\partial^2 u / \partial q_i \partial q_j]^{-1}$ . In view of (2), the symmetry of this Hessian means that the matrix of price coefficients  $[v_{ij}]$  is also symmetric. A sufficient second-order condition for a budget-constrained maximum is that the Hessian be negative definite; (2) thus implies that  $[v_{ij}]$  is negative definite.

The variable on the left of (1) has the dual interpretation as

(i) the contribution of good  $i$  to the Divisia volume index and (ii) the quantity component of the change in  $w_i$ ,  $dw_i = w_i d(\log p_i) + w_i d(\log q_i) - w_i d(\log M)$ . Equation (1) explains the change in the demand for  $i$  in terms of changes in real income and relative prices. By dividing both sides by  $w_i$ , we find that  $\theta_i/w_i$  and  $v_{ij}/w_i$  are the income and price elasticities, respectively. The marginal share  $\theta_i$  tells us what fraction of an additional dollar of income is spent on good  $i$ , with  $\sum_i \theta_i = 1$ . The price coefficient matrix  $[v_{ij}]$  is interpreted as being inversely proportional to the Hessian matrix of the utility function in expenditure terms (Theil, 1975/76, p. 29). The price coefficients are subject to the constraint that the row sums of  $[v_{ij}]$  are proportional to the corresponding marginal shares (see Appendix),

$$(3) \quad \sum_{j=1}^n v_{ij} = \phi \theta_i \quad i=1, \dots, n,$$

where  $\phi = (\partial \log \lambda / \partial \log M)^{-1}$  is the reciprocal of the income elasticity of the marginal utility of income. We shall refer to  $\phi$  as the income flexibility.

#### Block-Independent Preferences

Let the  $n$  goods now be divided into  $G$  groups,  $S_1, \dots, S_G$ , such that each good belongs to only one group. Further, let the consumer's preferences be such that the utility function is the sum of  $G$  sub-utility functions, each involving the quantities of only one group,

$$(4) \quad u(q) = \sum_{g=1}^G u_g(q_g),$$

where  $q = [q_1, \dots, q_n]'$  and  $q_g$  is the vector of the  $q_i$ 's that fall under  $S_g$ . Then, when the goods are numbered appropriately, the Hessian  $[\partial^2 u / \partial q_i \partial q_j]$  and its inverse become block-diagonal. Accordingly, specification (4) is known as block-independent preferences (Theil, 1975/76).

Under block-independence,  $v_{ij} = 0$  for  $i$  and  $j$  in different groups [see (2)] and (3) for  $i \in S_g$  becomes

$$(5) \quad \sum_{j \in S_g} v_{ij} = \phi \theta_i \quad g=1, \dots, G.$$

The demand equation (1) for  $i \in S_g$  becomes

$$(6) \quad w_i d(\log q_i) = \theta_i d(\log Q) + \sum_{j \in S_g} v_{ij} d\left(\log \frac{p_j}{P'}\right),$$

so that the only deflated prices which appear are those of goods belonging to the same group as  $i$ .

#### Composite Demand Equations

We write  $W_g = \sum_{i \in S_g} w_i$  and  $\Theta_g = \sum_{i \in S_g} \theta_i$  for the average and marginal shares of group  $g$ , and define the group volume and Frisch price indexes as  $d(\log Q_g) = \sum_{i \in S_g} (w_i/W_g) d(\log q_i)$ ,  $d(\log P'_g) = \sum_{i \in S_g} (\theta_i/\Theta_g) d(\log p_i)$ . If we then add (6) over  $i \in S_g$  and use (5) and the symmetry of  $[v_{ij}]$ , we obtain the composite demand equation for  $S_g$  as a group (see Appendix),

$$(7) \quad W_g d(\log Q_g) = \Theta_g d(\log Q) + \phi \Theta_g d\left(\log \frac{P'_g}{P'}\right).$$

Thus only the deflated price of the group  $d\left(\log \frac{P'_g}{P'}\right) = d(\log P'_g) - d(\log P')$  and income affects the demand for the group as a whole. The income and own-price elasticities for the group are  $\Theta_g/W_g$  and  $\phi \Theta_g/W_g$ , respectively. This own-price elasticity is the elasticity of the Divisia volume index of the group with respect to the Frisch-deflated Frisch price index of the group.

### Conditional Demand Equations

Combining (6) and (7) we obtain (see Appendix)

$$(8) \quad w_i d(\log q_i) = \frac{\theta_i}{\theta_g} w_g d(\log Q_g) + \sum_{j \in S_g} v_{ij} d\left(\log \frac{p_j}{p_g}\right).$$

This is the demand equation for  $i \in S_g$ , given the demand for the group as a whole  $w_g d(\log Q_g)$ . As the variables on the right of this equation are exclusively concerned with the group  $S_g$  to which the  $i^{\text{th}}$  commodity belongs, it is known as a conditional demand equation. The term  $\theta_i/\theta_g$  is the conditional marginal share of  $i$  within the group  $S_g$ , with  $\sum_{i \in S_g} \theta_i/\theta_g = 1$ . This share answers the question, if income increases by one dollar, resulting in a certain additional amount spent on the group  $S_g$ , what is the proportion of this additional amount that is allocated to  $i$ ?

Equation (8) can be formulated in terms of absolute (undeflated) prices by using the definition of  $d(\log p'_j)$  [see above (7)] to write the price term as

$$(9) \quad \begin{cases} \sum_{j \in S_g} v_{ij} \left[ d(\log p_j) - \sum_{k \in S_g} \frac{\theta_k}{\theta_g} d(\log p_k) \right] \\ = \sum_{j \in S_g} v_{ij} d(\log p_j) - \phi \theta_i \sum_{k \in S_g} \frac{\theta_k}{\theta_g} d(\log p_k) \\ = \sum_{j \in S_g} (v_{ij} - \phi \theta_g \theta'_i \theta'_j) d(\log p_j) = \sum_{j \in S_g} \pi_{ij}^g d(\log p_j), \end{cases}$$

where the first step is based on (5);  $\theta'_i = \theta_i/\theta_g$  is the conditional marginal share of  $i$ ; and

$$(10) \quad \pi_{ij}^g = v_{ij} - \phi \theta_g \theta'_i \theta'_j \quad i, j \in S_g$$

is the  $(i, j)^{\text{th}}$  conditional Slutsky coefficient. This coefficient describes the effect of a price change of  $j$  on the demand for  $i$  ( $i, j \in S_g$ ) under the condition that the total consumption of the group remains constant.

Substitution of the fourth member of (9) in (8) gives the absolute price version of the conditional demand equation for  $i \in S_g$ ,

$$(11) \quad w_i d(\log q_i) = \theta'_i w_g d(\log Q_g) + \sum_{j \in S_g} \pi_{ij}^g d(\log p_j).$$

By dividing both sides of this equation by  $w_i$ , we find that  $\frac{\theta_i}{\theta_g} \frac{w_g}{w_i} = \frac{\theta_i/w_i}{\theta_g/w_g}$  is the ratio of the income elasticity of the good to that of the group to which it belongs. We shall refer to this ratio as conditional income elasticity of  $i$ . We also find that  $\pi_{ij}^g/w_i$  is the conditional price elasticity; i.e. the elasticity of  $q_i$  with respect to the absolute price  $p_j$  ( $i, j \in S_g$ ).

It follows from (5) and (10) and the fact that  $\sum_{j \in S_g} \theta'_j = 1$  that

$$(12) \quad \sum_{j \in S_g} \pi_{ij}^g = 0 \quad i \in S_g.$$

This reflects the homogeneity proposition that a proportionate change in all prices in the group, total consumption of the group remaining unchanged, does not affect the demand for any good in the group. We shall refer to (12) as demand homogeneity.

If  $S_g$  consists of  $n_g$  commodities, the  $n_g \times n_g$  matrix of price coefficients referring to  $S_g$  is a principal submatrix of the  $n \times n$  price coefficient matrix  $[v_{ij}]$ . As the latter matrix is symmetric, so is the former. It then follows from (10) that the conditional Slutsky matrix  $[\pi_{ij}^g]$  is symmetric,

$$(13) \quad \pi_{ij}^g = \pi_{ji}^g \quad i, j = 1, \dots, n_g.$$

We shall refer to this as Slutsky symmetry. The negative definiteness of  $[v_{ij}]$ , together with (10) and (12) imply that  $[\pi_{ij}^g]$  is negative semidefinite with rank  $n_g - 1$ .



### A Parametrization of the Conditional Demand Equations

To apply (11) to finite-change data, we replace (i)  $w_i$  with its arithmetic average over the periods  $t-1$  and  $t$ ,  $\bar{w}_{it} = (w_{it} + w_{i,t-1})/2$  and (ii)  $d(\log x)$  with  $Dx_t = \log x_t - \log x_{t-1}$ , the log-change in  $x$ . We also use the Rotterdam parametrization of treating the coefficients of (11) as constants (Theil, 1975/76), so that the estimating equations are

$$(14) \quad \bar{w}_{it} Dq_{it} = \theta_i \bar{w}_{gt} DQ_{gt} + \sum_{j=1}^{n_g} \pi_{ij}^g Dp_{jt} + \epsilon_{it}, \quad i=1, \dots, n_g$$

where  $\bar{w}_{gt} = \sum_{i=1}^{n_g} \bar{w}_{it}$ ;  $DQ_{gt} = \sum_{i=1}^{n_g} (\bar{w}_{it}/\bar{w}_{gt}) Dq_{it}$ ; and the  $\epsilon_{it}$ 's are serially independent, normally distributed disturbances with zero means and a constant contemporaneous covariance matrix.

### 3. DEMAND EQUATIONS FOR ALCOHOLIC BEVERAGES

In this section we first present price-quantity data for the consumption of beer, wine and spirits. We then use these data to estimate (14) under two conditions, (i) that total consumption of alcohol is a predetermined variable and (ii) that it is endogenously determined. Finally, we give the unconditional demand responses.

#### The Data

Our data refer to the consumption of beer, wine and spirits in Australia over the period 1955/56-1976/77. Table 1 gives the price-quantity data and Table 2 the budget shares. As can be seen, on average beer consumption per capita increased by about 1.2 percent per annum, wine by 4.5 percent and spirits by 2.2 percent. The budget share for total alcohol has remained more or less constant over this period at about 6 percent (Table 2).

TABLE 1

## ALCOHOL QUANTITY AND PRICE LOG-CHANGES:

AUSTRALIA, 1955/56-1976/77

Year	Beer		Wine		Spirits	
	Quantity	Price	Quantity	Price	Quantity	Price
	Dq <sub>1</sub>	Dp <sub>1</sub>	Dq <sub>2</sub>	Dp <sub>2</sub>	Dq <sub>3</sub>	Dp <sub>3</sub>
1956/57	-5.359	14.205	-2.447	5.982	-10.427	0
1957/58	.209	1.230	-.730	4.879	1.220	0
1958/59	.476	.366	.684	6.108	4.853	0
1959/60	1.735	.849	.901	7.514	8.429	0
1960/61	-.292	1.795	-2.960	7.363	-.390	8.406
1961/62	-.410	.709	.479	1.361	.289	1.315
1962/63	1.235	.587	3.039	1.584	-2.588	5.656
1963/64	3.355	1.971	4.608	1.082	7.639	.894
1964/65	3.083	1.368	.708	5.809	7.271	1.982
1965/66	.045	8.152	8.737	7.395	-11.977	13.734
1966/67	2.452	4.291	11.501	4.709	-.712	-5.069
1967/68	3.304	4.114	10.430	6.953	11.586	0
1968/69	3.032	3.025	8.657	12.275	-1.068	6.766
1969/70	2.612	3.477	8.094	6.004	10.476	2.856
1970/71	1.699	6.274	-3.016	9.198	.939	3.041
1971/72	-.135	5.104	1.904	5.850	5.653	.264
1972/73	3.010	5.238	10.084	-.873	12.249	.875
1973/74	7.028	7.623	11.430	2.924	.643	20.202
1974/75	1.060	13.327	11.200	14.993	-4.268	25.660
1975/76	-2.130	22.672	6.158	18.523	-3.534	12.946
1976/77	-.965	8.943	4.463	7.748	9.773	.386
Mean	1.193	5.491	4.473	6.542	2.193	4.758

The quantities are expressed in per capita terms. The year 1956/57, for example, refers to the transition from 1955/56 to 1956/57. All entries are to be divided by 100.

TABLE 2

## ARITHMETIC AVERAGES OF UNCONDITIONAL AND CONDITIONAL BUDGET SHARES

FOR ALCOHOL: AUSTRALIA, 1955/56-1976/77

Year	Unconditional				Conditional		
	Beer $\bar{w}_1$	Wine $\bar{w}_2$	Spirits $\bar{w}_3$	Total alcohol $\bar{w}_g$	Beer $\bar{w}_1/\bar{w}_g$	Wine $\bar{w}_2/\bar{w}_g$	Spirits $\bar{w}_3/\bar{w}_g$
1956/57	4.6325	0.5256	0.9587	6.1168	75.734	8.593	15.673
1957/58	4.7115	0.5274	0.8823	6.1211	76.970	8.616	14.414
1958/59	4.6336	0.5415	0.8847	6.0597	76.465	8.936	14.599
1959/60	4.4809	0.5552	0.8991	5.9351	75.497	9.354	15.149
1960/61	4.3314	0.5609	0.9247	5.8170	74.462	9.643	15.896
1961/62	4.2709	0.5661	0.9477	5.7846	73.831	9.785	16.383
1962/63	4.1877	0.5673	0.9408	5.6957	73.524	9.959	16.517
1963/64	4.1115	0.5656	0.9446	5.6217	73.137	10.061	16.802
1964/65	4.0759	0.5676	0.9747	5.6181	72.549	10.102	17.349
1965/66	4.1326	0.6059	0.9802	5.7185	72.266	10.594	17.140
1966/67	4.2397	0.6778	0.9164	5.8339	72.674	11.618	15.707
1967/68	4.2709	0.7525	0.8839	5.9073	72.299	12.738	14.963
1968/69	4.2805	0.8550	0.9028	6.0383	70.889	14.160	14.951
1969/70	4.2479	0.9492	0.9278	6.1248	69.355	15.497	15.148
1970/71	4.2308	0.9749	0.9387	6.1444	68.857	15.866	15.277
1971/72	4.1829	0.9686	0.9139	6.0654	68.964	15.969	15.067
1972/73	4.0888	0.9646	0.9200	5.9734	68.451	16.148	15.401
1973/74	4.0500	0.9588	0.9632	5.9720	67.817	16.054	16.129
1974/75	3.9724	0.9969	1.0088	5.9781	66.449	16.676	16.875
1975/76	3.9885	1.0839	0.9927	6.0651	65.761	17.872	16.367
1976/77	3.9918	1.1303	0.9496	6.0716	65.745	18.616	15.639
Mean	4.2434	0.7569	0.9359	5.9363	71.509	12.708	15.783

The year 1956/57, for example, refers to the arithmetic averages of the budget shares in 1955/56 and 1956/57. All entries are to be divided by 100.

Expenditure on beer, expressed as a percentage of total alcohol expenditure, has fallen by about 10 percentage points to 66 percent in 1976/77 (see the third last column of Table 2). This relative decline in beer expenditure mirrors the dramatic growth of the share of wine in total alcohol, which increased from 8.6 percent in 1956/57 to 18.6 in 1976/77. One of our objectives is to explain this rapid growth in the wine share. The spirits share in total alcohol has been relatively stable at about 16 percent. Further details of the data and sources are given in a separate Appendix, available on request.

#### Estimates with Total Alcohol Consumption Predetermined

We assume that the total consumption of alcohol  $\bar{w}_{gt}$  and the prices  $D_{jt}$  are predetermined variables and use maximum likelihood to estimate (14) for  $i=1,2,3$  subject to the homogeneity and symmetry restrictions (12) and (13). The estimates are given in Table 3.<sup>1</sup> Constant terms have been added to each equation to take account of trend-like changes in tastes, etc. A preliminary analysis indicated that two constants are needed in each equation, one for the first nine observations ( $\alpha_i$ ) and one for the remaining twelve ( $\beta_i$ ). As can be seen, there is a significant trend into wine and out of spirits in the second part of the period. The estimate of  $\beta_i$  for wine implies that per capita consumption is growing autonomously at an exponential rate of  $.53/(\bar{w}_{it} \times 1000) = .53 \times 100/1.13 \times 1000 = 4.7$  percent per annum in 1976/77. The conditional marginal shares are estimated quite precisely and they indicate that when alcohol expenditure increases by one dollar, expenditure on beer rises by 54 cents, wine by 10 cents, with the remaining 37 cents being spent on spirits. All the diagonal elements of the conditional Slutsky matrix are negative as they should be, and significant.<sup>2</sup> The off-diagonal  $\pi_{ij}^g$ 's are positive, indicating that the three beverages are pairwise substitutes, and only one is insignificantly different from zero. The fit of the equations is satisfactory given that they are in first-difference form.

TABLE 3

## CONDITIONAL DEMAND EQUATIONS FOR ALCOHOLIC BEVERAGES:

AUSTRALIA, 1955/56-1976/77

$$\bar{w}_{it} D_{q_{it}} = \alpha_i D_t + \beta_i (1 - D_t) + \theta_i' \bar{w}_{gt} D_{q_{gt}} + \sum_{j=1}^3 \pi_{ij}^g D_{p_{jt}} + \varepsilon_{it}$$

(Asymptotic standard errors in parentheses)

Beverage	Constants		Conditional marginal share $\theta_i'$	Conditional Slutsky coefficients			$R^2$	DW
	$\alpha_i$ × 1000	$\beta_i$ × 1000		$\pi_{i1}^g$ × 100	$\pi_{i2}^g$ × 100	$\pi_{i3}^g$ × 100		
Beer	-.039 (.103)	-.107 (.115)	.539 (.046)	-.464 (.153)	.135 (.117)	.329 (.101)	.92	2.20
Wine	.066 (.078)	.525 (.084)	.095 (.033)		-.300 (.122)	.165 (.074)	.74	1.49
Spirits	-.027 (.100)	-.419 (.112)	.366 (.044)			-.494 (.105)	.78	1.66

The variable  $D_t = 1$  for 1956/57-1964/65, 0 otherwise.  $R^2$  is the squared correlation coefficient between the actual and predicted values of the dependent variable and thus lies in the range  $[0,1]$ .

The compatibility of the homogeneity and symmetry restrictions with the data can be verified by means of a likelihood ratio test. The unrestricted version of the model is (14), including constant terms, without the constraints (12) and (13). Asymptotically, minus twice the difference between the log-likelihood values for the restricted and unrestricted models is distributed as  $\chi^2(3)$ .<sup>3</sup> The observed value of the test statistic is 4.05, less than the critical value at the 5 percent level of 7.81. Thus we are unable to reject homogeneity and symmetry.

Table 4 gives the conditional demand elasticities evaluated at the beginning and end of the sample period, as well as at sample means. At sample means, the conditional income elasticities are .8, .8 and 2.3, for beer, wine and spirits, respectively. This indicates that, within alcohol, beer and wine are necessities and spirits is a strong luxury. Note, however,

TABLE 4

CONDITIONAL DEMAND ELASTICITIES FOR ALCOHOLIC BEVERAGES:

AUSTRALIA, 1955/56-1976/77

Beverage	Conditional income elasticity $\theta_{i\bar{w}_{gt}/\bar{w}_{it}}$	Conditional price elasticities		
		$\pi_{i1}^g/\bar{w}_{it}$	$\pi_{i2}^g/\bar{w}_{it}$	$\pi_{i3}^g/\bar{w}_{it}$
<u>1956/57</u>				
Beer	.71	-.10	.03	.07
Wine	1.11	.26	-.57	.31
Spirits	2.34	.34	.17	-.52
<u>1976/77</u>				
Beer	.82	-.12	.03	.08
Wine	.51	.12	-.27	.15
Spirits	2.34	.35	.17	-.52
<u>Sample means</u>				
Beer	.75	-.11	.03	.08
Wine	.75	.18	-.40	.22
Spirits	2.32	.35	.18	-.53

Based on Table 3 estimates and Table 2 data

that at the beginning of the period wine has a conditional income elasticity greater than one. All the conditional price elasticities are less than one in absolute value, with the own-price elasticities being -.1, -.4 and -.5 (at sample means). As expected, there is only a moderate amount of substitutability between the three beverages.

#### Estimates with Total Alcohol Consumption Endogenous

We now let total alcohol consumption  $\bar{w}_{gt} DQ_{gt}$  become endogenously determined by adding the composite demand equation to the three conditional

equations. The composite equation in terms of infinitesimal changes is (7). As before, we replace budget shares with their arithmetic averages and infinitesimal logarithmic changes by finite log-changes; and treat the coefficients as constants. Numbering goods such that the alcoholic beverages are the first three, the estimating equation is thus

$$(15) \quad \bar{w}_{gt} DQ_{gt} = \theta_g DQ_t + \phi \theta_g \left( \sum_{i=1}^3 \theta'_i Dp_{it} - \sum_{j=1}^n \theta_j Dp_{jt} \right) + E_{gt},$$

where  $DQ_t = \sum_{i=1}^n \bar{w}_{it} Dq_{it}$  and  $E_{gt}$  is a serially independent, normally distributed disturbance with a zero mean and a constant variance.

Equations (14) and (15) form a system of four simultaneous equations with endogenous variables  $\bar{w}_{it} Dq_{it}$  ( $i=1,2,3$ ) and  $\bar{w}_{gt} DQ_{gt}$ . The variables taken to be predetermined are the prices and  $DQ_t$ . Note that (15) implies that the only random component of  $\bar{w}_{gt} DQ_{gt}$  is the disturbance  $E_{gt}$ . Hence, we can treat  $\bar{w}_{gt} DQ_{gt}$  as predetermined in (14) if  $E_g$  is independent of the disturbance in (14)  $\epsilon_{it}$ . Remarkably, Theil's (1975/76, 1980) theory of rational random behavior implies that these disturbances are independent. Thus, our previous estimates of (14) by itself are consistent under the theory of rational random behavior.

In this sub-section we do not rely on this theory and estimate (14) and (15) simultaneously, allowing the disturbances  $E_{gt}$  and  $\epsilon_{it}$  to be correlated. A comparison of the two sets of estimates can be interpreted as an informal test of the theory. In addition, the estimation of (15) allows us to obtain the unconditional demand responses.

The overall Frisch price index in (15) can be written as

$$(16) \quad \sum_{j=1}^n \theta_j Dp_{jt} = \theta_g \sum_{j=1}^3 \theta'_j Dp_{jt} + (1 - \theta_g) \sum_{k=4}^n \frac{\theta_k}{\sum_{\ell=4}^n \theta_\ell} Dp_{kt}$$

as  $\theta'_j = \theta_j / \theta_g$  and  $\theta_g = \sum_{i=1}^3 \theta_i = 1 - \sum_{\ell=4}^n \theta_\ell$ . In words, the overall Frisch price index is a weighted average of the Frisch indexes for alcohol and all other, the weights being the group marginal shares. The estimation procedure can be simplified by eliminating the marginal shares not involving

alcohol. We do this by approximating the Frisch index of all other in (16),  $\sum_{k=4}^n (\theta_k / \sum_{\ell=4}^n \theta_\ell) DP_{kt}$ , by the change in the consumer price index excluding alcohol (see Appendix)  $DP_{0t}$ , so that

$$(17) \quad \sum_{j=1}^n \theta_j DP_{jt} \approx \theta_g \sum_{j=1}^3 \theta'_j DP_{jt} + (1 - \theta_g) DP_{0t}.$$

For estimation we substitute in (15) the right side of (17) for  $\sum_{j=1}^n \theta_j DP_{jt}$ . We also approximate the change in real income  $DQ_t$  by the difference between the log-change in per capita total consumption expenditure and that of the consumer price index.

The maximum likelihood estimates are given in Table 5. All the estimates for the conditional demand equations are highly consistent with those of Table 3. This result gives support to the theory of rational random behavior, which allows  $\bar{W}_{gt} DQ_{gt}$  to be treated as predetermined. Looking at the estimates for the composite equation, there is a significant autonomous trend out of alcohol in the first part of the period. The marginal share for the group is highly significant and indicates that a one dollar rise in income leads to a six cent increase in alcohol expenditure. Finally, the value of the income flexibility is quite close to previous estimates.<sup>4</sup> Testing the homogeneity and symmetry restrictions, as before, gives an observed  $\chi^2$  value of 5.66, again less than the critical value of  $\chi^2(3)$  at the 5 percent level.

Table 6 gives the conditional demand elasticities and the income and own-price elasticities for the group. As is to be expected, the conditional elasticities are similar to those of Table 4. The income elasticity of demand for alcoholic beverages as a whole is 1.0, while the own-price elasticity is -.6.



TABLE 5  
 CONDITIONAL AND COMPOSITE DEMAND EQUATIONS  
 FOR ALCOHOLIC BEVERAGES:  
 AUSTRALIA, 1955/56-1976/77

$$\bar{w}_{it} D_{it} = \alpha_i D_t + \beta_i (1 - D_t) + \theta_i' \bar{w}_{gt} D_{gt} + \sum_{j=1}^3 \pi_{ij}^g D_{p_{jt}} + \epsilon_{it}$$

$$\bar{w}_{gt} D_{gt} = \gamma D_t + \lambda (1 - D_t) + \theta_g D_{gt} + \phi \theta_g \left( \sum_{i=1}^3 \theta_i' D_{p_{it}} - \sum_{j=1}^n \theta_j D_{p_{jt}} \right) + E_{gt}$$

(Asymptotic standard errors in parentheses)

Beverage	Constants		Conditional marginal share $\theta_i'$	Conditional Slutsky coefficients			$R^2$	DW
	$\alpha_i$ × 1000	$\beta_i$ × 1000		$\pi_{i1}^g$ × 100	$\pi_{i2}^g$ × 100	$\pi_{i3}^g$ × 100		
Beer	-.065 (.106)	-.196 (.115)	.590 (.045)	-.390 (.145)	.150 (.114)	.240 (.097)	.67	1.72
Wine	.062 (.078)	.517 (.084)	.099 (.035)		-.293 (.124)	.144 (.072)	.68	1.24
Spirits	.003 (.104)	-.321 (.111)	.311 (.042)			-.384 (.102)	.69	2.34
Total alcohol	$\gamma \times 1000$ = -.686 (.332)	$\lambda \times 1000$ = .209 (.342)	$\theta_g = .0576$ $\theta_g$ (.0095)			$\phi = -.595$ (.130)	.76	1.73

$R^2$  refers to the reduced form. See notes to Table 3.

TABLE 6  
 CONDITIONAL AND COMPOSITE DEMAND ELASTICITIES  
 FOR ALCOHOLIC BEVERAGES:  
 AUSTRALIA, 1955/56-1976/77

Beverage	Conditional income elasticity $\theta_{i \bar{w}_{gt}/\bar{w}_{it}}$	Conditional price elasticities			Composite income elasticity $\theta_g/\bar{w}_{gt}$	Composite own-price elasticity $\phi\theta_g/\bar{w}_{gt}$
		$\pi_{i1}^g/\bar{w}_{it}$	$\pi_{i2}^g/\bar{w}_{it}$	$\pi_{i3}^g/\bar{w}_{it}$		
<u>1956/57</u>						
Beer	.78	-.08	.03	.05		
Wine	1.15	.29	-.56	.27		
Spirits	1.98	.25	.15	-.40		
Total alcohol					.94	-.56
<u>1976/77</u>						
Beer	.90	-.10	.04	.06		
Wine	.53	.13	-.26	.13		
Spirits	1.99	.25	.15	-.40		
Total alcohol					.95	-.56
<u>Sample means</u>						
Beer	.83	-.09	.04	.06		
Wine	.78	.20	-.39	.19		
Spirits	1.97	.26	.15	-.41		
Total alcohol					.97	-.58

Based on Table 5 estimates and Table 2 data

### The Unconditional Demand Responses

The conditional demand equation (14) depends on total alcohol consumption and the prices of the three beverages. Accordingly, the conditional Slutsky coefficient  $\pi_{ij}^g$  measures the effect of a change in the price of alcoholic beverage  $j$  on the consumption of beverage  $i$  with total alcohol consumption held constant. From equation (15), this total also depends on the price of  $j$ . Thus a change in  $p_j$  has a direct effect on  $i$ , via the conditional demand equation, and an indirect effect via the composite demand equation. These two effects can be combined to give the total effect by substituting the right side of (15) for  $\bar{w}_{gt} DQ_{gt}$  in (14). This yields

$$(18) \quad \bar{w}_{it} Dq_{it} = \theta_i DQ_t + \sum_{j=1}^3 \pi_{ij} Dp_{jt} + \pi_{i0} DP_{0t} + \eta_{it},$$

where

$$(19) \quad \theta_i = \theta_g \theta'_i$$

is the unconditional marginal share of  $i$ ;

$$(20) \quad \pi_{ij} = \pi_{ij}^g + \phi \theta_g (1 - \theta_g) \theta'_i \theta'_j \quad \pi_{i0} = -\phi \theta_g (1 - \theta_g) \theta'_i$$

are unconditional Slutsky coefficients; and  $\eta_{it} = \epsilon_{it} + \theta'_i E_{gt}$ . In deriving (18) we have used the right side of (17) to substitute for  $\sum_{j=1}^n \theta_j Dp_{jt}$  in (15). From (18) it can be seen that the unconditional income and price elasticities are  $\theta_i / \bar{w}_{it}$ ,  $\pi_{ij} / \bar{w}_{it}$  and  $\pi_{i0} / \bar{w}_{it}$ .

We use the Table 5 estimates to evaluate (19) and (20) for  $i, j=1, 2, 3$ . The results are given in Table 7. Thus the direct and indirect effects of a one dollar rise in income is to increase expenditure on beer by 3.4 cents, wine by .6 cents and spirits by 1.8 cents. All the own-Slutsky coefficients are estimated quite precisely and each is more negative than the corresponding conditional coefficient of Table 5. The reason is that an increase in the price of beverage  $i$  lowers total alcohol consumption which also lowers the consumption of  $i$ , as the estimate of  $\theta'_i$  is positive for each  $i$ . This

TABLE 7

## UNCONDITIONAL DEMAND EQUATIONS FOR ALCOHOLIC BEVERAGES:

AUSTRALIA, 1955/56-1976/77

$$\bar{w}_{it} D_{q_{it}} = \delta_i D_{it} + \psi_i (1 - D_{it}) + \theta_i D_{q_{it}} + \sum_{j=1}^3 \pi_{ij} D_{p_{jt}} + \pi_{i0} D_{p_{0t}} + \eta_{it}$$

(Asymptotic standard errors in parentheses)

Beverage	Constants		Marginal share $\theta_i$	Slutsky coefficients			
	$\delta_i$ × 1000	$\psi_i$ × 1000		$\pi_{i1}$ × 100	$\pi_{i2}$ × 100	$\pi_{i3}$ × 100	$\pi_{i0}$ × 100
Beer	-.469 (.236)	-.073 (.235)	.0340 (.0062)	-1.514 (.299)	-.039 (.125)	-.353 (.146)	1.906 (.377)
Wine	-.006 (.092)	.537 (.089)	.0057 (.0023)		-.325 (.132)	.044 (.080)	.319 (.132)
Spirits	-.210 (.139)	-.256 (.139)	.0179 (.0037)			-.697 (.130)	1.006 (.202)

The estimates from Table 5 are used in equations (19) and (20) to obtain the (unconditional) marginal shares and Slutsky coefficients. The constant term  $\delta_i$  is defined as  $\alpha_i + \theta_i^1 \gamma$ , with estimates taken from Table 5; and similarly for  $\psi_i$ . See notes to Table 3.

negative indirect effect is then added to the conditional Slutsky coefficient  $\pi_{ii}^g$  ( $< 0$ ) to give an unconditional coefficient  $\pi_{ii}$  larger in absolute value than  $\pi_{ii}^g$ . For a similar reason the estimates of  $\pi_{12}$  and  $\pi_{13}$  are negative, indicating that beer is an unconditional complement for wine and spirits, whereas these beverages are conditional substitutes ( $\pi_{12}^g, \pi_{13}^g > 0$ ; see Table 5). Finally, each of the three beverages is a substitute for all other goods.

Table 8 gives the unconditional elasticities. As the income elasticity for the group is about unity (see Table 6), the unconditional income elasticities given in Table 8 are quite close to the corresponding conditional elasticities. For the reason given above, the own-price

elasticities are substantially larger (in absolute value) than those of Table 6. At sample means, the unconditional own-price elasticities are  $-.4$ ,  $-.4$  and  $-.7$  for beer, wine and spirits, respectively.

TABLE 8

## UNCONDITIONAL DEMAND ELASTICITIES FOR ALCOHOLIC BEVERAGES:

AUSTRALIA, 1955/56 - 1976/77

Beverage	Income elasticity $\theta_i/\bar{w}_{it}$	Price elasticities			
		$\pi_{i1}/\bar{w}_{it}$	$\pi_{i2}/\bar{w}_{it}$	$\pi_{i3}/\bar{w}_{it}$	$\pi_{i0}/\bar{w}_{it}$
<u>1956/57</u>					
Beer	.73	-.33	-.01	-.08	.41
Wine	1.08	-.07	-.62	.08	.61
Spirits	1.87	-.37	.05	-.73	1.05
<u>1976/77</u>					
Beer	.85	-.37	-.01	-.09	.48
Wine	.50	-.03	-.29	.04	.28
Spirits	1.89	-.37	.05	-.73	1.06
<u>Sample means</u>					
Beer	.80	-.36	-.01	-.08	.45
Wine	.75	-.05	-.43	.06	.42
Spirits	1.91	-.38	.05	-.74	1.07

Based on Table 7 estimates and Table 2 data.

#### 4. WHY HAS WINE GROWN SO RAPIDLY?

As indicated in the previous section, wine consumption per capita grew by 4.5 percent per annum over our sample period; and the share of wine in total alcohol expenditure increased by 10 percentage points. In this section we analyse the reasons for this rapid growth by using the demand equations to (i) decompose the growth into a number of components and (ii) simulate alcohol consumption under several different scenarios.

##### A Decomposition of the Change in the Budget Share

Recalling that the  $i^{\text{th}}$  budget share is defined as  $w_i = p_i q_i / M$ , its change is  $dw_i = w_i d(\log p_i) + w_i d(\log q_i) - w_i d(\log M)$ . This can be expressed in terms of the relative price of  $i$  and real income by adding and subtracting from the right side the Divisia cost of living index  $d(\log P) = \sum_{i=1}^n w_i d(\log p_i)$ . This gives

$$(21) \quad dw_i = w_i d \left( \log \frac{p_i}{P} \right) + w_i d(\log q_i) - w_i d(\log Q),$$

where  $d \left( \log \frac{p_i}{P} \right) = d(\log p_i) - d(\log P)$  is the change in the relative price of  $i$  and  $d(\log Q) = d(\log M) - d(\log P) = \sum_{i=1}^n w_i d(\log q_i)$  is the change in real income.

Equation (21) states that  $dw_i$  is made up of relative price, quantity and real income components. From the consumer's viewpoint prices and income are given, while the quantity demanded is to be determined. Thus we use the demand equation (1) to express the quantity component in terms of income and relative prices,

$$(22) \quad dw_i = (\theta_i - w_i) d(\log Q) + \sum_{j=1}^n v_{ij} d \left( \log \frac{p_j}{p_i} \right) + w_i d \left( \log \frac{p_i}{P} \right).$$

Thus a rise in income causes the budget share of  $i$  to increase if the marginal share ( $\theta_i$ ) exceeds the average share ( $w_i$ ); i.e. if this good is a

luxury. The second component on the right of (22) is the price substitution term, which gives the effect of changes in relative prices on  $w_i$  via  $q_i$ . The final term is the direct effect of the relative price of  $i$  on the budget share.<sup>5</sup>

To apply (22) to the finite-change data for alcoholic beverages, we use the right side of equation (18) to substitute for the quantity component in (21). This gives

$$(23) \quad \Delta w_{it} = (\theta_i - \bar{w}_{it}) DQ_t + \sum_{j=1}^3 \pi_{ij} Dp_{jt} + \pi_{i0} DP_{0t} + \bar{w}_{it} (Dp_{it} - DP_t) + \eta_{it} + O_3,$$

where  $\Delta w_{it} = w_{it} - w_{i,t-1}$  and  $O_3$  is a remainder term of third degree

(Theil, 1975/76, pp. 37-40, 215). Note that (12) and (20) imply

$\sum_{j=1}^3 \pi_{ij} + \pi_{i0} = 0$ , which is a reflection of demand homogeneity. We use this to deflate the absolute prices in (23)  $Dp_{jt}$  and  $DP_{0t}$  by  $DP_t$  to give

$$(24) \quad \Delta w_{it} = (\theta_i - \bar{w}_{it}) DQ_t + \sum_{j=1}^3 \pi_{ij} (Dp_{jt} - DP_t) + \pi_{i0} (DP_{0t} - DP_t) + \bar{w}_{it} (Dp_{it} - DP_t) + \eta_{it} + O_3.$$

To evaluate (24) we use the estimates given in Table 7 and the log-change in the consumer price index for  $DP_t$ . The constant term in the demand equation  $\delta_i D_t + \psi_i (1 - D_t)$  means that this is an additional component of  $\Delta w_i$ . The results are given in Tables 9-11. Looking at Table 9, on average the budget share of beer fell by 2.94/100 percentage points per annum. The shift in preferences away from beer accounts for 2.43 of this. The growth in real income, together with the fact that beer is a necessity, accounts for 1.91 of the fall. The rise in the relative price of beer accounts for .75, while the other relative prices have a negligible effect. Finally, offsetting the fall in the beer share is the direct relative price component of 2.19. The conclusion which emerges is that the shift in preferences away from beer and the growth in real income are the two most important reasons for the decline in the budget share of beer.

TABLE 9

DECOMPOSITION OF CHANGE IN BUDGET SHARE OF BEER: AUSTRALIA, 1955/56 - 1976/77

Year	Change in budget share of beer  $\Delta w_1$  (1)	Components of $\Delta w_1$								Demand Equation Residual $\eta_1$  (10)
		Constant  $\delta_1 D + \psi_1 (1 - D)$  (2)	Income  $(\theta_1 - \bar{w}_1) DQ$  (3)	Price substitution					Direct Relative Price  $\bar{w}_1 (Dp_1 - DP)$  (9)	
				Beer  $\pi_{11} (Dp_1 - DP)$  (4)	Wine  $\pi_{12} (Dp_2 - DP)$  (5)	Spirits  $\pi_{13} (Dp_3 - DP)$  (6)	Total alcohol  $\sum_{j=1}^3 \pi_{1j} (Dp_j - DP)$  (7)	All other  $\pi_{10} (Dp_0 - DP)$  (8)		
1956/57	21.31	-4.69	1.77	-12.91	-.01	2.01	-10.91	-.69	39.50	-3.63
1957/58	-5.52	-4.69	-2.15	-.38	-.15	.34	-.19	-.05	1.19	.34
1958/59	-10.06	-4.69	-1.76	1.82	-.18	.55	2.19	.09	-5.57	-.23
1959/60	-20.50	-4.69	-5.07	2.47	-.20	.88	3.15	.14	-7.31	-6.78
1960/61	-9.39	-4.69	.31	3.34	-.13	-1.55	1.66	.07	-9.56	2.82
1961/62	-2.72	-4.69	-.43	-.40	-.04	-.31	-.74	-.05	1.12	2.05
1962/63	-13.91	-4.69	-3.88	-.55	-.05	-1.92	-2.52	-.15	1.53	-4.20
1963/64	-1.33	-4.69	-3.39	-1.64	-.01	-.00	-1.65	-.09	4.46	4.04
1964/65	-5.81	-4.69	-1.48	3.51	-.08	.60	4.02	.20	-9.44	5.58
1965/66	17.15	-.73	-.35	-6.96	-.15	-3.59	-10.71	-.63	19.01	10.62
1966/67	4.28	-.73	-2.60	-2.51	-.08	2.72	.13	-.03	7.02	.50
1967/68	1.97	-.73	-3.24	-1.31	-.14	1.15	-.31	-.07	3.70	2.56
1968/69	-.06	-.73	-3.06	-.67	-.36	-1.48	-2.53	-.28	1.90	4.70
1969/70	-6.47	-.73	-3.78	-.48	-.11	.11	-.49	-.08	1.36	-2.78
1970/71	3.06	-.73	-2.16	-2.47	-.18	.57	-2.08	-.20	6.90	1.34
1971/72	-12.64	-.73	-1.10	2.24	.03	2.23	4.50	.26	-6.19	-9.38
1972/73	-6.16	-.73	-2.68	.96	.26	1.76	2.98	.28	-2.59	-3.46
1973/74	-1.59	-.73	-1.86	6.89	.36	-2.83	4.41	.40	-18.42	14.65
1974/75	-13.95	-.73	-1.40	3.22	.02	-3.60	-.36	-.03	-8.45	-2.99
1975/76	17.17	-.73	-2.37	-15.86	-.25	-.26	-16.37	-1.00	41.77	-4.12
1976/77	-16.53	-.73	.48	6.05	.20	4.43	10.68	.68	-15.95	-11.70
Mean	-2.94	-2.43	-1.91	-.75	-.06	.09	-.72	-.06	2.19	-.00

Column (1) = (2) + (3) + (4) + (5) + (6) + (8) + (9) + (10) + a remainder term of third degree. The year 1956-57, for example, refers to the transition from 1955-56 to 1956-57. All entries are to be divided by 10000.



TABLE 10

## DECOMPOSITION OF CHANGE IN BUDGET SHARE OF WINE: AUSTRALIA, 1955/56 - 1976/77

Year	Change in budget share of wine	Components of $\Delta w_2$								Direct Relative Price	Demand Equation Residual
		Constant	Income	Price substitution							
				Beer	Wine	Spirits	Total alcohol	All other			
$\Delta w_2$	$\delta_2 D + \psi_2 (1-D)$	$(\theta_2 - \bar{w}_2) DQ$	$\pi_{21} (Dp_1 - DP)$	$\pi_{22} (Dp_2 - DP)$	$\pi_{23} (Dp_3 - DP)$	$\sum_{j=1}^3 \pi_{2j} (Dp_j - DP)$	$\pi_{20} (DP_0 - DP)$	$\bar{w}_2 (Dp_2 - DP)$	$\eta_2$		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)		
1956/57	-.40	-.06	-.06	-.33	-.10	-.25	-.68	-.12	.16	.40	
1957/58	.76	-.06	.07	-.01	-1.27	-.04	-1.32	-.01	2.06	.07	
1958/59	2.06	-.06	.04	.05	-1.48	-.07	-1.50	.02	2.46	1.10	
1959/60	.67	-.06	.07	.06	-1.64	-.11	-1.68	.02	2.79	-.45	
1960/61	.48	-.06	-.00	.09	-1.09	.19	-.81	.01	1.88	-.61	
1961/62	.55	-.06	.00	-.01	-.30	.04	-.27	-.01	.52	.33	
1962/63	-.30	-.06	.01	-.01	-.44	.24	-.22	-.03	.77	-.78	
1963/64	-.02	-.06	.02	-.04	-.06	.00	-.11	-.02	.11	.07	
1964/65	.41	-.06	.01	.09	-.69	-.07	-.68	.03	1.21	-.14	
1965/66	7.26	5.37	-.02	-.18	-1.25	.45	-.98	-.11	2.33	.74	
1966/67	7.14	5.37	-.33	-.06	-.67	-.34	-1.08	-.00	1.41	1.75	
1967/68	7.80	5.37	-.68	-.03	-1.20	-.14	-1.38	-.01	2.79	1.75	
1968/69	12.71	5.37	-.99	-.02	-3.15	.18	-2.98	-.05	8.29	3.08	
1969/70	6.13	5.37	-1.69	-.01	-.93	-.01	-.95	-.01	2.70	.74	
1970/71	-.99	5.37	-1.05	-.06	-1.48	-.07	-1.61	-.03	4.44	-8.14	
1971/72	-.26	5.37	-.56	.06	.24	-.28	.02	.04	-.71	-4.38	
1972/73	-.54	5.37	-1.54	.02	2.19	-.22	2.00	.05	-6.50	.10	
1973/74	-.63	5.37	-1.11	.18	3.01	.35	3.54	.07	-8.87	.37	
1974/75	8.25	5.37	-1.04	.08	.15	.45	.68	-.00	-.46	3.74	
1975/76	9.15	5.37	-2.07	-.41	-2.06	.03	-2.43	-.17	6.85	1.62	
1976/77	.11	5.37	.46	.16	1.69	-.55	1.29	.11	-5.87	-1.25	
Mean	2.87	3.04	-.50	-.02	-.50	-.01	-.53	-.01	.87	.00	

Column (1) = (2) + (3) + (4) + (5) + (6) + (8) + (9) + (10) + a remainder term of third degree. The year 1956-57, for example, refers to the transition from 1955-56 to 1956-57. All entries are to be divided by 10000.

TABLE 11

## DECOMPOSITION OF CHANGE IN BUDGET SHARE OF SPIRITS: AUSTRALIA, 1955/56 - 1976/77

Year	Change in budget share of spirits $\Delta w_3$	Components of $\Delta w_3$								Demand Equation Residual $\eta_3$
		Constant $\delta_3 D + \psi_3 (1-D)$	Income $(\theta_3 - \bar{w}_3) DQ$	Price substitution					Direct Relative Price $\bar{w}_3 (Dp_3 - DP)$	
				Beer $\pi_{31} (Dp_1 - DP)$	Wine $\pi_{32} (Dp_2 - DP)$	Spirits $\pi_{33} (Dp_3 - DP)$	Total alcohol $\sum_{j=1}^3 \pi_{3j} (Dp_j - DP)$	All other $\pi_{30} (Dp_0 - DP)$		
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	
1956/57	-13.98	-2.10	-1.20	-3.01	.01	3.96	.96	-.37	-5.45	-5.92
1957/58	-1.30	-2.10	1.49	-.09	.17	.68	.76	-.03	-.86	-.49
1958/59	1.77	-2.10	1.29	.42	.20	1.09	1.72	.05	-1.39	2.08
1959/60	1.12	-2.10	4.18	.58	.22	1.73	2.53	.07	-2.23	-1.32
1960/61	4.00	-2.10	-.29	.78	.15	-3.07	-2.14	.04	4.07	4.44
1961/62	.62	-2.10	.41	-.09	.04	-.60	-.66	-.03	.82	2.18
1962/63	-2.02	-2.10	4.18	-.13	.06	-3.79	-3.86	-.08	5.11	-5.21
1963/64	2.79	-2.10	4.03	-.38	.01	-.00	-.38	-.05	.01	1.22
1964/65	3.25	-2.10	1.79	.82	.09	1.19	2.10	.11	-1.66	3.06
1965/66	-2.18	-2.56	.39	-1.62	.17	-7.10	-8.55	-.33	9.98	-1.16
1966/67	-10.59	-2.56	2.70	-.58	.09	5.37	4.88	-.01	-7.06	-8.49
1967/68	4.10	-2.56	3.37	-.31	.16	2.26	2.12	-.04	-2.87	4.05
1968/69	-.32	-2.56	3.08	-.16	.43	-2.92	-2.65	-.15	3.78	-1.83
1969/70	5.32	-2.56	3.85	-.11	.13	.21	.22	-.04	-.28	4.11
1970/71	-3.12	-2.56	2.22	-.58	.20	1.12	.74	-.11	-1.50	-1.86
1971/72	-1.85	-2.56	1.23	.52	-.03	4.41	4.90	.14	-5.78	.18
1972/73	3.07	-2.56	3.39	.22	-.30	3.48	3.41	.15	-4.60	3.31
1973/74	5.58	-2.56	2.37	1.61	-.41	-5.60	-4.40	.21	7.73	2.24
1974/75	3.54	-2.56	1.91	.75	-.02	-7.11	-6.38	-.01	10.30	.27
1975/76	-6.76	-2.56	3.22	-3.70	.28	-.52	-3.94	-.53	.74	-3.70
1976/77	-1.87	-2.56	-.69	1.41	-.23	8.75	9.93	.36	-11.92	3.01
Mean	-.42	-2.36	2.04	-.17	.07	.17	.06	-.03	-.15	.01

Column (1) = (2) + (3) + (4) + (5) + (6) + (8) + (9) + (10) + a remainder term of third degree. The year 1956-57, for example, refers to the transition from 1955-56 to 1956-57. All entries are to be divided by 10000.

As can be seen from Table 10, the most important component of growth in the wine share on average is the shift in preferences toward wine. This is then followed by the direct relative price component, caused by the price of wine rising more rapidly than the CPI. Offsetting these two terms are the effects due to growth in real income and own-price substitution. For spirits (Table 11) on average the growth in income has the effect of almost offsetting the negative shift in preferences; and the other components are quite small.

#### Simulation of Alcohol Consumption

In this sub-section we attempt to isolate the key factors responsible for the rapid growth of wine consumption by using the demand model for counterfactual simulations. We simulate alcohol consumption with (i) alcohol tax rates held constant; (ii) a wine tax rate equal to the beer tax rate; and (iii) no constant terms in the demand equations. These simulations answer the question to what extent the growth in wine is due to (i) changes in all alcohol taxes; (ii) the fact that beer is subject to a substantial tax, while wine is not; and (iii) trend-like changes in tastes toward wine.

Table 12 gives the data on alcohol taxes, in terms of both revenue and tax rates.<sup>6</sup> As can be seen, although beer represents the most important source of revenue, its tax rate has almost halved over this period (from 117 to 63 percent). Aside from the early 1970s, the tax on wine is negligible, while the tax rate for spirits has increased.

We simulate consumption with the tax rates held constant at their 1955/56 values of 117 percent, 0 and 38 percent for beer, wine and spirits, respectively. With  $p_i$  the post-tax price of  $i$ ,  $p_i^0$  the pre-tax price and  $t_i$  the tax rate, we have  $p_{it} = (1 + t_{it})p_{it}^0$ , so that  $Dp_{it} = D(1 + t_{it}) + Dp_{it}^0$ , where  $D$  is the log-change operator (as before). Accordingly, we can simulate the constant tax rates by replacing in the

TABLE 12

## ALCOHOL TAXES: AUSTRALIA, 1955/56-1976/77

Year	Tax revenues (Dollars per capita)				Tax rates × 100 (Percentages of pre-tax prices)		
	Beer	Wine	Spirits	Total Alcohol	Beer	Wine	Spirits
	$\frac{t_1}{1+t_1} p_1 q_1$	$\frac{t_2}{1+t_2} p_2 q_2$	$\frac{t_3}{1+t_3} p_3 q_3$	$\sum_{i=1}^3 \frac{t_i}{1+t_i} p_i q_i$	$t_1$	$t_2$	$t_3$
1955/56	18.33	0	2.14	20.47	117.198	0	38.351
1956/57	21.72	0	2.27	23.99	141.132	0	48.401
1957/58	21.77	0	2.27	24.04	137.090	0	47.588
1958/59	21.17	0	2.39	23.56	126.086	0	47.704
1959/60	21.59	.01	2.63	24.23	124.296	.201	48.524
1960/61	21.51	.01	2.64	24.16	119.236	.192	43.421
1961/62	21.41	.01	2.67	24.09	117.250	.189	43.133
1962/63	21.72	.01	2.59	24.32	116.272	.180	39.602
1963/64	22.45	.01	2.78	25.24	111.358	.170	38.773
1964/65	23.17	.02	3.00	26.19	108.372	.320	37.927
1965/66	26.34	.02	3.31	29.67	119.674	.273	42.436
1966/67	27.43	.02	3.67	31.12	112.929	.232	53.891
1967/68	28.45	.03	4.09	32.57	104.365	.292	53.254
1968/69	29.26	.04	3.96	33.26	97.793	.316	46.589
1969/70	29.88	.05	4.41	34.34	90.491	.343	44.862
1970/71	30.08	.75	4.38	35.21	79.073	5.064	41.995
1971/72	30.53	.96	4.63	36.12	74.356	6.057	41.749
1972/73	31.65	.32	5.23	37.20	68.654	1.767	41.213
1973/74	34.31	.09	7.70	42.10	61.598	.425	53.584
1974/75	34.81	.11	10.73	45.65	50.353	.400	64.601
1975/76	50.17	.15	11.83	62.15	64.761	.426	64.965
1976/77	53.23	.18	13.40	66.81	62.615	.452	67.507
Mean	28.23	.13	4.67	33.02	100.225	.786	47.730

demand equations the observed price log-change  $Dp_{it}$  with  $Dp_{it} - D(1 + t_{it})$ , which is the price-change purged of its tax-change component. Using equation (18), the simulated quantity log-change is

$$Dq_{it}^S = (\theta_i/\bar{w}_{it})DQ_t + \sum_{j=1}^3 (\pi_{ij}/\bar{w}_{it}) [Dp_{jt} - D(1 + t_{jt})] + (\pi_{i0}/\bar{w}_{it})DP_{0t} + \eta_{it}/\bar{w}_{it}.$$

Subtracting from this the observed quantity log-change  $Dq_{it}$  and using (18) gives

$$(25) \quad Dq_{it}^S - Dq_{it} = - \sum_{j=1}^3 (\pi_{ij}/\bar{w}_{it}) D(1 + t_{jt}).$$

Converting from changes to levels, the simulated quantity is

$$q_{it}^S = \exp(Dq_{it} + \log q_{i,t-1}^S).$$

Finally, to evaluate (25) we use the estimates given in Table 7.

The results of this simulation are given in the first three columns of Table 13 (for changes) and in columns 4-6 of Table 14 (levels). As the observed tax rate for beer fell over this period and that for spirits rose, the constant tax rate policy causes beer consumption to be lower than otherwise and spirits to be higher. By 1976/77, simulated per capita consumption is 125 litres, 13.4 litres and 3.23 litres for beer, wine and spirits (see Table 14). Accordingly, this tax package causes beer consumption to be  $(124.57 - 136.14)/136.14 = 8.5$  percent lower than otherwise, wine to be  $(13.3616 - 13.6533)/13.6533 = 2.1$  percent lower and spirits to be  $(3.2300 - 3.1663)/3.1663 = 2.0$  percent higher. The reasons for the lower consumption of wine are (i) that it is an unconditional complement for beer (see Table 7) and in the simulation we increase the price of beer; and (ii) wine and spirits are unconditional substitutes and the price of spirits increases less rapidly in the simulation.

The conclusion from this simulation is that although changes in all alcohol taxes have contributed to the rapid growth of wine, this contribution is a small component of the overall growth.

TABLE 13

## SIMULATION OF CONSUMPTION OF ALCOHOLIC BEVERAGES: AUSTRALIA, 1955/56 - 1976/77

(Simulated quantity log-changes minus actual)

Year	Alcohol tax rates held constant			Wine tax rate equal to the beer tax rate			No constant terms in demand equations		
	Beer	Wine	Spirits	Beer	Wine	Spirits	Beer	Wine	Spirits
1956/57	3.95	.19	8.95	-.74	-54.43	4.04	1.01	.11	2.19
1957/58	-.58	-.08	-1.11	.01	1.04	-.08	1.00	.11	2.38
1958/59	-1.55	-.35	-1.83	.04	2.85	-.24	1.01	.11	2.37
1959/60	-.22	.02	.11	.01	.58	-.05	1.05	.11	2.34
1960/61	-1.08	.11	-3.51	.02	1.32	-.11	1.08	.11	2.27
1961/62	-.34	-.05	-.49	.01	.52	-.04	1.10	.11	2.22
1962/63	-.37	.16	-2.02	.00	.25	-.02	1.12	.11	2.23
1963/64	-.90	-.12	-1.30	.02	1.31	-.11	1.14	.11	2.22
1964/65	-.58	.04	-.96	.02	.90	-.07	1.15	.11	2.15
1965/66	2.21	.08	4.19	-.05	-2.86	.24	.18	-8.86	2.61
1966/67	-.47	-.70	4.68	.03	1.48	-.15	.17	-7.92	2.79
1967/68	-1.49	-.16	-1.97	.04	1.80	-.21	.17	-7.14	2.90
1968/69	-1.52	.09	-4.71	.03	1.25	-.16	.17	-6.28	2.84
1969/70	-1.44	-.09	-2.32	.03	1.30	-.18	.17	-5.66	2.76
1970/71	-2.34	1.38	-4.02	.10	3.59	-.51	.17	-5.51	2.73
1971/72	-.97	.22	-1.21	.03	1.21	-.17	.17	-5.54	2.80
1972/73	-1.30	-1.51	-1.37	-.01	-.27	.04	.18	-5.57	2.78
1973/74	-.88	-1.01	4.57	.03	1.00	-.13	.18	-5.60	2.66
1974/75	-2.13	-.60	2.26	.07	2.34	-.31	.18	-5.39	2.54
1975/76	3.49	.33	3.41	-.09	-2.74	.40	.18	-4.95	2.58
1976/77	-.36	-.10	.63	.01	.38	-.06	.18	-4.75	2.70
Mean	-.42	-.10	.09	-.02	-1.77	.10	.56	-3.44	2.53

The entries are  $Dq_{it}^S - Dq_{it}$ , where  $Dq_{it}^S$  is the simulated log-change in the quantity consumed per capita of  $i$  and  $Dq_{it}$  is the actual log-change. The year 1956/57, for example, refers to the transition from 1955/56 to 1956/57. All entries are to be divided by 100.

TABLE 14

## ACTUAL AND SIMULATED CONSUMPTION OF ALCOHOLIC BEVERAGES: AUSTRALIA, 1955/56 - 1976/77

(Litres per capita)

Year	Actual consumption			Simulated consumption with alcohol tax rates held constant			Simulated consumption with wine tax rate equal to the beer tax rate			Simulated consumption with no constant terms in demand equations		
	Beer	Wine	Spirits	Beer	Wine	Spirits	Beer	Wine	Spirits	Beer	Wine	Spirits
1955/56	105.98	5.3374	1.9977	105.98	5.3374	1.9977	105.98	5.3374	1.9977	105.98	5.3374	1.9977
1956/57	100.45	5.2084	1.7999	104.50	5.2182	1.9684	99.71	3.0223	1.8741	101.47	5.2144	1.8398
1957/58	100.66	5.1705	1.8220	104.11	5.1762	1.9705	99.93	3.0317	1.8955	102.70	5.1823	1.9072
1958/59	101.14	5.2060	1.9126	103.00	5.1936	2.0309	100.45	3.1409	1.9851	104.24	5.2237	2.0501
1959/60	102.91	5.2531	2.0808	104.57	5.2415	2.2119	102.21	3.1878	2.1586	107.18	5.2766	2.2832
1960/61	102.61	5.0999	2.0727	103.14	5.0943	2.1274	101.94	3.1359	2.1479	108.03	5.1282	2.3265
1961/62	102.19	5.1244	2.0787	102.37	5.1162	2.1232	101.53	3.1674	2.1532	108.78	5.1583	2.3855
1962/63	103.46	5.2825	2.0256	103.25	5.2824	2.0276	102.79	3.2734	2.0977	111.37	5.3231	2.3771
1963/64	106.99	5.5316	2.1864	105.82	5.5250	2.1603	106.32	3.4731	2.2619	116.49	5.5800	2.6234
1964/65	110.34	5.5709	2.3513	108.51	5.5662	2.3011	109.67	3.5294	2.4307	121.53	5.6256	2.8827
1965/66	110.39	6.0795	2.0859	110.98	6.0793	2.1288	109.66	3.7431	2.1615	121.80	5.6185	2.6250
1966/67	113.13	6.8205	2.0711	113.20	6.7726	2.2150	112.42	4.2618	2.1430	125.04	5.8231	2.6802
1967/68	116.93	7.5703	2.3255	115.27	7.5049	2.4386	116.24	4.8161	2.4013	129.46	6.0181	3.0979
1968/69	120.53	8.2549	2.3098	117.03	8.1909	2.3016	119.85	5.3178	2.3720	133.67	6.1629	3.1531
1969/70	123.72	8.9508	2.5549	118.41	8.8734	2.4971	123.07	5.8414	2.6292	137.45	6.3148	3.5993
1970/71	125.84	8.6849	2.5790	117.66	8.7291	2.4213	125.30	5.8753	2.6406	140.04	5.7988	3.7337
1971/72	125.67	8.8518	2.7290	116.36	8.9161	2.5313	125.17	6.0612	2.7893	140.10	5.5915	4.0631
1972/73	129.51	9.7910	3.0846	118.36	9.7144	2.8224	128.99	6.6861	3.1540	144.64	5.8499	4.7222
1973/74	138.94	10.9766	3.1045	125.87	10.7814	2.9734	138.42	7.5710	3.1701	155.45	6.2011	4.8807
1974/75	140.42	12.2775	2.9748	124.53	11.9875	2.9145	139.99	8.6691	3.0281	157.39	6.5722	4.7969
1975/76	137.46	13.0573	2.8715	126.24	12.7908	2.9108	136.92	8.9709	2.9348	154.36	6.6518	4.7513
1976/77	136.14	13.6533	3.1663	124.57	13.3616	3.2300	135.62	9.4165	3.2341	153.15	6.6327	5.3823
Mean	116.16	7.6251	2.3716	112.75	7.6722	2.3955	116.01	5.0568	2.4601	127.35	5.7594	3.2458

To simulate the effects of taxing wine at the same rate as beer, we impose a wine tax equal to the beer tax in 1956/57 and then adjust it in all subsequent years to keep it equal to the beer tax. To do this, we write  $t_2^S$  for the simulated value of the tax rate for wine and define it as follows. In 1955/56 it takes the value zero (which is also the observed value of  $t_2$  in that year; see Table 12) and in all subsequent years it is equal to the observed beer tax rate  $t_1$ . Applying the same argument that led to equation (25), simulated minus actual consumption can then be expressed as

$$Dq_{it}^S - Dq_{it} = (\pi_{12}/\bar{w}_{it}) [D(1 + t_{2t}^S) - D(1 + t_{2t})].$$

The results of this simulation are given in columns 4-6 of Table 13 and columns 7-9 of Table 14. On average, the tax causes the annual growth in wine consumption to be about 1.8 percentage points lower than actual. Simulated consumption of wine in 1976/77 is 9.4 litres per capita, which is  $(9.4165 - 13.6533)/13.6533 = 31.0$  percent lower than actual. The effect of the wine tax is to lower beer consumption by a small amount to 135.6 litres in 1976/77 and to increase spirits consumption to 3.23 litres. Hence, the fact that wine escaped a substantial tax does account for a large part of the observed growth in consumption over this period.

In the final simulation we take out the trend-like changes in tastes by setting to zero the constant terms in the demand equations of Table 7. Simulated minus actual consumption can be expressed for this case as

$$Dq_{it}^S - Dq_{it} = -[(\delta_i/\bar{w}_{it})D_t + (\psi_i/\bar{w}_{it})(1 - D_t)],$$

and the results are given in the last three columns of Tables 13 and 14. From Table 13, taking out this trend has the effect on average of beer consumption growing by .6 percentage points per annum more than actual, wine growing by 3.4 percentage points less and spirits 2.5 points more.

To summarize, the simulations indicate that there are two reasons for the rapid growth of wine consumption. First, wine has not attracted a substantial tax, whereas beer has done so. Second, there has been a



significant trend-like shift in preferences toward wine, away from beer and spirits. We also found that the observed changes in all alcohol taxes contributed very little to the growth of wine.

## 5. THE WELFARE COST OF ALCOHOL TAXES

In this section we measure the welfare cost of alcohol taxes by the reduction in consumer surplus not offset by government revenue from the taxes. This welfare cost can be expressed as (Harberger, 1964)

$$(26) \quad W = -\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 T_i S_{ij} T_j,$$

where  $T_i = t_i p_i^0$  is the tax per unit of  $i$  measured in terms of dollars and  $S_{ij} = \partial q_i / \partial p_j$  with real income constant. Dividing (26) by income  $M$ , the cost can be formulated as a fraction of  $M$  as (see Appendix)

$$(27) \quad \frac{W}{M} = -\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1+t_i} \pi_{ij} \frac{t_j}{1+t_j},$$

where  $\pi_{ij}$  is the  $(i,j)^{th}$  unconditional Slutsky coefficient and  $t_i = T_i/p_i^0$  is the tax rate on  $i$ . Using (20), (27) can be decomposed into the cost (i) within the alcoholic beverages group and (ii) between alcoholic beverages and all other goods,

$$(28) \quad \left\{ \begin{array}{ll} -\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1+t_i} \pi_{ij} \frac{t_j}{1+t_j} & \text{(total cost)} \\ \\ -\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1+t_i} \pi_{ij}^g \frac{t_j}{1+t_j} & \text{(cost within alcoholic} \\ & \text{beverages group)} \\ \\ -\frac{1}{2} \phi \theta_g (1 - \theta_g) \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1+t_i} \theta_i' \theta_j' \frac{t_j}{1+t_j} & \text{(cost between alcoholic} \\ & \text{beverages and all} \\ & \text{other goods).} \end{array} \right.$$

We evaluate (28) with the tax data given in Table 12 and the estimates given in Tables 5 and 7. The results are given in Table 15.

TABLE 15

## WELFARE COST OF ACTUAL ALCOHOL TAXES:

AUSTRALIA, 1955/56 - 1976/77

Year	Welfare cost as a fraction of total consumption expenditure $\times 100$			Total welfare cost		
	Within alcoholic beverages group	Between alcoholic beverages and all other goods	Total = within + between	Dollars per capita	As a percentage of alcohol expenditure	As a percentage of revenue from alcohol taxes
	$-\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1+t_i} \pi_{ij}^g \frac{t_j}{1+t_j}$	$-\frac{1}{2} \phi \theta_g (1-\theta_g) \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1+t_i} \theta_i' \theta_j' \frac{t_j}{1+t_j}$	$-\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1+t_i} \pi_{ij} \frac{t_j}{1+t_j}$	$\frac{(3)}{100} \times M$	$100 \times (4) / M_g$	$100 \times (4) / R$
	(1)	(2)	(3)	(4)	(5)	(6)
1955/56	.036	.264	.300	2.25	4.93	10.99
1956/57	.041	.322	.364	2.85	5.91	11.88
1957/58	.040	.315	.355	2.85	5.83	11.86
1958/59	.037	.298	.335	2.78	5.56	11.80
1959/60	.037	.297	.334	2.97	5.71	12.26
1960/61	.036	.278	.314	2.90	5.42	12.00
1961/62	.035	.275	.310	2.88	5.36	11.96
1962/63	.035	.266	.301	2.95	5.36	12.13
1963/64	.034	.256	.289	3.00	5.14	11.89
1964/65	.033	.249	.282	3.10	5.02	11.84
1965/66	.036	.277	.313	3.59	5.37	12.10
1966/67	.034	.288	.321	3.90	5.50	12.53
1967/68	.031	.271	.302	3.93	5.06	12.07
1968/69	.029	.247	.276	3.81	4.52	11.46
1969/70	.027	.229	.256	3.82	4.17	11.12
1970/71	.019	.206	.225	3.61	3.66	10.25
1971/72	.016	.197	.213	3.70	3.56	10.24
1972/73	.018	.179	.197	3.78	3.31	10.16
1973/74	.019	.180	.199	4.44	3.33	10.55
1974/75	.019	.165	.185	4.93	3.10	10.80
1975/76	.022	.203	.226	7.07	3.66	11.38
1976/77	.022	.201	.224	7.91	3.74	11.84
Mean	.030	.248	.278	3.77	4.69	11.51

Based on data given in Table 12 and the parameter estimates given in Tables 5 and 7.  $M_g = \sum_{i=1}^3 p_i q_i$  is expenditure on alcoholic beverages and  $R = \sum_{i=1}^3 [t_i / (1+t_i)] p_i q_i$  is total revenue from alcohol taxes.

In 1976/77 the welfare cost is .2 percent of income (total consumption expenditure) or \$7.91 per capita (in current dollars). This represents 3.7 percent of expenditure on alcoholic beverages and 11.8 percent of government revenue from alcohol taxes. The within group component represents about 10 percent of the total cost.

In the previous section we simulated the effects of the imposition of a tax on wine at the same rate as that on beer. The simulated taxes are given in Table 16. We now apply the above analysis to measure the welfare cost of this tax package and the results are given in Table 17. As the imposition of the wine tax goes in the direction of having uniform tax rates, the within group cost falls in relation to what it was previously. However, the between group and all other goods cost rises sufficiently to increase the total cost to \$8.72 per capita in 1976/77.

## 6. CONCLUDING COMMENTS

In this paper we have indicated how the system-wide approach to consumer demand can be extended so that it can be applied to quite narrowly defined commodity groups. Such applications have a number of attractions from the viewpoint of policy analysis for business and government. We analysed the consumption of beer, wine and spirits to illustrate the general principles and used the demand model for (i) a number of simulations designed to analyse the rapid growth of wine consumption and (ii) to measure the welfare cost of alcohol taxes.

TABLE 16

## SIMULATED ALCOHOL TAXES:

AUSTRALIA, 1955/56 - 1976/77

Year	Tax revenues (Dollars per capita)				Tax rates × 100 (Percentages of pre-tax prices)		
	Beer	Wine	Spirits	Total Alcohol	Beer	Wine	Spirits
	$\frac{t_1^s}{1 + t_1^s} p_1^s q_1^s$	$\frac{t_2^s}{1 + t_2^s} p_2^s q_2^s$	$\frac{t_3^s}{1 + t_3^s} p_3^s q_3^s$	$\sum_{i=1}^3 \frac{t_i^s}{1 + t_i^s} p_i^s q_i^s$	$t_1^s$	$t_2^s$	$t_3^s$
1955/56	18.33	0	2.14	20.47	117.198	0	38.351
1956/57	21.56	3.36	2.36	27.28	141.132	141.132	48.401
1957/58	21.61	3.43	2.36	27.41	137.090	137.090	47.588
1958/59	21.02	3.48	2.48	26.98	126.086	126.086	47.704
1959/60	21.44	3.74	2.73	27.91	124.296	124.296	48.524
1960/61	21.37	3.81	2.74	27.91	119.236	119.236	43.421
1961/62	21.27	3.83	2.77	27.87	117.250	117.250	43.133
1962/63	21.58	3.99	2.68	28.25	116.272	116.272	39.602
1963/64	22.31	4.10	2.88	29.28	111.358	111.358	38.773
1964/65	23.03	4.29	3.10	30.42	108.372	108.372	37.927
1965/66	26.17	5.41	3.43	35.01	119.674	119.674	42.436
1966/67	27.26	6.10	3.80	37.15	112.929	112.929	53.891
1967/68	28.28	6.82	4.22	39.32	104.365	104.365	53.254
1968/69	29.10	7.98	4.08	41.15	97.793	97.793	46.589
1969/70	29.72	8.60	4.54	42.87	90.491	90.491	44.862
1970/71	29.95	7.92	4.48	42.36	79.073	79.073	41.995
1971/72	30.41	8.07	4.73	43.21	74.356	74.356	41.749
1972/73	31.52	8.49	5.35	45.36	68.654	68.654	41.213
1973/74	34.18	9.00	7.86	51.05	61.598	61.598	53.584
1974/75	34.70	9.79	10.92	55.42	50.353	50.353	64.601
1975/76	49.97	15.68	12.09	77.74	64.761	64.761	64.965
1976/77	53.03	17.19	13.69	83.91	62.615	62.615	67.507
Mean	28.08	6.59	4.79	39.47	100.225	94.898	47.730

$t_i^s$  is the simulated tax rate on  $i$ ,  $p_i^s = p_i(1 + t_i^s)/(1 + t_i)$  is the simulated post-tax price of  $i$ , where  $p_i$  is the actual (post-tax) price and  $t_i$  the actual tax rate, and  $q_i^s$  is the simulated per capita consumption given in columns 7-9 of Table 14.

TABLE 17

## WELFARE COST OF SIMULATED ALCOHOL TAXES:

AUSTRALIA, 1955/56 - 1976/77

Year	Welfare cost as a fraction of total consumption expenditure × 100			Total welfare cost		
	Within alcoholic beverages group	Between alcoholic beverages and all other goods	Total = within + between	Dollars per capita	As a percentage of alcohol expenditure	As a percentage of revenue from alcohol taxes
	$-\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i^s}{1+t_i^s} \pi_{ij}^g \frac{t_j^s}{1+t_j^s}$	$-\frac{1}{2} \phi \theta_g (1-\theta_g) \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i^s}{1+t_i^s} \theta_i' \theta_j' \frac{t_j^s}{1+t_j^s}$	$-\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i^s}{1+t_i^s} \pi_{ij}^g \frac{t_j^s}{1+t_j^s}$	$\frac{(3)}{100} \times M$	$100 \times (4) / M_g^s$	$100 \times (4) / R^s$
	(1)	(2)	(3)	(4)	(5)	(6)
1955/56	.036	.264	.300	2.25	4.93	10.99
1956/57	.013	.411	.424	3.32	6.66	12.17
1957/58	.012	.402	.414	3.33	6.58	12.15
1958/59	.010	.379	.390	3.23	6.26	11.97
1959/60	.010	.377	.387	3.45	6.41	12.36
1960/61	.011	.355	.366	3.38	6.11	12.11
1961/62	.011	.350	.361	3.36	6.03	12.06
1962/63	.012	.340	.352	3.46	6.07	12.25
1963/64	.012	.327	.339	3.52	5.83	12.02
1964/65	.011	.318	.330	3.63	5.69	11.93
1965/66	.012	.354	.366	4.19	6.03	11.97
1966/67	.006	.363	.370	4.49	6.09	12.09
1967/68	.005	.342	.347	4.51	5.58	11.47
1968/69	.006	.312	.318	4.40	5.01	10.69
1969/70	.005	.290	.295	4.40	4.62	10.26
1970/71	.004	.254	.258	4.13	4.09	9.75
1971/72	.003	.240	.243	4.23	3.98	9.79
1972/73	.002	.223	.225	4.32	3.70	9.52
1973/74	.000	.222	.223	4.96	3.65	9.72
1974/75	.001	.201	.202	5.37	3.34	9.69
1975/76	.000	.250	.250	7.83	3.96	10.07
1976/77	.000	.246	.247	8.72	4.03	10.39
Mean	.008	.310	.319	4.30	5.21	11.16

Based on data given in Table 16 and the parameter estimates given in Tables 5 and 7.  $M_g^s = \sum_{i=1}^3 p_{ii}^s q_i^s$  is simulated expenditure on alcoholic beverages and  $R^s = \sum_{i=1}^3 [t_i^s / (1+t_i^s)] p_{ii}^s q_i^s$  is simulated total revenue from alcohol taxes.

## APPENDIX

Unconditional Demand Equations

Letting  $p = [p_1, \dots, p_n]'$  and  $q = [q_1, \dots, q_n]'$ , the consumer chooses  $q$  to maximize the utility function  $u(q)$  subject to the budget constraint  $p'q = M$ . The first-order conditions are the budget constraint and  $\partial u / \partial q = \lambda p$ , where  $\lambda$  is the marginal utility of income. Differentiating these conditions with respect to  $p$  and  $M$  gives Barten's (1964) fundamental matrix equation,

$$(A1) \quad \begin{bmatrix} U & p \\ p' & 0 \end{bmatrix} \begin{bmatrix} \partial q / \partial M & \partial q / \partial p' \\ -\partial \lambda / \partial M & -\partial \lambda / \partial p' \end{bmatrix} = \begin{bmatrix} 0 & \lambda I \\ 1 & -q' \end{bmatrix},$$

where  $U = \partial^2 u / \partial q \partial q'$  and  $\partial q / \partial M$  and  $\partial q / \partial p'$  are the income and price derivatives of the demand functions. Solving (A1) gives

$$(A2) \quad \frac{\partial q}{\partial p'} = \lambda U^{-1} - \frac{\lambda}{\partial \lambda / \partial M} \frac{\partial q}{\partial M} \frac{\partial q'}{\partial M} - \frac{\partial q}{\partial M} q',$$

for the price derivatives and

$$(A3) \quad \frac{\partial q}{\partial M} = \frac{\partial \lambda}{\partial M} U^{-1} p$$

for the income derivatives.

Defining  $P = \text{diag}[p]$ , we premultiply (A2) by  $P$  and postmultiply by  $P/M$  to give

$$(A4) \quad P \frac{\partial q}{\partial p'} P/M = v - \phi \theta \theta' - \theta w',$$

where  $v = \lambda P U^{-1} P/M = [v_{ij}]$ ,  $\phi = \frac{\lambda/M}{\partial \lambda / \partial M} = \left( \frac{\partial \log \lambda}{\partial \log M} \right)^{-1}$ ,  $\theta = P \partial q / \partial M = [\theta_i]$  and  $w = P q / M = [w_i]$ . Dividing (A3) by  $\partial \lambda / \partial M$  and premultiplying by  $\lambda P / M$  gives

$$\frac{\lambda/M}{\partial \lambda / \partial M} P \frac{\partial q}{\partial M} = \lambda P U^{-1} P/M = (\lambda P U^{-1} P/M) 1,$$

where  $1 = [1, \dots, 1]'$ , or

$$(A5) \quad \phi\theta = v_1,$$

which is equation (3) in vector form.

We write the demand equations in differential form as

$$dq = \frac{\partial q}{\partial M} dM + \frac{\partial q}{\partial p} dp.$$

Premultiplying by  $P/M$  gives

$$Wd(\log q) = \theta d(\log M) + \left( P \frac{\partial q}{\partial p}, P/M \right) d(\log p),$$

where  $W = \text{diag}[w]$ . Substituting the right side of (A4) for  $P \frac{\partial q}{\partial p}, P/M$ , we obtain

$$(A6) \quad \begin{aligned} Wd(\log q) &= \theta d(\log M) + (v - \phi\theta\theta' - \theta w') d(\log p) \\ &= \theta [d(\log M) - d(\log P)] + v(I - \theta\theta') d(\log p), \end{aligned}$$

where  $d(\log P) = w'd(\log p)$  and where we have used (A5) for substitute  $v_1$  for  $\phi\theta$ . The term  $d(\log M) - d(\log P)$  is the change in real income, which we write as  $d(\log Q)$ . Taking the differential of the budget constraint, we obtain  $w'd(\log p) + w'd(\log q) = d(\log M)$ , so that  $d(\log Q) = w'd(\log q)$  [see below equation (1)]. Writing  $d(\log P') = \theta'd(\log p)$  for the Frisch price index, (A6) can be expressed as

$$Wd(\log q) = \theta d(\log Q) + v[d(\log p) - \theta d(\log P')],$$

which is equation (1) in vector form.

#### Derivation of Equations (7) and (8)

Equation (7) is obtained by summing both sides of (6) over  $i \in S_g$ . The derivation of the variable on the left and the first term on the right of equation (7) is straightforward. We obtain the substitution term as follows. The sum over  $i \in S_g$  of the substitution term of equation (6) is

$$(A7) \quad \sum_{i \in S_g} \sum_{j \in S_g} v_{ij} d\left(\log \frac{p_j}{p_i}\right) = \phi \sum_{j \in S_g} \theta_j [d(\log p_j) - d(\log P')],$$

where we have used  $\sum_{i \in S_g} v_{ij} = \phi \theta_j$ , which follows from the symmetry of  $[v_{ij}]$  and (5). Since  $\theta_g = \sum_{j \in S_g} \theta_j$ , the second member of (A7) can be expressed as

$$(A8) \quad \phi \theta_g \left[ \sum_{j \in S_g} \frac{\theta_j}{\theta_g} d(\log p_j) - d(\log P') \right] = \phi \theta_g [d(\log P'_g) - d(\log P')],$$

where  $d(\log P'_g) = \sum_{j \in S_g} (\theta_j / \theta_g) d(\log p_j)$  is the Frisch price index of the group. The second member of (A8) is the substitution term of equation (7).

To derive equation (8), we rearrange (6) and (7) to give

$$(A9) \quad d(\log Q) = \frac{w_i}{\theta_i} d(\log q_i) - \sum_{j \in S_g} \frac{v_{ij}}{\theta_i} d\left(\log \frac{p_j}{P'}\right)$$

$$(A10) \quad d(\log Q) = \frac{w_g}{\theta_g} d(\log Q_g) - \phi d\left(\log \frac{P'_g}{P'}\right).$$

Equating the right side of (A9) with that of (A10) and rearranging gives

$$\begin{aligned} w_i d(\log q_i) &= \frac{\theta_i}{\theta_g} w_g d(\log Q_g) + \sum_{j \in S_g} v_{ij} d(\log p_j) \\ &\quad - \sum_{j \in S_g} v_{ij} d(\log P') - \phi \theta_i d(\log P'_g) + \phi \theta_i d(\log P') \\ &= \frac{\theta_i}{\theta_g} w_g d(\log Q_g) + \sum_{j \in S_g} v_{ij} [d(\log p_j) - d(\log P'_g)], \end{aligned}$$

which follows from (5). This is equation (8).

### The Construction of $DP_0$

We write the log-change in the consumer price index ( $DP^*$ ) as a weighted average of the price log-changes of the  $n$  goods, with the averages of the budget shares as weights. With the alcoholic beverages the first three goods, we have

$$(A11) \quad DP_t^* = \sum_{i=1}^3 \bar{w}_{it} DP_{it} + \sum_{i=4}^n \bar{w}_{it} DP_{it} = \bar{w}_{gt} DP_{gt} + (1 - \bar{w}_{gt}) DP_{ot},$$



## REFERENCES

- Barten, A.P. (1964). "Consumer Demand Functions Under Conditions of Additive Preferences." *Econometrica* 32: 1-38.
- \_\_\_\_\_ (1977). "The Systems of Consumer Demand Functions Approach: A Review." *Econometrica* 45: 23-51.
- Brown, A. and A. Deaton (1972). "Surveys in Applied Economics: Models of Consumer Behavior." *Economic Journal* 82: 1145-1236.
- Clements, K.W. (1981). "Changes in the Size of the Traded Goods Sector: Theory and Applications." *Empirical Economics*, forthcoming.
- \_\_\_\_\_ and P. Nguyen (1980). "Money Demand, Consumer Demand and Relative Prices in Australia." *Economic Record* 56: 338-46.
- \_\_\_\_\_ and H. Theil (1979). "A Cross-Country Analysis of Consumption Patterns." Report 7924 of the Center for Mathematical Studies in Business and Economics, The University of Chicago.
- Harberger, A.C. (1964). "Taxation, Resource Allocation and Welfare." In *The Role of Direct and Indirect Taxes in the Federal Reserve System*. Princeton: Princeton University Press for the NBER and the Brookings Institute. Reprinted in A.C. Harberger (1974), *Taxation and Welfare*. Chicago: The University of Chicago Press.
- Phlips, L. (1974). *Applied Consumption Analysis*. Amsterdam: North-Holland Publishing Company.
- Powell, A.A. (1974). *Empirical Analytics of Demand Systems*. Lexington, MA: D.C. Heath.

where  $\bar{w}_{gt} = \sum_{i=1}^3 \bar{w}_{it}$ ,  $DP_{gt} = \sum_{i=1}^3 (\bar{w}_{it}/\bar{w}_{gt}) DP_{it}$  is the Divisia price index of the group and  $DP_{ot} = \sum_{i=4}^n [\bar{w}_{it}/(1 - \bar{w}_{gt})] DP_{it}$  is the Divisia price index of all other goods. We express  $DP_{ot}$  in terms of observables by rearranging (All) to give

$$DP_{ot} = (DP_t^* - \bar{w}_{gt} DP_{gt}) / (1 - \bar{w}_{gt}) ,$$

which is the equation used to define  $DP_{ot}$ .

#### Derivation of Equation (27)

We divide both sides of (26) by  $M$  and then multiply and divide the right by  $p_i p_j$  to give

$$\begin{aligned} \frac{W}{M} &= -\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{T_i}{p_i} \frac{p_i p_j}{M} S_{ij} \frac{T_j}{p_j} \\ &= -\frac{1}{2} \sum_{i=1}^3 \sum_{j=1}^3 \frac{t_i}{1 + t_i} \frac{p_i p_j}{M} S_{ij} \frac{t_j}{1 + t_j} , \end{aligned}$$

as  $T_i = t_i p_i^0$  and  $p_i = (1 + t_i) p_i^0$ . To establish that this is equivalent to (27) we need to show that  $\pi_{ij} = (p_i p_j / M) S_{ij}$ . To do this, consider the change in demand for  $i$  when (i) real income is constant and (ii) only  $p_j$  changes. From (A6) this is

$$w_i d(\log q_i) = (v_{ij} - \phi \theta_i \theta_j) d(\log p_j) = \pi_{ij} d(\log p_j) ,$$

where the second step is based on (10) and (20). This can be written as

$$\frac{p_i}{M} dq_i = \pi_{ij} \frac{dp_j}{p_j} ,$$

so that

$$dq_i = (M/p_i p_j) \pi_{ij} dp_j .$$

As real income is constant,  $(M/p_i p_j) \pi_{ij} = S_{ij}$ , so that  $\pi_{ij} = (p_i p_j / M) S_{ij}$ .

## FOOTNOTES

1. We use Wymer's (1977) estimation program RESIMUL.
2. That is, these coefficients have  $|t|$ -values greater than two.
3. As one of three estimating equations is redundant, the homogeneity constraint (12) involves two restrictions while symmetry (13) involves one.
4. See, e.g., Clements (1981), Clements and Nguyen (1980), Clements and Theil (1979), Theil (1975/76, 1980) and Theil and Suhm (1981).
5. For a further analysis, see Theil (1975/76, pp. 31-2).
6. These are customs and excise taxes. Full details and sources of these data are given in a separate Appendix, available on request.