# The Direct Spectroscopy of Positronium Hyperfine Structure Using a Sub-THz Gyrotron

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Received: 24 April 2013 / Accepted: 3 July 2013 / Published online: 25 July 2013 © Springer Science+Business Media New York 2013

**Abstract** Positronium is an ideal system for research on Quantum Electrodynamics (QED), especially in a bound state. A discrepancy of 3.9 standard deviations has been found between the measured hyperfine structure (Ps-HFS) and the QED predictions. This may be due to the contribution of unknown new physics or common systematic effects in previous measurements, in all of which the Zeeman effect was used. We propose a new method to directly measure the Ps-HFS using a high power gyrotron. We compare two resonators which have been developed to supply sufficient power to drive the direct transition, a Fabry-Pérot resonator and a ring resonator with a diffraction grating. We plan to perform first direct measurement of Ps-HFS within the next six months.

**Keywords** Positronium · Hyperfine splitting · Gyrotron · Fabry-Pérot resonator · Ring resonator · Diffraction grating

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# 1 Introduction

Positronium (Ps), the bound state of an electron and a positron, is a purely leptonic system and is a good system with which to precisely study Quantum Electrodynamics (QED) [1]. Positronium has two spin eigenstates: *ortho*-positronium (*o*-Ps, Spin=1, lifetime=142 ns, three-photon decay) and *para*-positronium (*p*-Ps, Spin=0, lifetime=125 ps, two-photon decay). The positronium hyperfine structure (Ps-HFS) is the energy difference between ground-state *o*-Ps and *p*-Ps. Ps-HFS is about 203 GHz (0.84 meV), is significantly larger than the hyperfine structure of the hydrogen atom (1.4 GHz) [2].

Precise measurements have been performed in 1970's and 80's, the results of which are shown in Fig. 1. These results are all consistent, and the average of the two most accurate measurements is 203.388 65(67) GHz (3.3 ppm) [3], shown by a green band. A calculation of higher order corrections to the bound state was made in 2000 [4]. The QED prediction is 203.3917(6) GHz (2 ppm), shown as a red band in Fig. 1. A discrepancy of 3.04(79) MHz (15 ppm) is found between the measured value and the QED prediction, which is unlikely to be due to a statistical fluctuation (3.9 standard deviations).

In all previous measurements, the Ps-HFS transition is not observed because 203 GHz is too high a frequency to be handled. A static magnetic field is applied to cause Zeeman mixing, and Ps-HFS is extracted from the Zeeman shift [3]. As mentioned in Ref. [5], there are two possible uncertainties in this method. The first is due to a non-uniformity of the static magnetic field, and the second is due to the non-thermalization of positronium in gas, similar to effects seen in lifetime measurements of *o*-Ps [6]. We have previously proposed a new method to overcome these problems [7].

It is very important to re-measure Ps-HFS using a method totally different from previous experiments. Some independent experiments (using quantum interference [8], optical lasers [9], and a precise magnetic field and correcting gas effect [10])



have been performed, but have not yet reached a sufficient level of precision to address the observed discrepancy.

A direct measurement of the Ps-HFS transition without a static magnetic field is free from systematic uncertainties due to magnetic fields. This new method becomes possible by using a gyrotron which can produce high power sub-THz radiation. We are planning to directly measure Ps-HFS with an initial precision of about 0.1 %. Although this experiment faces certain technological difficulties connected to the use of sub-THz waves, it is the only method which does not use a static magnetic field, and has great potential to solve the problem in the future.

## 2 Direct Measurement of Ps-HFS

Figure 2 shows a schematic view of the direct transition. *O*-Ps transits directly into *p*-Ps when irradiated by electromagnetic waves of about 203 GHz. The transiting *p*-Ps immediately decays into back-to-back two photons (lifetime is 125 ps), whereas *o*-Ps decays slowly into three photons (lifetime is 142 ns). This direct transition can be probed by an increase of two photon decay. High power radiation of over 10 kW is needed to drive the transition because this is the magnetic dipole transition and severely suppressed (transition rate is  $3.37 \times 10^{-8} s^{-1}$  [11]). The radiation frequency should be tuned around 203 GHz  $\pm$  2 GHz in order to measure the Breit-Wigner resonance.

An optical system composed of a gyrotron and an optical resonator has been developed to produce high power and tunable sub-THz radiation. Figure 3a shows a schematic view of the experimental setup. A gyrotron is used as a sub-THz radiation source, with an output power of about 300 W. An optical resonator accumulates the gyrotron output to obtain a power equivalent to about 20 kW. Positronium is formed inside the resonator and decays into photons ( $\gamma$  rays) which are detected by  $\gamma$ -ray detectors.



Fig. 2 Schematic diagram of the direct transition of positronium in the ground state



Fig. 3 a Schematic view of the experimental setup. b Photograph of FU CW GI

# 2.1 Gyrotron

Figure 3b shows a photograph of the gyrotron (FU CW GI) developed specifically for Ps-HFS measurement [12]. The operation mode is the counter rotating  $TE_{52}$  mode, and its output is converted to a Gaussian mode by an internal mode converter as shown in Fig. 4a.

The output power of the Gaussian beam has been measured using a water load. Its peak power is about 300 W with a condition of duty ratio 30 % and repetition rate 5 Hz. The accelerating voltage and beam current of the magnetron injection gun are 18 kV and 0.5 A, respectively.



Fig. 4 a Mode pattern measured by an infrared camera after M2 as shown in Fig 3a. b Result of the frequency measurement using a harmonic mixer

The width of the Ps-HFS Breit-Wigner resonance is about 1.3 GHz (FWHM) corresponding to the lifetime of *p*-Ps. The gyrotron is developed to have interchangeable cavities of different diameters. Figure 4b shows the results of frequency measurement for different cavities. The frequency of the gyrotron is continuously tunable within range of a few hundred MHz by adjusting the magnetic field strength *B* according to the formula  $f_c = eB/2\pi m_0\gamma$ , where  $m_0$  is the electron rest mass and  $\gamma$  is the relativistic factor of the electron. The Ps-HFS value can be measured by selecting appropriate cavities and magnetic field strengths.

## 2.2 Optical Resonator

The Gaussian beam from the gyrotron is accumulated in an optical resonator to drive the direct transition. Two candidates have been developed in parallel: a *Fabry-Pérot resonator* with a gold mesh, and a *ring resonator* with a diffraction grating. The direct transition was firstly observed using the Fabry-Pérot resonator [13]. The ring resonator has the advantage of allowing the accumulation of very high power when the gyrotron output increases into the MW range.

## 2.2.1 Fabry-Pérot Resonator with a Gold Mesh Mirror

Figure 5a shows a photograph of the the Fabry-Pérot resonator, which consists of two parallel mirrors. The mirror on the input side, of diameter 50 mm, consists of a gold mesh. It has a high reflectance (over 99 %) and does not severely disturb the input Gaussian beam. The mirror on the other side is a concave copper mirror (with a radius of curvature of 300 mm and an expected reflectance of 99.85 %). A piezoelectric stage under the copper mirror controls the cavity length (about 160 mm) with submicron precision. A pyroelectric detector monitors the transmitted radiation through a small hole ( of diameter 0.6 mm) on the copper mirror. A second pyroelectric detector outside the resonator monitors the reflected power.

The gold mesh, shown in Fig. 5b, was evaporated onto the high resistivity silicon substrate. The good thermal conductivity (150 W/Km) of the silicon enables the mesh to be cooled by water. The mesh parameters (width, gap, and thickness of the mesh and the substrate) was carefully optimized using CST MW studio [14] to avoid interference between the gold mesh and substrate. The S-parameters of the mesh mirror were simulated in the frequency domain solver under periodic boundary conditions.

Two independent parameters, the finesse and coupling, are used to estimate the gain of the optical resonator. The finesse  $\mathcal{F}$  is equivalent to the Q factor and is defined as

$$\mathcal{F} = \frac{2\pi}{1 - R_f R_e},\tag{1}$$

where  $R_f$  and  $R_e$  are reflectance of the gold mesh and the copper mirror, respectively [15]. The coupling *C* is the effective power input into the resonator. It becomes 100 % when all input power enters the resonator. The gain *G* of the resonator is approximated by  $G = C \mathcal{F} / \pi$ .



Fig. 5 a Photograph of the Fabry-Pérot resonator. b Gold mesh pattern on a high-resistivity silicon substrate

Figure 6a shows the simulated finesse of the cavity with an optimized mesh mirror. Although the finesse has an inevitable frequency dependence because of the high refractive index of the silicon substrate at 203 GHz (n = 3.45), the finesse is over 400 between 201 GHz and 205 GHz and is adequate for the proposed measurement of Ps-HFS. Figure 6b shows the measured resonance of the Fabry-Pérot resonator at 202.1 GHz. Experimentally,  $\mathcal{F}$  can be obtained by  $\mathcal{F} = \frac{\text{FSR}}{\Gamma}$ , where FSR is Free Spectral Range ( $\lambda/2 = 735 \,\mu$ m), and  $\Gamma$  is FWHM of the resonance as shown in Fig. 6b. The measured  $\mathcal{F}$  is estimated to be 430, which is smaller than the simulated value at 202.1 GHz (about 600) due to the finite line width of the gyrotron oscillation ( $\Delta f \sim 1 \,\text{MHz}$ ). The coupling is the fractional decrease of reflected power on



**Fig. 6** a Calculated finesse of the Fabry-Pérot resonator with the optimized gold mesh (width=200  $\mu$ m, gap=140  $\mu$ m, thickness=1  $\mu$ m) on the silicon substrate (thickness=1960  $\mu$ m). The simulation only includes ohmic losses of the plane wave at the mirrors. **b** Measured resonance of the new Fabry-Pérot resonator at 202.1 GHz. The *red points* are transmitted power, and the *blue points* are reflected power. The *solid line* shows the best fitting Breit-Wigner curves

resonance, and is measured to be 62 % as shown in Fig. 6b. Therefore, the measured gain of the new Fabry-Pérot resonator is about 85. The equivalent power inside the resonator is 25 kW in case of 300 W input power. The accumulated power is affected by the line width of the gyrotron oscillation, but 25 kW is sufficient for this measurement.

## 2.2.2 Ring Resonator with a Diffraction Grating

We have also developed a ring cavity with a diffraction grating and compared its performance to the Fabry-Pérot resonator. It consists of three copper mirrors as shown in Fig. 7. The main mirror is a diffraction grating made of copper. It is easier to watercool this grating than the mesh mirror of the Fabry-Pérot resonator. The diffracted beam enters the cavity which resonantes when the length of the triangular optical path is an integer multiple of the wavelength ( $\lambda = 1.47$  mm). The reflected beam (0th diffraction) does not return into the incident direction, an advantage of the ring resonator over the Fabry-Pérot resonator. Denoting the incident angle  $\alpha$ , diffraction angle  $\beta$ , and spacing of the grating d, the grating equation is given by

$$d(\sin\alpha + \sin\beta) = m\lambda \ (m = 0, \pm 1, \pm 2, \ldots). \tag{2}$$

According to Eq. 2, the spacing *d* is uniquely determined if the cavity shape is fixed. The grating should be designed to reduce higher order diffractions since they cause loss of input power and therefore reduce the coupling. We chose  $\alpha = 60^\circ$ ,  $\beta = 15^\circ$  and m = -1, giving a spacing *d* of 1.31 mm.

Diffraction gratings with grooves of different shapes and depths have been fabricated and compared. Figure 8 shows a typical resonance. Table 1 summarizes the performance of different gratings. Gratings with shallower grooves have a higher finesse, however the coupling decreases if the grooves are too shallow. This is because a small amount of scattered radiation by the grating surface becomes comparable to the diffracted beam power. The circular type grating has cylindrical grooves



Fig. 7 Photograph of the diffraction grating (*left*) and schematic view of the ring resonator (*right*)



Fig. 8 Obtained resonance of the ring resonator at 202.9 GHz when grating type is circular, and depth is 48  $\mu$ m. The definition of the points and lines are the same as that of Fig. 6b

with sharp edges, while the sine type grating grooves have a a smooth sine-wave profile.<sup>1</sup> The circular shape grating has a higher finesse than a sine shape grating with the same groove depth. The best performance is obtained by the circular type with a groove depth of 48  $\mu$ m as shown in Fig. 8. The gain *G* is about 110, and accumulated power inside the resonator is expected to be over 30 kW.

The optical performance of the ring resonator is better than that of the Fabry-Pérot resonator. However, the Fabry-Pérot resonator has a significant advantage when we consider Ps formation. A positron source is used to form Ps with an electron in a gas molecule [5]. Since the optical path of the ring cavity is split into two separate paths, positronium cannot be efficiently formed in both. The direct transition signal (i.e. two photons from transiting *p*-Ps) from the ring resonator is half of that from the Fabry-Pérot resonator. We have therefore decided to use the Fabry-Pérot resonator for the first measurement of Ps-HFS.

Although the ring resonator is not suitable for Ps-HFS measurement using a positron source, it will be an excellent solution if a positron beam [16] is introduced in the future. Because of the split optical path, the energy density of the diffraction grating is half as small as that of the Fabry-Pérot resonator, which prevents saturation of the transition probability of positronium. If positronium can be efficiently formed in the large optical-path region by a positron beam, the transition signal from the resonator will be drastically enhanced.

The ring resonator has another possible application. The equivalent power inside the resonator will be of order 100 MW when we introduce a MW-class gyrotron [17]. Such high power millimeter waves can be used to search for hypothetical light particles predicted in particle physics [18]. The diffraction grating can endure a power of 1 MW, whereas the gold mesh of the Fabry-Pérot resonator definitely cannot. An additional advantage is that the beam reflected from the resonator does not return to the input source. In contrast, the reflected beam from the Fabry-Pérot resonator inevitably returns into the gyrotron, destabilizing the gyrotron oscillation [19], which should be prevented, especially when a MW-class gyrotron is used.

<sup>&</sup>lt;sup>1</sup>The popular blazed type grating is not suitable because its asymmetrical shape cannot maximize both finesse and coupling in the case of our ring cavity whose optical path is an isosceles triangle.

<b>Table 1</b> Comparison of different gratings at 202.9 GHz.The small coupling of circular type with depth of 36 $\mu$ m may be due to scratches on the surface				
	Shape	Depth ( $\mu$ )m	${\cal F}$	С
	circular	72	405	59 %
	circular	48	628	56 %
	circular	36	636	18 %
	circular	24	910	24 %
	sine	36	576	45 %

#### **3** Current Status and Future Prospect

We have already observed the direct transition at 202.9 GHz as shown in Fig. 9 (solid point) [13, 20]. The dotted line in Fig. 9 is the theoretical calculation of the Breit-Wigner shape of the transition. We will measure the transition at four additional points (201.8 GHz, 203.4 GHz, 204 GHz and 205.3 GHz) within half a year. The Ps-HFS will be directly measured with precision of about 0.1 % for the first time.

In order to test the Ps-HFS discrepancy, four technological progresses are needed. First, a precise power detector (relative accuracy is better than 0.3 %) should be developed in the 200 GHz region. Secondly, the quality and stability of the gyrotron oscillation should be improved. The line width of the oscillation frequency must be stable and less than 100 kHz. Thirdly, a high power gyrotron with continuously tunable frequency should be developed. A reflective gyro-backward-wave oscillator has been theoretically proposed, but not yet put into practice [21]. Lastly, a positron beam should be used to obtain better statistics.



Fig. 9 Transition curve of the Ps-HFS transition. The *solid point* shows the measured transition (only statistical error is shown); the *dotted line* does a theoretical prediction

# 4 Summary

There is a discrepancy between the measured Ps-HFS values and QED predictions. We propose that the direct measurement of Ps-HFS is free from the possible systematic uncertainties due to the magnetic field present in all the previous measurements. A gyrotron with an internal mode converter has been developed, whose frequency can be tuned to scan the entire resonance curve of the Ps-HFS transition. In order to obtain the 20 kW equivalent power needed to efficiently drive the direct transition, a Fabry-Pérot resonator and a ring resonator were developed and compared. We will directly measure the Ps-HFS using the Fabry-Pérot resonator for the first time within half a year.

Acknowledgments Sincere gratitude is extended to Dr. Daniel Jeans for the useful discussions.

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