# The earliest stars and their relics in the Milky Way 

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#### Abstract

We have implemented a simple model to identify the likely sites of the first stars and galaxies in the high-resolution simulations of the formation of galactic dark matter haloes of the Aquarius Project. The first star in a galaxy like the Milky Way formed around redshift $z=35$; by $z=$ 10 , the young galaxy contained up to $\sim 3 \times 10^{4}$ dark matter haloes capable of forming stars by molecular hydrogen cooling. These minihaloes were strongly clustered, and feedback may have severely limited the actual number of Population III stars that formed. By the present day, the remnants of the first stars would be strongly concentrated to the centre of the main halo. If a second generation of long-lived stars formed near the first (the first star relics), we would expect to find half of them within $30 h^{-1} \mathrm{kpc}$ of the Galactic Centre and a significant fraction in satellites where they may be singled out by their anomalous metallicity patterns. The first halo in which gas could cool by atomic hydrogen line radiation formed at $z=$ 25 ; by $z=10$, the number of such 'first galaxies' had increased to $\sim 300$. Feedback might have decreased the number of first galaxies at the time when they undergo significant star formation, but not the number that survive to the present because near neighbours merge. Half of all the 'first galaxies' that formed before $z=10$ merge with the main halo before $z \sim 3$ and most lose a significant fraction of their mass. However, today there should still be more than 20 remnants orbiting within the central $\sim 30 h^{-1} \mathrm{kpc}$ of the Milky Way. These satellites have circular velocities of a few kilometres per second or more, comparable to those of known Milky Way dwarfs. They are a promising hunting ground for the remnants of the earliest epoch of star formation.


Key words: methods: $N$-body simulations - methods: numerical - galaxies: formation galaxies: haloes - galaxies: structure - dark matter.

## 1 INTRODUCTION

The first stars probably formed through molecular hydrogen cooling of gas compressed in dark matter potential wells (Couchman \& Rees 1986; Tegmark et al. 1997; see Bromm \& Larson 2004 for a recent review). The temperature of the gas needs to be $\geq 10^{3} \mathrm{~K}$ for $\mathrm{H}_{2}$ formation to be efficient; in a $\Lambda$ cold dark matter ( $\Lambda \mathrm{CDM}$ ) universe dark matter haloes with deep enough potential wells to heat the gas to this temperature form as early as redshift $z \sim 50$ (Gao et al. 2004a; Reed et al. 2005). Such stars were very massive, $M \sim$ $10^{2} \mathrm{M}_{\odot}$ (Abel, Bryan \& Norman 2000; Bromm, Coppi \& Larson 2002; Yoshida et al. 2006; Gao et al. 2007) and, depending on their initial mass, would have ended their short lives as supernovae or by

[^0]collapsing directly into a black hole (Heger et al. 2003). In neither case can the remnants be identified today.

Very massive first stars ('Population III' or 'Pop. III' stars) emit copious amounts of ultraviolet (UV) photons (Schaerer 2002) which may affect star formation in nearby haloes through photoevaporation (Shapiro, Iliev \& Raga 2004; Whalen et al. 2008) and/or destruction of molecular hydrogen by photons in the Lyman-Werner bands (Haiman, Rees \& Loeb 1997). These photons could contribute to the reionization of the Universe (e.g. Sokasian et al. 2004). Elements synthesized during stellar evolution may pollute the surroundings, affecting the cooling rate of gas (Bromm, Yoshida \& Hernquist 2003). The combined 'feedback' of photoionization, energy injection and changes in composition may allow the formation of lower mass stars ( $M \sim 40 \mathrm{M}_{\odot}$, Yoshida et al. 2007) and their feedback may eventually allow the formation of even lower mass stars, some of which could still be present today. These very old

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Table 1. Properties of the six Aquarius haloes, Aq-A - Aq-F. The Aq-A halo has been resimulated at a variety of numerical resolutions, labelled Aq-A-1 - Aq-A-5. (In this paper, we analyse only Aq-A-1 and Aq-A-2.) From left- to right-hand side, the columns give: the halo identifier, particle mass, (comoving) force softening length in the high-resolution region, virial mass, virial radius, and maximum and virial circular velocity, all at redshift $z=0\left(M_{200}, r_{200}, V_{\max }\right.$ and $V_{200}$, respectively $)$.

| Name | $m_{\mathrm{p}}\left(h^{-1} \mathrm{M}_{\odot}\right)$ | $\epsilon\left(h^{-1} \mathrm{pc}\right)$ | $M_{200}\left(h^{-1} \mathrm{M}_{\odot}\right)$ | $r_{200}\left(h^{-1} \mathrm{kpc}\right)$ | $V_{\max }\left(\mathrm{s}^{-1} \mathrm{~km}\right)$ | $V_{200}\left(\mathrm{~s}^{-1} \mathrm{~km}\right)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Aq-A-1 | $1.25 \times 10^{3}$ | 15.0 | $1.34 \times 10^{12}$ | 179.40 | 208.8 | 179.2 |
| Aq-A-2 | $1.00 \times 10^{4}$ | 48.0 | $1.34 \times 10^{12}$ | 179.40 | 208.5 | 179.2 |
| Aq-B-2 | $4.70 \times 10^{3}$ | 48.0 | $0.60 \times 10^{12}$ | 136.51 | 157.7 | 137.5 |
| Aq-C-2 | $1.02 \times 10^{4}$ | 48.0 | $1.30 \times 10^{12}$ | 177.26 | 222.4 | 177.6 |
| Aq-D-2 | $1.02 \times 10^{4}$ | 48.0 | $1.30 \times 10^{12}$ | 177.26 | 203.2 | 177.6 |
| Aq-E-2 | $7.00 \times 10^{3}$ | 48.0 | $0.87 \times 10^{12}$ | 155.00 | 179.0 | 155.4 |
| Aq-F-2 | $4.95 \times 10^{3}$ | 48.0 | $0.83 \times 10^{12}$ | 152.72 | 169.1 | 153.2 |

stars could provide 'archaeological' evidence for early star formation through, for example, unusual element abundance patterns (e.g. Iwamoto et al. 2005). As structure formation progresses, more massive dark matter haloes form in which gas can now be cooled by radiation from atomic hydrogen. This can occur as early as redshift $z \sim 40$ (Reed et al. 2005). Star formation in such 'first galaxies' may be very different from that in the first haloes (see e.g. Wise \& Abel 2008) because of more efficient cooling by $\mathrm{H}_{\mathrm{I}}$ and the metals released by the previous Pop. III stars.

There are currently no direct observational constraints on this scenario and so many uncertainties remain. For example, first star formation in a Universe where structure on small scales is suppressed due to free streaming of the dark matter (as in Warm dark matter models) is very different (Gao \& Theuns 2007); annihilating dark matter, not fusion, may power the first stars if the dark matter consists of Majorana particles (Freese et al. 2009). Whilst the initial stages of cloud collapse can be understood in terms of the properties of the $\mathrm{H}_{2}$ molecule (Abel, Bryan \& Norman 2002; Yoshida et al. 2006), uncertainties from the modelling of radiative feedback of the proto-star make the final stellar mass uncertain (McKee \& Tan 2008), although the general view is that these stars are massive. The second-generation stars may, in fact, have relatively high metallicity if metal mixing is inefficient. Ionization front instabilities (Whalen \& Norman 2008) and the explosive growth of $\mathrm{H}_{2}$ following photoionization may also strongly affect the next generation of stars (Whalen et al. 2008).

A number of important questions remain unanswered. Did star formation in the Milky Way galaxy start with a display of fireworks? If so, where should we look for archaeological evidence? Will most of very old stars be in the bulge (White \& Springel 2000) or will some be found in the halo? Two recently discovered 'hyper metal poor' stars $[(\mathrm{Fe} / \mathrm{H}]<-5)$ have peculiar element abundances. Were these second-generation stars enriched by the first stars ${ }^{1}$ (see the review by Beers \& Christlieb 2005)? Finding more such unusual stars in the Milky Way is a key science driver for new surveys such as the Sloan Extension for Galactic Understanding and Exploration (SEGUE) and Large Sky Area Multi-Object Fiber Spectroscopic Telescope (LAMOST). Did any of the first galaxies survive to the present day? Where are their remnants? Are they related to the newly discovered dwarfs (Willman et al. 2005; Belokurov et al. 2006), as discussed in a number of recent papers (Madau, Diemand \& Kuhlen 2008; Bovill \& Ricotti 2009; Koposov et al. 2009). If so, what constraints do these place on the earliest star formation?

[^1]Helmi et al. (2006) argued that the remnants of early star formation in the Milky Way differ from those in dwarf galaxies because the latter had already been polluted with metals. However, Kirby et al. (2008) drew the opposite conclusion from more detailed modelling of stellar metallicities.

In this paper, we address some of these questions using a suite of ultra-high resolution cosmological dark matter simulations of galactic haloes - the Aquarius Project. The six dark matter haloes data from the Aquarius Project picked from a large cosmological simulation to be similar in mass to that of the Milky Way, and they were simulated at a variety of numerical resolutions. This enables us to investigate halo-to-halo variations, and establish the limitations imposed by resolution. We employ simple models to identify the sites of first star or first galaxy formation, and follow a suitable selection of dark matter particles to track where their progenitors are today, yielding generic cold dark matter predictions for early star formation in galaxies like the Milky Way.

The outline of the paper is as follows. In Sections 2-4, respectively, we describe the simulations, our models for identifying first star and first galaxy haloes, and investigate the clustering of these haloes. In Section 5, we trace the early objects to $z=0$ and discuss their properties and spatial distribution. Finally, in Section 6, we present a summary and discussion of our results.

## 2 SIMULATIONS

The dark matter simulations analysed in this study come from the Aquarius Project ${ }^{2}$ (Springel et al. 2008a,b; Navarro et al. 2009): a set of six haloes similar to that of the Milky Way (virial mass $M_{200} \sim 10^{12} h^{-1} \mathrm{M}_{\odot}$, circular velocity $V_{200} \sim 180 \mathrm{~km} \mathrm{~s}^{-1}$, where the subscript 200 refers to the region within which the density is 200 times the cosmic critical density; see Table 1). The haloes were identified in a larger cosmological simulation, the hMS simulation (Gao et al. 2008), which follows the growth of structure in a periodic box of comoving length $100 h^{-1} \mathrm{Mpc}$ with $900^{3}$ particles, assuming the same cosmological parameters as in the Millennium simulation ${ }^{3}$ (Springel et al. 2005): $\Omega_{\mathrm{m}}=0.25, \Omega_{\Lambda}=0.75, h=0.73, \sigma_{8}=0.9$. The hMS is itself a lower resolution version of the MillenniumII simulations ${ }^{4}$ (Boylan-Kolchin et al. 2009), so that the Aquarius haloes are also present in the Millennium-II simulation.

Resimulating the formation of haloes in such a large box correctly accounts for tidal forces and yields realistic formation times. The

[^2]'zoom' technique for resimulating haloes represents the mass which ends up inside or near the chosen halo with many low-mass particles and a small gravitational softening; the mass in more distant regions is represented with increasingly more massive particles with larger gravitational softening. Appropriate small-scale power is added in the initial conditions to perturb the high-resolution particles. The haloes, labelled Aq-A to Aq-F, are simulated with up to $10^{9}$ particles within the virial radius (particle mass $\sim 10^{3-4} h^{-1} \mathrm{M}_{\odot}$ ), using the GADGET-3 simulation code which is an updated version of GADGET-2 (Springel 2005). The Aq-A halo has been resimulated at different resolutions in order to study numerical convergence.

Snapshots are stored at 128 output times equally spaced in $\log (a)$, where $a=1 /(1+z)$ is the expansion factor, between redshifts $z=$ 127 and 0 . Dark matter haloes and their substructure are identified using a combination of the friends-of-friends algorithm (Davis et al. 1985) and SUBFIND (Springel et al. 2001). SUBFIND groups particles into substructures based on their density and binding energy. Haloes and their substructure are traced through the snapshots and linked together in a merger tree, as in Cole et al. (2008).

Although the Aquarius haloes range in mass only from $0.6 \times$ $10^{12}$ to $1.3 \times 10^{12} h^{-1} \mathrm{M}_{\odot}$, their mass accretion histories, plotted in Fig. 1, differ significantly. For example, the mass of the main progenitor of the Aq-F halo is nearly an order of magnitude lower than that of Aq-C as late as $z \sim 1$, and similarly large differences occur for other haloes at higher $z$. The thick dashed line is the extended Press-Schechter (Press \& Schechter 1974; Bond et al. 1991; Lacey \& Cole 1993) prediction for a halo of the median mass, $M=1.3 \times 10^{12} h^{-1} \mathrm{M}_{\odot}$, computed following Gao et al. (2004a). Apart from a systematic overestimate of the mass at high redshift ( $z>20$ ), the prediction works well.


Figure 1. Mass of the most massive progenitor of each of the six Aquarius haloes as a function of redshift [ $M(z)$, coloured lines], compared to the extended Press-Schechter theory for a halo of mass equal to the median for the six haloes, $M=1.3 \times 10^{12} h^{-1} \mathrm{M}_{\odot}$ (dashed line). There is over an order of magnitude variation in $M(z)$ between the haloes at certain redshifts, even though the $z=0$ masses are all within a factor of 2 (The number in brackets sorts haloes by their $z=0$ mass.). The extended Press-Schechter prediction works well, but systematically overestimates the mass above $z \sim$ 20.

## 3 IDENTIFYING SITES OF HIGH-REDSHIFT STAR FORMATION

In this section, we describe a simple model for identifying those haloes in the simulations which are likely to be the sites of early star formation.

### 3.1 Sites of Pop. III star formation

Our model is based on the results of a suite of hydrodynamical simulations of the formation of early structures in a $\Lambda$ CDM cosmology, carried out by Gao et al. (2007), which included nine species, non-equilibrium gas-phase chemistry of $\mathrm{H}_{2}$ production. The simulations used zoomed initial condition to follow the collapse to high densities ( $n_{\mathrm{H}} \sim 10^{10} \mathrm{~cm}^{-3}$ ) of gas in haloes with a wide range of formation redshifts $(50>z>10)$ and masses $\left(10^{5} h^{-1} \mathrm{M}_{\odot}<\right.$ $M<$ a few $\left.\times 10^{6} h^{-1} \mathrm{M}_{\odot}\right)$, and investigated how this depends on the assumed cosmological parameters. In agreement with previous studies (e.g. Abel et al. 2002; Bromm et al. 2002; Yoshida et al. 2006), these authors found that the virial temperature, $T_{\mathrm{vir}}$, of the parent dark matter halo is the key physical parameter that regulates how efficiently gas collapses and cools.

Once $T_{\text {vir }} \geq 10^{3} \mathrm{~K}$, the formation of molecular hydrogen becomes very efficient, a significant molecular hydrogen abundance ( $\mathrm{f}_{\mathrm{H}_{2}} \sim 10^{-4}$ ) builds up and the gas cools rapidly, becomes selfgravitating and collapses to higher and higher densities, presumably culminating in the formation of a star. The duration of this process scales with the dynamical time of the halo and is typically $\Delta z \sim 3-4$; during this time, a halo may increase its mass significantly through mergers and accretions. Therefore, neither the instantaneous halo mass nor the virial temperature is sufficient to describe the starforming properties of a halo; its merger history needs to be taken into account.

Gao et al. (2007) developed a simple model of Pop. III star formation, based on the merger trees of the parent haloes, which quite accurately matches the Pop. III star formation properties of all eight individual objects simulated in that study. Define the virial temperature $T_{\text {vir }}$ of a halo in terms of its circular velocity, $V_{200}$, at a radius $R_{200}$ (within which the mean density equals 200 times the critical density) as
$k_{\mathrm{B}} T_{\mathrm{vir}} \equiv \frac{1}{2} \mu m_{\mathrm{p}} V_{200}^{2}$,
where $k_{\mathrm{B}}$ is Boltzmann's constant, $\mu$ is the mean molecular weight ( $\mu=1.22$ for neutral $\mathrm{H}-\mathrm{He}$ admixture), and $m_{\mathrm{p}}$ is the hydrogen mass (e.g. White \& Frenk 1991). Once the virial temperature reaches $T_{\min }=1100 \mathrm{~K}$ (or, equivalently, the circular velocity exceeds $V_{200, \min }=4 \mathrm{~km} \mathrm{~s}^{-1}$ ), a star is assumed to form after a redshift delay of $\Delta z \sim 3-4$. We apply this model to identify which haloes form Pop. III stars, and when.

The first star may suppress or enhance star formation in neighbouring haloes through the combined effect of its ionizing and Lyman-Werner radiation (e.g. Haiman, Rees \& Loeb 1996; Machacek, Bryan \& Abel 2003; Yoshida et al. 2003; Wise \& Abel 2008; Whalen et al. 2008). The net effect is still unclear and so we introduce below a simplified feedback model based on the spatial clustering of the haloes.

### 3.2 Sites of the first galaxies

Once the virial temperature of the halo is high enough for atomic line cooling of gas to become important, $T_{\text {vir }} \sim 6000 \mathrm{~K}$, we assume that the nature of star formation changes. Rather than a single, massive
primordial star per halo, the cooling of the metal-enriched gas is assumed to lead to the formation of a normal stellar population with a range of masses. The depth of the potential well of these 'first galaxy' haloes is still so shallow that even a single supernova explosion can produce strong winds, as in the classic White \& Rees (1978) picture, leading to bursty behaviour which is difficult to model; see e.g. (Mori, Ferrara \& Madau 2002; Yoshida et al. 2007; Greif et al. 2008; Wise \& Abel 2008; Bromm et al. 2009). Whether it is simply the contribution of atomic lines to cooling that leads to the formation of lower mass stars alongside massive ones, or that of metals or dust (Schneider et al. 2006), or the change in the turbulent properties of the star-forming gas (Krumholtz \& McKee 2005), or all of the above, is presently unclear. Given these uncertainties, we adopt the simple criterion, $T_{\text {vir }} \geq 10^{4} \mathrm{~K}$, to separate haloes that form Pop. III stars from 'first galaxy' haloes that form stars with a broader IMF. Of course, if feedback from one halo strongly affects star formation in its surroundings, this distinction may be too simplistic.

## 4 FORMATION HISTORY AND CLUSTERING OF STAR FORMING HALOES

The general picture of early star formation sketched above changes dramatically as soon as the star-forming gas becomes ionized either through photons emitted by nearby stars or because the universe as a whole becomes ionized. The photoheating of the gas and the suppression of atomic cooling quenches star formation in dwarf galaxies with circular velocity, $V_{\max } \leq 25 \mathrm{~km} \mathrm{~s}^{-1}$ (e.g. Efstathiou 1992; Thoul \& Weinberg 1996; Gnedin 2000; Hoeft et al. 2006 Okamoto, Gao \& Theuns 2008). The Thomson scattering optical depth towards the last scattering surface, as determined from the


Wilkinson Microwave Anisotropy Probe (WMAP) data (Komatsu et al. 2009), suggests that the universe was reionized at a redshift, $z_{\mathrm{r}} \sim 10$. We will consider earlier times, $z>z_{\mathrm{r}}$, when the Universe was still mainly neutral, and star formation could take place in haloes with circular velocity as small as a few kilometres per second.

### 4.1 The first stars in galaxies like the Milky Way

Fig. 2 shows the evolution in the number of Aquarius progenitor dark matter haloes that, in the absence of feedback, would be able to form Pop. III stars. The numbers are calculated either using a simple virial temperature criterion (full lines) or the more detailed model of Gao et al. (2007; dashed lines). Star formation begins around $z \sim 40(z \sim 35$ in the Gao et al. 2007 model $)$, and the number of star-forming progenitor haloes increases very rapidly to reach $10^{3}$ at $z \sim 30$ and $10^{4}$ at $z \sim 15$; thereafter the numbers decrease as the haloes begin to merge. The halo-to-halo variation remains relatively small up to $z \sim 20$ but, by $z \sim 10$, it has increased to about a factor of 5 , with more massive Aquarius haloes tending to have more star-forming progenitors at $z \sim 10$.

The difference in the number of star-forming haloes predicted by the simple, $T_{\text {vir }}=1100 \mathrm{~K}$, cut and the Gao et al. (2007) model is large, of order a factor of 10 or more at $z \geq 15$. The reason for this difference is the delay (by $\Delta z \approx 3$ ) in the onset of star formation in the Gao et al. model at a time when the number of star-forming objects is rising extremely rapidly. Once the number of star-forming haloes reaches its maximum, the two models agree to within a factor of a few. The star formation rate is of order $\dot{N}_{\star} \approx 1 \mathrm{Myr}^{-1}$ at $z=$ 30 , increasing rapidly to reach a broad peak of $\dot{N}_{\star} \approx 10^{2} \mathrm{Myr}^{-1}$ at $z \sim 15$. According to the Gao et al. model, the first stars in a Milky Way sized halo appear around $z \sim 35$, later than in a


Figure 2. Pop. III star formation in galaxy halo progenitors as a function of redshift. Left-hand panel: cumulative number of progenitor haloes with virial temperature above 1100 K for each of the six Aquarius haloes (colour solid lines). The black dots show the extended Press-Schechter prediction which works well, but increasingly overestimates the number of haloes after $z \sim 15$. Gas in such haloes is hot enough for significant $\mathrm{H}_{2}$ formation. The dashed lines show the cumulative number of independent sites of Pop. III star formation according to the model of Gao et al. (2007) which, in addition to a virial temperature criterion, takes the merger history of the halo into account. This more stringent criterion reduces the number of forming stars; yet a Milky Way-type halo still had several hundreds of Pop. III star-forming progenitors at redshift $z=25$ and $\sim 10^{4}$ at $z=10$. The halo-to-halo variation is large, a factor of $\sim 5$ at $z=10$. The cumulative number of haloes drops after $z \sim 10$ as haloes begin to merge. Right-hand panel: the star formation rate. The rate increases from a few star forming events per Myr at $z=30$, to several tens at $z=20$ and changes little thereafter.
proto-cluster where star formation starts around $z \sim 47$ (Gao et al. 2007).

So far we have neglected potential feedback effects, arising from star formation, on neighbouring haloes which could, in fact, be quite severe. UV photons with energy, $h v>13.6 \mathrm{eV}$, emitted by massive stars may ionize and heat the gas in a neighbouring halo. Star formation may thus be quenched due to the suppression of atomic cooling and photoheating or altogether prevented as the halo loses gas through photoevaporation (e.g. Shapiro et al. 2004; Whalen et al. 2008; Okamoto \& Frenk 2009). On the other hand, $\mathrm{H}_{2}$ formation may be enhanced in photoionized gas, once the source of ionizing photons has faded (Haiman et al. 1996). These effects will be mostly restricted to the $\mathrm{H}_{\text {II }}$ region surrounding the star because of the high optical depth of ionizing radiation, except for the high-energy tail of the photon energy distribution.

Lyman-Werner photons with $11.2 \leq h \nu / \mathrm{eV} \leq 13.6$ may destroy the $\mathrm{H}_{2}$ coolant, also quenching or suppressing star formation. Most of the gas is optically thin to Lyman-Werner photons and so this 'sphere of influence' extends beyond the edge of the $\mathrm{H}_{\text {II }}$ region. However, some star-forming haloes may become dense enough to self-shield, even in the Lyman-Werner bands. Kinematical feedback from the star in the form of a stellar wind or supernova explosion, may also affect its surroundings.

Clearly, the details of these feedback effects are difficult to model accurately, and so the degree of suppression of star formation near a Pop. III star remains highly uncertain (see Yoshida et al. 2003, 2007; Ahn \& Shapiro 2007; O’Shea \& Norman 2007, 2008; Whalen et al. 2008; Wise \& Abel 2008, for recent discussions). In view of this, we have developed a simple model for feedback that takes into account the clustering of the haloes. We consider only radiative feedback and neglect external radiation from distant stars or galaxies. For each progenitor halo, we calculate the average number, $N(r)$, of neighbouring potentially star-forming haloes a function of separation, $r$. The number of neighbours, shown in Fig. 3, scales roughly as $N(r) \sim r^{2}$. At $z=30$, the typical pair separation is $r \sim$ $1 h^{-1} \mathrm{kpc}$ (note that here and below we give separations in proper, not comoving units).

A more direct measure of the redshift evolution of clustering is the mean separation of pairs, $N(1)$, and the mean distance to the 10th star-forming nearest neighbour halo, $N(9)$, as a function of
redshift, also shown in Fig. 3. Both curves fall rapidly with decreasing redshift as haloes begin to form in profusion, reach a minimum between $z=30$ and 20, and thereafter increasing slowly due to Hubble expansion of the proto-galactic region. On average, each potentially star-forming halo has another potentially star-forming halo within $0.5 h^{-1} \mathrm{kpc}$ at $z=30$, increasing slowly to $0.6 h^{-1} \mathrm{kpc}$ at $z=20$, and 10 others within $2 h^{-1} \mathrm{kpc}$ over the same redshift range.

To estimate the effect of feedback from ionizing radiation, we compare these numbers to the radius, $R$, of an $\mathrm{H}_{\text {II }}$ region in a uniform density medium,
$R=1.3\left(\frac{\dot{N}_{\gamma}}{10^{50} \mathrm{~s}^{-1}} \frac{\Delta t}{3 \mathrm{Myr}} \frac{100}{1+\delta}\right)^{1 / 3} \frac{10}{1+z} \mathrm{kpc}$,
around a source emitting ionizing photons at a rate, $\dot{N}_{\gamma}$, over a time interval, $\Delta t$. The medium is at an overdensity, $\delta$, has the cosmological baryon fraction, $\Omega_{\mathrm{b}} h^{2}=0.045$, and a hydrogen abundance of 0.75 by mass. Full numerical simulations find similar radii for the $H_{\text {II }}$ region (e.g. Abel, Wise \& Bryan 2007; Yoshida et al. 2007). The fact that $R$ is comparable to the mean interhalo separation implies that feedback from ionizing photons could indeed be rather important in quenching first star formation. The formation rate of first stars could then be significantly smaller than the no-feedback case depicted in Fig. 2.

### 4.2 The first galaxy haloes

Progenitors of Aquarius haloes first achieve a virial temperature, $T_{\text {vir }}>10^{4} \mathrm{~K}$, around $z \sim 25$; the abundance of such 'first galaxy' haloes rises rapidly to a few tens by $z \sim 18$ and reaches a broad peak of $\sim 300$ by $z=10$, as shown in Fig. 4. The scatter amongst the six Aquarius haloes is large. The rise in abundance is reasonably well described by the Press-Schechter formula, but this overestimates the number at $z=10$ by $\sim 50$ per cent. As was the case for Pop. III haloes discussed earlier, the first galaxy haloes in a proto-Milky Way object form at $z \sim 25$, substantially later than in a protocluster region where they form at $z \sim 40$ (Gao et al. 2004a). The more massive $z=0$ Aquarius haloes tend to have more first galaxy progenitors at $z \sim 10$.


Figure 3. Clustering of Pop. III star-forming progenitor haloes. Left-hand panel: mean number of progenitor halo pairs in Aq-A, as a function of proper separation at the three redshifts indicated in the panel. Right-hand panel: mean separation of progenitor haloes in each of the six Aquarius haloes. Each halo has one neighbour within the distance given by the solid line, and 10 neighbours within the distance given by the dashed lines. Star-forming haloes have relatively nearby companions, indicating that feedback effects could be important (see text). The linear rise in separation between substructures below $z \sim 20$ is because the proto-halo region is still expanding with the Hubble flow at this early time.


Figure 4. The abundance of haloes hosting 'first galaxies' (virial temperature $T_{\text {vir }}>10^{4} \mathrm{~K}$ ) as a function of redshift for the six Aquarius haloes (colours are the same as in Fig. 1). Dashed lines are the prediction from extended Press-Schechter theory. These haloes start to appear around $z \sim$ 25 and their abundance rises rapidly to reach a broad peak of 200-300 haloes by $z \sim 10$. Progenitors of haloes more massive at $z=0$ tend to have a higher abundance of first galaxy haloes at all $z$.

As before, we characterize the clustering of haloes that can cool through atomic processes by the number of neighbours, $N(r)$, at distance $r$. As shown in Fig. 5, N(r) is again approximately a power-law, $N(r) \propto r^{2}$. At $z=10$, a first galaxy halo has a neighbouring first galaxy halo within $\sim 6 h^{-1} \mathrm{kpc}$ and $\sim 10$ within $\sim 25 h^{-1} \mathrm{kpc}$. The halo-to-halo scatter in clustering properties is large at early redshift $z \sim 20$ (Fig. 5, right-hand panel), but as more haloes form, it decreases; the typical separation reaches $r \sim 6 h^{-1} \mathrm{kpc}$ at $z=10$. Consequently, the ionized regions formed by star formation around such


Figure 6. Fraction of first galaxies not affected by neighbouring first galaxies as a function of redshift, if the radius of influence of the feedback is $R=$ 10,5 or $1 h^{-1} \mathrm{kpc}$ (dashed, dotted, and solid lines, respectively). For the smaller value of $R$, feedback has little or no effect, but for larger $R$, feedback may decrease the number of first galaxies considerably, up to a factor of $\sim 2$.
first galaxies need not be very large, of order a few $h^{-1} \mathrm{kpc}$ before $\mathrm{H}_{\text {II }}$ regions percolate across a proto-Milky Way galaxy by $z=10$.

Feedback from star formation in a first galaxy may potentially affect a neighbouring halo. Fig. 6 displays the fraction of haloes that would be affected depending on the value of the radius, $R$, of influence of the feedback, when taking clustering into account. For $R=1 h^{-1} \mathrm{kpc}$, feedback has no effect, but for $R=5 h^{-1} \mathrm{kpc}, 20-$ 30 per cent of potential first galaxy haloes could be affected, rising to $40-50$ per cent for $R=10 h^{-1} \mathrm{kpc}$.


Figure 5. Clustering of 'first galaxy' progenitor haloes (virial temperature, $T_{\text {vir }}>10^{4} \mathrm{~K}$ ). Left-hand panel: mean number of progenitor halo pairs in Aq-A, as a function of proper separation, at the redshifts indicated in the panel. Right-hand panel: redshift evolution of the mean separation between pairs of haloes with $T_{\text {vir }}>10^{4} \mathrm{~K}$. By $z=10$, the mean separation between first galaxy haloes is $\sim 6 h^{-1} \mathrm{kpc}$ and each halo has on average another 10 haloes within $\sim 20 h^{-1} \mathrm{kpc}$. The typical distance to a neighbouring halo has a large scatter amongst realizations, reflecting the fact that these haloes only just began to form at these early times.

## 5 RELICS OF EARLY STAR FORMATION

### 5.1 Relics of the first stars

If, as seems likely, the first stars that form in a CDM universe are massive, then only their dark remnants will remain in the Milky Way today. However, evidence for their existence may be hidden in the anomalous abundance patterns of long-lived second generation stars that formed nearby, in gas predominantly enriched by Pop. III stars (e.g. Beers \& Christlieb 2005; Rollinde et al. 2009); we will call such stars 'first star relics'. Where are these fossils of primordial star formation to be found today? To answer this question, we make use of the merger history of the haloes hosting primordial stars which is readily available in the simulations.

It seems reasonable to assume that feedback from Pop. III stars will have prevented the gas enriched by them from forming further stars until it is accreted later into a first galaxy halo where it can cool by atomic processes (see e.g. the simulations of Wise \& Abel 2008). The earliest generation of stars formed in such a first galaxy may then have the peculiar abundance pattern characteristic of Pop. III nucleosynthesis. However, stars that form later may have been enriched by the elements produced by the previous generation of relatively metal-rich stars, so that eventually the net abundance pattern loses its characteristic Pop. III star signature. To implement this idea, we proceed as follows. We assume that each first galaxy halo contains a fixed total mass of 'first star relics' - stars that form in an environment enriched solely by truly primordial stars independent of redshift. To trace the location of such stars at later times, we tag the $N=100$ most bound particles at the time the virial temperature of the halo first exceeds $T=10^{4} \mathrm{~K}$. ${ }^{5}$ This assumes that these second-generation stars form in the centres of such darkmatter haloes. Once a halo has started forming stars, it will grow in mass, and may merge with other haloes. The number of first star relics in a halo will only change if it merges with a halo that contains its own population of first star relic stars. We continue tagging first star relics in haloes that reach the threshold $T_{\text {vir }}$ until $z=10$, after which we assume that reionization of the Universe evaporates all minihaloes.

In summary, we identify the epoch when a halo is first capable of sustaining gas that can cool through atomic processes and tag its 100 most bound particles as first star relics, until $z=10$. We can then investigate the spatial distribution of these first star fossils at any later epoch by tracing the tagged particles. The location of the first star relics today is illustrated in Fig. 7 where, for clarity, we show only a fraction of the stars. The image shows that most of the first star relics end up in the central regions of the halo, but some survive inside subhaloes.

The visual impression gained from Fig. 7 is quantified in Fig. 8 which shows that the distribution of the first star relics today (which is similar in all six Aquarius haloes) is expected to be much more concentrated than that of the dark matter. 50 per cent of these first star relics lie within $20 h^{-1} \mathrm{kpc}$ of the centre and $\sim 10$ per cent lie inside what would be the galactic bulge, at $r<2 h^{-1} \mathrm{kpc}$. In contrast, only $\sim 10$ per cent of the dark matter lies within $20 h^{-1} \mathrm{kpc}$, and only about 0.1 per cent is at $r<1 h^{-1} \mathrm{kpc}$. Even though the stars in our simulations are already very concentrated, earlier models of the remnants of Pop. III stars (White \& Springel 2000; Diemand, Madau \& Moore 2005) suggested they should be even more concentrated,

[^3]

Figure 7. Projected distribution at $z=0$ of first star relics (red), compared to that of the dark matter for the Aq-A-2 halo. A significant fraction of the stars lie in the central part of the main galaxy, but some end up in dark matter subhaloes. The image is 1080 kpc on a side, approximately twice the diameter of the virialized dark matter halo.


Figure 8. Cumulative distribution of second generation, first star relics, stars at redshift $z=0$ for all six Aquarius haloes (colour lines), compared to the dark matter profile for the Aq-A halo (dashed black line).
with almost all of them lying in the bulge where they would be very hard to detect.

Although most of the first star relics reside in the central parts of the main halo, a significant fraction end up in dark matter subhaloes. This is interesting because it may be easier to detect such unusual stars in a nearby dwarf galaxy than to hunt for them in the crowded surroundings of the Milky Way bulge.


Figure 9. Left-hand panel: cumulative mass function at $z=0$ of 'first galaxy' haloes (i.e. bound substructures which had a progenitor at $z>10$ with $T_{\text {vir }}>$ $10^{4} \mathrm{~K}$ ), for the Aq-A-1 (solid line) and the $8 \times$ lower resolution Aq-A-2 (dashed line) simulations. Numerical convergence is very good above 100 particles (corresponding to $10^{6} h^{-1} \mathrm{M}_{\odot}$ in Aq-A-2). For comparison, the dashed-dotted line is the $z=0$ mass function of all gravitationally bound substructures in Aq-A-1. Right-hand panel: as the left-hand panel, but for the maximum of the circular velocity curve, $V_{\max }$.

### 5.2 Relics of the first galaxies

In this section, we investigate the fate of first galaxy haloes. As discussed in Section 4.2, these are dark matter haloes which formed before $z=10$ and have $T_{\text {vir }}>10^{4} \mathrm{~K}$. We are particularly interested in descendants which today are to be found within the virial radius of the parent halo. To establish the range of descendant masses which are reliably simulated, we begin by carrying out a convergence test of the present-day mass function.

We compare results from the 1.4 billion particle Aq-A-1 simulation with those from the Aq-A-2 simulation which has 8 times poorer resolution. (All six Aquarius haloes have been simulated at the resolution of the Aq-A-2 halo, see Table 1.) The cumulative mass function of first galaxy haloes that survives to $z=0$, shown in Fig. 9, shows excellent numerical convergence above a mass of $10^{6} \mathrm{~h}^{-1} \mathrm{M}_{\odot}$, corresponding to 100 particles in Aq-A-2, and to a maximum circular velocity of $V_{\max } \sim 5 \mathrm{~km} \mathrm{~s}^{-1}$. We therefore adopt $N_{p}=100$ as the resolution limit of the simulations.

Aq-A-2 has 76 surviving first galaxy haloes with $N_{p}>100$ $\left(M>10^{6} h^{-1} \mathrm{M}_{\odot}\right)$. Aq-A-1 has 88 survivors with $N_{p}>100$, corresponding to $M>10^{5} h^{-1} \mathrm{M}_{\odot}$ and $V_{\max } \sim 2 \mathrm{~km} \mathrm{~s}^{-1}$. Thus, Aq-A-1 resolves dark matter subhaloes with circular velocities lower than the stellar velocity dispersions of the smallest dwarf galaxy satellites of the Milky Way discovered to date (e.g. Simon \& Geha 2007).

### 5.2.1 Abundance of the first galaxies and their descendants

The mass function at $z=10$ of those 'first galaxy' haloes, which ended up inside the virial radius $\left(\sim 170 h^{-1} \mathrm{kpc}\right.$ see Table 1$)$ of the main halo today, and the corresponding maximum circular velocity function are shown in the top two panels of Fig. 10 for all Aquarius haloes. The most massive of these subhaloes has $M \sim$ $10^{10} h^{-1} \mathrm{M}_{\odot}$, and circular velocity, $V_{\max } \sim 100 \mathrm{~km} \mathrm{~s}^{-1}$. There are typically $\sim 10$ subhaloes with $M>10^{9} h^{-1} \mathrm{M}_{\odot}$ (corresponding to $V_{\max }>40 \mathrm{~km} \mathrm{~s}^{-1}$ ) and 100 with $M>10^{8} h^{-1} \mathrm{M}_{\odot}$ (corresponding to $V_{\max }>20 \mathrm{~km} \mathrm{~s}^{-1}$ ).

The lower panels of Fig. 10 give the present-day mass and $V_{\max }$ distributions of the descendants of the first galaxy haloes illustrated in the top panels. Every halo contains $\sim 80$ first galaxy descendants with mass $M>10^{6} h^{-1} \mathrm{M}_{\odot}\left(\right.$ corresponding to $V_{\max }>5 \mathrm{~km} \mathrm{~s}^{-1}$ )
that survived since $z=10$. Note that there is a large variation in the number of survivors in the different Aquarius simulations, with the more massive haloes harbouring more massive substructures on average. The mass of the most massive $z=0$ remnant varies from $3 \times 10^{9}$ to nearly $10^{11} h^{-1} \mathrm{M}_{\odot}$.

The lower right panel in Fig. 10 shows that, at $z=0$, the Aq-A-2 halo contains over 60 first galaxy remnant subhaloes with $V_{\max }>$ $10 \mathrm{~km} \mathrm{~s}^{-1}$ inside its virial radius. This is a factor of a few larger than the number of classical satellites of the Milky Way. However, the total (i.e. not just descendants of first galaxies) number of subhaloes with $V_{\max }>10 \mathrm{~km} \mathrm{~s}^{-1}$ at $z=0$ is $\sim 400$, as can be seen from the right-hand panel of Fig. 9. By contrast, for $V_{\max }>22 \mathrm{~km} \mathrm{~s}^{-1}$ (corresponding to $M \gtrsim 3 \times 10^{8} h^{-1} \mathrm{M}_{\odot}$ ), the number of surviving first galaxy haloes equals the total number of haloes. From smoothed particle hydrodynamics ( SPH ) simulations of Aquarius haloes, Okamoto et al. (2009) found that all subhaloes with $V_{\max }=$ $23.5 \mathrm{~km} \mathrm{~s}^{-1}$ host a satellite with $V$-band luminosity, $L_{V}>2.5 \times$ $10^{5} \mathrm{~L}_{\odot}$, whereas below that value a diminishing fraction of subhaloes manage to make a visible satellite. It is therefore tempting to identify these more massive first galaxy remnants with bright satellite galaxies and to conclude that these must have formed before $z=10$.

The stellar content of a present-day subhalo is thought to be more tightly connected to its dark matter mass at the time when it was first accreted into the main halo than to its current dark matter mass (e.g. Gao et al. 2004a,b; Libeskind et al. 2005). This is because substructures may lose a significant fraction of their dark matter once they have been accreted into the main halo, whereas the more tightly bound stellar content is stripped to a lesser extent. Fig. 11 shows the redshift when first galaxy haloes surviving to the present were accreted by the main halo. The median accretion redshift varies between 2 and 3.5 in the different Aquarius haloes. Less than 1 per cent of the haloes were accreted before redshift 9 and less than 10 per cent before redshift 7 . Ninety per cent fell in before $z=1$.

The mass and maximum velocity functions at the time of accretion are shown in the middle panels of Fig. 10. Approximately half of the surviving substructures had a mass, $M>5 \times 10^{8} h^{-1} \mathrm{M}_{\odot}$ $\left(V_{\max }>30 \mathrm{~km} \mathrm{~s}^{-1}\right)$ at infall, compared to their present-day values of $M>1 \times 10^{8} h^{-1} \mathrm{M}_{\odot}\left(V_{\max }>15 \mathrm{~km} \mathrm{~s}^{-1}\right)$. Therefore such haloes have lost typically 80 per cent of their mass, and their circular velocity has correspondingly decreased by a factor of $\sim 2$.


Figure 10. Statistics of first galaxy haloes in all six Aquarius haloes (the colour scheme is as in Fig. 1) at $z=10$ (top), when they are accreted by the main halo (middle), and at $z=0$ (bottom). The left-hand panels show cumulative mass functions and the right-hand panels show cumulative $V_{\text {max }}$ distributions. There is a large variance between the different Aquarius haloes at all redshifts. For example, the mass of the most massive $z=0$ remnant varies between $3 \times$ $10^{9} h^{-1} \mathrm{M}_{\odot}$ and nearly $10^{11} h^{-1} \mathrm{M}_{\odot}$. The more massive Aquarius haloes tend to have the more massive substructures. Comparing the $z=0$ masses with those at infall or at $z=10$ demonstrates that most substructures lose a considerable fraction of their mass by the present.

As discussed earlier, the sites of first galaxy formation are highly clustered and, as a result, feedback may have had an important effect on the number of first galaxies at $z=10$. However, it is likely that feedback will have not affected the number of first galaxy remnants at $z=0$ since it only influences nearby haloes which are eventually likely to merge. So, although the stellar properties of these substructures may have been affected by feedback at $z>$ 10 , the number of remnants is unlikely to depend on the details of this process. As an example, our most extreme feedback model suppresses all star formation within $10 h^{-1} \mathrm{kpc}$ from a first galaxy, thereby decreasing the number of sites by 30 per cent. Yet, the number of first galaxy remnants in this model is the same as that of the no-feedback model.

### 5.3 Spatial distribution of first galaxy remnants

The remnants of the first galaxies are a small minority amongst surviving subhaloes. For example, of the $\sim 10^{3}$ surviving subhaloes within $R=20 h^{-1} \mathrm{kpc}$ in Aq-A-1, only $\sim 10$ are first galaxy rem-
nants. Their predicted spatial distribution is a useful pointer as to whether observed halo objects could, in fact, be first galaxy remnants.

The top left panel of Fig. 12 shows the cumulative number of first galaxy remnants as a function of distance in both Aq-A-1 and Aq-A-2. Both simulations have about 100 remnants within the virial radius but in the inner part of the halo there are more remnants in Aq-A-1 than in Aq-A-2. The deficit in Aq-A-2 is a resolution effect. As can be seen in Fig. 9, the smallest resolved haloes in Aq-A-2 have $V_{\text {max }}=5 \mathrm{~km} \mathrm{~s}^{-1}$ whereas in Aq-A-1 they have $V_{\text {max }}=$ $2 \mathrm{~km} \mathrm{~s}^{-1}$. These small haloes are missing from the central parts of Aq-A-2. Indeed, for $V_{\text {max }}>5 \mathrm{~km} \mathrm{~s}^{-1}$, the distributions in the two simulations agree within the errors, as may be seen by comparing the dashed and dotted lines.

The bottom left panel in Fig. 12 shows that the abundance of remnants at a given radius varies by about a factor of 2 between realizations. Five of them have no first galaxy remnants closer to the centre than $10 h^{-1} \mathrm{kpc}$, but one of them (Aq-B), has five, including one at only $3.5 h^{-1} \mathrm{kpc}$ from the centre. The top right panel of


Figure 11. Cumulative fraction of first galaxy haloes that were accreted before a given redshift and survive until $z=0$. The different lines correspond to the six Aquarius haloes. Typically 50 per cent of haloes fell in before $z=3$.

Fig. 12 shows that the distribution of first galaxy remnants is more centrally concentrated than the overall distribution of all surviving subhaloes with $V_{\max }>5 \mathrm{~km} \mathrm{~s}^{-1}$. For example, 50 per cent of the first galaxy remnants are within $50 h^{-1} \mathrm{kpc}$ of the centre, whereas 50 per cent of the subhalo population is within twice that distance. In the outer parts of the halo ( $R \gtrsim 40 h^{-1} \mathrm{kpc}$ ), the distribution of first galaxy remnants tracks that of the dark matter but, in the inner parts ( $R \lesssim 30 h^{-1} \mathrm{kpc}$ ) it is shallower.

Typically, around 30 first galaxy halo remnants end up in the inner $35 h^{-1} \mathrm{kpc}$ of the halo. In the Milky Way there are six known satellites within this distance which, when allowing for the partial coverage of observational searches for satellites, yields an expected number of $\sim 25$ dwarfs (Tollerud et al. 2008). The cumulative radial distribution of the 24 known Milky way satellites, normalized to the total number within $120 h^{-1} \mathrm{kpc}$, is plotted in the lower right panel of Fig. 12 and is interestingly similar to the distribution of the first galaxy remnants. Detailed treatments of the satellite populations in the Aquarius haloes may be found in Cooper et al. (2009), Okamoto \& Frenk (2009) and Okamoto et al. (2009).

Various physical properties of the first galaxy remnants: mass, $V_{\text {max }}$, half-mass radius, and mean density, $\rho$, within the half mass radius are plotted in Fig. 13 as a function of distance from the centre in Aq-A-1 and Aq-A-2. The numerical convergence of these properties is very good. As pointed out by Springel et al. (2008a,b), and apparent in the figure, many of the substructures at the two resolutions can be matched spatially. As noted earlier, haloes with $V_{\text {max }}<5 \mathrm{~km} \mathrm{~s}^{-1}$ are resolved in Aq-A-1, but not in Aq-A-2. This limit approximately corresponds to a mass of $10^{6} h^{-1} \mathrm{M}_{\odot}$. Above the resolution limit of Aq-A-2 the results for the two simulations agree remarkably well.
Within $\sim 80 h^{-1} \mathrm{kpc}$ from the centre, there is a large scatter in the properties of the remnants. Further out, there is a clear increase in mass and $V_{\text {max }}$ with radius, reminiscent of the trends found by Springel et al. (2008a,b) for the population of subhaloes as a whole. The half-mass radius of the remnants increases systemati-
cally with halocentric distance, from about 100 pc in the inner parts to $10 h^{-1} \mathrm{kpc}$ in the outer parts. The central dark matter densities of the remnants are correspondingly larger in the inner parts. (The apparent convergence of the central density in Aq-A-2 to a constant value at small distances is purely a resolution effect.) The smallest remnants have masses and $V_{\max }$ values similar to those of globular clusters.

## 6 SUMMARY AND DISCUSSION

We have used the set of six high resolution cosmological simulations of galactic haloes from the Aquarius Project Springel et al. (2008a,b) to investigate the formation and fate of haloes capable of hosting the first stars and the first galaxies. Our main results may be summarized as follows.

### 6.1 First stars

(i) The first haloes with virial temperature high enough to form stars, according to the model of Gao et al. (2007), appear at redshift $z=35$; the number of such haloes increases exponentially to $\sim 2 \times$ $10^{3}$ by $z=20$ and to $\sim 10^{4}$ by redshift $z=10$.
(ii) First star haloes are very highly clustered. The mean interhalo separation increases, in physical units, from $\sim 0.5 h^{-1} \mathrm{kpc}$ at $z=25$ to $\sim 1 h^{-1} \mathrm{kpc}$ by $z=10$. Thus, if the $\mathrm{H}_{\text {II }}$ region created by a Pop. III star is larger than a few hundred parsecs, then feedback due to ionizing radiation is likely to have had a large impact on the number of first stars in the proto-galaxy.
(iii) The spatial distribution of the remnants of primordial stars today, as traced by the most strongly bound dark matter particles in the original halo, is more concentrated than that of the dark matter, and scales as $n(R) \sim R^{-2.9}$ with distance, $R$, from the Galactic Centre. A few percent of the remnants lie in the galactic bulge, $\sim 10$ per cent in the central $10 h^{-1} \mathrm{kpc}$ of the halo, and $\sim 50$ per cent in the inner $30 h^{-1} \mathrm{kpc}$ of the galactic halo. A significant fraction is associated with subhaloes, suggesting that the remnants of some of the first stars could be found today in satellite galaxies, confirming earlier conjectures (e.g. Ricotti \& Gnedin 2005; Muñoz et al. 2009).

### 6.2 First galaxies

(i) The first pre-galactic haloes capable of hosting gas that could undergo atomic hydrogen cooling appear at redshift $z \sim 25$; their number increases to $\sim 100$ by redshift $z=20$ and to $\sim 300$ by at redshift $z=10$, with substantial scatter from halo to halo. The mean interhalo separation is $4 h^{-1} \mathrm{kpc}$ at redshift $z \sim 20$, and does not evolve much until $z=10$. Early pre-ionization by UV photons produced in the first galaxies may have had a significant effect on their numbers at $z=10$, although the total number of remnants left over by $z=0$ is unaffected because most haloes that could plausibly suppress each other's star formation merge by $z=0$ anyway.
(ii) The majority of the surviving first galaxy halo remnants were accreted into the main halo early. 50 per cent fell in before $z=3.5$ and 90 per cent before $z=1$.
(iii) About 80 first galaxy halo remnants end up within the virial radius ( $\sim 160 h^{-1} \mathrm{kpc}$ ) of a galaxy like the Milky Way as satellites with dark matter mass above $10^{6} h^{-1} \mathrm{M}_{\odot}$ (corresponding to a maximum velocity $V_{\max } \sim 5 \mathrm{~km} \mathrm{~s}^{-1}$ ). More than half of them had a mass above $5 \times 10^{8} h^{-1} \mathrm{M}_{\odot}\left(V_{\max } \sim 20 \mathrm{~km} \mathrm{~s}^{-1}\right)$ before they were accreted by the main progenitor. Many are heavily stripped after infall.


Figure 12. Left-hand panels: present-day cumulative number of first galaxy halo remnants (i.e. substructures whose progenitors had $T_{\text {vir }}>10^{4} \mathrm{~K}$ at $z=10$ ), as a function of distance, $R$, from the centre of the main halo. In the top panel, the solid line shows all haloes in Aq-A-1, the thick dotted line haloes with $V_{\max }>5 \mathrm{~km} \mathrm{~s}^{-1}$ in Aq-A-1 and the dashed lines all haloes in Aq-A-2. Haloes with $V_{\max }<5 \mathrm{~km} \mathrm{~s}^{-1}$ are not resolved in Aq-A-2; for $V_{\max }>5 \mathrm{~km} \mathrm{~s}^{-1}$ the distributions in the two simulations agree within the noise. The thin dotted lines shows the cumulative number of all substructures with $V_{\text {max }}>2 \mathrm{~km} \mathrm{~s}^{-1}$ which is almost two orders of magnitude higher than the number of first galaxy remnants. The bottom panel shows results for all five level-2 haloes. Top right panel: as the left-hand panels, but showing the cumulative fraction normalized to the number within the virial radius, for Aq-A-1 (thin solid line) and Aq-A-2 (dashed line). Bottom right panel: as the left-hand panels, but showing the cumulative fraction within $R=120 h^{-1} \mathrm{kpc}$ for all five Aquarius haloes. The black solid lines in the top and bottom panels indicate the dark matter profile and the dotted line in the top panel the radial profile of all substructures. The pentagons in the lower panel correspond to known Milky Way satellites. Their radial distribution resembles that of the outer first galaxy remnants.
(iv) The spatial distribution of the first galaxy halo remnants today follows that of the dark matter in the outer parts of the galactic halo, but is much less concentrated towards the centre. The remnants, however, are significantly more concentrated than the substructure population as a whole. A typical Aquarius halo has 20 first galaxy remnants within $30 h^{-1} \mathrm{kpc}$ of the centre with a velocity dispersion of few kilometres per second, similar to the faintest Milky Way satellites known. Of course, the presence of the disc may have affected the survival of early substructures.
(v) The mass, $V_{\max }$, and half-mass radius of the first galaxy remnant haloes increase with radius. The largest, most massive haloes are typically found beyond $100 h^{-1} \mathrm{kpc}$ of the centre. The scatter in these trends increases substantially at smaller radii. At $r<100 h^{-1} \mathrm{kpc}$, the median mass of the remnant subhaloes is $\sim 10^{7} h^{-1} \mathrm{M}_{\odot}$ and the median $V_{\text {max }}$ is $\sim 7 \mathrm{~km} \mathrm{~s}^{-1}$.

Our results suggest the following history of early star formation in a galaxy like the Milky Way. Star formation begins at around $z=35$ in mini-haloes and the number of sites where these Pop. III stars can form rapidly builds up to thousands or even tens of thousands depending on the efficiency with which energy from one star prevents neighbouring haloes from making their own star. Since these potential sites are strongly clustered, it is to be expected that many of them will remain barren for some time. A second generation of stars (first star relics) forming near the first stars may
be long-lived and their remnants would be found primarily in the inner parts of the galaxy today but also inside satellite galaxies, where they could be identified though their anomalous metallicity patterns.

Following this episode of metal-free star formation, the first 'galaxies' begin to form around $z=25$. The presence of local radiation sources, enrichment of gas by heavy elements, and possibly mechanical feedback from the first supernovae, may all contribute to a change in the stellar initial mass function, leading to the formation of the first low mass stars. A significant fraction of the haloes that hosted these first galaxies are destroyed by mergers or stripping and their stellar remnants could have contributed to the stellar halo (Cooper et al. 2009). Over 20 per cent of the primordial fossils survive as bound structures until the present and some could have developed into satellite galaxies. Our simulations therefore suggest that some of the Milky Way's dwarf satellites should contain a small fraction of the oldest stars that formed during the early stages of formation of the Milky Way.

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Figure 13. Mass, maximum circular velocity, $V_{\max }$, half-mass radius, and mean density within the half-mass radius, $\rho$, at $z=0$ of first galaxy haloes as function of their distance to the centre of the main halo: high resolution simulation Aq-A-1 (open circles), and the lower resolution simulation of the same halo, Aq-A-2 (filled circles). Resolution effects are notable inside $\sim 40 h^{-1} \mathrm{kpc}$ where there are more haloes at higher resolution. More massive haloes tend to be located at $r>100 h^{-1} \mathrm{kpc}$. At smaller $R$ there is a large scatter in halo properties, but a notable tendency towards increased subhalo concentration.

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[^1]:    ${ }^{1}$ We will refer to nearly primordial stars contaminated only by metals from the first stars as 'first star relics'.

[^2]:    ${ }^{2}$ http://www.mpa-garching.mpg.de/aquarius/
    ${ }^{3} \mathrm{http}: / /$ www.mpa-garching.mpg.de/galform/virgo/millennium/
    ${ }^{4}$ http://www.mpa-garching.mpg.de/galform/millennium-II/

[^3]:    ${ }^{5}$ We verified that our final results do not depend strongly on the arbitrary choice of $N$.

