

The effect of violent star formation on the state of the molecular gas in M 82

A. Weiß¹, N. Neininger¹, S. Hüttemeister¹, and U. Klein¹

Radioastronomisches Institut der Universität Bonn (RAIUB), Auf dem Hügel 71, 53121 Bonn, Germany

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Abstract. We present the results of a high angular resolution, multi-transition analysis of the molecular gas in M 82. The analysis is based on the two lowest transitions of ^{12}CO and the ground transition of the rare isotopes ^{13}CO and C^{18}O measured with the PdBI, the BIMA array and the IRAM 30 m telescope. In order to address the question of how the intrinsic molecular cloud properties are influenced by massive star formation we have carried out radiative transfer calculations based on the observed CO line ratios. The calculations suggest that the kinetic temperature of the molecular gas is high in regions with strong star formation and drops towards the outer molecular lobes with less ongoing star formation. The location of the highest kinetic temperature is coincident with that of the mid infrared (MIR) peaks which trace emission from hot dust. The hot gas is associated with low H_2 densities while the cold gas in the outer molecular lobes has high H_2 densities. We find that CO intensities do not trace H_2 column densities well. Most of the molecular gas is distributed in a double-lobed distribution which surrounds the starburst. A detailed analysis of the conversion factor from CO intensity to H_2 column density shows that X_{CO} depends on the excitation conditions. We find $X_{\text{CO}} \sim T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2}$, as expected for virialized clouds.

Key words. ISM: evolution – ISM: molecules – ISM: structure – galaxies: individual: M 82 – galaxies: ISM – galaxies: starburst

1. Introduction

M 82 is regarded as the archetypical starburst galaxy (Rieke et al. 1980). Its distance of only 3.9 Mpc (Sakai & Madore 1999) makes M 82 an excellent laboratory for studying the relevant physical processes connected with starburst activity in detail. The central few hundred parsecs of this galaxy are heavily obscured by dust and gas which hides the central starburst region against direct observations at optical wavelengths. Evidence for the strong star-forming activity in the central region comes from radio (e.g. Kronberg et al. 1985; Wills et al. 1999) and infrared observations (e.g. Telesco & Gezari 1992) and also from the prominent bipolar outflow visible in $\text{H}\alpha$ (e.g. Bland & Tully 1988; McKeith et al. 1995; Shopbell & Bland-Hawthorn 1998) and X-rays (e.g. Bregman et al. 1995). The massive star formation (SF) is believed to be fueled by the large amount of molecular gas which is present in the center of M 82.

On the other hand, SF affects the distribution, kinematics and physical conditions of the surrounding interstellar medium (ISM). Early studies of the distribution of the molecular gas in M 82 unveiled a double-lobed circumnuclear distribution of CO which was interpreted as a molecular torus with a depletion of molecular gas in the central region (Nakai et al. 1987). More recent high-resolution studies by Shen & Lo (1995) using BIMA and Neininger et al. (1998) using the IRAM interferometer at Plateau de Bure (PdBI) showed a third molecular peak 65 pc west of the $2.2 \mu\text{m}$ nucleus (Dietz et al. 1986). Using these high-resolution CO maps Weiß et al. (1999) identified an expanding superbubble in the molecular gas of M 82 which links the triple peak CO distribution and its disturbed velocity field to the prominent outflow visible in $\text{H}\alpha$ and X-rays.

Multi-transition analyses of molecular emission lines (CO, CS, HCN) showed that the starburst also affects the physical conditions of the molecular gas (Wild et al. 1992; Henkel & Bally 1985; Brouillet & Schilke 1993). A large fraction of the molecular gas is concentrated in warm ($T_{\text{kin}} = 50 \text{ K}$) and dense ($n(\text{H}_2) = 10^4 \text{ cm}^{-3}$) clouds

Send offprint requests to: A. Weiß,
e-mail: aweiss@astro.uni-bonn.de

(Wild et al. 1992; Güsten et al. 1993). In a recent study Mao et al. (2000) analyzed CO mm and sub-mm emission lines in M 82 to investigate the physical properties of the molecular clouds. They conclude that the bulk of CO emission arises from photon-dominated regions (PDRs) while tracers of high-density gas like CS and HCN are less affected by the strong UV radiation from massive stars.

Even though these studies already provided a good global picture of the physical conditions of the molecular gas in M 82, no detailed high-resolution study exists so far that allows to resolve variations of the excitation conditions of the molecular gas over the central part of M 82. In this paper we present the results of a high angular resolution, multi-transition CO analysis and compare the intrinsic gas properties with observations of high-level star formation. In Sect. 2 we briefly summarize our observations and the data reduction. In Sect. 3 we describe the main results including a description of the CO morphology and kinematics, the CO line ratios, results from the LVG calculation and on X_{CO} . In Sect. 4 we compare our results to previous studies. Section 5 summarizes our conclusions.

2. Observations

2.1. PdBI observations

We have used the PdBI to observe the $^{12}\text{CO}(J = 2 \rightarrow 1)$ ($\nu_{\text{obs}} = 230.361$ GHz) and $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ ($\nu_{\text{obs}} = 109.698$ GHz) emission lines in the central region of M 82. The observations were carried out in April 1997. Due to the dual frequency setup of the PdBI we were able to observe both emission lines simultaneously. The observations were carried out in mosaic mode with seven pointings covering the central kpc of M 82. The central pointing was centered on the $2.2 \mu\text{m}$ nucleus at $\alpha = 09^{\text{h}}55^{\text{m}}51^{\text{s}}.94$, $\delta = 69^{\circ}40'47.14''$ (J2000.0) (Dietz et al. 1986). The other pointings were shifted with respect to the central position by $(\alpha, \delta) = (-30'', -8'')$, $(-20'', -6'')$, $(-10'', -4'')$, $(10'', 4'')$, $(20'', 8'')$, $(30'', 10'')$ which ensured sufficient overlap of the observed fields at 230 GHz. The primary beam of the PdBI is $22''$ and $45''$ at 230 GHz and 109 GHz respectively. The observations were carried out in the DC2 antenna configuration with baselines ranging from 24 m to 176 m leading to a synthesized beam of $3.8'' \times 3.5''$ at 109 GHz and $1.5'' \times 1.4''$ at 230 GHz.

The $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ data were recorded using two correlator units leading to a total bandwidth of 780 km s^{-1} with 6.83 km s^{-1} resolution. For the $^{12}\text{CO}(J = 1 \rightarrow 0)$ transition we used four correlator units which resulted in a total bandwidth of 390 km s^{-1} and a velocity resolution of 3.25 km s^{-1} . The $^{12}\text{CO}(J = 2 \rightarrow 1)$ emission line was observed in the lower sideband of the 230 GHz, the $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ emission line in the upper sideband of the 109 GHz receiver. The flux and complex bandpass calibration was determined by observing

3C 273 and MWC 349. The nearby calibrator 0836+710 was used as a secondary amplitude and phase calibrator. The seven fields were combined in a mosaic and subsequently CLEANed using the MAPPING procedure of the GILDAS software package. This yields a roughly constant sensitivity along the major axis of M 82 with an rms noise of 6 mJy/beam at 109 GHz and 30 mJy/beam at 230 GHz. For both data sets the channels with $v_{\text{lsr}} > 385 \text{ km s}^{-1}$ and $v_{\text{lsr}} < 30 \text{ km s}^{-1}$ were used to generate a continuum map at 109 GHz and 230 GHz. The continuum emission was subtracted from both emission line data cubes.

2.2. IRAM 30 m telescope observations

In addition to the high-resolution CO data we observed the $^{12}\text{CO}(J = 1 \rightarrow 0)$, $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $^{13}\text{CO}(J = 1 \rightarrow 0)$ emission lines with the IRAM 30 m telescope in on-the-fly mode. The observations covered an area of $3' \times 3'$ centered on the $2.2 \mu\text{m}$ nucleus. The $^{12}\text{CO}(J = 1 \rightarrow 0)$ observations were carried out in Nov. 1997. The $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $^{13}\text{CO}(J = 1 \rightarrow 0)$ data were observed in Nov. 1997, Dec. 1998 and June 1999. For all observations we used the same observing procedure: The scanning velocity was $2''/\text{s}$ and the readout sampling 1 s leading to a spatial separation of $2''$ between individual spectra in scanning direction. The spatial separation between individual scans was $4''$. Thus each on-the-fly map was sampled on a $2'' \times 4''$ grid. For the $^{12}\text{CO}(J = 1 \rightarrow 0)$ transition we performed two coverages, for the other two transitions we performed four coverages with perpendicular scanning directions. The combined data therefore were sampled on a $2'' \times 2''$ grid. After first-order baseline subtraction the spectra were summed on a $3'' \times 3''$ grid using the beam ($11''$ at 230 GHz, $22''$ at 109 GHz) and the rms noise level for weighting. This observing and reduction procedure guarantees a smooth data sampling and avoids artifacts in the combination with the interferometric data. The total integration time per beam was 65 s for the $^{12}\text{CO}(J = 1 \rightarrow 0)$, 45 s for the $^{12}\text{CO}(J = 2 \rightarrow 1)$ and 130 s for $^{13}\text{CO}(J = 1 \rightarrow 0)$ transition resulting in an rms noise of 40 mK, 65 mK and 15 mK. As backends we used the autocorrelators which lead to a total bandwidth and velocity resolution of $650 \text{ km s}^{-1}/2.6 \text{ km s}^{-1}$, $650 \text{ km s}^{-1}/1.3 \text{ km s}^{-1}$ and $695 \text{ km s}^{-1}/2.7 \text{ km s}^{-1}$ for the $^{12}\text{CO}(J = 1 \rightarrow 0)$, $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $^{13}\text{CO}(J = 1 \rightarrow 0)$ transitions respectively. For the conversion from T_{A}^* to T_{mb} we used $F_{\text{eff}}/B_{\text{eff}} = 1.35$ at 115 GHz (Guélin et al. 1995) and $F_{\text{eff}}/B_{\text{eff}} = 2.05$ at 230 GHz (Greve et al. 1998).

2.3. Short-spacing correction

To ensure that the interferometric line intensities do not suffer from missing flux due to extended emission we combined the interferometer and the single-dish data cubes.

Table 1. Summary of the relevant parameters of the short-spacing correction

	$^{12}\text{CO}(1-0)$	$^{12}\text{CO}(2-1)$	$^{13}\text{CO}(1-0)$
<i>FWHM</i>	22''	11''	22''
D_{eff}	28.1 m	24.4 m	28.1 m
S_{min}	unknown	24 m	24 m
$SD[\frac{D_{\text{eff}}}{k\lambda}]$	<9.4	<18.5	<8.0
miss. flux	20 %	60 %	35 %

From top to bottom the parameters are the *FWHM* of the IRAM 30 m telescope beam, the corresponding effective diameter of the 30 m telescope, the shortest baseline in the interferometer data, the part of the *uv*-plane that has been replaced by the single-dish data and the average missing flux in the interferometer maps. Since the shortest baseline of the $^{12}\text{CO}(J = 1 \rightarrow 0)$ observations from Shen & Lo is not given in their paper we replaced the part of the *uv*-plane which corresponds to the effective diameter of the 30 m telescope.

For the combination we used a method that works on the final reduced (CLEANed and corrected for primary beam attenuation) interferometer cubes. The only free parameter in this method is the choice of which part of the *uv*-plane in the interferometer cube is replaced by the single-dish values. A detailed description of the method is given in the Appendix. The parameters for the 30 m beam sizes, the corresponding effective diameter of the 30 m telescope, the shortest baseline, the replaced part of the *uv*-plane and the missing flux of the interferometer maps are given in Table 1. All reduction steps were done using the MIRIAD software package. We applied the short-spacing correction to the $^{12}\text{CO}(J = 1 \rightarrow 0)$ cube obtained by Shen & Lo (1995), the $^{13}\text{CO}(J = 1 \rightarrow 0)$ cube from Neininger et al. (1998) and to the $^{12}\text{CO}(J = 2 \rightarrow 1)$ cube.

3. Results

3.1. CO morphology and kinematics

Figures 1 and 2 show the integrated $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ line intensities. The overall morphology of both images is very similar to the $^{12}\text{CO}(J = 1 \rightarrow 0)$ distribution published by Shen & Lo (1995) and the $^{13}\text{CO}(J = 1 \rightarrow 0)$ distribution published by Neininger et al. (1998). It shows a triple peak morphology of which the two outer lobes have been interpreted as the edge of a central molecular toroid (Nakai et al. 1987; Shen & Lo 1995) and a weaker central peak located 65 pc west of the M 82's center (2.2 μm peak; Dietz et al. 1986). The two outer lobes have a projected separation of 410 pc (26''). The separation of the central and the western molecular lobe is only about 130 pc (8''). More diffuse CO emission is detected in the $^{12}\text{CO}(J = 2 \rightarrow 1)$ intensity distribution east and west of the CO peaks and in the south-west of the galaxy. The eastern part of the CO distribution is

significantly warped to the north. The total extent of the emission region is about 1 kpc from east to west. With respect to M 82's center the distribution of the molecular gas is clearly displaced to the west. South of the central and western CO peak two CO spurs are detected (see Fig. 1). They extend about 100 pc below the main molecular disk and join just below the expanding molecular superbubble which is located between the central and western CO peak (Neininger et al. 1998; Weiß et al. 1999). At the same location hot gas emerges into the halo of M 82 (e.g. Shopbell & Bland-Hawthorn 1998; Bregman et al. 1995) supporting the idea that the CO spurs indicate the walls of the superbubble.

Note that the chain of CO emission south of the eastern end of the $^{12}\text{CO}(J = 2 \rightarrow 1)$ distribution is most likely not real but an artifact from the primary beam correction. The kinematic of the central 400 pc is dominated by solid body rotation. The rotation amplitude is about 200 km s^{-1} ranging from 115 km s^{-1} at the western peak up to 320 km s^{-1} at the eastern peak. A *pv*-diagram along the major axis of M 82 in the $^{12}\text{CO}(J = 2 \rightarrow 1)$ transition is shown in Fig. 3. (For the corresponding diagram in the $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ data see Weiß et al. 1999). The *pv*-diagram is centered on the brightest supernova remnant SNR 41.9+58. The intense, velocity crowded regions at 20'', 5'' and -7'' offset correspond to the western, central and eastern CO peak. Between the central and western CO peaks two velocity components at 100 km s^{-1} and 190 km s^{-1} are detected. These features have been interpreted as an expanding superbubble. The velocity of the CO spurs is about 140 km s^{-1} (see Figs. 4 and 5) which is similar to the centroid velocity of the expanding superbubble. Outside the central 400 pc the CO rotation curve flattens. The dynamical center derived from the $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ data agrees very well with the value of $v_{\text{sys}} = 225 \pm 10 \text{ km s}^{-1}$ published by Shen & Lo (1995) for the $^{12}\text{CO}(J = 1 \rightarrow 0)$, and Neininger et al. (1998) for the $^{13}\text{CO}(J = 1 \rightarrow 0)$ transition. The channel maps of the $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ line emission are presented in Figs. 4 and 5.

3.2. Location of the starburst with respect to CO

Most tracers of star formation in M 82 indicate that the highest star-forming activity is not associated with the molecular peaks, which presumably indicate the location of the reservoirs for the “fuel” for star formation, but rather takes place between the peaks. The high-resolution 12.4 μm image of the central region of M 82 published by Telesco & Gezari (1992) suggests that the young stellar clusters, which heat the dust, are located between the western molecular lobe and the 2.2 μm nucleus (western mid infrared (MIR) peaks), at the central CO peak, and between the central CO peak and the eastern CO lobe (eastern MIR peak). A similar morphology is visible in

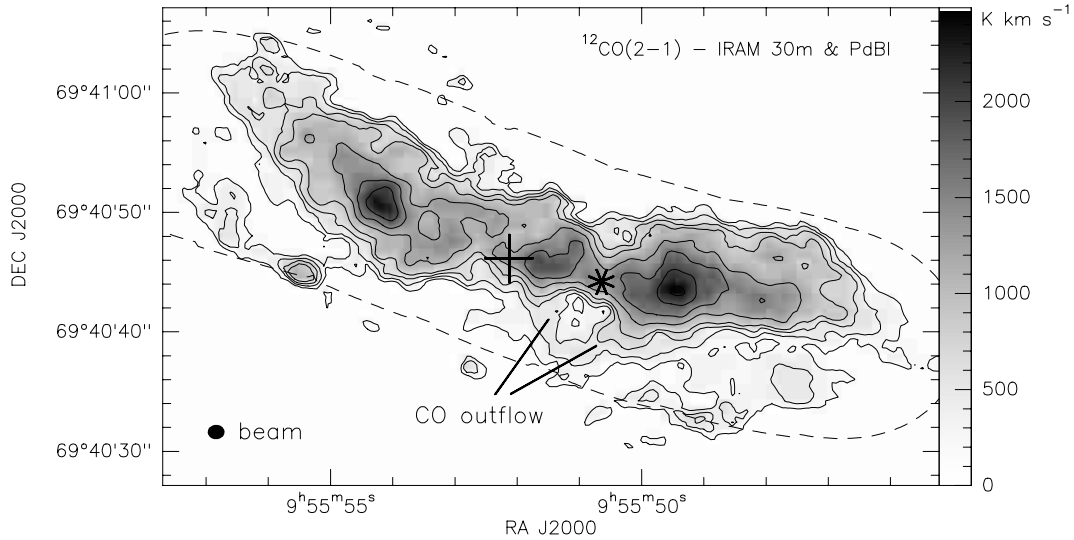


Fig. 1. Integrated $^{12}\text{CO}(J = 2 \rightarrow 1)$ line intensity derived from the short-spacing corrected data cube. The contours correspond to 200, 400, 600, 800, 1 200, 1 600, 2 000 and 2 400 K km s^{-1} . The cross indicates the center of M 82 ($2.2 \mu\text{m}$ peak), the star represents the location of the brightest radio continuum point source (SNR 41.9+58) in M 82. The dotted line shows the 50% sensitivity level of the primary beam mosaic

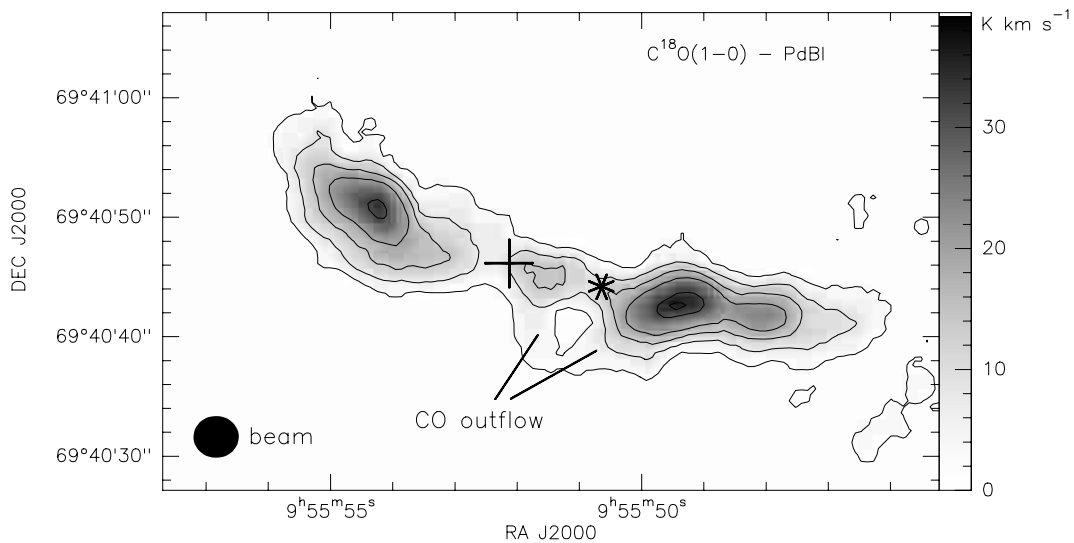


Fig. 2. Integrated $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ line intensity. The contours correspond to 2, 8, 14, 20, 26 and 32 K km s^{-1} . The cross indicates the center of M 82 ($2.2 \mu\text{m}$ peak), the star marks the location of the brightest radio continuum point source (SNR 41.9+58) in M 82

the NeII line emission (Achtermann & Lacy 1995). The radio continuum point sources, which are believed to be supernova remnants (SNR) and compact HII regions, are spread across a much wider region and seem to avoid MIR and NeII peaks (Kronberg et al. 1985). Only the strongest SNR in M 82, SNR41.9+58, appears to be related to features at other wavelengths: it is located near the center of the expanding molecular superbubble, between the central and western CO peak, from which hot X-ray emitting gas is released into the halo of M 82 (Weiß et al. 1999). At the same location recent radio continuum studies by

Wills et al. (1999) identified a blow-out in the form of a cone of missing 5-GHz continuum emission. In the same study three other chimneys were identified within the central 300 pc of M 82. All these observations indicate that the regions of violent star formation are confined by the molecular lobes. Since no indications for high activity have been found at the $2.2 \mu\text{m}$ nucleus itself, it seems that the starburst is arranged in a toroidal topology around the nucleus.

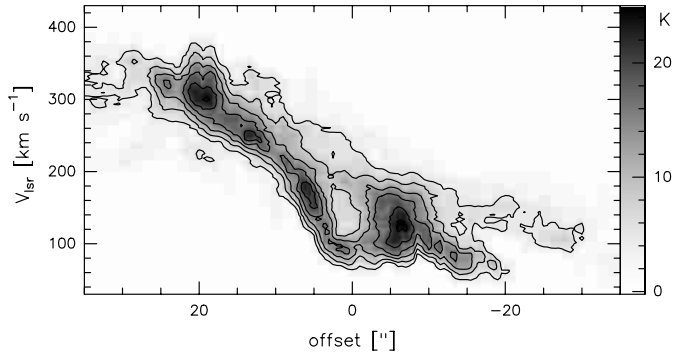


Fig. 3. A pv -diagram along the major axis of M 82 in the $^{12}\text{CO}(J = 2 \rightarrow 1)$ transition. The contours correspond to 4, 8, 12, 14, 18, and 22 K. The pv -diagram is centered on the brightest radio continuum point source SNR 41.9+58 (see Figs. 1 and 2). The velocity crowded regimes at $20''$, $5''$ and $-7''$ offset correspond to the western, central and eastern CO peak

3.3. CO line ratios

To calculate the line ratios properly we used the short-spacing corrected $^{12}\text{CO}(J = 1 \rightarrow 0)$, $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $^{13}\text{CO}(J = 1 \rightarrow 0)$ data cubes. Note that the missing flux in the pure interferometric maps can be as high as 60% (see Table 1). Therefore the short-spacing correction is vital to derive proper line ratios. The short-spacing correction is less crucial for the peak line intensities. Here the missing flux is 10%–30% only. The $^{12}\text{CO}(J = 1 \rightarrow 0)$, $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ data were smoothed to the resolution of the $^{13}\text{CO}(J = 1 \rightarrow 0)$ observations ($4.2''$). Since no single-dish data were obtained for the $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ transition we applied the missing flux factors derived from the $^{13}\text{CO}(J = 1 \rightarrow 0)$ peak intensity distribution to the $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ observations. This procedure is justified because the frequency of both transitions is similar and the observations were carried out in the same configurations with the PdBI. This leads to similar uv -coverages for both observations. Furthermore the morphology in the interferometer maps is similar and both transitions are optically thin (see Sect. 3.4). To take the remaining uncertainties into account we assumed an error of 50% for the $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ line intensities. The line ratios were calculated at 19 positions across the CO distribution of M 82. The spacing between individual positions is about $4''$. The analyzed positions are marked by the crosses in Fig. 8. The circles indicate the $FWHM$ of $4.2''$ used in the study. The positions include all molecular peaks, the $2.2 \mu\text{m}$ nucleus, the MIR peaks, the CO spurs and the diffuse emission in the outer regions of M 82. For clarity the positions have been labeled 1 to 16 from east to west. Positions 17 to 19 correspond to positions on the CO outflow (see Fig. 8). The line ratios at the analyzed positions are summarized in Table 2. Errors include 10% uncertainty of the flux calibrators, errors of the amplitude calibration (typically about 10%) and statistical errors. Our high-resolution line ratios for ^{12}CO

and ^{13}CO differ slightly from values derived from single dish observations by Mao et al. (2000). But our data confirms that $^{12}\text{CO}(J = 2 \rightarrow 1)/^{12}\text{CO}(J = 1 \rightarrow 0)$ ratios larger than 1.8 (e.g. Knapp et al. 1980; Olofsson & Rydbeck 1984; Loiseau et al. 1990) can firmly be rejected. $^{12}\text{CO}(J = 1 \rightarrow 0)/^{13}\text{CO}(J = 1 \rightarrow 0)$ and $^{12}\text{CO}(J = 1 \rightarrow 0)/\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ line intensity ratios are about 10–20 and 40–60 respectively.

3.4. Radiative transfer calculations

The excitation conditions of the CO-emitting volume were modeled using a spherical, isothermal one-component large velocity gradient (LVG) model (Goldreich & Kwan 1974; de Jong et al. 1975). LVG line intensities were calculated for a kinetic temperature and H_2 density range from 5 K to 200 K by 5 K and $\log n(\text{H}_2)$ from 1.8 to 5.0 by 0.2 respectively. In addition, we varied the CO abundance relative to H_2 , $[\text{CO}]$, per velocity gradient and the fractional ^{13}CO and C^{18}O abundances ($[\text{CO}]/\text{grad}(V)$): $1 \cdot 10^{-5}$ to $2 \cdot 10^{-4}$ by $1 \cdot 10^{-6}$; $[\text{CO}]/[^{13}\text{CO}]$: 30 to 100 by 5; $[\text{CO}]/[\text{C}^{18}\text{O}]$: 100 to 300 by 20). For the comparison between the observed peak intensity ratios (Table 2, Cols. 3, 5, 7) and the predicted LVG ratios we used a χ^2 test. To account for the absolute intensities across the disk of M 82 we also fitted the $^{12}\text{CO}(J = 2 \rightarrow 1)$ intensity at each position by varying the beam filling from 0.1 to 0.9 by 0.1. The “best” solutions are shown for positions 3 and 9 in Figs. 6 and 7. Position 3 on the western CO lobe is an example for a solution with low kinetic temperatures and high H_2 densities; position 9 on the brightest MIR peak is representative for solutions with high kinetic temperatures and low H_2 densities.

The observed line ratios and $^{12}\text{CO}(J = 2 \rightarrow 1)$ intensities can be modeled within the errors at all positions. The fit agrees very well with the data at positions where $^{12}\text{CO}(J = 2 \rightarrow 1)/^{12}\text{CO}(J = 1 \rightarrow 0)$ is less than 1.2. At position 6 (eastern MIR peak) we do not find any intersection for all observed line ratios in the H_2 density and kinetic temperature plane. For a more detailed discussion see Sect. 4.1. The best agreement with the observed line ratios and absolute intensities is found for a beam filling of 0.4. Positions 6 and 7 at the eastern MIR peak (Telesco & Gezari 1992) and positions 18 and 19 at the CO outflow require a somewhat lower beam filling of 0.2 and 0.3 respectively.

The LVG parameters of the “best-fit” across the major axis of M 82 are shown in Figs. 8a–d. The CO abundance relative to H_2 per velocity gradient ($[\text{CO}]/\text{grad}(V)$) varies between $1 \cdot 10^{-5} \text{ pc/km s}^{-1}$ and $7 \cdot 10^{-5} \text{ pc/km s}^{-1}$. Assuming $\text{grad}(V) \approx 1 \text{ km s}^{-1} \text{ pc}^{-1}$, as suggested by comparing the linewidth with the linear extent of the region, this corresponds to CO abundances in the range of $[\text{CO}] \approx 10^{-5}$ – $7 \cdot 10^{-5}$. Similar values have been determined in the Orion region (Blake et al. 1987) and were suggested by chemical models (Farquhar et al. 1994).

Table 2. CO line ratios in M 82 at 4'' resolution. The offsets are given relative to $\alpha = 09^{\text{h}}55^{\text{m}}51^{\text{s}}.94, \delta = 69^{\circ}40'47.14''$ (J2000.0). For Cols. 8 & 9 we have corrected the C^{18}O intensities with the missing flux factor determined from the ^{13}CO data. The corresponding percentage is given in Col. 10. Errors include 10% uncertainty of the flux calibrators, errors of the amplitude calibration (typically about 10%) and statistical errors. For the C^{18}O intensities we assumed an error of 50% due to the unknown missing flux

	$\Delta\alpha$	$\Delta\delta$	$\frac{I(\text{CO}(2-1))}{I(\text{CO}(1-0))}$	$\frac{T(\text{CO}(2-1))}{T(\text{CO}(1-0))}$	$\frac{I(\text{CO}(1-0))}{I(^{13}\text{CO}(1-0))}$	$\frac{T(\text{CO}(1-0))}{T(^{13}\text{CO}(1-0))}$	$\frac{I(\text{CO}(1-0))}{I(\text{C}^{18}\text{O}(1-0))}$	$\frac{T(\text{CO}(1-0))}{T(\text{C}^{18}\text{O}(1-0))}$	MF $^{13}\text{CO}^1$
	[']	[']							[%]
1	16.5	7.5	1.16 ± 0.3	1.02 ± 0.3	15.2 ± 4.9	19.2 ± 5.7	44 ± 24	66 ± 35	23.5
2	14.5	5.0	1.17 ± 0.3	0.96 ± 0.3	12.7 ± 3.9	15.4 ± 4.9	38 ± 21	45 ± 24	10.3
3	11.5	3.0	1.12 ± 0.3	0.98 ± 0.3	11.5 ± 3.4	12.2 ± 3.7	40 ± 21	44 ± 24	8.0
4	9.5	1.0	1.19 ± 0.3	1.09 ± 0.3	12.0 ± 3.6	13.0 ± 4.1	39 ± 21	43 ± 23	7.0
5	6.5	0.5	1.34 ± 0.4	1.03 ± 0.3	14.2 ± 4.4	12.8 ± 4.2	37 ± 20	40 ± 22	9.0
6	4.0	0.5	1.42 ± 0.4	1.28 ± 0.4	15.0 ± 4.8	12.6 ± 4.1	33 ± 18	37 ± 20	12.4
7	2.0	-0.5	1.39 ± 0.4	1.26 ± 0.4	17.3 ± 5.7	16.5 ± 6.1	37 ± 20	61 ± 33	10.3
8	-1.0	-1.5	1.06 ± 0.3	1.01 ± 0.3	25.9 ± 8.5	20.7 ± 8.0	36 ± 20	56 ± 30	13.0
9	-4.0	-2.0	0.98 ± 0.3	0.98 ± 0.3	21.3 ± 6.6	22.1 ± 8.4	53 ± 28	56 ± 30	15.6
10	-6.5	-3.0	1.07 ± 0.3	0.95 ± 0.3	25.4 ± 8.4	17.0 ± 6.0	41 ± 22	45 ± 24	12.9
11	-10.0	-4.0	1.12 ± 0.3	1.08 ± 0.3	13.2 ± 3.9	11.7 ± 3.8	45 ± 24	29 ± 15	14.0
12	-14.0	-4.0	1.00 ± 0.3	0.98 ± 0.3	15.3 ± 4.5	11.5 ± 3.5	48 ± 26	36 ± 20	4.3
13	-17.5	-4.0	1.14 ± 0.3	1.02 ± 0.3	14.6 ± 4.4	10.9 ± 3.3	48 ± 26	39 ± 21	6.6
14	-20.5	-4.5	1.05 ± 0.3	0.95 ± 0.3	14.3 ± 4.3	11.1 ± 3.6	49 ± 27	39 ± 21	4.1
15	-23.5	-4.5	1.07 ± 0.3	1.00 ± 0.3	16.3 ± 5.1	14.7 ± 4.7	60 ± 32	48 ± 26	5.6
16	-26.5	-4.0	1.14 ± 0.3	1.09 ± 0.3	14.5 ± 4.8	14.3 ± 4.9	62 ± 34	56 ± 30	6.2
17	-2.5	-5.5	1.02 ± 0.3	1.07 ± 0.3	20.2 ± 6.8	21.2 ± 8.3	40 ± 22	54 ± 29	19.0
18	-3.5	-9.0	1.20 ± 0.3	0.91 ± 0.3	12.0 ± 4.1	21.5 ± 8.6	29 ± 16	52 ± 28	27.4
19	-8.5	-7.0	1.36 ± 0.4	1.12 ± 0.3	11.8 ± 3.8	11.6 ± 3.9	32 ± 17	33 ± 18	10.8

¹Missing flux determined from the ^{13}CO data.

$[\text{CO}]/\text{grad}(V)$ increases towards the MIR peaks which indicates higher CO abundances at the active star-forming regions than in the more quiescent outer regions. The fractional ^{13}CO abundance $[^{12}\text{CO}]/[^{13}\text{CO}]$ across M 82 does not show any significant spatial variation. The mean value of all positions is 70 ± 20 . A low fractional ^{13}CO abundance is consistent with recent radiative transfer calculations by Mao et al. (2000) and an independent chain of arguments based on CN and ^{13}CN measurements (Henkel et al. 1998). In contrast, the fractional C^{18}O abundance $[^{12}\text{CO}]/[\text{C}^{18}\text{O}]$ shows a trend towards higher C^{18}O abundances at the MIR peaks and in the outflow. While the average $[^{12}\text{CO}]/[\text{C}^{18}\text{O}]$ ratio in the quiescent regions is about 270, it is only about 160 at position 6, 11, 17 and 19 (see Fig. 8d). Note that these values suggest C^{18}O abundances 2–3 times higher than those used by Wild et al. (1992) for their LVG calculations of CO line ratios in M 82.

The kinetic temperature is well correlated with the MIR emission and other tracers of high-level star formation. Within the prominent CO lobes with less signs of ongoing star formation, the kinetic temperature is about 50 K. Towards the active star-forming regions we find two kinetic temperature peaks above 150 K. These

“hot-spots” coincide with the location of MIR peaks (for a comparison between the MIR emission and the CO distribution see Telesco & Gezari 1992). Near the 2.2 μm nucleus the LVG models suggest temperatures of about 75 K. Along the CO outflow the temperature drops with increasing distance from the active regions. At position 17 and 19 we find temperatures above 100 K. At position 18 (100 pc distance from the plane) the kinetic temperature has dropped to 60 K. The spatial variation of the kinetic temperature along the major axis of M 82 is shown in Fig. 8a. The corresponding diagram of the H_2 density distribution is shown in Fig. 8b. Solutions are found between $n(\text{H}_2) = 10^{2.7}$ and $10^{4.2} \text{ cm}^{-3}$. In general, the H_2 densities are high in regions with low kinetic temperatures and vice versa. The solutions for the outer CO lobes suggest an H_2 density about $n(\text{H}_2) = 10^{4.0} \text{ cm}^{-3}$ with a tendency towards somewhat lower values at the very edge of the CO distribution ($n(\text{H}_2) = 10^{3.5} \text{ cm}^{-3}$). These values are in agreement with H_2 densities calculated by Wild et al. (1992) and Mao et al. (2000). At the “hot-spot”, low H_2 densities of $n(\text{H}_2) = 10^{2.8-3.1} \text{ cm}^{-3}$ are required to match the observed line ratios. H_2 densities in the CO outflow are about $n(\text{H}_2) = 10^{3.0} \text{ cm}^{-3}$.

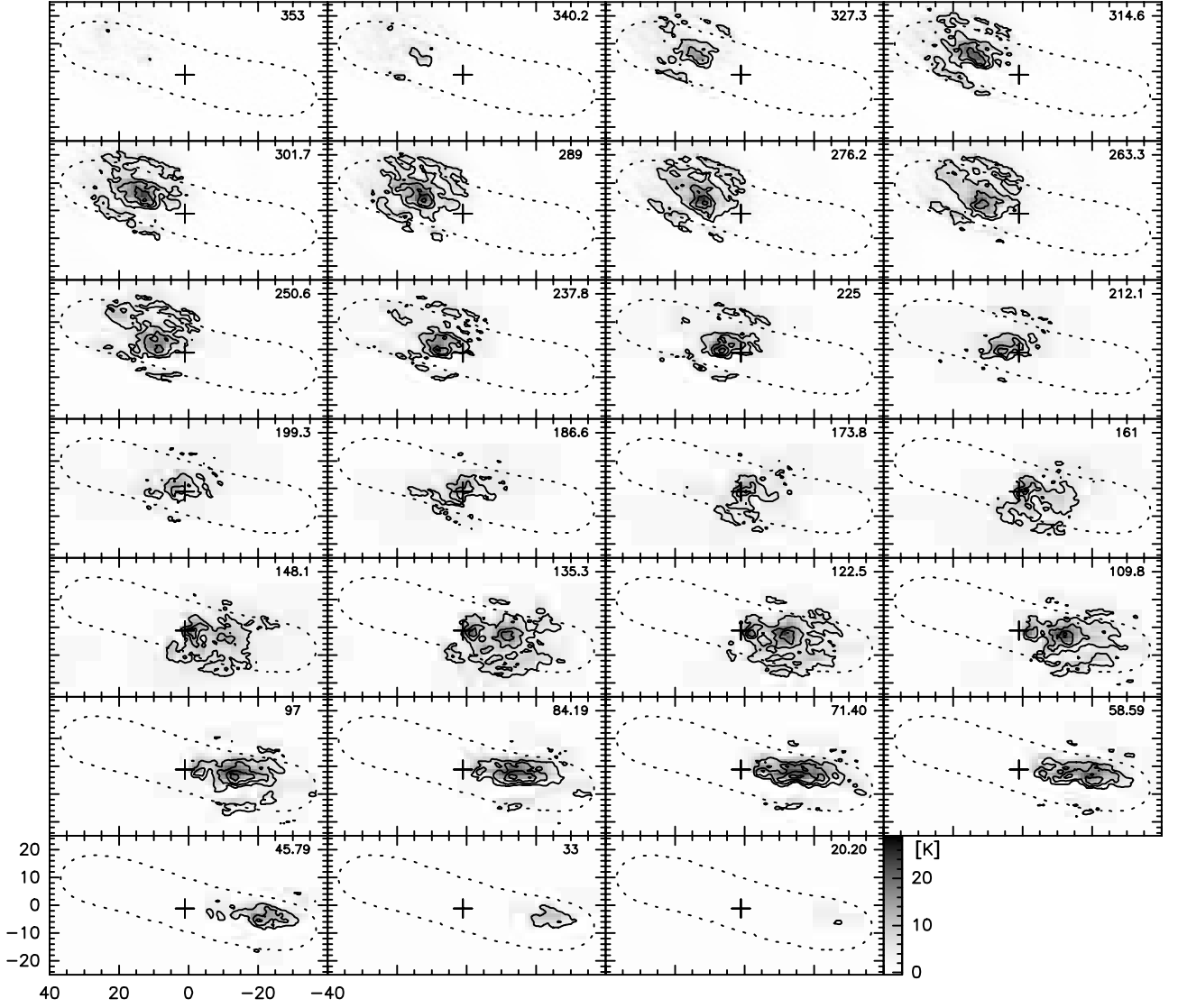


Fig. 4. $^{12}\text{CO}(J = 2 \rightarrow 1)$ velocity channel maps of the short-spacing corrected data cube. Offsets in RA, DEC are given relative to the $2.2 \mu\text{m}$ nucleus indicated by the cross in each channel map. The velocity spacing between individual maps is 12.8 km s^{-1} , the central velocity (V_{Isr}) of each map is given in the top right corner in units of km s^{-1} . The intensities are corrected for attenuation of the primary beam. The contours correspond to 6, 12, 18, 24 and 30 K. The dotted line in each channel map shows the 50% sensitivity level of the primary beam mosaic

Both the $^{12}\text{CO}(J = 1 \rightarrow 0)$ and the $^{12}\text{CO}(J = 2 \rightarrow 1)$ transitions are optically thick. In the cold dense regions we find an optical depth of $\tau_{^{12}\text{CO}(J=1\rightarrow 0)} = 2\text{--}5$ and $\tau_{^{12}\text{CO}(J=2\rightarrow 1)} = 7\text{--}15$. At the “hot-spots” the derived optical depths are somewhat lower and reach unity in the $^{12}\text{CO}(J = 1 \rightarrow 0)$ transition at the eastern MIR peak (position 6 & 7). For the ground transitions of the rare isotopes ^{13}CO and C^{18}O we find optically thin emission at all positions. Typical optical depths are $\tau_{^{13}\text{CO}(J=1\rightarrow 0)} = 5 \cdot 10^{-2}$ and $\tau_{\text{C}^{18}\text{O}(J=1\rightarrow 0)} = 5 \cdot 10^{-3}$.

3.5. Column densities and mass distribution

For the determination of CO and H_2 column densities at each position we used three methods:

- LVG: The column densities were derived from the CO and H_2 densities, the velocity gradient and the observed line widths using $N(\text{CO}) = 3.08 \cdot 10^{18} n(\text{CO}) \frac{dV}{\text{grad}(V)}$ and $N(\text{H}_2) = 3.08 \cdot 10^{18} n(\text{H}_2) \frac{dV}{\text{grad}(V)}$, where dV is the observed line width. Therefore $\frac{dV}{\text{grad}(V)}$ is an equivalent path length through the clouds;
- LVG_{PF} (PF = partition function): the ^{13}CO and C^{18}O column densities were calculated from the general relation between optical depth, excitation temperature and column density at rotation level J : $N_J = 93.5 \frac{g_J V^3}{g_{(J+1)} A_{J+1,J}} (1 - \exp(-4.8 \cdot 10^{-2} \nu / T_{\text{ex}}))^{-1} \int \tau dv$ where g_J is the statistical weight of level J and $A_{J+1,J}$ is the Einstein coefficient for the transition $J + 1$ to J . $\int \tau dv$ was approximated by $\int \tau dv \approx 1.06 \tau dV$. T_{ex} and τ are given by the LVG code for each level. ^{13}CO and C^{18}O column densities were

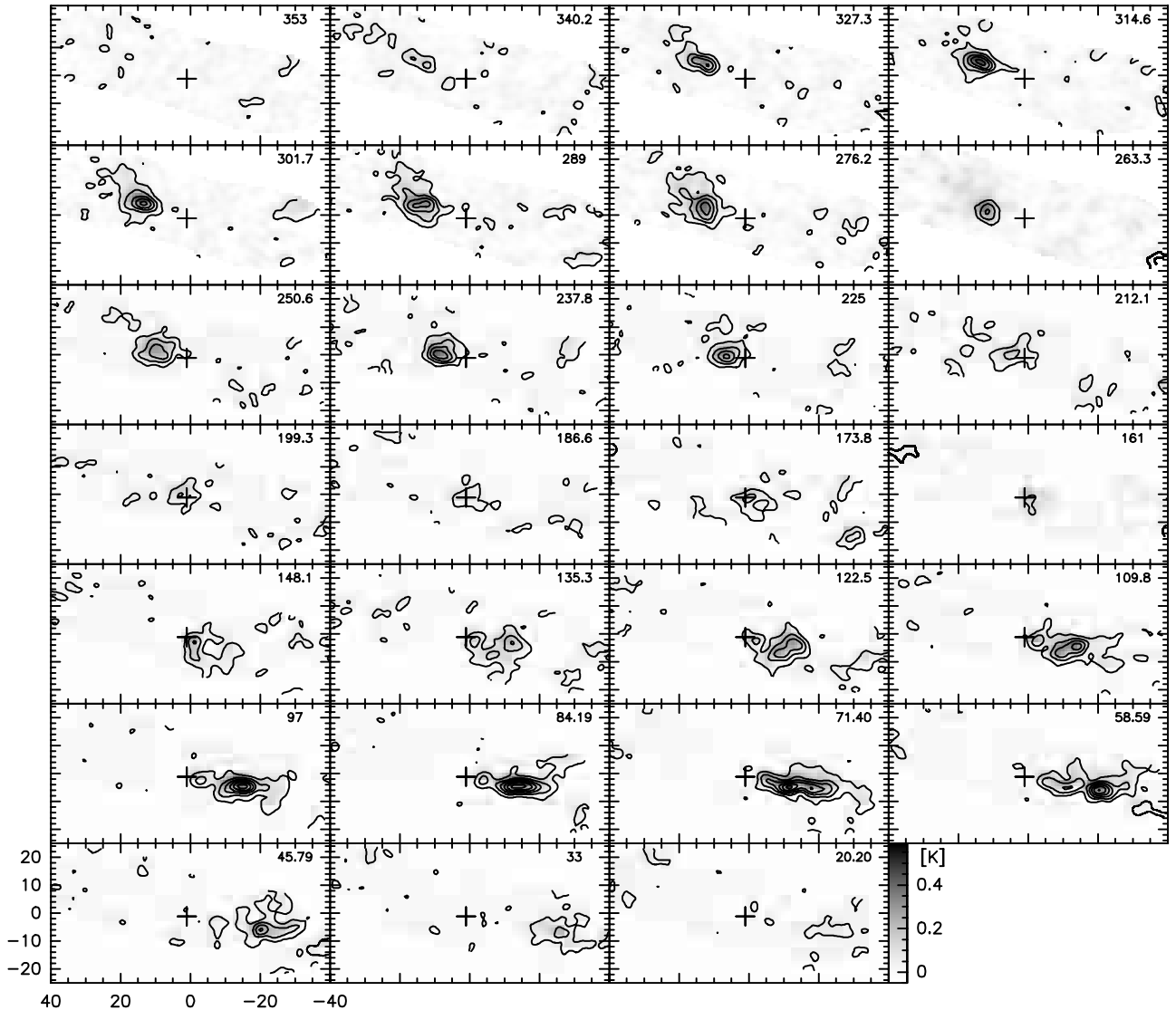


Fig. 5. $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ velocity channel maps of the PdBI data cube. The figure has the same layout and specifications as Fig. 4; contours correspond to 0.05, 0.15, 0.25, 0.35, 0.45 and 0.55 K

determined using the sum of the 6 lowest levels for each isotope. H_2 and CO column densities were derived from the relative abundances of the rare isotopes relative to H_2 and CO;

– LTE: ^{13}CO and C^{18}O column densities were derived using a standard LTE approach (e.g. Dickman 1978). As for the LVG_{PF} method, CO and H_2 column densities were derived from the abundances of the rare isotopes relative to CO and H_2 at each position.

Column densities calculated from ^{13}CO and C^{18}O via the LTE method match each other with less than 5% difference at each position. The same holds for the LVG_{PF} column densities calculated from T_{ex} and τ of the ^{13}CO and C^{18}O transition. For simplicity we therefore give in the following the average between the column densities calculated from ^{13}CO and C^{18}O via the LTE and LVG_{PF} method.

The spatial variations of the beam-averaged H_2 column density across the major axis of M 82 as calculated with the three methods is shown in Fig. 9. The spatial distribution of the H_2 column densities is in good agreement for all three methods. This suggests that the low J levels are almost thermalized. The largest difference between the methods is apparent at the central CO peak. While the LTE solutions suggest a local H_2 column density maximum of about $N(\text{H}_2)_{4''} = 1 \cdot 10^{23} \text{ cm}^{-2}$, the peak is less prominent ($N(\text{H}_2)_{4''} = 5 \cdot 10^{22} \text{ cm}^{-2}$) and displaced by $4''$ in the LVG and LVG_{PF} solution (see Fig. 9).

Nevertheless, all methods clearly show that most of the molecular gas traced by CO is located in the outer CO lobes. The central 300 pc between the molecular lobes contain only about 20–30% of the molecular gas mass. Furthermore, the H_2 column density distribution is clearly asymmetric with respect to the $2.2 \mu\text{m}$ nucleus. We find that the centroid of mass is located about

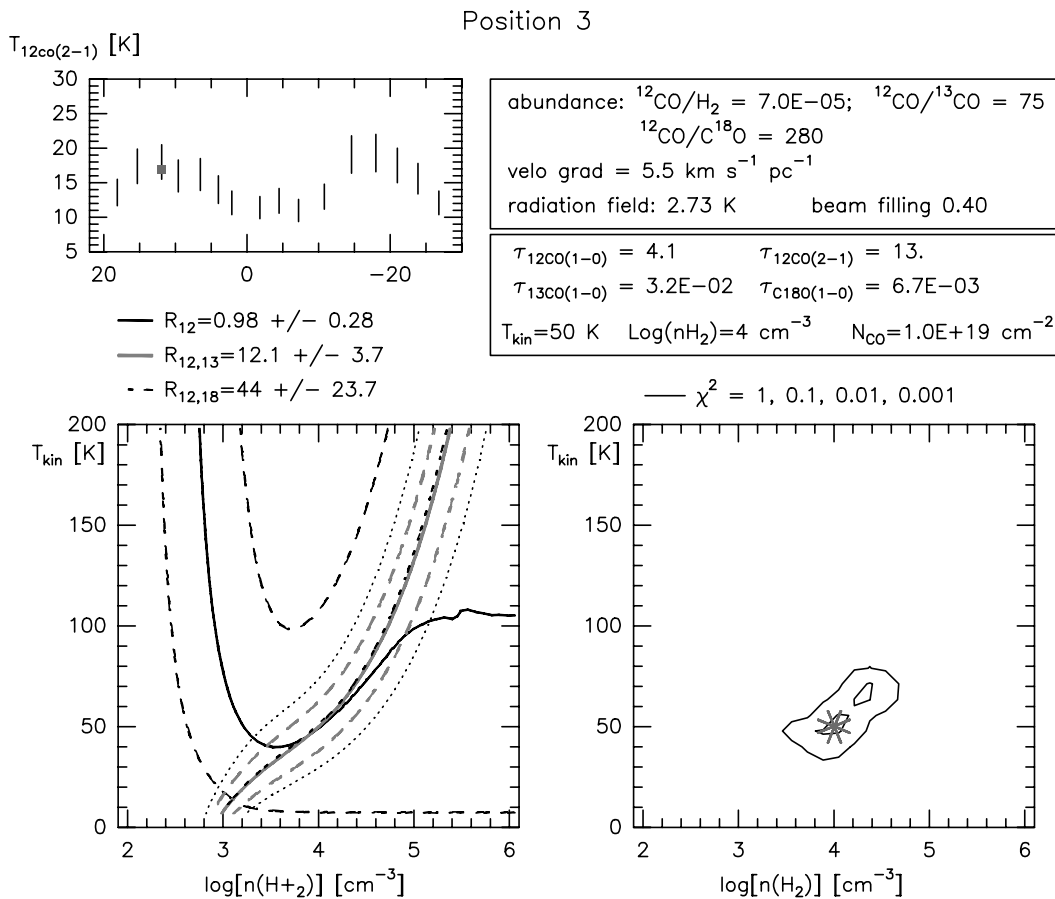


Fig. 6. “Best” LVG solution at position 3 (the eastern CO lobe). The top left diagram shows the observed $^{12}\text{CO}(J = 2 \rightarrow 1)$ line intensities across the major axis of M82 and the $^{12}\text{CO}(J = 2 \rightarrow 1)$ intensity as given by the LVG-model for position 3. The fixed LVG-parameters (abundances, velocity gradient, radiation field and beam filling) are given in the upper right box. The parameters below the LVG input parameters summarize the optical depth for each transition, the CO column density, the kinetic temperature and H_2 density for the “best fit”. The black and the grey solid line in the lower left diagram are the $^{12}\text{CO}(J = 2 \rightarrow 1)/^{12}\text{CO}(J = 1 \rightarrow 0)$ (R_{12}) and $^{13}\text{CO}(J = 1 \rightarrow 0)/^{12}\text{CO}(J = 1 \rightarrow 0)$ ($R_{12,13}$) line intensity ratio, respectively. The dashed lines indicate the observational errors for the corresponding line ratio. The $^{18}\text{O}(J = 1 \rightarrow 0)/^{12}\text{CO}(J = 1 \rightarrow 0)$ ($R_{12,18}$) line intensity ratio is given by the dashed-dotted line. Its error is indicated by the dotted line. The contours in the lower right diagram are results of the χ^2 test comparing the predicted line ratios and the $^{12}\text{CO}(J = 2 \rightarrow 1)$ line intensity with the observed values. The star indicates the best solution in the kinetic temperature and H_2 density plane

100 pc south-east of the nucleus. The location of the centroid of mass for each method is indicated by the vertical line in Fig. 9. The highest H_2 column density is found at the western CO lobe (position 12). Its beam-averaged LVG column densities are $N(\text{CO})_{4''} = 2 \cdot 10^{19} \text{ cm}^{-2}$ and $N(\text{H}_2)_{4''} = 2.3 \cdot 10^{23} \text{ cm}^{-2}$. The corresponding cloud-averaged LVG column densities are $N(\text{CO})_{\text{cloud}} = 4 \cdot 10^{19} \text{ cm}^{-2}$ and $N(\text{H}_2)_{\text{cloud}} = 6 \cdot 10^{23} \text{ cm}^{-2}$, respectively. The corresponding values for the eastern CO lobe (position 3) are $N(\text{CO})_{4''} = 1 \cdot 10^{19} \text{ cm}^{-2}$, $N(\text{H}_2)_{4''} = 1.5 \cdot 10^{23} \text{ cm}^{-2}$, $N(\text{CO})_{\text{cloud}} = 2.5 \cdot 10^{19} \text{ cm}^{-2}$ and $N(\text{H}_2)_{\text{cloud}} = 3.8 \cdot 10^{23} \text{ cm}^{-2}$. For an assumed line-of-sight of 350 pc (for comparison with Mao et al. 2000) the mean molecular density in the CO lobes is $\langle n(\text{H}_2) \rangle_{4''} = 140\text{--}210 \text{ cm}^{-3}$. This corresponds to a volume filling factor of $f_{v,4''} = \langle n(\text{H}_2) \rangle_{4''}/n(\text{H}_2) \approx 0.01$. With $f_{a,4''} = 0.4$ and a linear resolution of 65 pc we obtain

characteristic cloud sizes of $r_{\text{cloud}} = \frac{1}{2} 65 \text{ pc } f_{v,4''}/f_{a,4''} \approx 1 \text{ pc}$. Volume filling factors and characteristic cloud sizes do not change significantly in the central star forming regions. These values are in good agreement with PDR models published by Wolfire et al. (1990).

H_2 column densities in the molecular outflow are in the range $N(\text{H}_2)_{4''} = 1.5\text{--}3.0 \cdot 10^{22} \text{ cm}^{-2}$. The total mass of the outflow is $7.2 \cdot 10^5 M_{\odot}$ ($D = 3.9 \text{ Mpc}$, Sakai & Madore 1999).

3.6. Conversion from $I(\text{CO})$ to $N(\text{H}_2)$ and total mass

To derive the conversion factor from $I(\text{CO})$ to $N(\text{H}_2)$, we have compared LVG, LTE, and LVG_{PF} H_2 column densities with the integrated $^{12}\text{CO}(J = 1 \rightarrow 0)$ intensities at $4.2''$ resolution at the analyzed positions across the central part of M82. The variation of

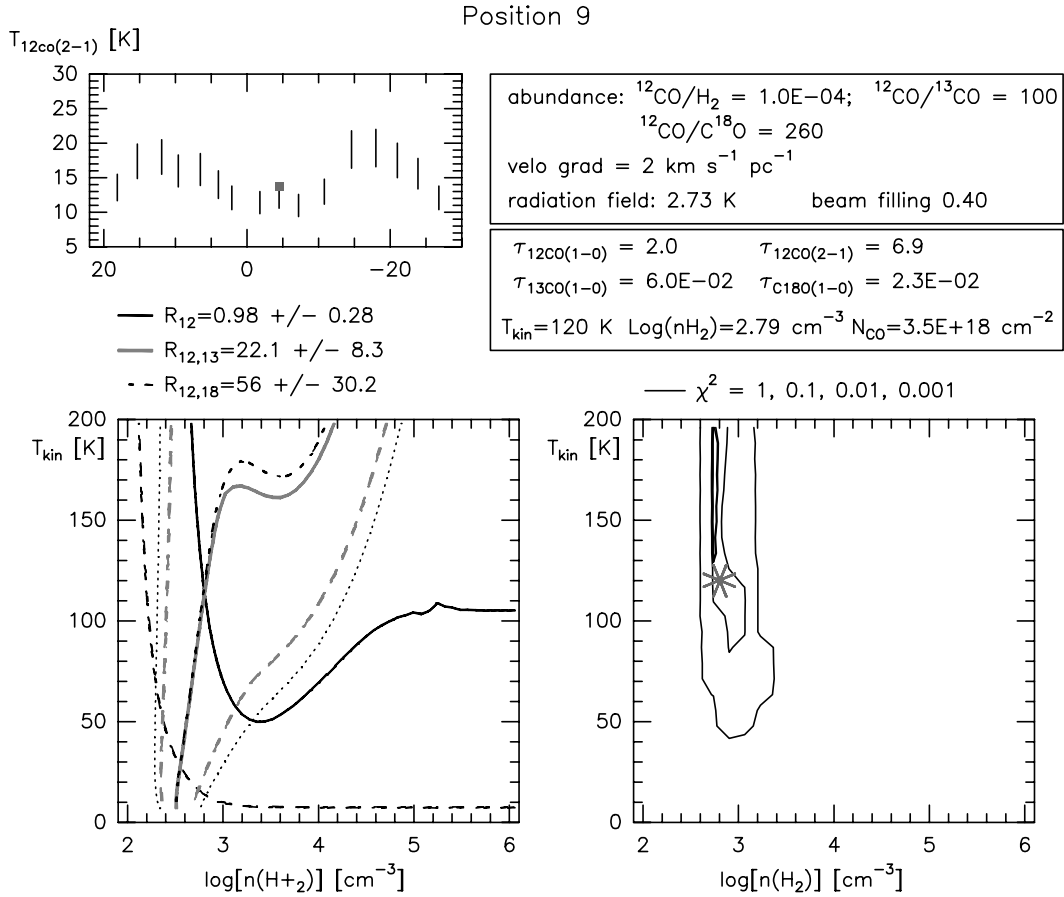


Fig. 7. “Best” LVG solution at position 9 (central MIR peak). The items and parameters are the same as in Fig. 6

the conversion factor $X_{\text{CO}} = N(\text{H}_2)/I(\text{CO})$ with position is shown in Fig. 10. Note that X_{CO} is lower than the Galactic value of $1.6 \cdot 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ (Hunter et al. 1997) at all positions and for all methods. We find that X_{CO} varies across the disk of M 82 by about a factor of 5 if one considers the LTE solutions ($X_{\text{CO}} = 2.1\text{--}10.8 \cdot 10^{19} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$) and by a factor of 8–9 for the LVG and LVG_{PF} solutions ($X_{\text{CO}} = 1.3\text{--}11.5 \cdot 10^{19} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ and $X_{\text{CO}} = 1.5\text{--}12.2 \cdot 10^{19} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$). All methods show that the lowest conversion factors are associated with the central star-forming regions where the gas is heated by UV photons from the newly formed stars and cosmic-rays from SNRs. The CO-emitting volumes at these positions have high kinetic temperatures. Towards the outer molecular lobes with higher H_2 densities and lower kinetic temperatures, the conversion factor rises. This is in agreement with simple theoretical arguments that suggest that the conversion factor X_{CO} should be proportional to $T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2}$ for virialized clouds (Maloney & Black 1988). The variation of X_{CO} with $T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2}$ is shown in Fig. 11. The linear correlation between X_{CO} and $T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2}$ for $T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2} > 0.5$ is clearly visible. For $T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2} < 0.5$ the scatter in the plot increases. This is in particular true for X_{CO} calculated

under the assumption of LTE. This suggests that the gas is not close to LTE at the “hot spots”. The increased scatter of X_{CO} calculated with the LVG and LVG_{PF} method might suggest that either the clouds are not virialized or that more appropriate models (like PDR models) are required to calculate the physical gas properties in the center of the starburst. For a more detailed discussion see Sect. 4.1. Nevertheless, this result not only shows that the standard Galactic X_{CO} factor is not appropriate for a starburst system like M 82, but that X_{CO} is a function of the intrinsic gas properties which strongly depend on environmental effects. This implies that spatial variations of $^{12}\text{CO}(J = 1 \rightarrow 0)$ intensities can be due to variations of the excitation conditions of the gas rather than variations of column density. Similar results have been obtained by Wild et al. (1992) using low-resolution CO data (see also Sect. 4.3). Based on the analysis of X_{CO} we have calculated the “true” H_2 distribution in M 82 by interpolating the changes of X_{CO} from the analyzed positions across the central CO distribution. Multiplication of this X_{CO} -map with the integrated $^{12}\text{CO}(J = 1 \rightarrow 0)$ intensity distribution thus results in an H_2 column density map. We show these maps in Fig. 12 for X_{CO} derived from the LVG_{PF} (top) and LTE solutions (middle) in comparison with the H_2 distribution one would derive assuming a

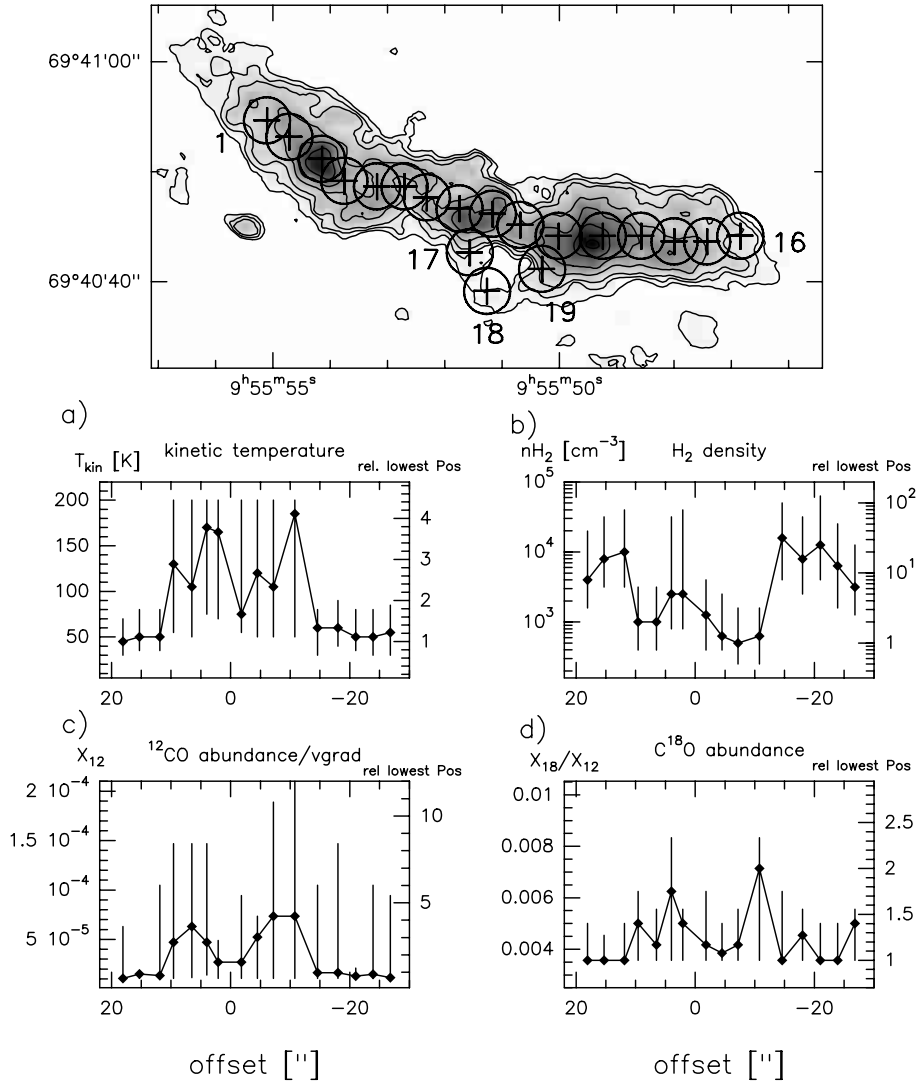


Fig. 8. LVG solutions for positions 1 to 16. Top: locations of the analyzed positions. The radii of the circles indicate the spatial resolution for which the line ratios have been determined. **a) to d):** spatial variations of the kinetic temperature, the H₂ density, the CO abundance per velocity gradient and the fractional C¹⁸O abundance across the major axis of M 82. The error bars in **a)** and **b)** correspond to the parameter range of kinetic temperatures and H₂ densities for which the LVG line ratios and the ¹²CO($J = 2 \rightarrow 1$) intensity is consistent with the observations within the errors. This corresponds to the area within the $\chi^2 = 1$ contour shown for position 3 and 9 in Figs. 6 and 7. The error bars in **c)** and **d)** correspond to the range for [CO]/grad(V) and fractional C¹⁸O abundance where the χ^2 of the corresponding fit is 50 times higher than for the “best” solution

constant, standard Galactic conversion (bottom) to illustrate the importance of detailed studies of X_{CO} to derive H₂ column density distributions. The H₂ column density maps in Fig. 12 (top and middle) indicate that the central star-forming region is surrounded by a double-lobed distribution of molecular gas, while H₂ seems to be depleted in the central starburst region itself (see also Fig. 9).

The total H₂ mass of the region shown in Fig. 12 is $2.3 \cdot 10^8 M_{\odot}$ for the LVG_{PF} and LVG and $2.7 \cdot 10^8 M_{\odot}$ for the LTE solution at a distance of $D = 3.9$ Mpc (Sakai & Madore 1999). The corresponding values at $D = 3.25$ Mpc (Tammann & Sandage 1968) are 1.6 and $1.9 \cdot 10^8 M_{\odot}$, respectively. These values are in good agreement with estimates from 450 μm dust continuum measurements

(Smith et al. 1991) and from C¹⁸O($2 \rightarrow 1$) intensities (Wild et al. 1992). Therefore, the total molecular mass is 3 times lower than the mass one would derive using the standard Galactic conversion factor of $1.6 \cdot 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ ($4.9 \cdot 10^8 M_{\odot}$ $D = 3.25$ Mpc; $7.1 \cdot 10^8 M_{\odot}$ $D = 3.9$ Mpc).

4. Discussion

4.1. Comparison with other radiative transfer analyses

Analyses of the physical conditions of the molecular gas in M 82 have been published by Tilanus et al. (1991), Wild et al. (1992), Güsten et al. (1993) and more recently by Mao et al. (2000) and Petitpas & Wilson (2000) using

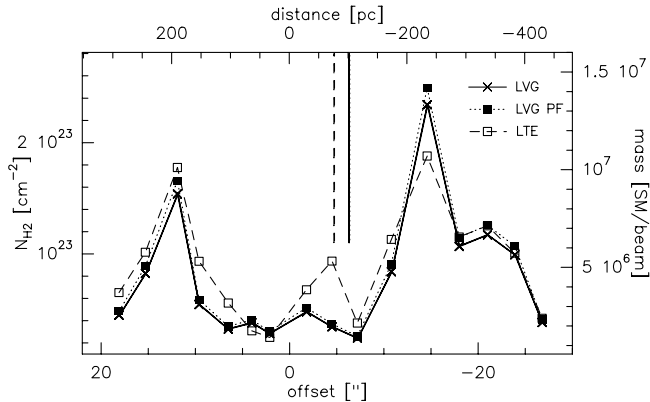


Fig. 9. Beam averaged H_2 column densities across the major axis of M 82. Offsets are given relative to the center of M 82 ($2.2 \mu\text{m}$ peak). The thick solid line corresponds to the H_2 column densities derived from the LVG solutions. The dashed and the dotted lines give the corresponding values for the LTE approximation and the solution calculated from the partition functions (LVG_{PF}), respectively. The vertical lines indicate the location of the centroid of mass of the three H_2 distributions. Note that the location of the centroid of mass is identical for the LVG and LVG_{PF} solution. The labeling of the right axes gives the H_2 mass per beam in units of solar masses

single-dish CO data and other tracers of the molecular gas. The kinetic gas temperature of the CO-emitting gas phase derived in these studies are of order $T_{\text{kin}} = 30\text{--}70$ K. H_2 densities range between $n(\text{H}_2) = 10^3\text{--}10^4 \text{ cm}^{-3}$. Thus our solutions at the CO lobes and the outer parts of the CO distribution ($n(\text{H}_2) = 10^{3.5\text{--}4.2} \text{ cm}^{-3}$, $T_{\text{kin}} = 45\text{--}60$ K) are consistent with previous studies.

The situation is different for our LVG solutions within the starburst region. Kinetic gas temperatures above 150 K are clearly inconsistent with results published in literature so far. In the most recent analysis of the excitation conditions of the molecular gas using mm and sub-mm CO emission lines (up to $J = 7\text{--}6$), Mao et al. (2000) suggested kinetic gas temperatures as high as 130 K. However, they rejected their LVG solution because of intrinsic inconsistencies regarding almost equal area and volume filling factors derived from the one-component LVG model. This leads to characteristic cloud sizes of about 150 pc which is inconsistent with high-resolution studies of the CO distribution in M 82 (Shen & Lo 1995; Neininger et al. 1998 and this work). Characteristic cloud sizes derived from our analysis are only ≈ 1 pc, hence more realistic. This difference results mainly from a very low area filling factor of only $f_{\text{a},22''} = 0.04\text{--}0.07$ found by Mao et al. (2000). From the CO morphology (see Fig. 1) and $f_{\text{a},4''} = 0.4\text{--}0.2$ we would expect area filling factors of $f_{\text{a},22''} = 0.2\text{--}0.15$ at $22''$ resolution. The reason for this discrepancy remains unclear. But obviously the assumption of an isothermal gas phase used in the LVG model is more reasonable for our high spatial resolution study than for the low-resolution data used by Mao et al. (2000). Even though

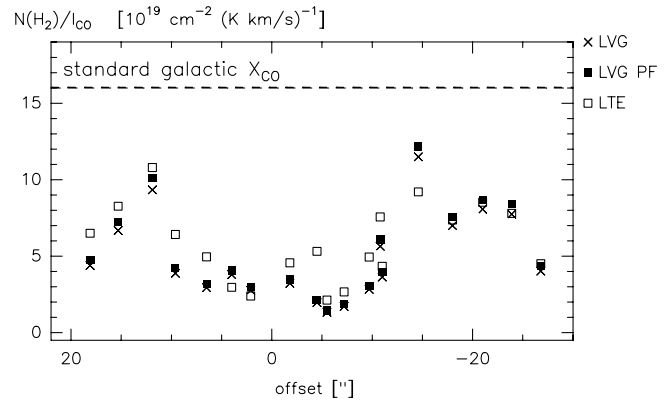


Fig. 10. Variation of X_{CO} across the analyzed positions in M 82. Offsets are given relative to the center of M 82 ($2.2 \mu\text{m}$ peak). The H_2 column densities were derived using the LTE, the LVG and LVG_{PF} solutions. The dotted line at $X_{\text{CO}} = 1.6 \cdot 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ corresponds to the standard Galactic conversion factor

our LVG analysis does not lead to internal inconsistencies we also find that the observed line ratios are difficult to reproduce with the one-component LVG model at the “hot spots”. This is in particular true for positions 6, 7 and 11 (eastern MIR peak and expanding superbubble) where no intersection of all observed line ratios (disregarding the errors of the observations) exists within the calculated parameter space. At these positions more sophisticated radiative transfer models like PDR models probably lead to more consistent results. However, a comparison between LVG and PDR models in M 82 shows that constraints on H_2 densities and beam-averaged column densities are very similar for both methods (Mao et al. 2000). Güsten et al. (1993) and Mao et al. (2000) concluded that in order to explain the observed line ratios, a two-component model of the molecular gas in M 82 is needed. But while models of Güsten et al. (1993) favor the existence of a warm, dense ($T_{\text{kin}} = 50\text{--}70$ K; $n(\text{H}_2) = 10^5 \text{ cm}^{-3}$) and a cold, diffuse ($T_{\text{kin}} = 20\text{--}30$ K; $n(\text{H}_2) = 10^3 \text{ cm}^{-3}$) gas component, Mao et al. (2000) find that the bulk of CO emission arises from a warm, diffuse component. Our high-resolution LVG results confirm the PDR calculations of Mao et al. (2000). In particular, their conclusion that the bulk of CO emission in the core of M 82 arises from a warm, low-density interclump medium is consistent with our findings.

Further support for a highly excited CO component towards the active regions in M 82 comes from the morphology of the high- J CO lines observed by Mao et al. (2000). They find that the spatial separation of the CO lobes decreases with increasing J . While the spatial separation of the outer CO lobes in the $^{12}\text{CO}(J = 1 \rightarrow 0)$ and $^{12}\text{CO}(J = 2 \rightarrow 1)$ transition is about $26''$, it decreases to only $15''$ in the $^{12}\text{CO}(J = 7 \rightarrow 6)$ transition. This distance is in good agreement with the spatial separation of the kinetic temperature peaks that we find in our LVG solutions (Fig. 8a).

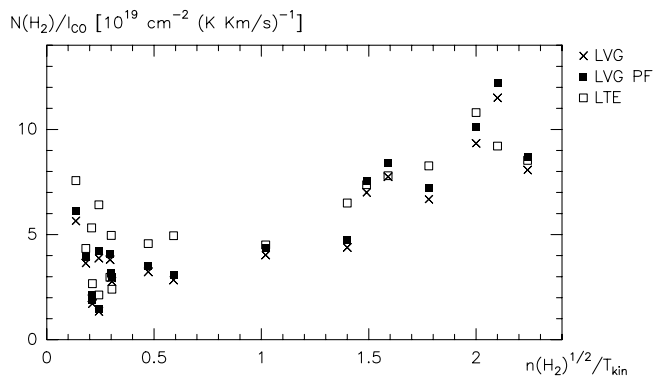


Fig. 11. X_{CO} as derived from the LTE, LVG and LVG_{PF} solutions versus $T^{-1} n(\text{H}_2)^{1/2}$. The plot shows a linear correlation between the conversion factor and the associated H_2 densities and kinetic temperatures beyond $T^{-1} n(\text{H}_2)^{1/2} \approx 0.5$

To further test the reliability of the modeled kinetic temperature and H_2 density distribution across M 82 we calculated line ratios for the high- J transitions of ^{12}CO and ^{13}CO at $22''$ resolution and compared our prediction with the line ratios published by Mao et al. (2000). Note that the spatial smoothing of our high-resolution one-component excitation model leads to a multi-component model at lower resolution because it encompasses the individual solutions (weighted with a Gaussian of $22''$ width) at all positions. The predicted line ratios from a single CO isotope match the observations extremely well. For different CO isotopes the predicted line ratios are lower than suggested by the observations, but consistent within the observational errors. The predicted and observed line ratios are summarized in Table 3.

An independent chain of arguments favoring a temperature gradient towards the central starburst region comes from the different separation of the eastern and western “hot spots” in MIR and FIR observations. Hughes et al. (1994) stated that the larger separation of the peaks at $450 \mu\text{m}$ reflects the radial temperature gradient that must exist within the torus if the dust is heated by the central starburst population.

4.2. The state of the molecular gas in M 82’s center

Our study does not imply that the central part of M 82 does not contain dense molecular cloud cores as traced by other molecular species like HCN (see e.g. Seaquist et al. 1985; Brouillet & Schilke 1993). Most of the CO emission from the core of M 82, however, arises from a warm, low density interclump medium. This conclusion was already reached by Mao et al. (2000) using PDR models. The existence of such a gas component, which we can be confident of, raises the question if it can survive under the extreme conditions in the starburst center or whether it is indicative of cloud evaporation and thus of a destruction of molecular clouds. From the observed UV field

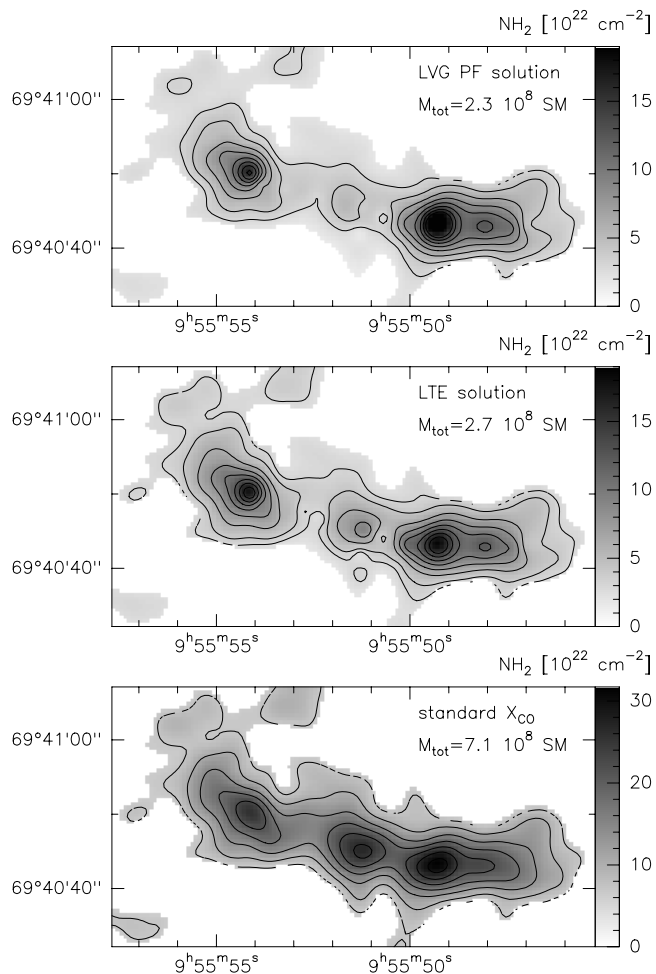


Fig. 12. H_2 column density maps calculated from the integrated $^{12}\text{CO}(J = 1 \rightarrow 0)$ intensity distribution at $4.2''$ resolution. The H_2 maps were derived using the X_{CO} distribution across the major axis of M 82 as calculated from the LVG_{PF} solutions (top), from the LTE solutions (middle) and from the standard Galactic X_{CO} conversion factor ($1.6 \cdot 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$) (bottom). The total H_2 mass is denoted in the upper right corner of each plot. Contour levels correspond to 1.4, 2, 3, 4, 6, 8, 10, 12, 14 and 16 10^{22} cm^{-2} (top), 3, 4, 6, 8, 10, 12, 14 and 16 10^{22} cm^{-2} (middle) and 7, 10, 14, 18, 22, 26 and 30 10^{22} cm^{-2} (bottom)

strength one would expect that the molecular clouds with densities less than 10^4 cm^{-3} cannot exist in M 82’s center (Brouillet & Schilke 1993). In addition, such a gas component is barely dense enough to avoid tidal disruption (Mao et al. 2000) which would support a rather diffuse distribution of the gas. Such a scenario would explain the high $[\text{C I}]/[\text{CO}]$ abundance ratios observed in M 82 (Schilke et al. 1993; White et al. 1994) and the depletion of H_2 in the central 300 pc of M 82. As a consequence, this would imply that the clouds are not virialized. This could explain why the linear correlation between $T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2}$ and X_{CO} is not valid for $T_{\text{kin}}^{-1} n(\text{H}_2)^{1/2} < 0.5$, hence for the warm and low-density gas in the starburst center (see Fig. 11). Therefore, there seems to be observational evidence that

Table 3. Line ratios for the high- J transition of ^{12}CO and ^{13}CO at the center and the eastern and western CO lobe of M 82. The line ratios are given for a spatial resolution of $22''$. The first row of each line ratio gives the value calculated from the LVG model. The second and third row are the observed peak and integrated line ratios adopted from Mao et al. (2000)

CO line ratio	east	center	west	
$^{12}\text{CO}(7\rightarrow 6)/^{12}\text{CO}(4\rightarrow 3)$	0.36	0.25	0.31	model
	0.32	0.29	0.37	peak
	0.28	0.36	0.33	integral
$^{12}\text{CO}(4\rightarrow 3)/^{13}\text{CO}(3\rightarrow 2)$	7.07	8.02	5.81	model
	8.50	10.1	9.07	peak
	9.09	6.88	7.40	integral
$^{13}\text{CO}(2\rightarrow 1)/^{13}\text{CO}(1\rightarrow 0)$	1.92	1.67	1.87	model
	1.53	1.63	1.93	peak
	1.47	1.44	1.17	integral
$^{12}\text{CO}(2\rightarrow 1)/^{13}\text{CO}(2\rightarrow 1)$	7.82	9.27	7.48	model
	9.04	13.7	9.19	peak
	11.4	14.2	11.7	integral

molecular clouds are partly disrupted and dissociated in the starburst center. More detailed numerical analysis of evaporation time scales and related questions are needed to settle this question.

4.3. X_{CO}

The suitability of a global Galactic factor X_{CO} to convert $^{12}\text{CO}(J = 1 \rightarrow 0)$ intensities to H_2 column densities has been discussed by many authors (e.g. Young & Scoville 1982; Bloemen et al. 1986; Hunter et al. 1997). As seen, theoretical studies of X_{CO} showed that it is sensitive to the kinetic temperature of the emitting gas and that the conversion factor should be lower for starburst galaxies like M 82 than for the Milky Way (Maloney & Black 1988). Investigations of X_{CO} in M 82 confirmed this prediction: Wild et al. (1992) used the optically thin $\text{C}^{18}\text{O}(2\rightarrow 1)$ transition to derive H_2 column densities and hence X_{CO} along the major axis of M 82. They found $X_{\text{CO}} \leq 1 \cdot 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ and variations by a factor of 2 along the major axis. Similar results were obtained by Smith et al. (1991) using the $450 \mu\text{m}$ continuum emission from dust grains to derive H_2 column densities. Even though both studies suggest a low conversion factor, its variation across the major axis shows significant differences. While Smith et al. (1991) found that X_{CO} decreases

from east to west, with no changes in the central star-forming regions, the results by Wild et al. (1992) suggest very low conversion factors near the eastern MIR peak and an increasing X_{CO} towards the western molecular lobe. Therefore our variations of X_{CO} in general support the results by Wild et al. (1992). Nevertheless our conversion factors are slightly lower than those inferred by Wild et al. (1992), and the location of the western X_{CO} maximum is displaced by $\approx 7''$. The discrepancies between the X_{CO} factors derived from the molecular lines (Wild et al. 1992 and this work) and the estimates from the dust emission might result from the single-temperature model used by Smith et al. (1991). In particular in the central region, which shows strong MIR emission from heated dust (Telesco & Gezari 1992), this might lead to an overestimate of the H_2 column density and thus to an overestimate of X_{CO} . Furthermore, the different morphology of the $450 \mu\text{m}$ map published by Hughes et al. (1994) raises doubts on the reliability of the $450 \mu\text{m}$ intensities used by Smith et al. (1991) for their calculation. From this we conclude that the X_{CO} factor in M 82 is not only lower than the standard Galactic conversion factor, but that in addition X_{CO} in the central 300 pc is at least 3 times lower than in the molecular lobes. A similar gradient for the conversion factor has been found in the Milky Way towards the Galactic Center (e.g. Blitz et al. 1985; Sodroski et al. 1994; Dahmen et al. 1998). Furthermore, our analysis suggests that the variations of X_{CO} are mainly caused by variations of the kinetic temperature of the CO-emitting volume due to environmental effects while abundance variations play a minor role.

5. Conclusions

We have observed the $^{12}\text{CO}(J = 2 \rightarrow 1)$ and $\text{C}^{18}\text{O}(J = 1 \rightarrow 0)$ emission lines in the starburst galaxy M 82 with high spatial resolution using the Plateau de Bure interferometer. Our main conclusions are:

- 1) The overall morphology and kinematics for both transitions are similar to those of $^{12}\text{CO}(J = 1 \rightarrow 0)$ and $^{13}\text{CO}(J = 1 \rightarrow 0)$ published by Shen & Lo (1995) and Neinger et al. (1998). The dynamical center of the molecular gas coincides with the $2.2 \mu\text{m}$ nucleus while the centroid of the molecular mass is located 100 pc west of M 82's center. South of the expanding molecular superbubble (Weiß et al. 1999) an outflow of molecular gas with a total mass of $7.2 \cdot 10^5 M_{\odot}$ is detected;
- 2) The $^{12}\text{CO}(J = 2 \rightarrow 1)/^{12}\text{CO}(J = 1 \rightarrow 0)$ line intensity ratios are lower (≤ 1.4) than previously reported. Thus, CO line ratios in M 82 are not outstanding, but comparable to values found in other starburst galaxies like NGC 253. Line ratios vary across the disk of M 82. Near the MIR peaks, the $^{12}\text{CO}(J = 2 \rightarrow 1)/^{12}\text{CO}(J = 1 \rightarrow 0)$

ratios are high; in the outer parts, that are less affected by the starburst, this ratio drops to unity;

3) An LVG excitation analysis of the CO lines suggests that the excitation conditions of the molecular gas are strongly influenced by environmental effects. In the outer parts of the CO distribution we find H_2 densities of $n(H_2) = 10^{3.5-4.2} \text{ cm}^{-3}$ and kinetic temperatures of $T_{\text{kin}} = 45-60 \text{ K}$. Towards the star-forming regions, indicated by strong MIR emission, the kinetic temperatures raise above 150 K. The hot gas is associated with low H_2 densities of only $n(H_2) = 10^{2.8-3.1} \text{ cm}^{-3}$. Area filling factors of $f_a = 0.2 - 0.4$ and volume filling factors of $f_v = 0.001 - 0.02$ indicate that the gas is organized in small clumps with a typical size of $r_{\text{cloud}} \approx 1 \text{ pc}$. $[^{12}\text{CO}]/[^{13}\text{CO}]$ abundance ratios are about 70 without significant spatial variations across the galaxy. In contrast, $[^{12}\text{CO}]/[\text{C}^{18}\text{O}]$ abundance ratios in the outer parts of M82 are comparable to those found at the Galactic Center ($[^{12}\text{CO}]/[\text{C}^{18}\text{O}] = 270$) but decrease to only $[^{12}\text{CO}]/[\text{C}^{18}\text{O}] = 160$ at the star-forming regions. Beam-averaged H_2 column densities range from $N(H_2)_{4''} = 2.4 \cdot 10^{22} \text{ cm}^{-2}$ near the MIR peaks to $N(H_2)_{4''} = 2.3 \cdot 10^{23} \text{ cm}^{-2}$ at the western CO lobe. The H_2 distribution has a double-peak morphology which surrounds the central starburst region. The central 300 pc are depleted in H_2 . Thus the H_2 distribution differs from the CO distribution. This result even holds when the H_2 column densities are calculated under the assumption of LTE conditions. The total molecular mass is $2.3 \cdot 10^8 M_{\odot}$;

4) The conversion factor from $I(\text{CO})$ to $N(H_2)$ (X_{CO}) depends on the excitation conditions of the CO-emitting volume. Even in regions which are less affected by the starburst X_{CO} is about 3 times lower than the standard Galactic value. From the LVG analysis we find that $X_{\text{CO}} \sim T_{\text{kin}}^{-1} n(H_2)^{1/2}$. Therefore X_{CO} is lower in the central star-forming regions than in the outer molecular lobes.

Appendix: Short-spacing correction

A major difficulty related to flux determinations from interferometer maps is the missing flux problem. In brief it arises from the lack of coverage at low spatial frequencies in interferometric observations. This leads to an insensitivity to emission more extended than $\lambda/S_{\text{min}}^{\text{proj}}$, where $S_{\text{min}}^{\text{proj}}$ is the length of the shortest projected baseline. The recovered flux therefore only represents clumpy parts of a brightness distribution which leads to an underestimate of the total flux of a source. For a more detailed description see e.g. Wilner & Welch (1994) and Helfer & Blitz (1995). The only way to overcome this problem is to derive the visibility at the origin of the uv -plane (which represents the integrated flux of a brightness distribution) and the low spatial frequencies from single-dish measure-

ments and combine them with the interferometric observations. Methods for the combination of single-dish and interferometer data have been described e.g. by Vogel et al. (1984) and Herbstmeier et al. (1996). Both methods generate the central visibilities from the single-dish data, as if they were measured with the interferometer. The combined visibility set is then processed in the standard interferometer reduction procedure. In this method the relative weight between single-dish and interferometer visibilities has a strong effect on the resulting brightness distribution. Furthermore the dirty image calculated from the combined visibility set still needs to be deconvolved using CLEAN or other deconvolution algorithms. In particular the CLEAN deconvolution algorithm is problematic for short-spacing corrected images because it fails on extended structures. We therefore used a different approach to combine the PdBI and 30 m telescope data.

The basic idea behind our method is that the missing flux problem only arises from an incorrect interpolation of the visibilities in the central part of the uv -plane ($\sqrt{u^2 + v^2} < \lambda/S_{\text{min}}^{\text{proj}}$). Therefore the missing flux problem in a finally reduced interferometer map can be solved by replacing the questionable part of the uv -plane by the values calculated from a single-dish map with identical extent, grid and flux units. This procedure avoids additional CLEANing on the combined data set and the choice of different weightings between interferometer and single-dish data. The requirement for the single-dish data is the same as described by Vogel et al. (1984). For the combination we regridded the single-dish data cube to the same spatial and velocity grid as the interferometer data. We then converted the flux units from T_{mb} to Jy/pixel using the Rayleigh-Jeans approximation, $S/\text{beam} = \frac{2k}{\lambda^2} T_{\text{mb}}$ and $\text{beam} = 1.133 f_s^2$ where f_s is the $FWHM$ of the 30 m telescope beam in units of the pixel size. The flux units of the CLEANed and primary beam corrected interferometer cube were also converted to Jy/pixel with $\text{beam} = 1.133 f_{i,\text{maj}} \cdot f_{i,\text{min}}$, where $f_{i,\text{maj}}$ and $f_{i,\text{min}}$ are the $FWHM$ of the major and minor axis of the clean beam in units of the pixel size. Furthermore we generated a model for the 30 m telescope main beam and the interferometer clean beam. The 30 m beam was assumed to be represented by a circular Gaussian with $FWHM = f_s$. The interferometric beam was described as a Gaussian with major and minor axis $f_{i,\text{maj}}$ and $f_{i,\text{min}}$. The normalization of both Gaussians was such that the amplitude of the visibility at the origin of the uv -plane was 1. We then transformed both data cubes and the model beams to the uv -domain using an FFT algorithm. The real and imaginary parts of the single-dish data were divided by the amplitudes of the model 30 m beam to deconvolve the single-dish visibilities from the 30 m telescope beam. In order to match the interferometer data the result was then multiplied by the amplitudes of the clean beam. At this stage of the combination the real and imaginary parts in the single-dish and interferometer data are comparable and the central interferometer pixels can be replaced by the single-dish values. The part of the uv -domain to be

Short-Spacing Correction

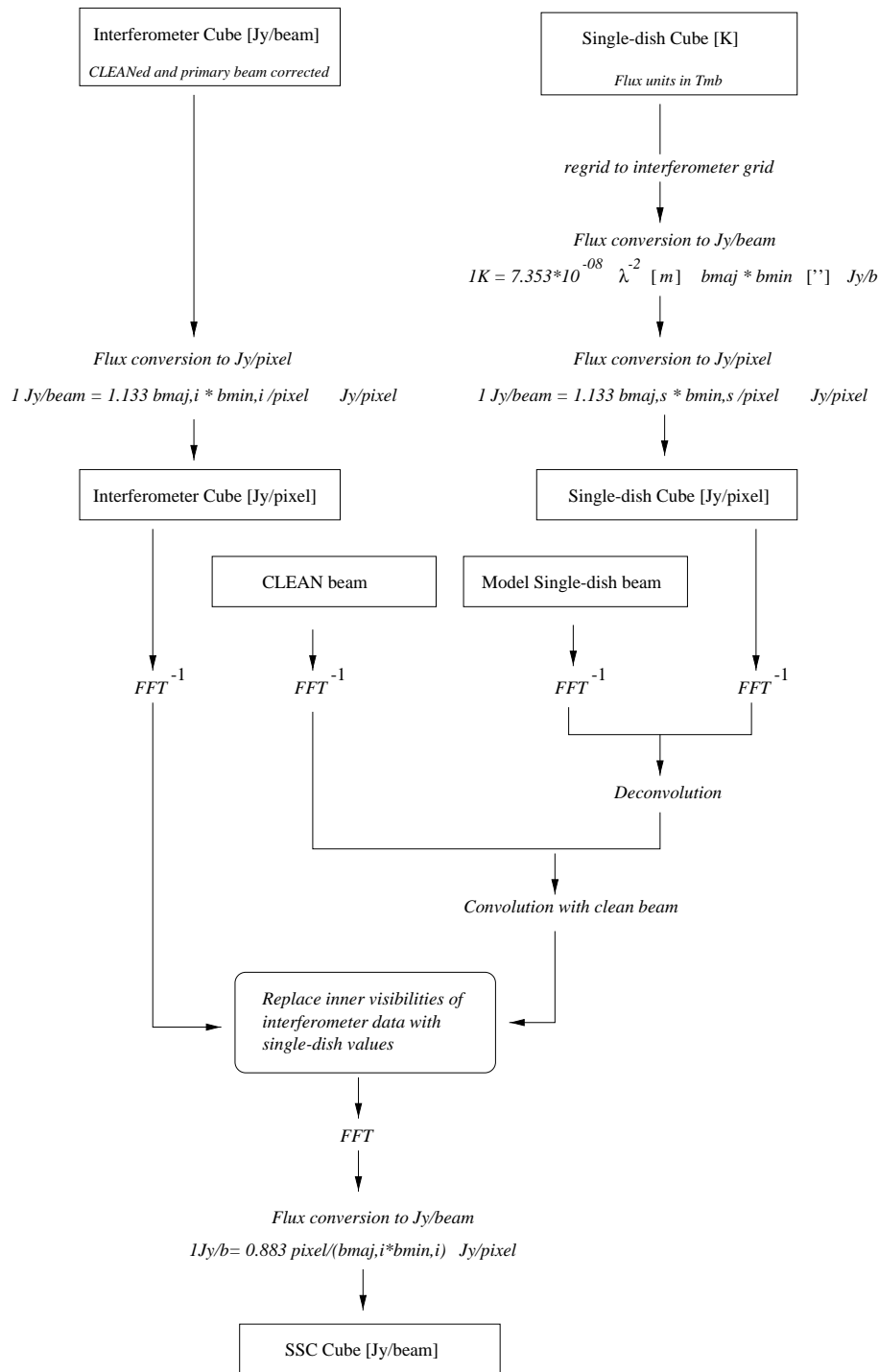


Fig. 13. Flow chart of the short-spacing correction

replaced by the single-dish values in general depends on the spacing of the shortest baseline and on the effective diameter of the single-dish telescope. For data sets with no overlap in the uv -domain we replaced the part that corresponds to the effective diameter of the 30 m telescope (amplitude of the visibilities for the 30 m beam model > 0.5). Otherwise we selected the part smaller than the shortest interferometer baseline. Finally the combined real and imaginary parts were transformed back to the image domain and the flux units were converted to Kelvin considering that the combined beam is equal to the clean beam.

Note that there are no free parameters in the combination of the data sets except for the choice which part of the uv -plane is replaced by the single-dish data. The methods require the knowledge of the single-dish beam pattern and the clean beam only. A flow chart for the Short-Spacing correction is given in Fig. 13.

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