

Research Article

The Effects of Air Preheating and Fuel/Air Inlet Diameter on the Characteristics of Vortex Flame

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The effects of fuel/air inlet diameter as well as air preheating on the flame stability, temperature distribution, pollutant formation, and combustion characteristics of a lab-scaled asymmetric vortex flame have been investigated. A three-dimensional steady-state finite volume solver has been used to solve the governing and energy equations. The solver uses a first-order upwind scheme to discretize the governing equations in the space. The semi-implicit method for pressure linked equations has been applied to couple the pressure to the velocity terms. Several turbulence models were applied to predict the flame temperature and it was found that $K-\epsilon$ RNG has given the best results in accordance with the experimental results. The results reveal that the inlet air diameter can enhance the thermal properties and reduce the NO_x emission while the inlet fuel diameter has less significant impact. Increasing diameters are accompanied with a pressure drop. It was found that preheating the air and fuel would significantly affect the flame temperature and NO_x emission with constant mass flow rate.

1. Introduction

Emissions of nitrogen oxides (NO_x) are allied with a range of environmental anxieties that include increasing ground level ozone, acidification of aquatic systems, forest damage, and formation of fine particles in the atmosphere [1–3]. These anxieties have resulted in a need to reduce emissions in various combustion systems. Vortex combustion has been known for its ability to improve flame stability and decrease NO_x formation [4, 5]. Vortex combustion is widely employed in furnaces and gas turbine combustors. Due to the wide industrial applications of vortex combustion, there has been a considerable amount of research on such flames, both premixed and nonpremixed. The first discussion of vortex flames was reported in 1998 by Gabler [6]. The turbulent vortex flame was described for the first time in such work by both experimental and computational methods. The major objective of

Gabler's work was to identify the possible reduction in pollutant formation from vortex flames. A concise description of the flame anatomy was presented, and some of the basic features of vortex flames were reported. These features include the enhanced stability near the lean flammability limit of the fuel and some primary temperature profiling. In previous studies, a description of the flame anatomy was presented, and some of the basic features of vortex flames were reported. These features include the enhanced stability near the lean flammability limit of the fuel and some primary temperature profiling [7, 8]. Recent issues in the vortex combustion could be found in modern gas turbines, which rely on premixed combustion to reduce NO_x emissions but are more sensitive to resonant coupling, leading to instability [9–11]. Gas turbine combustion dynamics have been considered in a series of articles edited by Lieuwen and Yang [12]. Effect of the oxygen concentration, preheating, pressure, and equivalence ratio

on the vortex flame characteristics of oxy-fuel flames, at an atmospheric pressure, showed that the percentage of O_2 in the oxidizer plays a crucial role in the flame stabilization. Flames with lower O_2 concentrations were seen to be more sensitive to stoichiometry and preheating temperatures [13]. Vortex interactions play a key role in many practical combustion applications by enhanced mixing, organize the flame region, and improve the flame stabilization process [14]. Around the lower stagnation point for partially premixed swirl flame with the lean blowout, the flame root is inherently unstable near lean blowout due to the presence of high strain rates, featuring frequent extinction and reigniting [15]. The lack of a strong recirculation zone and the shorter residence time within the low-swirl injector is a promising solution for attaining ultralow emissions in gas turbines [16]. Vortex flame is stabled by using cavity as flame holder which is essential for the better performance of the engine and more efficiency of combustion [17, 18]. The interplay of a vortex pair with a premixed flame provides an important model for premixed turbulent combustion. Investigation of this behavior has proven that the vortex not only stretches and strains the flame, but also scours material from the preheating region in front of the flame and at early times replaces it with inlet gases [19].

In the previous studies of vortex flows, the role of the air/fuel inlet as well as swirl number is underlined. Conditions giving increase to the central recirculation zone (CRZ) have been surveyed by Beer [20] and Gupta and Lilley [21], who found that this area is formed when the swirl number (S_n) exceeds a certain threshold, with a value of $S_n \geq 0.6$ given tentatively. Choi et al. [22] indicated that the CRZ resulted from a swirling flow instability that depends on the level of swirl, tube length, end conditions, and flow exothermicity. The precessing vortex core (PVC) rotates in the flow direction, and its frequency increases linearly with the flow velocity but does not necessarily coincide with the flow rotation rate [23]. The PVC modifies conditions of flame anchoring, and, under similar aerodynamic conditions, flame stabilization is improved by effectively enhancing hot gas recirculation [24, 25]. Saqr et al. [26] analyzed a low-emission combustion process based on the vortex flame concept by computational and experimental investigations of a turbulent asymmetric vortex flame. The three-dimensional reacting flow fields were described using a computational methodology where the $Re/k-\epsilon$ turbulence model and the Eddy-dissipation combustion model were implemented. The results have shown uniform trend for modified $k-\epsilon$ and standard $k-\epsilon$ and it is evident that the vortex flames for a nonpremixed combustion exhibit the characteristics of premixed flames in terms of color and temperature.

The major motivation of the present study is to discover some of the main characteristics of the reactive flow field of the asymmetric vortex flames such as effects of air/fuel inlet diameter and preheating air/fuel on the flame stability, temperature distribution, and pollutant formation. The paper has been motivated by two major concerns. The first concern is the recent growing global trends to reduce nitrogen emission from the industrial and power generation sectors. The second concern is the absence of complete understanding of the aerodynamic stability mechanism of vortex flames. Such

absence significantly impedes their practical utilization in different applications.

2. The Asymmetric Vortex Combustor

Based on the schematic of the combustor presented in Figure 1, the vortex combustor was designed to enhance the aerodynamics of vortex flames and create a strong vortex field for the flame stabilization. This concept has two inlets for air and two inlets for fuel. The allocation of each pair of air and fuel inlets was designed to allow the mixing between fuel and air to occur in the vicinity of a strong forced vortex field. Such vortex is created by the introduction of the air with a full tangential velocity component to the asymmetric combustor. The fuel and air inlet nozzles were circular in cross section with a diameter of 2 mm and 5 mm, respectively. The equivalence ratio was controlled by varying the inlet mass flow rate of air and fuel. Methane has been utilized as a fuel. Air and fuel flow rates were measured by columnar flowmeters, and the values were corrected to account for the inlet conditions of both pressure and gas density. Air was supplied at 2-bar pressure from a compressor equipped with a damping tank. Fuel was supplied from a pressurized tank at 2 bars.

3. Experimental Setup

The experimental stage was settled to allow direct photography from one plane and intrusive access of gas analyzer for emission and temperature measurements. A schematic of the experimental platform is shown in Figure 2. Air was delivered at 2 bars from a gush tank connected to a single stage reciprocating compressor, equipped with a pressure gauge and regulator. Methane was supplied at 2 bars from a pressurized cylinder. Two columnar flowmeters with flow-regulating screw from Cole-Palmer were used to measure the flow rate of fuel and air. Stretchy plastic plumbing was applied to connect the combustor chamber to the fuel-air supply system. A Sony 300 FPS digital camera was installed perpendicular to the outlet plane of the combustor to execute direct photographs for the flame. A TELEGAN Tempest-100 gas analyzer with a stainless steel probe was used to measure the emissions and temperature inside the combustor. To enable the axial movement of the probe, a traverse system was set.

4. Mathematical Model

4.1. Governing Equations. The three-dimensional steady-state Favre-averaged governing equations for mass, momentum, species transport, and energy in Cartesian coordinates are given as [27]

$$\frac{\partial \rho \tilde{u}_j}{\partial x_j} = 0,$$

$$\frac{\partial \rho \tilde{u}_i \tilde{u}_j}{\partial x_j} = -\frac{\partial P}{\partial x_i} + \frac{\partial}{\partial x_j} \left[(\mu + \mu_t) \left(\frac{\partial \tilde{u}_i}{\partial x_j} + \frac{\partial \tilde{u}_j}{\partial x_i} \right) \right],$$

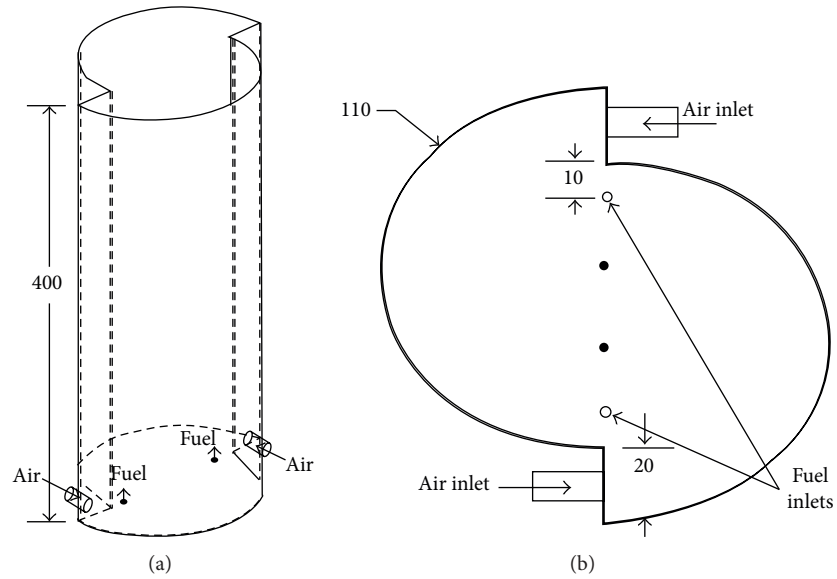
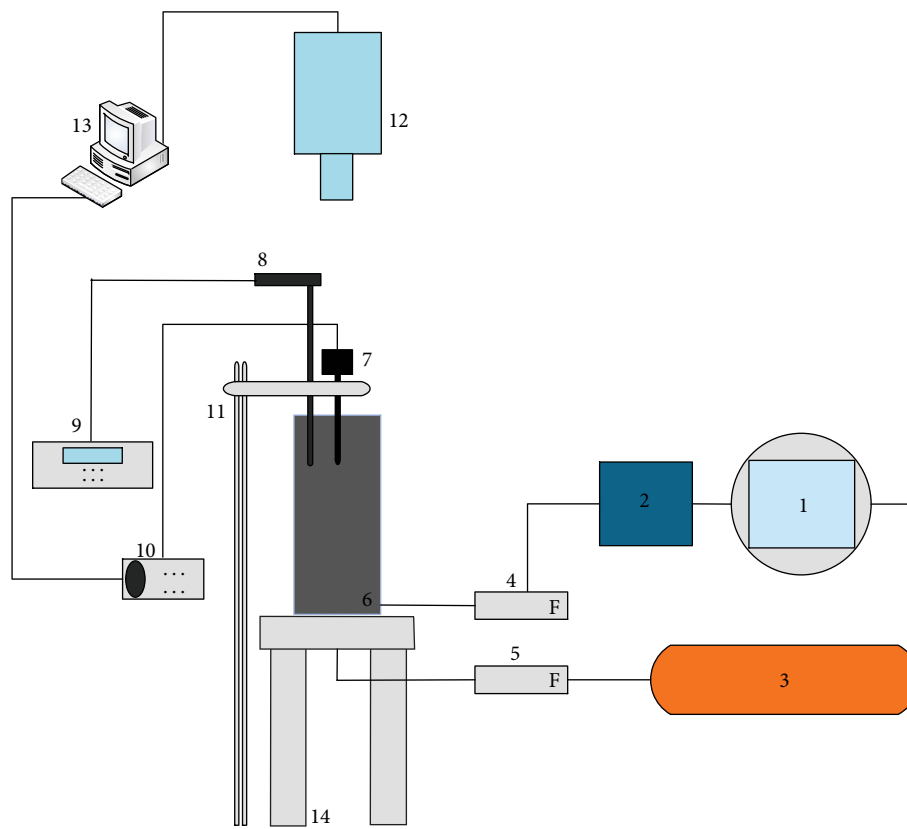


FIGURE 1: Schematic diagram of the asymmetric combustor: (a) isometric view and (b) top view; all dimensions are in mm.



- | | |
|---------------------------------|---------------------------------|
| (1) Air compressor | (8) TELEGAN gas analyzer probe |
| (2) Settling tank | (9) TELEGAN gas analyzer logger |
| (3) Pressurized fuel tank | (10) DAQ |
| (4) Air flowmeter | (11) Traverse system |
| (5) Fuel flowmeter | (12) Sony 300 fps video camera |
| (6) Asymmetric vortex combustor | (13) PC |
| (7) Thermocouple | (14) Support structure |

FIGURE 2: Schematic of the experimental setup of the asymmetric vortex combustor.

$$\begin{aligned} \frac{\partial \rho \tilde{u}_i \tilde{Y}_n}{\partial x_j} &= \frac{\partial}{\partial x_j} \left[\left(\rho D_n + \frac{\mu_t}{Sc_t} \right) \left(\frac{\partial \tilde{Y}_n}{\partial x_j} \right) \right] + \dot{\omega}_n, \\ \frac{\partial \rho \tilde{u}_j \tilde{H}}{\partial x_j} &= \frac{\partial}{\partial x_j} \left[\lambda \frac{\partial \tilde{T}}{\partial x_j} + \frac{\mu_t}{Pr_t} \frac{\partial \tilde{h}}{\partial x_j} + \sum_{n=1}^N \rho D_n h_n \frac{\partial \tilde{Y}_n}{\partial x_j} \right] \\ &\quad - \sum_{n=1}^N h_n^f \dot{\omega}_n, \end{aligned} \quad (1)$$

where ρ is the density, u_{ij} is the velocity vector components, P is the pressure, λ is the thermal conductivity, Pr_t is the turbulent Prandtl number, D_n is the mass diffusivity of species (n) which was assumed to be constant for each species, Y_n is the mass fraction of species (n), $\dot{\omega}_n$ is the chemical reaction rate, μ is the dynamic viscosity, and μ_t is the turbulent viscosity. \sim denotes the Favre averaging [28].

4.2. Numerical Procedures. A three-dimensional (3D) finite volume solver has been used to discretize the flow domain through a second-order upwind scheme. Several tetrahedron grids have been generated for ensuring that the solution is grid independent. The SIMPLE algorithm has been employed to achieve the mass conservation between the pressure and velocity terms in the discretized momentum equation. Chemical reaction has considered volumetric and Eddy-dissipation (ED) algorithm has been selected for turbulence-chemistry interactions. The ED reaction model ignores chemical kinetics (i.e., the Arrhenius rate) and uses only the parameters in reaction flow. The operating pressure and temperature were set to 1.01 bars and 300 K, respectively. The partial-equilibrium model is utilized to predict the O radical concentration required for thermal NO_x prediction. In all the simulations, a steady-state pressure based solver was used to solve the governing equations by CFD code ANSYS Fluent 14.0 [29].

The solution is considered to be converged when the residuals of each governing equation at consecutive iterations became less than 1×10^{-3} except for energy equation and chemical reactions equation which are converged at quantities less than 1×10^{-6} . At such condition, the flow field variables reached stable local values with respect to any number of iterations. Also, monitor for parameters of NO_x and temperature converged separately as well. This convergence criterion was applied on reacting flow cases. The equivalence ratio, air mass flow rate, and fuel mass flow rate in all cases are constant and equal to $\varphi = 0.97$, 0.0011 kg/s, and 6.45×10^{-5} kg/s, respectively. The dimensions of the computational domain were similar to the full-scale actual dimensions of the asymmetric vortex combustor illustrated in Figure 3.

4.3. Grid Testing and Model Validation

4.3.1. Grid Independence Test. A grid independence test was performed to evaluate the effects of grid sizes on the results as shown in Figure 4. Four sets of meshes were generated using tetrahedron elements with 211,606 nodes, 375,534 nodes,



FIGURE 3: Schematic diagram of the computational domain of asymmetric vortex chamber.

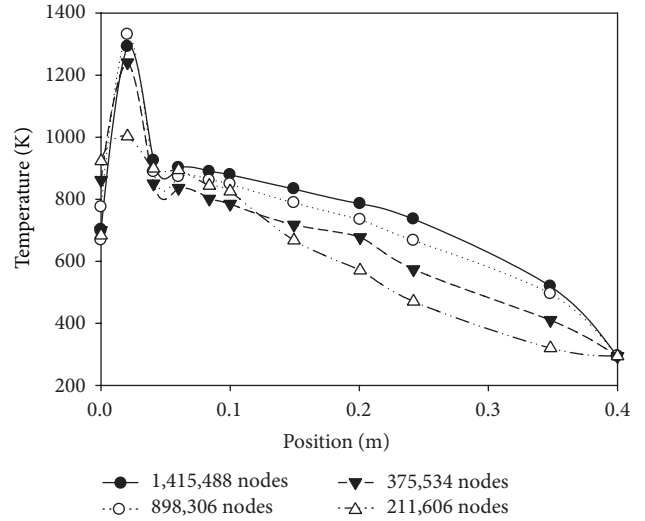


FIGURE 4: Grid independence test on the central temperature profile.

898,306 nodes, and 1,415,488 nodes. Laminar flow with counterflow configuration was considered for the fuel/oxidizer inlets at this test where the inlet air and fuel temperature were set at 300 K. It was observed that the 375,534 nodes and 898,306 nodes produce almost identical results along the chamber with a percentage error of less than 2%. Hence, a domain with 375,534 nodes was chosen to reduce the computing time.

4.3.2. Code Validation. The model validation was done based on the geometry and boundary conditions which were used by Wu et al. [7]. Air flows with a full tangential velocity component to the asymmetric combustor (300 K) and fuel flows coaxially with the center line (300 K). The mass flow rate for the air inlet was set to 0.0011 kg/s and the reacting case was performed at equivalence ratios of $\varphi = 0.974$. Six trials were performed with different turbulence models to compare with the experimental results. As can be seen in Figure 5, the central temperature profile is in good agreement with the experimental results when $k-\epsilon$ RNG was chosen as turbulence model. The code was further validated by comparing the other turbulence models' results with the experimental correlation developed by Saqr and Khaleghi [30, 31]. From Figure 5, it can be seen that the temperature values fall between the accepted ranges for $k-\epsilon$ turbulence model.

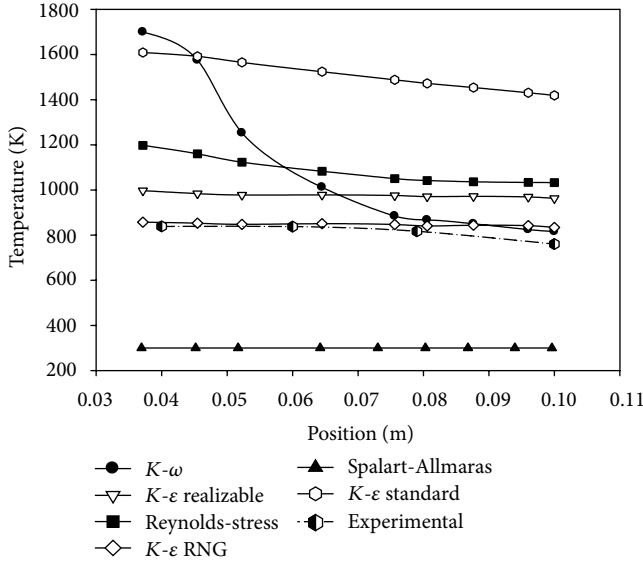
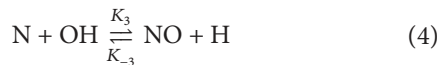
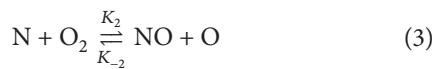
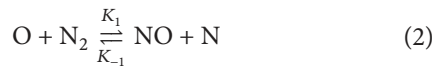


FIGURE 5: Comparison of the present results of central temperature profile along the chamber with the experimental result.

This figure clearly shows that Spalart-Allmaras could not estimate the vortex flame and also resulted in a fixed axis temperature of 300 K. It could be observed that $k-\epsilon$ turbulence model deviates significantly from the experimental results. Turbulence model of $k-\omega$ except for region near the end of chamber was not acceptable compared to the experimental results, while the error of Reynolds-stress model is low. It is noticed that $K-\epsilon$ realizable turbulence model had little error and $k-\epsilon$ RNG has good adjustment with the experimental results.

5. NO_x Formation Mechanisms

5.1. Thermal and Prompt NO_x. Oxygen and nitrogen in extremely high temperature can react inside the combustion furnace according to the following reactions which are called Zeldovich formulation [32]:



where K_1 , K_2 , and K_3 are forward rate constant and K_{-1} , K_{-2} , and K_{-3} are the reverse rate constants according to Table 1 [33]. Thermal NO_x formation is accelerated exponentially according to formula (5) at temperatures more than 1500°C [34, 35]:

$$K_i = A_i T^{B_i} \exp\left(\frac{-C_i}{T}\right). \quad (5)$$

TABLE 1: Thermal NO_x reaction rate constants [m³/gmol s].

K_1	$(1.8 \times 10^8) e^{-38370/T}$
K_{-1}	$(3.8 \times 10^7) e^{-425/T}$
K_2	$(1.8 \times 10^4) T e^{4680/T}$
K_{-2}	$(3.8 \times 10^3) T e^{-20820/T}$
K_3	$(7.1 \times 10^7) e^{-450/T}$
K_{-3}	$(1.7 \times 10^8) e^{-24560/T}$

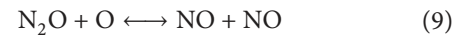
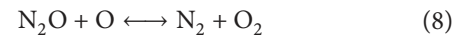
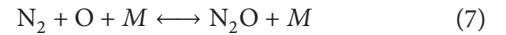
The rate of NO formation is achieved by formula (6) when the nitrogen radical (N) is assumed in steady-state conditions:

$$\begin{aligned} \frac{d[\text{NO}]}{dt} &= \frac{1}{1 + K_{-1}[\text{NO}] / (K_2[\text{O}_2] + K_3[\text{OH}] + 2K_1[\text{O}][\text{N}_2])} \\ &\times \left[-\frac{2K_{-1}}{K_2[\text{O}_2] + K_3[\text{OH}]} \times (K_{-2}[\text{O}][\text{NO}]) \right. \\ &\left. + K_{-3}[\text{H}][\text{NO}] \right], \quad (6) \end{aligned}$$

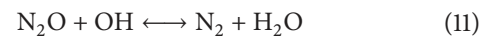
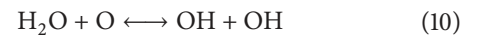
where T is temperature (K) and the reaction constants A_i , B_i , and C_i were taken from Fernando et al. [33]. As there are back-and-forth reactions, it can be seen that when the rate of reaction decreases, NO_x formation declines because combustion takes place in limited time in the furnace. Moreover, NO_x constitution mitigates in low temperatures.

Prompt NO_x formation mechanism was introduced by Fenimore in 1971. Prompt or Fenimore NO_x formation occurs in fuel rich conditions (equivalence ratio greater than 1.2) [36]. The rate of prompt NO_x constitution augments near equivalence ratio of 1.4 [37].

5.2. N₂O Intermediate NO Formation. Malte and Pratt [38] introduced N₂O intermediate NO formation mechanism which occurred in lean fuel, moderate temperatures, and low pressure combustion conditions. In these circumstances N₂O is converted to NO via the following formulas [39]:



According to Bédard and Cheng, the presence of H₂O impurities conspicuously affects the N₂O decomposition [40]:



In (7), M is general third body. N₂O which was constituted in (7) decomposes by (8) and (10). Equation (12) shows the chemical kinetics law for the rate of NO_x formation via N₂O intermediate mechanism:

$$\frac{d[\text{NO}]}{dt} = K'_5[\text{N}_2\text{O}][\text{O}] - K'_6[\text{NO}]^2. \quad (12)$$

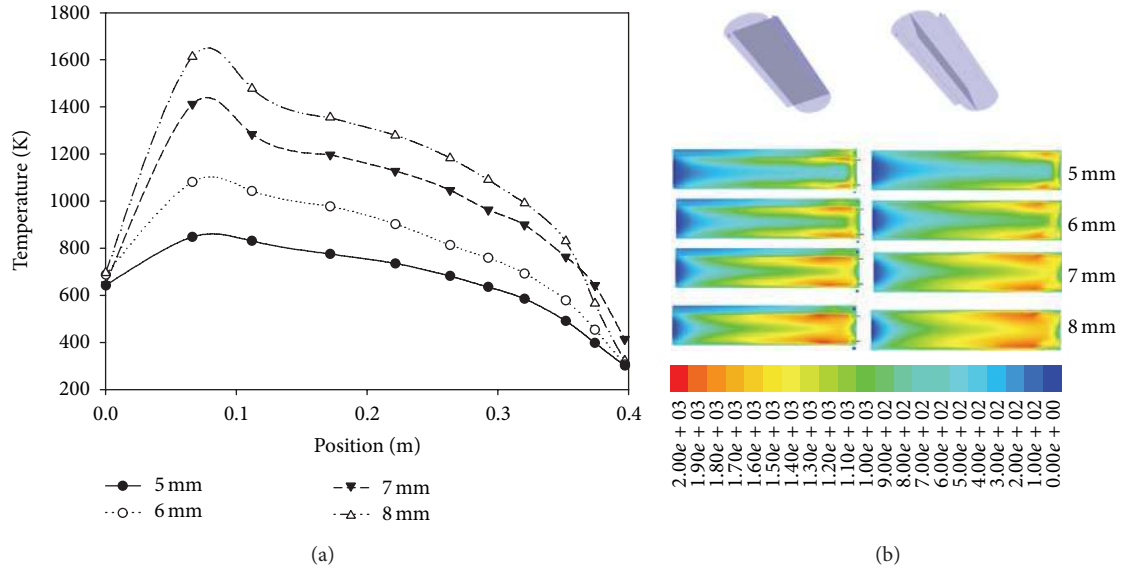


FIGURE 6: Effect of variations of air diameter on central temperature (K) profile: (a) line type and (b) contour type.

The reaction rate constants are calculated by

$$K'_i = K_0 T^\beta \exp\left(-\frac{E_a}{RT}\right). \quad (13)$$

If $d[\text{N}_2\text{O}]/dt = 0$ then (13) can be written as

$$\begin{aligned} & [\text{N}_2\text{O}] \\ &= \frac{[K'_1 [\text{N}_2] [\text{O}] [\text{M}] + K'_4 [\text{N}_2] [\text{O}_2] + K'_6 [\text{NO}]^2 + K'_8 [\text{N}_2] [\text{OH}]]}{K'_2 [\text{M}] + (K'_3 + K'_5) [\text{O}] + K'_7 [\text{H}]} \end{aligned} \quad (14)$$

The concentration of radicals like O, OH, and H affects the concentration rates and NO constitution [41]. N_2O intermediate NO formation increases in low oxygen concentration conditions [42].

5.3. Fuel-Bond NO_x Formation Mechanism. Fuel-bond NO_x formation mechanism occurs when the molecular structures of the fuel are constituted by nitrogen species. In the combustion of these fuels the nitrogen atoms are decomposed to intermediate products form which can react with NO_x [43].

6. Results and Discussion

6.1. The Influence of Inlet Air Diameter on the Characteristics of Vortex Combustion. The effect of inlet air diameter changing on the performance of vortex combustion is analyzed while the mass flow of fuel and air is kept constant. Therefore, the equivalence ratio was constant and equal to 0.974. Figure 6(a) depicts the effect of inlet diameter changing on the static temperature along the centerline with respect to the constant mass flow rate. The temperature increases along the central axis due to the heat released by reactions. For larger inlet air diameter, the temperature first sharply increases and then decreases along the axial direction. Figure 6(b) demonstrates the temperature contours on two various surfaces. There are

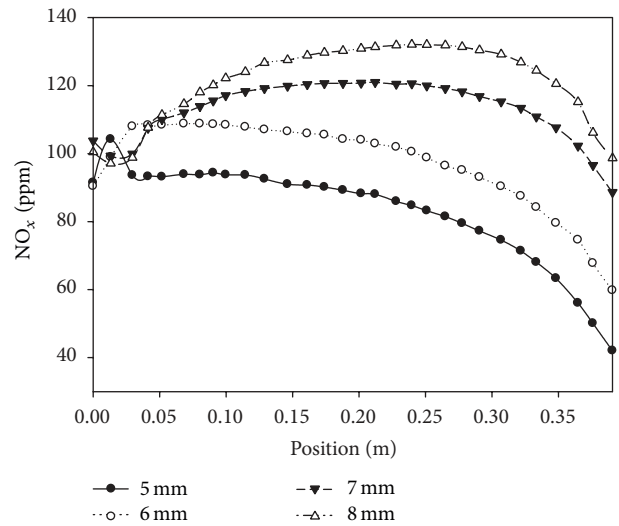


FIGURE 7: Effect of air diameter variation on the central NO_x profile.

obvious differences in these contours. From this figure, it can be interpreted that increasing in inlet air diameter with constant mass flow rate (decreasing inlet velocity) leads to increase in residence time. The decrease of speed of vortex flame and diffusion of flame to the center of chamber are the two original reasons of these changes.

The effect of diameter variation on the flame structure showed that the NO_x value on the centerline of the chamber increased when the inlet air diameter increased as shown in Figure 7. It should be noted that the NO_x concentration increased with the increase of air inlet diameter due to increase of the excess air and flame high temperature as shown in Figure 8 and Table 2. It is concluded that NO_x formation (Based on Zeldovich equations) is mainly controlled by temperature of combustion.

TABLE 2: Average outlet quantity of chamber.

Inlet air diameter	Average NO _x outlet	Average temperature outlet
5	72	470
6	82	500
7	95	535
8	98	568

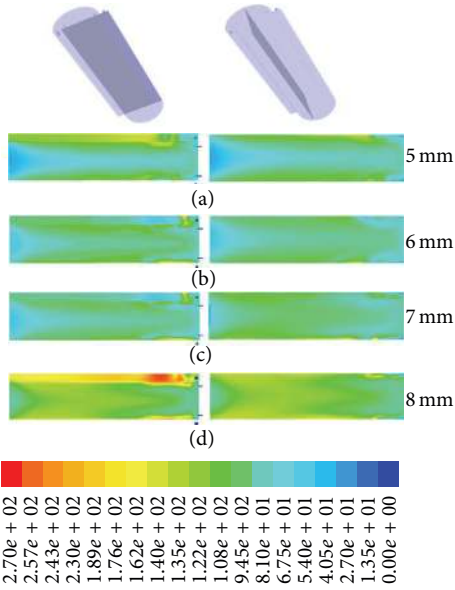


FIGURE 8: NO_x emissions (ppm) contour for different air diameters: (a) $d = 5$ mm, (b) $d = 6$ mm, (c) $d = 7$ mm, and (d) $d = 8$ mm.

6.2. *The Effect of Inlet Fuel Diameter on the Characteristics of Vortex Combustion.* Figure 9 illustrates the trend of NO_x formation and temperature distribution along with the chamber length with respect to the various fuel diameters (2, 2.5, 3, 3.5, and 4 mm). From this figure, it can be construed that the size of the fuel inlet has insignificant effect on the NO_x formation and static temperature. This shows that temperature flame as well as NO_x emission in the chamber has more effect on inlet air compared to inlet fuel; in other words, the inlet fuel velocity has negligible contribution to vortex flames compared to air inlet velocity.

6.3. *Preheating Air Effects.* Figure 10 shows temperature distribution and NO_x emissions formation when oxidizer is applied in four different air temperatures ($T = 300$ K, 400 K, 500 K, and 600 K) while the diameter of the air and fuel inlet, the mass flow rate of air and fuel inlet, and equivalence ratio are kept constant at 5 mm, 2 mm, 0.0011 kg/s, 6.45×10^{-5} kg/s, and 0.97, respectively. All of the predictions are performed at the same central axis location with the above discussed conditions. It was found that increasing the preheating air temperature and decreasing the air viscosity could limit the maximum flame temperature and improve the temperature

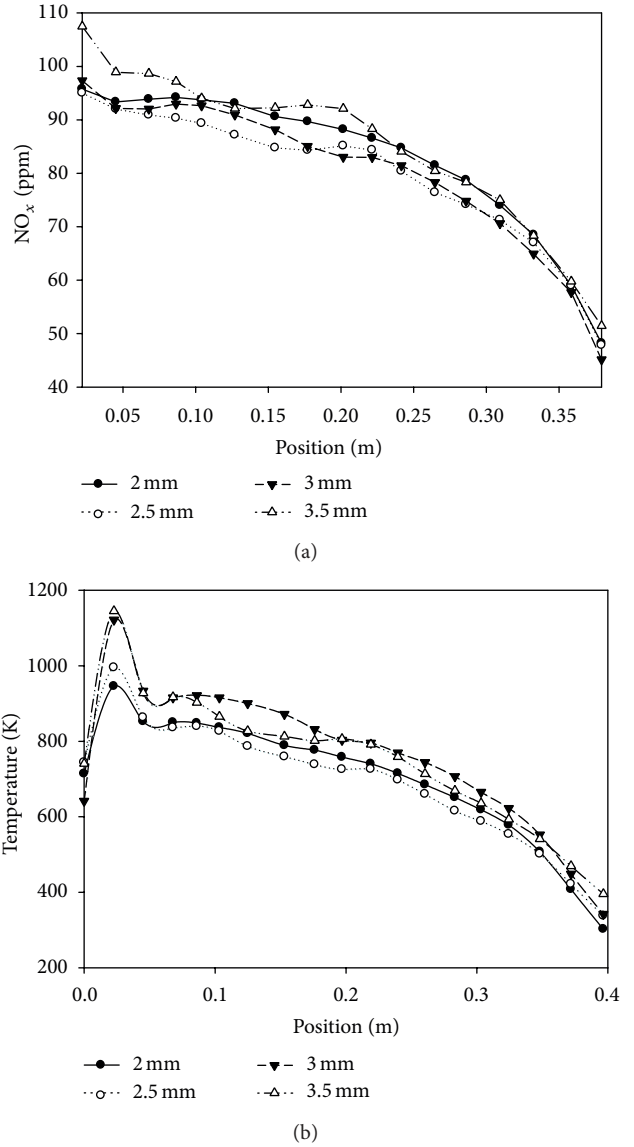


FIGURE 9: Effect of variations of fuel diameter on central (a) NO_x profile and (b) temperature profile.

uniformity in the furnace. The data shows that, with increasing preheating air at a constant mass flow rate, the flame location moves toward the air inlet because the momentum of the air stream decreases. Because the flame tends to approach the wall, the temperature along the central axis decreases with increase of air inlet temperature. As a result, the NO_x emission decreases when the flame temperature decreases.

6.4. *Preheating Fuel Effects.* Figures 11 and 12 show a minimum effect of preheating fuel on the flame characteristics such as static temperature and NO_x emissions. The temperature and oxygen mole fraction of air kept constant and equal to 300 K and 20%, respectively. It can be seen that the temperature along the central axis of the combustion chamber has no significant change with increasing of the fuel temperature. In

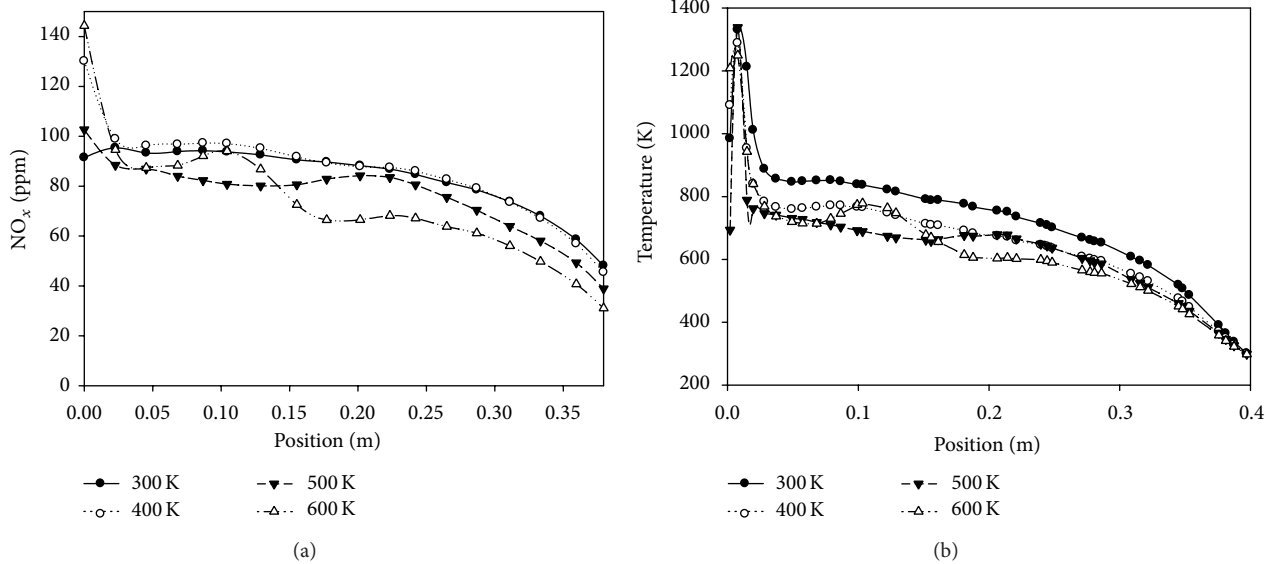


FIGURE 10: Effect of preheating air on the central (a) NO_x profile and (b) temperature profile.

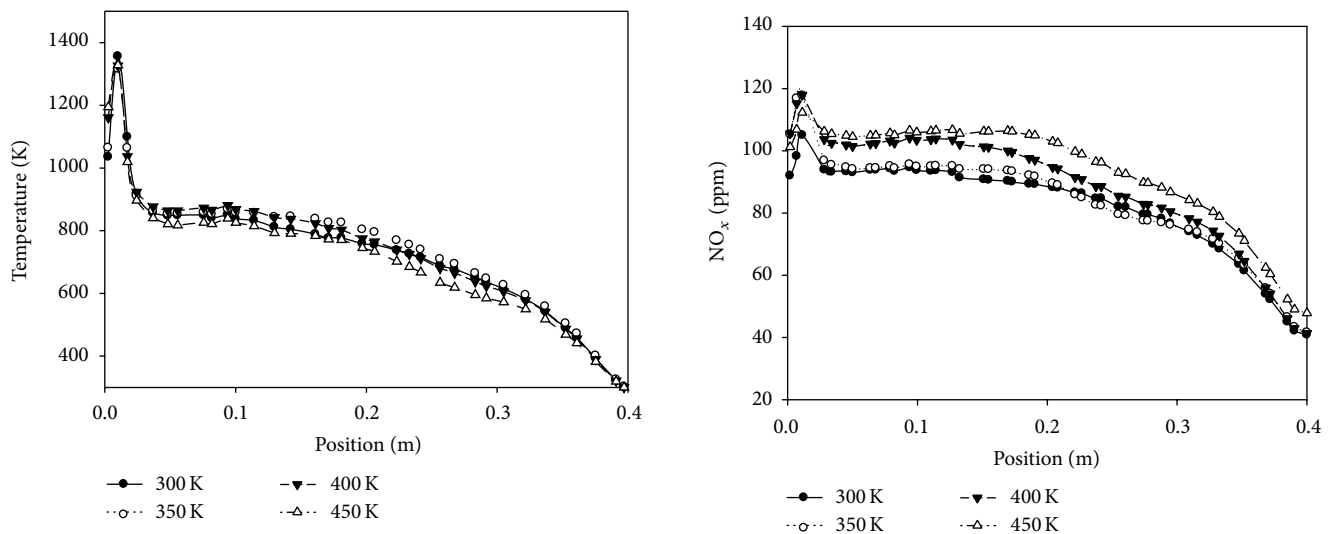


FIGURE 11: The effect of preheating fuel on the central temperature profile.

FIGURE 12: The effect of preheating fuel on the central NO_x profile.

addition, the results show that, at all fuel temperatures, the temperature decreases along the combustion chamber due to recession of flame and design of exhaust chamber. The maximum temperature is found in the vicinity of the bottom wall, where the fuel enters the combustion chamber. The results reveal that preheating inlet fuel has insignificant effect on the maximum flame temperature.

Figure 12 shows that the NO_x emission rises as the maximum flame temperature increases. With the increase of the fuel temperature at a fixed air flow rate there is a high temperature mixing in the flame zone, so there will be more thermal NO_x products with the fuel and increases in the temperature. The increased NO_x, caused by fuel preheating, is consistent with the hypothesis that preheating levels of 300 K, 500 K, and 700 K enhance fuel pyrolysis rates.

7. Conclusions

A computational study on the performance of asymmetric vortex flame for various inlet flow diameters (air and fuel) and effect of preheating air and fuel was analyzed. The results showed that increasing the inlet fuel diameter has negligible effect on the flame compared to effect of increasing inlet air to flame temperature and NO_x emission. The thermal field results show that the effect of preheating can attain low-emission NO_x as compared to fuel. It is found that increasing the preheated air temperature and fuel temperature could decrease the flame temperature and the combustion intensity and NO_x emission, when the air mass flow rate, fuel mass flow rate, and equivalence ratio were considered constant for all simulations. Increasing the air velocity due to preheated air

in constant mass flow rate and equivalence ratio is found to be an effective way to control the NO_x emission because of the decrease of the flame temperature.

Nomenclature

- d : Chamber diameter (mm)
 D_n : Mass diffusivity (m^2/s)
 L : Length of chamber (mm)
 m : Air and fuel mass flow rate (kg/s)
 p : Pressure (pa)
 Pr_t : Prandtl number
 Re : Reynolds number ($Re = \rho u d / \mu$)
 T : Temperature (K)
 u_{ij} : Velocity vector component (m/s)
 Y_n : Mass fraction of species n .

Greek Symbols

- λ : Thermal conductivity ($\text{W}/(\text{m}\cdot\text{K})$)
 μ : Dynamic viscosity ($\text{kg}/\text{m}\cdot\text{s}$)
 μ_t : Turbulent viscosity ($\text{kg}/\text{m}\cdot\text{s}$)
 ρ : Density (kg/m^3)
 φ : Equivalence ratio
 $\dot{\omega}_n$: Chemical reaction rate.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

References

- [1] S. E. Hosseini, M. A. Wahid, and A. A. A. Abuelnuor, "High temperature air combustion: sustainable technology to low NO_x formation," *International Review of Mechanical Engineering*, vol. 6, no. 5, pp. 947–953, 2012.
- [2] R. K. Srivastava, R. E. Hall, S. Khan, K. Culligan, and B. W. Lani, "Nitrogen oxides emission control options for coal-fired electric utility boilers," *Journal of the Air and Waste Management Association*, vol. 55, no. 9, pp. 1367–1388, 2005.
- [3] R. K. Srivastava, W. Neuffer, D. Grano, S. Khan, J. E. Staudt, and W. Jozewicz, "Controlling NO_x emission from industrial sources," *Environmental Progress*, vol. 24, no. 2, pp. 181–197, 2005.
- [4] M. Khaleghi, S. E. Hosseini, and M. Abdul Wahid, "Investigations of asymmetric non-premixed meso-scale vortex combustion," *Applied Thermal Engineering*, vol. 81, pp. 140–153, 2015.
- [5] D. Feikema, R. H. Chen, and J. F. Driscoll, "Enhancement of flame blowout limits by the use of swirl," *Combustion and Flame*, vol. 80, no. 2, pp. 183–195, 1990.
- [6] H. Gabler, *An Experimental and Numerical Investigation of Asymmetrically-Fueled Whirl Flames*, Princeton University, 1998.
- [7] M.-H. Wu, Y. Wang, V. Yang, and R. A. Yetter, "Combustion in meso-scale vortex chambers," *Proceedings of the Combustion Institute*, vol. 31, pp. 3235–3242, 2007.
- [8] M. Khaleghi, M. A. Wahid, M. M. Seis, and A. Saat, "Investigation of vortex reacting flows in asymmetric Meso scale combustor," *Applied Mechanics and Materials*, vol. 388, pp. 246–250, 2013.
- [9] K. R. McManus, T. Poinso, and S. M. Candel, "A review of active control of combustion instabilities," *Progress in Energy and Combustion Science*, vol. 19, no. 1, pp. 1–29, 1993.
- [10] S. Candel, "Combustion dynamics and control: progress and challenges," *Proceedings of the Combustion Institute*, vol. 29, no. 1, pp. 1–28, 2002.
- [11] Y. Huang and V. Yang, "Dynamics and stability of lean-premixed swirl-stabilized combustion," *Progress in Energy and Combustion Science*, vol. 35, no. 4, pp. 293–364, 2009.
- [12] T. C. Lieuwen and V. Yang, *Combustion Instabilities in Gas Turbine Engines: (Operational Experience, Fundamental Mechanisms, and Modeling)*, Progress in Astronautics and Aeronautics, American Institute of Aeronautics and Astronautics, 2005.
- [13] B. Kapadia and P. Kutne, "Combustion behavior of swirl stabilised oxyfuel flames at elevated pressure," in *Proceedings of the 9th AIAA Annual International Energy Conversion Engineering Conference (IECEC '11)*, AIAA-5593, San Diego, Calif, USA, July-August 2011.
- [14] P.-H. Renard, D. Thévenin, J. C. Rolon, and S. Candel, "Dynamics of flame/vortex interactions," *Progress in Energy and Combustion Science*, vol. 26, no. 3, pp. 225–282, 2000.
- [15] M. Stöhr, I. Boxx, C. Carter, and W. Meier, "Dynamics of lean blowout of a swirl-stabilized flame in a gas turbine model combustor," *Proceedings of the Combustion Institute*, vol. 33, no. 2, pp. 2953–2960, 2011.
- [16] M. R. Johnson, D. Littlejohn, W. A. Nazeer, K. O. Smith, and R. K. Cheng, "A comparison of the flowfields and emissions of high-swirl injectors and low-swirl injectors for lean premixed gas turbines," *Proceedings of the Combustion Institute*, vol. 30, pp. 2867–2874, 2005.
- [17] P. K. Ezhil Kumar and D. P. Mishra, "Numerical investigation of the flow and flame structure in an axisymmetric trapped vortex combustor," *Fuel*, vol. 102, pp. 78–84, 2012.
- [18] J. Yuan and I. Naruse, "Effects of air dilution on highly preheated air combustion in a regenerative furnace," *Energy & Fuels*, vol. 13, no. 1, pp. 99–104, 1999.
- [19] J. B. Bell, N. J. Brown, M. S. Day, M. Frenklach, J. F. Grcar, and S. R. Tonse, "The dependence of chemistry on the inlet equivalence ratio in vortex-flame interactions," *Proceedings of the Combustion Institute*, vol. 28, no. 2, pp. 1933–1939, 2000.
- [20] J. Beer, *Combustion Aerodynamics*, Combustion Technology: Some Modern Developments, 2012.
- [21] A. K. Gupta and D. G. Lilley, *Flowfield Modeling and Diagnostics*, Taylor & Francis, London, UK, 1985.
- [22] J. J. Choi, Z. Rusak, and A. K. Kapila, "Numerical simulation of premixed chemical reactions with swirl," *Combustion Theory and Modelling*, vol. 11, no. 6, pp. 863–887, 2007.
- [23] N. Syred, "A review of oscillation mechanisms and the role of the precessing vortex core (PVC) in swirl combustion systems," *Progress in Energy and Combustion Science*, vol. 32, no. 2, pp. 93–161, 2006.
- [24] M. Stöhr, I. Boxx, C. D. Carter, and W. Meier, "Experimental study of vortex-flame interaction in a gas turbine model combustor," *Combustion and Flame*, vol. 159, no. 8, pp. 2636–2649, 2012.
- [25] M. Stöhr, R. Sadanandan, and W. Meier, "Phase-resolved characterization of vortex-flame interaction in a turbulent swirl flame," *Experiments in Fluids*, vol. 51, no. 4, pp. 1153–1167, 2011.

- [26] K. M. Saqr, H. S. Aly, M. M. Sies, and M. A. Wahid, "Computational and experimental investigations of turbulent asymmetric vortex flames," *International Communications in Heat and Mass Transfer*, vol. 38, no. 3, pp. 353–362, 2011.
- [27] A. Obieglo, J. Gass, and D. Poulikakos, "Comparative study of modeling a hydrogen nonpremixed turbulent flame," *Combustion and Flame*, vol. 122, no. 1-2, pp. 176–194, 2000.
- [28] K. M. Saqr, M. M. Sies, and M. A. Wahid, "Numerical investigation of the turbulence-combustion interaction in nonpremixed CH₄/air flames," *International Journal of Applied Mathematics and Mechanics*, vol. 5, no. 8, pp. 69–79, 2009.
- [29] ANSYS, *ANSYS FLUENT User's Guide*, ANSYS, Canonsburg, Pa, USA, 2011.
- [30] K. M. Saqr, H. S. Aly, M. M. Sies, and M. A. Wahid, "Effect of free stream turbulence on NO_x and soot formation in turbulent diffusion CH₄-air flames," *International Communications in Heat and Mass Transfer*, vol. 37, no. 6, pp. 611–617, 2010.
- [31] M. Khaleghi, S. E. Hosseini, and M. A. Wahid, "Emission and combustion characteristics of hydrogen in vortex flame," *Jurnal Teknologi*, vol. 66, no. 2, pp. 47–51, 2014.
- [32] C. T. Bowman, "Kinetics of pollutant formation and destruction in combustion," *Progress in Energy and Combustion Science*, vol. 1, no. 1, pp. 33–45, 1975.
- [33] S. Fernando, C. Hall, and S. Jha, "NO_x reduction from biodiesel fuels," *Energy & Fuels*, vol. 20, no. 1, pp. 376–382, 2006.
- [34] W. C. Gardiner, Ed., *Gas-Phase Combustion Chemistry*, Springer, New York, NY, USA, 2000.
- [35] G. Lavoie, J. Heywood, and J. Keck, "Experimental and theoretical study of nitric oxide formation in internal combustion engines," *Combustion Science and Technology*, vol. 1, no. 4, pp. 313–326, 1970.
- [36] C. P. Fenimore, "Formation of nitric oxide in premixed hydrocarbon flames," *Symposium (International) on Combustion*, vol. 13, no. 1, pp. 373–380, 1971.
- [37] L. Pillier, A. El Bakali, X. Mercier et al., "Influence of C₂ and C₃ compounds of natural gas on NO formation: an experimental study based on LIF/CRDS coupling," *Proceedings of the Combustion Institute*, vol. 30, pp. 1183–1191, 2005.
- [38] P. C. Malte and D. T. Pratt, "Measurement of atomic oxygen and nitrogen oxides in jet-stirred combustion," pp. 1061–1070, 1975.
- [39] G. Löffler, V. J. Wargadalam, F. Winter, and H. Hofbauer, "Decomposition of nitrous oxide at medium temperatures," *Combustion and Flame*, vol. 120, no. 4, pp. 427–438, 2000.
- [40] B. Bédard and R. K. Cheng, "Experimental study of premixed flames in intense isotropic turbulence," *Combustion and Flame*, vol. 100, no. 3, pp. 485–494, 1995.
- [41] A. Khoshhal, M. Rahimi, and A. A. Alsairafi, "CFD study on influence of fuel temperature on NO_x emission in a HiTAC furnace," *International Communications in Heat and Mass Transfer*, vol. 38, no. 10, pp. 1421–1427, 2011.
- [42] W. Yang and W. Blasiak, "Mathematical modelling of NO emissions from high-temperature air combustion with nitrous oxide mechanism," *Fuel Processing Technology*, vol. 86, no. 9, pp. 943–957, 2005.
- [43] I. Glassman, *Combustion*, Academic Press, 1997.

