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Research Article

The Impact of Price Comparison Service on Pricing Strategy in a Dual-Channel Supply Chain

Qi Xu, Zheng Liu, and Bin Shen

School of Glorious Sun of Business and Management, Donghua University, 200051 Shanghai, China

Correspondence should be addressed to Zheng Liu; liuzheng960@163.com

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Recently, price comparison service (PCS) websites are more and more popular due to its features in facilitating transparent price and promoting rational purchase decision. Motivated by the industrial practices, in this study, we examine the pricing strategies of retailers and supplier in a dual-channel supply chain influenced by the signals of PCS. We categorize and discuss three situations according to the signal availability of PCS, under which the optimal pricing strategies are derived. Finally, we conduct a numerical study and find that in fact the retailers and supplier are all more willing to avoid the existence of PCS with the objective of profit maximization. When both of retailers are affected by the PCS, the supplier is more willing to reduce the availability of price information. Important managerial insights are discussed.

1. Introduction

Price is one of the key competitive dimensions of purchasing a product. As consumers are eager to have access to the better price information in the market, price comparison service (PCS) is naturally born. The PCS provides specific product information and price differences for consumer's reference [1]. By checking the PCS, consumers are able to compare prices with other retailers and make better decisions [2, 3]. For example, Skyscanner, an online air ticket price comparison website, helps online consumers to compare flight prices of any given route over a month period among different airline and agents. More examples of PCS are summarized in Table 1. According to Table 1, products shown in the PCS include air ticket, hotel, fashion, home product, computer, and electronics. One observation from Table 1 is noteworthy: all products shown in PCS are under fierce price competition.

Price differences and price fluctuations exert an impact on the decision making among consumers and supply chain parties. Huang and Swaminathan [4] compare various products from Amazon and BELK and find that there exists price difference under an online duopoly environment. This observation motivates us to explore the pricing strategy with consideration of PCS. Serenko and Hayes [3] state that the PCS offers tremendous benefits for consumers who may

potentially receive lower prices and for online vendors (i.e., retailer), who may not only capture more price information of their rivals but also get more exposure for their brands.

Pricing issues have been extensively studied by the scholars of supply chain; however, the impact of PCS has rarely been investigated. In this study, we first examine how the signals of PCS affect the decision making of supply chain members in a dual-channel supply chain. More specifically, we mainly develop a model with consideration of PCS and assume that supplier's pricing decision is affected by the PCS, while the retailers' pricing decision can be divided into three situations: (i) neither of retailers is affected by the PCS; (ii) either of retailers is affected by the PCS; and (iii) both of retailers are affected by the PCS. According to the three situations mentioned above, we derive the optimal pricing decision of supply chain parties in such a dual-channel supply chain, and our numerical results show that the best strategies for the retailers and supplier are to avoid the existence of PCS. In addition, we find if both of the retailers are affected by the PCS, the supplier should tend to reduce the availability of price information, and if either of retailers is affected by the PCS, the retailer should tend to exclusively cooperate with

The paper is organized as follows. We show the related literature in Section 2. The model is presented in Section 3,

TABLE 1: Examples of PCS [3].

Name	URL	Products
Become	http://www.become.com/	Fashion, electronics, home, and so forth
BizRate	http://www.bizrate.com/	Fashion, electronics, home, and so forth
Boxz	http://www.boxz.com/	Mobile phones
Eprice	http://www.eprice.com.hk/	Electronics
MySimon	http://www.mysimon.com/	Fashion and computer
PriceGrabber	http://www.pricegrabber.com/	Computer and electronics
Shopping	http://www.shopping.com/	Fashion, electronics, home, and so forth
Shopzilla	http://www.shopzilla.com/	Fashion, electronics, home, and so forth
Smarter	http://www.smarter.com/	Fashion, electronics, home, and so forth
Skyscanner	http://www.skyscanner.com/	Air ticket and hotel

and we obtain the optimal retail prices on both channels under vertically competition in Section 4. In Section 5, we study the supplier's pricing strategies when facing two competing retailers. We further conduct numerical studies to investigate the impact of PCS on pricing and expected profit among supply chain parties in Section 6. Finally, conclusion is presented in Section 7.

2. Literature Review

In the last decade, researchers have studied many issues related to the dual-channel supply chain with traditional and internet channel (please refer to [5, 6] for more discussions and review). More recently, Yao and Liu [7] study the pricing competition between retail and e-tail distribution channels under the Bertrand and the Stackelberg price competition models. Interestingly, they find that an optimal wholesale price exists under a different market structure in which the retailer is encouraged to accommodate the additional e-tail channel. Cai [8] examines the impact of channel structure on various supply chain parties with and without coordination under a dual-channel supply chain. Chen et al. [9] investigate the contracting strategies in a dual-channel supply chain. According to their results, the wholesale price contract could coordinate the dual-channel supply chain.

Pricing is popularly investigated in supply chain management, particularly in the dual-channel supply chain [10]. An early research, conducted by Ingene and Parry [11], discusses the case of a single manufacturer selling an identical product to two competing retailers with a linear quantity discount schedule and a two-part tariff. Ingene and Parry claim that coordination is not always in the manufacturer's interest when retailers are competing. Chiang et al. [12] also examine a price competition game in a dual-channel supply chain. They find that a direct channel strategy could lead the manufacturer to be more profitable by posing a viable threat to draw

customers away from the retailer. Huang and Swaminathan [4] investigate the pricing strategies in a dual-channel supply chain by assuming a stylized deterministic demand model. Under such demand function, the retailers tend to set a higher retail price in order to make more profit. Recently, Tang and Xing [13] compare the pricing behavior between online branches of traditional retailers and pure internet retailers. They conclude that the price charged by pure e-tailers for DVD titles is 14% lower than those charged by e-tailers with traditional channels. From the marketing perspective, price comparison can affect buyer's perceptions of acquisition value, transaction value, and behavioral intentions [2]. The impact of PCS on pricing decision is thus inevitable.

The service is significantly important for supply chain management. Dumrongsiri et al. [14] consider the impact of retailer's service quality on a dual-channel supply chain in which a manufacturer sells to a retailer as well as to consumers directly. They reach an interesting conclusion that a higher retailer's service quality may lead to a higher manufacturer's profit in a dual-channel supply chain. Dan et al. [15] examine the retail services in a centralized and a decentralized dual-channel supply chain using the twostage optimization technique and Stackelberg game. Their results imply that retail services could strongly influence the manufacturer and the retailer's pricing strategies. In this paper, we examine the impact of PCS on a dual-channel supply chain. PCS is new to the literature of supply chain management, although it has been largely explored in the area of electronic business [1, 3].

The signals of PCS are closely related to information availability, namely, information asymmetry or symmetry. However, information asymmetry has been largely discussed in the literature of supply chain management. Desiraju and Moorthy [16] study information asymmetry regarding a price- and service-sensitive demand curve. They show that the coordination can be achieved by requiring service performance. Cakanyildirim and Sethi [17] find that information asymmetry regarding a manufacturer's production cost does not necessarily cause inefficiency in supply chain. Mukhopadhyay et al. [18] examine the mixed channels under information asymmetry and propose retailer to add differentiated value to the product so as to eliminate the possibility of channel conflict. In this study, we consider both information asymmetry and symmetry cases.

3. The Model

In this paper, we consider a dual-channel supply chain system in which one supplier provides the products to two retailers at the same wholesale price, and then two retailers (e.g., Wal-Mart and Amazon) sell products to consumers. Here, we consider one retailer is a physical retailer and the other is an online retailer (As a remark, the physical retailer and the online retailer may or may not be homogenous due to the signal availability of PCS. The heterogeneous structure has particularly happened in the scenario that either of retailers is affected by the PCS). To simplify, the two retailers are referred as retailer1 and retailer2. We consider the retail

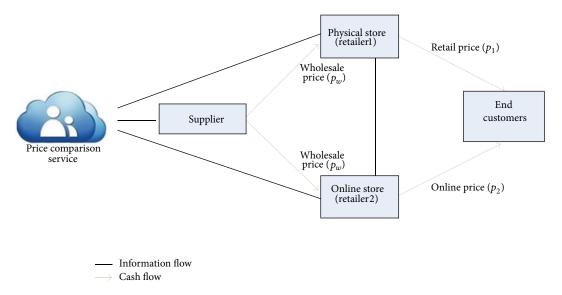


FIGURE 1: Dual-channel supply chain system with PCS.

prices are public information for every party in this supply chain system. All parties face the risk of price competition brought by price comparison service (PCS) (The PCS is a third party who is independent with all parties in such a supply chain), which positively affect their pricing decisions. The sequence of events is as follows. First, supplier decides wholesale price. Second, based on the wholesale price offered by supplier, both retailer1 and retailer2 determine the retail price simultaneously. As a remark, all decisions made by supply chain parties might be influenced by the PCS. This game is analyzed by using backward induction technique. This dual-channel supply chain with the PCS is depicted in Figure 1.

3.1. Notations

 D_1, D_2 : Market demand for retailer1 and retailer2

D_s: Market demand

 p_w : Wholesale price offered by supplier

 p_1 , p_2 : Retail prices decided by retailer1 and retailer2

d: Market size base

α: Demand sensitivity for retailerl's market price

 β : Demand sensitivity for retailer2's market price

 μ : Impact of PCS on demand, which follows a normal distribution $\mu \sim N(0, \sigma)$

 x_0, x_1, x_2 : Impact of PCS on pricing decision determined by supplier, retailer1, and retailer2, respectively

 θ_m, δ_m : Adjusted coefficients of retail pricing, $m \in 1, 2, 3, 4$

 λ_0 , λ : Adjusted coefficients of wholesale pricing.

3.2. Basic Model. Without any loss of generality, we consider that the demand curve in the dual-channel supply chain is

a linear function of the selling price, where $\mu \sim N(0, \sigma^2)$ is a random parameter to represent random uncertain information [19]. The function of market demand is expressed as follows:

$$D_i(p_i, p_i, \mu) = d_i - \alpha p_i + \beta p_i + \mu, \tag{1}$$

where $i, j \in (1, 2), i \neq j$, and d, α, β are constants.

Supply chain parties might enable to receive the signal of PCS. We denote x_0 , x_1 , and x_2 as the degree of PCS signal the supplier and two retailers received, respectively. According to the degree of signal, the parties would make price adjustment, and the adjusted price will in turn affect the market demand. Assuming $x_i = \mu + \varepsilon_i$, both μ and ε_i are independent random variables, where ε_i follows normal distribution with mean of η , $(\eta > 0)$ and variance of ε_i , $i \in 0, 1, 2$. Covariance matrix of ε_i can be denoted as $\Sigma = \text{diag}(\sigma, s_0, s_1, s_2)$. For example, if the price comparison exerts greater impact on retailerl, then the retailer1 will adjust its price, which will cause decrease in demand; while if the impact is much less, then the retailer1 will tend to keep the price stable, which will not affect the market demand. Prices offered by the supplier and retailers are functions of x_0, x_1, x_2 , namely, $p_w = f_0(x_0)$ and $p_i =$ $f_i(x_i)$.

Supplier adjusts its wholesale price based on the signal of PCS. However, due to asymmetry of transmission, the retailers may or may not be affected by the PCS. Here, we divide it into three situations accordingly.

Situation 1. The supplier does not share price comparison information x_0 with both of the retailers, namely, neither of retailers are not affected by the PCS information x_0 directly. Instead, they are able to adjust retail price based on respective price comparison x_i as well as wholesale price p_w . The adjusted retail price hence is $p_i = \theta_1 + \theta_2 x_i + \theta_3 p_w$, $i \in 1, 2$.

Situation 2. PCS information x_0 exerts impact on either of retailers, then the one who is affected by x_0 will adjust its price

and the corresponding retail price is $p_i = \theta_1 + \theta_2 x_i + \theta_3 p_w + \theta_4 x_0$, i = 1 or i = 2.

Situation 3. PCS information x_0 exerts impact on both of retailers, namely, retailers make pricing decisions based on x_0 and x_i . The adjusted retail price is $p_i = \theta_1 + \theta_2 x_i + \theta_3 p_w + \theta_4 x_0$, $i \in 1, 2$.

4. Retail Pricing Strategy

4.1. Neither of Retailers Is Directly Affected by x_0 . We consider the supplier is affected by price comparison x_0 , and its updated wholesale pricing strategy is

$$p_w = \lambda_0 + \lambda x_0, \tag{2}$$

where λ_0 , λ are price coefficients (see [20]). In this subsection, we consider that the supplier does not share information with the two retailers who are only affected by x_1 and x_2 , respectively. The updated pricing strategies of the two retailers are hence as follows:

$$p_1 = f_1(x_1, p_w) = \theta_1 + \theta_2 x_1 + \theta_3 p_w, \tag{3}$$

$$p_2 = f_2(x_2, p_w) = \delta_1 + \delta_2 x_2 + \delta_3 p_w. \tag{4}$$

Assume that the competitive relationship between the two retailers who are well-matched in strength and the impact of PCS on each retailer are equal. Then, the expected demand of retailer1 can be expressed as:

$$E(\mu \mid x_1, x_0) = \frac{\sigma s_0 x_1 + \sigma s_1 x_0}{\sigma s_1 + \sigma s_0 + s_1 s_0}.$$
 (5)

According to the above assumption, the formula can be further described as:

$$E(\mu \mid x_1, p_w) = E(x_2 \mid x_1, p_w)$$

$$= \frac{\sigma s_0 x_1 \lambda + \sigma s_1 (p_w - \lambda_0)}{(\sigma s_1 + \sigma s_0 + s_1 s_0) \lambda},$$
(6)

and the expected demand of retailer2 can be expressed as:

$$E(\mu \mid x_2, p_w) = E(x_1 \mid x_2, p_w)$$

$$= \frac{\sigma s_0 x_2 \lambda + \sigma s_2 (p_w - \lambda_0)}{(\sigma s_2 + \sigma s_0 + s_2 s_0) \lambda}.$$
(7)

In addition, the signal of PCS is symmetric for both retailers; the expected prices of retailer1 and retailer2 are

$$E(p_2 \mid x_1, p_w) = \delta_1 + \delta_2 E(x_2 \mid x_1, p_w) + \delta_3 p_w,$$
 (8)

$$E(p_1 \mid x_2, p_w) = \theta_1 + \theta_2 E(x_1 \mid x_2, p_w) + \theta_3 p_w.$$
 (9)

Then, the expected profits of retailer1 and retailer2 are expressed as:

$$E(\Pi_{1} \mid x_{1}, p_{w}) = [d_{1} - \alpha p_{1} + \beta E(p_{2} \mid x_{1}, p_{w}) + E(\mu \mid x_{1}, p_{w})](p_{1} - p_{w}),$$
(10)

$$E(\Pi_{2} \mid x_{2}, p_{w}) = [d_{2} - \alpha p_{2} + \beta E(p_{1} \mid x_{2}, p_{w}) + E(\mu \mid x_{2}, p_{w})](p_{2} - p_{w}).$$
(11)

Proposition 1. When neither of retailers is influenced by the supplier price comparison impact x_0 , the profit functions $E(\Pi_1 \mid x_1, p_w)$ and $E(\Pi_2 \mid x_2, p_w)$ are strictly concave in p_1 and p_2 , respectively, namely, the optimal retail prices p_1^* and p_2^* uniquely exist.

To enhance the presentation, all proofs are relegated to the Appendices.

By solving the first-order derivative of p_1 in $E(\Pi_1 \mid x_1, p_w)$ and p_2 in $E(\Pi_1 \mid x_1, p_w)$, respectively, one can have optimal retail pricing strategies of retailer1 and retailer2 in this situation as follows:

$$p_{1}^{*} = \frac{1}{2\alpha} \left[d_{1} + \alpha p_{w} + \beta E \left(p_{2} \mid x_{1}, p_{w} \right) + E \left(\mu \mid x_{1}, p_{w} \right) \right],$$

$$p_{2}^{*} = \frac{1}{2\alpha} \left[d_{2} + \alpha p_{w} + \beta E \left(p_{1} \mid x_{2}, p_{w} \right) + E \left(\mu \mid x_{2}, p_{w} \right) \right].$$
(12)

By solving (2)–(12) simultaneously, one finds θ_i , i = 1, 2, 3, 4 and δ_i , i = 1, 2, 3. Consider

$$\begin{split} \theta_{1} &= \frac{1-t}{2-t} \\ &- \left(\left(2\sigma \left(1-t^{2} \right) \left[4\left(\left(\frac{1}{\alpha+\beta} - d \right) s_{1}k_{2} + 2ds_{2}k_{1} \right) \right. \right. \\ &+ d\sigma s_{0} \left(2s_{1} + ts_{2} \right) \right] \right) \\ &\times \left(V\left(4-t^{2} \right) \right)^{-1} \right), \\ \theta_{2} &= \frac{\sigma s_{0} \left(1-t^{2} \right) \left[\left(2/\left(\alpha+\beta \right) - 2d \right) k_{2} + d\sigma s_{0} \right]}{V}, \\ \theta_{3} &= \frac{1}{2-t} \\ &- \left(\left(2\sigma \left(1-t^{2} \right) \left[4\left(\left(\frac{1}{\alpha+\beta} - d \right) s_{1}k_{2} + 2ds_{2}k_{1} \right) \right. \right. \\ &+ d\sigma s_{0} \left(2s_{1} + ts_{2} \right) \right] \right) \\ &\times \left(V\left(4-t^{2} \right) \right)^{-1} \right), \\ \delta_{1} &= \frac{1-t}{2-t} \\ &- \left(\left(2\sigma \left(1-t^{2} \right) \left[4\left(\left(\frac{1}{\alpha+\beta} - d \right) s_{2}k_{1} + 2ds_{1}k_{2} \right) \right. \right. \\ &+ d\sigma s_{0} \left(2s_{2} + ts_{1} \right) \right] \right) \\ &\times \left(V\left(4-t^{2} \right) \right)^{-1} \right), \end{split}$$

$$\delta_{2} = \frac{\sigma s_{0} \left(1 - t^{2}\right) \left[\left(2/\left(\alpha + \beta\right) - 2d\right) k_{1} + d\sigma s_{0}\right]}{V},$$

$$\delta_{3} = \frac{1}{2 - t}$$

$$-\left(\left(2\sigma \left(1 - t^{2}\right) \left[4\left(\left(\frac{1}{\alpha + \beta} - d\right) s_{1} k_{1} + 2d s_{2} k_{2}\right) + d\sigma s_{0} \left(2s_{2} + t s_{1}\right)\right]\right)$$

$$\times \left(V\left(4 - t^{2}\right)\right)^{-1},$$
(13)

where $t = \beta/\alpha$, $d_1 = d_2 = d/2$, $k_1 = (\sigma + s_0)s_1 + \sigma s_0$, $k_2 = (\sigma + s_0)s_2 + \sigma s_0$, and $V = 4k_1k_2 - t^2\sigma^2s_0^2$.

Thus, the optimal pricing strategies of the two retailers can be obtained by substituting (13) into $p_1^* = \theta_1 + \theta_2 x_1 + \theta_3 p_w$ and $p_2^* = \delta_1 + \delta_2 x_2 + \delta_3 p_w$.

4.2. Either of Retailers Is Affected by x_0 . In this situation, either of retailers is affected by price comparison information x_0 . We assume that retailer1 is affected by x_0 while retailer2 is not affected by x_0 directly, therefore, we can have

$$p_1 = \theta_1 + \theta_2 x_1 + \theta_3 p_w + \theta_4 x_0, \tag{14}$$

$$p_2 = \delta_1 + \delta_2 x_2 + \delta_3 p_w. \tag{15}$$

Retailer1 enables to speculate pricing strategy of retailer2 based on x_0 and x_1 . Consider

$$E(p_2 \mid x_1, x_0) = \delta_1 + \delta_2 \frac{\sigma s_0 x_1 + \sigma s_1 x_0}{\sigma s_1 + \sigma s_0 + s_1 s_0} + \delta_3 p_w.$$
 (16)

But retailer2 enables to speculate pricing strategy of retailer1 based on x_2 and p_w . Consider

$$E(p_1 \mid x_2, p_w) = \theta_1 + \theta_2 \frac{\sigma s_0 x_2 + \sigma s_2 p_w - \sigma s_2}{\sigma s_2 + \sigma s_0 + s_2 s_0} + \theta_3 p_w + \theta_4 (p_w - 1),$$
(17)

$$E(\mu \mid x_1, x_0) = \frac{\sigma s_0 x_1 + \sigma s_1 x_0}{\sigma s_1 + \sigma s_0 + s_1 s_0},$$
 (18)

$$E(\mu \mid x_2, p_w) = \frac{\sigma s_0 x_1 \lambda + \sigma s_1 (p_w - \lambda)}{(\sigma s_1 + \sigma s_0 + s_1 s_0) \lambda}.$$
 (19)

In order to reduce potential risks brought by price changes with the signal of PCS, the two retailers determine the optimal retail price by maximizing the expected profit. To this end, the expected profits for retailer1 and retailer2 are

$$E(\Pi_{1} \mid x_{1}, x_{0})$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{1} + \beta p_{2} + \mu\right)(p_{1} - p_{w}) \mid x_{1}, x_{0}\right],$$

$$E(\Pi_{2} \mid x_{2}, p_{w})$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{2} + \beta p_{1} + \mu\right)(p_{2} - p_{w}) \mid x_{2}, p_{w}\right].$$
(21)

Proposition 2. When either of retailers is influenced by the supplier price comparison impact x_0 , the profit functions $E(\Pi_1 \mid x_1, x_0)$ and $E(\Pi_2 \mid x_2, p_w)$ are strictly concave in p_1 and p_2 , respectively, namely, the optimal retail price p_1^* and p_2^* uniquely exist.

By solving the first derivative of p_1 and p_2 , one can have the optimal pricing strategies of the two retailers as follows:

$$p_{1}^{*} = \frac{1}{2\alpha} \left[\frac{d}{2} + \beta E(p_{2} \mid x_{1}, x_{0}) + E(\mu \mid x_{1}, x_{0}) + \alpha p_{w} \right],$$

$$p_{2}^{*} = \frac{1}{2\alpha} \left[\frac{d}{2} + \beta E(p_{1} \mid x_{2}, p_{w}) + E(\mu \mid x_{2}, p_{w}) + \alpha p_{w} \right].$$
(22)

Then, solving (14)–(22) simultaneously, one finds θ_i , i = 1, 2, 3, 4 and δ_i , i = 1, 2, 3. Consider

$$\theta_{1} = \frac{1-t}{2-t}$$

$$-\frac{\sigma d \left(1-t^{2}\right) \left[2 \left(\sigma+s_{0}\right) s_{1} s_{2}+\sigma s_{0} \left(2 s_{2}+t s_{1}\right)\right]}{V \left(2-t\right)},$$
(23)

$$\theta_{2} = \frac{\sigma s_{0} \left(1 - t^{2}\right) \left[2 \left(1 / \left(\alpha + \beta\right) - d\right) k_{2} + d\sigma s_{0}\right]}{V}, \tag{24}$$

$$\theta_{3} = \frac{1}{2 - t}$$

$$\sigma d \left(1 - t^{2}\right) \left[2 \left(\sigma + s_{0}\right) s_{1} s_{2} + \sigma s_{0} \left(2 s_{2} + t s_{1}\right)\right]$$

$$-\frac{\sigma d (1-t^{2}) \left[2 (\sigma + s_{0}) s_{1} s_{2} + \sigma s_{0} (2 s_{2} + t s_{1})\right]}{\alpha V (2-t)},$$
(25)

$$\theta_4 = \frac{1}{2-t} - \frac{\alpha \sigma s_1 \left(1 - t^2\right) \left(2k_2 + t \sigma s_1\right)}{V},\tag{26}$$

$$\delta_{1} = \frac{1-t}{2-t}$$

$$-\left(\left(4\sigma^{2}\left(1-t^{2}\right)\left(\frac{1}{\alpha+\beta}-d\right)\right)$$

$$\times\left[\left(\frac{2}{\alpha+\beta}-2d\right)\left(\sigma+s_{0}\right)s_{1}s_{2}+\sigma s_{0}\right]\right)$$

$$\times\left(V\left(4-t^{2}\right)\right)^{-1},$$
(27)

$$\delta_{2} = \frac{\sigma s_{0} \left(1 - t^{2}\right) \left[\left(2/\left(\alpha + \beta\right) - 2d\right) k_{1} + d\sigma s_{0}\right]}{V},$$

$$\delta_{3} = \frac{1}{2 - t}$$

$$-\left(\left(2\sigma \left(1 - t^{2}\right) \left[2s_{2} \left(\frac{2}{\alpha + \beta} - 2d\right) k_{1} + d\sigma s_{0}\right]\right)$$

$$+ds_{1} \left[\left(\frac{2}{\alpha + \beta} - 2d\right) k_{2} + d\sigma s_{0}\right]\right)$$

$$\times \left(\alpha V \left(4 - t^{2}\right)\right)^{-1},$$
(29)

where $t = \beta/\alpha$, $k_1 = (\sigma + s_0)s_1 + \sigma s_0$, $k_2 = (\sigma + s_0)s_2 + \sigma s_0$, and $V = 4k_1k_2 - t^2\sigma^2s_0^2$.

The optimal pricing strategies of the two retailers can be obtained by substituting (22) to (29) into $p_1^* = \theta_1 + \theta_2 x_1 + \theta_3 p_w + \theta_4 x_0$ and $p_2^* = \delta_1 + \delta_2 x_2 + \delta_3 p_w$.

4.3. Both of Retailers Are Affected by x_0 . In this situation, the supplier shares price comparison information with retailers, which enables both of retailers to be affected by x_0 directly. Hence, price functions of retailer1 and retailer2 are as follows:

$$p_1 = \theta_1 + \theta_2 x_1 + \theta_3 p_m + \theta_4 x_0, \tag{30}$$

$$p_2 = \delta_1 + \delta_2 x_2 + \delta_3 p_w + \delta_4 x_0. \tag{31}$$

In this situation, due to price competition, the retailer enables to speculate pricing strategy of its rival according to x_1 or x_2 . The new pricing strategies of retailer1 and retailer2 are

$$E(p_{2} \mid x_{1}, x_{0}) = \delta_{1} + \delta_{2} \frac{\sigma s_{0} x_{1} + \sigma s_{1} x_{0}}{\sigma s_{1} + \sigma s_{0} + s_{1} s_{0}} + \delta_{3} p_{w} + \delta_{4} x_{0},$$
(32)

$$E(p_1 \mid x_2, x_0) = \theta_1 + \theta_2 \frac{\sigma s_0 x_1 + \sigma s_1 x_0}{\sigma s_1 + \sigma s_0 + s_1 s_0} + \theta_3 p_w + \theta_4 x_0,$$
(33)

$$E(\mu \mid x_1, x_0) = \frac{\sigma s_0 x_1 + \sigma s_1 x_0}{\sigma s_1 + \sigma s_0 + s_1 s_0},$$
 (34)

$$E(\mu \mid x_2, x_0) = \frac{\sigma s_0 x_2 + \sigma s_1 x_0}{\sigma s_1 + \sigma s_0 + s_1 s_0}.$$
 (35)

The expected profits of retailer1 and retailer2 are expressed as:

$$E(\Pi_{1} \mid x_{1}, x_{0})$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{1} + \beta p_{2} + \mu\right)(p_{1} - p_{w}) \mid x_{1}, x_{0}\right],$$

$$E(\Pi_{2} \mid x_{2}, x_{0})$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{2} + \beta p_{1} + \mu\right)(p_{2} - p_{w}) \mid x_{2}, x_{0}\right].$$
(37)

Proposition 3. When both of retailers are influenced by the supplier price comparison impact x_0 , the profit functions $E(\Pi_1 \mid x_1, x_0)$ and $E(\Pi_2 \mid x_2, x_0)$ are strictly concave in p_1 and p_2 , respectively, namely, the optimal retail prices p_1^* and p_2^* uniquely exist.

By solving the first derivative of p_1 and p_2 , one can have the optimal pricing strategies of the two retailers as follows:

$$p_{1}^{*} = \frac{1}{2\alpha} \left[\frac{d}{2} + \beta E(p_{2} \mid x_{1}, x_{0}) + E(\mu \mid x_{1}, x_{0}) + \alpha p_{w} \right],$$

$$p_{2}^{*} = \frac{1}{2\alpha} \left[\frac{d}{2} + \beta E(p_{1} \mid x_{2}, x_{0}) + E(\mu \mid x_{2}, x_{0}) + \alpha p_{w} \right].$$
(38)

Solving (30)–(38) simultaneously, one finds θ_m , m = 1, 2, 3, 4 and δ_m , m = 1, 2, 3, 4. Consider

$$\begin{split} \theta_{1} &= \frac{1-t}{2-t} - \frac{\sigma d \left(1-t^{2}\right) \left[\left(4\sigma + ds_{0}\right) k_{1} + \sigma s_{0} \left(2s_{1} + ts_{2}\right)\right]}{U\left(2-t^{2}\right)}, \\ \theta_{2} &= \frac{\sigma s_{0} \left(1-t^{2}\right) \left[2 \left(1/\left(\alpha + \beta\right) - d\right) k_{2} + d\sigma s_{0}\right]}{U}, \\ \theta_{3} &= \frac{1}{2-t} \\ &- \frac{\sigma d \left(1-t^{2}\right) \left[\left(4\sigma + ds_{0}\right) k_{2} + \sigma s_{0} \left(2s_{2} + ts_{1}\right)\right]}{\alpha V\left(4-t^{2}\right)}, \\ \theta_{4} &= \frac{\alpha \sigma s \left(1-t^{2}\right)_{0} \left(2k_{2} + t\sigma s_{0}\right)}{U}, \\ \delta_{1} &= \frac{1-t}{2-t} \\ &- \left(\left(4\sigma^{2} \left(1-t^{2}\right) \left(\frac{1}{\alpha + \beta} - d\right)\right) \\ &\times \left[\left(\frac{2}{\alpha + \beta} - 2d\right) \left(\sigma + s_{0}\right) s_{1} s_{2} \right. \\ &+ \sigma s_{0} \left(2 + t\right) \left(s_{1} + s_{2}\right)\right]\right) \\ &\times \left(U\left(2-t^{2}\right)\right)^{-1}, \end{split}$$

$$\begin{split} \delta_{2} &= \frac{\sigma s_{0} \left(1-t^{2}\right) \left[\left(2/\left(\alpha+\beta\right)-2d\right) k_{1}+d\sigma s_{0}\right]}{U}, \\ \delta_{3} &= \frac{1}{2-t} - \frac{\sigma d \left(1-t^{2}\right) \left[\left(4\sigma+ds_{0}\right) k_{1}+\sigma s_{0} \left(2s_{1}+ts_{2}\right)\right]}{V \left(4-t^{2}\right)}, \\ \delta_{4} &= \frac{\alpha \sigma s_{0} \left(1-t^{2}\right) \left(2k_{1}+t\sigma s_{0}\right)}{U}, \end{split}$$

$$(39)$$

where $t = \beta/\alpha$, $k_1 = (\sigma + s_0)s_1 + \sigma s_0$, $k_2 = (\sigma + s_0)s_2 + \sigma s_0$, $V = 4k_1k_2 - t^2\sigma^2s_0^2$, and $U = 2k_1k_2 - t^2\sigma^2s_0^2$.

The optimal pricing strategies of the two retailers can be obtained by substituting (39) into $p_1^* = \theta_1 + \theta_2 x_1 + \theta_3 p_w + \theta_4 x_0$ and $p_2^* = \delta_1 + \delta_2 x_2 + \delta_3 p_w + \delta_4 x_0$.

5. Wholesale Pricing Strategy

In this section, we investigate the supplier's pricing decision. The supplier is affected by the signal of PCS. We denote the impact as x_0 . Then, it can be divided into three situations according to previous section, namely, according to whether or not the retailers are affected by x_0 . We consider the wholesale pricing is $p_w = \lambda_0 + \lambda x_0$, and the supplier aims to maximize its expected profit

$$E(\Pi_3 \mid x_0) = E[(D_1 + D_2) p_w \mid x_0], \tag{40}$$

where $D_1(p_1, p_2, \mu) = d_1 - \alpha p_1 + \beta p_2 + \mu$, $D_2(p_1, p_2, \mu) = d_2 - \alpha p_2 + \beta p_1 + \mu d_1 = d_2 = d/2$; that is,

$$E(\Pi_{3} \mid x_{0})$$

$$= E\{[d - (\alpha - \beta)(p_{1} + p_{2}) + 2\mu] p_{w} \mid x_{0}\}$$

$$= \{d - (\alpha - \beta) E[(p_{1} + p_{2}) \mid x_{0}] + 2E(\mu \mid x_{0})\} p_{w},$$

$$E(x_{1} \mid x_{0}) = E(x_{2} \mid x_{0}) = E(\mu \mid x_{0}) = \frac{\sigma}{x_{0}(\sigma + s_{0})}.$$
(41)

Denoting $\sigma/(x_0(\sigma + s_0))$ as Δ , optimal wholesale pricing is discussed in the following parts.

5.1. Neither of Retailers Is Affected by x_0 . In this subsection, we consider that x_0 is not correlated with the two retailers, but retailers are affected indirectly by x_0 of p_w . According to (3), (4), and (41), we can get the expected profit of supplier as follows:

$$E(\Pi_3 \mid x_0)$$

$$= \{d - (\alpha - \beta) [(\theta_1 + \delta_1) - (\theta_2 + \delta_2) \Delta + (\theta_3 + \delta_3) E(p_w \mid x_0)] + 2\Delta\} p_w.$$

$$(42)$$

Proposition 4. When x_0 exerts impact to neither of retailers, the profit function $E(\Pi_3 \mid x_0)$ is strictly concave in p_{w1} , and the optimal wholesale price p_{w1}^* uniquely exists.

Solving the first-order derivative of $E(\Pi_3 \mid x_0)$ with respect to p_w , one can get

$$p_{w1}^{*} = 8\alpha d\sigma^{2} s_{0} (s_{2} + s_{1}) ((2 - t) \alpha - t\beta + 1)$$

$$\times (2 - t)^{2} (1 - t^{2}) (k_{1} + k_{2})$$

$$\times \left(\left(\frac{1}{\alpha + \beta} - d \right) s_{1} + 2 d s_{2} (1 + k_{1}) \right)$$

$$+ \frac{\sigma^{2} s_{0}}{\sigma + s_{0}} (2 - t) (\alpha - \beta) (1 - t^{2}) (k_{1} + k_{2})$$

$$\times \left(\left(\frac{2}{\alpha + \beta} - 2 d \right) + d \sigma s_{0} \right)$$

$$- \frac{(2 - t) (d (\sigma + s_{0}) + 2 \sigma)}{(1 - t) (\sigma + s_{0})},$$
(43)

where $t = \alpha/\beta$, θ_1 , δ_1 , θ_2 , δ_2 , θ_3 , δ_3 are the same as the results mentioned in Section 4.1.

5.2. Either of Retailers Is Affected by x_0 . In this subsection, we consider either of retailers is affected by x_0 . According to (14), (15), and (41), we can get the expected profit of supplier as follows:

$$E(\Pi_{3} \mid x_{0})$$

$$= \{d - (\alpha - \beta) [(\theta_{1} + \delta_{1}) + (\theta_{2} + \delta_{2}) \Delta + (\theta_{3} + \delta_{3}) \times E(p_{w} \mid x_{0}) + \delta_{4} E(x_{0} \mid x_{0})] + 2\Delta\} p_{w}.$$
(44)

Proposition 5. When x_0 exerts impact on either of the retailers, the supplier's profit function $E(\Pi_3 \mid x_0)$ is strictly concave in p_{w2} , and the optimal wholesale price p_{w2}^* uniquely exists.

Solving the first-order derivative of $E(\Pi_3 \mid x_0)$ with respect to p_w , and let $dEp_w/dp_w = 0$, one can get p_{w2}^*

$$\begin{split} p_{w2}^* &= \left[\left(4k_1k_2 - t^2\sigma^2s_0^2 \right) \right. \\ &- \left(\left(d \left(4k_1k_2 - t^2\sigma^2s_0^2 \right) \left(4 - t^2 \right) \right) \right. \\ &\times \left(\left(1 - t \right) \left(4k_1k_2 - t^2\sigma^2s_0^2 \right) - 4\sigma \left(2 - t \right) \right. \\ &\left. \times \left(2 \left(\frac{1}{\alpha + \beta} - d \right) s_1k_2 + ds_2k_1 \right) \right)^{-1} \right) \right] \cdot x_0 \\ &+ 4\sigma\alpha \left(\left(2 - t \right)\alpha - t\beta \right) \left(1 - t^2 \right) \left(k_1 + k_2 \right) \\ &\times \left(\left(2s_1 \left(\frac{1}{\alpha + \beta} - d \right) + ds_2 \right) + d\sigma s_0 \left(2 + t \right) \left(s_1 + s_2 \right) \right) \\ &+ \frac{2s_0\sigma^2}{\sigma + s_0} \left(2 - t \right) \left(\alpha - \beta \right) \left(1 - t^2 \right) \left(k_1 + k_2 \right) \end{split}$$

$$\times \left(\left(\frac{1}{\alpha + \beta} - d \right) + d\sigma s_0 \right)$$

$$- \left(\left(\sigma s_1 \left(2k_2 + t\sigma s_1 \right) (1+t) \right) \right.$$

$$\times \left(\left(4k_1k_2 - t^2\sigma^2 s_0^2 \right) \left(4 - t^2 \right) - 4\sigma \left(2 - t \right) (1+t) \right.$$

$$\times \left(2 \left(\frac{1}{\alpha + \beta} - d \right) s_1 k_2 + ds_2 k_1 \right) \right)^{-1} \right), \tag{45}$$

where $t = \alpha/\beta$, θ_1 , δ_1 , θ_2 , δ_2 , θ_3 , δ_3 are the same as the results in Section 4.2.

5.3. Both of Retailers Are Affected by x_0 . In this subsection, x_0 exerts impact on both of retailers. According to (30), (31), and (41), we can get the expected profit of supplier as follows:

$$E(\Pi_{3} \mid x_{0})$$

$$= \{d - (\alpha - \beta) [(\theta_{1} + \delta_{1}) + (\theta_{2} + \delta_{2}) \Delta + (\theta_{3} + \delta_{3}) \times E(p_{w} \mid x_{0}) + (\theta_{4} + \delta_{4}) E(x_{0} \mid x_{0})] + 2\Delta\} p_{w}.$$
(46)

Proposition 6. When x_0 exerts impact on both of retailers, the profit function $E(\Pi_3 \mid x_0)$ is strictly concave in p_{w3} , and the optimal wholesale price p_{w3}^* uniquely exists.

Solving the first-order derivative of $E(\Pi_3 \mid x_0)$ with respect to p_w , one obtains the optimal wholesale price p_{w3}^* as follows:

$$\begin{split} p_{w3}^* &= \frac{\alpha \sigma s_0 \left(1 - t^2\right) \left(2 \left(k_1 + k_2\right) + t \sigma s_0\right)}{2 k_1 k_2 - t^2 \sigma^2 s_0^2} \cdot x_0 \\ &+ \left(\alpha - t \beta - \frac{1}{d}\right) \\ &\times \left[\left(\left(4 \alpha \sigma^2 \left(1 - t^2\right) \left(\frac{1}{\alpha + \beta} - d\right)\right.\right.\right. \\ &\left. \times \left(\left(\frac{2}{\alpha + \beta} - 2 d\right) + (2 + t) \sigma s_0 \left(s_1 + s_2\right)\right) \right.\right. \\ &\left. + \alpha \sigma^2 d \left(1 - t^2\right) \\ &\times \left(\left(4 \sigma + d s_0\right) k_1 + \sigma s_0 \left(2 s_1 + s_2\right)\right) \right) \end{split}$$

$$\times \left(\alpha \left(2k_{1}k_{2}-t^{2}\sigma^{2}s_{0}^{2}\right)\left(2-t^{2}\right)\right.$$

$$\times \left(4k_{1}k_{2}-t^{2}\sigma^{2}s_{0}^{2}\right)\left(4-t^{2}\right)\right)^{-1}\right)-\frac{\sigma}{\sigma+s_{0}}$$

$$\cdot \frac{\left(1-t^{2}\right)\sigma s_{0}\left(\left(2/\left(\alpha+\beta\right)-2d\right)\left(k_{1}+k_{2}\right)+ds_{0}\right)}{2k_{1}k_{2}-t^{2}\sigma^{2}s_{0}^{2}}\right],$$

$$(47)$$

where $t = \alpha/\beta$, θ_1 , δ_1 , θ_2 , δ_2 , θ_3 , δ_3 are the same as the results in Section 4.3.

6. Simulation Analysis

Assuming that d=200, $\alpha=0.5$, $\beta=0.3$, $\mathrm{diag}(\sigma,s_0,s_1,s_2)=\mathrm{diag}(10,2,4,3)$, and $\lambda=10$, $\lambda_0=40$ based on the three situations discussed above, we make an analysis of how x_0,x_1,x_2 affects optimal pricing p_1^*,p_2^*,p_w^* . Based on the analysis of the three situations shown above, we are able to obtain optimal wholesale prices in different situations. The numerical results are shown in Tables 2, 3, 4, and 5.

6.1. Simulation Analysis of Retail Pricing Model. Recall that x_0, x_1, x_2 represent the degree of PCS signal on price, we take the values of x_0, x_1, x_2 from 0 to 1, where $x_0, x_1, x_2 = 0$ implies that the corresponding parties are not affected by the signal of PCS, whereas $x_0, x_1, x_2 = 1$ implies that the corresponding party are fully affected by the signal of PCS. As for the retailers, from Figure 2, we can see when x_0, x_1, x_2 take values from 0 to 1, the line of Situation 1 p_1^* is higher than those in Situations 2 and 3; the line of Situation 2 p_2^* is higher than the line of Situation 2 p_1^* ; the line of Situation 3 p_1^* is the lowest one among all situations. Besides, optimal prices in every situation are increasing with x_0, x_1, x_2 . From Figure 3, we can find that the line of Situation 1 $E(p_1^*)$ is the highest among all situations. When x_0, x_1, x_2 are from 0.4 to 0.7, the line of Situation 2 $E(p_1^*)$, $E(p_2^*)$ and the line of Situation 3 $E(p_1^*)$ are getting closer. Besides, optimal profits of every situation are increasing with x_0, x_1, x_2 .

According to Figures 2 and 3, three observations for the retailers are noteworthy.

Observation 1. The optimal retail price of Situation 1 and its corresponding optimal profit are higher than those of Situations 2 and 3. In other words, in order to obtain a higher profit, the retailers are more willing to avoid the existence of PCS.

Observation 2. Although the retailers tend to avoid the existence of PCS, they are also willing to seek more availability of price information because the optimal retail price and their corresponding profit would be higher if the availability of pricing information is more sufficient.

Observation 3. In Situation 2, obtaining the information from the PCS could lead retailer1 to set a higher retail price and gain more profits than those of retailer2. Hence, the retailer should

$x_0 = x_1 = x_2$												
		0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
Situation 1	p_1^*, p_2^*	174	176	178	180	183	187	189	193	198	201	205
Situation 2	p_1^*	96	103	111	120	125	130	134	140	147	152	158
Situation 2	p_2^*	150	156	160	163	166	169	172	174	176	178	181
Situation 3	p_1^*, p_2^*	71	76	80	89	101	111	120	126	138	147	152

TABLE 2: Optimal retail pricing strategies in different situations.

TABLE 3: Optimal profits in different situations.

$x_0 = x_1 = x_2$												
		0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
Situation 1	$E(p_1^*), E(p_2^*)$	22358	22248	22411	22468	22712	23089	23194	23564	24060	24289	24645
Situation 2	$E(p_1^*)$	7918	8083	8289	8540	8649	9758	9829	9985	10180	10301	10453
	$E(p_2^*)$	6432	6908	7382	7845	8071	8384	8624	8909	9516	9918	10099
Situation 3	$E(p_1^*), E(p_2^*)$	5659	5968	6192	6781	7548	8134	8444	8644	8850	8972	9132

Table 4: Optimal wholesale price offered by supplier under different x_0 .

x_0												
	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1	
p_{w1}^*	150	150	150	150	150	150	150	150	150	150	150	
p_{w2}^*	167	182	197	212	227	242	257	272	287	302	317	
p_{w3}^*	233	273	313	353	393	433	473	513	553	593	633	

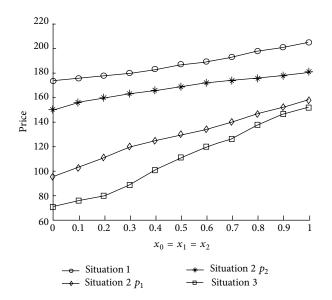


FIGURE 2: Optimal retail prices for 4.1, 4.2, and 4.3.

tend to exclusively cooperate with the PCS. This observation enhances the value of the existence of PCS.

Based on Observations 1, 2, and 3, the best strategy for the retailers is to avoid the PCS and meanwhile to increase the availability of price information. In reality, the PCS might be a third party service who is out of the control of the retailers.

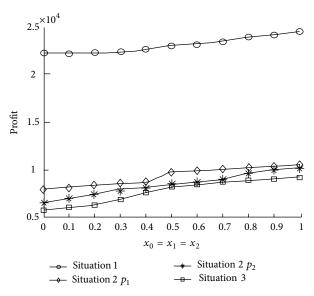


FIGURE 3: Optimal profits of retailers for 4.1, 4.2, and 4.3.

However, our results provide an important implication about how the retailers react if the PCS existed.

6.2. Simulation Analysis of Wholesale Pricing Model. As for the supplier, from Figure 4, we can see that the wholesale prices in every situation are linearly correlated with x_0 . For certain x_0 , the optimal wholesale prices in Situation 3 is higher than those in Situations 1 and 2. And the optimal wholesale prices in Situations 2 and 3 are increasing with x_0 . From Figure 5, we can find that profits in Situations 2 and 3 are increasing with x_0 ; however, the one in Situation 1 is linearly negatively correlated with x_0 .

According to Figures 4 and 5, three observations are noteworthy.

x_0											
	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
$E(p_{w1}^*)$	23400	22050	21300	20100	18450	17250	16350	15150	14100	13200	12150
$E(p_{w2}^*)$	27555	27664	28171	29468	29964	30976	31611	32096	32431	32616	33285
$E(p_{w3}^*)$	34018	38493	41316	43713	45195	46764	47773	49248	51429	52777	53805

TABLE 5: Optimal profits of supplier under different x_0 .

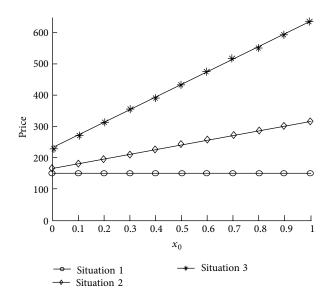


FIGURE 4: Optimal wholesale prices for 5.1, 5.2, and 5.3.

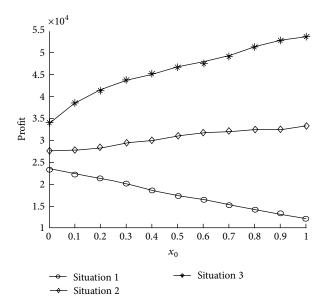


FIGURE 5: Optimal profits of supplier for 5.1, 5.2, and 5.3.

Observation 4. The optimal wholesale price of Situation 1 is lower than those of Situations 1 and 2, while the corresponding optimal profit is higher than those of Situations 1 and 2. This observation implies that the supplier tends to set a higher wholesale price if the PCS affects the decisions of retail price

made by both of retailers. Similar to the results of retailers, the supplier is also more willing to avoid the existence of PCS.

Observation 5. We notice that, in Situation 3, both of the retailers are affected by the PCS; more availability of price information would lead to a decrease in the supplier's profit. Hence, the supplier in Situation 3 should keep the availability of price information as much as possible.

Observations 4 and 5 indicate that the supplier is more willing to avoid the impact of PCS and also increase the availability of price information; however, if both of the retailers are affected by the PCS, he should tend to reduce the availability of price information.

7. Conclusions

With the rapid development of e-commerce, the PCS enables to provide transparent price and promote rational consumption. However, the PCS would also affect the pricing decision made by supply chain parties. In this study, we derived the optimal pricing strategies with respective to three situations of signal availability of PCS. Our numerical study implied that when both of retailers are affected by the PCS, the supplier is more willing to reduce the availability of price information, and when either of retailers is affected by the PCS, the retailer should tend to exclusively cooperate with the PCS. In addition, the retailers and supplier are all more willing to avoid the existence of PCS and increase the availability of price information. This result implied that (1) if the entire supply chain belongs to an identical corporate, the corporate is better to merge the PCS; (2) more transparency in price information actually hurts the supply chain parties' and supply chain's profit. This is consistent with the industrial practice in which price war could lead to a big drop in both market and price [21].

For the research limitations, we admit that the findings are mainly based on the analytical models and numerical studies we have developed under various assumptions, such as a linear demand function with respect to the PCS. In addition, the analysis is conducted on a relatively simple dual-channel supply chain of one supplier and two competing retailers, which is an abstract version of the more complex real world supply chain. In this paper, we consider that the PCS is independent from the parties in supply chain; however, according to the practices in China, we observe that Baidu has developed new business model as a reaction to price comparison impact. It would be interesting to investigate the mechanism of how the supply chain parties should cooperate with the PCS. It is also promising to extend

the model and the analysis to more complex supply chain systems (such as the ones that are risk averse agents [22–24]). It is also meaningful to investigate whether it is beneficial for the supplier to always share information from contracting perspective among supply chain parties [25, 26]. This would address another interesting topic from the perspective of social influence on the PCS in supply chain management [27].

Appendices

Proof of Proposition 1. According to (2), (4), (6), (8), and (10), we have

$$E(\Pi_{1} \mid x_{1}, p_{w})$$

$$= [d_{1} - \alpha p_{1} + \beta E(p_{2} \mid x_{1}, p_{w}) + E(\mu \mid x_{1}, p_{w})]$$

$$\times (p_{1} - p_{w})$$

$$= [d_{1} - \alpha p_{1} + \beta(\delta_{1} + \delta_{2} E(x_{2} \mid x_{1}, p_{w}) + \delta_{3} p_{w})]$$

$$\times (p_{1} - p_{w})$$

$$= [d_{1} - \alpha p_{1}$$

$$+\beta(\delta_{1} + \delta_{2} \cdot \frac{\sigma s_{0} x_{2} \lambda + \sigma s_{2} (p_{w} - \lambda_{0})}{(\sigma s_{2} + \sigma s_{0} + s_{2} s_{0}) \lambda} + \delta_{3} p_{w})]$$

$$\times (p_{1} - p_{w})$$

$$= [d_{1} - \alpha p_{1} + \beta(\delta_{1} + \delta_{2} \cdot \frac{\sigma s_{0} x_{2} + \sigma s_{2} x_{0}}{\sigma s_{2} + \sigma s_{0} + s_{2} s_{0}} + \delta_{3} (\lambda_{0} + \lambda x_{0}))][p_{1} - (\lambda_{0} + \lambda x_{0})]$$

$$= -\alpha p_{1}^{2} + W_{1} p_{1} + Y_{1}, \qquad (A.1)$$

where $\alpha > 0$, $W_1 = d_1 + \beta(\delta_1 + \delta_2 \cdot (\sigma s_0 x_2 + \sigma s_2 x_0) / (\sigma s_2 + \sigma s_0 + s_2 s_0) + \delta_3(\lambda_0 + \lambda x_0)) + \alpha(\lambda_0 + \lambda x_0)$ and $Y_1 = -(\lambda_0 + \lambda x_0)(d_1 + \beta(\delta_1 + \delta_2 \cdot (\sigma s_0 x_2 + \sigma s_2 x_0) / (\sigma s_2 + \sigma s_0 + s_2 s_0) + \delta_3(\lambda_0 + \lambda x_0)))$. According to (2), (3), (7), (9), and (11), we have

$$\begin{split} E\left(\Pi_{2} \mid x_{2}, p_{w}\right) \\ &= \left[d_{2} - \alpha p_{2} + \beta E\left(p_{1} \mid x_{2}, p_{w}\right)\right. \\ &+ E\left(\mu \mid x_{2}, p_{w}\right)\right]\left(p_{2} - p_{w}\right) \\ &= \left[d_{2} - \alpha p_{2} + \beta \frac{\lambda \sigma s_{0} x_{2} + \sigma s_{2}\left(p_{w} - \lambda_{0}\right)}{\left(\sigma s_{2} + \sigma s_{0} + s_{2} s_{0}\right)\lambda}\right. \\ &\left. + \frac{\lambda \sigma s_{0} x_{2} + \sigma s_{2}\left(p_{w} - \lambda_{0}\right)}{\left(\sigma s_{2} + \sigma s_{0} + s_{2} s_{0}\right)\lambda}\right]\left(p_{2} - p_{w}\right) \end{split}$$

$$= \left[d_2 - \alpha p_2 + \beta \frac{\sigma s_0 x_2 + \sigma s_2}{\sigma s_2 + \sigma s_0 + s_2 s_0} + \frac{\sigma s_0 x_2 + \sigma s_2}{\sigma s_2 + \sigma s_0 + s_2 s_0} \right] \left[p_2 - (\lambda_0 + \lambda x_0) \right]$$

$$= -\alpha p_2^2 + W_2 p_2 + Y_2,$$
(A.2)

where $\alpha > 0$, $W_2 = \alpha(\lambda_0 + \lambda x_0)(d_2 + \beta(\sigma s_0 x_2 + \sigma s_2)/(\sigma s_2 + \sigma s_0 + s_2 s_0) + (\sigma s_0 x_2 + \sigma s_2)/(\sigma s_2 + \sigma s_0 + s_2 s_0)$, $Y_2 = -(\lambda_0 + \lambda x_0)(\beta((\sigma s_0 x_2 + \sigma s_2)/(\sigma s_2 + \sigma s_0 + s_2 s_0)) + (\sigma s_0 x_2 + \sigma s_2)/(\sigma s_2 + \sigma s_0 + s_2 s_0)$.

According to the nature of the quadratic function and $Y_2 < 0$, the profit functions $E(\Pi_1 \mid x_1, p_w)$ and $E(\Pi_2 \mid x_2, p_w)$ are strictly concave in p_1 and p_2 , respectively.

Proof of Proposition 2. According to (2), (15), (18), and (20), we have

$$E(\Pi_{1} \mid x_{1}, x_{0})$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{1} + \beta p_{2} + \mu\right)(p_{1} - p_{w}) \mid x_{1}, x_{0}\right]$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{1} + \beta(\delta_{1} + \delta_{2}x_{2} + \delta_{3}(\lambda_{0} + \lambda x_{0}) + \delta_{4}x_{0}) + \mu\right)(p_{1} - \lambda_{0} - \lambda x_{0}) \mid x_{1}, x_{0}\right]$$

$$= -\alpha p_{1}^{2} + W_{3}p_{1} + Y_{3},$$
(A.3)

where $\alpha > 0$, W_3 represents a coefficient, and Y_3 represents constant in this quadratic function.

According to (2), (14), (17), and (19), we have

$$E(\Pi_{2} \mid x_{2}, p_{w})$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{2} + \beta p_{1} + \mu\right)(p_{2} - p_{w}) \mid x_{2}, p_{w}\right]$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{2} + \beta(\theta_{1} + \theta_{2}x_{1} + \theta_{3}p_{w} + \theta_{4}x_{0}) + \mu\right) \times (p_{2} - \lambda_{0} - \lambda x_{0}) \mid x_{2}, p_{w}\right]$$

$$= -\alpha p_{2}^{2} + W_{4}p_{2} + Y_{4},$$
(A.4)

where $\alpha > 0$, W_4 represents a coefficient, and Y_4 represents constant in this quadratic function.

Similar to Proposition 1, according to the nature of the quadratic function, both $E(\Pi_1 \mid x_1, x_0)$ and $E(\Pi_2 \mid x_2, p_w)$ are strictly concave in p_1 and p_2 , respectively.

Proof of Proposition 3. According to (2), (31), (32), (34), and (36), we have

$$E(\Pi_{1} \mid x_{1}, x_{0})$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{1} + \beta p_{2} + \mu\right)(p_{1} - p_{w}) \mid x_{1}, x_{0}\right]$$

$$= E\left[\left(\frac{d}{2} - \alpha p_{1} + \beta\left(\delta_{1} + \delta_{2}x_{2} + \delta_{3}p_{w} + \delta_{4}x_{0}\right) + \mu\right) \times (p_{1} - \lambda_{0} - \lambda x_{0}) \mid x_{1}, x_{0}\right]$$

$$= -\alpha p_{1}^{2} + W_{5}p_{1} + Y_{5},$$
(A.5)

where $\alpha > 0$, W_5 represents a coefficient, and Y_5 represents constant in this quadratic function.

According to (2), (30), (33), and (35), we have

$$\begin{split} E\left(\Pi_{2} \mid x_{2}, x_{0}\right) \\ &= E\left[\left(\frac{d}{2} - \alpha p_{2} + \beta p_{1} + \mu\right) (p_{2} - p_{w}) \mid x_{2}, x_{0}\right] \\ &= E\left[\left(\frac{d}{2} - \alpha p_{2} + \beta (\theta_{1} + \theta_{2} x_{1} + \theta_{3} p_{w} + \theta_{4} x_{0}) + \mu\right) \\ &\times (p_{2} - \lambda_{0} - \lambda x_{0}) \mid x_{2}, x_{0}\right] \\ &= -\alpha p_{2}^{2} + W_{6} p_{2} + Y_{6}, \end{split} \tag{A.6}$$

where $\alpha > 0$, W_6 represents a coefficient, and Y_6 represents constant in this quadratic function.

Similar to Proposition 1, the profit functions $E(\Pi_1 \mid x_1, x_0)$ and $E(\Pi_2 \mid x_2, x_0)$ are strictly concave in p_1 and p_2 , respectively.

Proof of Proposition 4. According to (3), (4), and (41), we have

$$E(\Pi_{3} \mid x_{0})$$

$$= E\{[d - (\alpha - \beta) (p_{1} + p_{2}) + 2\mu] p_{w} \mid x_{0}\}$$

$$= \{d - (\alpha - \beta) E[(p_{1} + p_{2}) \mid x_{0}] + 2E(\mu \mid x_{0})\} p_{w}$$

$$= \{d - (\alpha - \beta) [(\theta_{1} + \delta_{1}) - (\theta_{2} + \delta_{2}) \Delta + (\theta_{3} + \delta_{3}) E(p_{w} \mid x_{0})] + 2\Delta\} p_{w}$$

$$= (\beta - \alpha) (\theta_{3} + \delta_{3}) p_{w}^{2} + W_{7} p_{w} + Y_{7},$$
(A.7)

where $\alpha > \beta$, W_7 represents a coefficient, and Y_7 represents constant in this quadratic function.

Similarly, according to the nature of the quadratic function, the profit function $E(\Pi_3 \mid x_0)$ is strictly concave in p_{w1} .

Proof of Proposition 5. According to (14), (15), and (41), we have

$$E(\Pi_{3} \mid x_{0})$$

$$= E\{[d - (\alpha - \beta) (p_{1} + p_{2}) + 2\mu] p_{w} \mid x_{0}\}$$

$$= \{d - (\alpha - \beta) E[(p_{1} + p_{2}) \mid x_{0}] + 2E(\mu \mid x_{0})\} p_{w}$$

$$= \{d - (\alpha - \beta) [(\theta_{1} + \delta_{1}) + (\theta_{2} + \delta_{2}) \Delta + (\theta_{3} + \delta_{3}) \times E(p_{w} \mid x_{0}) + \delta_{4}E(x_{0} \mid x_{0})] + 2\Delta\} p_{w}$$

$$= (\beta - \alpha) (\theta_{3} + \delta_{3}) p_{w}^{2} + W_{8}p_{w} + Y_{8},$$
(A.8)

where $\alpha > \beta$, W_8 represents a coefficient, and Y_8 represents constant in this quadratic function.

Similarly, according to the nature of the quadratic function, the profit function $E(\Pi_3 \mid x_0)$ is strictly concave in p_{w2} .

Proof of Proposition 6. According to (30), (31), and (41), we have

$$\begin{split} E\left(\Pi_{3} \mid x_{0}\right) \\ &= E\left\{\left[d - (\alpha - \beta)\left(p_{1} + p_{2}\right) + 2\mu\right] p_{w} \mid x_{0}\right\} \\ &= \left\{d - (\alpha - \beta) E\left[\left(p_{1} + p_{2}\right) \mid x_{0}\right] + 2E\left(\mu \mid x_{0}\right)\right\} p_{w} \\ &= \left\{d - (\alpha - \beta)\left[\left(\theta_{1} + \delta_{1}\right) + \left(\theta_{2} + \delta_{2}\right)\Delta\right. \\ &+ \left(\theta_{3} + \delta_{3}\right) E\left(p_{w} \mid x_{0}\right) \\ &+ \left(\theta_{4} + \delta_{4}\right) E\left(x_{0} \mid x_{0}\right)\right] + 2\Delta\right\} p_{w} \\ &= \left(\beta - \alpha\right) \left(\theta_{3} + \delta_{3}\right) p_{w}^{2} + W_{9} p_{w} + Y_{9}, \end{split} \tag{A.9}$$

where $\alpha > \beta$, W_9 represents a coefficient, and Y_9 represents constant in this quadratic function.

Similarly, according to the nature of the quadratic function, the profit function $E(\Pi_3 \mid x_0)$ is strictly concave in p_{w3} .

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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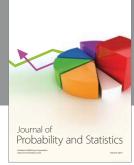
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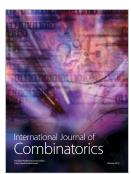








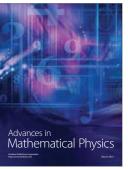


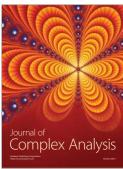




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