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2 extremes

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10 Abstract The important role of the evolution of mean temperature in the changes 11 of extremes has been recently documented in the literature, and variability is 12 known to play a role in the occurrence of extremes too. This paper aims at further 13 investigating the role of their evolutions in the observed changes of temperature 14 extremes. Analyses are based on temperature time series for Eurasia and the 15 United States and concern absolute minima in winter and absolute maxima in 16 summer of daily minimum and maximum temperature. A test is designed to check 17 whether the extremes of the residuals after accounting for a time-varying mean 18 and standard deviation can be considered stationary. This hypothesis is generally 19 true for all extremes, seasons and locations. Then, the comparison between the 20 directly fitted parameters and the retrieved ones from those of the residuals 21 compare favorably. Finally, a method is proposed to compute future return levels 22 from the stationary return levels of the residuals and the projected mean and 23 variance at the desired time horizon. Comparisons with return levels obtained 24 through the extrapolation of significant linear trends identified in the parameters 25 of the GEV distribution show that the proposed method gives relevant results. It 26 allows taking mean and/or variance trends into account in the estimation of 27 extremes even though no significant trends in the GEV parameters can be 28 identified. Moreover, the role of trends in variance cannot be neglected. Lastly, 29 first results based on two CMIP5 climate models show that the identified link 30 between mean and variance trends and trends in extremes is correctly reproduced by the models and is maintained in the future. 31

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33 **1 Introduction**

Global temperature has increased since the beginning of the last century and will 34 35 most likely continue to do so in the next decades [IPCC, 2007]. This increasing 36 trend may induce more frequent and more intense heat waves in the future [Meehl 37 and Tebaldi, 2004; Fischer and Schaer, 2010; Barriopedro et al., 2011]. Coumou 38 and Rahmstorf [2012] recently showed that the unprecedented occurrence of 39 record-breaking events in the last decade can be attributed to anthropogenic 40 climate change. As temperature extremes may cause multiple severe social and 41 economic impacts, their evolutions have been studied using different approaches. 42 Some studies are based on the analysis of observed daily data, recently made 43 available through homogenized or, at least, scrutinized series regarding 44 homogeneity, like the European Climate Assessment and Dataset (ECA&D) 45 project series or the Caesar et al. [2006] gridded dataset. Important decreases are 46 found in the number of frost days, while coherent increases appear in extreme 47 night time temperatures [Alexander et al, 2006; Frich et al., 2002]. Generally, 48 trends in extreme night time temperature are higher than trends in day time 49 maximum temperature, and the warming is largest in the northern hemisphere during winter and spring. Moreover, Kiktev et al. [2003] showed that these 50 51 evolutions are linked to anthropogenic greenhouse gas emissions. It is thus clear 52 that the highest and lowest temperatures exhibit trends all over the world. One 53 question thus concerns the link between these trends and that of the mean and/or 54 of other moments of the distribution.

55 This question has been tackled by Barbosa et al. [2011], for daily mean 56 temperature in Central Europe using quantile regression and clustering. They 57 showed that for most of their studied stations, the slopes of the lowest and highest 58 quantiles are not the same as those of the median, and thus that the trends are not 59 the same for all parts of the distribution. Using a different approach, Ballester et 60 al. [2010a] analyzed the link between trends in extreme and in mean temperature. 61 Using climate simulation results from the European PRUDENCE project and the 62 E-OBS gridded observation dataset [Haylock et al., 2008] they showed that the 63 increasing intensity of the most damaging summer heat waves over Central 64 Europe is mostly linked to higher base summer temperatures.

Few papers analyze the most extreme events using statistical Extreme Value
Theory (EVT). *Zwiers et al.* [2011] used Generalized Extreme Value (GEV)

67 distributions and climate model simulations of the CMIP3 project database to 68 detect anthropogenic influence. They found that the most detectable influence of 69 external forcing is on annual maximum daily minimum temperature (TN) and the 70 least detectable on annual maximum daily maximum temperature (TX). They also 71 stated that the waiting time for the 1960's 20-year return level (expected to recur 72 once every 20 years) has now increased for annual minimum TX and TN and 73 decreased for annual maximum TN. Brown et al. [2008] went further in studying 74 the link between the identified trends in extreme and in mean temperature. They 75 used an EVT-model with time varying parameters to study the global changes in 76 extreme daily temperatures since 1950 from the Caesar et al. [2006] gridded daily 77 dataset. Applying the Marked Point Process technique, they found that only trends 78 in the location parameter are significant and that both maximum and minimum 79 TN present higher trends than their TX counterparts. They then compared the 80 trends in the location parameter to the trends in mean, and found that the trends in 81 extremes are consistent with the trends in mean.

82 Starting from these results, this paper aims at going further in researching the link 83 between the evolutions of extremes and of the bulk of the distribution of 84 temperature. It can obviously be expected that if the mean is changing, the 85 induced shift of the tails of the distribution will lead to changes in extremes. Katz 86 and Brown [1992] and Fisher and Schär [2009] highlighted the role of variability 87 in the occurrence of extremes. Other moments of the distribution could be studied. For example, Ballester et al. [2010b] use standard deviation and skewness of the 88 89 annual distribution of detrended temperature. Using climate model simulation 90 results only, they stress the role of standard deviation change in the modification 91 of frequency, intensity and duration of warm events, whereas skewness change is 92 also important for cold extremes.

93 This study focuses on the estimation of temperature extremes in the climate 94 change context. One commonly used methodology relies on the identification and 95 estimation of trends in the parameters of the EVT distributions [Coles, 2001; 96 Parey et al., 2007; Parey et al., 2010b]. However, such trends are identified on 97 relatively short samples made of the highest (or lowest) observed values and may 98 not be as robust as trends identified on the whole dataset. Therefore a systematic 99 study of the link between trends in extremes and trends in mean and variance is 100 helpful to determine whether extremes exhibit unique trends in addition to those 101 induced by trends in mean and variance. If they do not, future extremes can be 102 derived from the stationary extremes of the residuals, after accounting for a time-103 varying mean and standard deviation, and the changes in mean and variance of the 104 whole dataset, as proposed in Parey et al. 2010b. The aim of this paper is then to 105 check this link for a large number of time series of temperature from weather 106 stations. It will therefore be organized as follows: section 2 is dedicated to the 107 observational data and section 3 to methods descriptions. The link between the non-parametric trends in mean and variance and in extremes is investigated and 108 109 discussed in section 4, as well as its use in the estimation of future return levels, 110 before concluding with a discussion and perspectives in section 5.

111 **2 Observational data**

112 For Eurasia, weather station time series are taken from the ECA&D project 113 database. The project gives indications of homogeneity through the results of 114 different break identification techniques [Klein Tank et al., 2002]. For this study 115 the series which could be considered as homogenous (stated as "useful" in the database) over the period1950-2009 have first been selected for both TN and TX. 116 117 Then, these series have been checked for missing data and those with more than 118 5% missing data have again been excluded. This selection left 106 series for TX 119 and 120 for TN (many TX series, mostly in Russia, have missing values from 120 2007 onward whereas the corresponding TN series have missing values only in 121 2009).

122 For the United States, weather station TX and TN time series are obtained from 123 the Global Historical Climatology Network - Daily Database (GHCN daily) 124 [Menne et al., 2011]. These time series have been quality checked through an 125 automated quality insurance described in Durre et al. [2010]. The first step has 126 been to select the highest quality time series, as stated by the quality indicators, 127 with less than 5% of missing data. Then, only the series starting before 1966 and 128 ending after 2008 are kept. Finally a new check-up for missing values has been 129 conducted, together with a visualization of the evolution of annual mean values. 130 The TX time series for the station of Eureka (Arizona) and the TN time series for 131 Ajo (California) One TX and one TN time series present a stepwise-like 132 evolution between 1970 and 1980 looking like a break and have been eliminated 133 (figure 1), which leaves us with 86 series for TX and 85 for TN.

134 **3 Statistical methods**

135 **3.1 Extreme value theory**

EVT relies on the well known Extremal Types Theorem which states that, if the 136 137 maximum of a large sample of observations, suitably normalized, converges in 138 distribution to G when the sample size tends to infinity, then G belongs to the 139 GEV family [Coles, 2001]. The assumptions behind the theorem are that the data 140 in every block are stationary and weakly dependent with a regular tail distribution. 141 Temperature maxima are expected to occur mostly in summer and temperature 142 minima in winter. For each time series, the distribution of the 2, 3 or 5 highest or 143 lowest values each year in the different months is computed. Then the months 144 with more extremes than expected under the identical distribution assumption are 145 selected. For maximal TN or TX, the months of June, July, August or July, 146 August, September occur quite regularly as the favored ones, and thus the summer season is defined as a period of 100 days between the 14th of June and the 21st of 147 September. The selection of 100 days is convenient but may appear somewhat 148 149 arbitrary. However, it is a good compromise between length and weak remaining 150 seasonality. In fact, tests with different selections in these months of June to 151 September showed that the results are not sensitive to this choice (not shown). For 152 minimal TN or TX, the minima rather occur during the month of January, 153 followed by December or February, but no other months emerge. Thus the winter 154 season is defined as the 90 days of the months of December, January and 155 February (the 29 February is omitted during leap years, except if the temperature 156 is lower than that of the 28 in which case it is considered as the temperature of the 157 28). Then the choice of block length is based on the classical bias / variance trade-158 off. Defining 2 blocks per season (blocks of 50 days in summer and 45 days in 159 winter) have been chosen as a reasonable balance, leading, with series of around 160 50 to 60 years to more than 100 block maxima or minima.

161 Thus the GEV distribution will be fitted to the maxima of TN and TX in summer 162 and the minima of TN and TX (maxima of the opposite series) in winter 163 considering 2 blocks per season.

164 **3.2 Trends**

165 3.2.1 Non-parametric trends in mean and variance

Let X(t) be an observed temperature time series. For each day t, m(t) and $s^{2}(t)$ 166 167 (continuous time functions) represent the associated mean and variance, respectively. If $\Gamma(t)$ is a (k,T) matrix, where T is the length of the time period, 168 169 whose components are associated to different characteristics of the process at time t, then $\Gamma(t)$ is called multidimensional trend [Hoang et al., 2009]. For instance, 170 171 $\Gamma(t)$ consists here of the trends in mean and standard deviation, but skewness and 172 kurtosis trends could also be considered. The goal is to estimate as objectively as 173 possible $\Gamma(t)$, in order to capture the structure in the data and in the same time, to 174 smooth local extrema. As in *Hoang et al.* [2009] or in *Parey et al.* [2010a and b], the LOESS (Local regression, Stone, 1977) technique is used to do so. The choice 175 176 of the smoothing parameter (and thus the window length) has to be adapted to the 177 analyzed data to keep the trend identification as intrinsic as possible. This is made by using a modified partitioned cross-validation (MPCV) technique [Hoang, 178 179 2010]. Cross-validation has to be modified in order to eliminate as far as possible 180 time dependence and take heteroscedasticity into account. The idea of MPCV is to partition the observations into g subgroups by taking every g^{th} observations, for 181 example the first subgroup consists of observations 1, 1+g, 1+2g,..., the second 182 183 subgroup consists of observations 2, 2+g, 2+2g,... The observations in each subgroup are then independent for high g. Chu and Marron [1991] define the 184 185 optimal bandwidth for Partitioned Cross-Validation in the case of constant $h_{PCV} = h_0 g^{1/5}$, with h_0 estimated as the minimiser of 186 variance as

187
$$PCV_g(h) = \frac{1}{g} \sum_{k=1}^{g} CV_{0,k}(h) (CV_{0,k} \text{ is the ordinary Cross-Validation score for the k-}$$

188 th group). This approach has been modified to take heterocedasticity into account. 189 Then, the optimal g corresponds to the minimum of a more complicated 190 expression [*Hoang*, 2010] and in practice, it is preferred to estimate h_{MPCV} (the 191 optimal bandwidth of the Modified Partitioned Cross Validation) for different 192 values of g and to retain the values of g for which h_{MPCV} is not too bad (that is not 193 too close to zero and not higher than 0.7). For each g the trends m and s are 194 estimated by loess with bandwidth \hat{h}_{MPCV}^g to obtain an estimator of the expression 195 to minimize. The value of g corresponding to the minimum value is retained, 196 giving the corresponding optimal bandwidth h_{MPCV}. Up to now, this seems to be 197 the best way to estimate the optimal bandwidth in this situation for which 198 mathematical theory is not complete. For temperature, the dependence between 199 the dates can be assumed as negligible if the dates are distant by more than 5 days. 200 We used a cross validation method on data sampled every 10 days (g=10) to be 201 conservative, and an optimal parameter is computed for each temperature time 202 series.

203 3.2.2 Non-parametric trends in extremes

204 In the same way, if EVT can be applied and G(t) is the GEV distribution at time t, 205 $\Theta(t)$ represents the parameters of G(t), that is location $\mu(t)$, scale $\sigma(t)$ and shape 206 $\xi(t)$. The shape parameter ξ is the most difficult to estimate, and it could be tricky 207 to differentiate possible evolutions from estimation errors. In their study, Zhang et 208 al. [2004] did not consider any trend in this parameter, as they assume that it is 209 not likely to show a trend in climate series. Tests on different periods of a long 210 observation series have shown that this parameter does not significantly evolve 211 with time [Parey et al., 2007], and more sophisticated non-parametric studies lead 212 to the same conclusion [Hoang, 2010]. Thus, in the following, the shape 213 parameter ξ will be considered constant. Then, the trends in location and scale 214 parameters are estimated in a non-parametric way using cubic splines (through penalized likelihood maximization, Cox and O'Sullivan [1996]) and the classical 215 216 cross validation technique (in an iterative way) since the extremes are selected as 217 independent values. Cubic splines are preferred here because they are convenient 218 to deal with edge effects for the relatively short series of maxima. An iterative 219 procedure is used to smooth both the location and scale parameters consistently. 220 The estimation of constant parameters is obtained through likelihood 221 maximization (see section 3.3).

222 **3.3 Stationarity test**

The question we wish to address is whether trends in extremes can mostly be characterized by trends in mean and variance. To analyse this, Y(t) is defined as the standardized residuals:

226
$$Y(t) = \frac{X(t) - m(t)}{s(t)}$$
 (1)

The hypothesis we want to test becomes: "the extremes of Y(t) in every block can be considered as a stationary sequence", which means that both the location μ and scale σ parameters are constant. A methodology to test this hypothesis has been proposed and detailed in *Hoang* [2010] and is summarized here. First, Y(t) is estimated as $\hat{Y}(t) = \frac{X(t) - \hat{m}(t)}{\hat{s}(t)}$ and the stationarity of its extremes is tested. The

set of possible evolutions of the extreme parameters of Y(t) is very large. So the test cannot easily be formulated as a choice between two well defined alternatives. This is the reason why the use of a squared distance Δ between two functions of time, defined as:

236
$$\Delta(f,g) = \int_{t \in D} (f(t) - g(t))^2 dt$$
, D being the time period, (2)

is preferred. If any function of time f is estimated by g, $\Delta(f,g)$ is a measure of the 237 238 quality of g as an estimate of f. Two different estimations of the parameters $\mu(t)$ 239 and $\sigma(t)$ can be made: they can be estimated non-parametrically as $\tilde{\mu}(t)$ and $\tilde{\sigma}(t)$ or as constant as $\hat{\mu}$, $\hat{\sigma}$. The stationarity hypothesis being true or not, 240 241 $\tilde{\mu}(t)$ and $\tilde{\sigma}(t)$ converges to the 'real' values μ , σ when the sample size T tends to 242 infinity, the rate of convergence depends on the supposed smoothness of the function. The situation is of course different for $\hat{\mu}, \hat{\sigma}$: if the stationarity 243 hypothesis is true, they converge to μ , σ with a rate of the order of \sqrt{T} and in this 244 245 case $\Delta(\hat{\mu}, \tilde{\mu})$ is, for a large sample, very close to $\Delta(\mu, \tilde{\mu})$. On the contrary if the hypothesis is false, $\hat{\mu}$ converges to a constant which is of course different from the 246 247 non constant function $\mu(t)$ and $\Delta(\hat{\mu}, \tilde{\mu})$ does not tend to zero and remains larger than some A>0. The intuitive reason is that we try to find μ in a set of functions 248 "far away" from μ if the hypothesis is false. The same is true for $\Delta(\hat{\sigma}, \tilde{\sigma})$. A test 249 250 could be based on an asymptotic result [Hoang, 2010]. We prefer the use of a 251 numerical approach based on simulation. Our proposed solution is then to 252 statistically evaluate (by simulation or bootstrapping) the distribution of $\Delta(\hat{\mu}, \hat{\mu})$ if the hypothesis is true, that is the distribution of the distances between the non-253 254 parametric estimates and the best constant to estimate μ . To do this, we simulate a

large number of samples of the stationary GEV (μ_Y, σ_Y, ξ_Y) distribution with the 255 256 same size as the series of the maxima of Y(t). From each sample, we estimate the 257 GEV parameters in two ways: first, by considering them as constant; second, by 258 considering them as functions of time. Then we calculate the distances between 259 these two estimates and obtain a distribution of the statistical error of estimation 260 provided the hypothesis is true. If the distances obtained from the observations are found lower than the 90th percentile, then the hypothesis is considered satisfied: 261 262 the distances cannot be distinguished from such arising due to statistical errors. 263 The power of the test has been evaluated and is reasonable (see appendix).

4 Results for temperature time series

265 **4.1 Stationarity test**

Brown et al. [2008], among others, have shown that significant trends can be identified in the evolutions of temperature extremes, especially the location parameter. The investigated issue is whether these trends can mostly be characterized by trends in mean and variance. Therefore, the previously described test has been applied to different temperature time series for different variables (TN and TX), parameters (location and scale) and locations (Eurasia and the United States).

The results are shown in figure 21. Grey points indicate that the cross validation 273 274 could not converge to an optimal smoothing parameter for the non-parametric 275 estimation of the location and scale parameters, and thus, the test could not be 276 performed. This mostly happens in winter in the United-States: around 20% of the 277 stations (18.8% for minimal TN and 19.8% for minimal TX) experience this 278 problem. The reason for this will have to be more carefully investigated in future 279 work. For the other seasons and locations, this concerns less or around 10% of the 280 stations. Among points where the test could be performed, the hypothesis is 281 accepted for both location and scale parameters for around 80 to 90% of the 282 stations (from 76.6% for maximum TN in summer in the United-States to 94.2% 283 for minimum TN in winter in the United-States), and for at least one of the 284 parameters for more than 94% of the stations (from 94.7% for maximum TX in 285 summer in the United-States to 100% for minimum TX and minimum TN in 286 winter in the United-States and minimum TX in winter in Eurasia). This means

that the stationarity of the extremes of the standardized residuals can reasonablybe assumed globally.

4.2 Impact on Return Level estimation

290 Previous results show that the trends in extremes closely follow that of mean and 291 variance. The extreme distribution parameters of the observed temperature time 292 series X(t) are linked to those of the standardized residuals Y(t) in the following 293 way:

294
$$\begin{cases} \xi_{X} = \xi_{Y} \\ \sigma_{X}(t) = \sigma_{Y}(t) * s(t) \\ \mu_{X}(t) = m(t) + \mu_{Y}(t) * s(t) \end{cases}$$
(3)

295 where μ , σ and ξ are respectively the location, scale and shape parameters of the 296 GEV distribution, subscripts X and Y referring to the observed temperature time 297 series and the residuals time series, and m(t) and s(t) are the trends in mean and 298 standard deviation. We thus first compared the non-parametric GEV parameters 299 directly obtained from X(t), with their bootstrap confidence intervals, to the same 300 parameters reconstructed from the constant Y(t) parameters and the non-301 parametric trends in mean and standard deviation of X(t) by using (3). The plot 302 obtained for the French station of Déols in figure 3 shows The obtained results 303 show that the reconstructed parameters are reasonably comparable to the 304 directly estimated ones (not shown) fall most of the time inside the 95% 305 bootstrap confidence interval of the directly computed ones, which checks the 306 validity of the tested hypothesis.

Then, the GEV parameters for a given future period can be derived from those of Y(t), which are constant, and future values of the mean and the standard deviation,

309 to compute some future Return Level (RL), as proposed in *Parey et al.* [2010b].

310 As an example, 50-year RLs are computed for the year 2030 for TX in Eurasia:

311 1) through extrapolation of optimal linear trends (according to a likelihood
312 ratio test with a 10% significance 90% confidence level) in location and
313 scale parameters of the GEV for X(t)

through (3) with m(t) and s(t) being significant linear trends extrapolated
to 2030 (future m and s are computed over 10 years around 2030). Trend
significance is assessed with a Mann-Kendall test on seasonal means and
variances with a 10% significance 90% confidence level.

318 In each case, confidence intervals are computed by bootstrapping, in order to take 319 uncertainties in the identified trends into account. The obtained differences in RL 320 do not exceed 3°C, and method 2 generally gives higher RLs. The confidence 321 intervals of the two methods do not overlap for 16 out of the 106 TX time series 322 (figure 4 2). The confidence intervals are said "not overlapping" if the RL 323 computed with method 1 does not fall in the confidence interval of the RL 324 computed with the method 2 and vice-versa. This avoids choosing a threshold to 325 eliminate small overlapping. For 14 of them, no trends are found in the GEV 326 parameters but a significant trend in mean, in variance or in both mean and 327 variance is identified, and for the 2 others a significant trend is found for the 328 location parameter of the GEV and in mean and variance. For these 16 TX time 329 series, the second approach leads to a higher RL, except for Gurteen in Ireland 330 (open red circle in figure 4 2). This can be explained by differences in the shape 331 parameter obtained for the extremes of X(t) and those of Y(t) in this case. 332 Theoretically, the shape parameters are identical (equation 3), but due to 333 adjustment uncertainties, in practice, it may not be the case (the confidence 334 intervals are large for this parameter). For the Gurteen TX time series $\xi_{\rm X} = -0.13$ and $\xi_{\rm Y}$ = -0.33. If the RL is computed with $\xi_{\rm Y}$ = $\xi_{\rm X}$ with method 2, then the two 335 336 confidence intervals do overlap.

337 The role of a trend in variance can be illustrated by the TX time series of Dresden 338 and Berlin in Germany. For these two time series, no significant trends are 339 identified in the location and scale parameters of the GEV. If the non-parametric 340 trends are drawn for these parameters, it can be seen that they show a small 341 increasing trend, which is not found significant through the likelihood ratio test 342 when looking for a linear trend (figure 5 3). The two time series differ regarding 343 the mean and variance evolutions: whereas in Berlin a significant linear trend is 344 found for both mean and variance, in Dresden, only the linear trend in mean is 345 significant (figure 6 4). Then, the 50-year RL in Dresden computed with method 346 2 falls inside the confidence interval of the RL computed with method 1:

347 Method 1: RL=36.9°C [35.7;38.1] Method 2: RL=37.8 [36.3;38.7]

348 whereas in Berlin, it does not:

Method 1: RL=38.2°C [37.2;39.3] Method 2: RL=40.9°C [39.1;42.4] The proposed method based on mean and variance trends allows taking changes in extremes into account, even though no significant trends in the GEV parameters are identified. Furthermore, the role of a variance change in the computed RL isnot negligible and has to be taken into account.

4.3 First results with climate models

355 A preliminary study has been made with climate model results to check:

- whether the stationarity of the extremes of the residuals found with
 observations is reproduced
- whether this stationarity remains true in the future with continued
 increasing greenhouse gas emissions

360 The TN and TX daily time series for Eurasia and the United States for only two 361 CMIP5 model simulations have been considered: IPSL-CM5B-LR and CNRM-362 CM5 (made available by the French teams of the Institut Pierre Simon Laplace 363 and Météo-France/CERFACS), with the highest RCP8.5 emission scenario. For 364 both models, the historical period is 1950-2005 and the considered future period 365 extends from 2006 to 2100 for IPSL-CM5B-LR and from 2006 to 2060 for 366 CNRM-CM5 (the downloaded results concern this period only, although the 367 model simulations run to the end of the century). Because the computation of the 368 test is time consuming (500 simulations are done for each temperature time 369 series), all grid points time series could not be considered for testing. The interest 370 here is on local extremes behavior, and thus grid point time series have to be 371 considered. However, temperature shows important spatial correlations, and 372 coherent regions can easily be identified. Therefore, it does not seem 373 necessary to compute the test for all grid points, especially for the highest 374 resolution models. Thus, Oonly the land grid points are considered, and among 375 those, all are tested in the US and only one over two points in longitude for 376 Eurasia for IPSL-CM5B-LR. For CNRM-CM5 one land point over two in the US 377 and one over two in longitude in Eurasia are used for testing, since this model grid has a higher resolution. The results obtained for minimum TN in winter and 378 379 maximum TX in summer show that for both periods and both models, our 380 hypothesis is likely to be true (figures 57 and 68). This means that these models 381 reliably reproduce the observed link between trends in extremes and trends in 382 mean and variance, and maintain it in the future. This has the interesting 383 consequence that future RLs can be computed with our proposed method by using 384 climate model results, and thus, projections are possible at later time horizons, 385 which is not reasonably possible when extrapolating observed linear trends. This 386 is however a very preliminary insight, a more complete study of the behavior 387 of climate models regarding this link will have to be further investigated by 388 considering more models and by better designing the testing methodology for 389 an optimal set of grid points.

390 5 Discussion and perspectives

In this paper, two sets of observed temperature time series, in Eurasia and in the United States, chosen to be as homogenous as possible over the period 1950-2009, have been used to extend studies on the role of mean and variance change in the evolutions of temperature extremes. **Only point-wise analyses are made first to avoid smoothing the extremes by spatial averages and secondly because return levels are required, in practice, for specific locations.**

397 This role may be well known, but here Although the role of mean and variance 398 in the evolution of extremes has been previously documented, here a test is 399 proposed and applied to check the stationarity of the extremes of the residuals. The results show that, for local daily temperature, trends in mean and variance 400 401 mostly explain the trends in extremes for both TN and TX, in winter and in 402 summer, and in Eurasia and in the United States. This allows estimating future 403 return levels from the stationary return levels of the residuals and the projected 404 mean and variance at the desired future period. Trends in mean and variance are 405 more robustly estimated than trends in the parameters of the extreme value 406 distribution, as they rely on much larger samples. Then, in case significant trends 407 in the parameters of the GEV distribution cannot be detected, this method allows 408 computing the future return levels in taking mean and/or variance trends into 409 account. Furthermore, some significant trends in variance are found and their 410 impact on the estimated future return level is not negligible. One practical 411 difficulty with the proposed method lies in the fitting of the shape parameters: 412 although the shape parameters of the observed time series and of the residuals are 413 theoretically the same, practically they may differ and induce differences in the 414 return levels. If this happens, it is advised to consider the lowest of both values as 415 the same shape parameter for both time series.

416 These results, and especially the identified trends in variance and their role 417 in the evolution of extremes, although coherent with most of the previous 418 findings, seem to contradict some recent ones (Simolo et al., 2011; Rhines and 419 Huybers, 2013). However, Rhines and Huybers 2013, following and 420 commenting Hansen et al. 2012, analyze summer mean temperatures and 421 discuss the role of changes in mean and variance in the recent occurrence of 422 very hot summers. They conclude that variance does not change, but the 423 variance they consider is rather interannual variability, whereas in the 424 present paper, variance means daily variability. They indeed acknowledge 425 that their analysis "pertains only to summer averages and that other analyses 426 based on, for example, shorter-term heat waves or droughts, may yield 427 different results." In Simolo et al. 2011, the study is made on spatial averages 428 over three different sub-domains and deals with so called "soft extremes", 429 that is high and low percentiles of the temperature distributions. Spatial 430 averaging necessarily leads to a reduction in variance and a smoothing of extreme events. On the other hand, our study is devoted to more extreme 431 432 events through the application of EVT. It is thus very difficult to compare the 433 results.

434 Then Finally, the reproduction by two climate models of the identified link 435 between trends in mean and variance and trend in extremes for temperature has 436 been verified. Moreover, the same models maintain the validity of the link in the 437 future, until 2100, which allows the use of the proposed method to estimate future 438 return levels based on model projected mean and variance at any desired future 439 horizon. The analysis of climate models behavior regarding this link needs 440 however to be further investigated using more models and a more robust 441 testing methodology. Physical mechanisms able to explain such a link need 442 furthermore to be identified.

These findings are important for practical applications, because most safety regulations are based on the estimation of rare events, defined as long period return levels. In the climate change context, at least for temperature, it is not yet possible to apply EVT as if the time series were stationary to make such estimations. The proposed method is a way of tackling this problem.

448 Only point-wise results are shown, and it could be interesting to further

449 investigate field significances. However in practice, return levels are often

450 required for specific locations.

451 **6. Appendix: power of the test**

A synthetic study is presented to check the ability of the test to assess stationarity
of the GEV parameters. To do so, 1000 samples are drawn from a distribution
with imposed trends in mean and standard deviation, but not in extremes:

455 $X(t) = m(t) + s(t)\varepsilon$, where m(t)=at+b and s(t)=ct+d and ε is drawn from a GEV 456 distribution with location 0, scale 1 and shape -0.15. Coefficients a to d has been chosen to be reasonable for temperature: $a=3.8*10^{-4}$; b=23.8; $c=4.4*10^{-5}$; d=4.4. 457 For each sample, m(t) and s(t) are re-estimated through LOESS with a smoothing 458 459 parameter of 0.17 to compute the residuals Y(t). Then non-parametric and 460 constant GEV parameters for the extremes of Y(t) are computed in the previously 461 described way, and the table of distances under stationarity is calculated, to test 462 whether the GEV parameters are found constant, with a 10% significance level. 463 The non-parametric (splines) estimates of the GEV parameters converge for 943 464 of the 1000 samples. Among these, the test accepts the stationarity of μ for 925 465 samples (98%), the stationarity of σ for 846 (\cong 90%) and the stationarity of both μ 466 and σ for 837 samples (\cong 89%), which results in around 10% false rejection, 467 coherent with the 10% significance level used.

Now, to compute the power of the test, we consider a sample for which stationarity is rejected. We then compute 500 distances between constant and nonparametric estimates of the GEV parameters of the extremes of Y(t) for a non stationary GEV and count the number of times the distance falls in the rejection region of the table computed with a stationary GEV. 84.4% of these distances fall in the rejection region, which gives a power of 84.4%.

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483

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- 594 List of figures

595 Figure 1: Annual mean temperature evolution between 1950 and 2009 for TX in-

596 Eureka (top panel) and TN in Ajo (bottom panel)

597 Figure 2-1: Results of the stationarity test of the GEV parameters (location μ and 598 scale σ) of the residuals Y(t) for **a**) minimum TN in winter, **b**) maximum TN in 599 Summer, c) minimum TX in winter and d) maximum TX in Summer in Eurasia 600 (left panels) and in the United States (right panels). Non convergence means that 601 the cross-validation could not converge to an optimal smoothing parameter and 602 thus the non-parametric evolution of the GEV parameters could not be computed. 603 Green means that stationarity is valid for μ and σ , blue for μ only, orange for σ 604 only and red means that the hypothesis is rejected for both μ and σ

605 **Figure 3**: Non parametric location μ (top panel) and scale σ (bottom panel) 606 parameters for the extremes of X(t) directly obtained from the maxima of X(t) 607 (black solid line) with their 95% bootstrap confidence interval (black dotted lines) 608 and reconstructed from the stationary parameters of Y(t) and the non-parametric 609 evolutions of the mean and standard deviation of X(t) (red line).

610 **Figure 4 2**: Comparison of the 50-year Return Levels for maximum TX in 611 summer computed by extrapolation of the significant linear trends in the location 612 μ and scale σ parameters of the fitted GEV ($RL_{\mu,\sigma}$) or by extrapolation of the 613 significant linear trends in mean m and standard deviation s ($RL_{m,s}$). Red dots 614 indicate that $RL_{m,s}$ falls outside the 95% confidence interval of $RL_{\mu,\sigma}$ and is higher 615 (closed dots) or lower (open dots) and green points indicate that the 95% 616 confidence intervals overlap. 617 **Figure 5** 3: Non-parametric (green curve) and optimal parametric (red curve) 618 trends in the location μ and scale σ parameters of the GEV distribution fitted on 619 TX summer block maxima for the stations of Berlin and Dresden.

Figure 6 4: Non-parametric (black curve) and linear (blue curve) trends in mean m and standard deviation s for TX in summer for the stations of Berlin and Dresden. The significance of the linear trend is indicated in the top left corner of each curve and is assessed by a Mann-Kendall test with a 10% significance level.

624 Figure 7 5: Results of the stationarity test of the GEV parameters (location μ and 625 scale σ) of the residuals Y(t) for minimum TN in winter for **a**) IPSL-CM5-LR and 626 b) CNRM-CM5 model and maximum TX in Summer for c) IPSL-CM5-LR and d) 627 CNRM-CM5 model in Eurasia (left panels) and in the United States (right 628 panels) in the period 1950-2005. Non convergence means that the cross-validation 629 could not converge to an optimal smoothing parameter and thus the non-630 parametric evolution of the GEV parameters could not be computed. Green means 631 that stationarity is valid for μ and σ , blue for μ only, orange for σ only and red 632 means that the hypothesis is rejected for both μ and σ .

633 Figure 8 6: same as figure 7 5 but for period 2006-2100 (2006-2060 for CNRM-

634 CM5) with RCP8.5