The large trans-Neptunian object 2002 TC₃₀₂ from combined stellar occultation, photometry, and astrometry data*

J. L. Ortiz¹, P. Santos-Sanz¹, B. Sicardy², G. Benedetti-Rossi^{2,3}, R. Duffard¹, N. Morales¹, F. Braga-Ribas^{4,5,3},
E. Fernández-Valenzuela⁶, V. Nascimbeni^{7,8}, D. Nardiello^{7,8,9}, A. Carbognani¹⁰, L. Buzzi¹¹, A. Aletti¹¹, P. Bacci¹²,
M. Maestripieri¹², L. Mazzei¹², H. Mikuz^{13,14}, J. Skvarc¹³, F. Ciabattari¹⁵, F. Lavalade¹⁶, G. Scarfi¹⁷, J. M. Mari¹⁸,
M. Conjat¹⁹, S. Sposetti²⁰, M. Bachini²¹, G. Succi²¹, F. Mancini²¹, M. Alighieri²¹, E. Dal Canto²¹, M. Masucci²¹,
M. Vara-Lubiano¹, P. J. Gutiérrez¹, J. Desmars^{22,23}, J. Lecacheux², R. Vieira-Martins^{5,3}, J. I. B. Camargo^{5,3},
M. Assafin^{24,3}, F. Colas²³, W. Beisker²⁵, R. Behrend²⁶, T. G. Mueller²⁷, E. Meza², A. R. Gomes-Junior^{28,3}, F. Roques²,
F. Vachier²³, S. Mottola²⁹, S. Hellmich²⁹, A. Campo Bagatin^{30,31}, A. Alvarez-Candal^{5,31}, S. Cikota³², A. Cikota³³,
J. M. Christille³⁴, A. Pál³⁵, C. Kiss^{35,36}, T. Pribulla^{37,38,39}, R. Komžík³⁷, J. M. Madiedo¹, V. Charmandaris^{40,41},
J. Alikakos⁴⁰, R. Szakáts³⁵, A. Farkas-Takács^{35,42}, E. Varga-Verebélyi³⁵, G. Marton³⁵, A. Marciniak⁴³, P. Bartczak⁴³,
M. Butkiewicz-Bąk⁴³, G. Dudziński⁴³, V. Alí-Lagoa²⁷, K. Gazeas⁴³, N. Paschalis⁴⁴, V. Tsamis⁴⁵, J. C. Guirado⁴⁶,
V. Peris⁴⁶, R. Iglesias-Marzoa^{47,48}, C. Schnabel^{25,49}, F. Manzano⁴⁹, A. Navarro⁴⁹, C. Perelló^{25,49}, A. Vecchione⁵⁰,
A. Noschese⁵⁰, and L. Morrone⁵¹

(Affiliations can be found after the references)

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ABSTRACT

Context. Deriving physical properties of trans-Neptunian objects is important for the understanding of our Solar System. This requires observational efforts and the development of techniques suitable for these studies.

Aims. Our aim is to characterize the large trans-Neptunian object (TNO) 2002 TC₃₀₂.

Methods. Stellar occultations offer unique opportunities to determine key physical properties of TNOs. On 28 January 2018, 2002 TC₃₀₂ occulted a $m_v \sim 15.3$ star with designation 593-005847 in the UCAC4 stellar catalog, corresponding to *Gaia* source 130957813463146112. Twelve positive occultation chords were obtained from Italy, France, Slovenia, and Switzerland. Also, four negative detections were obtained near the north and south limbs. This represents the best observed stellar occultation by a TNO other than Pluto in terms of the number of chords published thus far. From the 12 chords, an accurate elliptical fit to the instantaneous projection of the body can be obtained that is compatible with the near misses.

Results. The resulting ellipse has major and minor axes of 543 ± 18 km and 460 ± 11 km, respectively, with a position angle of 3 ± 1 degrees for the minor axis. This information, combined with rotational light curves obtained with the 1.5 m telescope at Sierra Nevada Observatory and the 1.23 m telescope at Calar Alto observatory, allows us to derive possible three-dimensional shapes and density estimations for the body based on hydrostatic equilibrium assumptions. The effective diameter in equivalent area is around 84 km smaller than the radiometrically derived diameter using thermal data from *Herschel* and *Spitzer* Space Telescopes. This might indicate the existence of an unresolved satellite of up to ~300 km in diameter, which is required to account for all the thermal flux, although the occultation and thermal diameters are compatible within their error bars given the considerable uncertainty of the thermal results. The existence of a potential satellite also appears to be consistent with other ground-based data presented here. From the effective occultation diameter combined with absolute magnitude measurements we derive a geometric albedo of 0.147 \pm 0.005, which would be somewhat smaller if 2002 TC₃₀₂ has a satellite. The best occultation light curves do not show any signs of ring features or any signatures of a global atmosphere.

Key words. Kuiper belt objects: individual: 2002 TC302 – Kuiper belt: general – techniques: photometric – occultations – astrometry

1. Introduction

Trans-Neptunian objects (TNOs) are thought to be among the least evolved relics of the formation of the Solar System, residing in its outer parts where the influence of the Sun is less severe than in the inner parts. Thus, these icy objects are very important bodies that carry abundant information on the physical and dynamical processes that shaped the Solar System, and are therefore key to our understanding of its formation and evolution. According to Fernández (2020), the Trans-Neptunian region holds the potential for many new and important discoveries that will very likely revolutionize our current view of the history of the Solar System, and its exploration has only just begun.

At the time of writing (February 2020) there are 2416 TNOs (including Pluto), 1085 scattered disc objects (SDOs) plus Centaurs, and 24 Neptune Trojans as listed by the Minor Planet Center¹. Many different observational strategies have

^{*} Tables A.1-A.3 are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via http://cdsarc.u-strasbg.fr/viz-bin/cat/J/A+A/639/A134

¹ https://www.minorplanetcenter.net/iau/lists/MPLists. html.

Table 1. Main characteristics of the occulted star.

Gaia ID	RA	Dec	G	Ang. Diam.	Speed
	(hh mm ss.s)	(° ′ ″)	(mag)	(mas)	(km s ⁻¹)
130957817758443648	02 21 49.3853105797	+28 24 13.439342645	15.6	0.009	4.77

Notes. Abbreviations are defined as follows: *Gaia* DR2 identification number (*Gaia* ID), J2000 coordinates of the star from *Gaia* DR2 (right ascension and declination, RA and Dec, respectively), *G* magnitude (G), angular diameter (Ang. Diam.), speed relative to the observer (speed).

been developed to study these objects, and among the tools available, stellar occultations offer the most powerful means of observation from the ground to determine key physical properties such as size and shape. Through stellar occultations, sizes and shapes with kilometric accuracy can be derived, as well as accurate geometric albedos (when the data are combined with reflected light measurements). This technique is especially fruitful in combination with thermal measurements and modeling (Müller et al. 2018). Finding potential atmospheres on the abovelisted objects is also theoretically possible through occultations. In addition, after the recent discovery of a dense ring around Haumea (Ortiz et al. 2017) in the context of the previous findings of a ring system around the centaur Chariklo (Braga-Ribas et al. 2014), and a structure in Chiron closely resembling that of Chariklo (Ortiz et al. 2015; Sickafoose et al. 2020), interest in the field of stellar occultations by TNOs continues to build as more rings can potentially be found in the Trans-Neptunian region.

However, the process from predicting to observing stellar occultations by TNOs is complex and many difficulties must be overcome. As a result, most of the positive occultation detections thus far have been made from single sites, offering only limited information (for a review see, e.g., Ortiz et al. 2020). Fortunately, there have been several cases with multichord detections, from which abundant information was retrieved and published (e.g., Elliot et al. 2010; Sicardy et al. 2011; Ortiz et al. 2012, 2017; Braga-Ribas et al. 2013; Benedetti-Rossi et al. 2016, 2019; Schindler et al. 2017; Dias-Oliveira et al. 2017; Leiva et al. 2017). Here we present the observations and the results of the stellar occultation by 2002 TC₃₀₂ on 28 January, 2018, which set a record in the number of detections. We also present additional information on rotational light curves and time series astrometry in order to try and put together a coherent picture of 2002 TC_{302} . The results are interpreted in the context of other bodies of similar size and features.

2. Occultation predictions

The occultation by 2002 TC_{302} on 28 January 2018 was predicted within our program of physical characterization of TNOs by means of stellar occultations. Important international efforts in this regard are currently being coordinated within the framework of the Lucky Star project² and the observations of this event were organized in that context of collaboration. The predictions of stellar occultations by 2002 TC_{302} were made in different steps with different star catalogs. We used the HSOY (Altmann et al. 2017) and UCAC5 (Zacharias et al. 2017) catalogs because the *Gaia* DR2 catalog (Lindegren et al. 2018) did not exist until April 2018 and *Gaia* DR1 did not have information on proper motions, whereas UCAC5 and HSOY contained that information for a subset of bright *Gaia* stars. Additionally, we used different orbit solutions for the TNO (from the AstOrb³, MPCORB⁴, JPL Horizons⁵, AstDys⁶ sites and our own orbit fits). Once the potential occultation seemed favorable enough to be observed, we carried out specific astrometric monitoring runs for 2002 TC₃₀₂ to narrow down the shadow path uncertainty. As is well known, the positions of stars down to ~20 magnitude in V are now available to a good accuracy of approximately or below a milliarcsecond (mas) thanks to the Gaia DR2 catalog including proper motion information (Lindegren et al. 2018). However, unfortunately, the positions of the TNOs are not known to that level of accuracy. Therefore, specific methods have to be developed to solve this problem (see Ortiz et al. 2020). Usually, a careful astrometric monitoring of the target TNO with sufficiently large telescopes and within a few months to a few days prior to the potential occultation combined with a specific analysis of the measurements is one of the preferred techniques, and has vielded positive occultation results. However, care must be taken with the existence of satellites, contamination from faint background stars, and with other effects that may bias astrometric observations. The main parameters of the star relevant for the occultation are listed in Table 1. We note that the angular diameter was estimated according to the expressions given in van Belle (1999) with colors from the NOMAD catalog (Zacharias et al. 2004).

From the astrometric monitoring of 2002 TC₃₀₂ carried out over several days in October, November, and December 2017 and January 2018 through the use of the Sierra Nevada 1.5 m telescope (Granada, Spain) and the Calar Alto 1.2 m telescope (Almería, Spain), we obtained refined predictions with respect to the initial one. From the latest measurements, made just a few days prior to the stellar occultation by 2002 TC_{302} , the path of the occultation was predicted to be favorable to a large area in Europe (see Fig. 1), although there was some concern that these measurements could be affected by the presence of a potential satellite and that the centroid could be biased to an incorrect position. Nevertheless, the prediction made with a specific orbital fit to all the available data with a special numerical integration method for asteroids (NIMA), as described in Desmars et al. (2015), indicated a similar path on Earth⁷. The final path, reconstructed from the fit to the occultation chords that are described in the following sections, is depicted in Fig. 2.

The astrometric observations at the 1.5m telescope of Sierra Nevada Observatory consisted of CCD images taken with the $2k \times 2k$ Versarray camera⁸, which has a field of view (FoV) of 7.8×7.8 arcmin and a scale of 0.23 arcsec pixel⁻¹. The integration time was 400 s and no filters were used in order to maximize the signal-to-noise ratio (S/N) of the observations. Typical seeing ranged from 1.3 to 2.5 arcsec. The Calar Alto 1.2 m telescope

² http://lesia.obspm.fr/lucky-star/

³ https://asteroid.lowell.edu/main/astorb

⁴ https://minorplanetcenter.net/iau/MPCORB.html

⁵ https://ssd.jpl.nasa.gov/?horizons

⁶ https://newton.spacedys.com/astdys/

⁷ http://lesia.obspm.fr/lucky-star/predictions/single. php?p=3492

⁸ https://www.osn.iaa.csic.es/en/page/ccdt150-camera



Fig. 1. Map showing the shadow path prediction (blue lines) for the stellar occultation by 2002 TC_{302} on 28 January, 2018, based on the last set of astrometry measurements obtained prior to the occultation. The green line shows the center of the shadow path. The motion of the shadow is from north to south. The width of the shadow path in the map is 500 km. The real shadow path of the occultation obtained after the analysis of the occultation chords is shown in Fig. 2.



Fig. 2. Map showing shadow path (blue lines) reconstructed after the occultation results were obtained. The width of the shadow path used in the map is 500 km, which is the equivalent-area diameter derived from the occultation. The green line shows the center of the shadow path. The shadow moved from north to south. The blue marks show the observatory sites where the occultation was detected. The two red marks indicate the two observatory sites closest to the shadow, where the event was negative.

images were acquired using the $4k \times 4k$ DLR camera⁹, which has a FoV of 22×22 arcmin and a pixel scale of 0.32 arcsec pixel⁻¹. We used the Johnson-Cousins *R* filter to avoid fringing in the near-infrared (NIR), which is a known problem with this camera. The typical seeing was around 1.5 arcsec and the used integration times were 400 s with sidereal tracking. At both telescopes, images were obtained using 2×2 binning mode and sidereal tracking. All images were bias subtracted and flatfield corrected using bias frames taken each night and using a median of flatfield frames obtained on each observing night (if this was not possible, flatfield frames from a previous night were used).

The images were analyzed with our own software, which extracts the sources of the images, solves for the plate constants using a specific astrometric catalog (selected by the user), and then performs the astrometry of the target. The astrometric catalog used was Gaia DR1 because Gaia DR2 had not been released prior to the occultation. Therefore, no proper-motion corrections were applied to the reference stars. This process is fully automated, but visual inspection was made to discard images in which the target could be blended with a background star and to discard images with cosmic-ray hits near the target. Also, care was taken so that charge bleeding, blooming, or ghosts from bright stars in the FoV, or any other anomalous aspect, did not affect the TNO measurements. Table A.1 lists all the measurements referring to the J2000 equinox. The NIMA prediction also included observations performed at Pico dos Dias Observatory (OPD) on October 18, 2017, and November 12, 2017, with the 1.6 m Perkin Elmer Telescope and using the Andor-IKon camera¹⁰ (pixel scale = 0.180 arcsec pixel⁻¹, $FoV = 7 \times 7$ arcsec). The images were calibrated with bias and flatfields taken during the same night and the used exposure times were 180s in Johnson - *I* filter.

3. Occultation observations

The occultation observations were performed with different telescopes and with various camera setups. The main observational details for the occultation observations at the main sites involved in the campaign are listed in Table 2. We list only the sites where the event was positive or where a close miss to the final shadow path was produced (providing at least constraints on the final fit of a shape model). Additional observatories to those listed in Table 2 monitored the event, but did not achieve positive results for a variety of reasons (because they were far from the final occultation path or because of clouds or technical problems). Unfortunately, a complete list of all the observatories that participated in the campaign cannot be derived, because there were amateur observers alerted through different internet tools and other procedures that we could not monitor. Nevertheless, we are keeping a registry¹¹ of all the observers who report their participation. This registry will be updated whenever new information becomes available.

Most of the observations from the sites in Table 2 consisted of sequences of images taken with different telescopes and different CCDs or CMOS detectors, as specified in the table. Other observations, indicated also in the table, were acquired in video mode. The video observations required a different analysis as explained in Sect. 4. No filters were used to maximize the number of photons received in order to get the highest possible S/N. Table 2 shows the names of the observing sites, their topocentric coordinates (longitude and latitude), the exposure time, the cycle time between consecutive exposures, the diameters of the telescopes, and the detector manufacturers and models.

The observations started typically 15 min before the predicted time for the occultation and were finalized around 15 min after the event. This was done in order to determine a good base line for the photometric analysis, and to determine its noise level before and after the occultation event. The moon was 90%

⁹ https://www.caha.es/CAHA/Instruments/IA123/index. html

¹⁰ http://www.lna.br/opd/instrum/ccd/manual_ikon.pdf

¹¹ http://asteroidstnos.iaa.es/content/sharedfiles

Site	Longitude (E) (°)	Latitude (N) (°)	Exp. time (s)	Cycle time (s)	Telescope diameter (cm)	Detector
Crni Vrh	14.071083	45.945833	3.4	4.995	60	Apogee Alta U9000HC
Asiago	11.568806	45.849444	5.0	8.301	67	Moravian G4-16000LC, KAF-16 803
S. Marcello Pistoiese	10.803889	44.064167	3.0	3.933	60	Apogee Alta U6
Tavolaia	10.673306	43.736500	7	7.23	40	ASI 174MM
Mount Agliale	10.514944	43.995278	2.0	3.718	50	FLI proline 4710
La Spezia	9.853528	44.126278	4.0	7.830	40	Sbig STXL 6303e
Gnosca	9.024028	46.231444	2.56	2.568	28	video WAT-910HX-RC, ICX429ALL
Varese, Schiaparelli Observatory	8.770278	45.868056	2.0	5.716	84	SBIG STX-16 803
Observatoire de Cote d'Azur, Nice	7.299833	43.725806	2.2	2.2005	40	ASI 174MM
Aosta Valley	7.478333	45.789444	2.0	2.695	40	FLI1001E
Biot, Nice	7.077778	43.617222	20.0	26.463	20	video QSI 583 wsg, KAF 8300
Vinon sur Verdon	5.796111	43.737778	10	30.467	30	Atik 383L, KAF 8300
Near Misses						
Osservatorio Salvatore Di Giacomo	14.564056	40.623944	2	3.4	50	FLI PL4220, E2V
Agerola	14.571556	40.626083	2.5	2.5	25	ASI 178M, IMX178
Sabadell	2.090167	41.550000	2.56	2.56	50	Watec 910HX-RC
San Esteve	1.872528	41.493750	2	2	40	Point Grey Chameleon3

Table 2. Observatories and characteristics of the observations.

full at 52 degrees from the target. This means that considerable sky background affected the observations and therefore the S/N of the observations was not as high as it could have been in the absence of moon illumination. Weather conditions were mostly clear in all the observatories except at Tavolaia, where intermittent clouds were present. Nevertheless, all the observing sites achieved enough S/N in the images (see last column of Table 3) for the occultation brightness drop to be clearly detected. The campaign around this occultation was a major achievement because no stellar occultation by a TNO had ever been observed with so many chords across the main body and with near misses.

4. Analysis of the occultation observations

Synthetic aperture photometry of the occultation star (blended with the TNO) was derived for the sequences of images of the different cameras in order to obtain the light curves for each site. The synthetic aperture photometry results were derived by means of an interactive data language (IDL) code that uses the implementation of the well-known DAOPHOT photometry package (Stetson 1987). Also, synthetic aperture photometry was derived for comparison stars close to the target star in the FoV of the cameras so that sky transparency fluctuations as well as

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seeing variations could be taken into account. The final light curves were obtained by taking the ratio of the occulted star flux in ADUs to that of a comparison star (or the combination of several comparison stars if this was possible). We carefully monitored the dispersion of the final light curves and chose the synthetic aperture diameters and the parameters of the synthetic aperture technique to get the least possible scatter in the photometry. Centroid tracking to recenter the apertures was done for the reference stars but not for the occultation star, whose position was kept fixed with respect to the references. The time of each photometry point was derived from the time stamps in the FITS headers of the images. It must be noted that some cameras inserted header times rounded off to the nearest second or truncated seconds. In these cases, we interpolated times for each point by using linear fits to the times versus frame number, in the same way as described in Sicardy et al. (2011). It must also be noted that for the Tavolaia observations, there was a problem in the acquisition that prevented us from saving the time in the headers of the images, and so we could only use the time of the recording of the file to disk as provided by the operating system. Hence, the timing of these observations is more uncertain than that of others, but we have accounted for this as explained in Sect. 5. The rest of the sites other than Tavolaia used internet NTP time servers to synchronize their image acquisition

Table 3. Disappeara	ance and reapp	pearance times.
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Site	Ingress time (hh:mm:ss.s ± s.s)	Egress time (hh:mm:ss.s ± s.s)	rms of the normalized flux
Crni Vrh	21:52:51.687 ± 1.150	$21:53:35.510 \pm 0.350$	0.085
Asiago	$21{:}52{:}43.400 \pm 1.400$	$21{:}54{:}08.875 \pm 0.200$	0.042
S. Marcello Pistoiese	$21:53:22.837 \pm 0.475$	$21:54:54.051 \pm 0.163$	0.062
Tavolaia	$21:53:36.3 \pm 2.5$	$21:55:08.7 \pm 2.5$	0.36
Mount Agliale	$21:53:23.150 \pm 0.300$	$21:54:57.450 \pm 0.100$	0.061
La Spezia	$21:53:18.850 \pm 0.500$	$21{:}54{:}55{.}550 \pm 2{.}400$	0.139
Gnosca	$21:52:37.170 \pm 1.250$	$21:54:21.850 \pm 1.250$	0.173
Varese, Schiaparelli Observatory	$21:52:42.585 \pm 0.100$	$21:54:24.775 \pm 0.100$	0.049
Observatoire de Cote d'Azur, Nice	$21:53:39.661 \pm 0.280$	$21:55:23.301 \pm 0.720$	0.174
Aosta Valley	$21{:}52{:}49{.}240\pm0{.}440$	$21:54:31.565 \pm 0.420$	0.176
Biot, Nice	$21:53:46.800 \pm 5.500$	$21:55:24.750 \pm 3.500$	0.174
Vinon sur Verdon	$21{:}53{:}52.08 \pm 6.70$	$21:55:21.13 \pm 6.00$	0.096

computers. Even though this technique is capable of providing accuracies of 0.01 s, the way in which different operating systems and camera control software deal with time (and possible shutter opening delays) is often not accurate to the level of 0.1 s. Indeed, errors up to a few tenths of a second have been reported in internet-synchronized devices under Windows operating systems (e.g., Barry et al. 2015). As we mention in a paragraph below, these time errors are nevertheless smaller than those arising from the square-well fits to determine ingress and egress times (given the photometric errors and relatively large exposure times as well as large readout times).

The video observations required a specific analysis. We used the Tangra video analysis tool¹² to derive the light curves and the timings that came from the video-inserted GPS-based time stamps whose accuracy is in the order of the millisecond once the small time delays of the video cameras (which depend on the manufacturer) are taken into account. For the instrumental delay Tangra uses the tables provided by Gerhard Dangl¹³.

All the light curves were normalized to the mean brightness level of the blended star and TNO, outside the main occultation event, by dividing the flux by that mean level. Hence, the mean level of the normalized light curve has a value of 1 outside the occultation part. The light curves in normalized flux are shown in Fig. 3. The uncertainties in the fluxes were derived from the photometry using Poisson noise estimations as obtained in the photometry software package DAOPHOT. We note that all the uncertainties or error bars given throughout the present paper are 1σ . The average values of the theoretical uncertainties were obtained and compared with the standard deviation of the observations. If a departure was present in the theoretical errors compared to the standard deviation, the individual errors were multiplied by the ratio of the observed and the computed standard deviation. This was often needed because the gain values (number of electrons per count on the detector) were not well known for most of the devices. Hence, we assigned a different error bar to each individual measurement (in other words, we did not assume a constant error bar equal to the standard deviation of the measurements). This is particularly relevant for the values at the occultation, when the relative uncertainties are much higher than outside the occultation.

Once all the occultation light curves were derived, we proceeded to fit square well models to the parts of the light curves that showed the occultation. The fits were performed using the same expressions and methodology as in other occultation studies (e.g., Braga-Ribas et al. 2014; Benedetti-Rossi et al. 2016, 2019; Dias-Oliveira et al. 2017; Ortiz et al. 2017). From those fits, the star disappearance and reappearance times were derived and their uncertainties were determined as those values providing fits such that the values of χ^2 were within the interval $[\chi^2_{min}, \chi^2_{min} + 1]$. The disappearance and reappearance times and their errors are listed in Table 3.

Since the brightness drops at the occultation were all sharp, there is no evidence at all for a global atmosphere in 2002 TC_{302} . The square well models provided very satisfactory fits, without any need for incorporating an atmosphere. Specific calculations to derive upper limits for the pressure of putative atmospheres of different compositions would be needed, but such calculations are beyond the scope of this paper because the range of possible atmospheric compositions and temperature profiles is too wide. However, to give an approximation, based on similar calculations made for Makemake (Ortiz et al. 2012), Quaoar (Braga-Ribas et al. 2013), and 2003 AZ₈₄ (Dias-Oliveira et al. 2017), for which similar noise levels of the light curves were obtained and given that the sizes of the bodies were similar, we can guess that 2002 TC₃₀₂ lacks a global atmosphere with upper limits of the order of 100 nbar in pressure for N2 and CH4 compositions, as described in the papers mentioned above.

The apparent magnitude of 2002 TC₃₀₂ on 22 January, 2018, measured with respect to the *Gaia* DR1 G band was calculated as 20.40 \pm 0.07 mag using the image set from the 1.5 m Sierra Nevada telescope taken closest to the occultation date. Given that the occulted star has a *G* magnitude of 15.589 according to the *Gaia* DR1 catalog, this means that the expected brightness at the bottom of the occultation would be 0.012 in normalized flux.

The derived times of ingress and egress and their uncertainties were the basis on which the chords of the occultation were determined once the positions of the TNO were projected in the plane of the sky. The chords were then used for the subsequent step of determining the projected size and shape.

5. Projected size and shape

Since we expect that large TNOs like 2002 TC_{302} should be triaxial ellipsoids or spheroids (e.g., Tancredi & Favre 2008), and the two-dimensional projection of these shapes is an ellipse, it appears logical to fit such an ellipse to the extremities of the chords.

¹² http://www.hristopavlov.net/Tangra3/

¹³ http://www.dangl.at/ausruest/vid_tim/vid_tim1.htm



Fig. 3. Light curves in normalized flux from all the observatories. The light curves have been displaced in the horizontal axis to account for the different longitudes so that all the occultation drops are visually aligned.

Because the chord from Tavolaia was affected by considerable uncertainty in time due to the technical issue, as explained in Sect. 3, we decided to look for the best shifts of the chords that would result in their centers lying on a straight line. We know that this condition must be satisfied by an ellipse and we have the a priori knowledge that the projected shape of 2002 TC₃₀₂ must be an ellipse. Hence, by shifting the chords in this way we make sure that we get the shape that best matches with the theoretical one. We note that, in addition to small topographic relief, which can cause small decentering of the chords, unexplained time shifts of up to 27s have been reported before (Elliot et al. 2010), and Braga-Ribas et al. (2013) also identified smaller but noticeable shifts, meaning that the possibility of shifting the chords must therefore be considered. Hence, a linear fit of the chord centers (with each chord center weighted by its nominal uncertainty) was performed (see Fig. 4). The shifts were determined from the residuals of the straight line fit.

The ellipse fit was carried out following the same methods as in previous occultations (e.g., Braga-Ribas et al. 2013, 2014; Benedetti-Rossi et al. 2016, 2019; Dias-Oliveira et al. 2017; Ortiz et al. 2017). The fitted parameters are the center, the semiaxes, and the tilt angle of the ellipse.

The resulting ellipse fit is illustrated in Fig. 5. The axes of the ellipse are 543.2 ± 18 km and 459.5 ± 11 km, with a position angle of 3 ± 1 degrees. In this case the errors were determined using the same procedure as in previous occultation studies (e.g., Braga-Ribas et al. 2013, 2014; Benedetti-Rossi et al. 2016, 2019; Dias-Oliveira et al. 2017; Ortiz et al. 2017). The equivalent diameter in projected area is 499.6 km.

Whether the 3D shape of 2002 TC₃₀₂ is a triaxial ellipsoid (with a > b > c, and a, b, c being the semiaxes of the body)

or an oblate spheroid (with a = b > c) is something that cannot be determined from an occultation alone (several occultations at different rotational phases would be needed, or rotational light curves should be obtained to complement the occultation information). In our case we combined rotational light curves with the occultation. We discuss the two possible shapes in the following sections.

Light curves of 2002 TC₃₀₂ to determine the rotational period

The occultation-derived ellipse is just an instantaneous projection of the 3D shape. Therefore, the rotation period and rotational light curve must be determined in order to interpret the occultation results. If the rotational light curve is double peaked, then it is very likely that the object is a triaxial body, although it could also be an oblate spheroid with a large irregularity. There are also cases of bodies with an oblate shape that present doublepeaked rotational light curves arising from albedo variability on their surfaces. A notable example of this is the dwarf planet Ceres, whose oblate shape is well known from stellar occultations (e.g., Gomes-Júnior et al. 2015) and the DAWN spacecraft visit (e.g., Russell et al. 2016), while it exhibits a low-amplitude double-peaked rotational light curve due to albedo features (e.g., Chamberlain et al. 2007).

Thirouin et al. (2012) obtained the rotational light curve of 2002 TC_{302} in 2010 using the 1.5 m telescope at Sierra Nevada Observatory. That rotational light curve appeared to be single-peaked with a period of 5.41 h, although periods of 4.87 and 6.08 h were also possible. Unfortunately, the amplitude of the



Fig. 4. Chords of the occultation in the sky plane and a linear fit to the centers of the chords. North is up, east to the left. Each color represents a different chord as labeled in the insert. The time shifts needed for the centers of the chords to be aligned are also shown in the insert. The black dots denote the centers of the chords and the dashed line represents the fit.

variability was not high (only 0.04 ± 0.01 mag), and in such cases, the confidence in the determined rotation period is difficult to assess. A clear example of this problem is illustrated with the case of the dwarf planet Makemake, for which 24 h aliases can have very similar spectral power or even higher spectral power than the true rotation period when using data with noise levels similar to the amplitude of the variability. For the dwarf planet Makemake, potential periods of 11.24, 11.41, and 20.57 h were initially identified in the periodogram derived shortly after its discovery (Ortiz et al. 2007), but later on, it was found that the 11.41 h period was the closest 24 h alias of a preferred singlepeaked period of 7.77 h (Heinze & DeLahunta 2009). However, the most recent work on Makemake photometry, using a very large time series, indicates that a double-peaked rotational light curve is favored and the true rotation period is twice the 11.41 h period (Hromakina et al. 2019). Therefore, finding the correct rotation period and rotational light curve of bodies with variability of low amplitude is considerably difficult and there is a clear bias toward detecting shorter periods, which are much easier to detect than longer periods (Sheppard et al. 2008).

It was therefore important to analyze more data on 2002 TC_{302} in an attempt to shed light on its rotational light curve and rotation period. Within our program of physical characterization of TNOs, we observed 2002 TC_{302} in 2014 and 2016 with the 1.5 m telescope at Sierra Nevada Observatory and with the 1.2m telescope at Calar Alto observatory in specific photometry

runs. After the successful occultation we also carried out specific runs in 2018 and 2019. The observations were performed in the same way and with the same instruments as described in Sect. 2. The methods and tools used to extract the photometry were the same as those explained in Fernández-Valenzuela et al. (2019). A total of 875 measurements were obtained, which can be found in Table A.2 associated with this publication.

The observing runs in 2019 were the most complete ones in terms of the number of consecutive observation nights and the coverage in number of hours per night (and also in terms of S/N). In those runs we observed the target for 7 to 9 nights in a row, and most of the nights covered more than 8 h and up to 10 h on the target. Using the photometry from those observation nights in 2019 it was already clear that a rotation period of ~5.41 h was not seen in the data. The light curves folded to that period (or values close to it) did not show convincing variability or low dispersion. Given that most of the nights had data in time spans longer than 8 h and no clear variability was seen, it appeared that longer periods than 8 h would be favored.

There is additional reasoning to believe that the preferred rotation period for 2002 TC₃₀₂ should be longer than ~5.4 h. According to Tancredi & Favre (2008) the typical size for which hydrostatic equilibrium would be expected in icy bodies like the TNOs is well below that of 2002 TC₃₀₂. The equilibrium shapes can be Maclaurin or Jacobi shapes (Chandrasekhar 1987).



Fig. 5. Chords of the occultation in the plane of the sky and elliptical fit to the chords. The color coding is the same as that in Figs. 3 and 4. The red segments at the chord extremities show the uncertainties from the ingress and egress fits. We note the asymmetry between ingress and egress timing uncertainties in tracks 1, 2, and 6. This is due to operational overheads of the detectors and if the ingress (or the egress) takes place during one of these periods, the uncertainty is larger than that solely due to the photometry noise. The near misses at Sabadell and Agerola are indicated as dashed red lines (easternmost and westernmost respectively).

The minimum density that a Maclaurin body with 5.4 h rotation could have is ~1150 kg m⁻³. For this density the axial ratio a/cis larger than 2.5 using the Maclaurin sequence. Hence, in order to give rise to the projected axial ratio a/c of 1.18 seen in the occultation, the aspect angle would have to be extremely low, which is very unlikely, and in any case, the density is considerably high for a TNO of this size (see e.g., density vs. size plots in Grundy et al. 2015, 2019; Bierson & Nimmo 2019). Another possibility is a Jacobi body; however, given the short rotation period and axis ratio detected from the occultation, this would require an even larger density. For more plausible densities, well below 1150 kg m⁻³, there is no hydrostatic equilibrium shape possible for a homogeneous body with rotation period of 5.4 h. There is the possibility that 2002 TC₃₀₂ has adopted an oblate spheroid shape while having a smaller density than that predicted by the hydrostatic equilibrium if the system behaves like a granular medium or if the object is not homogeneous (differentiated). These are two scenarios to explain the low density of Haumea compared to the hydrostatic equilibrium scenario for a homogeneous body, as shown in Ortiz et al. (2017). In other words, the same scenarios that make Haumea less dense than expected could be at play for 2002 TC₃₀₂. In summary, either 2002 TC₃₀₂ is governed by granular physics (and/or it is differentiated) or the rotation of the body is slower than 5.4 h. We think the latter

possibility is more plausible. On the other hand, as already mentioned, it is well known that the scientific literature is biased against long periods (Sheppard et al. 2008) and in order to look for long rotation periods, extensive datasets are needed.

Hence, we combined all our runs in order to look for long periods in the data. To combine all our runs from 2014 to 2019, we did not use absolute photometry because it is often extremely difficult to achieve 0.02 mag accuracy in the absolute calibrations using standard Johnson or Sloan filters, and we would still have to correct for solar phase angle effects. The absolute calibrations are even more problematic where unfiltered observations are used, which is our case (in order to achieve high S/N). For all the above, the use of absolute calibrations results in jumps of a few per cent in brightness from run to run, which is prohibitive when deriving low-amplitude light curves. Therefore, we normalized the fluxes of each campaign to the mean value of the run. In other words, the fluxes were divided by the mean flux of the run. For long runs, this method should work properly because the mean flux in the run should be similar to the mean flux averaged over a rotation cycle, but for short runs or for very long rotation periods, this method can introduce small shifts in the photometry and spurious frequencies in the periodograms. In our case, all runs lasted more than 3 days and so the way of combining the runs by normalizing to the



Fig. 6. Phase dispersion minimization results for the entire photometry data set from 2014 to 2019. The horizontal line indicates where the minimum value is obtained, which corresponds to a period of \sim 56.1 h.

mean value is much better than using absolute calibrations; nevertheless we cannot completely discard that some effects are present.

Once we combined all the datasets we analyzed all the photometry (with times corrected for light travel time) from 2014 to 2019 using the phase dispersion minimization (PDM) technique. The PDM technique confers an advantage over other periodfinding techniques in that a period is found independently of the shape of the light curve, and it is therefore better at finding double-peaked light curves caused by shape effects than other techniques. We found that a period of ~56.1 h gives a clear minimum (see Fig. 6). This period corresponds to a shape-induced rotational light curve because a relative minimum at ~28 h (half the best period) is also seen in the PDM plot. In the plot, there is also a sharp minimum at ~64 h, but it is considerably less pronounced, and so our preferred period is ~56.1 h. From the analysis with the PDM technique, it appears that we have a shape-induced rotational light curve of low amplitude with a period of ~56.1 h. The peak to valley amplitude of a fourth-order Fourier fit to the light curve folded to 56.1 h is 0.06 ± 0.01 mag (see Fig. 7). This period is consistent with the period found in the astrometry residuals (explained in the following section) and therefore it would be consistent with the orbital period of a potential satellite whose spin and orbit are locked. Nevertheless, it is possible that we have two or more photometric periods superimposed in the light curve (from the satellite and from the primary), making the analysis of this low-amplitude light curve even more complicated and making the identification of just one period difficult.

7. Time series astrometry

The same large image dataset that was obtained for photometry purposes was also analyzed astrometrically with the same tools and techniques described in Sect. 2. The astrometry was derived with respect to the *Gaia* DR2 catalog because it was already available when we started this analysis (but not at the time when the occultation predictions were made). The complete astrometry dataset from 2014 to 2019 is presented in Table A.3 associated with this publication. An orbital fit to all the data was carried out and the residuals to the orbit were obtained both in right ascension (RA) and declination.



Fig. 7. Photometry measurements of 2002 TC_{302} folded to a period of 56.0642 h. The small dots correspond to the single data points whereas the asterisks represent the median values binned in phase bins of 0.083. The error bars show the dispersion of the data in each bin. The solid line represents a smoothed curve using a width of 80 points and the dashed line shows a fourth-order Fourier fit to the data. The light-travel-corrected epoch for zero phase is JD 2 456 895.252777.

The standard deviation of the residuals is 0.06 arcsec. This is somewhat larger than expected given the S/N of the observations, and could mean that there are systematic errors or real short-term or long-term oscillations in the data. If the oscillations are real, they can be tied to the presence of a satellite.

The epochs of the residuals were corrected for light travel time and the residuals were analyzed using the Lomb-Scargle periodogram technique as done for Orcus to reveal the oscillation caused by its satellite Vanth (Ortiz et al. 2011). Depicted in Fig. 8, the periodogram of the declination residuals shows three main peaks at 0.4239, 0.4265, and 0.4408 cycles day⁻¹ (56.61, 56.27, and 54.44 h, respectively). The spectral power of these peaks is well above any other and their significance levels are well above 99.9%. The peak at 0.4239 cycles day⁻¹ has a higher spectral power than the other two peaks but the other two cannot be ruled out. It is therefore clear that there is a periodic signal with frequency in the range 0.4239 to 0.4408 cycles day⁻¹, or periods between 54.4 and 56.6 h. The periodogram of the RA residuals (Fig. 9) shows peaks at 0.4233 and 0.4260 cycles day⁻¹ although the highest peak in the periodogram corresponds to a frequency of 0.05823 cycles day⁻¹ or a period of 412.1 h (17.17 days). If such a 17.17 day oscillation were caused by a satellite, the satellite would have been easily spotted in Hubble Space Telescope (HST) images (see discussion), and so we tend to believe that it is an artifact because the residuals in RA showed larger scatter and might be more affected by differential chromatic refraction than those in declination.

It therefore appears that the residuals have a periodicity in the range 0.4239 to 0.4408 cycles day⁻¹. Although the exact frequency or period is difficult to determine within this interval, our preferred estimate is 0.4239 cycles day⁻¹ (56.61 h), which is very similar the period found with the PDM technique in the photometric datasets (see Sect. 5). The peak to valley amplitude of a sinusoidal fit to the RA residuals folded to the 56.61 h period is 0.017 \pm 0.006 arcsec. The peak to valley amplitude of a sinusoidal fit to the declination residuals phased to the 56.61 h period is 0.009 \pm 0.003 arcsec.



Fig. 8. Lomb-Scargle periodogram of the declination residuals of an orbital fit to the astrometry measurements of 2002 TC_{302} .



Fig. 9. Lomb-Scargle periodogram of the RA residuals of an orbital fit to the astrometry measurements of 2002 TC_{302} .

The above phenomenology is consistent with the idea that a satellite could be causing oscillations in the position of the photocenter. This is analyzed in some detail in the discussion below (Sect. 8). In principle, the study of the phase of the RA and the phase of the declination errors (when folded to the orbital period) could potentially give an idea of the orbit orientation of the satellite. If the orbit is more face on, the RA and declination residuals should be out of phase with one another. For instance, a circular, clockwise, face-on orbit would first show the maximum of the declination residuals, followed by the minimum in the RA residuals and after that the minimum of declination would follow. Finally, the maximum in RA residuals would be reached. If the orbit is more edge-on, the RA and declination residuals would be more in phase. Unfortunately, in our case we do not know the exact orbital period and the phases change dramatically depending on the period. We note that the 56.61 h period is close but not an exact match to the \sim 56.1 h period in the photometry. We would expect the two periods to be identical if the putative satellite has its spin locked to its orbit.

8. Discussion

Not counting the Pluto-Charon system, the observations presented here reveal the best observed occultation by a TNO in terms of the number of chords published in the literature thus far. More recently, a stellar occultation by the TNO Huya was observed and the number of chords was even larger than for the case of 2002 TC₃₀₂, but the analysis of the Huya results is still ongoing and only preliminary results have been presented in Santos-Sanz & Ortiz (2019). The large number of chords obtained on 2002 TC₃₀₂ has allowed us to accurately determine its size and shape.

From Herschel and Spitzer thermal measurements, Fornasier et al. (2013) derived an equivalent-area diameter of 584.1_{-88}^{+105} km for 2002 TC₃₀₂ with uncertainties at the 1σ confidence level. This is around 84 km larger than the value derived here from the occultation $(543 \times 460)^{1/2} = 499.8$ km. Even though the values are compatible within the large 88 km error bar of the thermal measurements (which is only at the 1σ level), it is pertinent to note that thermal models tend to underestimate the real effective diameters for ellipsoidal bodies, especially for those with high obliquity, as pointed out by Brown (1985) and as clearly demonstrated for Haumea (Ortiz et al. 2017). In other words, we were expecting the occultation to give a larger equivalent-area diameter than that of the thermal models, but found the opposite. Therefore, the difference of ~84 km could be even more significant. The difference can potentially be explained by the existence of a satellite. We note that the equivalent-area diam-eter of a binary would be $(543 \times 460) + D_s^2 = 584^2$, where D_s^2 is the equivalent-area diameter of the putative satellite. When solving for D_s^2 we come up with $D_s = 302$ km. An upper limit to the diameter for the putative satellite can be obtained from $(543 \times 460) + (D_s^{\text{max}})^2 = (584 + 105)^2$. The resulting maximum diameter for the satellite D_s^{max} would be 474 km, which is almost as large as the main body and this is probably too large to have been undetected in the occultation. If the albedo of the potential satellite was smaller than that of the primary, a somewhat smaller satellite diameter would be possible while still giving the thermal output modeled in Fornasier et al. (2013). For that reason we suggest a plausible size range of 100-300 km for the potential satellite. It is also worth mentioning that the 88 km error bar of the thermal diameter reported in Fornasier et al. (2013) is strikingly large compared to other error bars determined for TNOs of similar size. When looking at the fit to the spectral energy distribution of 2002 TC₃₀₂ in this latter paper (their Fig. 15), it turns out that the fit is poor. According to Kiss (2019, priv. comm.) the Herschel PACS fluxes used in Fornasier et al. (2013) came from the combination of observations at two epochs, but a close look at the Herschel PACS images of the second epoch revealed contamination from a bright source. If only the uncontaminated epoch is used to derive the fluxes, the fit improves considerably, decreasing the error bars and the fitted effective diameter is somewhat larger. With this information, the difference from the thermal diameter and the occultation diameter is probably significant at more than 2σ .

The existence of a satellite close to the body of at least around 100 km in size and up to ~300 km might explain at least part of the difference in size with the thermal measurements and could also explain the oscillations in the high-accuracy time series astrometry as well as the photometry variability. Regarding the photometry variability, if 2002 TC₃₀₂ were found to have a satellite of >100 km in size, with a similar albedo to the main body, the contribution of the satellite to the total brightness of the system would be >(100/499.8)² in percentage, or around ≥ 0.05 mag.

A satellite with a diameter of 200 km would be capable of contributing 0.16 mag, and a satellite of 300 km would give rise to a 0.26 mag contribution; therefore, rotational modulation of the satellite would have contributions below 0.05, 0.16 and 0.26 mag respectively and might explain the low amplitude of the light curve. Hence, we believe that an unresolved satellite could account for a large part of the short-term variability observed. Given that a satellite of 200km in size with 30% variability due to shape irregularities would produce oscillations of $0.3 \times 0.16\%$ or around 0.05 mag, which is not far from the 0.06 mag variability observed, the scenario of a ~200 km satellite producing the observed light curve appears to be coherent. We note that TNOs in the 200 km size range may already be too small to have hydrostatic-equilibrium-dominated shapes and there is some evidence that small TNOs have higher light curve amplitudes than the larger TNOs. Indeed, there is a correlation of light curve amplitude with absolute magnitude (Sheppard et al. 2008).

A potential scenario to explain our photometric observations is that the putative satellite gives rise to the \sim 56.1 h period. However, if this were the case, the main body would be slowed down by the tidal interaction with the satellite and be an oblate spheroid with low variability, which would be difficult to detect and disentangle from the longer period. The periodicity of \sim 56.1 h seems consistent with the orbital period of an unresolved satellite from the astrometry residuals, although the two periods do not exactly match. We note that the light curve would be induced by the shape of the satellite, not by eclipses.

According to the different expressions for the tidal locking timescales applied to TNOs with satellites in Thirouin et al. (2014) and Fernández-Valenzuela et al. (2019), the putative satellite would have synchronized its orbit and spin over a time period of the order of 1–100 Myr, assuming typical values for the tidal dissipation parameter Q and for the rigidity of ice, and assuming a satellite radius of 100 km and a density of 600 kg m⁻³. This timescale is orders of magnitude lower than the age of the Solar System. Hence, it appears likely that the putative satellite would be tidally locked, although a caveat exists in the sense that most of the tidal timescale expressions often rely on oversimplifications of the complex physics of the tidal interaction (Efroimsky & Williams 2009). Therefore, we cannot discard that the rotation period of the potential satellite could be different from the orbital period.

Regarding the rotation period of the primary, as mentioned before, we were not able to firmly determine it. It appears possible that the primary rotation could also be tidally locked with the satellite orbital period, but in that case, a large body such as 2002 TC₃₀₂, presumably in hydrostatic equilibrium or close to it, and spinning at ~56.1 h, would have an oblate shape with axial ratios close to 1. This is far from the observed value of 1.18 for the projected axial ratio seen in the occultation. Hence, a faster spin period than ~56.1 h for the primary seems to be required. If the primary rotated at half that period, the axial ratio of a Maclaurin body with a density around 800 kg m⁻³ would be 1.02, still considerably below 1.18. Therefore, this possibility also seems incompatible with the occultation observations and a shorter rotation period for the primary would be favored.

The putative satellite would have to be very close to the main body to remain unseen in HST observations. There are only two images of 2002 TC_{302} in the HST archive from which no satellite has been reported. We know that HST cannot resolve binary objects that are separated by less than at least several tens of mas, which is the diffraction limit of the telescope. Therefore, any satellite orbiting at less than \sim 2000 km from the main body, would be challenging to detect.

Assuming that the density of 2002 TC₃₀₂ is around 800 kg m⁻³, which is the density expected for a TNO of this size (according to the plots shown in, e.g., Grundy et al. 2015, 2019; Bierson & Nimmo 2019), the mass of the central body can be estimated. This allows us to compute the distance at which a putative satellite would have an orbital period of ~56.1 h. This distance would be ~1780 km. Given that 2002 TC₃₀₂ is currently at 43 Astronomical Units (AU), a semiaxis of 1780 km implies 0.058 arcsec. This is the maximum angular separation and would already be challenging to resolve with HST. During most of the parts of the orbit, the angular separation would be well below the resolution limit for HST, but it may be possible to resolve using the Near Infrared Camera on board the *James Webb* Space Telescope, which has a pixel scale of 0.031 arcsec pixel⁻¹ at short wavelengths (0.6–2.3 μ m).

If the putative satellite has an effective equivalent-area diameter of 200 km and that of the main body is 499.8 km, the ratio of areas and therefore the ratio of brightness is $(200/499.8)^2 = 0.16$. Hence, the photocenter would lie at a distance of $0.058 \times 0.16 =$ 0.009 arcsec from the central body and this means that the total oscillation would be twice that value, or 0.018 arcsec. This is close to the fitted amplitude of the oscillation of the astrometric residuals. A small correction must be applied because the photocenter rotates around the barycenter and the main body is not exactly at the barycenter, but 0.004 arcsec away from it. Therefore, the expected amplitude of the residuals would be 0.014 arcsec, which is even closer to the observational results. This derivation assumes equal albedo for the satellite and the main body. The reality may be somewhat different, and so the required diameter for the satellite may not be exactly 200 km, depending on the exact value of its geometric albedo.

A close satellite would have also been capable of slowing down the rotation of 2002 TC₃₀₂ through tidal interaction. This would also explain the oblate shape that 2002 TC₃₀₂ could have potentially adopted instead of a more triaxial shape as is the case for 2003 VS₂, which is a very similar body to 2002 TC₃₀₂ in terms of size (its triaxial shape has been determined using the same techniques presented in this work; Benedetti-Rossi et al. 2019). A slow rotation of ~20 h could be explained by the tidal interaction of, for instance, a ~200 km satellite orbiting at ~1800 km from the primary.

In this regard, it is pertinent to analyze the system in terms of the specific angular momentum (angular momentum divided by $(GM^3R)^{1/2}$ where *G* is the gravitational constant, *M* the mass, and *R* the radius of the body). The specific total angular momentum (*H*) of a system formed by a primary and a satellite (understood as the sum of the orbital angular momentum plus the angular momentum of the primary and that of the satellite) was computed according to the following equations from Descamps & Marchis (2008):

$$H = \frac{q}{(1+q)^{\frac{13}{6}}} \sqrt{\frac{a(1-e^2)}{R_p} + \frac{2}{5}} \frac{\lambda_p}{(1+q)^{\frac{5}{3}}} \Omega + \frac{2}{5} \lambda_s \frac{q^{\frac{5}{3}}}{(1+q)^{\frac{7}{6}}} \left(\frac{R_p}{a}\right)^{\frac{3}{2}},$$
(1)

where *q* is the secondary-to-primary mass ratio, *a* the semimajor axis, *e* the eccentricity, and R_p the primary radius. The Ω parameter is the normalized spin rate expressed as:

$$\Omega = \frac{\omega_{\rm p}}{\omega_{\rm c}},\tag{2}$$

where ω_p is the primary rotation rate and ω_c the critical spin rate for a spherical body:

$$\omega_{\rm c} = \sqrt{\frac{GM_{\rm p}}{R_{\rm p}^3}};\tag{3}$$

here G is the gravitational constant and M_p the mass of the primary. Assuming a triaxial primary with semi-axes as $a_o > a_1 > a_2$, the λ_p shape parameter is

$$\lambda_{\rm p} = \frac{1+\beta^2}{2(\alpha\beta)^{\frac{2}{3}}},\tag{4}$$

where $\alpha = a_2/a_0$ and $\beta = a_1/a_0$.

In this work, we considered the primary to be nearly spherical ($\lambda_p = 1.0$) and the satellite to be somewhat nonspherical with $\lambda_s = 1.2$.

Using the above expressions, the specific angular momentum of a body of the size of 2002 TC_{302} (with an expected density of around 800 kg m⁻³) spinning at a primordial \sim 7.7 h period would be ~ 0.2 . The primordial rotation period is taken from the Maxwellian fit to the rotation periods of TNOs presented in Duffard et al. (2009). On the other hand, a body with a rotation period of 20 h would have a much smaller specific angular momentum than 0.21, but if 2002 TC₃₀₂ rotates at 20 h and has for instance a tidally locked satellite with a mass ratio of 0.065 to the primary and orbiting at 1780 km from the main body, the specific angular momentum would be 0.21, meaning that such a satellite could have slowed down 2002 TC₃₀₂ from a primordial spin to a rotation period of ~20 h, conserving the total angular momentum of the system. We note that a body with a size around 200 km and with the same density as the central body would have a mass ratio of 0.065 (which is the q parameter that enters the specific angular momentum expression). If the density of the satellite is somewhat smaller than that of the primary, a slightly larger size would be needed for the satellite to give the required angular momentum. Other satellite configurations with smaller mass ratios are possible, and would have slowed down the primary to a period smaller than 20 h. For instance, a satellite with a 145 km diameter would give a mass ratio around 0.024 and would have slowed down the primary to ~ 10 h if orbiting at 1780 km. As a summary, a satellite with a size ranging from \sim 145 to ~200 km orbiting at ~1800 km seems to offer a good overall fit to the phenomenology observed.

Using the projected area of the occultation ellipse and the absolute magnitude of 2002 TC₃₀₂ ($H_V = 4.23$; Tegler et al. 2016), we can derive the geometric albedo as done in Ortiz et al. (2017), for example, for Haumea. The resulting value is 0.147 for 2002 TC₃₀₂. Comparing the geometric albedo of 2002 TC₃₀₂ to those of similar size TNOs for which stellar occultations have been observed (meaning that the size is accurately known and thus the geometric albedo can also be derived with high accuracy), it turns out that 2002 TC_{302} has a higher geometric albedo than that of 2003 AZ_{84} (after accounting for its known satellite as shown in Ortiz et al. 2020), a slightly higher albedo than that of 2003 VS₂ (Benedetti-Rossi et al. 2019) and also slightly higher than that of G!kún||'hòmdímà (2007 UK126; also accounting for its known satellite, Ortiz et al. 2020). Also, the geometric albedo of 2002 TC₃₀₂ is higher than that of Quaoar, which is considerably larger than 2002 TC_{302} . The somewhat higher albedo than expected might also be a hint that 2002 TC_{302} could have a large satellite because in that case, we would be using the H_V corresponding to the combination of the satellite and the main body, whereas we should use a larger H_V value, which would decrease the geometric albedo computation. A satellite of 200 km with a similar albedo to the primary would contribute around 16% of the brightness, meaning that the geometric albedo would be around 16% smaller or around 0.127. This value is closer to the geometric albedo determined by Herschel and Spitzer measurements (Fornasier et al. 2013) and closer to that of similar-sized TNOs. Nevertheless, we cannot expect that the geometric albedo of the TNOs depends only on size. Different formation processes in different areas of the solar nebula may imply different surface compositions, and also posterior dynamical and evolution processes including collisions may have important effects on the final albedo of a TNO. Therefore, the argument on the albedo is just another hint but cannot be considered as conclusive evidence. According to Barkume et al. (2008), 2002 TC₃₀₂ has water ice spectroscopically detected and since water ice is highly reflective, it makes sense that 2002 TC_{302} could be somewhat brighter than the average TNO (for non-water-icebearing bodies), but note that 2003 VS₂, 2007 UK₁₂₆, 2003 AZ₈₄ and Quaoar also have indications of water ice in their spectra (Barucci et al. 2011) whereas their geometric albedos are lower than for 2002 TC_{302} . In the context of the Uranian satellites, it is well known that they show strong water ice bands, and have a variety of moderately low albedos, starting just a little higher than that of 2002 TC₃₀₂ (e.g., Buratti & Mosher 1991), that depend on the mixture of water ice with pollutants. There is also abundant laboratory and modeling literature that describes how the visible albedo and NIR absorption band depths in granular water ice are affected by admixture of dark pollutants (e.g., Clark & Lucey 1984).

While there are clear indications of a satellite, none of the 12 occultation light curves have detected one. Given that the inter-spacing of the chords is smaller than 200 km, the putative satellite should have been detected if it were sufficiently close to the main body at the time of the occultation. However, the sampling of the chords is not good enough away from the main body in the cross track direction, and so a satellite could easily have been missed. We know that Huya, a TNO of similar size to 2002 TC₃₀₂, has a large and close satellite of 213 ± 30 km in diameter, as estimated from unresolved thermal observations (Fornasier et al. 2013), but this satellite has not been detected in the stellar occultation preliminary reported in Santos-Sanz & Ortiz (2019), despite a large number of chords. This clearly illustrates that the putative satellite of 2002 TC_{302} could have easily gone undetected.

Apart from no satellite detection, no ring features or dust structures have been detected during the occultation either. From the occultation dataset with the least scatter, an upper limit to the width of a Chariklo-like dense ring is 7 km at 3σ . This means that a ring similar to that observed at Chariklo would have been missed, but a ring similar in width to that of Haumea would have been detectable. An intermediate ring between that of Chariklo and Haumea, in terms of width, would also have been detected if it existed.

9. Conclusions

On 28 January 2018, 2002 TC₃₀₂ caused a stellar occultation from which we were able to derive its projected size and shape at the time of the occultation with high accuracy. Not counting the Pluto-Charon system, this is the best-observed occultation by a TNO in terms of the number of chords published in the scientific literature to date. The elliptical fit to the 12 chords has a major axis of 543 ± 18 km and minor axis of 460 ± 11 km. This implies an equivalent-area diameter of 499.8 km and a geometric albedo of 0.147 (for an absolute magnitude of 4.32). The smaller equivalent diameter than the radiometrically derived value from Herschel and Spitzer observations and the larger albedo could be evidence for the presence of a large satellite close to 2002 TC_{302} . There are other hints from ground-based observations that point in that direction. From the sharp disappearance and reappearance of the star in the occultation, we can conclude that 2002 TC_{302} lacks a global atmosphere, with an upper limit of the order of 100 nbar. No ring features or dust structures were detected close to the nucleus, although the data lacked the required quality to discover a dense ring of the width of that of Chariklo. However, a dense ring of the width of that of Haumea would have been easily detected. An intermediate ring in terms of width would also have been detected if present.

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- ¹ Instituto de Astrofísica de Andalucía, IAA-CSIC, Glorieta de la Astronomía s/n, 18008 Granada, Spain e-mail: ortiz@iaa.es
- LESIA, Observatoire de Paris, Université PSL, CNRS, Sorbonne Université, Université de Paris, 5 place Jules Janssen, 92195 Meudon, France
- Laboratório Interinstitucional de e-Astronomia LIneA, Rua Gal. José Cristino 77, Rio de Janeiro 20921-400, Brazil
- Federal University of Technology-Paraná (UTFPR / DAFIS), Curitiba, Brazil
- Observatório Nacional/MCTIC, Rio de Janeiro, Brazil
- Florida Space Institute, University of Central Florida, 12354 Research Parkway, Partnership 1, Orlando, FL, USA
- Dipartimento di Fisica e Astronomia, 'G. Galilei', Universita degli Studi di Padova, Padova, Italy
- INAF Osservatorio Astronomico di Padova, Padova, Italy
- Aix Marseille Univ, CNRS, CNES, LAM, Marseille, France
- 10 INAF - Osservatorio di Astrofisica e Scienza dello Spazio, Bologna, Italy
- 11 Schiaparelli Astronomical Observatory, Varese, Italy
- 12 Astronomical Observatory San Marcello Pistoiese CARA Project, Italy
- 13 Crni Vrh Observatory, Crni Vrh nad Idrijo, Slovenia
- ¹⁴ Faculty of Mathematics and Physics, University of Ljubljana, Slovenia

- ¹⁵ Osservatorio Astronomico di Monte Agliale, Lucca, Italy
- ¹⁶ 55 impasse de la Marjolaine, 83560 Vinon sur Verdon, France
- ¹⁷ Observatorio Astronomico Iota-Scorpii, La Spezia, Italy
- ¹⁸ 1075 avenue Saint Philippe, 06410 Biot, France
- ¹⁹ Observatoire de la Côte d'Azur, France
- ²⁰ Gnosca Observatory, In Fun I Vign 7, 6525, Gnosca, Switzerland
- ²¹ Osservatorio Astronomico di Tavolaia, Pisa, Italy
- ²² Institut Polytechnique des Sciences Avancées IPSA, 63 boulevard de Brandebourg, 94200 Ivry-sur-Seine, France
- ²³ Institut de Mécanique Céleste et de Calcul des Éphémérides, IMCCE, Observatoire de Paris, PSL Research University, CNRS, Sorbonne Universités, UPMC Univ Paris 06, Univ. Lille, 77 Av. Denfert-Rochereau, 75014 Paris, France
- ²⁴ Observatório do Valongo/UFRJ, Rio de Janeiro, Brazil
- ²⁵ International Occultation Timing Association European Section (IOTA-ES), Germany
- ²⁶ Observatoire de Geneve, Sauverny, Switzerland
- ²⁷ Max Planck Institut f
 ür extraterrestrische Physik (MPE), Garching, Germany
- ²⁸ UNESP São Paulo State University, Grupo de Dinâmica Orbital e Planetologia, Guaratinguetá 12516-410, Brazil
- ²⁹ German Aerospace Center (DLR), Institute of Planetary Research, Berlin, Germany
- ³⁰ DFISTS, Universidad de Alicante, Alicante, Spain
- ³¹ IUFACyT, Unversidad de Alicante, Alicante, Spain
- ³² University of Zagreb, Faculty of Electrical Engineering and Computing, Unska 3, 10000 Zagreb, Croatia
- ³³ Physics Division, E.O. Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, CA, 94720 USA
- ³⁴ Astronomical Observatory of the Autonomous Region of the Aosta Valley (OAVdA), Lignan 39, 11020 Nus, Italy

- ³⁵ Konkoly Observatory, Research Centre for Astronomy and Earth Sciences, Konkoly-Thege Miklós út 15-17, 1121 Budapest, Hungary
- ³⁶ ELTE Eötvös Loránd University, Institute of Physics, Pázmány Péter sétány 1/A, 1117 Budapest, Hungary
- ³⁷ Astronomical Institute, Slovak Academy of Sciences, Tatranská Lomnica, Slovakia
- ³⁸ MTA-ELTE Exoplanet Research Group, 9700 Szombathely, Szent Imre h. u. 112, Hungary
- ³⁹ ELTE Gothard Astrophysical Observatory, 9700 Szombathely, Szent Imre h. u. 112, Hungary
- ⁴⁰ Institute for Astronomy, Astrophysics, Space Applications & Remote Sensing, National Observatory of Athens, Athens, Greece
- ⁴¹ University of Crete, Department of Physics, Heraklion, Greece
- ⁴² Eötvös Loránd University, Faculty of Science, Pázmány Péter sétány 1/A, 1117 Budapest, Hungary
- ⁴³ Astronomical Observatory Institute, Faculty of Physics, A. Mickiewicz University, Poznan, Poland
- ⁴⁴ Nunki Observatory, Greece
- ⁴⁵ Ellinogermaniki Agogi Observatory, Greece
- ⁴⁶ Observatorio Astronómico, Universidad de Valencia, Valencia, Spain
- ⁴⁷ Centro de Estudios de Física del Cosmos de Aragón, Teruel, Spain
- ⁴⁸ Dpto. de Astrofísica, Universidad de La Laguna, Tenerife, Spain
- ⁴⁹ Agrupació Astronómica de Sabadell, Barcelona, Spain
- ⁵⁰ Astrocampania, Osservatorio Salvatore di Giacomo, Agerola (NA), Italy
- ⁵¹ via Radicosa 44, 80051 Agerola, Italy