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The Lockman Hole project: LOFAR observations and spectral index properties of low-frequency radio sources

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ABSTRACT

The Lockman Hole is a well-studied extragalactic field with extensive multi-band ancillary data covering a wide range in frequency, essential for characterizing the physical and evolutionary properties of the various source populations detected in deep radio fields (mainly star-forming galaxies and AGNs). In this paper, we present new 150-MHz observations carried out with the LOw-Frequency ARray (LOFAR), allowing us to explore a new spectral window for the faint radio source population. This 150-MHz image covers an area of 34.7 square degrees with a resolution of 18.6×14.7 arcsec and reaches an rms of $160 \mu\text{Jy beam}^{-1}$ at the centre of the field. As expected for a low-frequency selected sample, the vast majority of sources exhibit steep spectra, with a median spectral index of $\alpha_{150}^{1400} = -0.78 \pm 0.015$. The median spectral index becomes slightly flatter (increasing from $\alpha_{150}^{1400} = -0.84$ to $\alpha_{150}^{1400} = -0.75$) with decreasing flux density down to $S_{150} \sim 10$ mJy before flattening out and remaining constant below this flux level. For a bright subset of the 150-MHz selected sample, we can trace the spectral properties down to lower frequencies using 60-MHz LOFAR observations, finding tentative evidence for sources to become flatter in spectrum between 60 and 150 MHz. Using the deep, multi-frequency data available in the Lockman Hole, we identify a sample of 100 ultra-steep-spectrum sources and 13 peaked-spectrum sources. We estimate that up to 21 per cent of these could have $z > 4$ and are candidate high- z radio galaxies, but further follow-up observations are required to confirm the physical nature of these objects.

Key words: surveys – galaxies: active – radio continuum: galaxies.

1 INTRODUCTION

Although the majority of the earliest radio surveys were carried out at very low frequencies (i.e. the 3rd, 6th and 7th Cambridge Surveys; Edge et al. 1959; Bennett 1962; Hales, Baldwin & Warner 1988; Hales et al. 2007 and the Mills, Slee and Hill survey; Mills, Slee & Hill 1958), in more recent years large-area radio surveys have primarily been performed at frequencies around 1 GHz such as the NRAO VLA Sky Survey (NVSS; Condon et al. 1998), the Sydney University Molonglo Sky Survey (Mauch et al. 2003) and the Faint Images of the Radio Sky at Twenty centimeters (FIRST) survey

(Becker, White & Helfand 1995). With the advent of radio interferometers using aperture arrays such as the LOw-Frequency ARray (LOFAR), we now have the ability to re-visit the low-frequency radio sky and survey large areas down to much fainter flux density levels, and at higher resolution, than these earlier surveys.

LOFAR is a low-frequency radio interferometer based primarily in the Netherlands with stations spread across Europe (van Haarlem et al. 2013). It consists of two different types of antenna which operate in two frequency bands: the low-band antennas (LBA) are formed from dipole arrays which operate from 10 to 90 MHz, and the high-band antennas (HBA) are tile aperture arrays which can observe in the frequency range 110–240 MHz. The long baselines of LOFAR allow us to probe this frequency regime at much higher spatial resolution than previously done, up to 5-arcsec resolution

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for the longest Dutch baseline, and up to 0.5-arcsec resolution for the European baselines. The combination of LOFAR's large field of view, long baselines and large fractional bandwidth make it an ideal instrument for carrying out large surveys.

The majority of sources detected in these surveys to date have been radio-loud AGN, with star-forming galaxies only beginning to come into the sample at lower flux densities ($S < 5\text{--}10$ mJy). Obtaining large samples of these objects allows us to study the source population in a statistically significant manner and investigate how the properties of radio galaxies evolve over cosmic time. In addition, large surveys allow us to search for rare, unusual objects in a systematic way.

However, in order to maximize the scientific value of these large surveys, complementary multi-wavelength data are essential to obtain a comprehensive view of the source populations. One such field with extensive multi-band coverage is the Lockman Hole field. This field was first identified by Lockman, Jahoda & McCammon (1986) who noted that the region had a very low column density of Galactic H I. This smaller amount of foreground H I makes it an ideal field for deep observations of extragalactic sources, particularly in the infrared (IR) due to the low IR background (Lonsdale et al. 2003). Because of this, there are extensive multi-band ancillary data available, including deep optical/NIR data from ground-based telescopes (e.g. Fotopoulou et al. 2012), mid-IR/FIR/sub-mm data from the *Spitzer* and *Herschel* satellites (Mauduit et al. 2012; Oliver et al. 2012) and deep X-ray observations from *XMM-Newton* and *Chandra* (Polletta et al. 2006; Brunner et al. 2008).

In addition, the Lockman Hole field has an extensive amount of radio data covering a wide range in frequency. This includes the 15-GHz 10C survey (Davies et al. 2011; Whittam et al. 2013), deep 1.4-GHz observations over 7 square degrees observed with the Westerbork Synthesis Radio Telescope (WSRT; Guglielmino 2012; Prandoni et al. 2016a, in preparation), 610-MHz Giant Metrewave Radio Telescope (GMRT) observations (Garn et al. 2008) and 345-MHz WSRT observations (Prandoni et al. 2016b, in preparation). In this paper, we present LOFAR observations of the Lockman Hole field, which extends this multi-frequency information down to 150 MHz, allowing us to study the low-frequency spectral properties of the faint radio source population. For a brighter subsample, we were also able to perform a preliminary analysis of the spectral properties down to 60 MHz.

Studying the spectral index properties of the radio source population can provide insight into a range of source properties. For example, the radio spectral index is often used to distinguish between source components in AGN (i.e. flat-spectrum cores versus steep-spectrum lobes or ultra-steep-spectrum relic emission). Spectral information can also be used to derive approximate ages of the radio source based on spectral ageing models (see e.g. Harwood et al. 2013; Harwood, Hardcastle & Croston 2015 and references therein), providing insight into the average life cycle of radio-loud AGN.

Previous studies that have looked at the average spectral index properties of large samples have reported conflicting results as to whether the median spectral index changes as a function of flux density (Prandoni et al. 2006; Ibar et al. 2010; Randall et al. 2012; Whittam et al. 2013). These studies have generally been carried out at GHz frequencies, with studies of low-frequency selected sources typically showing evidence for the median spectral index to become flatter at fainter flux densities (Ishwara-Chandra et al. 2010; Intema et al. 2011; Williams, Intema & Röttgering 2013). However, most of these latter studies have been biased against detecting steep-spectrum sources at the fainter end of the flux

density distribution due to the flux limits imposed by the different surveys used.

The wide frequency coverage available in the Lockman Hole, along with the large area surveyed, also allows us to search for sources with more atypical spectral properties such as those with ultra-steep or peaked spectra.

In this paper, we present 150-MHz LOFAR observations of the Lockman Hole field. In Section 2, we discuss the observational parameters, data reduction and source extraction of the 150-MHz LOFAR observations, followed by a brief overview of additional 60-MHz LOFAR observations that are used for the spectral analysis. In Section 3, we present an analysis of the source sizes and resolution bias which are used to derive the 150-MHz source counts and in Section 4 we investigate the spectral index properties of low-frequency selected radio sources. Section 5 presents a deeper look at sources that exhibit more unusual spectral properties (e.g. ultra-steep-spectrum or peaked-spectrum sources), providing insight into how many of these sources we might expect to find in the completed LOFAR all-sky survey. We conclude in Section 6. Throughout this paper, we use the convention $S_\nu \propto \nu^\alpha$.

2 OBSERVATIONS AND DATA REDUCTION

2.1 LOFAR HBA observations

The Lockman Hole field (centred at $\alpha = 10^{\text{h}}47^{\text{m}}00^{\text{s}}.0$, $\delta = +58^{\text{d}}05^{\text{m}}00^{\text{s}}$ in J2000 coordinates) was observed on 2013 March 18 for 10 h using the LOFAR HBA array. A total of 36 stations were used in these observations: 23 core and 13 remote stations. The 'HBA_DUAL_INNER' array configuration was used, meaning that the two HBA substations of each core station were treated as separate stations, resulting in 46 core stations. In addition, only the inner 24 HBA tiles in the remote stations are used so that every station has the same beam.¹ Using this array configuration resulted in baselines ranging from 40 m up to 120 km. These observations used a bandwidth of 72 MHz, covering the frequency range from 110 to 182 MHz, which was split into 366 subbands of 0.195 MHz. Each subband consists of 64 channels. In order to set the flux scale, primary flux calibrators 3C 196 and 3C 295 were observed for 10 min on either side of the Lockman Hole observations with the same frequency setup. An overview of the LOFAR observation details of the Lockman Hole field is given in Table 1.

2.2 Data reduction

2.2.1 Pre-processing pipeline

The initial steps of the data reduction were carried out using the automated Radio Observatory pre-processing pipeline (Heald et al. 2010). This involves automatic flagging of RFI using `AOFLAGGER` (Offringa, van de Gronde & Roerdink 2012; Offringa et al. 2013) and averaging in time and frequency down to 5-s integration time and four channels per subband. Since LOFAR views such a large sky area, the brightest radio sources at these frequencies (referred to as the 'A-team' sources: Cygnus A, Cassiopeia A, Taurus A and Virgo A) often need to be subtracted from the visibilities following a process termed 'demixing' (van der Tol, Jeffs & van der Veen 2007). Using simulations of the predicted visibilities for these observations,

¹ Full width at half-maximum (FWHM) of $\sim 3^{\circ}.5$ at 150 MHz in the case of the Lockman Hole field.

Table 1. Observational parameters for the Lockman Hole field.

Observation IDs	L108796 (3C 295) L108798 (Lockman Hole) L108799 (3C 196)
Pointing centres (J2000)	08 ^h 13 ^m 36 ^s .0 +48 ^d 13 ^m 03 ^s (3C 196) 10 ^h 47 ^m 00 ^s .0 +58 ^d 05 ^m 00 ^s (Lockman Hole) 14 ^h 11 ^m 20 ^s .5 +52 ^d 12 ^m 10 ^s (3C 295)
Date of observation	2013 March 18
Total observing time	9.6 h (Lockman Hole) 10 min (3C 196, 3C 295)
Integration time	1 s
Correlations	XX, XY, YX, YY
Number of stations	59 total 23 core (46 split) 13 remote
Frequency range	110–182 MHz
Total bandwidth	72 MHz
Subbands (SB)	366
Bandwidth per SB	195.3125 kHz
Channels per SB	64

it was determined that there was no significant contribution of the A-team sources so no demixing was required for these data.² These averaged data are then stored in the LOFAR Long Term Archive.

2.2.2 Calibration of the data

To set the amplitude scale, we used the primary flux calibrator 3C 295. Antenna gains for each station were obtained using the Black Board Self-calibration (BBS) tool (Pandey et al. 2009), solving for *XX*, *YY* and the rotation angle for each subband separately. Solving for the rotation angle allows us to simultaneously solve for the differential Faraday rotation and remove this effect from the amplitudes measured in *XX* and *YY* without directly solving for *XY* and *YX*, thereby speeding up the process. The amplitude and phase solutions were calculated for each station according to the model of 3C 295 presented by Scaife & Heald (2012) and transferred to the target field for every subband separately. Although the phases are expected to be quite different between the calibrator field and the target field, this was done as an approximate, first-order correction for the delays associated with the remote stations not being tied to the single clock of the core station. As such, the subsequent phase-only calibration solves for the phase difference between the target and calibrator fields rather than the intrinsic phases for that pointing.

To ensure that there was enough signal in the target field for the initial phase calibration, the data were combined into groups of 10 subbands (corresponding to a bandwidth of ~ 2 MHz), but maintaining the 4 channel/subband frequency resolution. An initial phase calibration was performed on 10 subbands centred at 150 MHz using a sky model obtained from LOFAR commissioning observations of the Lockman Hole field (Guglielmino 2012). These 10 subbands were then imaged using the LOFAR imager AWImager (Tasse et al. 2013) which performs both *w*-projection to account for non-coplanar effects (Cornwell & Perley 1992) and *A*-projection to properly account for the changing beam (Bhatnagar et al. 2008) during the 10 h observation.

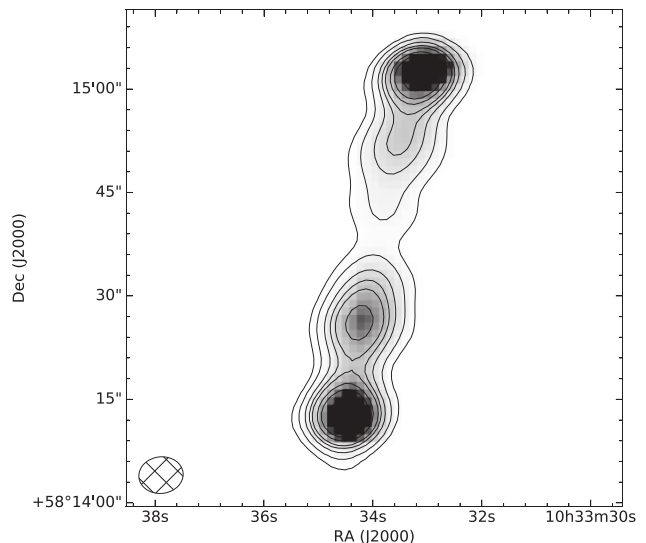


Figure 1. The bright source 3C 244.1 that falls in the LOFAR f.o.v. This source has a flux density of ~ 35 Jy beam⁻¹ and has been removed from the LOFAR images due to the artefacts it produced. The contour levels shown are 0.1, 0.25, 0.5, 0.75, 1.0, 1.5, 2.0, 3.0, 4.0 Jy. This image was made from 8-h observation with LOFAR using a bandwidth of 195 kHz at 150.7 MHz. The beam size is 5.3×6.4 arcsec and the rms reached in this image is 2.6 mJy beam⁻¹.

2.2.3 Peeling 3C 244.1

During the imaging step, it became clear that a single source (3C 244.1, 1.78 deg from the pointing centre) was dominating the visibilities at these frequencies and producing artefacts across the full field of view. To remove these artefacts, 3C 244.1 was ‘peeled’ by first subtracting all other sources in the field, calibrating only 3C 244.1 using a model derived from separate LOFAR observations of this source, and subtracting these visibilities. In order to obtain an accurate model, we observed 3C 244.1 for 8 h at 150 MHz with LOFAR. A single subband at 150.7 MHz was reduced following the procedure described in Section 2.2.2 and then imaged in *CASA* using multi-scale, multi-frequency synthesis (with *nterms* = 2) *CLEAN*. The best image obtained of 3C 244.1 is shown in Fig. 1. After 3C 244.1 had been successfully peeled, all other sources in the Lockman Hole field were added back and another round of phase calibration performed (this time excluding 3C 244.1³). A new sky model for the target field was extracted from these data using *PYBDSM* (Mohan & Rafferty 2015) and the same process repeated on the remaining groups of 10 subbands.

2.2.4 Imaging the data

Once calibrated, and 3C 244.1 successfully peeled, each 10 subband block was imaged with the AWImager using Briggs weighting and a robust parameter of -0.5 in order to inspect the image quality across the full bandwidth. Images with obvious artefacts were excluded from further analysis (66 subbands were excluded, most of which were at the edges of the LOFAR band where the sensitivity decreases). The remaining 300 subbands were then averaged by a factor of 2 in both frequency and time and re-imaged in groups of 50 subbands (10-MHz bandwidth) in order to detect fainter sources.

² The nearest of the A-team sources is Virgo A at an angular distance of 50° .

³ 3C 244.1 has been excluded from all following images and analysis.

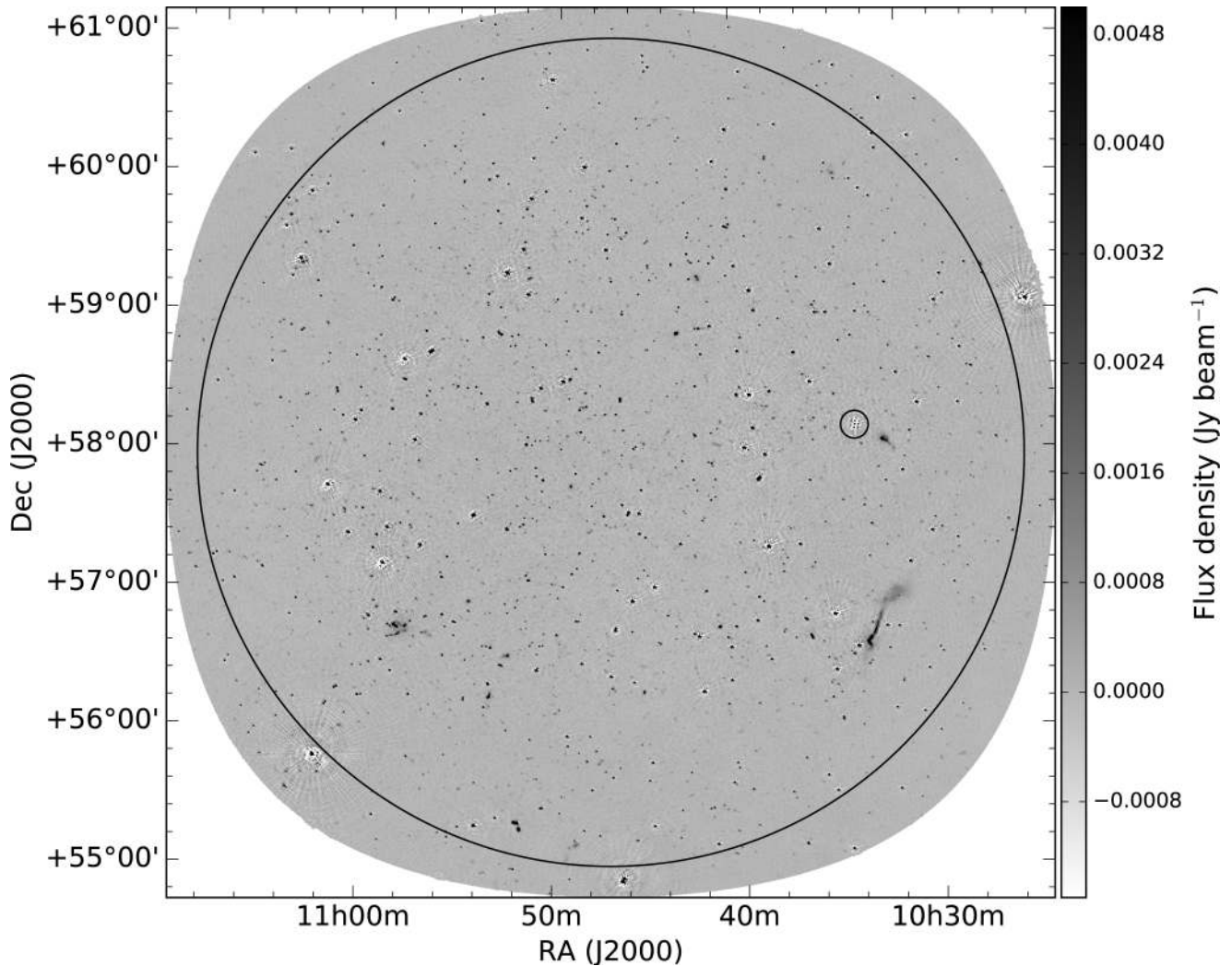


Figure 2. LOFAR image of the Lockman Hole field at 150 MHz. This image has a resolution of 18.6×14.7 arcsec and reaches a noise level of $0.16 \text{ mJy beam}^{-1}$ in the centre of the field. Almost 5000 sources are detected in this image above the 5σ peak flux density level. The smaller circle marks the position of 3C 244.1 which has been subtracted from this image, and the larger circle denotes the 3-deg radius from which we extract sources.

At the time of reducing these data, the software available did not allow us to image large bandwidths taking into account the spectral index of the radio sources (i.e. multi-frequency synthesis with n_{term} higher than 1). As such, we chose to image the data in chunks of 10 MHz to optimize the depth to which we could CLEAN the image without introducing too many errors.

This imaging was carried out in three steps following the procedure presented in Shimwell et al. (2016, submitted). First, an initial image was created using a pixel size of 3.4 arcsec, $\text{robust} = -0.5$ and longest baseline $12 \text{ k}\lambda$. This image was deconvolved down to a relatively high threshold of 20 mJy to create a CLEAN mask which was made from the restored image. Due to artefacts around brighter sources, the deconvolution was then done in two stages to better enable CLEANING of the fainter sources, but avoid CLEANING bright artefacts. The data were first re-imaged using the ‘bright-source’ CLEAN mask down to a threshold set by the largest rms measurement in the noise map. This output image (with the bright sources already deconvolved) was then reprocessed using the ‘faint-source’ CLEAN mask to CLEAN down to a lower threshold approximately equal to the median value of the rms map. Since the synthesized beam changes as a function of frequency, each 50 SB image was then convolved

to the same beam size and all images combined in the image plane, weighted by the variance. This results in a central frequency of 148.7 MHz, but we refer to this image as the 150-MHz LOFAR image hereafter for simplicity.

The resulting image has a final beam size of 18.6×14.7 arcsec with $\text{PA} = 85.7$ and an rms of $\sim 160 \mu\text{Jy beam}^{-1}$ in the centre of the beam. Figs 2 and 3 show the 150-MHz LOFAR image of the Lockman Hole field. The full ~ 30 square degree field is shown in Fig. 2, and a zoomed-in region (approximately 1.5×1 deg) is shown in Fig. 3.

2.3 Ionospheric distortions

One of the biggest challenges with wide-field imaging, particularly at low frequencies, is correcting for the changing ionosphere across the field of view. As a result of applying the same phase solutions to the full field of view, phase errors are still evident around bright sources, particularly in regions furthest away from the pointing centre. In addition, errors in the beam model (in both amplitude and phase) mean that artefacts become worse farther from the pointing centre. In order to image the full field of view at high resolution

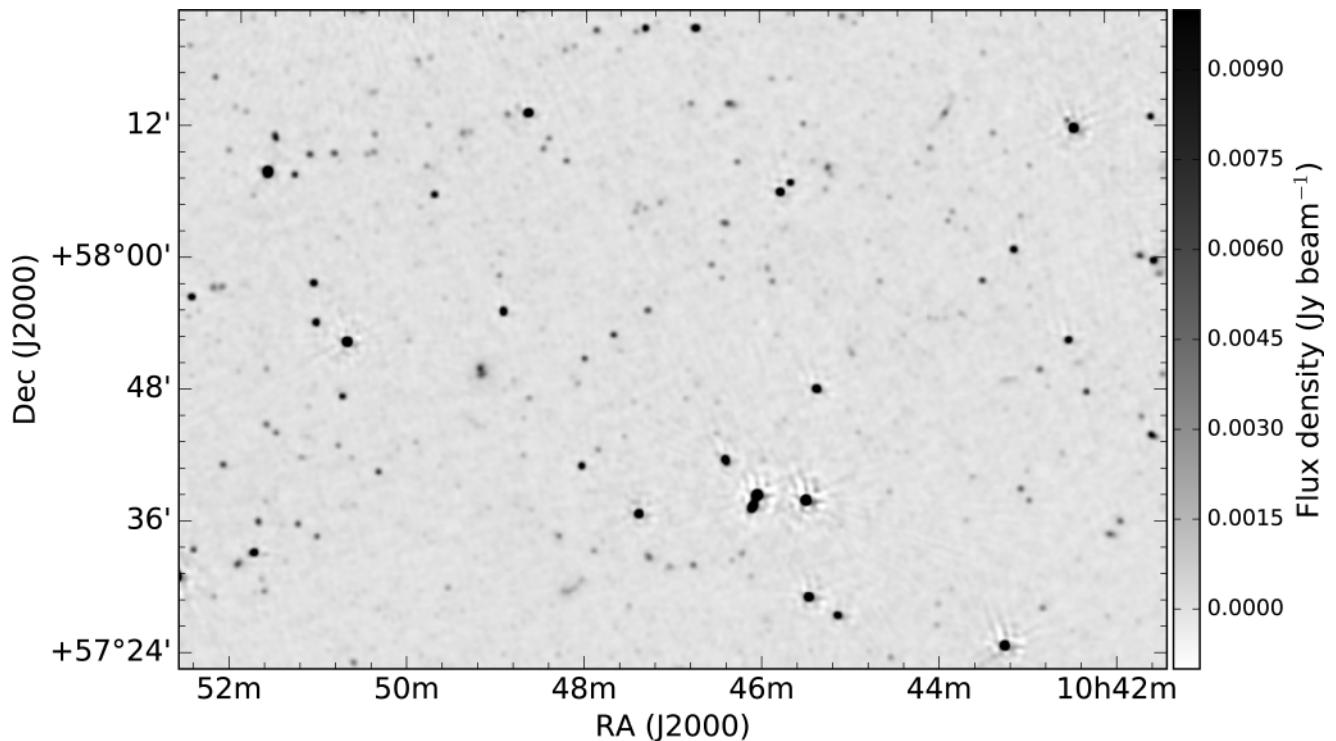


Figure 3. Zoomed-in region of the Lockman Hole field covering an area of 1.5×1 deg. The image details are the same as given in Fig. 2.

(i.e. ~ 5 arcsec using all of the Dutch stations), direction-dependent effects need to be corrected for, requiring a more thorough calibration strategy such as the ‘facet-calibration’ technique presented by van Weeren et al. (2016) and Williams et al. (2016). However, standard calibration techniques are still adequate down to a resolution of ~ 20 arcsec as presented here (see also Shimwell et al., submitted).

Due to the significant computational time required to apply the facet-calibration method, and the fact that for the analysis presented here we are focused on a statistical cross-matching of sources with multi-band radio data (which are typically at ~ 15 -arcsec resolution or lower), we have elected to limit the resolution to ~ 20 arcsec. Calibrating and imaging these data at higher resolution using the facet-calibration technique will be the subject of a future paper.

2.4 Noise analysis and source extraction

A source catalogue was extracted using the LOFAR source extraction package PYBDSM (Mohan & Rafferty 2015). To limit any effects of bandwidth or time smearing, we only extracted sources within 3 deg of the phase centre.⁴ PYBDSM initially builds a noise map from the pixel data using variable mesh boxes. The noise (σ_{local}) increases from $\sim 160 \mu\text{Jy beam}^{-1}$ at the phase centre to $\sim 700 \mu\text{Jy beam}^{-1}$ at the maximum radial distance of 3 deg. However, phase errors result in regions of much higher noise (up to $\sim 5 \text{ mJy beam}^{-1}$) around bright sources. The cumulative distribution of σ_{local} over the region of the map considered for source extraction is shown in Fig. 4. 50 per cent of the total area has $\sigma_{\text{local}} < 400 \mu\text{Jy}$ (see the dotted lines

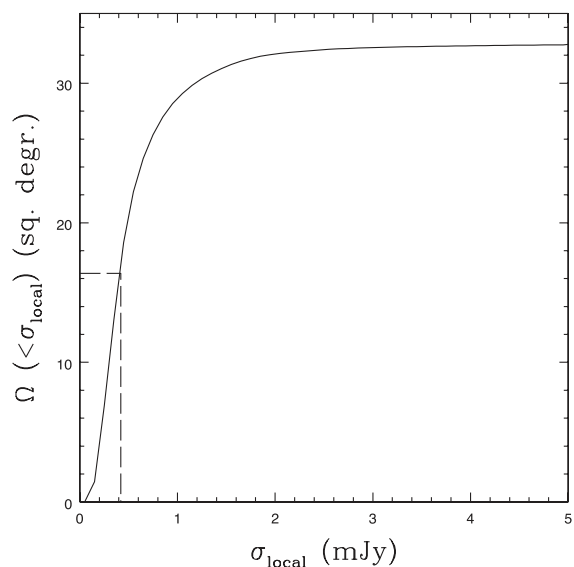


Figure 4. Visibility area of the LOFAR HBA image within 3 deg of the phase centre. Cumulative fraction of the total area of the noise map characterized by a measured noise lower than a given value. Dotted lines indicate the noise value measured over 50 per cent of the total area.

in Fig. 4). This value can therefore be considered as representative of our HBA image.

PYBDSM extracts sources by first identifying islands of contiguous emission above a given threshold, then decomposing this into Gaussian components. A peak threshold of $5\sigma_{\text{local}}$ was used to define sources, and an island threshold of $4\sigma_{\text{local}}$ was used to define the island boundary. The ‘wavelet-decomposition’ option was used during the source extraction, meaning that the Gaussians fitted were then decomposed into wavelet images of various scales. This

⁴ Following the equations given in Bridle & Schwab (1999) and Heald et al. (2015), the combined time and bandwidth smearing at 18.6-arcsec resolution, 3 deg from the pointing centre is $I/I_0 = 0.93$, where I/I_0 refers to the reduction in peak response of a source in the image.

method is useful for extracting information on extended objects. Sources were flagged according to the Gaussian components fitted; ‘S’ means the source was fitted by a single Gaussian component, ‘M’ denotes that multiple Gaussian components were needed to fit the source and ‘C’ refers to a single Gaussian component that is in a shared island with another source.

The final source catalogue consists of 4882 sources above a 5σ flux limit of 0.8 mJy. Of these, 3879 are flagged as ‘S’ (i.e. well described by a single Gaussian), 391 are flagged as ‘C’ (i.e. probable close-spaced double-lobed radio galaxies) and 612 are marked as ‘M’, indicating a more complicated source structure.

2.5 Flux scale and positional accuracy

As discussed in Section 2.2.2, flux densities have been calibrated according to the Scaife & Heald (2012) flux scale. While this in theory should mean that the LOFAR flux densities are consistent with other radio surveys, in practice a number of instrumental and observational effects can combine leading to uncertainties in the absolute flux calibration. These can include errors associated with uncertainties in the LOFAR beam model (which also change with time and frequency), the transfer of gain solutions and ionospheric smearing effects. To confirm that the LOFAR flux densities are consistent with previous low-frequency observations, we have compared the LOFAR flux densities with sources detected in the 151-MHz Seventh Cambridge (7C) survey (Hales et al. 2007) and the alternate data release of the TIFR GMRT Sky Survey (TGSS; Intema et al. 2016⁵). We first cross-matched the LOFAR 150-MHz catalogue with the 151-MHz 7C catalogue. Due to the difference in resolution (~ 20 arcsec compared to ~ 70 arcsec), we have only selected point sources in the LOFAR catalogue (since this has been derived at the higher resolution) for this comparison. Although we are only comparing point sources, here, and in any following analysis, we use the total flux densities for the flux comparison as the peak flux densities might be affected by ionospheric smearing (see discussion in Section 3.2). Using a matching radius of 20 arcsec, we find a total of 60 LOFAR sources that have a counterpart in the 7C survey with the median ratio of the LOFAR flux density to 7C flux density being 1.07 with a standard deviation of 0.25. Due to this systematic offset, the LOFAR 150-MHz flux densities are corrected by 7 per cent.

To verify this correction, we compared the corrected LOFAR flux densities with the TGSS survey. Due to the similar resolutions of the LOFAR data presented here and the TGSS survey, we can also include resolved sources in the cross-matching of these two catalogues, resulting in 631 matches (using a matching radius of 10 arcsec). Using the corrected LOFAR fluxes, we obtain a median flux ratio of $\text{LOFAR}/\text{TGSS} = 1.00$ with standard deviation 0.27. Using the uncorrected flux densities, we obtain a median flux ratio of 1.07, in agreement with the comparison of the 7C survey. Fig. 5 shows the flux density comparisons with both the 7C (red squares) and TGSS (black circles) surveys. For a direct comparison, we plot the uncorrected LOFAR flux densities for both the 7C and TGSS matches.

Given the uncertainties associated with imperfect calibration at these frequencies, and the fact that comparisons with other 150 MHz data sets reveal flux offsets of 7 per cent, a global 7 per cent flux error is added in quadrature to the flux density errors associated with the source extraction (typically of the order of 10 per cent,

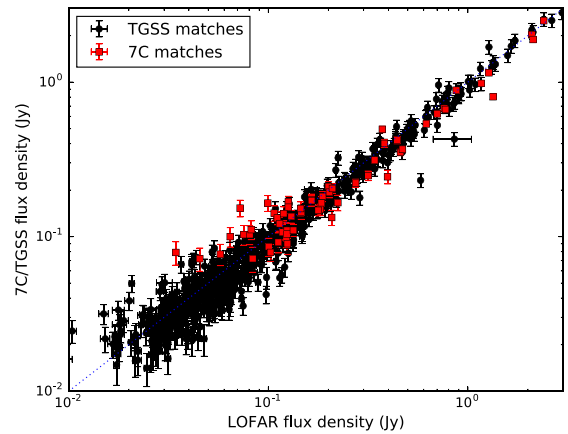


Figure 5. Flux comparison between the LOFAR and the 7C (red squares) and TGSS (black circles) surveys. Only point sources are included when cross-matching with the 7C survey due to the different resolutions of the two surveys, but we use integrated flux densities as the peak flux densities are more heavily affected by ionospheric smearing.

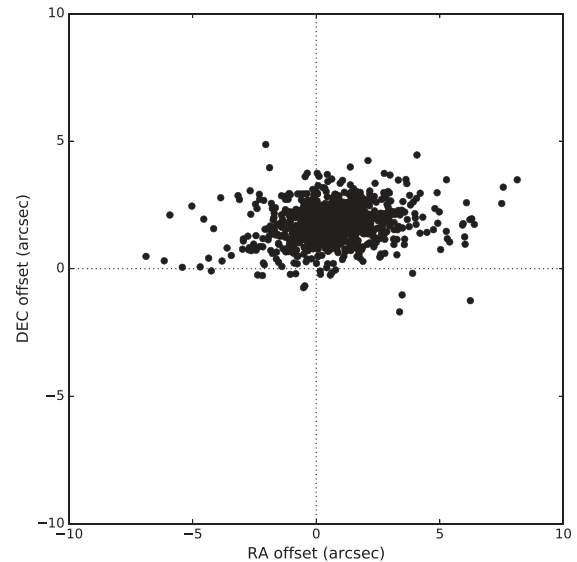


Figure 6. Offset in positions of LOFAR sources compared to FIRST catalogued positions.

but this can vary significantly depending on the flux density of the source).

We also checked the positional accuracy by cross-matching with the FIRST catalogue (Becker et al. 1995), again only including point sources. Fig. 6 shows the offset in right ascension and declination between the LOFAR positions and FIRST positions. This shows a clear systematic offset, primarily in declination, for all sources, not uncommon when doing phase-only self-calibration which can result in positions being shifted by up to a pixel. The offsets are 0.6 arcsec in right ascension and 1.7 arcsec in declination, well below the adopted pixel size. As such, we do not correct for these positional offsets in this work, but care should be taken when using these positions to cross-match with higher resolution observations, in particular when searching for optical or IR counterparts. Any optical/IR counterparts presented in this paper were cross-matched based on more accurate positions provided by deeper observations at 1.4 GHz (see Section 4.3.1).

⁵ <http://tgss.ncra.tifr.res.in/> and tgssadr.strw.leidenuniv.nl/

2.6 LOFAR LBA observations

The Lockman Hole field was also observed at lower frequencies using the LBA array. The LBA observations were carried out at 22–70 MHz on 2013 May 15, using the LBA_OUTER station configuration.⁶ The integration time was 1 s, and each sub-band had 64 channels. Using the multi-beaming capabilities of the LBA, the flux calibrator 3C 196 was observed simultaneously using the same frequency settings (248 subbands of 195.3 kHz each). Flagging and averaging of the data were performed in the same way as for the HBA observations. Due to the larger field of view for the LBA observations, demixing was also carried out on these observations using the observatory’s pre-processing pipeline (Heald et al. 2010). For a preliminary analysis, a set of 10 subbands around 60 MHz were selected for further processing, using the same packages as for the HBA data reduction (see Section 2.2).

The amplitude calibration was carried out in a similar fashion to the HBA data, but in this case using the model of 3C 196 provided by V. N. Pandey. The amplitude gains were smoothed in time to remove the noise and applied to the corresponding target subband. To correct for clock offsets found in the observations, the phase solutions from a single timestamp were also applied. Subsequently, the 10 subbands were merged into a single 2 MHz data set, while maintaining the 40 channel spectral resolution. The merged data set was then phase calibrated using the sky model derived from the 150-MHz HBA observations. Again, 3C 244.1 was peeled to remove strong artefacts from this source and another round of phase calibration performed with the same 150-MHz sky model (this time without 3C 244.1). No direction-dependent ionospheric phase solutions have been derived.

The resolution and noise of the LBA images were optimized using tapering and weighting in order to minimize the effect of moderate to severe ionospheric disturbances, allowing us to trace the spectral properties of the bright sources detected in the HBA image (Fig. 2) down to lower frequencies. The images were produced using AWImager, with a cell size of 5 arcsec and an image size of 6000 pixels. The primary beam (FWHM) at this frequency is ~ 4.5 . The maximum uv range was set at $5 k\lambda$, and the Briggs robust parameter was set to 0. The noise level in the 60-MHz map is 20 mJy beam^{-1} at a resolution of 45 arcsec. Sources were extracted using PYBDSM with the same parameters as used for the HBA source extraction, resulting in a catalogue of 146 sources.

2.6.1 Verification of LBA flux densities

To check the reliability of the flux densities extracted from the LBA image, we cross-matched the 60-MHz LOFAR catalogue with the 74-MHz VLA Low-Frequency Sky Survey Redux (VLSSr) catalogue (Lane et al. 2014). To account for the difference in frequency, we predict 60-MHz flux densities from the VLSSr survey assuming a spectral index of $\alpha_{60}^{74} = -0.8$. Based on these predicted flux densities, we calculate a median flux ratio of LOFAR/VLSSr = 0.80 with a standard deviation of 0.23. Fig. 7 shows the flux density comparison for LOFAR 60-MHz sources against predicted 60-MHz flux densities from the VLSSr survey. Only point sources are included in this analysis due to the difference in resolution (VLSSr has a

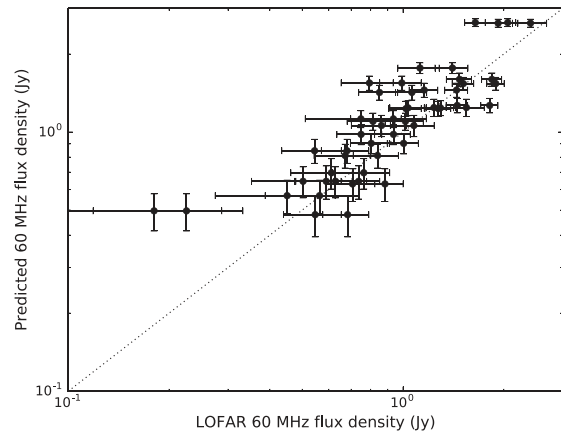


Figure 7. Flux comparison between LOFAR 60-MHz data and predicted 60-MHz fluxes from the VLSSr survey (assuming a spectral index of $\alpha_{60}^{74} = -0.8$). Only point sources are included due to the different resolution of the two surveys, but integrated flux densities are used to avoid the ionospheric smearing effects associated with the peak flux densities.

resolution of 80 arcsec), but we use the integrated flux densities as the peak flux densities are more heavily affected by ionospheric smearing.

The underestimation of the LOFAR LBA flux densities is not unexpected due to the ionospheric conditions during the observations and the fact that these have not been corrected for during the data reduction. Based on the comparison with the VLSSr survey, we scale the LBA fluxes by a factor of 1.25. We also increase the flux densities errors by 20 per cent (added in quadrature to the flux errors reported by PYBDSM) to account for the uncertainties associated with the absolute flux calibration at these frequencies.

3 SOURCE COUNTS AT 150 MHZ

In this section, we present the source counts derived from our 150-MHz catalogue. In order to derive the source counts, we first need to correct for resolution bias and incompleteness at low flux densities. We do this following the procedures outlined by Prandoni et al. (2001, 2006) and by Williams et al. (2016) in deriving the HBA counts in the Boötes field. An early analysis of the source counts in the Lockman Hole region is also presented by Guglielmino (2013).

3.1 Visibility area

To derive the source counts, we weight each source by the reciprocal of its visibility area ($A(< \sigma_{\text{local}})/A_{\text{tot}}$) as derived from Fig. 4. This takes into account the varying noise in the image by correcting for the fraction of the total area in which the source can be detected. However, due to the Gaussian noise distribution, there is still some incompleteness in the lowest flux density bins (i.e. if a source happens to fall on a noise dip, the flux will either be underestimated or the source will potentially go undetected). As demonstrated through Monte Carlo simulations by Prandoni et al. (2000), incompleteness can be as high as 50 per cent at the 5σ threshold, reducing down to 15 per cent at 6σ and to 2 per cent at 7σ . However, such incompleteness effects can be (at least partially) counterbalanced by the fact that sources below the detection threshold can be pushed above it when they sit on a noise peak.

⁶ The LBA stations can only use 48 of the 96 elements. The choice is provided between the inner 48 and the outer 48 (a ring-like configuration).

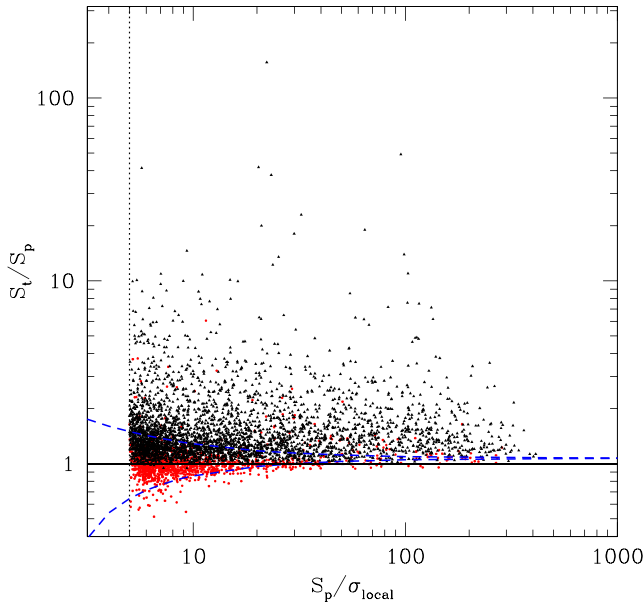


Figure 8. Flux density ratio (S_i/S_p) as a function of S/N of the source. The envelope function defined by equation (2) is shown by the upper dashed line, while the dotted line refers to the S/N = 5 cut-off used in the source extraction. Red dots refer to sources that were detected as unresolved by PYBDSM; black triangles refer to resolved or partially resolved sources (according to the model extracted using PYBDSM). Only sources that lie above the upper dashed line are marked as resolved in the final catalogue. The lower dashed line is obtained by mirroring the upper dashed line.

Williams et al. (2016) have shown through Monte Carlo simulations undertaken in a LOFAR HBA field (Boötes) with a similar noise level (rms ≥ 120 – $150 \mu\text{Jy}$) that such incompleteness effects become negligible above 2 mJy.⁷ As such, we only derive the source counts down to this flux density limit.

3.2 Source size distribution and resolution bias

To measure the extension of a radio source, we can use the following relation:

$$S_i/S_p = \theta_{\text{maj}}\theta_{\text{min}}/b_{\text{maj}}b_{\text{min}}, \quad (1)$$

where S_i/S_p is the ratio of the integrated to peak flux density, θ_{maj} and θ_{min} are the source sizes and b_{maj} and b_{min} refer to the synthesized beam axes (assuming a Gaussian-shaped source). Plotting this flux density ratio (S_i/S_p) against signal-to-noise (S/N), we can establish a criterion for determining if a source is extended. This is shown in Fig. 8. Since the integrated flux density must always be equal to or larger than the peak flux density, sources with $S_i/S_p < 1$ provide a good measure of the error fluctuations. This allows us to determine the 90 per cent envelope function which is characterized by the following equation:

$$S_i/S_p = 1.07 + 2.13 \left(\frac{S_p}{\sigma_{\text{local}}} \right)^{-1}, \quad (2)$$

where σ_{local} refers to the local rms. Here we have assumed two-dimensional elliptical Gaussian fits of point sources in the presence

⁷ While the noise levels reached are similar, the Boötes field was reduced using the facet-calibration technique meaning that the contribution of artefacts will be less in this image. The impact of artefacts on the source counts is mentioned at the end of Section 3.3.

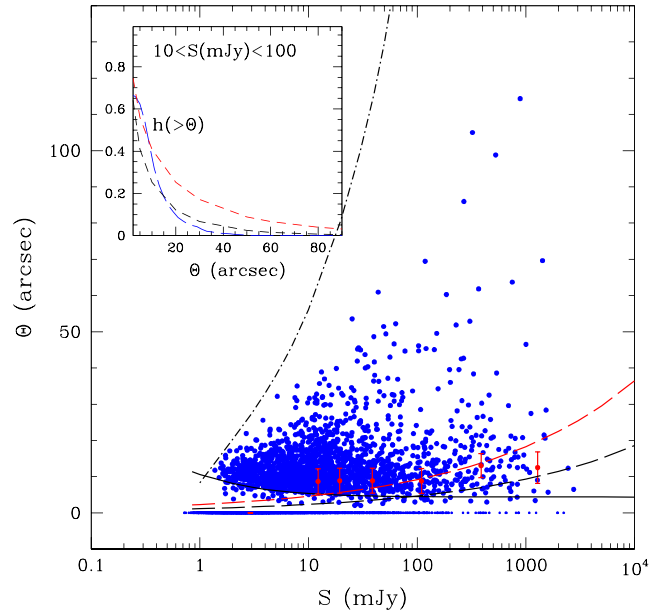


Figure 9. Deconvolved angular size ($\Theta = \sqrt{\theta_{\text{maj}} \cdot \theta_{\text{min}}}$) as a function of integrated flux density. The red points with interquartile bars denote the median source sizes of the sample. The black dot-dashed line represents the maximum size a source can have (Θ_{max}) and still be detected in the source catalogue (i.e. have $S_p = 5\sigma_{\text{local}}$). Above this line, the sample is incomplete due to resolution bias. The black solid line shows the smallest size detectable in these observations (Θ_{min}). The two dashed lines show the median source size relations presented by Windhorst et al. (1990); the black shows the median source size rescaled to 150 MHz using $\alpha = -0.8$ which better describes the larger source sizes, while the red line assumes a factor of 2 larger normalization factor which better describes the smaller sources in our sample. These are also shown in the inner panel which plots the angular size distribution. The distribution obtained from this sample is shown in blue and the Windhorst relations shown in red and black.

of Gaussian noise following the equations of error propagation given by Condon (1997). We have also incorporated the correction for time and bandwidth smearing, which causes a maximum underestimation of the peak flux of 0.93.

This envelope function is shown by the upper dashed line in Fig. 8. Sources that lie above this line are classified as extended or resolved, and sources below the line are considered to be point sources. Note that this is different from the criterion used by PYBDSM during the source extraction (red points are classified as unresolved by PYBDSM and black points show resolved, or partially resolved, sources).

Using equations (1) and (2), we can derive the minimum angular size, Θ_{min} , detectable in these observations. This is shown by the solid line in Fig. 9 where we plot the deconvolved angular sizes against flux density for sources detected in the Lockman Hole. Resolved sources account for ~ 40 per cent of the full sample, increasing to ~ 70 per cent for sources with $S > 10$ mJy and ~ 80 per cent for sources with $S > 60$ mJy. We compare the median angular sizes (for sources with $S > 10$ mJy) and the angular size integral distribution (for sources with $10 \leq S_{\text{mJy}} \leq 100$, inner panel) with the relations presented by Windhorst, Mathis & Neuschaefer (1990) for deep 1.4-GHz samples: $\Theta_{\text{med}} = 2 \times (S_{1.4\text{GHz}})^{0.30}$ (S in mJy and Θ_{med} in arcsec) and $h(>\Theta) = \exp[-\ln 2(\Theta/\Theta_{\text{med}})^{0.62}]$, where Θ_{med} is rescaled to 150 MHz by assuming a spectral index

of $\alpha = -0.8$.⁸ Our sources tend to have larger median sizes with respect to the ones expected from the Windhorst et al. (1990) relation (see the black dashed line in Fig. 9). A better description of the median size distribution of our sources is obtained by assuming a two times larger normalization factor (see the red dashed line).

While somewhat larger sizes can be expected going to lower frequency, such a discrepancy can be explained by the presence of residual phase errors affecting our LOFAR image in the absence of direction-dependent calibration. Phase errors can broaden or smear out sources by a larger factor than bandwidth and time-averaging smearing alone. In addition, at these frequencies, the point spread function is a combination of the synthesized beam and ionospheric smearing effects which varies across the field of view and is not taken into account by the above equations. This hypothesis seems to be supported by the fact that for well-resolved sources (>10 – 15 arcsec), where size measurements are less affected by phase errors, the integral size distribution of our sample is in good agreement with the one proposed by Windhorst et al. (1990).

It is also worth noting that larger source sizes were also noticed by Williams et al. (2016) in their analysis of the Boötes field. In that case, facet calibration was performed, but their higher resolution HBA image was affected by larger combined bandwidth and time-averaging smearing, resulting respectively in radial and tangential size stretching.

The black dot–dashed line in Fig. 9 represents the resolution bias limit. While we are using total flux densities for the source counts, the extraction of the source catalogue is based on the peak flux densities (i.e. $S_p = 5\sigma_{\text{local}}$ to be detected). The resolution bias takes into account the fact that an extended source with flux S_i will fall below the detection limit of the survey before a point source of the same S_i .

Following Prandoni et al. (2001, 2006), a correction c has been defined to account for incompleteness due to resolution bias:

$$c = 1/[1 - h(> \Theta_{\text{lim}})], \quad (3)$$

where $h(> \Theta_{\text{lim}})$ is the assumed integral angular size distribution and Θ_{lim} is the angular size upper limit. This limit is defined as a function of the integrated source flux density:

$$\Theta_{\text{lim}} = \max[\Theta_{\text{min}}, \Theta_{\text{max}}], \quad (4)$$

where Θ_{min} and Θ_{max} are the parameters defined in Section 3.2. Above this limit (Θ_{lim}) we expect to be incomplete. We introduce Θ_{min} in the equation as this accounts for the effect of having a finite synthesized beam size. This becomes important at low flux densities where Θ_{max} approaches 0.

3.3 Source counts

The normalized 150-MHz differential source counts are listed in Table 2. Here we list the flux interval used (ΔS), the geometric mean of that interval ($\langle S \rangle$), number of sources in that bin (N_S), the differential counts normalized to a non-evolving Euclidean model ($dN/dS S^{2.5}$) and the Poissonian errors (calculated following Regeer 1951). Two determinations are provided for the normalized counts: the one obtained by correcting for resolution bias using the Windhorst et al. (1990) relation and the one obtained by modifying the Windhorst et al. $\Theta_{\text{med}}-S$ relation as discussed in the text. For the

Table 2. 150-MHz source counts derived from our LOFAR HBA survey. The normalized counts are derived using both the Windhorst et al. (1990) relation (W90 relation) and the modified $\Theta_{\text{med}}-S$ relation (mod. Θ_{med}) for resolution bias as discussed in Section 3.2.

ΔS (mJy)	$\langle S \rangle$ (mJy)	N_S	$dN/dS S^{2.5}$		$\pm\sigma$
			W90 relation ($\text{sr}^{-1} \text{Jy}^{1.5}$)	mod. Θ_{med} ($\text{sr}^{-1} \text{Jy}^{1.5}$)	
1.9–3.3	2.5	981	72.7	83.0	+2.3, –2.4
3.3–5.7	4.3	872	75.6	86.1	+2.6, –2.7
5.7–9.9	7.5	717	123.3	153.0	+4.6, –4.8
9.9–17	13	561	252.7	288.4	+10.7, –11.1
17–30	23	349	257.9	308.1	+13.8, –14.5
30–50	39	283	734.8	866.3	+43.7, –46.3
50–90	68	165	718.3	820.4	+55.9, –60.3
90–150	117	123	1058	1271	+95, –104
150–270	203	69	1816	2116	+219, –245
270–460	351	59	3280	4025	+427, –483
460–800	608	37	3565	4068	+586, –682
800–1400	1052	20	4515	5224	+1010, –1235
1400–2400	1823	9	4636	5274	+1545, –2060
2400–4200	3157	4	5324	6105	+2542, –4206

counts derivation, we used all sources brighter than ~ 2 mJy, to minimize the incompleteness effects at the source detection threshold discussed above. Artefacts around bright sources can still contaminate our source counts above this threshold as discussed later.

Fig. 10 shows our 150-MHz source counts in comparison with other determinations from the literature. We notice that at high flux densities the counts obtained assuming the $\Theta_{\text{med}}-S$ relation of Windhorst et al. (1990) are more reliable (black filled circles), while at low flux densities, where most sources are characterized by intrinsic angular sizes <10 – 15 arcsec, the counts derived assuming two times larger median sizes (black open circles) should provide a better representation.

Our 150-MHz counts broadly agree with the counts obtained in the Boötes HBA field (Williams et al. 2016), as well as with extrapolations from higher frequencies, with the exception of a few points that are higher than expected. We note that contamination by artefacts (approximately 3.6 per cent, see Section 4.1) can have some impact on our source counts at low/intermediate flux densities, where this effect is of comparable size to the counts associated errors. In addition, extrapolations from 1.4 GHz counts in the Lockman Hole region also show somewhat higher counts at these flux densities, suggesting that cosmic variance effects could play a role in explaining the differences in the source counts between the Lockman Hole and Boötes fields.

4 SPECTRAL INDEX PROPERTIES OF LOW-FREQUENCY RADIO SOURCES

Studying the spectral index properties of low-frequency radio sources allows us to gain insight into the source populations detected at these frequencies. In order to carry out an unbiased analysis, we have defined different subsamples, each with different flux density limits, to best match the corresponding multi-frequency radio information available and represent a complete sample.

We first cross-matched the full LOFAR catalogue with all-sky surveys to form the ‘Lockman-wide’ subsample. Whilst this sample covers the entire field of view, the depth is limited due to the flux density limits of these surveys. In order to investigate the properties of low-frequency radio sources at fainter flux densities, we also formed the ‘Lockman-WSRT’ sample by cross-matching the

⁸ Θ and Θ_{med} represent the geometric mean of the source major and minor axes.

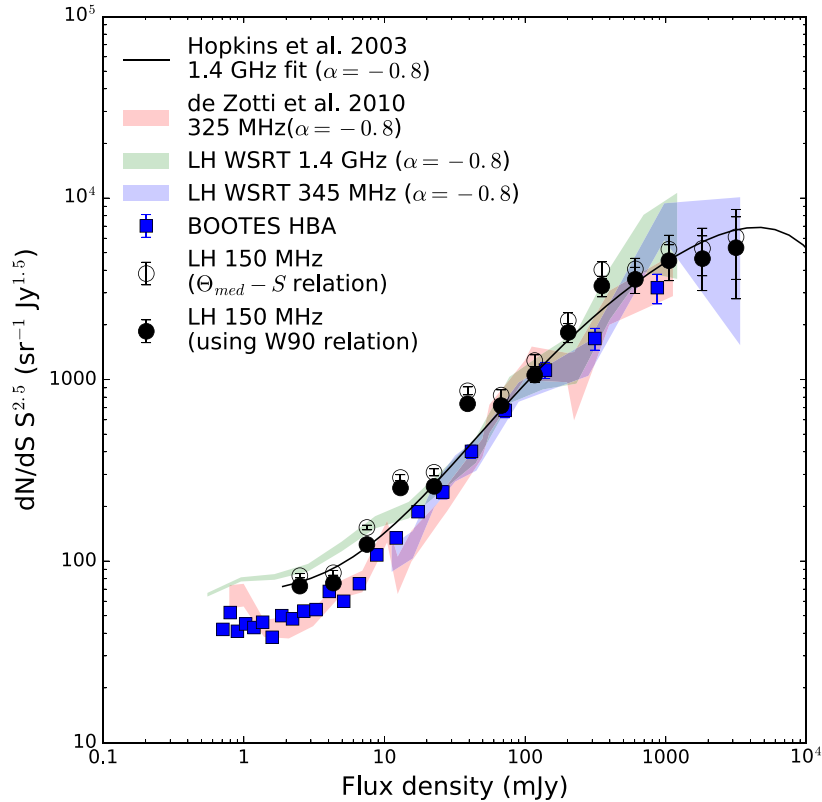


Figure 10. Normalized 150-MHz differential source counts as derived from the catalogue discussed in this work (black points): the two different symbols represent the two recipes adopted for resolution bias correction: Windhorst et al. (1990) relation (filled circles) and modified $\Theta_{\text{med}}-S$ relation (open circles, see the text for detail). Vertical bars represent Poissonian errors on the normalized counts. Our counts are compared to the ones derived in the LOFAR HBA Boötes field (Williams et al. 2016, blue squares) and from extrapolations from higher frequencies. All extrapolations assume a spectral index of $\alpha = -0.8$. The green and blue shaded regions respectively refer to extrapolations from 1.4 GHz and 345 MHz of the recent source counts derived in the same region as part of the Lockman Hole project (Prandoni et al. 2016a,b, in preparation). The red shaded region refers to the 325-MHz data collection discussed by de Zotti et al. (2010), while the black solid line shows the polynomial best fit to 1.4-GHz counts derived by Hopkins et al. (2003).

LOFAR 150-MHz catalogue with deeper 1.4-GHz observations carried out with WSRT. The ‘Lockman-deep’ sample was then formed by cross-matching this deeper Lockman–WSRT subsample with deeper surveys at other frequencies. Forming these subsamples is discussed in more detail in the following sections. An overview of the number of sources falling into each subsample is given in Table 3.

We note that the observations used in this analysis are not contemporaneous so in some cases variability could lead to incorrect spectral indices, particularly for sources with peaked or rising spectra (where emission from the AGN core may be dominating the emission). However, since we select sources at 150 MHz, where the radio emission is dominated by the steep-spectrum lobes built up over time-scales of Myr–Gyr, we do not expect variability to significantly affect the majority of sources.

4.1 Cross-matching with wide-area sky surveys

To investigate the spectral index properties of low-frequency selected sources, we cross-matched the 150-MHz LOFAR catalogue with the 1.4-GHz NVSS (Condon et al. 1998), 325-MHz Westerbork Northern Sky Survey (WENSS; Rengelink et al. 1997) and 74-MHz VLSSr (Lane et al. 2014). Since these surveys are all at lower resolution, we only include LOFAR sources that have deconvolved source sizes less than 40 arcsec, approximately matching the resolution of NVSS. This excludes 25 sources (6.1 per cent)

from the following analysis, potentially biasing against some of the larger radio galaxies. However, given the additional complexities in obtaining accurate spectral indices for these sources, excluding these objects leads to a cleaner sample where the spectral indices are calculated in the same manner.

For each survey, we conducted a Monte Carlo test to compare how many spurious matches are included as a function of search radius. Fig. 11 shows the results of these Monte Carlo tests for each of the NVSS, WENSS and VLSSr catalogues. From this analysis, it was determined that the optimal search radius (to include the majority of real identifications, but limit the number of false IDs) was 15 arcsec for the NVSS catalogue, 20 arcsec for the WENSS catalogue and 25 arcsec for the VLSSr catalogue. For the vast majority of sources, there was only a single match within the search radius so we simply accepted the closest match when cross-matching these catalogues. Most sources are unresolved at the resolution of these surveys, but sources with extreme spectral indices were checked visually to confirm resolution effects were not affecting the spectral index calculation.

All LOFAR sources that were not detected in NVSS were checked by eye to exclude any artefacts that were catalogued during the LOFAR source extraction. This process revealed 14 sources that were identified as artefacts in the LOFAR image, corresponding to 3.6 per cent of the cross-matched sample. This does not include any artefacts that happened to be associated with an NVSS source, but from Fig. 11 this number is expected

Table 3. Radio surveys that were used to form the multi-frequency samples. The numbers listed for each survey in the Lockman-deep sample refer to sources that have $S_{150} > 9$ mJy. The cross-matching of these surveys was carried out for the full Lockman–WSRT sample so the total number of detections for each survey is slightly higher. See Sections 4.3.3–4.3.6 for the total number of matches in each catalogue.

	Survey	Frequency	Resolution (arcsec)	Area covered (square degrees)	rms (mJy)	No. of matches
<i>Lockman-wide:</i>	LOFAR	150 MHz	18.6×14.7	34.7	0.16	4882
	LOFAR	150 MHz	18.6×14.7	34.7	0.16	385
	(Point sources with $S_{150} > 40$ mJy)					
	NVSS	1.4 GHz	45	34.7	0.5	377
	WENSS	345 MHz	54×64	34.7	3.6	367
<i>Lockman–WSRT:</i>	VLSS	74 MHz	80	34.7	100	93
	LOFAR	150 MHz	18.6×14.7	6.6	0.16	1302
	(All sources in same area as WSRT field)					
<i>Lockman-deep:</i>	WSRT	1.4 GHz	11×9	6.6	0.011	1289
	LOFAR	150 MHz	18.6×14.7	6.6	0.16	326
	(Sources in WSRT field with $S_{150} > 9$ mJy)					
	WSRT	1.4 GHz	11×9	6.6	0.011	322
	10C	15 GHz	30	4.6	0.05–0.1	81
	GMRT ^a	610 MHz	6×5	13	0.06	103
	WSRT 90 cm (W90)	345 MHz	70×44	7	0.8	211
LBA	60 MHz	45	6.6	20	42	

^aFor the GMRT catalogue, only point sources with flux densities above 5 mJy were used in the cross-matching (see Section 4.3.4).

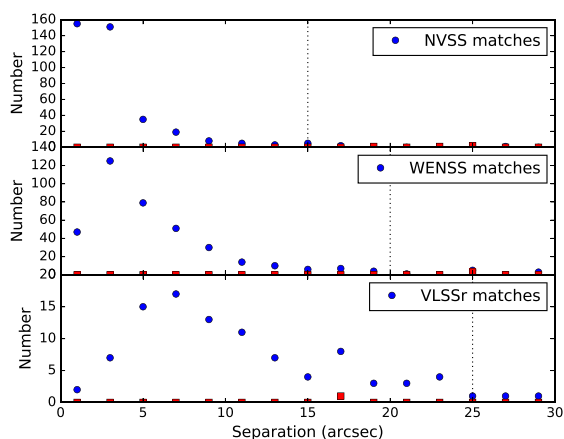


Figure 11. Monte Carlo tests to determine the optimal matching radius for automatically accepting associations in the NVSS, WENSS and VLSSr catalogues. The blue circles show the number of matches as a function of search radius using the LOFAR positions, while the red squares show the number of matches for a random catalogue. The dashed lines mark the search radii chosen for each survey.

to be minimal (i.e. only 1 random match within a 20-arcsec search radius).

Due to the different flux limits of each of these surveys, we have only included sources with $S_{150} > 40$ mJy such that the sample is not dominated by too many unrestrictive limits on the spectral indices. This flux limit was chosen such that any LOFAR sources not detected in NVSS (above a flux limit of 2.5 mJy) have spectra steeper than $\alpha_{150}^{1400} = -1.2$, typically defined as ultra-steep-spectrum (USS) sources (see Section 5.2). Similarly, sources not detected in WENSS (flux limited at 18 mJy) have an upper limit of the spectral index of $\alpha_{150}^{345} < -1.0$. Due to the higher flux limit of the VLSSr survey, only a small number of sources are detected at 74 MHz. For a complete comparison, we have identified a subset of the Lockman-wide sample with $S_{150} > 300$ mJy which, if undetected in the VLSSr survey, gives us a lower limit on the spectral index of $\alpha_{74}^{150} > -0.7$.

All limits were confirmed by visual inspection to ensure that they were true non-detections.

This leaves us with 385 sources that form the Lockman-wide sample. Of this sample, 377 have counterparts at 1.4 GHz in NVSS, 367 have counterparts in WENSS and 93 have VLSSr matches. A summary of the number of matches found in each catalogue is shown in Table 3. Scaife & Heald (2012) note that the WENSS flux densities need to be scaled by a factor of 0.9 for agreement with the flux scale of Roger, Costain & Bridle (1973). However, by comparing with the spectral indices from 150 to 1400 MHz, we found that this correction resulted in underestimated flux densities at 325 MHz for sources in the Lockman Hole. As such, we do not apply this correction in the following analysis.

4.2 Spectral analysis of the Lockman-wide sample

We first study the two-point spectral index from 150 MHz to 1.4 GHz for sources in the Lockman-wide sample. Fig. 12 shows the spectral index distribution which has a median spectral index of $\alpha_{150}^{1400} = -0.82 \pm 0.018$ (errors from bootstrap) and an interquartile range of $[-0.94, -0.70]$. This is slightly steeper than found in previous studies which find the spectral index over these frequencies to be typically around -0.78 (Williams et al. 2016, 2013; Ishwara-Chandra et al. 2010; Intema et al. 2011) but can range from -0.76 (Hardcastle et al. 2016) to -0.85 (Ishwara-Chandra & Marathe 2007).

Based on the spectral indices between 150 MHz and 1.4 GHz, we can classify sources into three different categories: flat-spectrum sources, which we define as $\alpha_{150}^{1400} > -0.5$, make up 5.7 per cent of the sample, steep-spectrum sources ($-1.2 < \alpha_{150}^{1400} < -0.5$) make up 89.4 per cent and USS sources ($\alpha_{150}^{1400} < -1.2$) account for 4.9 per cent of the sample. As expected for a low-frequency survey, the sample is predominately comprised of steep-spectrum radio sources. To determine the fraction of sources that are genuinely ultra-steep, we fit a Gaussian to the distribution shown by the dotted line in Fig. 12. From this distribution, we would expect only 2 per cent of sources to have $\alpha < -1.2$ if we were probing a single

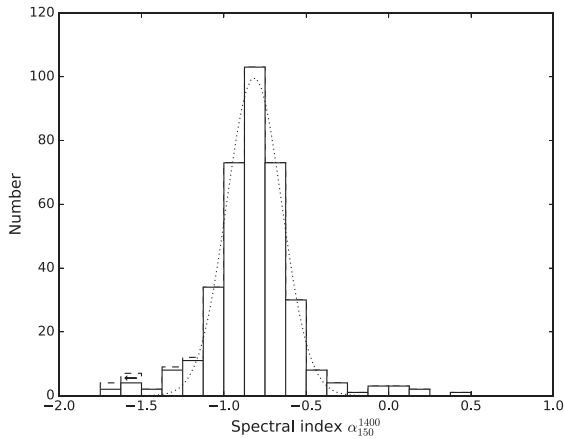


Figure 12. Histogram of spectral indices from 150 MHz–1.4 GHz for sources in the Lockman-wide sample (385 sources). The dashed line indicates upper limits on the spectral index for sources that were not detected at 1.4 GHz. The dotted line marks a Gaussian fit to the distribution showing that there are more ultra-steep and flat-spectrum sources than would be expected in the tail of the distribution (if the spectral indices followed a normal distribution). This indicates that the source population probed by these surveys cover a wide range of source properties which cannot be explained by a single population.

population with finite S/N. This confirms that the source populations revealed in these observations follow a more complicated distribution in source properties and suggests that the majority of outlying spectral indices are real and an intrinsic property of the radio source.

Whilst the two-point spectral index can provide information on the dominant source of the radio emission, assuming a power law over such a large frequency range does not probe any curvature that

may be present. To investigate this, Fig. 13 shows the radio colour–colour plots, which compare the spectral indices between different frequency ranges, for sources in the Lockman-wide sample. The errors on the spectral index were calculated using the following formula:

$$\alpha_{\text{err}} = \frac{1}{\ln \frac{\nu_1}{\nu_2}} \sqrt{\left(\frac{S_{1,\text{err}}}{S_1}\right)^2 + \left(\frac{S_{2,\text{err}}}{S_2}\right)^2}, \quad (5)$$

where $\nu_{1,2}$ refers to the frequencies and $S_{1,2}$ the corresponding flux densities at those frequencies. This takes into account the larger errors associated with spectral indices calculated over a smaller frequency range.

The left-hand plot in Fig. 13 shows the spectral indices between 150 and 345 MHz compared to the spectral indices from 345–1400 MHz. Nearly all of the sources lie on the diagonal line indicating that they exhibit power-law spectra across the entire frequency range (i.e. 150 MHz to 1.4 GHz). The figure on the right probes the spectral indices at the lowest end of the frequency range studied: 74–150 MHz compared to 150–1400 MHz for sources that fall into the VLSSr subset of the Lockman-wide sample. Sources that fall into this subset are marked in black in the left-hand plot, while the full sample is shown by the grey points. Sources that are not detected are shown as limits indicated by the triangles.

Although there is no indication of any spectral curvature between 150 MHz and 1.4 GHz, when going to lower frequencies there is a tendency for objects to lie slightly to the right of the diagonal line, suggesting that the radio spectra of these objects begin to flatten between 74 and 150 MHz. However, to verify if this trend is an intrinsic property of the source population, we first need confidence in our absolute flux calibration.

While the VLSSr flux densities have already been corrected to bring them on to the Scaife & Heald (2012) flux scale,

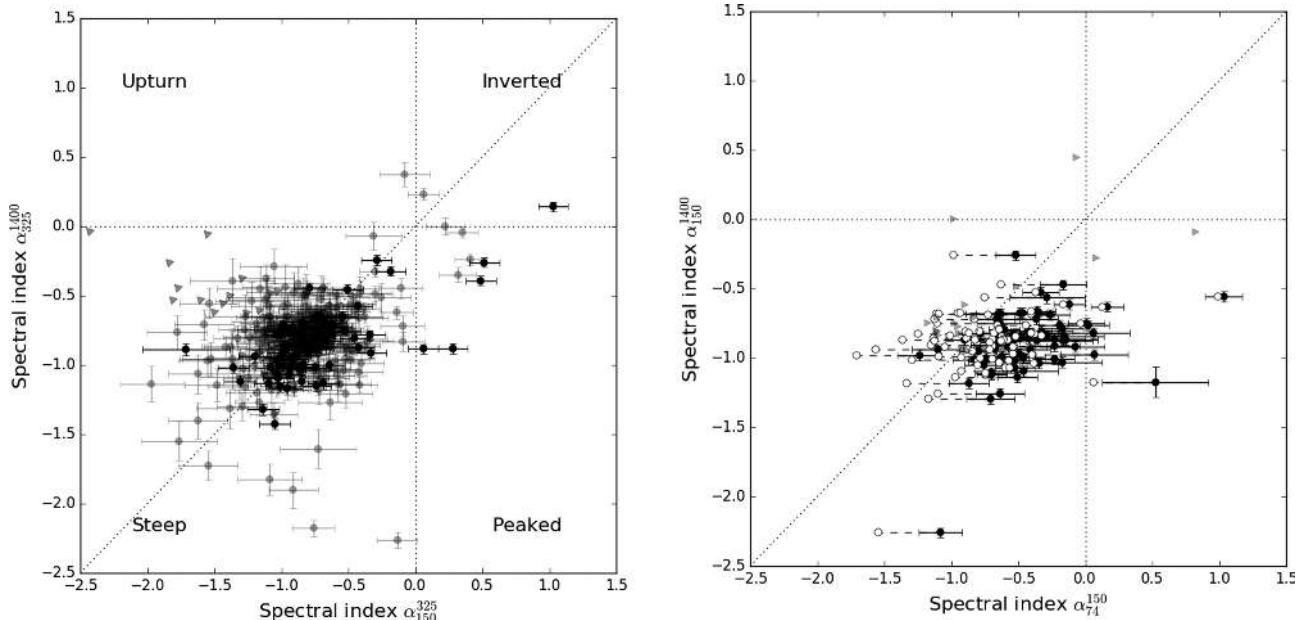


Figure 13. Radio colour–colour plots for sources in the Lockman-wide sample. Left: the spectral indices of the sample between 150 and 325 MHz against the spectral indices from 325 MHz–1.4 GHz. The black points identify the subset of sources which are also shown on the right (i.e. $S_{150} > 300$ mJy). The grey points show the remaining sources in the Lockman-wide sample, and the grey triangles denote upper limits for sources not detected at 325 MHz. Right: spectral indices between 74 and 150 MHz against 150 MHz–1.4 GHz spectral indices. The filled symbols show the spectral indices using the catalogued VLSSr flux densities, while the open circles show the spectral indices if the flux density corrections reported by Lane et al. (2014) are applied. The grey triangles denote upper limits for sources not detected at 74 MHz. The diagonal dashed lines mark a power law across the full frequency range plotted.

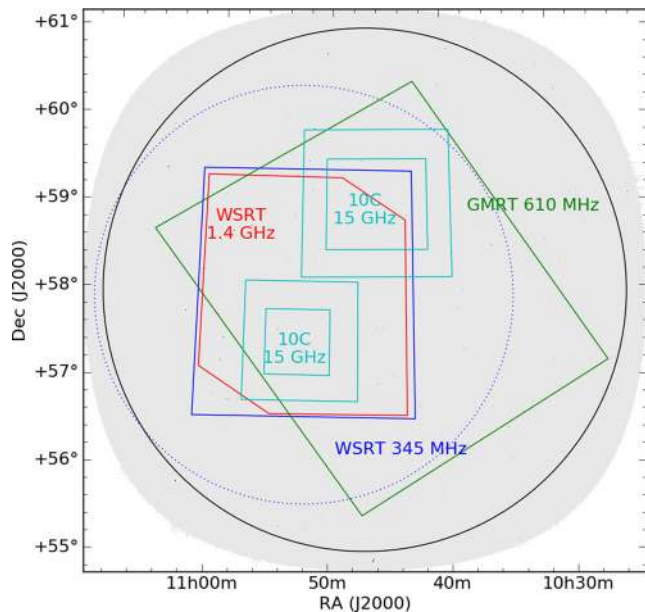


Figure 14. The footprints of each survey used in the spectral index analysis. The grey-scale shows the LOFAR HBA primary beam, and the black circle shows the area that was included in the source catalogue (i.e. up to 3 deg from the pointing centre). Footprints of other survey areas are labelled accordingly. The primary beam of the LOFAR LBA observations is not shown here, but it has the same pointing centre as the HBA data and, since it is at lower frequency, covers a larger area.

Lane et al. (2014) noted that the VLSSr fluxes were slightly underestimated compared to the predicted flux density extrapolated from the 6C and 8C catalogues. Predicting the 74 MHz flux densities from the 6C and 8C surveys, Lane et al. (2014) reported flux density ratios of VLSSr/predicted = 0.97 for sources with $S_{74} > 1$ Jy and VLSSr/predicted = 0.72 for sources fainter than 1 Jy. Applying these corrections to the 74 MHz flux densities results in steeper spectral indices as shown by the open circles in Fig. 13. Due to the uncertainties associated with the absolute flux scale at these frequencies, we show both the corrected (open symbols) and uncorrected (filled symbols) spectral indices. These large uncertainties make it difficult to ascertain if there is any intrinsic spectral flattening at these frequencies. This is discussed further in Section 4.4.2.

4.3 Cross-matching with deeper radio surveys in the Lockman Hole field

One of the limitations in carrying out this analysis using all-sky surveys such as VLSSr and NVSS is that these surveys do not reach sufficient depths for all the LOFAR sources to be detected at these frequencies. However, the advantage of observing well-studied fields such as the Lockman Hole is that there are extensive, deeper multi-band data available in these regions as discussed in Section 1. The survey area covered by each of these observations is shown in Fig. 14, and a summary of the different surveys used in this analysis is given in Table 3. Cross-matching with deeper high-frequency data allows us to exploit the depth of the LOFAR data and push this study of the low-frequency spectral properties to much fainter radio source populations.

To obtain a complete subset of sources that probe fainter flux densities, we first cross-match the full LOFAR 150-MHz catalogue with WSRT observations at 1.4 GHz. We then use this

catalogue to cross-match with other deep radio surveys of the Lockman Hole field. In this section, we briefly describe each of these surveys and how they were matched to their LOFAR counterparts.

4.3.1 Westerbork 1.4-GHz mosaic

A 16-pointing mosaic of the Lockman Hole field was observed at 1.4 GHz with the WSRT. This covers a 6.6 square degree field down to an rms noise level of 11 μ Jy at the centre of the field with a resolution of 11×9 arcsec. For more details of the Westerbork observations, we refer the reader to the accompanying paper (Prandoni et al. 2016a, in preparation).

These WSRT observations resulted in a catalogue of over 6000 sources which was then cross-matched with the 150-MHz LOFAR catalogue. To find the optimal search radius, a Monte Carlo test was again carried out. Comparing the number of real matches to random matches revealed that a search radius of 10 arcsec was the ideal cut-off to limit the number of spurious matches whilst also including the maximum number of real matches.

Although the majority of sources are catalogued as point sources in both the WSRT and LOFAR catalogues, simply finding the closest match is not as reliable for sources with complex morphology or sources which have been separated into multiple components. To ensure that objects were not being excluded due to the 10-arcsec search radius, and to check the reliability of the matches, we applied the following criteria to determine the best matched catalogue.

- (i) If there was a single WSRT match within 10 arcsec of the LOFAR source, this match was automatically accepted.
- (ii) If there were multiple WSRT matches within 10 arcsec of the LOFAR source, both matches were visually inspected to choose the best match by eye. This was particularly useful for the cases where the LOFAR sources had been catalogued as separate components, but were listed as a single source in the WSRT catalogue (note that these are flagged in the catalogue as discussed at the end of this section).
- (iii) For LOFAR sources which did not have a WSRT counterpart, the search radius was expanded to 15 arcsec. This was primarily needed for extended sources where the fitted peak position differed between the LOFAR and WSRT catalogues. All sources matched in this way were visually inspected to confirm that the match was likely to be real.
- (iv) Sources that were identified as extended in either the LOFAR or WSRT source catalogues were checked by eye to confirm that the correct counterparts were identified.

This resulted in a final sample of 1302 sources, which we refer to hereafter as the Lockman–WSRT sample. An additional flag was added to the catalogue referring to how the match was identified. The numbers in brackets refer to the number of sources which fall into each category.

- (i) V – This match was identified and/or confirmed by visual inspection (299 sources).
- (ii) A – This match was automatically accepted (974 sources).
- (iii) C – A complex match (16 sources). Likely to be a genuine match, but a mismatch between the two source catalogues. For example, a double-lobed radio galaxy may have been classified as a single source in the WSRT catalogue, but catalogued as two separate

components in the LOFAR catalogue. These sources are included in the catalogue,⁹ but have been excluded from further analysis.

(iv) L – A LOFAR source with no WSRT counterpart (six sources). These are discussed further in Section 5.2.1.

(v) LC – A LOFAR component with no WSRT counterpart (seven sources). Also discussed further in Section 5.2.1.

4.3.2 Lockman–WSRT catalogue format

The full Lockman–WSRT catalogue is included as supplementary material in the electronic version of the journal. A sample of the catalogue is shown in Table 4, and below we list the columns included in the published catalogue. Note that this catalogue only includes LOFAR sources in the area covered by the WSRT 1.4-GHz mosaic since virtually all of the LOFAR sources have a match in the WSRT catalogue. This reduces the risk of artefacts around bright sources in the larger LOFAR field being included. The catalogue of the full LOFAR field at higher resolution will be published in a future paper.

Column 1: LOFAR name.

Columns 2, 3: LOFAR 150-MHz source position (RA, Dec.).

Columns 4, 5: Integrated 150-MHz flux density and error.

Column 6: Local rms.

Column 7: Source flag (from PYBDSM - S/C/M).

Column 8: WSRT name.

Columns 9, 10: WSRT position (RA, Dec.).

Columns 11, 12: Integrated 1.4-GHz flux density and error.

Columns 13, 14: Peak 1.4-GHz flux density and error.

Columns 15–17: Deconvolved 1.4-GHz source size and orientation.

Column 18: Spectral index between 150 MHz and 1.4 GHz (α_{150}^{1400}).

Column 19: Identification flag (see Section 4.3.1).

We use this Lockman–WSRT catalogue for cross-matching with other frequency data sets discussed in Sections 4.3.3–4.3.6.

4.3.3 WSRT 90-cm observations

Deep 345-MHz observations of the same region imaged at 1.4 GHz were obtained with the WSRT in maxi-short configuration during winter 2012. The expected thermal noise in our 345-MHz image (uniform weighting) was ~ 0.11 mJy beam⁻¹. However, given the poor resolution of Westerbork at 90-cm band (~ 70 arcsec \times 44 arcsec in our case), confusion limited the effective noise to ~ 0.5 mJy beam⁻¹. These data are presented in further detail in an accompanying paper (Prandoni et al. 2016b, in preparation).

A catalogue of 234 sources was extracted from the inner ~ 7 square degrees of the image (extending to ~ 90 arcmin distance from the image centre), where the noise is lowest and flattest. About half of this inner region is characterized by noise values ≤ 0.8 mJy, assumed as a reference noise value for the source extraction. This catalogue was then cross-matched with the WENSS catalogue to verify the extracted flux densities at this frequency. A correction factor of 1.1 was applied to the WSRT 345-MHz sources to align with the WENSS flux density scale.

The region covered by the extracted catalogue at 345 MHz covers the same region as the deep WSRT 1.4-GHz catalogue. This is marked by the rectangular area in Fig. 14 while the primary beam

⁹ Sources were catalogued based on the LOFAR source extraction. For example, if a source was catalogued as two components in the LOFAR catalogue, then both these are listed and matched to the same WSRT source.

Table 4. First 10 lines of the Lockman–WSRT catalogue. The full catalogue is available in the online version of this paper.

LOFAR name	RA	Dec.	St ₁₅₀ (mJy)	err (mJy)	rms (mJy)	Flag	WSRT name	RA	Dec.	Sint _{1.4} (mJy)	err (mJy)	Spk _{1.4} (mJy)	err (mJy)	maj ^a (arcsec)	min (arcsec)	PA °	α_{150}^{1400}	ID flag
J104316+572452	10:43:16.3	+57:24:52.8	277.8	19.54	0.73	M	LHWJ104316+572453	10:43:16.11	+57:24:53.7	42.4	0.39	39.2	0.36	4.05	0.00	39.1	-0.8	V
J104321+583440	10:43:21.6	+58:34:40.3	19.8	1.44	0.22	S	LHWJ104321+583438	10:43:21.65	+58:34:38.3	5.7	0.21	5.5	0.20	0.00	0.00	0.0	-0.6	A
J104325+581854	10:43:25.6	+58:18:54.5	6.3	0.55	0.19	S	LHWJ104325+581852	10:43:25.49	+58:18:52.0	2.3	0.25	2.0	0.22	4.62	3.04	46.3	-0.4	A
J104328+575809	10:43:28.1	+57:58:09.1	23.1	1.66	0.21	S	LHWJ104328+575807.3	10:43:28.16	+57:58:07.3	13.4	0.23	12.8	0.22	2.71	1.51	-22.0	-0.2	A
J104336+574017	10:43:36.4	+57:40:17.9	5.2	0.50	0.21	S	LHWJ104336+574015.4	10:43:36.35	+57:40:15.4	1.3	0.19	1.1	0.16	0.00	0.00	0.0	-0.6	A
J104343+575513	10:43:43.0	+57:55:13.6	5.1	0.51	0.21	C	LHWJ104342+575509	10:43:42.93	+57:55:09.4	0.9	0.16	0.8	0.14	0.00	0.00	0.0	-0.8	V
J104344+574258	10:43:44.3	+57:42:58.5	1.8	0.37	0.20	S	LHWJ104344+574252	10:43:44.89	+57:42:52.5	0.8	0.13	0.7	0.13	0.00	0.00	0.0	-0.4	A
J104348+580427	10:43:48.1	+58:04:28.0	7.3	0.62	0.20	S	LHWJ104348+580412A	10:43:48.10	+58:04:25.8	9.5	0.13	8.8	0.12	3.41	1.76	12.8	0.1	V
J104351+565550	10:43:51.0	+56:55:50.3	6.5	0.77	0.36	S	LHWJ104350+565552	10:43:50.93	+56:55:52.8	2.1	0.37	2.2	0.39	0.00	0.00	0.0	-0.5	A
J104351+580338	10:43:51.2	+58:03:38.1	9.8	0.76	0.20	S	LHWJ104348+580412B	10:43:51.32	+58:03:35.7	3.4	0.12	3.3	0.12	0.00	0.00	0.0	-0.5	V

^aObjects listed with source sizes of 99.9 have been detected as two separate components in the WSRT mosaic, but combined together and catalogued as one object in post-processing. See Prandoni et al. (2016a, in preparation) for further details.

of the 345-MHz observations is shown by the dotted circle. An association radius of 25 arcsec was used resulting in 225 matches to the LOFAR–WSRT catalogue. Due to the large difference in resolution between the WSRT 345-MHz data and the LOFAR and WSRT 1.4-GHz data, sources with extreme spectral indices were visually inspected and flagged in the cases where this was a problem (typically associated with multiple LOFAR sources being matched to the same WSRT 345-MHz source). This process excluded 16 sources. Due to the varying rms of the image (in particular around bright sources), any sources not detected at 345 MHz were given upper limits of $5\times$ the local rms. For the majority of sources, this was approximately 4 mJy.

4.3.4 GMRT 610-MHz mosaic

A large mosaic of the Lockman Hole field was made from observations at 610 MHz with the GMRT from 2004–2006 covering a total area of 13 deg² (Garn et al. 2008, 2010). This mosaic covers the central region of the LOFAR primary beam and overlaps with the majority of the deep 1.4-GHz WSRT mosaic (excluding a small area in the south-eastern corner of the WSRT coverage) and reaches an rms of 60 μ Jy in the central regions at a resolution of 5×6 arcsec.

When cross-matching this catalogue with the LOFAR–WSRT catalogue, only point sources at 610 MHz were included due to the difference in resolution. On inspection of the spectral indices between 150 MHz, 610 MHz and 1.4 GHz, it was also discovered that GMRT sources fainter than 5 mJy tend to have underestimated flux density measurements so a flux density limit of $S_{610, pk} = 5$ mJy was applied for the cross-matching. The underestimation of fluxes for the fainter sources in this 610-MHz mosaic was also noted by Whittam et al. (2013). One possible explanation for this is that the mosaic was not CLEANED deeply enough; therefore, the fainter sources were not deconvolved sufficiently. We used a search radius of 10 arcsec which resulted in 121 matches at 610 MHz.

4.3.5 10C survey

The 10C survey was observed with the Arcminute Microkelvin Imager at 15.7 GHz. This survey covers 27 deg² at 30-arcsec resolution across 10 different fields, two of which are in the Lockman Hole region. These two fields cover 4.64 deg² down to an rms noise level of 0.05 mJy in the central regions of each field and 0.1 mJy in the outskirts. For more details on the observations and data reduction for the 10C survey, we refer the reader to Davies et al. (2011). When cross-matching with the LOFAR–WSRT catalogue, we used a search radius of 15 arcsec to match the analysis carried out by Whittam et al. (2013). There are 119 LOFAR sources detected in the 10C survey.

4.3.6 LBA LOFAR observations

The LBA observations, data reduction and source extraction are discussed in Section 2.6. Although the 60-MHz LOFAR data do not reach the fainter flux density limits of the surveys listed in the previous sections, the advantage of cross-matching with the Lockman–WSRT catalogue is that it limits the chance of including artefacts in the spectral analysis. For sources not detected in the LBA image, we place a 5σ upper limit on the 60-MHz flux density of 100 mJy. Using a matching radius of 20 arcsec, we find 46 matches in the LOFAR 60-MHz catalogue.

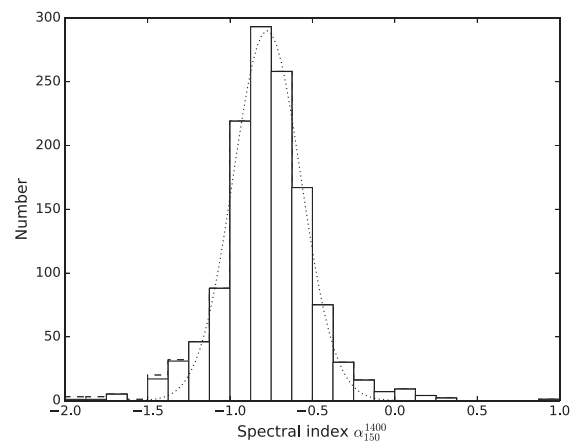


Figure 15. Histogram of spectral indices from 150 MHz–1.4 GHz for sources in the Lockman–WSRT sample (1302 sources). Upper limits of the spectral index are marked by the dashed line. The dotted line marks a Gaussian fit to the distribution, showing that a large number of the USS and flat-spectrum sources cannot be attributed to the tail of the distribution.

4.4 Multi-frequency spectral analysis of the LOFAR–WSRT and Lockman-deep samples

Using the multi-frequency information available in the Lockman Hole field, we can study the spectral properties of low-frequency radio sources in a similar manner as was done for the Lockman-wide sample. As much of the complementary data go to fainter flux density limits, albeit in a smaller area of sky, we can study a larger sample of radio sources to confirm if the trends found earlier are significant, and also investigate if the spectral behaviour of these radio sources changes at lower flux densities.

Due to the similar, or lower, resolution of most of the surveys, we were able to include all the LOFAR sources in this analysis. Again, all upper limits were confirmed by visual inspection, and in cases of a clear mismatch, these were excluded from the analysis.

4.4.1 Spectral analysis from 150 MHz to 1.4 GHz

We first investigate the spectral indices between 150 MHz and 1.4 GHz in the Lockman–WSRT catalogue. Due to the flux limit reached in the WSRT mosaic, any LOFAR sources not detected at 1.4 GHz have upper limits of $\alpha_{150}^{1400} < -1.2$. The distribution of the 150 MHz–1.4 GHz spectral index is shown in Fig. 15 with upper limits denoted by the dashed line. The median spectral index is $\alpha_{150}^{1400} = -0.78 \pm 0.015$ (errors from bootstrap) with an interquartile range of $[-0.95, -0.65]$, consistent with previous studies of 150-MHz selected radio sources (Intema et al. 2011; Williams et al. 2013, 2016; Hardcastle et al. 2016).

Separating the Lockman–WSRT sample into the three primary categories discussed earlier, we find that flat-spectrum sources ($\alpha_{150}^{1400} > -0.5$) represent 11.3 per cent of the sample, steep-spectrum sources ($\alpha_{150}^{1400} < -0.5$) make up 82.1 per cent and USS sources ($\alpha_{150}^{1400} < -1.2$) account for 6.6 per cent of the sample. The majority of these sources are genuinely ultra-steep, with only 2 per cent of sources with $\alpha_{150}^{1400} < -1.2$ expected in the tail of a Gaussian distribution (shown by the dotted line in Fig. 15).

These USS sources are discussed further in Section 5.2.1. The division of the Lockman–WSRT sample into these three categories is roughly the same as for the Lockman-wide sample, suggesting that the source populations probed at these frequencies do not significantly change by going deeper at 150 MHz.

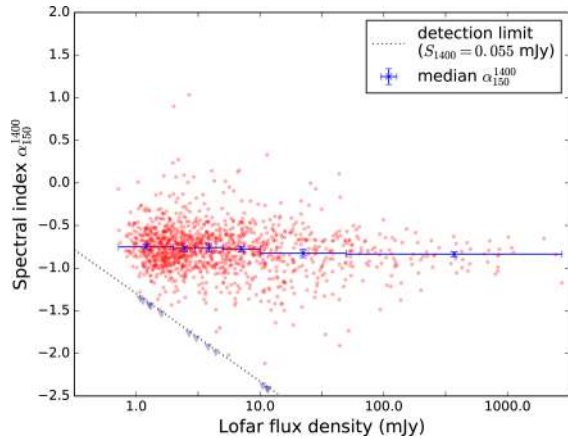


Figure 16. Median spectral index as a function of 150 MHz flux density for sources in the Lockman–WSRT sample. The small red points show the individual measurements for all sources in the sample, while the blue squares show the median spectral index in each bin (these are shown in Table 5). The horizontal error bars denote the bin widths and the vertical error bars represent the 95 per cent confidence interval of the median (from bootstrap). Blue triangles mark the upper limits of the spectral index for sources detected in the LOFAR catalogue that do not have a WSRT counterpart (see Section 5.2.1).

Other studies of spectral index properties of radio sources have reported a flattening of the spectral index as a function of flux density. For example, Prandoni et al. (2006) found that the spectral indices between 1.4 and 5 GHz became flatter with decreasing flux density down to ~ 0.5 mJy. On the other hand, Randall et al. (2012) did not see any evidence for a flattening of the spectral index with decreasing flux density between 843 MHz and 1.4 GHz. However, it is important to note a key difference in the selection of these samples; Prandoni et al. (2006) selected sources at 5 GHz which will be more dominated by flat-spectrum sources than the 843-MHz selected sample studied by Randall et al. (2012).

At lower frequencies, Intema et al. (2011) found that the median spectral index between 153 MHz and 1.4 GHz became flatter with decreasing flux density between 5 mJy and 2 Jy. This is in agreement with the studies of Ishwara-Chandra et al. (2010) and Williams et al. (2013), which both report a spectral flattening below approximately 20–50 mJy using spectral indices from 150 MHz to 610 MHz and 150 MHz to 1.4 GHz, respectively. However, the spectral index limits imposed by the flux density limits in these latter studies systematically bias against detecting steep-spectrum sources at the fainter end of the flux density distribution, as noted in Williams et al. (2013).

The Lockman–WSRT catalogue provides the ideal sample to conclusively determine whether there is any evidence for spectral flattening as a function of flux density, since virtually all LOFAR sources have a 1.4-GHz counterpart. We have divided the Lockman–WSRT sample into bins of flux density and plotted the median spectral index as shown in Fig. 16 and Table 5. The errors shown are the 95 per cent confidence interval determined by the bootstrap method. The median spectral indices become slightly flatter down to a flux density of 10 mJy, in agreement with Intema et al. (2011). Below these fluxes, the median spectral index stays roughly constant. This change in median spectral index also explains the higher median α_{150}^{1400} noted in the Lockman-wide sample which is flux density limited at $S_{150} = 40$ mJy.

It is also interesting to note that the integrated spectral index of the brighter sources (>50 mJy), where powerful AGN are likely to

Table 5. Median spectral indices shown in Fig. 16.

Flux density bins	Median α_{150}^{1400}	95 per cent CI
<2 mJy	−0.75	−0.79, −0.73
2–3 mJy	−0.77	−0.79, −0.72
3–5 mJy	−0.76	−0.81, −0.71
5–10 mJy	−0.77	−0.81, −0.75
10–50 mJy	−0.83	−0.87, −0.77
>50 mJy	−0.84	−0.86, −0.80

dominate, broadly agrees with that of bright radio galaxies in both large samples (e.g. Laing, Riley & Longair 1983, 178–750 MHz) and in detailed studies at very low frequencies (e.g. Harwood et al. 2016, 10–1400 MHz) and so is likely to be robust.

4.4.2 Spectral analysis of the Lockman-deep sample

To investigate any spectral curvature that may be occurring at lower flux densities, we form a complete sample with multi-band radio information from 60 MHz to 15 GHz. Although the majority of these radio surveys go to fainter flux density limits, we still define a flux-limited sample at 150 MHz in order to form a complete sample with which we can carry out a useful analysis of the low-frequency radio source population.

We set a 150-MHz flux density limit of $S_{150} = 9$ mJy primarily driven by the ~ 4 mJy flux limit of the 345-MHz WSRT observations. This means that any sources not detected at 345 MHz must have spectral indices steeper than $\alpha_{150}^{345} \sim -1.0$, analogous to the Lockman-wide sample. Using this flux threshold gives upper limits at other frequencies of $\alpha_{150}^{1400} < -1.25$ and $\alpha_{150}^{15000} < -0.6 / -0.75$ (depending on where the object falls in the 10C field).

The only frequency that does not have reliable limits is the GMRT 610-MHz data. Due to the higher resolution of this data set, and underestimated flux densities for faint sources, we have only included point sources above $S_{610} = 5$ mJy in this cross-matching. As such, any source without a match at 610 MHz could simply indicate that the source is extended at this frequency rather than below a certain flux density limit. We therefore include the 610-MHz information where available (i.e. when plotting spectra of individual sources), but cannot conclude anything significant about the source population at these frequencies. Fig. 17 shows radio colour–colour plots for sources in the Lockman-deep sample. On the left, we plot spectral indices between 150 MHz and 1.4 GHz against 1.4–15 GHz spectral indices and on the right spectral indices between 150 and 345 MHz against 345 MHz–1.4 GHz spectral indices. All sources that are undetected at either 15 GHz or 345 MHz are shown as limits indicated by the triangles. As with the Lockman-wide sample, the majority of sources exhibit a steep spectrum from the lowest to highest frequencies plotted, with a few sources showing evidence of curved spectra.

We also investigate the trend for sources to become slightly flatter at lower frequencies using the 60-MHz LOFAR LBA observations. Again, due to the high flux density cut-off at low frequencies, we define a subset of bright sources with the aim of forming a complete sample. Selecting sources with $S_{150} > 80$ mJy means that any sources not detected in the 60-MHz observations are flatter than $\alpha_{60}^{150} = -0.7$.

Fig. 18 shows the spectral index between 60 and 150 MHz against spectral indices between 150 and 1400 MHz. While many sources continue to exhibit a straight, power-law spectrum over this frequency range, an increasing number of sources fall to the right of this diagonal line. Since the 60-MHz flux densities have been scaled

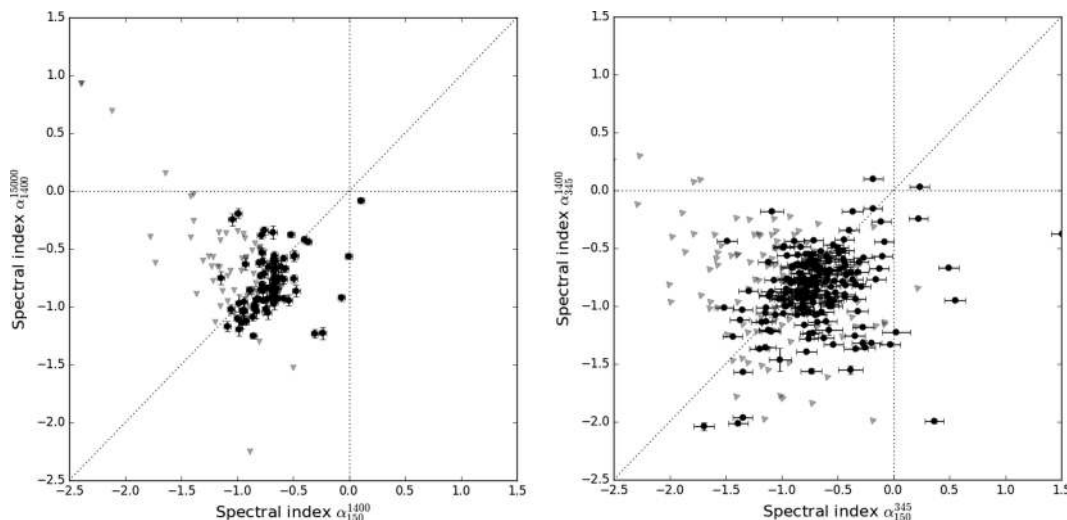


Figure 17. Radio colour–colour plots of sources in the Lockman-deep sample. The left-hand plot only shows sources that fall in the areas covered by the 10C survey. The grey triangles represent upper limits for sources undetected at 15 GHz on the left and 345 MHz in the right-hand plot.

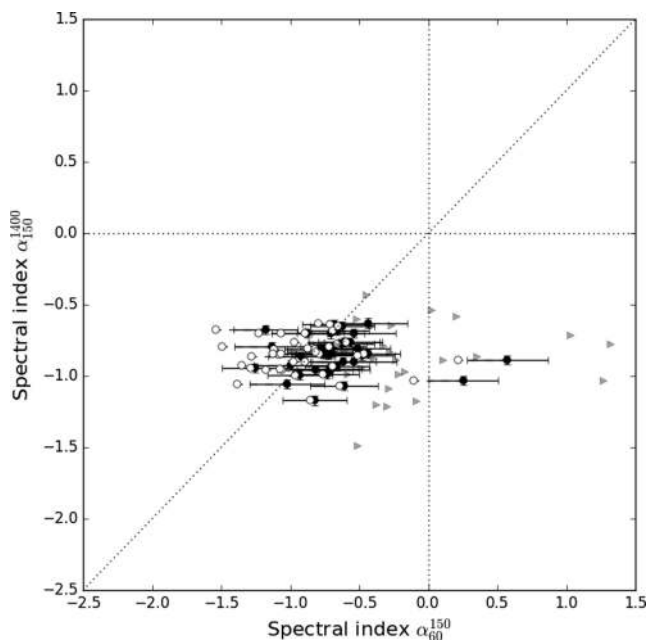


Figure 18. Radio colour–colour plots from 60 MHz to 1.4 GHz using LOFAR LBA observations. Only sources with $S_{150} > 80$ mJy are shown here to form a complete sample. The filled sources show the original LBA flux densities, and the open circles show the spectral indices if corrections are made to the LBA fluxes to bring them in line with predicted flux densities from the 6C and 8C surveys (see Section 4.2).

to the VLSSr flux densities, we also applied the corrections noted in Section 4.2. These are shown by the open symbols in Fig. 18.

The broader distribution of spectral indices between 60 and 150 MHz suggests that a number of sources begin to flatten at these frequencies, in agreement with previous low-frequency studies of the Böttes field (Williams et al. 2013; van Weeren et al. 2014). However, it is difficult to draw a conclusive result from these plots due to the uncertainties associated with the absolute flux calibration at these frequencies.

This is most clearly highlighted by the difference in spectral indices shown by the filled and open circles in Figs 13 and 18.

Even though they are tied to the same absolute flux scale (Scaife & Heald 2012), the VLSSr and LOFAR LBA catalogues appear to have underestimated flux densities compared to that predicted from the 6C and 8C surveys (see Section 4.2 and Lane et al. 2014). This flux density offset of 20–30 per cent can lead to differences in the spectral indices of up to $\Delta\alpha_{60}^{150} = 0.36$. In addition, it is important to keep in mind that the LOFAR LBA fluxes have been scaled to the VLSSr flux scale assuming a spectral index of $\alpha_{60}^{74} = -0.8$ which also adds to the uncertainty of the intrinsic spectral index of the source.

To confirm if this spectral flattening is real, a more thorough investigation is needed with careful consideration of the flux calibration issues associated with low-frequency radio observations. However, we note that spectral flattening at lower frequencies was also detected in the LOFAR Multifrequency Snapshot Sky Survey Verification Field (Heald et al. 2015). Here it was found that the spectral indices were slightly flatter when including the full bandwidth (30–158 MHz) compared to the spectral indices measured just using the HBA (119–158 MHz).

5 INTERESTING SOURCES IN THE LOCKMAN HOLE FIELD

The radio colour–colour plots also serve as useful tools for identifying sources with more atypical spectra. For example, sources that are located in the lower-right quadrant of the diagram are peaking within the frequency range plotted, in this case anywhere between 60 MHz and 15 GHz. Alternatively, sources with very steep spectra lie towards the lower-left corner of the plot. In this section, we discuss these two classes of sources in more detail and search for these objects in the Lockman Hole field.

5.1 Peaked-spectrum sources

Radio sources with peaked spectra at around 1 GHz are typically classified as gigahertz peaked-spectrum (GPS) sources, thought to be the youngest radio galaxies (Fanti et al. 1995; O’Dea 1998). The spectral peak marks the transition between the optically thin and optically thick emitting regimes and is generally associated with regions of dense nuclear material. As the radio source evolves,

increasing in linear size up to scales of ~ 10 kpc, the spectral peak shifts to lower frequencies with the source then classified as a compact steep-spectrum (CSS) source (O’Dea 1998; Snellen et al. 2000; de Vries et al. 2009). Studying these sources allows us to probe the intermediate stages of radio galaxy evolution, bridging the gap between the young, compact sources detected at high frequencies (generally GPS sources) and typical kpc-scale radio galaxies. Obtaining a complete census of CSS sources will provide insight into whether all GPS sources evolve into CSS sources and ultimately large radio galaxies, or whether this happens only under select conditions.

Sources with a spectral peak at low frequencies could also represent a population of high-redshift GPS sources, where the intrinsic high-frequency spectral peak of the source has been redshifted into the LOFAR band (Falcke, Körding & Nagar 2004; Coppejans et al. 2015). These sources could represent the first generation of radio-loud AGN, providing insight into the formation of the earliest supermassive black holes.

Observing GPS and CSS sources at low frequencies also allows us to investigate the cause of the spectral turnover. The generally favoured model is synchrotron self-absorption (Fanti et al. 1990; de Vries et al. 2009), but there is evidence for free-free absorption in some objects (see e.g. Bicknell, Dopita & O’Dea 1997; Callingham et al. 2015; Tingay et al. 2015).

We identify candidate peaked-spectrum sources by selecting sources that lie in the lower-right quadrant of the plots shown in Figs 13, 17 and 18 – i.e. a flat or rising spectral index at the lower frequencies ($\alpha_{\text{low}} > -0.2$) and a steep spectral index between the higher frequencies ($\alpha_{\text{high}} < 0.0$). The radio spectra of these sources were then inspected by eye to only include sources with a distinct spectral peak (primarily to exclude variable flat-spectrum sources that may appear peaked between certain frequencies due to the non-contemporaneous observations). In addition, detections at a minimum of four different frequencies (or at least a constraining upper limit) were required to classify a spectrum as peaked.

This selection reveals six candidate GPS or CSS sources in the Lockman-wide sample and seven in the Lockman-deep sample. These are shown in Fig. 19 and listed in Appendix A. While the low-frequency information is essential in identifying these objects as candidate GPS or CSS sources, ancillary data at other wavelengths are needed to determine the nature of these sources. In addition, repeating multi-frequency radio observations would confirm these sources as intrinsically peaked and limit the number of variable sources erroneously classified as peaked spectrum. A preliminary analysis of GPS and CSS sources in the Lockman Hole is also presented in Mahony et al. (2016).

5.1.1 Multi-wavelength properties of peaked-spectrum sources

Searching the literature for existing observations of these targets revealed a number of optical/IR counterparts. Two out of the six candidates found in the Lockman-wide sample have known counterparts, both detected in the Sloan Digital Sky Survey (SDSS; York et al. 2000): J104833+600845 is identified as a QSO at a redshift of $z = 1.72$ and J103559+583408 is a candidate QSO with a photometric redshift of $z_{\text{ph}} = 1.65$ (Richards et al. 2009).¹⁰

For sources in the Lockman-deep sample, a large fraction of the area has been observed by the *Spitzer* Extragalactic Representa-

tive Volume Survey (SERVS; Mauduit et al. 2012) or the *Spitzer* Wide-area Infrared Extragalactic Survey (SWIRE; Lonsdale et al. 2003) providing us with deep IR information in this area. This information has been collated in the SERVS data fusion catalogue (Vaccari et al. 2010; Vaccari 2015) which also includes IR information from the Two Micron All Sky Survey (Skrutskie et al. 2006) and the UKIRT Deep Sky Survey Deep eXtragalactic Survey (UKIDSS DXS; Lawrence et al. 2007) as well as optical information from SDSS. This data fusion catalogue was cross-matched with the WSRT 1.4-GHz mosaic to search for multi-wavelength counterparts (for full details, see Prandoni et al. 2016a, in preparation).

Of the candidate peaked-spectrum sources found in the Lockman-deep sample, only one is detected in SDSS: J105119+564018 is identified as a $z = 2.38$ QSO with $g = 20.2$ mag. Four sources are detected in the SERVS data fusion catalogue, three have K (Kron) magnitudes ranging from 16.5 to 19.9 mag and the fourth has an upper limit of $K \sim 21.0$. No additional redshift information is available, but were these galaxies to fall on the K - z relation (see e.g. Rocca-Volmerange et al. 2004) we can infer that of these, two are potentially high-redshift GPS sources at $z > 3$ (following the K - z relation given in Brookes et al. 2008).

Sources that are not detected are outside the SERVS and SWIRE footprints; hence, we cannot place useful limits on the IR properties of these sources. Further follow-up optical/IR observations are required to identify the host galaxies and determine the redshift. Another way to distinguish the high- z GPS sources from lower redshift CSS sources would be through high-resolution imaging with very long baseline interferometry. This would provide approximate ages of the radio source by placing limits on the linear size of these objects (see e.g. Coppejans et al. 2016).

5.2 USS sources

Another interesting class of sources detected in the Lockman Hole are the USS sources. As the name suggests, these sources exhibit an extremely steep spectrum, generally attributed to radiation losses of relativistic electrons in the radio lobes, meaning they are most luminous at lower radio frequencies. LOFAR is therefore an ideal instrument to detect these sources. Finding sources with ultra-steep spectra is thought to be a good way of identifying a variety of different source populations including high- z ($z > 2$) radio galaxies (HzRGs; Blumenthal & Miley 1979; Miley & De Breuck 2008), remnant emission from ageing radio galaxies (Slee et al. 2001; Murgia et al. 2011; Brienza et al. 2016), relic cluster emission (see e.g. Ferrari et al. 2008; Feretti et al. 2012) or radio haloes in clusters (Brunetti et al. 2008).

A number of different selection criteria are used to identify USS sources, ranging from $\alpha_{151}^{4850} < -0.981$ (Blundell et al. 1998) to $\alpha_{843}^{1400} < -1.3$ (De Breuck et al. 2004). To search for USS sources in the Lockman Hole, we selected sources that had spectral indices between 150 MHz and 1.4 GHz steeper than $\alpha_{150}^{1400} = -1.2$, primarily driven by the upper limit of the spectral index for sources not detected in NVSS. Using this criterion, we find 19 sources (4.9 per cent) with ultra-steep spectra in the Lockman-wide sample, including eight upper limits for sources that are not detected in NVSS. Like the peaked-spectrum sources, follow-up observations are needed to confirm these as either high- z sources, remnant AGN, or cluster emission. There is also the possibility that some of these steep-spectrum sources are galactic sources (e.g. pulsars). However, given the high galactic latitude of the Lockman Hole ($b > 50^\circ$), it is unlikely that these account for a significant fraction of the ultra-steep population found here.

¹⁰ For sources in the Lockman-wide sample, the optical counterparts were found using the NASA/IPAC Extragalactic Database where the radio-optical association was already made.

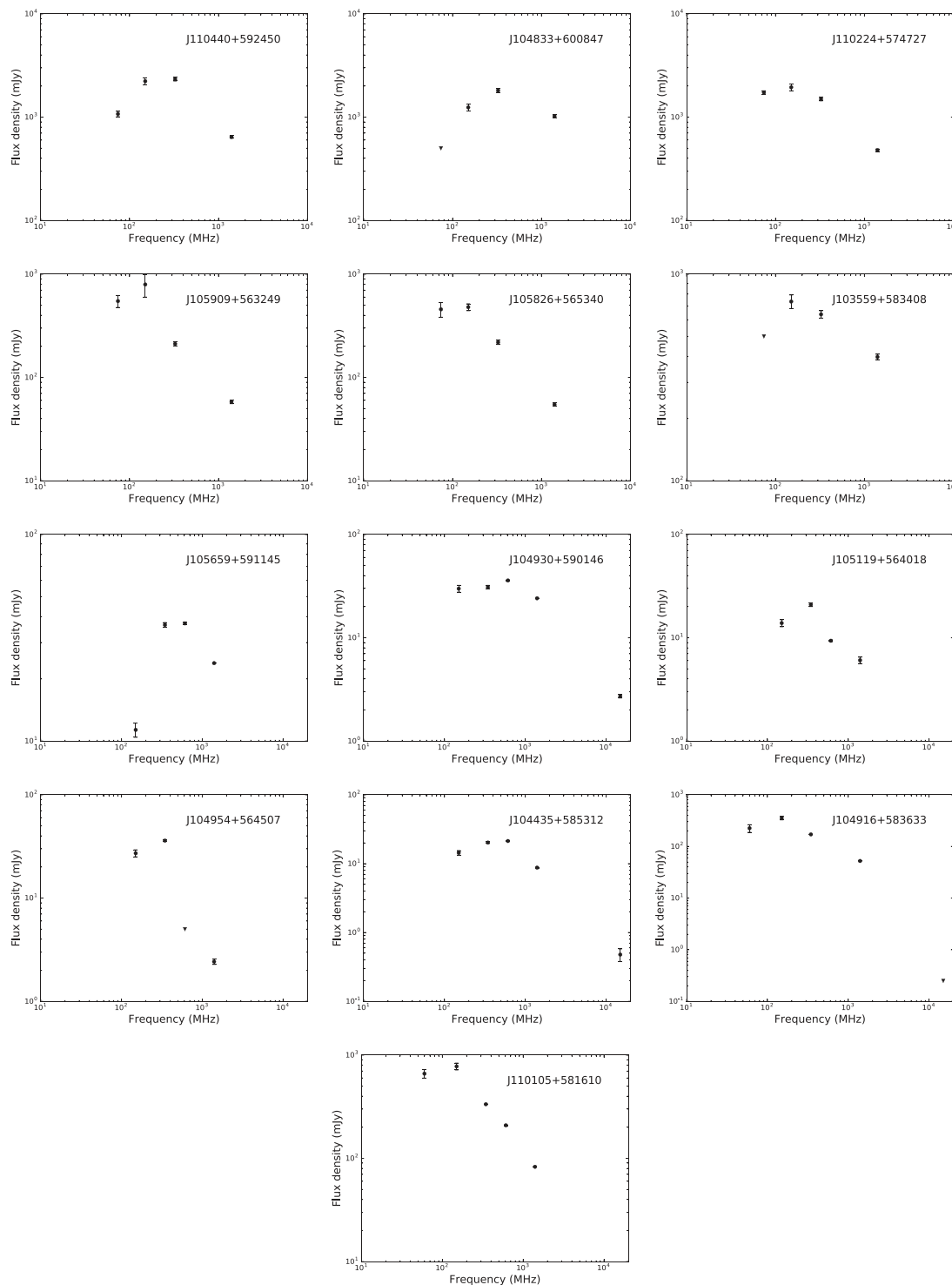


Figure 19. Peaked-spectrum sources detected in the Lockman Hole. The first six sources are detected in the Lockman-wide sample and the remaining in the Lockman-deep sample. Error bars are shown, but in many cases are smaller than the data points.

5.2.1 USS sources in the Lockman–WSRT sample

Since the WSRT 1.4 GHz catalogue is more than an order of magnitude deeper than the NVSS catalogue, we can carry out a much more comprehensive search for USS sources using the Lockman–WSRT catalogue. Of the 1302 sources in the Lockman–WSRT catalogue, we find 85 candidate USS sources with $\alpha_{150}^{1400} < -1.2$,

including 13 upper limits that were undetected in the WSRT 1.4 GHz image.¹¹ These undetected sources can be separated into two different categories: faint LOFAR sources with no detectable emission

¹¹ Four USS sources fall in both the Lockman-wide and Lockman-deep samples.

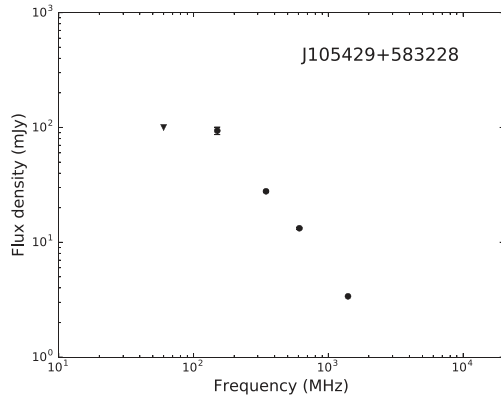


Figure 20. An example of one unusual USS source detected in the Lockman Hole. This source has an ultra-steep spectrum of $\alpha_{150}^{1400} = -1.6$ between 150 and 1.4 GHz, but is undetected at 60 MHz and therefore has a much flatter spectral index from 60–150 MHz of $\alpha_{60}^{150} > -0.07$ (assuming a 5σ upper limit at 60 MHz).

at 1.4 GHz – these are flagged as ‘L’ in the Lockman–WSRT catalogue, or larger, more complex radio sources where excess emission has been detected in the LOFAR image, possibly indicative of an older phase of AGN activity (e.g. remnant lobes). These sources could be candidate restarted radio galaxies, where the time-scales between the two sets of radio lobes can be used to probe the duty cycle of radio AGN activity; however, further follow-up observations are needed to confirm this. These have been flagged as ‘LC’ in the catalogue. Some examples are shown in Appendix B.

Including the upper limits derived from the undetected sources at 1.4 GHz, this corresponds to 6.6 per cent of the Lockman-deep sample being classified as ultra-steep. Previous searches for USS sources in the Lockman Hole field using deep 610 and 1.4 MHz have revealed a similar percentage of 6.3 per cent based on $\alpha_{610}^{1400} < -1.3$ (Ibar et al. 2009; Afonso et al. 2011).

5.2.2 Multi-wavelength properties of USS sources

To confirm if these LOFAR-selected USS candidates are HzRGs or potential relic sources, further follow-up observations at other wavelengths are required. A more complete analysis on the USS sources and the remnant AGN population in the Lockman Hole is discussed by Brienza et al. (2016) and will be further expanded in an upcoming paper (Brienza et al., in preparation).

To investigate how many of these sources are potential HzRGs, we cross-matched the USS sources with the SERVS data fusion catalogue (Vaccari et al. 2010; Vaccari 2015) using a search radius of 1.75 arcsec. Of the 85 USS sources detected in the Lockman-deep sample, 82 of them overlap with the SERVS footprint. Of these, 26 (32 per cent) are detected in SERVS and 19 sources are detected in the K band as part of the UKIDSS DXS survey with K (Kron) magnitudes ranging from 14.48 to 20.23 mag. While none of these have known redshift information, we can get a rough estimation of the redshift by placing them on the K – z relation. Based on these K -band magnitudes, and following the K – z relation given in Brookes et al. (2008), we estimate that eight (42 per cent) objects have $z > 3$ and four (21 per cent) are at $z > 4$. However, further spectroscopic follow-up would be required to confirm if these candidates are genuinely high- z objects.

The spectrum of one intriguing USS source detected in the Lockman Hole is shown in Fig. 20. This object has a flux density of 100 mJy in the LOFAR HBA image and exhibits an ultra-steep spec-

trum of $\alpha_{150}^{1400} = -1.6$ between 150 MHz and 1.4 GHz. However, the spectrum appears to turn over quite sharply below 150 MHz, with the source undetected in the 60 MHz LBA image. Using a conservative 5σ upper limit of 100 mJy at 60 MHz, we can place a lower limit of the spectral index between 60 and 150 MHz of $\alpha_{60}^{150} > -0.07$. The ultra-steep spectral index, combined with the IR properties of this source ($K = 19.9$ from UKIDSS DXS), indicates that this could be an HzRG ($z > 4$). Observations at higher spatial resolution could also indicate if this source is a high- z GPS or CSS source.

We also note the similarities between this source and one of the peaked-spectrum sources presented in Section 5.1. J104954+564507 also shows a very sharp spectral peak with a rising spectral index of $\alpha_{150}^{345} = 0.36$ before turning over to exhibit an ultra-steep spectrum of $\alpha_{345}^{1400} = -1.99$. This also has a K magnitude of 19.9 potentially placing it at a similar redshift. Another GPS source observed with the Murchison Widefield Array (Tingay et al. 2013) shows a similarly sharp turnover (Callingham et al. 2015), indicating that these could be part of a larger population of extreme peaked-spectrum sources.

5.3 Implications for larger LOFAR surveys

The LOFAR data presented here represent just a single night observation of one field, a tiny fraction of the large-area sky survey currently being carried out with LOFAR (see Shimwell et al. 2016, submitted). As such, we can use the results found here to predict what we might expect to detect if similar observations were carried out across the whole sky above $\delta = 0^\circ$. In the ~ 7 square degrees covered by these observations (the Lockman-deep survey area), we have identified 85 USS sources and 7 sources with peaked spectrum at MHz frequencies. Extrapolating from these numbers, we can therefore expect up to $\sim 300\,000$ and $\sim 20\,000$ USS and peaked-spectrum sources, respectively, assuming a survey carried out at the same depth and resolution presented here.¹²

However, these numbers assume that there are deep multi-frequency radio data available across large areas of sky, which is far from being the case. Limiting these numbers to just those sources that have been cross-matched with all-sky surveys such as NVSS, WENSS and VLSSr, these numbers decrease to $\sim 13\,000$ potential USS candidates and ~ 2000 sources with peaked spectra (above a flux limit of $S_{150} = 40$ mJy). None the less, this still represents an order-of-magnitude increase in the numbers of these source populations known, allowing for a better understanding of the evolution of these sources and how they relate to the general radio galaxy population.

This highlights the need for complementary deep radio surveys at higher frequencies such as the continuum surveys planned at 1.4 GHz with Apertif (APERture Tile in Focus – a focal plane array system installed on the WSRT; Oosterloo et al. 2009) and the 3-GHz VLA Sky Survey. This will enable us to push the spectral analysis presented here down to much deeper flux density limits and investigate how the source population changes in the sub-mJy regime. In addition to deeper multi-frequency radio data, ancillary data at other wavelengths would enable us to obtain a more comprehensive picture of the radio source population, providing more insight into the evolutionary stages of radio AGN.

¹² The LOFAR all-sky survey aims to reach an rms of 0.1 mJy with resolution of ~ 5 arcsec, slightly deeper and at higher resolution than presented here.

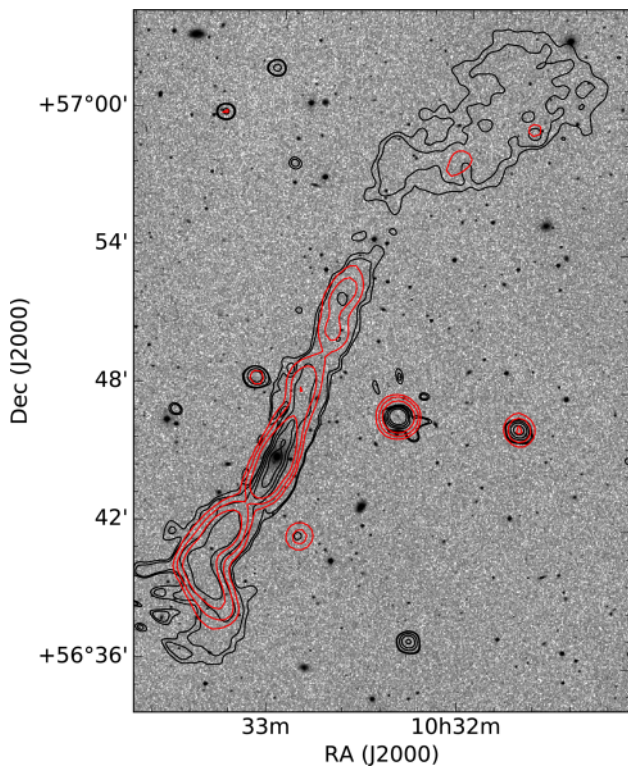


Figure 21. The giant radio galaxy HB13. The grey-scale image shows the optical image from DSS overlaid with NVSS 1.4-GHz contours in red (1, 2.5 and 5 mJy beam^{-1}) and LOFAR 150-MHz contours in black (0.75, 1, 2.5, 5 and 10 mJy beam^{-1}).

5.4 The giant radio galaxy: HB13

Rather than only selecting sources based on spectral information, we can also search for interesting sources based on morphology. One such example is HB13, a known giant radio galaxy, at the position $10^{\text{h}}32^{\text{m}}58^{\text{s}}.9 +56^{\text{d}}44^{\text{m}}53^{\text{s}}$, that was detected in early radio surveys but since then relatively neglected [but see tables with comparison to other giant radio galaxies discussed by Palma et al. (2000) and Saripalli et al. (1986)]. This object was studied by Masson (1979) at 151 MHz (using data from the 6C survey) but originally selected, and named HB13, in the pencil beam survey of Hanbury Brown & Hazard (1953). The radio galaxy is identified with a galaxy at redshift $z = 0.0450$. Masson (1979) presents observations at 151 MHz and 1.4 GHz, although with very poor spatial resolution, reporting a total size of the radio source at low frequencies of 35 arcmin.

Our image (see Fig. 21) shows radio emission extending about 30 arcmin, corresponding to about 1.6 Mpc (using the scale, $0.890 \text{ kpc arcsec}^{-1}$).¹³ In the inner 2.5 arcmin ($\sim 80 \text{ kpc}$), both sides of the radio jets appear to be relatively straight and symmetric while beyond that their structure seems to be less collimated and reminiscent of ‘plumes’. Large oscillations are also visible in the outer part of the jets.

As illustrated by Fig. 21, the detailed structure of HB13 is seen in much more detail with LOFAR than in NVSS. Due to the low surface brightness sensitivity of the array, and the fact that these sources

typically have steep spectrum, LOFAR is the ideal instrument to search for giant radio galaxies (see also Hardcastle et al. 2016).

6 CONCLUSIONS

We present 150-MHz LOFAR observations of the Lockman Hole field, allowing us to study the spectral index properties of low-frequency radio sources. The field was observed for 10 h using the HBA array covering the frequency range 110–172 MHz. The final 150 MHz image covers an area of 34.7 square degrees, has a resolution of $18.6 \times 14.7 \text{ arcsec}$ and reaches an rms of $160 \mu\text{Jy beam}^{-1}$ at the centre of the field. This results in a catalogue of 4882 sources within 3 deg from the pointing centre. From these data, we derive the 150-MHz source counts, which are in good agreement with other observations at 150 MHz (e.g. Williams et al. 2016) as well as with extrapolations from observations of the Lockman Hole at other frequencies (Prandoni et al. 2016a,b, in preparation).

By cross-matching this LOFAR 150-MHz catalogue with the NVSS, WENSS and VLSSr all-sky surveys, we form a sample with which to study the spectral index properties of low-frequency radio sources. Due to the different flux limits and resolutions of each of these surveys, we only include sources with deconvolved sizes less than 40 arcsec and with $S_{150} > 40 \text{ mJy}$. This results in a sample of 385 LOFAR sources which we term the Lockman-wide sample. As expected for low-frequency selected sources, the sample is dominated by steep-spectrum sources, with a median spectral index of $\alpha_{150}^{1400} = -0.82 \pm 0.02$ and an interquartile range of $[-0.94, -0.70]$.

Although we reach sub-mJy flux densities in the LOFAR 150-MHz observations, the spectral analysis is severely limited by the much higher flux limits of other surveys that cover the entire LOFAR field of view (i.e. NVSS, WENSS, VLSSr). To investigate the spectral index properties of mJy sources selected at 150 MHz, we cross-match the LOFAR catalogue with deeper 1.4 GHz observations from WSRT (Prandoni et al. 2016a, in preparation). This deep WSRT mosaic covers 7 square degrees with resolution $11 \times 9 \text{ arcsec}$ and reaches an rms of $11 \mu\text{Jy}$. This results in a sample of 1302 matched sources which we refer to as the Lockman–WSRT catalogue.

Investigating the spectral index properties of this larger sample, again we find that the sample is dominated by steep-spectrum sources (82.1 per cent), with 11.3 per cent classified as flat-spectrum and 6.6 per cent classified as USS. The median spectral index of this much larger sample is $\alpha_{150}^{1400} = -0.78 \pm 0.015$ with an interquartile range of $[-0.95, -0.65]$. The median spectral indices become slightly flatter with decreasing flux density, increasing from $\alpha_{150}^{1400} = -0.84$ for sources above 50 mJy to $\alpha_{150}^{1400} = -0.76$ at 5–10 mJy. At fainter flux densities, the median spectral index stays relatively constant.

Cross-matching this Lockman–WSRT catalogue with other deep, multi-frequency radio surveys available in the Lockman Hole, we form the Lockman-deep sample with which to study the spectral properties of low-frequency radio sources above a flux density threshold of $S_{150} = 9 \text{ mJy}$. This again shows that the majority of sources exhibit straight, power-law spectra over the full frequency range from 150 MHz to 15 GHz. Preliminary 60-MHz LOFAR observations of the Lockman Hole field shows tentative evidence that a large fraction of sources begin to flatten between 60 and 150 MHz, but a more comprehensive analysis of the absolute flux calibration is needed to confirm this result.

Using this wide-frequency coverage, we also search for sources with more extreme spectral properties such as USS sources and

¹³ Assuming a cosmology with $H_0 = 69.6 \text{ km s}^{-1}$, $\Omega_0 = 0.29$ and $\Omega_\Lambda = 0.71$.

peaked-spectrum sources. We identify a total of 100 USS sources and 13 candidate peaked-spectrum sources in the Lockman Hole. Using the $K-z$ relation, we estimate that approximately 42 per cent of these could be at $z > 3$ and up to 21 per cent at $z > 4$ indicating that these could be candidate high- z galaxies. However, further follow-up is required to confirm the physical properties of these objects.

The depth reached in these observations closely matches that expected for the ‘Tier-1’ all-sky LOFAR survey at 150 MHz. As such, the results obtained here provide insight into what we can expect to detect in the completed all-sky survey. However, this study also highlights the need for complementary, sensitive data sets across a wide range in frequency to maximize the scientific return of low-frequency radio surveys.

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SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article:

Table 4. First 10 lines of the Lockman–WSRT catalogue.

(<http://www.mnras.oxfordjournals.org/lookup/suppl/doi:10.1093/mnras/stw2225/-/DC1>).

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APPENDIX A: CANDIDATE PEAKED-SPECTRUM SOURCES

Table of candidate peaked-spectrum sources detected in the Lockman Hole.

Table A1. Catalogue of candidate GPS/CSS sources from both Lockman-deep and Lockman-wide samples. Flux densities are listed in mJy. The last three sources listed fall below the $S_{150} = 9$ mJy flux density threshold used to define the Lockman-deep sample so are not included in the analysis presented in this paper. We list them here for future reference.

Source ID	RA (h m s)	Dec. (d m s)	S_{60} (mJy)	S_{150} (mJy)	S_{345} (mJy)	S_{610} (mJy)	S_{1400} (mJy)	S_{15000} (mJy)	Counterpart
J110440+592450	11 04 40.1	59 24 51	1074.0±65 ^a	2230.3 ± 172	2335.0 ± 94 ^b	–	644.2 ± 19	–	
J110224+574727	11 02 24.0	57 47 27	1732.0±66 ^a	1946.3 ± 149	1500.0 ± 60 ^b	–	478.0 ± 14	–	
J105909+563249	10 59 09.0	56 32 49	549.0±73 ^a	795.2 ± 196	212.0 ± 10 ^b	–	58.0 ± 2	–	
J105826+565340	10 58 26.6	56 53 40	457.0±74 ^a	479.9 ± 36	219.0 ± 10 ^b	–	54.7 ± 2	–	
J104833+600847	10 48 33.8	60 08 47	<500.0 ^a	1242.5 ± 95	1813.0 ± 73 ^b	–	1021.8 ± 31	–	$z = 1.72$ QSO ^c
J103559+583408	10 35 59.4	58 34 08	<500.0 ^a	737.3 ± 56	639.0 ± 26 ^b	–	397.7 ± 12	–	$z_{\text{ph}} = 1.65$ QSO ^d
J105659+591145	10 56 59.9	59 11 45	–	11.4 ± 0.9	40.1 ± 0.03	37.1±0.5	23.9 ± 0.002	–	
J105119+564018	10 51 19.6	56 40 19	–	14.6 ± 1.1	23.0 ± 0.04	9.4±0.17	6.1 ± 0.07	–	$K = 17.6$ mag, $z = 2.378$ QSO ^c
J104954+564507	10 49 54.6	56 45 07	–	29.2 ± 2.1	39.6 ± 0.01	–	2.4 ± 0.06	–	$K = 19.9$ mag
J104435+585312	10 44 35.7	58 53 12	–	14.8 ± 1.1	22.3 ± 0.02	21.3±0.25	8.8 ± 0.01	0.48±0.06	$K > 21.0$ mag
J110105+581610	11 01 05.4	58 16 10	661.3±146	835.7 ± 59	367.9 ± 3	209.0±2	83.0 ± 3	–	
J104930+590146	10 49 30.4	59 01 47	<100	28.2 ± 2.0	34.0 ± 0.04	35.9±0.38	24.1 ± 0.001	2.7±0.17	
J104917+583633	10 49 17.0	58 36 33	225.4±58.7	381.0 ± 26.9	188.2 ± 0.004	–	52.3 ± 0.0003	<0.25	$K = 19.5$ mag
J105131+584950	10 51 31.4	58 49 50	–	2.0 ± 0.44	<4.0	17.4 ± 0.21	14.9 ± 0.001	0.78 ± 0.11	$K > 21.0$ mag
J105556+591654	10 55 55.9	59 16 54	–	4.1 ± 0.57	8.1 ± 0.11	7.6 ± 0.24	5.6 ± 0.02	–	
J105226+575508	10 52 25.5	57 55 08	–	2.7 ± 0.48	<4.0	12.3 ± 0.18	27.0 ± 0.0004	22.5 ± 1.3	$K = 19.1$ mag

^a74-MHz flux density from VLSSr.

^b325-MHz flux density from WENSS.

^cRedshift from SDSS (York et al. 2000).

^dRedshift from Richards et al. (2009).

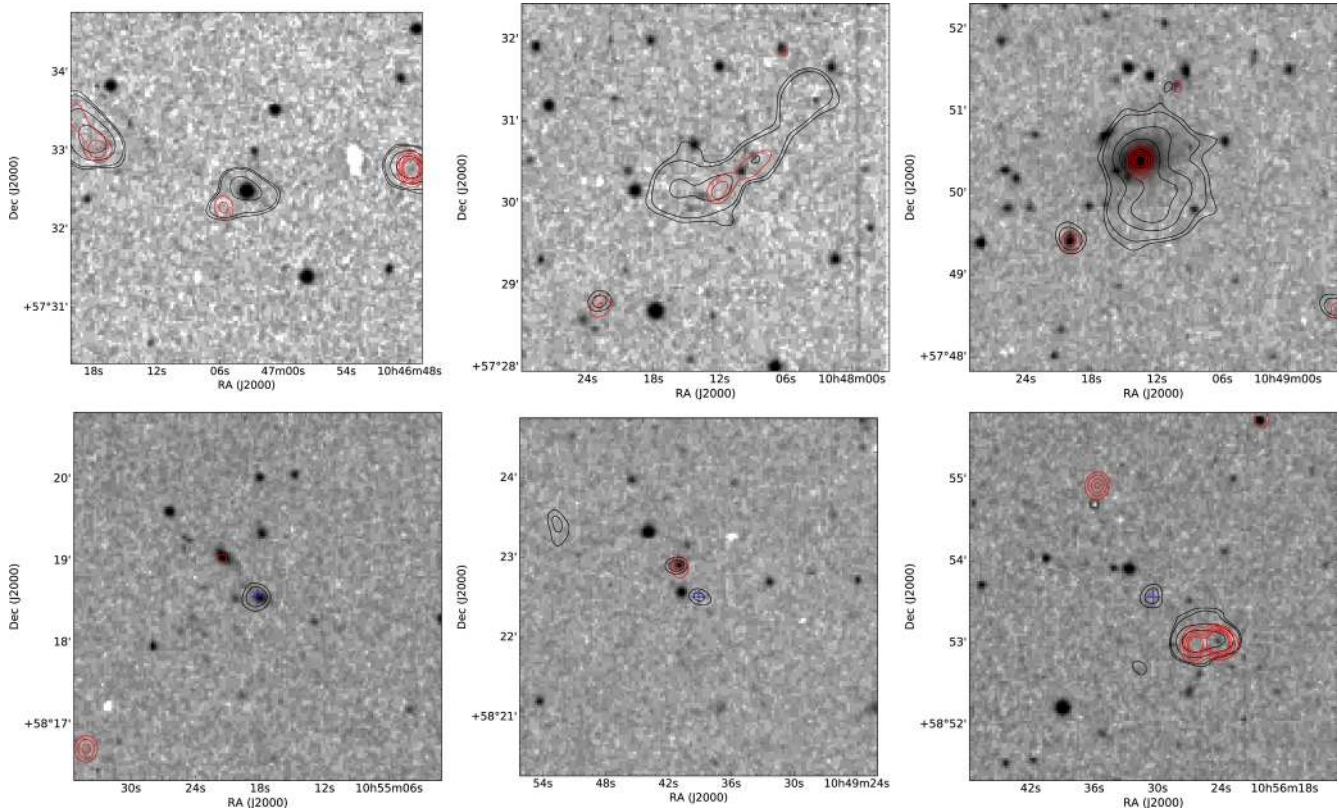


Figure B1. LOFAR sources showing excess low-frequency emission not detected in the WSRT 1.4-GHz image. The flux limits of each survey mean that these sources must have spectral indices steeper than $\alpha_{1500}^{1400} < -1.2$. The grey-scale shows an optical image from DSS, the WSRT contours are shown in red at levels of 0.1, 0.25, 0.5, 0.75, 1.0 and 5.0 mJy beam⁻¹ and the LOFAR contours are shown in black (0.75, 1.0, 2.5, 5.0 and 10.0 mJy beam⁻¹). The bottom row shows sources shown that were completely undetected in the WSRT image (i.e. flag ‘L’ in the Lockman–WSRT catalogue, the LOFAR positions are marked by the blue cross), and the top row shows objects where the LOFAR image detects additional components/emission that are not detected at 1.4 GHz (flag ‘LC’).

APPENDIX B: LOFAR SOURCES WITH EXCESS EMISSION AT 150 MHZ

Postage stamp images of some example LOFAR sources (including components) that do not have counterparts in the deep 1.4-GHz WSRT mosaic. This implies that the spectral index is steeper than $\alpha_{150}^{1400} = -1.2$.

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