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# The Neo-Fisher Effect: Econometric Evidence from Empirical and Optimizing Models\*

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#### **Abstract**

In this paper I investigate whether the neo-Fisher effect, according to which a permanent monetary tightening leads to an increase in inflation in the short run, is present in U.S. data. I estimate an empirical and a New-Keynesian model driven by transitory and permanent monetary and real shocks. I find that both models produce similar dynamics. Temporary increases in the nominal interest-rate lead, in accordance with conventional wisdom, to a temporary increase in real rates that is contractionary and deflationary. The main result of the paper is that in response to a permanent increase in the nominal interest rate, inflation increases immediately, reaching its higher long-run level within a year. Furthermore, the adjustment entails no output loss and is characterized by low real interest rates. In both models permanent monetary shocks are an important driver of nominal variables, explaining more than 40 percent of the variance of changes in inflation.

JEL Classification: E52,E58.

**Keywords:** Monetary Policy, Neo-Fisher Effect, Inflation, Monetary Policy, SVAR Models, New-Keynesian Models.

New-Neymesian Models.

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## 1 Introduction

According to the neo-Fisher effect, a monetary tightening that is expected to be permanent leads to an increase in inflation in the short run. In this paper, I investigate whether the neo-Fisher effect is present in U.S. data. To this end, I estimate an empirical and an optimizing New-Keynesian model, both driven by transitory and permanent monetary and real shocks. I estimate both models on postwar quarterly data using Bayesian techniques.

I find that both estimated models produce similar dynamics. In accordance with conventional wisdom, they predict that a transitory increase in the nominal interest rate causes a fall in inflation and a contraction in real activity. These effects take place in the context of elevated real interest rates. The main result of the paper is that in response to a permanent increase in the nominal interest rate, inflation increases immediately, reaching its higher long-run level within a year. Furthermore, the adjustment to a permanent increase in the nominal interest rate entails no output loss and is characterized by low real interest rates. In both the empirical and optimizing models permanent monetary shocks are estimated to be the main drivers of inflation, explaining 45 percent of the variance of changes in inflation. By contrast, transitory monetary shocks are estimated to play a modest role in explaining nominal and real variables.

These results have policy, theoretical, and econometric implications. With regard to policy, the results suggest that in countries suffering from below-target inflation and near-zero nominal rates, a credible normalization of nominal rates can achieve reflation swiftly and without a recession. In regard to how the findings inform monetary theory, the fact that the empirical and optimizing models have similar dynamic properties together with the fact that the empirical model is mute about how expectations are formed while the optimizing model assumes rational expectations provides discipline to theories of the transmission of monetary shocks that deviate from the assumption of model-consistent expectations. Finally, with regard to the econometric implications, the results of this paper suggest that distinguishing temporary and permanent monetary disturbances provides a resolution of the well-known

price puzzle, according to which a transitory increase in the nominal interest rate is estimated to cause a short-run increase in inflation.

This paper is related to a number of theoretical and empirical contributions on the effects of interest-rate policy on inflation and aggregate activity. De Michelis and Iacoviello (2016) estimate an SVAR model with permanent monetary shocks to evaluate the Japanese experience with Abenomics. They also study the effect of monetary shocks in the context of a calibrated New Keynesian model. The present paper departs from their work in two important dimensions. First, their SVAR model does not include the short-run policy rate. The inclusion of this variable is key in the present paper, because the short-run comovement of the policy rate with inflation is at the core of the neo-Fisher effect. Second, their theoretical model is not estimated and does not include permanent monetary shocks. By contrast, I allow permanent and transitory monetary shocks to compete in the econometric estimation and, as pointed out above, I find that permanent monetary shocks are the main driver of nominal variables, while the estimated transitory monetary shock plays a small role. King and Watson (2012) find that in estimated New-Keynesian models postwar U.S. inflation is explained mostly by variations in markups. In this paper, I show that once one allows for permanent monetary shocks, almost half of the variance of inflation changes is explained by monetary disturbances. Sims and Zha (2006) estimate a regime-switching model for U.S. monetary policy and find that during the postwar period there were three policy regime switches, but that they were too small to explain the observed increase in inflation of the 1970s or the later disinflation that started with the Volker chairmanship. The empirical and optimizing models estimated in the present paper attribute much of the movements in inflation in these two episodes to the permanent nominal shock. Cogley and Sargent (2005) use an autoregressive framework to produce estimates of long-run inflationary expectations. The predictions of both models estimated in the present paper are consistent with their estimates. This paper is also related to a body of work that incorporates inflation target shocks in the New-Keynesian model. In this regard, the contribution of the present paper is to

allow for a permanent component in this source of inflation dynamics. For example, Ireland (2007) estimates a new-Keynesian model with a time-varying inflation target and shows that, possibly as a consequence of the Fed's attempt to accommodate supply-side shocks, the inflaiton target increased significantly during the 1960s and 1970s and fell sharply in the early 2000s. Using a similar framework as Ireland's, Milani (2009) shows that movements in the inflation target become less pronounced if one assumes that agents must learn about the level of the inflation target.

This paper is also related to recent theoretical developments on the neo-Fisher Effect. Schmitt-Grohé and Uribe (2014 and 2017) show that the neo-Fisher effect obtains in the context of standard dynamic optimizing models with flexible or rigid prices, respectively. Specifically, they show that a credible permanent increase in the nominal interest rate gives rise to an immediate increase in inflationary expectations. Cochrane (2017) shows that if the monetary policy regime is passive, an increase in the nominal interest rate causes an increase in the short-run rate of inflation. Erceg and Levin (2003) study a calibrated dynamic general equilibrium model with nominal rigidity in which private agents have imperfect information about the permanent and transitory components of monetary-policy shocks. They show that imperfect information of this type can provide an adequate explanation of the observed inflation persistence during disinflation episodes.

The remainder of the paper is presented in 6 sections. Section 2 presents evidence consistent with the long-run validity of the Fisher effect. Section 3 presents the proposed empirical model and discusses the econometric estimation. The predictions of the empirical model are presented in section 4. Section 5 presents the New-Keynesian model and discusses its econometric estimation. Section 6 presents the predictions of the estimated New-Keynesian model in regard to the neo-Fisher effect. Section 7 closes the paper with a discussion of actual monetary policy in the ongoing low-inflation era from the perspective of the two estimated models.

#### 2 Preliminaries: Evidence on the Fisher Effect

What is the effect of an increase in the nominal interest rate on inflation and output? One can argue on theoretical grounds that the answer to this question depends on (a) whether the increase in the interest rate is expected to be permanent or transitory; and (b) whether the horizon of interest is the short run or the long run. Table 1 summarizes the answer according to conventional wisdom.

Table 1: Effect of an Increase in the Nominal Interest Rate on Inflation

	Long	Short
	Run	Run
	Effect	Effect
Transitory shock	0	$\downarrow$
Permanent shock	1	↑?

Note. Entry  $(2,\overline{1})$ : The Fisher effect. Entry (2,2): The Neo-Fisher effect.

A transitory positive disturbance in the nominal interest rate causes a transitory increase in the real interest rate, which in turn depresses aggregate demand and inflation, entry (1,2) in the table (see, for example, Christiano, Eichenbaum, and Evans, 2005, figure 1). A property of virtually all modern models studied in monetary economics is that a transitory increase in the nominal interest rate has no effect on inflation in the long ru, entry (1,1). By contrast, if the increase in the nominal interest rate is permanent, sooner or later, inflation will have to increase by roughly the same magnitude, since the real interest rate, given by the difference between the nominal rate and expected inflation, is not determined by nominal factors in the long run, entry (2,1) in the table. This one-to-one long-run relationship between nominal rates and inflation is known as the Fisher effect. The neo-Fisher effect says that a permanent increase in the nominal interest rate causes an increase in inflation not only in the long run but also in the short run, entry (2,2) in the table. Ascertaining whether the neo-Fisher effect is present in U.S. data is the focus of the present investigation.

Before plunging into an econometric analysis of the neo-Fisher effect, I wish to briefly

present evidence consistent with the Fisher effect. The rationale for doing so is that my empirical analysis of the neo-Fisher effect assumes the empirical validity of the Fisher effect, interpreted as a description of the long-run relationship between the nominal interest rate and inflation. The Fisher equation takes the form

$$i_t = R_t + E_t \pi_{t+1}$$

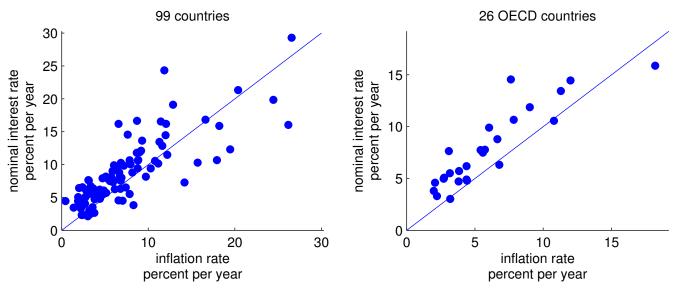
where  $i_t$  denotes the nominal interest rate,  $R_t$  denotes the real interest rate,  $\pi_t$  denotes the inflation rate, and  $E_t$  denotes expectations conditional on information available in period t. This expression says that the nominal interest rate incorporates two types of compensation to lenders. One is a compensation for the loss of purchasing power of money due to expected inflation during the investment period, and the other is a real empensation for postponing consumption. Assuming that on average expected inflation equals actual inflation, we have that

$$i = R + \pi$$
,

where variables without a subscript refer to long-run averages. Further assuming that the average real interest rate is determined solely by non-monetary factors (such as technology, demographics, distortionary taxes, or economic openness), the above expression delivers a one-to-one long-run relationship between the nominal interest rate and the rate of inflation.

The left panel of figure 1 displays times averages of inflation and nominal interest rates across 99 countries. Each dot in the graph corresponds to one country. The typical sample covers the period 1989 to 2012. The scatter plot is consistent with the Fisher effect in the sense that increases in the nominal interest rate are roughly associated with one-for-one increases in the rate of inflation. This is also the case for the subsample of OECD countries (right panel), which are on average half as inflationary as the group of non-member countries. Figure 2 presents empirical evidence consistent with the Fisher effect from the time perspective. It plots inflation and the nominal interest rate in the United States over

Figure 1: Average Inflation and Nominal Interest Rates: Cross-Country Evidence



Notes. Each dot represents one country. For each country, averages are taken over the longest available noninterrupted sample. The average sample covers the period 1989 to 2012. The solid line is the 45-degree line. Source: World Development Indicators (data.worldbank.org/indicator). Inflation is the CPI inflation rate (code FP.CPI.TOTL.ZG). The nominal interest rate is the t-bill rate, computed as the difference between the lending interest rate (code FR.INR.LEND) and the risk premium on lending (lending rate minus treasury bill rate, code FR.INR.RISK). Countries for which one or more of these series were missing as well as outliers, defined as countries with average inflation or interest rate above 50 percent, were dropped from the sample.

United States

United States

inflation
nominal interest rate

14

12

10

4

2

1960
1970
1980
1990
2000
2010

Figure 2: Inflation and the Nominal Interest Rate in the United States

Notes. Quarterly frequency. Source: See section 3.3.

the period 1954:Q4 to 2018:Q2. In spite of the fact that the data have a quarterly frequency, it is possible to discern a positive long-run association between inflation and the nominal rate. This relation becomes even more apparent if one removes the cyclical component of both series as in Nicolini (2017). The high-inflations of the 1970s and 1980s coincided with high levels of the interest rate. Symmetrically, the relatively low rates of inflation observed since the early 1990s have been accompanied by low nominal rates.

The Fisher effect, however, does not provide a prediction of when inflation should be expected to catch up with a permanent increase in the nominal interest rate. It only states that it must eventually do so. A natural question, therefore, is how quickly does inflation adjust to a permanent increase in the nominal interest rate? The remainder of this paper is devoted to addressing this question.

# 3 The Empirical Model

The empirical model aims to capture the dynamics of three macroeconomic indicators, namely, the logarithm of real output per capita, denoted  $y_t$ , the inflation rate, denoted  $\pi_t$  and expressed in percent per year, and the nominal interest rate, denoted  $i_t$  and also expressed in percent per year. I assume that  $y_t$ ,  $\pi_t$ , and  $i_t$  are driven by four exogenous shocks: a nonstationary (or permanent) monetary shock, denoted  $X_t^m$ , a stationary (or transitory) monetary shock, denoted  $z_t^m$ , a nonstationary nonmonetary shock, denoted  $X_t^n$ , and a stationary nonmonetary shock, denoted  $z_t^n$ . The focus of my analysis is the short-run effects of permanent and transitory interest-rate shocks, embodied in the exogenous variables  $X_t^m$  and  $z_t^m$ . The shocks  $X_t^n$  and  $z_t^n$  are meant to capture the nonstationary and stationary components of combinations of nonmonetary disturbances of different natures, such as technology shocks, preference shocks, or markup shocks, which my analysis is not intended to individually identify.

I assume that output is cointegrated with  $X_t^n$  and that inflation and the nominal interest rate are both cointegrated with  $X_t^m$ . I can then define the following vector containing stationary variables

$$\begin{bmatrix} \widehat{y}_t \\ \widehat{\pi}_t \\ \widehat{i}_t \end{bmatrix} \equiv \begin{bmatrix} y_t - X_t^n \\ \pi_t - X_t^m \\ i_t - X_t^m \end{bmatrix}.$$

The variable  $\hat{y}_t$  can be interpreted as detrended output, and  $\hat{\pi}_t$  and  $\hat{i}_t$  as the cyclical components of inflation and the nominal interest rate, respectively. Because inflation and the nominal interest rate share a common nonstationary component, they are cointegrated. In other words, the Fisher effect holds, in the sense that shocks that cause a permanent change in the nominal interest rate also cause the same permanent change in the inflation rate. But the assumption that  $\pi_t$  and  $i_t$  are cointegrated says nothing about the neo-Fisher effect, that is, about the short-run effect on inflation and output of a permanent monetary shock.

I assume that the law of motion of the vector  $\left[ \widehat{y}_t \ \widehat{\pi}_t \ \widehat{i}_t \right]$  takes the autoregressive form<sup>1</sup>

$$\begin{bmatrix} \widehat{y}_t \\ \widehat{\pi}_t \\ \widehat{i}_t \end{bmatrix} = \sum_{i=1}^{L} B_i \begin{bmatrix} \widehat{y}_{t-i} \\ \widehat{\pi}_{t-i} \\ \widehat{i}_{t-i} \end{bmatrix} + C \begin{bmatrix} \Delta X_t^m \\ z_t^m \\ \Delta X_t^n \\ z_t^n \end{bmatrix}$$
(1)

where  $\Delta X_t^m \equiv X_t^m - X_{t-1}^m$  and  $\Delta X_t^n \equiv X_t^n - X_{t-1}^n$ . denote changes in the nonstationary shocks. The objects  $B_i$ , for i = 1, ..., L, are 3-by-3 matrices of coefficients, C is a 3-by-4 matrix of coefficients, and L is a scalar denoting the lag length of the SVAR system.

I assume that the driving forces follow univariate AR(1) laws of motion of the form

$$\begin{bmatrix} \Delta X_{t+1}^m \\ z_{t+1}^m \\ \Delta X_{t+1}^n \\ z_{t+1}^n \end{bmatrix} = \rho \begin{bmatrix} \Delta X_t^m \\ z_t^m \\ \Delta X_t^n \\ z_t^n \end{bmatrix} + \psi \begin{bmatrix} \epsilon_{t+1}^1 \\ \epsilon_{t+1}^2 \\ \epsilon_{t+1}^3 \\ \epsilon_{t+1}^3 \\ \epsilon_{t+1}^4 \end{bmatrix}$$
(2)

where  $\rho$  and  $\psi$  are 4-by-4 diagonal matrices of coefficients, and  $\epsilon_t^i$  are i.i.d. disturbances distributed N(0,1).

#### 3.1 Identification Restrictions

Thus far, I have introduced three identification assumptions, namely, that output is cointegrated with  $X_t^n$  and that inflation and the interest rate are cointegrated with  $X_t^m$ . In addition, to identify the transitory monetary shock, I adopt a methodology pioneered by Uhlig (2005) and impose sign restrictions on the impact effect of these disturbances on endogenous variables. Specifically, I assume that

$$C_{12} \le 0$$
 and  $C_{22} \le 0$ ,

<sup>&</sup>lt;sup>1</sup>The presentation of the model omits intercepts. A detailed exposition is in the appendix.

where  $C_{ij}$  denotes the (i, j) element of C. These two conditions restrict transitory exogenous increases in the interest rate to have nonpositive impact effects on output and inflation. Finally, without loss of generality, I introduce the normalizations  $C_{32} = C_{14} = 1$ .

#### 3.2 Observables, Priors, and Estimation Method

All variables in the system (16)-(17) are unobservable. To estimate the parameters of the matrices defining this system, I use observable variables for which the model has precise predictions. Specifically, I use observations of output growth, the change in the nominal interest rate, and the interest-rate-inflation differential, defined as

$$r_t \equiv i_t - \pi_t$$
.

These three variables are stationary by the maintained long-run identification assumptions. The following equations link the observables to variables included in the unobservable system (16)-(17):

$$\Delta y_t = \widehat{y}_t - \widehat{y}_{t-1} + \Delta X_t^n$$

$$r_t = \widehat{i}_t - \widehat{\pi}_t$$

$$\Delta i_t = \widehat{i}_t - \widehat{i}_{t-1} + \Delta X_t^m$$
(3)

I assume that  $\Delta y_t$ ,  $r_t$ , and  $\Delta i_t$  are observed with measurement error. Formally, letting  $o_t$  be the vector of variables observed in quarter t, I assume that

$$o_t = \begin{bmatrix} \Delta y_t \\ r_t \\ \Delta i_t \end{bmatrix} + \mu_t \tag{4}$$

where  $\mu_t$  is a 3-by-1 vector of measurement errors distributed i.i.d.  $N(\emptyset, R)$ , and R is a diagonal variance-covariance matrix.

To compute the likelihood function, it is convenient to use the state-space representation of the model. Define the vector of endogenous variables  $\hat{Y}_t \equiv [\hat{y}_t \ \hat{\pi}_t \ \hat{i}_t]'$  and the vector of driving forces  $u_t \equiv [\Delta X_t^m \ z_t^m \ \Delta X_t^n \ z_t^n]'$  The state of the system is given by

$$\xi_t \equiv \begin{vmatrix} \widehat{Y}_t \\ \widehat{Y}_{t-1} \\ \vdots \\ \widehat{Y}_{t-L+1} \\ u_t \end{vmatrix}.$$

Then the system composed of equations (16), (17), (18), and (19) can be written as follows:

$$\xi_{t+1} = F\xi_t + P\epsilon_{t+1}$$

$$o_t = H'\xi_t + \mu_t,$$

where the matrices F, P, and H are known functions of  $B_i$ , i = 1, ..., L, C,  $\rho$ , and  $\psi$  and are presented in the appendix. This representation allows for the use of the Kalman filter to evaluate the likelihood function, which facilitates estimation.

I estimate the model on quarterly data using Bayesian techniques. I include 4 lags in equation (16) (L=4), which is a lag length commonly adopted in the related literature (e.g., Christiano, Eichenbaum, and Evans, 2005). Table 2 displays the prior distributions of the estimated coefficients. The prior distributions of all elements of  $B_i$ , for  $i=1,\ldots,L$ , are assumed to be normal. In the spirit of the Minnesota prior (MP), I assume a prior parameterization in which at the mean of the prior parameter distribution the elements of  $\hat{Y}_t$  follow univariate autoregressive processes. So when evaluated at their prior mean, only the main diagonal of  $B_1$  takes nonzero values and all other elements of  $B_i$  for  $i=1,\ldots,L$ 

Table 2: Prior Distributions

Parameter	Distribution	Mean.	Std. Dev.
Main diagonal elements of $B_1$	Normal	0.95	0.5
All other elements of $B_i$ , $i = 1,, L$	Normal	0	0.25
$C_{21}, C_{31}$	Normal	-1	1
$-C_{12}, -C_{22}$	Gamma	1	1
All other estimated elements of $C$	Normal	0	1
$\psi_{ii}, i = 1, 2, 3, 4$	Gamma	1	1
$\rho_{ii}, i = 1, 2, 3$	Beta	0.3	0.2
$ ho_{44}$	Beta	0.7	0.2
$R_{ii}$	Uniform $\left[0, \frac{\operatorname{var}(o_t)}{10}\right]$	$\frac{\text{var}(o_t)}{10 \times 2}$	$\frac{\operatorname{Var}(o_t)}{10 \times \sqrt{12}}$

are nil. Because the system (16)-(17) is cast in terms of stationary variables, I deviate from the random-walk assumption of the MP and instead impose an autoregressive coefficient of 0.95 in all equations, so that all elements along the main diagonal of  $B_1$  take a prior mean of 0.95. I assign a prior standard deviation of 0.5 to the diagonal elements of  $B_1$ , which implies a coefficient of variation close to one half (0.5/0.95). As in the MP, I impose lower prior standard deviations on all other elements of the matrices  $B_i$  for i = 1, ..., L, and set them to 0.25.

The coefficient  $C_{21}$  takes a normal prior distribution with mean -1 and standard deviation 1. The value assigned to the mean of this distribution implies a prior belief that the impact effect of a permanent interest rate shock on inflation, given by  $1 + C_{21}$ , can be positive or negative with equal probability. I make the same assumption about the impact effect of permanent monetary shocks on the nominal interest rate itself, therefore assign to  $C_{31}$  a normal prior distribution with mean -1 and standard deviation 1. All other unrestricted parameters of the matrix C are assigned a normal prior distribution with mean 0 and standard deviation 1.<sup>2</sup> The remaining 2 estimated elements of C are, as explained above, subject to inequality

<sup>&</sup>lt;sup>2</sup>One might wonder whether a rationale like the one I used to set the prior mean of  $C_{21}$  could apply to  $C_{13}$ , the parameter governing the impact output effect of a nonstationary nonmonetary shock,  $X_t^n$ , which is given by  $1 + C_{13}$ . To see why a prior mean of 0 for  $C_{13}$  might be more reasonable, consider the effect of an innovation in the permanent component of TFP, which is perhaps the most common example of a nonstationary nonmonetary shock in business-cycle analysis. Specifically, consider a model with the Cobb-

restrictions. Specifically,  $-C_{12}$  and  $-C_{22}$  are restricted to be nonnegative. I assume that these objects have Gamma prior distributions with mean and standard deviations equal to one. Thus, identification of the transitory monetary shock is achieved via restrictions of prior distributions.

The parameters  $\psi_{ii}$ , for i = 1, ..., 4, representing the standard deviations of the four exogenous innovations in the AR(1) process (17) are all assigned Gamma prior distributions with mean and standard deviation equal to one. I impose nonnegative serial correlations on the four exogenous shocks  $(\rho_{ii} \in (0,1))$  for  $i=1,\ldots,4$ , and adopt Beta prior distributions for these parameters. I assume relatively small means of 0.3 for the prior serial correlations of the two monetary shocks and the nonmonetary nonstationary shock and a relatively high mean of 0.7 for the stationary nonmonetary shock. The small prior mean serial correlations for the monetary shocks reflect the usual assumption in the related literature of serially uncorrelated monetary shocks. The relatively small prior mean serial correlation for the nonstationary nonmonetary shock reflects the fact that the growth rate of the stochastic trend of output is typically estimated to have a small serial correlation. Similarly, the relatively high prior mean of the serial correlation of the stationary nonmonetary shock reflects the fact that typically these shocks (e.g., the stationary component of TFP) are estimated to be persistent. The prior distributions of all serial correlations are assumed to have a standard deviation of 0.2. The variances of all measurement errors are assumed to have a uniform prior distribution with lower bound 0 and upper bound of 10 percent of the sample variance of the corresponding observable indicator.

Finally, to draw from the posterior distribution of the estimated parameters, I apply the

Douglas production function  $y_t = X_t^n + z_t^n + \alpha k_t + (1 - \alpha)h_t$  expressed in logarithms. Consider first a situation in which capital and labor, denoted  $k_t$  and  $h_t$ , do not respond contemporaneously to changes in  $X_t^n$ . In this case, the contemporaneous effect of a unit increase in  $X_t^n$  on output is unity, which implies that a prior mean of 1 for  $1 + C_{13}$ , or equivalently a prior mean of 0 for  $C_{13}$  is the most appropriate. Now consider the impact effect of changes in  $X_t^n$  on  $k_t$  and  $k_t$ . It is reasonable to assume that the stock of capital,  $k_t$ , is fixed in the short run. The response of  $k_t$  depends on substitution and wealth effects. The former tends to cause an increase in employment, and the latter a reduction. Which effect will prevail is not clear, giving credence to a prior of 0 for  $k_t$  one could further think about the role of variable input utilization. An increase in  $k_t$  is likely to cause an increase in utilization, favoring a prior mean of 0 over one of -1 for  $k_t$  for  $k_t$  is likely to cause an increase in utilization, favoring a prior mean of 0 over one of -1 for  $k_t$  for  $k_t$  is likely to cause an increase in utilization, favoring a prior mean of 0 over one of -1 for  $k_t$  for  $k_t$  is likely to cause an increase in utilization, favoring a prior mean of 0 over one of -1 for  $k_t$  for  $k_t$  is likely to cause an increase in utilization, favoring a prior mean of 0 over one of -1 for  $k_t$  for  $k_t$  is likely to cause an increase in utilization.

Metropolis-Hastings sampler to construct a Monte-Carlo Markov chain of one million draws after burning the initial 100 thousand draws. Posterior means and error bands around the impulse responses shown in later sections are constructed from a random subsample of the MCMC chain of length 100 thousand with replacement.

#### 3.3 Data and Unit Root Tests

I estimate the SVAR model on quarterly U.S. data spanning the period 1954:Q3 to 2018:Q2. The proxy for  $y_t$  is the logarithm of real GDP seasonally adjusted in chained dollars of 2012 minus the logarithm of the civilian noninstitutional population 16 years old or older. The proxy for  $\pi_t$  is the growth rate of the implicit GDP deflator expressed in percent per year. In turn, the implicit GDP deflator is constructed as the ratio of GDP in current dollars and real GDP both seasonally adjusted. The proxy for  $i_t$  is the monthly Federal Funds Effective rate converted to quarterly frequency by averaging and expressed in percent per year. The source for nominal and real GDP is the Bureau of Economic Analysis (bea.gov), the source for population is the Bureau of Labor Statistics (bls.gov) and the source for the Federal Funds rate is the Board of Governors of the Federal Reserve System (federalreserve.gov). All series were downloaded in August 2018.

Before plunging into the predictions of the SVAR model, I briefly report standard unitroot tests based on univariate representations of the data. The augmented Dickey-Fuller (ADF) test, which is a commonly used test of the null hypothesis of a unit root, fails to reject the null hypothesis for  $y_t$ ,  $i_t$ , and  $\pi_t$ , and rejects it for  $i_t - \pi_t$  at standard confidence levels of 10 percent or less.<sup>3</sup> These results are in line with the assumption that the interest rate, inflation, and output, all possess unit roots, and that the interest-inflation differential is stationary.

<sup>&</sup>lt;sup>3</sup>Specifically, for a random variable  $x_t$ , the ADF test considers the null hypothesis that  $x_t = x_{t-1} + \eta_0 + \sum_{i=1}^{I} \eta_i \Delta x_{t-i} + \epsilon_t$ , where  $\epsilon_t$  is white noise, against the alternative hypothesis that  $x_t = \delta x_{t-1} + \gamma t + \eta_0 + \sum_{i=1}^{I} \eta_i \Delta x_{t-i} + \epsilon_t$ , with  $\delta < 1$ . For  $i_t$  and  $\pi_t$ , I restrict  $\gamma$  to be zero (no time trend), and for  $i_t - \pi_t$ , I restrict  $\gamma$  and  $\eta_0$  to be zero (no time trend or drift). I include 4 lags of  $\Delta x_t$  (I = 4). The p values for  $x_t = y_t, i_t, \pi_t, i_t - \pi_t$  are, respectively, 0.604, 0.131, 0.135, and 0.0351.

# 4 The Neo-Fisher Effect in the Empirical Model

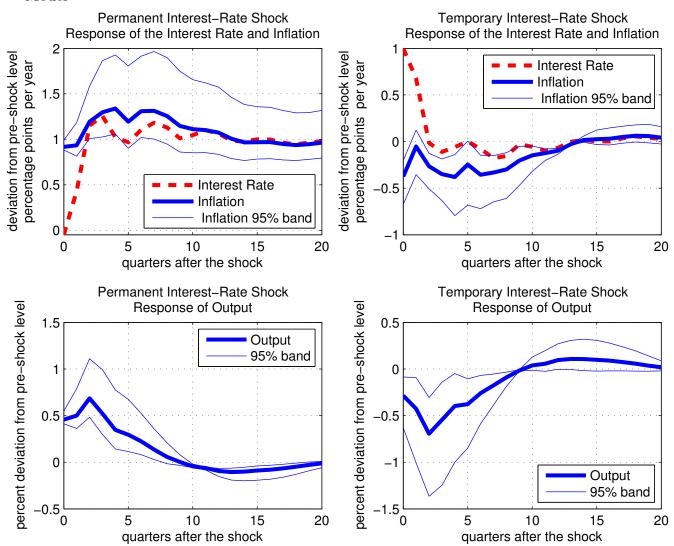
Figure 3 displays mean posterior estimates of the responses of inflation, output, and the nominal interest rate to permanent (left panels) and temporary (right panels) interest-rate shocks, along with asymmetric 95-percent error bands constructed using the method proposed by Sims and Zha (1999). The size of the permanent interest-rate shock is set to ensure that on average it leads to a 1 percent increase in the nominal interest rate in the long run, where the average is taken over the posterior distribution of impulse responses. Because inflation is cointegrated with the nominal interest rate, it also is expected to increase by 1 percent in the long run. The main result conveyed by figure 3 is that the adjustment of inflation to its higher long-run level takes place in the short run. In fact, inflation increases by 1 percent on impact and remains around that level thereafter.

On the real side of the economy, the permanent increase in the nominal interest rate does not cause a contraction in aggregate activity. Indeed, output exhibits a transitory expansion. This effect could be the consequence of low real interest rates resulting from the swift reflation of the economy following the permanent interest-rate shock. The left panel of figure 4 displays with a solid line the response of the real interest rate, defined as  $i_t - E_t \pi_{t+1}$ , to a permanent interest-rate shock. Because of the faster response of inflation relative to that of the nominal interest rate, the real interest rate falls by almost 1 percent on impact and converges to its steady-state level from below, implying that the entire adjustment to a permanent interest-rate shock takes place in the context of low real interest rates.

The responses of nominal and real variables to a transitory interest-rate shock, shown in the right panels of figure 3 are quite conventional. Both inflation and output fall below trend and remain low for a number of quarters. The real interest rate, whose impulse response is shown with a broken line in figure 4, increases on impact and remains above its long-run value during the transition, which is in line with the contractionary effect of the transitory increase in the interest rate.

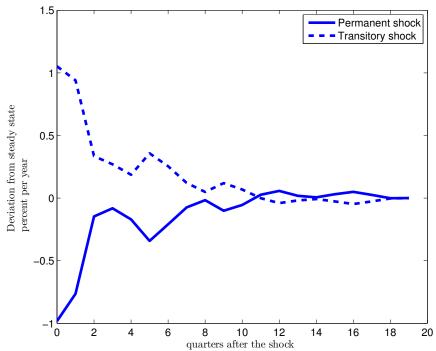
Interestingly, the model does not suffer from the price puzzle, which plagues empiri-

Figure 3: Impulse Responses to Permanent and Temporary Interest-Rate Shocks: Empirical Model



Notes. Impulse responses are posterior mean estimates. Asymmetric error bands are computed using the Sims-Zha (1999) method.

Figure 4: Response of the Real Interest Rate to Permanent and Transitory Interest-Rate Shocks: SVAR Model



Notes. Posterior mean estimates. The real interest rate is defined as  $i_t - E_t \pi_{t+1}$ .

cal models with only stationary monetary shocks, pointing to the importance of explicitly distinguishing between temporary and permanent shocks.

What does the permanent component of U.S. inflation look like according to the estimated empirical model? Figure 5 displays the actual rate of inflation along with its permanent component, given by the nonstationary monetary shock,  $X_t^m$ , over the sample period, 1954:Q4 to 2018: Q2. The path of  $X_t^m$  resembles the estimate of long-run inflation expectations reported in Cogley and Sargent (2005). The figure reveals a number of features of the predicted low-frequency drivers of postwar inflation in the United States. First, inflationary factors began to build up much earlier than the oil crisis of the early 1970s. Indeed, the period 1963 to 1972, corresponding to the last seven years in office of Fed Chairman William M. Martin and the first three years of Chairman Arthur F. Burns, were characterized by a continuous increase in the permanent component of inflation, with an accumulated increase of about 3 percentage points. Second, the high inflation rates associated with the oil crisis

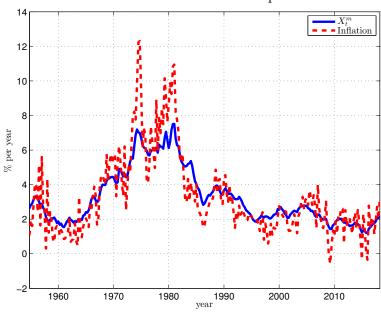


Figure 5: Inflation and Its Permanent Component: SVAR Model

Note. Quarterly frequency. The inferred path of the permanent component of inflation,  $X_t^m$ , was computed by Kalman smoothing and evaluating the SVAR model at the posterior mean of the estimated parameter vector. The initial value of  $X_t^m$  was normalized to make the average value of  $X_t^m$  equal to the average rate of inflation over the sample period, 1954:Q4 to 2018:Q2.

of the mid 1970s was not entirely due to nonmonetary shocks. The Fed itself contributed by maintaining  $X_t^m$  at the high level it had reached prior to the crisis. Third, the empirical model says that the Volker disinflation was driven to a large extent by the permanent component of monetary policy. This is suggested by the fact that after peaking around 1980, the permanent component of inflation fell sharply until the end of that decade. Finally, figure 5 shows that the normalization of rates that began in 2015 and put an end to seven years of near-zero nominal rates triggered by the global financial crisis, is interpreted by the SVAR model as having a significant permanent component.

How important are nonstationary monetary shocks? The relevance of the neo-Fisher effect depends not only on whether it can be identified in actual data, which has been the focus of this section thus far, but also on whether permanent monetary shocks play a significant role in explaining short-run movements in the inflation rate. If nonstationary monetary shocks played a marginal role in explaining cyclical movements in nominal variables, the

Table 3: Variance Decomposition: SVAR Model

	$\Delta y_t$	$\Delta \pi_t$	$\Delta i_t$
Permanent Monetary Shock, $\Delta X_t^m$	9.1	44.6	21.9
Transitory Monetary Shock, $z_t^m$	2.1	6.2	10.9
Permanent Non-Monetary Shock, $\Delta X_t^n$	49.8	27.9	13.5
Transitory Non-Monetary Shock, $z_t^n$	39.1	21.4	53.7

Note. Posterior means. The variables  $\Delta y_t$ ,  $\Delta \pi_t$ , and  $\Delta i_t$  denote output growth, the change in inflation, and the change in the nominal interest rate, respectively.

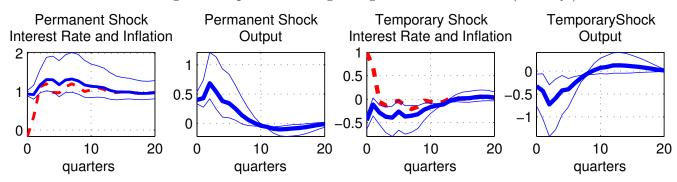
Fisher effect would just be an interesting curiosity. To shed light on this question, table 3 displays the variance decomposition of the three variables of interest, output growth, the change in inflation, and the change in the nominal interest rate, predicted by the estimated SVAR model. The table shows that the nonstationary monetary shock, explains 45 percent of the change in inflation, 22 percent of changes in the nominal interest rate, and 9 percent of the growth rate of output. Thus, the SVAR model assigns a significant role to this type of monetary disturbance, especially in explaining movements in nominal variables. In comparison, the stationary monetary shock explains a relatively small fraction of movements in the three macroeconomic indicators included in the model. These results suggest that the neo-Fisher effect emanates from a relevant driver of nominal variables. More generally, in light of the fact that the majority of studies in Monetary Economics limits attention to the study of stationary nominal shocks, the results reported in table 3 call for devoting more attention to understanding the effects of nonstationary monetary disturbances.

#### 4.1 Robustness

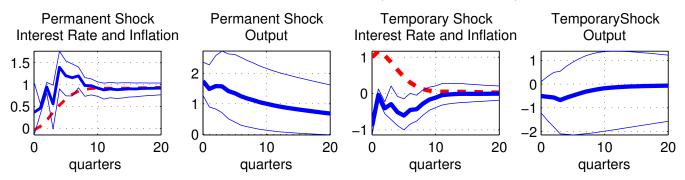
Between 2009 and 2015, the Federal Funds rate was technically nil, and interest-rate policy was said to have hit the zero lower bound (ZLB). Theoretically, the zero lower bound on nominal rates introduces nonlinearities in the equilibrium dynamics. The empirical model I study is linear, which may be problematic for capturing the effects of monetary policy, in a world in which occasionally the monetary authority's actions are constrained by the

Figure 6: Robustness Checks: Empirical Model

Truncating the Sample at the Beginning of the ZLB Period (2008:Q4)



Estimation on Japanese Data (1955.Q3 to 2016.75)



Notes. Thick lines are posterior means. Thick broken lines correspond to the nominal interest rate. Thin lines are 95% asymmetric error bands computed using the Sims-Zha (1999) method.

nonnegativity restriction on its policy instrument. Formulating and estimating a nonlinear model is beyond the scope of this paper. As an imperfect alternative, I estimate the linear model truncating the sample in 2008:Q4. The results are shown in the top panels of figure 6. The impulse responses are qualitatively similar to those obtained with the longer sample.

As a second robustness check, I estimate the model on Japanese data from 1955.Q3 to 2016.Q4. I rely on the results of the previous robustness check in deciding not to truncate the zero-rate period that started in 1995. There are two additional benefits of keeping the period 1995-2016. First, this period might provide valuable information on the effect of permanent monetary shocks, as it involves more than two decades of highly stable rates. Second, excluding the period 1995-2016 results in a relatively short sample of slightly over 20 years, which might make it difficult to distinguish the transitory and permanent components of monetary disturbances. The estimated impulse responses appear in the bottom panel of figure 6. The figure suggests that the main results obtained using U.S. data carry over to employing Japanese data.

Summarizing, the main result of this section is that the estimated SVAR model predicts that a permanent increase in the nominal interest rate causes an immediate increase in inflation and transitional dynamics characterized by low real interest rates, and no output loss. The remainder of this paper is devoted to ascertaining whether these results carry over to optimizing models.

# 5 A New-Keynesian Model

I assume that there is a representative household with preferences defined over streams of consumption and labor effort and exhibiting external habit formation in consumption. Specifically, the lifetime utility function of the household is given by

$$E_0 \sum_{t=0}^{\infty} \beta^t e^{\xi_t} \left\{ \frac{\left[ (C_t - \delta \widetilde{C}_{t-1})(1 - e^{\theta_t} h_t)^{\chi} \right]^{1-\sigma} - 1}{1 - \sigma} \right\}, \tag{5}$$

where  $C_t$  denotes consumption in period t,  $\widetilde{C}_t$  denotes the cross sectional average of consumption,  $h_t$  denotes hours worked in period t,  $\xi_t$  and  $\theta_t$  denote exogenous preference shocks,  $E_t$  denotes the expectations operator conditional on information available in period t, and  $\beta, \delta \in (0,1)$  and  $\sigma, \chi > 0$  are parameters.

The preference shocks are assumed to follow AR(1) processes of the form

$$\xi_{t+1} = \rho_{\xi} \xi_t + \sigma_{\xi} \epsilon_{t+1}^{\xi}$$

and

$$\theta_{t+1} - \theta = \rho_{\theta}(\theta_t - \theta) + \sigma_{\theta}\epsilon_{t+1}^{\theta},$$

where  $\epsilon_t^{\xi}$  and  $\epsilon_t^{\theta}$  are i.i.d. innovations distributed N(0,1), and  $\rho_{\xi}, \rho_{\theta} \in (-1,1)$  and  $\sigma_{\xi}, \sigma_{\theta} > 0$  are parameters.

Households are subject to the budget constraint

$$P_t C_t + \frac{B_{t+1}}{1 + I_t} + T_t = B_t + W_t^n h_t + \Phi_t, \tag{6}$$

where  $P_t$  denotes the nominal price of consumption,  $B_{t+1}$  denotes a one-period, nominal discount bond purchased in t and paying the nominal interest rate  $I_t$  in t+1,  $T_t$  denotes nominal lump-sum taxes,  $W_t^n$  denotes the nominal wage rate, and  $\Phi_t$  denotes nominal profits received from firms.

Households choose processes  $\{C_t, h_t, B_{t+1}\}_{t=0}^{\infty}$  to maximize the utility function (5) subject to the budget constraint (6) and to some borrowing limit that prevents them from engaging in Ponzi schemes. Letting  $\beta^t \Lambda_t/P_t$  denote the Lagrange multiplier associated with the budget constraint, the first-order conditions of the household's optimization problem are

$$e^{\xi_t} (C_t - \delta \widetilde{C}_{t-1})^{-\sigma} (1 - e^{\theta_t} h_t)^{\chi(1-\sigma)} = \Lambda_t$$
$$\frac{\chi e^{\theta_t} (C_t - \delta \widetilde{C}_{t-1})}{1 - e^{\theta_t} h_t} = W_t$$

and

$$\Lambda_t = \beta(1+I_t)E_t \left[\frac{\Lambda_{t+1}}{1+\Pi_{t+1}}\right],$$

where  $W_t \equiv W_t^n/P_t$  denotes the real wage, and  $\Pi_t \equiv P_t/P_{t-1} - 1$  denotes the consumer-price inflation rate.

The consumption good  $C_t$  is assumed to be a composite of a continuum of varieties  $C_{it}$  indexed by  $i \in [0, 1]$ . The aggregation technology is assumed to be of the CES form

$$C_t = \left[ \int_0^1 C_{it}^{1-1/\eta} di \right]^{\frac{1}{1-1/\eta}},$$

where the parameter  $\eta > 0$  denotes the elasticity of substitution across varieties. Given  $C_t$ , the household chooses the consumption of varieties  $C_{it}$  to minimize total expenditure,  $\int_0^1 P_{it}C_{it}di$ , subject to the aggregation technology, where  $P_{it}$  denotes the nominal price of variety i. This problem delivers the following demand for individual varieties:

$$C_{it} = C_t \left(\frac{P_{it}}{P_t}\right)^{-\eta},\tag{7}$$

where the price level  $P_t$  is given by

$$P_t \equiv \left[ \int_0^1 P_{it}^{1-\eta} di \right]^{\frac{1}{1-\eta}}, \tag{8}$$

and represents the minimum cost of one unit of composite consumption.

The firm producing variety i operates in a monopolistically competitive market, and faces quadratic price adjustment costs à la Rotemberg. The production technology uses labor and is buffeted by stationary and nonstationary productivity shocks. Specifically, output of variety i is given by

$$Y_{it} = e^{z_t} X_t^n h_{it}^{\alpha}, \tag{9}$$

where  $Y_{it}$  denotes output of variety i in period t,  $h_{it}$  denotes labor input used in the produc-

tion of variety i, and  $z_t$  and  $X_t^n$  denote the stationary and nonstationary productivity shocks, respectively. The transitory productivity shock and the growth rate of the nonstationary productivity shock,  $g_t \equiv \ln(X_t^n/X_{t-1}^n)$ , are assumed to follow AR(1) processes of the form

$$z_{t+1} = \rho_z z_t + \sigma_z \epsilon_{t+1}^z$$

and

$$g_t - g = \rho_g(g_{t-1} - g) + \sigma_g \epsilon_t^g,$$

where  $\epsilon_t^z$  and  $\epsilon_t^g$  are exogenous disturbances distributed i.id. N(0,1), and  $\sigma_z, \sigma_g > 0$  and  $\rho_z, \rho_g \in (0,1)$  are parameters.

The expected present discounted value of profits of the firm producing variety i is given by

$$E_0 \sum_{t=0}^{\infty} q_t \left[ \frac{P_{it}}{P_t} C_{it} - W_t h_{it} - \frac{\phi}{2} X_t^n \left( \frac{P_{it}}{\widetilde{X}_t^m P_{it-1}} - 1 \right)^2 \right], \tag{10}$$

where the parameter  $\phi > 0$  governs the degree of price stickiness. The variable  $q_t$ , defined as

$$q_t \equiv \beta^t \frac{\Lambda_t}{\Lambda_0},$$

denotes a pricing kernel reflecting the assumption that profits belong to the representative household.

Note that the price adjustment cost in the profit equation (10) is multiplied by the nonstationary technological factor  $X_t^n$ . This keeps nominal rigidities from vanishing along the balanced growth path. Also, the model features price indexation to a variable  $\widetilde{X}_t^m$ , which is taken as exogenous by the firm. To ensure that the Fisher effect hold in equilibrium the indexation factor  $\widetilde{X}_t^m$  must be cointegrated with the permanent components of inflation and the interest rate, which I denote  $X_t^m$  and will define more precisely later on. Failing to incorporate this type of indexation would imply lack of cointegration between inflation and the nominal interest rate. In this case, the model would be unable to capture the empirical

evidence on the long-run comovement between inflation and nominal rates presented in section 2. Within the general class just described, however, indexation can take different forms. Here, to allow for the possibility that in the short run firm-level inflation and  $X_t^m$  be decoupled, the evolution of the indexation factor  $\widetilde{X}_t^m$  is assumed to be of the form

$$\widetilde{X}_t^m = (X_t^m)^{\gamma_m} \left( \widetilde{X}_{t-1}^m \right)^{1-\gamma_m}, \tag{11}$$

where  $\gamma_m \in [0, 1)$  is smoothing parameter. The smaller  $\gamma_m$  is, the less responsive the indexation factor  $\widetilde{X}_t^m$  will be to short-run movements in the permanent component of inflation. In subsection 6.1 I generalize this formulation to allow firms to index to past inflation.

The problem of the firm producing variety i is to choose process  $\{P_{it}, C_{it}, Y_{it}, h_{it}\}_{t=0}^{\infty}$  to maximize (10) subject to the demand equation (7), to the production technology (9), and to the requirement that demand be satisfied at the price set by the firm,<sup>4</sup>

$$Y_{it} \ge C_{it} \tag{12}$$

Letting  $q_t P_{it}/(P_t \mu_t)$  be the Lagrange multiplier on the demand constraint (12), the first-order conditions associated with the firm's profit maximization problem are

$$\mu_t = \frac{P_{it}/P_t}{W_t/(\alpha e^{z_t} X_t^n h_{it}^{\alpha - 1})}$$

$$\eta C_{it} \left( \frac{\eta - 1}{\eta} - \frac{1}{\mu_t} \right) = -\phi X_t^n \frac{P_t}{\widetilde{X}_t^m P_{it-1}} \left( \frac{P_{it}}{\widetilde{X}_t^m P_{it-1}} - 1 \right) + \phi E_t \frac{q_{t+1}}{q_t} \widetilde{X}_{t+1}^n \frac{P_{it+1} P_t}{\widetilde{X}_{t+1}^m P_{it}^2} \left( \frac{P_{it+1}}{\widetilde{X}_{t+1}^m P_{it}} - 1 \right)$$

The first optimality condition says that the multiplier  $\mu_t$  represents the markup of prices over marginal cost. The second optimality condition says that, all other things equal, if the

<sup>&</sup>lt;sup>4</sup>Strictly speaking, the right-hand side of this constraint must include the demand for goods of variety i by all firms for the purpose of generating the units of composite goods devoted to cover the price adjustment costs. However, because price adjustment costs are quadratic in the transitory component of firm-level inflation and because the latter is nil along the deterministic balanced growth path, this source of demand for good i and all of its derivatives with respect to  $P_{it}$  are zero in equilibrium up to first order.

price markup is above its normal level,  $\mu_t > \eta/(\eta - 1)$ , the firm will increase prices at a rate below normal,  $P_{it}/P_{it-1} < \widetilde{X}_t^m$ .

I assume that the monetary authority follows a Taylor-type interest-rate feedback rule with policy smoothing, as follows

$$1 + I_t = \left[ A \left( \frac{1 + \Pi_t}{X_t^m} \right)^{\alpha_{\pi}} \left( \frac{Y_t}{X_t^n} \right)^{\alpha_y} X_t^m \right]^{1 - \gamma_I} (1 + I_{t-1})^{\gamma_I} e^{z_t^m},$$

where  $Y_t$  denotes aggregate output,  $z_t^m$  denotes a stationary monetary shock,  $X_t^m$  represents a permanent monetary shock, and A,  $\alpha_{\pi}$ ,  $\alpha_{y}$  and  $\gamma_{I} \in [0, 1)$  are parameters.

Let

$$g_t^m \equiv \ln\left(\frac{X_t^m}{X_{t-1}^m}\right)$$

denote the growth rate of the permanent monetary shock. I postulate AR(1) processes for  $g_t^m$  and  $z_t^m$ ,

$$g_t^m = \rho_{gm} g_{t-1}^m + \sigma_{gm} \epsilon_t^{gm}$$

and

$$z_t^m = \rho_{zm} z_{t-1}^m + \sigma_{zm} \epsilon_t^{zm},$$

where  $\epsilon_t^{gm}$  and  $\epsilon_t^{zm}$  are exogenous i.i.d. innovations distributed N(0,1), and  $\rho_{gm}, \rho_{zm} \in (0,1)$  and  $\sigma_{gm}, \sigma_{zm} > 0$  are parameters.

I assume that government consumption is nil at all times. Thus, the fiscal authority faces the budget constraint

$$T_t + \frac{B_{t+1}}{1 + I_t} = B_t.$$

Further, I assume that fiscal policy is Ricardian, in the sense that the government sets  $T_t$  to ensure intertemporal solvency independently of the paths of the price level or the nominal interest rate.

Clearing of the labor market requires that the demand for labor by firms equal the

household's supply of labor, that is,

$$\int_0^1 h_{it} di = h_t. \tag{13}$$

Because all households are identical, so are individual and aggregate consumption per capita,

$$C_t = \widetilde{C}_t$$
.

I focus attention on a symmetric equilibrium in which all firms charge the same nominal price and employ the same amount of labor, that is, an equilibrium in which  $h_{it}$  and  $P_{it}$  are the same for all  $i \in [0, 1]$ . We then have from equations (7), (8), (9), and (13) that  $P_{it} = P_t$ ,  $C_{it} = C_t$ ,  $h_{it} = h_t$ , and  $Y_{it} = e^{z_t} X_t^n h_t^{\alpha}$ , for all i. Output, measured in units of the final good is then given by  $Y_t \equiv \left(\int_0^1 P_{it} Y_{it} di\right) / P_t = e^{z_t} X_t^n h_t^{\alpha}$ . As long as the nominal wage is positive, the firm will choose to satisfy the demand constraint (12) with equality. By virtue of this condition, we have that in equilibrium

$$Y_t = C_t$$
.

Finally, I express the model in terms of stationary variables by dividing all variables with stochastic trends by their respective permanent components. Thus, I create the variables  $c_t \equiv C_t/X_t^n$ ,  $y_t \equiv Y_t/X_t^n$ ,  $w_t \equiv W_t/X_t^n$ ,  $\lambda_t \equiv \Lambda_t/X_t^{n-\sigma}$ ,  $1 + \pi_t \equiv (1 + \Pi_t)/X_t^m$ ,  $1 + i_t \equiv (1 + I_t)/X_t^m$ , and  $\widetilde{x}_t^m \equiv \widetilde{X}_t^m/X_t^m$ .

A competitive equilibrium is then a set of process  $\{y_t, h_t, \lambda_t, \pi_t, i_t, w_t, \text{mc}_t, \widetilde{x}_{t+1}^m\}$  satisfying

$$e^{\xi_t} \left( y_t - \delta \frac{y_{t-1}}{e^{g_t}} \right)^{-\sigma} \left( 1 - e^{\theta_t} h_t \right)^{\chi(1-\sigma)} = \lambda_t$$

$$\frac{\chi e^{\theta_t} \left( y_t - \delta \frac{y_{t-1}}{e^{g_t}} \right)}{1 - e^{\theta_t} h_t} = w_t$$

$$\lambda_t = \beta (1 + i_t) E_t \left[ \frac{\lambda_{t+1}}{1 + \pi_{t+1}} e^{-g_{t+1}^m - \sigma g_{t+1}} \right],$$

$$y_{t} = e^{z_{t}} h_{t}^{\alpha}$$

$$mc_{t} = \frac{w_{t}}{\alpha e^{z_{t}} h_{t}^{\alpha - 1}}$$

$$\frac{1 + \pi_{t}}{\widetilde{x}_{t}^{m}} \left(\frac{1 + \pi_{t}}{\widetilde{x}_{t}^{m}} - 1\right) = \beta E_{t} e^{(1 - \sigma)g_{t+1}} \frac{\lambda_{t+1}}{\lambda_{t}} \frac{1 + \pi_{t+1}}{\widetilde{x}_{t+1}^{m}} \left(\frac{1 + \pi_{t+1}}{\widetilde{x}_{t+1}^{m}} - 1\right) + \frac{1}{\phi(\mu - 1)} (\mu mc_{t} - 1) y_{t}$$

$$1 + i_{t} = \left[A \left(1 + \pi_{t}\right)^{\alpha_{\pi}} y_{t}^{\alpha_{y}}\right]^{1 - \gamma_{I}} \left(\frac{1 + i_{t-1}}{e^{g_{t}^{m}}}\right)^{\gamma_{I}} e^{z_{t}^{m}},$$

$$\widetilde{x}_{t}^{m} = e^{-(1 - \gamma_{m})g_{t}^{m}} \widetilde{x}_{t+1}^{m(1 - \gamma_{m})}$$

$$(14)$$

where  $mc_t \equiv 1/\mu_t$  and  $\mu \equiv \eta/(\eta - 1)$  denote, respectively, the equilibrium real marginal cost and the steady-state product markup. Equation (14) is a Phillips curve and says that all other things equal, current inflation is increasing in the marginal cost. A first-order approximation of the Phillips curve around  $\pi_t = \pi = 0$  yields

$$\widehat{\pi}_t - \widehat{\widetilde{x}}_t^m = \widetilde{\beta} E_t(\widehat{\pi}_{t+1} - \widehat{\widetilde{x}}_{t+1}^m) + \kappa \widehat{\mathrm{mc}}_t, \tag{15}$$

where  $\widetilde{\beta} \equiv \beta e^{(1-\sigma)g}$ ,  $\kappa \equiv \frac{(\eta-1)y}{\phi}$ ,  $\widehat{\pi}_t \approx \pi_t - \pi$ ,  $\widehat{\mathrm{mc}}_t \approx \ln(\mathrm{mc}_t/\mathrm{mc})$ ,  $\widehat{\widetilde{x}}_t^m \approx \ln \widetilde{x}_t^m$ , and  $\mathrm{mc} = 1/\mu$ . This is a familiar expression of a linear Phillips curve, except that it is cast in terms of deviations of the cyclical component of inflation,  $\widehat{\pi}_t$  from the cyclical component of the indexation factor,  $\widehat{\widetilde{x}}_t^m$ .

#### 5.1 Data, Priors, and Estimation

As in much of the DSGE literature, I estimate a subset of the parameters of the model and calibrate the remaining parameters of the model using standard values in business-cycle analysis. The set of estimated parameters includes those that play a central role in determining the model's implied short-run dynamics.

Table 4 displays the values assigned to each calibrated parameter. I set the subjective discount factor,  $\beta$ , equal to 0.9982, which implies a growth-adjusted discount factor,  $\beta e^{-\sigma g}$ 

Table 4: Calibrated Parameters in the New Keynesian Model

Parameter	Value	Description
β	0.9982	subjective discount factor
$\sigma$	2	inverse of intertemp. elast. subst.
$\eta$	6	intratemporal elast. of subst.
$\alpha$	0.75	labor semielast. of output
g	0.004131	mean output growth rate
$\theta$	0.4055	preference parameter
$\chi$	0.625	preference parameter

Note. The time unit is one quarter.

equal to 0.99; the reciprocal of the intertemporal elasticity of substitution,  $\sigma$ , to 2; the intratemporal elasticity of substitution across varieties of intermediate goods,  $\eta$ , to 6, which implies a steady-state markup of price over marginal cost of 20 percent (Galí, 2008); the labor semi elasticity of the production function,  $\alpha$  to 0.75, the unconditional mean of per capita output growth, g, equal to 0.004131 (1.65 percent per year), which matches the average growth rate of real GDP per capita in the United States over the estimation period (1954:Q4 to 2018:Q2); and the parameters  $\theta$  and  $\chi$  to ensure, given all other parameter values, that in the steady state households allocate one third of their time to work, h = 1/3, and a unit Frisch elasticity of labor supply,  $(1 - e^{\theta}h)/(e^{\theta}h) = 1$ , as in Galí (2008).

I estimate the remaining parameters of the model using the same observables as in the estimation of the empirical model of section 3, namely, per-capita output growth, the interest-rate-inflation differential, and the change in the nominal interest rate. The data sources are as described in subsection 3.3. As in the case of the empirical model, the econometric estimation employs Bayesian techniques. Table 5 displays means, standard deviations, and 95% intervals of the prior and posterior distributions of the estimated parameters. I impose loose priors on all estimated parameters. I assume a Gamma prior distribution with a mean of 50 and a standard deviation of 20 for the parameter  $\phi$  governing the degree of price stickiness. The assumed mean prior value of  $\phi$  ensures that given the calibrated values of  $\eta$ ,  $\alpha$ , and  $\theta$ , the value of  $\kappa$  in equation (15) is 0.043, as in Galí (2008). The speed of adjustment of the

Table 5: Prior and Posterior Parameter Distributions: New-Keynesian Model

	Prior Distribution			Posterior Distribution			
Parameter	Distribution	Mean	Std	Mean	Std	5%	95%
$\overline{\phi}$	Gamma	50	20	159	31.3	111	214
$lpha_\pi$	Gamma	1.5	0.25	1.83	0.31	1.35	2.37
$lpha_y$	Gamma	0.125	0.1	0.687	0.2	0.386	1.03
$\gamma_m$	Uniform	0.5	0.289	0.464	0.195	0.201	0.851
$\gamma_I$	Uniform	0.5	0.289	0.579	0.108	0.366	0.722
$\delta$	Uniform	0.5	0.289	0.294	0.0508	0.21	0.378
$ ho_{m{\xi}}$	Beta	0.7	0.2	0.902	0.0259	0.856	0.941
$ ho_{ heta}$	Beta	0.7	0.2	0.673	0.201	0.305	0.954
$ ho_z$	Beta	0.7	0.2	0.667	0.206	0.289	0.954
$ ho_g$	Beta	0.3	0.2	0.403	0.0915	0.236	0.538
$ ho_{gm}$	Beta	0.3	0.2	0.331	0.176	0.0553	0.625
$ ho_{zm}$	Beta	0.3	0.2	0.195	0.126	0.0346	0.432
$\sigma_{\xi}$	Gamma	0.01	0.01	0.0251	0.00393	0.0199	0.0325
$\sigma_{ heta}$	Gamma	0.01	0.01	0.00164	0.0013	0.000119	0.00417
$\sigma_z$	Gamma	0.01	0.01	0.00124	0.001	9.22e-05	0.00318
$\sigma_g$	Gamma	0.01	0.01	0.00626	0.000841	0.00492	0.00769
$\sigma_{gm}$	Gamma	0.0025	0.0025	0.00103	0.00032	0.000567	0.0016
$\sigma_{zm}$	Gamma	0.0025	0.0025	0.00155	0.000271	0.00107	0.00189
$R_{11}$	Gamma	3.78e-06	2.18e-06	4.3e-06	2.43e-06	1.17e-06	8.95e-06
$R_{22}$	Gamma	2.08e-06	1.2e-06	4.43e-06	4.99e-07	3.66e-06	5.29e-06
$R_{33}$	Gamma	2.36e-07	1.36e-07	2.24e-07	1.25 e-07	6.29 e-08	4.65e-07

Note. The time unit is one quarter. Growth rates and log-deviations from trend are expressed in per one (1 percent is denoted 0.01).

indexation factor, dictated by  $\gamma_m \in (0,1)$ , takes a uniform distribution with support [0,1]. The parameters  $\alpha_{\pi}$  and  $\alpha_{y}$  have Gamma prior distributions with means equal to 1.5 and 0.5/4 (two commonly used values) and standard deviation equal to 0.25 and 0.1, respectively. The parameter  $\gamma_I$  measuring the smoothness of monetary policy has a uniform prior distribution with support [0, 1]. The degree of external habit formation, given by  $\delta \in [0, 1)$ , adopts a uniform prior distribution with support [0, 1]. Echoing the priors imposed in the empirical model, I assume that the serial correlations of the permanent nonstationary shock and of the two monetary shocks ( $\rho_g$ ,  $\rho_{gm}$ , and  $\rho_{zm}$ , respectively) have Beta distributions with mean equal to 0.3 and standard deviation equal to 0.2, and that the serial correlations of all stationary nonmonetary shocks  $(\rho_{\xi}, \rho_{\theta}, \text{ and } \rho_z)$  have Beta distributions with mean 0.7 and standard deviation 0.2. Similarly, In line with the empirical model, I assume that the standard deviations of the two monetary shocks,  $\sigma_{gm}$  and  $\sigma_{zm}$ , take Gamma distributions with mean and standard deviation equal to 1/400, that the standard deviation of the permanent nonmonetary shock,  $\sigma_g$ , has a Gamma distribution with mean and standard deviation equal to 1/100, and that the standard deviations of all stationary nonmonetary shocks ( $\sigma_{\xi}$ ,  $\sigma_{\theta}$ , and  $\sigma_z$ ) have Gamma distributions with mean and standard deviation equal to 1/100. Finally, as in the empirical model, I introduce measurement error and assume that their variances have uniform distributions with an upper bound equal to 10 percent of the variance. of the observables.

The last four columns of table 5 displays key features of the estimated posterior distributions, based on a Random Walk Metropolis Hastings MCMC chain of length one million after discarding 100 thousand burn-in draws. Most parameters are estimated with significant uncertainty, a feature that is common in estimates of small-scale New Keynesian models (Ireland, 2007). Nonetheless, the data speaks with a strong voice on the parameters  $\phi$  and  $\delta$ , governing price stickiness and habit formation, which are key determinants of the propagation of nominal and real shocks. Furthermore, it is reassuring, given the focus of this paper, that the estimated path of the nonstationary monetary shock, the latent variable

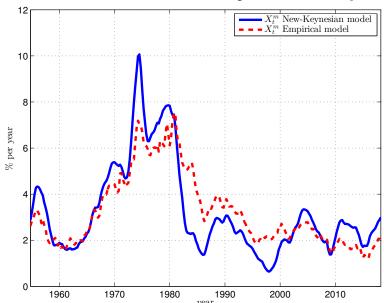


Figure 7: Inflation and Its Permanent Component: New Keynesian Model

Note. Quarterly frequency. The inferred path of the permanent component of inflation,  $X_t^m$ , was computed by Kalman smoothing and evaluating the model at the posterior mean of the estimated parameter vector. The initial value of  $X_t^m$  was normalized to make the average value of  $X_t^m$  equal to the average rate of inflation over the sample period, 1954:Q4 to 2018:Q2.

 $X_t^m$ , resembles its counterpart in the empirical model. This is shown in Figure 7, which displays the inferred paths of  $X_t^m$  from the New-Keynesian and empirical models. Overall, the nonstationary monetary shock implied by the optimizing model tracks the one stemming from the empirical model quite well. The sample correlation of the two series is 0.86. The path of  $X_t^m$  implied by the New-Keynesian model is more volatile than the one coming from the SVAR model, perhaps due to the fact that the latter model has a richer lag structure.

An additional measure of coherence between the predictions of the estimated empirical and New-Keynesian models is a comparison of their implied variance decompositions. Table 6 displays this information for the New Keynesian model. Comparing tables 3 and 6 shows that both the SVAR and New Keynesian models predict that the permanent monetary shock explains more than 40 percent of changes in the rate of inflation. Thus, in both models the nonstationary component of monetary disturbances plays a significant role in explaining movements in nominal variables. Also, in both models the stationary monetary

Table 6: Variance Decomposition: New Keynesian Model

	$\Delta y_t$	$\Delta \pi_t$	$\Delta i_t$
Permanent Monetary Shock, $g_t^m$	1.7	42.8	9.3
Transitory Monetary Shock, $z_t^m$	3.0	2.1	35.7
Permanent Productivity Shock, $g_t$	84.7	2.2	4.8
Transitory Productivity Shock, $z_t$	0.4	5.1	2.1
Preference Shock, $\xi_t$	9.7	42.8	46.0
Labor-Supply Shock, $\theta_t$	0.4	5.1	2.0

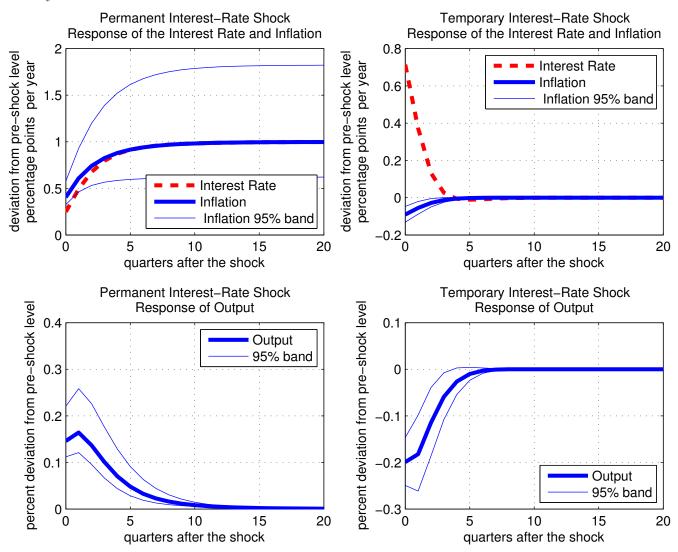
Note. Posterior means. The variables  $\Delta y_t$ ,  $\Delta \pi_t$ , and  $\Delta i_t$  denote output growth, the change in inflation, and the change in the nominal interest rate, respectively.

shock accounts for a relatively small share of movements in the rate of inflation. Another similarity between the empirical and optimizing models is that in both the nonstationary nonmonetary shock explains a significant fraction of the variations in output growth, although in the New Keynesian model this role is estimated to be much larger. Finally, in both models nonmonetary stationary shocks explain almost half of changes in the nominal interest rate. Thanks to its more structural nature, the optimizing model is able to say more about which specific nonmonetary stationary sources of uncertainty are the most relevant. Specifically, while the SVAR model encapsulates all stationary nonmonetary disturbances in a single shock,  $z_t^n$ , the New Keynesian model can distinguish finer categories and suggests that it is a demand shock,  $\xi_t$ , that has the largest impact on the nominal interest rate.

# 6 The Neo-Fisher Effect in the New-Keynesian Model

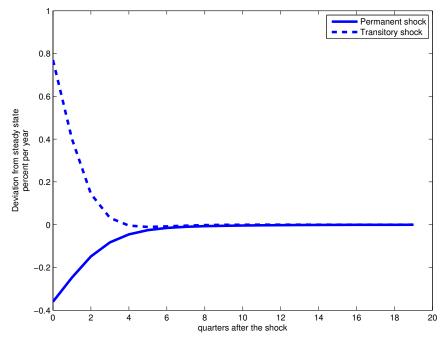
Figure 3 displays the impulse responses of inflation, the policy rate, and output to permanent and transitory monetary shocks implied by the estimated New-Keynesian model. The main message conveyed by the figure is that qualitatively the responses implied by the New-Keynesian model concur with those implied by the empirical model of sections 3 and 4. An increase in the nominal interest rate that is understood to be permanent by private agents (left panels of the figure) causes an increase in inflation in the short run, without loss of

Figure 8: Impulse Responses to Permanent and Temporary Interest-Rate Shocks: New-Keynesian Model



Notes. Impulse responses are posterior mean estimates. Asymmetric error bands are computed using the Sims-Zha (1999) method.

Figure 9: Response of the Real Interest Rate to Permanent and Transitory Interest-Rate Shocks: New-Keynesian Model



Notes. Posterior mean estimates. The real interest rate is defined as  $i_t - E_t \pi_{t+1}$ .

aggregate activity. By contrast, an increase in the nominal interest rate that is interpreted to be transitory (right panels of the figure) causes a fall in inflation and a contraction in aggregate activity.

Why does a permanent increase in the nominal interest rate cause no loss in aggregate activity and a temporary tightening does? In the discussion of the predictions of the empirical model, I suggested that the answer could be in the behavior of the real interest rate. This conjecture is supported by the dynamics of the optimizing model. Figure 9 shows that in response to a permanent increase in the nominal interest rate inflation not only begins to increase immediately, but does so at a rate faster than the nominal interest rate. As a result, the real interest rate falls. By contrast, a temporary increase in the nominal interest rate causes a fall in inflation and an increase in the real interest rate. A natural question is why inflation moves faster than the interest rate in the short run when the monetary shock is expected to be permanent. The answer has to do with the presence of nominal rigidities and with the way the central bank conducts monetary policy. In response to a permanent

monetary shock that increases the nominal interest rate by one percent in the long run, the central bank raises the short-run policy rate quickly but gradually. At the same time, firms know that, by the Fisher effect, the price level will increase by one percent in the long run, and that they too will have to increase their own price in the same proportion in the long run to avoid making losses. Since firms face quadratic costs of adjusting prices, they find it optimal to begin increasing the price immediately. Since all firms do the same, inflation itself begins to increase as soon as the shock is announced.

#### 6.1 Robustness

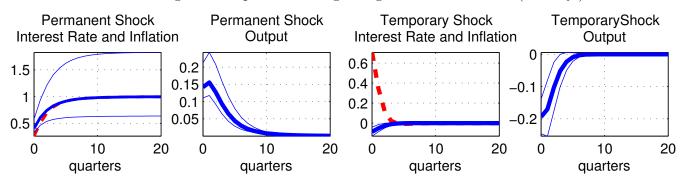
Figure 10 displays three tests. The top two panels are the counterparts of the robustness checks applied on the empirical model (see figure 6). They show that the predictions of the theoretical model are qualitatively stable to truncating the sample in 2008:Q4 to exclude the period in which U.S. monetary policy could have been limited by the zero lower bound on interest rate, and to estimating the model on Japanese data. The bottom panel considers a variant of the New-Keynesian model in which firms can index prices to past aggregate inflation. Specifically, this version assume that the indexation factor  $\tilde{X}_t^m$  takes the form

$$\widetilde{X}_{t}^{m} = \left[X_{t}^{m\gamma_{mm}}(1+\Pi_{t-1})^{1-\gamma_{mm}}\right]^{\gamma_{m}} (\widetilde{X}_{t-1}^{m})^{1-\gamma_{m}}$$

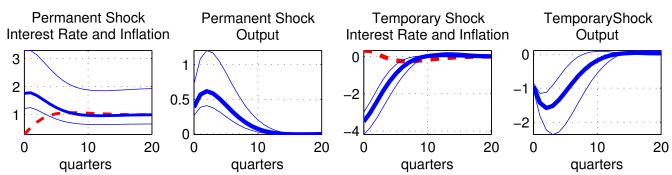
with the new parameter  $\gamma_{mm} \in [0, 1]$ . This formulation nests the baseline formula given by (11). Reestimating the model on the baseline dataset (i.e., U.S. data over the period 1954:Q4 to 2018:Q2) yields a posterior mean value of  $\gamma_{mm}$  of 0.061 and a posterior standard deviation of 0.058, suggesting that indexation to past inflation is relevant. The bottom panel of figure 10 shows that this version of the model produces predictions that are qualitatively in line with the baseline ones.

Figure 10: Robustness Checks: Optimizing Model

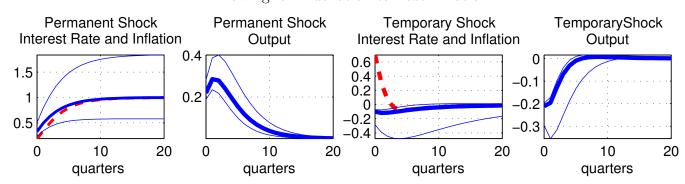
Truncating the Sample at the Beginning of the ZLB Period (2008:Q4)



Estimation on Japanese Data (1955.Q3 to 2016.75)



Allowing for Indexation to Past Inflation



Notes. Thick lines are posterior means. Thick broken lines correspond to the nominal interest rate. Thin lines are 95% asymmetric error bands computed using the Sims-Zha (1999) method.

## 7 Conclusion

Discussions of how monetary policy can lift an economy out of chronic below-target inflation are almost always based on the logic of how transitory interest-rate shocks affect real and nominal variables. Nowadays, there is little theoretical or empirical controversy around how this type of monetary shock transmits to the rest of the economy: An increase in the nominal interest rate causes an increase in the real interest rate, which puts downward pressure on both aggregate activity and price growth. Within this logic, a central bank trying to reflate a low-inflation economy will tend to set interest rates as low as possible. Soon enough these economies find themselves with zero or negative nominal rates and with the low-inflation problem not going away. After some time, the Fisher effect kicks in, and the situation perpetuates. The monetary authority keeps the interest rate low because inflation is still below target (the temporary-interest-rate-shock logic) and inflation is low because the interest rate has been low for a long period of time (the Fisher effect).

In this paper I argue, based on econometric evidence drawn from an empirical and optimizing model that a gradual and permanent increase in the nominal interest rate causes a fast adjustment of inflation to a permanently higher level, low real interest rates, and no output loss. These findings are consistent with the prediction, sometimes referred to as neo-Fisherian, that a credible announcement of a gradual return of the nominal interest rate to normal levels can achieve a swift reflation of the economy with sustained levels of economic activity.

# Appendix: Detailed Exposition of the Empirical Model

Let  $Y_t$  be a vector collecting these three variables,

$$Y_t \equiv \left[ \begin{array}{c} y_t \\ \pi_t \\ i_t \end{array} \right],$$

where  $y_t$  denotes the logarithm of real output per capita,  $\pi_t$  denotes the inflation rate expressed in percent per year, and  $i_t$  denotes the nominal interest rate expressed in percent per year. Let  $\tilde{Y}_t$ 

$$\tilde{Y}_t \equiv \begin{bmatrix} (y_t - X_t^n) \times 100 \\ \pi_t - X_t^m \\ i_t - X_t^m \end{bmatrix},$$

where  $X_t^m$  is a permanent monetary shock,  $z_t^m$  is a transitory monetary shock,  $X_t^n$  is a nonstationary nonmonetary shock, and  $z_t^n$  is a stationary nonmonetary shock. Let  $\hat{Y}_t$  denote the deviation of  $\tilde{Y}_t$  from its unconditional mean, that is,

$$\hat{Y}_t \equiv \left[ egin{array}{c} \hat{y}_t \\ \hat{\pi}_t \\ \hat{i}_t \end{array} 
ight] \equiv \tilde{Y}_t - E\tilde{Y}_t,$$

where E denotes the unconditional expectations operator.

The law of motion of  $\hat{Y}_t$  takes the autoregressive form

$$\hat{Y}_t = \sum_{i=1}^{L} B_i \hat{Y}_{t-i} + C u_t \tag{16}$$

where

$$u_{t} \equiv \begin{bmatrix} x_{t}^{m} \\ z_{t}^{m} \\ x_{t}^{n} \\ z_{t}^{n} \end{bmatrix},$$
$$x_{t}^{m} \equiv \Delta X_{t}^{m} - \Delta X^{m}$$

and

$$x_t^n \equiv (\Delta X_t^n - \Delta X^n) \times 100.$$

with  $\Delta$  denoting the time-difference operator,  $\Delta X^m \equiv E\Delta X^m_t$ , and  $\Delta X^n \equiv E\Delta X^n_t$ . The variables  $x^m_t$  and  $x^n_t$  denote demeaned changes in the nonstationary shocks. The objects  $B_i$ , for  $i=1,\ldots,L$ , are 3-by-3 matrices of coefficients, C is a 3-by-4 matrix of coefficients, and L is a scalar denoting the lag length of the empirical model. The vector  $u_t$  is assumed to follow an AR(1) law of motion of the form

$$u_{t+1} = \rho u_t + \psi \epsilon_{t+1},\tag{17}$$

where  $\rho$  and  $\psi$  are 4-by-4 diagonal matrices of coefficients, and  $\epsilon_t$  is a 4-by-1 i.i.d. disturbance distributed  $N(\emptyset, I)$ .

The observable variables used in the estimation of the empirical model are output growth expressed in percent per quarter, the change in the nominal interest rate, and the interestrate-inflation differential, defined as

$$r_t \equiv i_t - \pi_t$$
.

The following equations link the observables to variables included in the unobservable system

(16)-(17):

$$100 \times \Delta y_{t} = 100 \times \Delta X^{n} + \hat{y}_{t} - \hat{y}_{t-1} + x_{t}^{n}$$

$$r_{t} = r + \hat{i}_{t} - \hat{\pi}_{t}$$

$$\Delta i_{t} = \Delta X^{m} + \hat{i}_{t} - \hat{i}_{t-1} + x_{t}^{m}$$
(18)

where  $r \equiv Er_t$  represents the unconditional mean of the interest-rate-inflation differential. The variables  $\Delta y_t$ ,  $r_t$ , and  $\Delta i_t$  are assumed to be observed with measurement error. Let  $o_t$  be the vector of variables observed in quarter t. Then

$$o_t = \begin{bmatrix} \Delta y_t \times 100 \\ r_t \\ \Delta i_t \end{bmatrix} + \mu_t \tag{19}$$

where  $\mu_t$  is a 3-by-1 vector of measurement errors distributed i.i.d.  $N(\emptyset, R)$ , and R is a diagonal variance-covariance matrix.

The state-space representation of the system composed of equations (16), (17), (18), and (19) can be written as follows:

$$\xi_{t+1} = F\xi_t + P\epsilon_{t+1}$$

$$o_t = A' + H'\xi_t + \mu_t,$$

where

$$\xi_t \equiv \begin{bmatrix} \hat{Y}_t \\ \hat{Y}_{t-1} \\ \vdots \\ \hat{Y}_{t-L+1} \\ u_t \end{bmatrix},$$

The matrices F, P, A, and H are known functions of  $B_i$ , i = 1, ..., L, C,  $\rho$ ,  $\psi$ ,  $\Delta X^n$ ,  $\Delta X^m$ ,

and r. Specifically, let

$$B \equiv [B_1 \cdots B_L],$$

and let  $I_j$  denote an identity matrix of order j,  $\emptyset_j$  denote a square matrix of order j with all entries equal to zero, and  $\emptyset_{i,j}$  denote a matrix of order i by j with all entries equal to zero. Also let L, S, and V denote, respectively, the number of lags, the number of shocks, and the number of endogenous variables included in the SVAR model. Then, for  $L \geq 2$  we have

$$F = \begin{bmatrix} B & C\rho \\ \left[I_{V(L-1)} \emptyset_{V(L-1),V}\right] & \emptyset_{V(L-1),S} \\ \emptyset_{S,VL} & \rho \end{bmatrix}, P = \begin{bmatrix} C\psi \\ \emptyset_{V(L-1),S} \\ \psi \end{bmatrix};$$

$$A' = \begin{bmatrix} 100 \times \Delta X^n \\ r \\ \Delta X^m \end{bmatrix}, \text{ and } H' = \begin{bmatrix} M_{\xi} & \emptyset_{V,V(L-2)} & M_u \end{bmatrix},$$

where, in the specification considered in the body of the paper (S = 4, V = 3, and a)particular ordering of the endogenous and exogenous variables in the vectors  $\hat{Y}_t$  and  $u_t$ ), the matrices  $M_{\xi}$  and  $M_u$  take the form

$$M_{\xi} = \begin{bmatrix} 1 & 0 & 0 & -1 & 0 & 0 \\ 0 & -1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 \end{bmatrix} \text{ and } M_{u} = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}.$$

The case L=1 is a special case of L=2 in which  $B_2=\emptyset_V$ .

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