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THE PARKABLE PIEZOPROBE FOR DETERMINING C_V AND STRENGTH – MODELLING AND INTERPRETATION METHODS

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ABSTRACT

The parkable piezoprobe (PPP) is a site investigation tool for measuring the coefficient of consolidation, in-situ offshore, at shallow embedment depths. The device applies a similar bearing pressure to subsea infrastructure so reaches a comparable self-weight penetration when 'parked' at the seabed, representative of an unburied pipeline. Instrumentation on the device allows the dissipation of penetration-induced excess pore pressure to be recorded at various locations on the surface. From these dissipation responses the coefficient of consolidation can be inferred, which is a key parameter in the design of many offshore structures founded in surficial soil, such as pipelines or shallow foundations. The intent is that this device is deployed from a seabed frame while other activities such as penetrometer testing or sampling take place in parallel.

This paper presents robust interpretation methods for the parkable piezoprobe by using a combination of centrifuge experiments and large deformation finite element analyses. The centrifuge tests demonstrate that the penetration response of the parkable piezoprobe is adequately captured by existing bearing capacity models, allowing the optimum device weight to be identified. A comprehensive interpretation method is then developed for the dissipation stage. This yields accurate estimates of the coefficient of consolidation, even for cases where there is no prior knowledge of the soil parameters or the depth to which the device embeds under its own self-weight.

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INTRODUCTION

Offshore infrastructure to extract hydrocarbons or develop renewable energy (e.g. pipelines, cables or shallow foundations) is increasingly founded in regions with very soft surficial soils. Robust design of these structures requires reliable measurements of the soil properties, such as undrained strength, s_u, and coefficient of consolidation, c_v. Conventional tools such as the cone penetrometer (Teh & Houlsby, 1991), piezoprobe (Whittle et al. 2001) and Piezoball (Colreavy et al. 2015) are not suited to the very shallow embedment depths relevant to pipeline design. Specialist tools such as actuator-controlled instrumented model pipes (Hill & Jacob 2008; White et al. 2011) are able to measure c_v at the shallow depths required but are prohibitively expensive to routinely deploy.

The parkable piezoprobe (PPP) – as described by Chatterjee et al. (2014) and illustrated in Figure 1 – is a device intended primarily to measure the coefficient of consolidation, c_v. The main benefit of the device is that it does not have to be attached to a drill string or a set of push rods during operation (when 'parked'), making deployment simple and allowing other activities to be performed in parallel, before retrieving the probe. This is a valuable feature since in-situ dissipation tests are costly to perform offshore, due to the time occupied waiting. The ability to run PPP tests unmonitored allows the device to be of similar scale to the infrastructure intended to be installed at the location (e.g. similar to the diameter of a seabed pipeline).

Chatterjee et al. (2014) first described the PPP and reported non-dimensional dissipation solutions for a limited range of soil conditions derived from large deformation finite element analyses. This paper first presents experimental modelling of the PPP concept via small-scale centrifuge model tests. The centrifuge experiments are used to validate a large deformation finite element model, which is then harnessed in an extensive parametric study exploring the sensitivity of the PPP response to the range of soil conditions likely to be found offshore in regions with soft fine-grained surficial soil. Finally, a simple interpretation method is

proposed that could be used to interpret measurements derived from field deployment of a PPP, which results in accurate estimates of the coefficient of consolidation.

PARKABLE PIEZOPROBE

The parkable piezoprobe (PPP) is an elongated spheroid with pore pressure transducers located at the invert and midface positions (see Figure 1). The cross-section of the shape (in elevation) and its diameter (at prototype scale) are comparable to a small seabed pipeline. The probe is envisaged to be lowered on a cable winch from a vessel or from a seabed frame. Alternatively, it could also be deployed from a remotely-operated vehicle (ROV).

After the initial undrained penetration stage, which generates excess pore pressures in the soil, the dissipation response is recorded by an on-board logging system. With suitable interpretation methods this data can be used to estimate the coefficient of consolidation. More accurate estimates can be gained if the settlement is also measured during penetration, as is demonstrated later in the paper. The embedment depth could be estimated via additional pore pressure transducers along the surface of the PPP[1], so that soil contact would be indicated by an initial spike in the corresponding pore water pressure reading. Alternatively, contact image sensors (CIS) could be installed on the surface of the device and used to estimate the soil contact (An et al. 2016).

A probe diameter of 250 mm is suggested for field application of the device. The following discussion uses the initial dissipation solutions of Chatterjee et al. (2014) to illustrate the practical timescale of a PPP test for measuring dissipation characteristics, i.e. the coefficient of consolidation (referred to as c_v for a conventional oedometer or Rowe cell test and c_h for a cone penetrometer or pipe section test) relative to other available devices.

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[1] This was not possible on the centrifuge scale model developed for this study but would be possible on a larger field scale device.

The time required for 50% of the excess pore pressure at the invert of a 250 mm PPP to dissipate, t_{50}, is between 2.9 and 4.4 times that of a standard cone penetrometer ($D = 35.7$ mm) for an embedment of $w/D = 0.5$ and $w/D = 1$, respectively. Although this testing time exceeds the CPT t_{50}, the PPP is uniquely able to measure c_v at very shallow depths where the conventional CPT dissipation interpretation is not reliable. The only other device suited to shallow dissipation characteristics determination is the SMARTPIPE (Hill & Jacob 2008; White et al. 2011). This pipe-like site investigation tool has dissipation times between 1.5 and 2.3 times longer than the PPP, even though the device diameters are similar (PPP: 250 mm; SMARTPIPE: 225 mm). This is due to the planar drainage around the SMARTPIPE. The radial drainage paths around the PPP ($D = 250$ mm) result in shorter test durations despite its slightly larger diameter. Figure 2 shows the time required for 50% of the excess pore pressure to dissipate for different values of the coefficient of consolidation, for the PPP, cone penetrometer and SMARTPIPE. The comparison is based on the following dimensionless dissipation time $T_{50} = c_v t_{50}/D^2$: for the PPP, $T_{50} = 0.036$ for $w/D = 0.5$ and $T_{50} = 0.055$ for $w/D = 1$ (Chatterjee et al., 2014); for the cone penetrometer $T_{50} = 0.613$ for $I_R = 100$ (Teh & Houlsby, 1991); and for the SMARTPIPE $T_{50} = 0.10$ (Gourvenec & White, 2010).

CENTRIFUGE MODELLING

A total of four centrifuge tests of the PPP were carried out in the geotechnical beam centrifuge at UWA. In each test an initial undrained penetration to a target depth of either $0.5D$ or $1D$ (achieved using the actuator in displacement controlled (DC) mode) was followed by a pore pressure dissipation stage (achieved using the actuator in load controlled (LC) mode using feedback from the load cell). During the consolidation phase either the vertical load (LC: load controlled mode) or the displacement (DC: displacement controlled mode) was held constant. The LC mode represents the PPP resting in equilibrium with the self-weight

balanced by the seabed bearing capacity, although in practice the device was fixed to an actuator under feedback control. All model tests are summarized in Table 1.

Table 1: Summary of experimental tests. LC: Load control; DC: displacement control.

Test	Penetration to w/D (-)	Dissipation mode
LC - 0.5D	0.5	LC
DC - 0.5D	0.5	DC
LC - 1D	1.0	LC
DC - 1D	1.0	DC

The model PPP was 50 mm in diameter and manufactured from aluminium with a polished surface (see Figure 1). All tests were performed at an acceleration of 10 g, representing an equivalent field scale PPP with a diameter of 500 mm. The probe was instrumented with a 100 N S-type load cell designed in-house to measure the penetration resistance and 50 kPa range pore pressure transducers located at the invert and midface positions.

Commercial kaolin clay was preconsolidated in-flight at a centrifuge acceleration of 30 g, before reducing the acceleration to 10 g for testing. This resulted in a constant over-consolidation ratio (*OCR*) of 3 and an elevated strength gradient which represents surficial soil conditions commonly found offshore. Penetration was conducted at a rate (0.125 mm/s at model scale), which was sufficiently fast to avoid any significant dissipation of excess pore pressures during the embedment of the PPP. At the end of penetration dissipation was allowed until the penetration induced excess pore pressures had reduced to ~10% of their initial value. To characterise the sample and benchmark the penetration resistance measurements, miniature T-bar penetrometer tests were conducted to measure the undrained strength profile of the sample.

NUMERICAL MODELLING (LDFE)

To correctly capture the soil heave around the PPP during undrained penetration, coupled large deformation FE-analyses (LDFE) were performed. An axisymmetric model based on the "Remeshing and Interpolation Technique with Small Strains (RITSS)" methodology of Hu & Randolph (1998) was developed and implemented in ABAQUS (Dassault Systèmes, 2011), following Wang et al. (2010). In brief, each large deformation analysis is subdivided into many consecutive small strain simulation steps. To preclude severe mesh distortions the whole soil domain is remeshed at the beginning of each step, with all stresses and state parameters remapped from the old mesh of the previous step, to the new undistorted mesh, using the super-convergent patch recovery technique proposed by Zienkiewicz & Zhu (1992). The consolidation phase was simulated using a final conventional small strain analysis, i.e. without further remeshing. The derived stresses and state parameters at the target penetration depth served as initial conditions for the dissipation stage.

The analysis domain was specified to be sufficiently large – with a depth of 10D and a radius of 8D – as to eliminate boundary effects. The Modified Cam Clay soil model (MCC) of Roscoe and Burland (1968) was used in combination with a void ratio-dependent permeability function, developed by Mahmoodzadeh et al. (2014), calibrated to Rowe cell tests performed on kaolin clay. Free drainage was allowed at the mudline but precluded where the soil was in contact with the probe. This was achieved by prescribing hydrostatic conditions (pore pressure relative to the vertical location of each node on the free surface) at all freely draining surface boundary nodes. The PPP was modelled as a rigid body with a smooth interface to represent the polished metal surface of the centrifuge model.

The penetration process was modelled fast enough for drainage to be negligible, with dimensionless velocity V (= vD/c_v) equal to 100 at the invert of the device at the start of the penetration process. Additionally, a minimum time increment was enforced to avoid spurious

non-physical oscillations in the pore pressure fields (Vermeer & Verruijt, 1981), following the guidance given in the ABAQUS user manual (Dassault Systèmes, 2011).

The numerical procedures were initially checked and benchmarked against existing solutions published by Chatterjee et al. (2014) and Stanier & White (2014). Additionally, the validity of the modelling assumptions (mesh density, penetration speed, surface drainage assumption and permeability function) was assessed via sensitivity analyses that are summarised in the Appendix.

COMPARISON OF RESULTS: CENTRIFUGE VS. LDFE

For the following comparisons all units are given in prototype scale using the applicable scaling laws according to Garnier et al. (2007). For the numerical back-analyses a probe diameter of 0.5 m was modelled (prototype scale). All penetration phases simulated a target penetration depth of either $0.5D$ or $1D$. Only the load-controlled (LC) dissipation phases that followed were modelled, since these tests are more representative of the anticipated field use of the device (i.e. dissipation under the self-weight of the device). The simulation parameters and in-situ stress state are summarised in Table 2.

Table 2: Modified Cam Clay simulation parameters (after Stewart, 1992)

Parameter	Value
Critical state constant, M	0.92
Void ratio on CSL (at p' = 1 kPa), e_{cs}	2.14
Slope of normal consolidation line, λ	0.205
Slope of swelling line, κ	0.044
Poisson's ratio, υ	0.3
Effective unit weight, γ' (kN/m^3)	6
Unit weight of water, γ_w (kN/m^3)	10
Modelled in-situ stress state	Value
Over-consolidation ratio, OCR	3

For simplicity in back-analysing the centrifuge experiments, isotropic permeability ($k_h = k_v$) was assumed. The influence of potential anisotropic permeability is discussed later in the paper. A small surcharge of 0.25 kPa was applied at the mudline to improve numerical stability and create a non-zero strength intercept at the soil surface, $s_{u,m}$ consistent with the centrifuge sample, which had been lightly scraped to flatten the sample surface prior to testing.

Sample properties

Figure 3 shows the measured effective unit weight and undrained shear strength profiles of the centrifuge soil sample. Undrained strength measurements are presented with and without shallow depth corrections (White et al., 2010), which in this case have minimal influence on the interpretation due to the lightly over-consolidated state of the sample. A T-bar factor of 10.5 was adopted, corresponding to an intermediate T-bar roughness (Randolph & Houlsby, 1984). The MCC model formulation inbuilt in ABAQUS has a circular yield surface and plastic potential in the π-plane. The corresponding undrained strength profile in the numerical simulations, which as shown in Figure 3b, is in close agreement with the measured strength in the centrifuge sample, was derived from (Wood, 1990):

$$s_u = \frac{M}{2}\left(\frac{n_p}{r}\right)^\Lambda \frac{\left(1+2K_{0,oc}\right)}{3}\sigma_v' \qquad n_p = \frac{\left(1+2K_{0,nc}\right)}{\left(1+2K_{0,oc}\right)}OCR \qquad r = exp\left(\frac{M-\eta}{M}\right)$$

(1)

$$K_{0,nc} = 1 - \sin\varphi' \qquad K_{0,oc} = K_{0,nc}OCR^{(\sin\varphi')}$$

with the parameters η and Λ defined as q/p' and $(\lambda-\kappa)/\lambda$, respectively.

Penetration stage

The total vertical resistance V_{tot} during PPP penetration is the sum of the geotechnical resistance of the soil V_{geot} and the soil buoyancy $V_b \left(= f_b \gamma' v_{sub} \right)$ where f_b is an adjustment factor and v_{sub} the embedded volume. The bearing capacity equation, rearranged in terms of the bearing capacity factor or normalised penetration resistance $N_{c,nom}$, is therefore:

$$N_{c,nom} = \left(\frac{V_{geot}}{A_{nom}\, s_{u0}} \right) = \left(\frac{V_{tot}}{A_{nom}\, s_{u0}} \right) - f_b \left(\frac{\gamma'\, v_{sub}}{A_{nom}\, s_{u0}} \right) \quad with \quad A_{nom} = \frac{\pi D^2}{4} \tag{2}$$

The initial undrained shear strength at the corresponding invert depth is represented by s_{u0} and can be calculated using Equation 1. The contribution of soil buoyancy in excess of Archimedes' principle, caused by the generation of soil heave, is accounted for by the factor f_b. Stanier & White (2014) determined that the f_b factor for a hemiball penetrometer, which has exactly the same geometry as the parkable piezoprobe, could be adequately captured by

$$f_{b,PPP} \cong f_{b,hemi} = 1.19 + 0.06 \left(k_{su} D / s_{u,avg} \right) \quad with \quad s_{u,avg} = s_{u,m} + 0.5 k_{su} D \tag{3}$$

where $s_{u,m}$ represents the soil strength at the mudline, k_{su} the strength gradient with depth and D the probe diameter. For a given embedment depth, w, the embedded volume v_{sub} of the device (below the original soil surface) can be determined by

$$v_{sub} = \frac{\pi w^2}{3} (1.5D - w) \quad for \quad w \le 0.5D$$

$$v_{sub} = \frac{\pi D^3}{12} + \frac{\pi D^2}{8} (2w - D) \quad for \quad 0.5D < w \le D \tag{4}$$

The linear shear strength profile (Figure 3b) is used to estimate the penetration resistance for the PPP through: (i) direct numerical modelling of the experiments and via (ii) a prediction of the undrained penetration resistance using the model for undrained hemiball penetration resistance based on the equations above and the functions for $N_{c,nom}$ given by Stanier & White

(2014). Figure 4 compares the numerical simulations, centrifuge measurements and calculation model given above. All four centrifuge tests are in relatively close agreement with each other, showing excellent test repeatability and lateral homogeneity of the centrifuge sample. There is also very good agreement between the experimental results and the numerical simulations. The bearing capacity model after Stanier & White (2014), which was originally derived from parametric large deformation FE-analyses based on the Tresca model, provides upper and lower bounds that fall on either side of the MCC simulation. The normalised resistance of the smooth Tresca simulation based model fit is ~15% less than the MCC simulations. This discrepancy is not unexpected and is partly due to the different yield surface shapes assumed by the two models (MCC: circular vs. Tresca: hexagonal). The difference is close to the maximum deviation theoretically possible between the two models ($2/\sqrt{3} \sim 15.5\%$ if plane strain shear conditions are prevalent) and may therefore also be a consequence of slight drainage during the penetration phase. Similar observations were made by Mahmoodzadeh et al. (2015) where coupled MCC penetrometer analyses yielded between 9 and 12% higher penetration resistance compared to equivalent Tresca simulations.

The simulations illustrate that the prediction model of Stanier & White (2014) is adequate to either: (i) deduce an undrained strength profile at shallow depth if the vertical soil resistance is measured (as in this instance), (ii) deduce a spot measurement of undrained strength if the penetration depth and self-weight of a PPP are known; or to (iii) estimate the self-weight requirements of the PPP for different anticipated soil conditions.

Dissipation stage

A challenge associated with developing a simple interpretation method from numerical simulations using the Modified Cam Clay soil model, is to calculate an appropriate value for the consolidation coefficient with which to normalise the simulated dissipation response. This is a necessary step in order to determine the non-dimensional time required for 50%

dissipation to occur (T_{50}) for general application of the interpretation method. The choice is a compromise, as in reality, dissipation is a highly non-linear process with spatial and temporal variations in stiffness, so a representative value for c_v is required, and must be selected carefully. Depending on the current soil state (e.g. lightly over-consolidated or normally consolidated conditions) the operational stiffness can change during the course of the dissipation stage (i.e. transitioning between the reloading and normal compression lines). The initial coefficient of consolidation c_{v0} is defined conventionally (e.g. Chatterjee et al. (2014); Chatterjee et al. (2013)) as a function of the slope of the normal compression line, λ. The implications of this assumption will be revisited later in the paper.

The initial coefficient of consolidation c_{v0} at the invert depth, corresponding to the start of the dissipation phase, may be estimated as

$$c_{v0} = \frac{k_0}{m_v \gamma_w} = \frac{k_0 \left(1 + e_0\right) p_0'}{\lambda \gamma_w} \tag{5}$$

The parameter is defined as a function of the initial permeability k_0, void ratio e_0 and mean effective stress p'_0 at the same embedment. Figure 5 presents dimensional and non-dimensional interpretations of the centrifuge measurements alongside their numerical simulations for a normalised embedment of $w/D = 0.5$ and $w/D = 1$. The centrifuge measurements are shown with and without the correction suggested by Sully et al. (1999), where back-extrapolation is used to estimate the initial excess pore pressure at the start of dissipation (the so-called root-time method). This correction, which was originally suggested for non-monotonic dissipation measurements, is necessary to account for lag in the measured pore pressure response and to ensure that an appropriate initial excess pore pressure is used in the following normalisation. The excess pore pressure, $\Delta u(t)$, is normalised by its initial value, Δu_i, at the onset of the dissipation stage, whilst the normalised time, T, is expressed as a function of the dissipation time t as:

$$T = \frac{c_{v0}\, t}{D^2} \tag{6}$$

The normalised dissipation responses are of similar shape for both the numerical LDFE-simulations and the centrifuge tests. In this interpretation the non-dimensional dissipation curves extracted from the numerical simulations at the invert and midface locations are normalised by the same value of c_{v0}, taken at the invert depth. Therefore, the coefficient of consolidation, c_{v0}, derived by matching the experimental and numerical dissipation curves (varying the c_{v0} value used to normalise the experimental measurements), should be very similar for both the midface and invert locations.

Table 3: Summary of c_{v0} and T_{50} from experiments and simulations

w/D	c_{v0} (m^2/yr)		T_{50} (-)	
	inferred c_{v0} (back-fitting to LDFE)	simulated c_{v0} (Equation 5)	invert	midface
0.5	0.6	0.6	0.005	0.007
1.0	2.4	0.67	0.009	0.010

Table 3 compares the inferred coefficients of consolidation with the simulated values. Additionally, the normalised times T_{50} required to dissipate 50% of the accumulated excess pore pressures, are presented in the table. For an embedment depth of 0.5D, the dissipation response is well-predicted by the LDFE-simulation for both the invert and midface locations. As a consequence, excellent agreement between the inferred (back-fitted by varying the value of c_{v0} used in the normalisation until the experimental and numerical curves aligned) and the simulated c_{v0} values is also achieved in non-dimensional terms. For an embedment depth of 1D and the input model parameters adopted, the experimentally measured dissipation is significantly faster than that simulated. The back-fitted coefficient of consolidation is consequently higher than the value prescribed in the numerical simulations.

There are a number of potential causes for this disparity. For example, there is some suggestion in the literature that the horizontal permeability, k_h, of kaolin clay is greater than the vertical permeability, k_v, by a factor of 2-3 (Al-Tabbaa & Wood, 1987). Under the assumption that radial dissipation dominates and is therefore mostly controlled by the horizontal permeability, the back-calculated coefficient of consolidation, c_{v0}, could increase by a factor of about $n_k = k_h / k_v \sim 3$.

The magnitude of this discrepancy when comparing the LDFE and centrifuge results at the two embedment depths prompted a further parametric study varying the parameters that control the consolidation coefficient to systematically identify the most likely source. This study provides a better basis to interpret PPP dissipations in a given soil sample, beyond a single estimate of c_{v0}.

PARAMETRIC STUDY AND INTERPRETATION MODEL

Procedure and assumptions

The parametric study examines the effect of permeability anisotropy, over-consolidation ratio and also changes in the elastic stiffness. The operative coefficient of consolidation, c_{h0}, is explored by varying these parameters systematically. The results are interpreted by adjusting the previously-defined coefficient of consolidation, c_{v0}, by factors f_k, and f_{st} which account for the effect of anisotropic permeability and the operative stiffness, respectively, resulting in:

$$c_{h0} = f_k \, f_{st} \, c_{v0} \qquad with \qquad c_{v0} = \frac{k_v \left(1 + e_0\right) p_0^{'}}{\lambda \, \gamma_w} \tag{7}$$

The c_{v0} value adopted in the previous section corresponds to a value measured in an oedometer or conventional Rowe cell test, where vertical pore water flow typically dominates. For soils with anisotropic permeability, the isotropic permeability, k_0, in Equation 5, is replaced by the vertical permeability, k_v, in the definition of c_{v0}. A dimensionless time, T^*, is then defined in

terms of the operative coefficient of consolidation, c_{h0}, and two further influence factors, f_{RI} and f_w, which account for the influence of the rigidity index and the embedment depth, to give:

$$T^* = f_{RI} \, f_w \, \frac{c_{h0} \, t}{D^2} \tag{8}$$

Suitable functions to generate these factors have been derived from the LDFE-simulations summarised in Table 4. The rigidity index in the MCC Model was adjusted by varying the Poisson's ratio.

Table 4: Summary of scope of parametric analyses (**bold text: baseline case**)

Parameter	Value	Target Sensitivity	Target Factor
Poisson's ratio, υ	0.25 / **0.30** / 0.35	Rigidity index I_R	f_{RI}
Permeability ratio, $n_k = k_h / k_v$	**1** / 2 / 3	Anisotropy: $k_h > k_v$	f_k
Slope of normal consolidation line, λ	0.110 / **0.205** / 0.352	Ratio of κ/λ *	f_{st}
Slope of swelling line, κ	**0.044** / 0.062 / 0.082	Ratio of κ/λ *	f_{st}
Over-consolidation ratio, *OCR*	**1** / 1.5 / 2 / 3 / 4 / 5	Effect of *OCR*	f_{st}
Normalised embedment depth, *w/D*	0.3 / 0.4 / **0.5** … 1	Effect of embedment	f_w

* The λ and κ values selected lead to ratios of $\kappa/\lambda = 0.125, 0.215, 0.3, 0.40$.

For each simulation one parameter was varied from the baseline case (values given in bold in Table 4) to assess its influence on the non-dimensional dissipation response. For all parameter combinations (14 in total) an initial undrained penetration to a depth of 1*D* was simulated (at a dimensionless penetration rate, $V = 100$). A smooth probe with a diameter of 0.25 m was considered following Chatterjee et al. (2014). An effective unit weight of 5 kN/m³ was adopted for the soil and a constant vertical permeability of $k_v = 10^{-9}$ m/s was assumed for all cases. To improve numerical stability and generate a small strength intercept at the soil surface a surcharge of 1 kPa was introduced at the mudline (following Chatterjee et al., 2014). All other parameters remain as in the previous section (see Table 2).

Consolidation phases corresponding to normalised embedment depths of $w/D = 0.3$, 0.4, 0.5 ... 1 were analysed. Depths less than $0.3D$ were not modelled as this is approximately the minimum depth required for both the midface and invert pore pressure measurement locations to be sufficiently embedded to achieve reliable dissipation measurements for the current configuration of device. Figures that illustrate the influence of the parameters and the effectiveness of the proposed factors in collapsing all dissipation responses to a single curve are given in the following sections. For brevity, only dissipation at the invert location for an embedment of $0.5D$ is shown, however the midface performance and the responses at all other embedment depths were very similar.

Effect of rigidity index

To investigate the influence of the rigidity index $I_R = G/s_u$ on the dissipation solution, LDFE-calculations assuming different values of Poisson's ratio were conducted. The rigidity index is estimated based on the initial undrained shear strength s_{u0} and shear modulus G_0 at the invert level of the probe. The initial shear stiffness G_0 can be calculated as:

$$G_0 = \frac{3\,p'_0\left(1+e_0\right)\left(1-2v\right)}{2\,\kappa\left(1+v\right)} \qquad (9)$$

Poisson's ratios of 0.25, 0.30 and 0.35 correspond to rigidity indexes of 130, 100 and 72, respectively. For the cone and ball penetrometers a function for the influence factor due to changes in rigidity index, referred to as f_{RI} here, is typically defined as (Teh & Houlsby, 1991):

$$f_{RI} = \frac{1}{\left(I_R\right)^{\beta}} \qquad (10)$$

The numerical simulations with rigidity indexes varying in the range of 72-130 indicated that the appropriate value for β for the PPP was objectively defined via best fitting as 0.001. This

results in an insignificant influence factor f_{RI} of effectively unity. In other words, the rigidity index has practically no influence on the dissipation response of the PPP due to the lack of confinement at shallow embedment; therefore the influence factor f_{RI} can be discarded. This is in contrast to cone and ball penetrometers, where values of 0.5 (Mahmoodzadeh et al., 2014) and 0.25 (Mahmoodzadeh et al., 2015) apply, respectively.

Effect of permeability anisotropy

The permeability ratio n_k was varied to evaluate the effect of anisotropic flow conditions. A function for the influence factor f_k is defined as follows:

$$f_k = \frac{2n_k + 1}{3} \tag{11}$$

Figure 6 illustrates that this function collapses all responses to a unique curve, which means that the operative permeability is essentially the geometric mean of the permeability components in three dimensions. An expression, yielding similar f_k factors, was found by Wang et al. (2015) for the piezoball, with the slight deviation mainly due to the difference in device geometry and embedment conditions.

Effect of operative stiffness for normally-consolidated conditions

The influence of the operative stiffness was examined by changing the value of λ or κ. The dissipation response normalized by c_{v0} varies with the ratio of κ/λ, and this is confirmed in Figure 7a, where two different parameter combinations – both with a ratio of κ/λ of 0.4 – lead to the same dissipation response. For normally consolidated clay the influence factor, f_{st}, can

be defined as follows (Mahmoodzadeh et al., 2014 & 2015), where α controls the influence of the stiffness ratio, κ/λ:

$$f_{st} = \left(\frac{\lambda}{\kappa}\right)^{\alpha} \tag{12}$$

A value of $\alpha \sim 0.25$ collapses all of the dissipation responses for normally consolidated soil, where the slope of the normal compression line dominates the operative stiffness, as shown in Figure 7b. Numerical analyses of piezocone dissipation tests by Mahmoodzadeh et al. (2014) revealed the same for the cone, namely that the stress-paths observed in the vicinity of the cone are partially influenced by the reloading stiffness, even for normally consolidated conditions. The responses for κ/λ of 0.3 and 0.4 were almost indistinguishable, hence for clarity, the dissipation response for the κ/λ equal to 0.3 case is omitted in Figure 7a.

Effect of over-consolidation ratio

To calibrate the sensitivity of the dissipation response to lightly over-consolidated conditions, additional LDFE-simulations were run with constant *OCR* in the range of 1 to 5.

Figure 8a illustrates the sensitivity of the dissipation response to these lightly over-consolidated conditions. The dissipation responses can be collapsed to a unique curve as shown in

Figure 8b by modifying the stiffness factor for normally consolidated conditions, f_{st}, by: (i) applying a factor OCR^{Λ} to account for the difference in mean stress caused by over-consolidation (Mahmoodzadeh et al., 2014); and (ii) varying the weighting factor α in Equation 12, as a function of the *OCR*. The factor f_{st} becomes

$$f_{st} = \left(\frac{\lambda}{\kappa}\right)^{\alpha} OCR^{\Lambda} \qquad with \qquad \Lambda = \frac{\lambda - \kappa}{\lambda} \tag{13}$$

A suitable relationship for α was determined via back-fitting to the optimal values for each simulation (see Figure 9), resulting in

$$\alpha = a \cdot e^{(b/OCR)} \qquad with \qquad a = 0.647 \ \& \ b = -0.913 \tag{14}$$

This expression retains $\alpha = 0.25$ at $OCR = 1$ as determined previously. The change in α from ~0.25 for normally consolidated conditions to ~0.55 for an OCR equal to 6 (where Equation 14 is approaching an asymptotic state) reflects that the reloading stiffness κ increasingly dominates the dissipation response as the soil becomes more over-consolidated.

Influence of embedment depth

Finally, all dissipation responses for embedment depths in the range of 0.3 to $1D$ can also be collapsed to a unique curve by applying a scaling factor that varies with embedment. This is useful for assessing the uncertainty in consolidation coefficient that would exist if the embedment of the PPP was not known.

For each analysis the fitting parameters $T_{50}*$ and $m*$, which describe the dissipation solution according to Equation 15, were back-fitted for all cases simulated, after accounting for the influence factors f_k, f_{st}, and f_{OCR}.

$$\frac{\Delta u}{\Delta u_i} = \frac{1}{1 + (T/T_{50})^m} \tag{15}$$

The data points (finite element simulation increments) that make up the numerical dissipation responses generally had non-uniform time intervals. Consequently each data point was weighted in the back-fitting process so that its influence on the fitting process was proportional to the time interval that it represented. Figure 10 shows the dependency of the back-fitted parameters $T_{50}*$ and $m*$ on the normalised penetration depth w/D for the invert location. Using the estimated average values of T_{50}^* a suitable relationship for the influence

factor f_w was established, collapsing all of the dissipation responses to a unique curve equal to that for an embedment of 0.5D, given by:

$$f_w = \frac{\overline{T_{50}^*}\left(w/D = 0.5\right)}{\overline{T_{50}^*}\left(w/D\right)} \quad \leftrightarrow \quad f_w = a\left(w/D\right)^b \quad with \quad a = 0.65 \ \& \ b = -0.67 \tag{16}$$

Figure 11 shows the fit of Equation 16 versus the optimally back-fitted values for w/D in the range of 0.3 to 1. For simplicity a single relationship for f_w is recommended, which is valid for both the invert and the midface pore pressure sensor locations, with minimal error.

The operative coefficient of consolidation c_{h0} can be determined with reasonable accuracy even if the exact embedment depth of the probe is unknown (i.e. the embedment is not measured). In this event an f_w factor of 1 – corresponding to a normalised embedment, w/D, of 0.5 – can be assumed, resulting in a maximal deviation from the optimal value of ~50% for an actual embedment of 0.3D or ~35% for an embedment of 1D, assuming the probe embedment is within this range.

Proposed interpretation model

Using the influence factor relationships developed in the preceding sections, unique dissipation curves for the invert and midface locations can be determined for a normalised embedment, w/D, of 0.5, which can then be used to back-analyse any field dissipation tests with reasonable accuracy. Values for T_{50}^* and m^* are given in Table 5 for general use for both the midface and invert pore pressure sensor locations.

Table 5: Dissipation solution fitting parameters for the proposed interpretation model.

Location	T_{50}^* (-)	m^* (-)
Invert	0.035	1.05
Midface	0.041	1.05

Field data from parkable piezoprobe dissipation tests can be interpreted with the following simple procedure:

1. Evaluate f_w (Equation 16) if embedment was measured; otherwise assume an influence factor f_w of 1.

2. Normalise the dissipation data according to Equations 8 (note: $f_{RI} = 1$) and fit the resulting data to the curve described by Equation 15 (using the appropriate parameters from Table 5) by varying the operative coefficient of consolidation, c_{h0}, used in the normalisation.

3. Optional: Estimate the sensitivity of the oedometric coefficient of consolidation, c_{v0}, using Equations 7, 11, 13 and 14 and an expected potential range for the various unknown soil parameters.

Verification of interpretation model

The interpretation model was verified by performing additional LDFE simulations for randomly selected embedment depths and parameter combinations not used in the development of the interpretation model, but within the bounds of the parametric study presented in the previous section. In Figure 12 the operative coefficient of consolidation, c_{h0}, inferred from the interpretation model is plotted against the expected value determined from Equation 7 for fifteen validation cases. The interpretation model proves to be accurate and robust for all cases studied with errors generally within ±10%.

EXAMPLE APPLICATION

The proposed interpretation model was next used to reinterpret the centrifuge test results, following the steps developed in the previous section:

1. Appropriate values of the embedment influence factor, f_w, were taken for the embedment depths of 0.5D and 1D.

2. The measured dissipation data was then normalised according to Equation 8, (taking $f_{RI} = 1$). Equation 15 was used to generate a model fit (using the appropriate best estimate parameters for the test data as summarised in Table 5) to which the measured dissipation was back-fitted by adjusting the operative coefficient of consolidation, c_{h0}. This procedure yielded best estimate values of c_{h0} of 3.1 m²/yr and 14 m²/yr for embedment depths of 0.5D and 1D, respectively

3. The sensitivity of the oedometric coefficient of consolidation, c_{v0}, was estimated over an expected potential range for the various unknown soil parameters via a Monte Carlo analysis using the parameters outlined in Table 6.

Table 6: Soil parameter inputs to Monte Carlo analysis.

Input parameter	Lower bound	Mean value, μ	Upper bound	Distribution
κ/λ	0.125	0.215	0.4	*
n_k	1	2	3	uniform
OCR	N/A	3	N/A	N/A

* Normal distributions for λ and κ, with $\mu_\lambda = 0.205$ and $\mu_\kappa = 0.044$ (after Stewart, 1992) and corresponding standard deviations σ_λ and σ_κ chosen so that ~99% of all resulting κ/λ-ratios fall within stated range

For comparison purposes the best estimate c_{h0} values derived from step 2, valid for an *OCR* of 3, were converted to values representative of normally consolidated conditions, using Equation 13 (λ and κ assumed according to Table 2). The estimated $c_{h0,nc}$ values are in good agreement with trends back-extrapolated from other published data for UWA kaolin clay under higher stress conditions (Figure 13). The interpretation of the operative coefficient of consolidation at the invert, c_{h0}, was consistent irrespective of the considered pore pressure sensor location (midface or invert), demonstrating that the interpretation model derived is internally consistent.

The estimated distributions of the oedometric c_{v0} values, derived via the Monte Carlo simulation conducted as part of step 3, are presented in Figure 14. The 5% and 95% percentiles, which are often used in design, are also indicated in the figure. This latter example serves as a demonstration of how the PPP interpretation method developed can be used to interpret dissipation data to estimate operative coefficients of consolidation, c_{h0}, and a potential range of equivalent oedometric coefficient of consolidation, c_{v0}, given approximate expected ranges of the governing soil parameters. The range of c_{v0} can be refined using other site investigation data as input as it becomes available.

CONCLUSIONS

The parkable piezoprobe is a promising tool for economically measuring the coefficient of consolidation offshore. This paper has presented results from centrifuge model tests and a comprehensive suite of large deformation finite element simulations investigating the performance of the parkable piezoprobe have been reported, leading to the following conclusions:

- All centrifuge measurements of the undrained penetration stage were in excellent agreement with the results of the numerical large deformation simulations. The experimentally recorded and numerically simulated dissipation responses were consistent with each other in both non-dimensional and dimensional terms.

- Back-analyses of the centrifuge tests revealed that the model of Stanier & White (2014) is adequate to define the effective weight of device required to achieve a penetration in the range of 0.3-1D for anticipated in-situ conditions.

- A simple interpretation model for inferring the operative coefficient of consolidation c_{h0} from field test data was developed from a series of LDFE analyses. In its simplest form – with no prior knowledge of soil properties or the initial embedment depth of the device – reasonably accurate estimates of the operative coefficient of

consolidation, c_{h0}, can be achieved. More accurate estimates can be achieved in the event that some of the soil parameters are measured independently.

- Due to the radial drainage of excess pore pressures around the device dissipation tests for the PPP ($D = 250$ mm) are about twice as fast as for the SMARTPIPE ($D = 225$ mm), where planar drainage dominates. Piggybacking these tests onto a site investigation survey would therefore provide an economical way to reliably gain near surface seabed properties.

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Schneider, M. A., Stanier, S. A., Chatterjee, S., White, D. J. and Randolph, M. F.

The parkable piezoprobe for determining c_v and strength - modelling and interpretation methods

NOTATION

A_{nom}	nominal area
a, b	fitting parameters
c_h	operative coefficient of consolidation
c_{h0}	initial operative coefficient of consolidation at invert level
$c_{h0,nc}$	initial c_{h0} at invert level (converted to normally consolidated conditions)
c_v	coefficient of consolidation
c_{v0}	initial coefficient of consolidation at invert level
D	device diameter
e_0	initial void ratio
e_{cs}	void ratio on critical state line at $p'=1$kPa
f_b	buoyancy factor
f_k	influence factor for anisotropic flow conditions
f_{ocr}	influence factor for over-consolidation ratio
f_{RI}	influence factor for rigidity index
f_{st}	influence factor for operative stiffness
f_w	influence factor for embedment depth
G	shear modulus
G_0	initial shear modulus
I_R	rigidity index
$K_{0,nc}$	earth pressure coefficient at rest (NC-soil)
$K_{0,oc}$	earth pressure coefficient at rest (OC-soil)
k_0	isotropic permeability
k_h	horizontal permeability component
k_{su}	undrained shear strength gradient
k_v	vertical permeability component
M	slope of critical state line in q-p' space
m, m^*	fitting parameter for consolidation solution
m_v	coefficient of volume compressibility
$N_{c,nom}$	nominal bearing capacity factor
N_T	bearing capacity factor for T-Bar
n_k	permeability ratio
n_p	isotropic over-consolidation ratio
OCR	over-consolidation ratio
p'	mean effective stress
p_0'	initial mean effective stress
q	deviator stress
r	ratio of pressures on normal compression and critical state line
s_u	undrained shear strength
s_{u0}	initial undrained shear strength
$s_{u,avg}$	average undrained shear strength
$s_{u,m}$	undrained shear strength at mudline
T	dimensionless time
T^*	adjusted dimensionless time
T_{50}	dimensionless time to reach 50% of dissipation
T^*_{50}	adjusted dimensionless time to reach 50% of dissipation

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The parkable piezoprobe for determining c_v and strength - modelling and interpretation methods

t	time
t_{50}	time to reach 50% of dissipation
V	dimensionless velocity
V_b	soil buoyancy
V_{geot}	geotechnical soil resistance
V_{tot}	total soil resistance
v_{sub}	submerged volume
w	embedment depth

α	exponent regarding stiffness contributions
β	exponent regarding influence of rigidity index
Δu	excess pore water pressure
Δu_i	initial excess pore water pressure
γ'	effective unit weight
γ_{sat}	saturated bulk unit weight
γ_w	unit weight of water
η	stress ratio q/p'
φ'	internal friction angle
κ	slope of swelling line
Λ	plastic compression ratio
λ	slope of normal consolidation line
v	Poisson ratio
σ_v'	effective vertical stress

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APPENDIX

The LDFE code developed to generate the simulations presented in this manuscript were first benchmarked against results published by Chatterjee et al. (2014) using the geometries and soil parameters outlined in that paper, before exploring the effects of finite element mesh density, penetration rate, surface drainage assumption and permeability function.

Figure 15 presents results from a simulation with a voids ratio dependent permeability function (after Mahmoodzadeh et al. 2014) and a simulation with a constant permeability ($k = $ 1e-9 m/s). There is a relatively small difference between the simulations for the normally consolidated conditions modelled in this benchmarking exercise, however, both are in close agreement with the result published by Chatterjee et al. (2014). This indicates that the LDFE code developed is robust and consistent with that used in previous work and that the difference in permeability distributions modelled (isotropic permeability vs. permeability derived from voids ratio) has minimal impact on the undrained penetration resistance.

Figure 16 presents results for two free surface pore pressure assumptions: that used in this study where the free surface pore pressure was elevation dependent and another where it was assumed to always be zero (as in Chatterjee et al. 2014). There is a small increase in penetration resistance for the case with elevation dependent surface pore pressure, which is due to local heave leading to a pressure differential that increases the drainage rate within the heaving material surrounding the penetrometer.

Figure 17 presents the results of the mesh sensitivity analysis. The coarse mesh gives a higher penetration resistance, whereas the mesh used in this study and the finer mesh show no discernible variation in response, therefore validating the use of the mesh used throughout the current study.

Figure 18 presents the results of simulations with varying non-dimensional penetration velocity ($V = vD/c_v$) over the range of 50-150 with 100 being the value used throughout this

study. There is a significant reduction in non-dimensional penetration resistance when V is increased from 50 to 100 (> 5%); however, in contrast, when V is increased further to 150 the reduction is far less significant (< 1%). This illustrates that a non-dimensional penetration velocity of 100 is sufficiently high to ensure minimal dissipation of excess pore pressures during penetration.

FIGURES

(a)

(b)
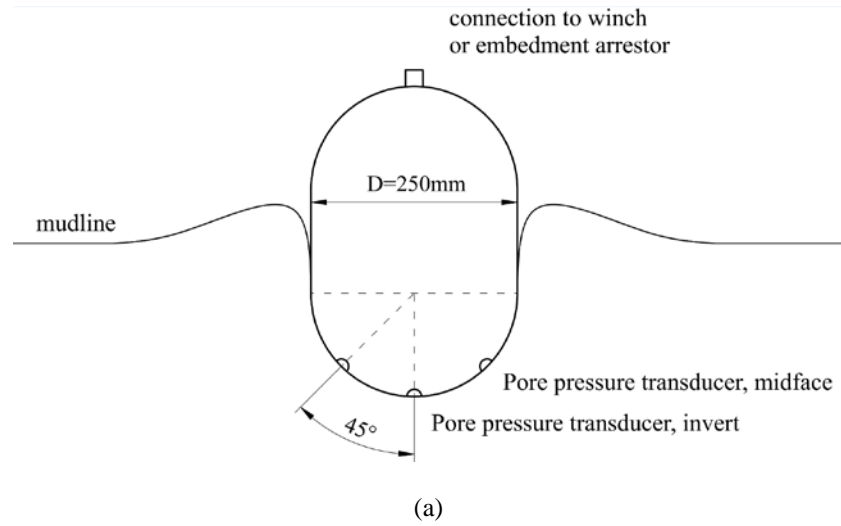
Figure 1: (a) Illustration of parkable piezoprobe; (b) and small-scale centrifuge model.
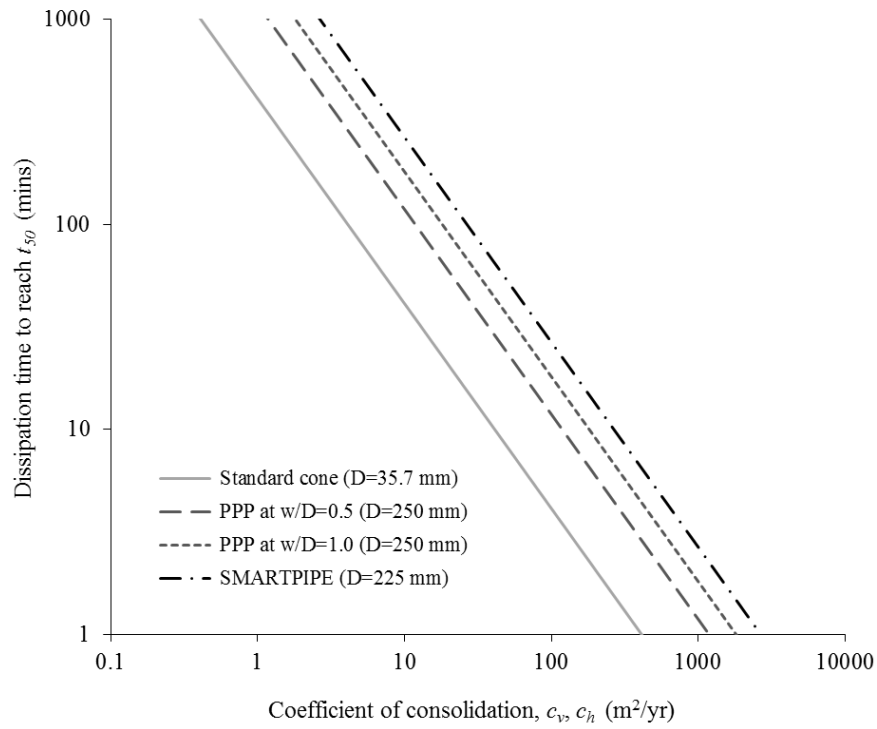
Figure 2: Dimensional time required for 50% of excess pore pressures to dissipate, t_{50}, for the PPP, cone penetrometer and SMARTPIPE.
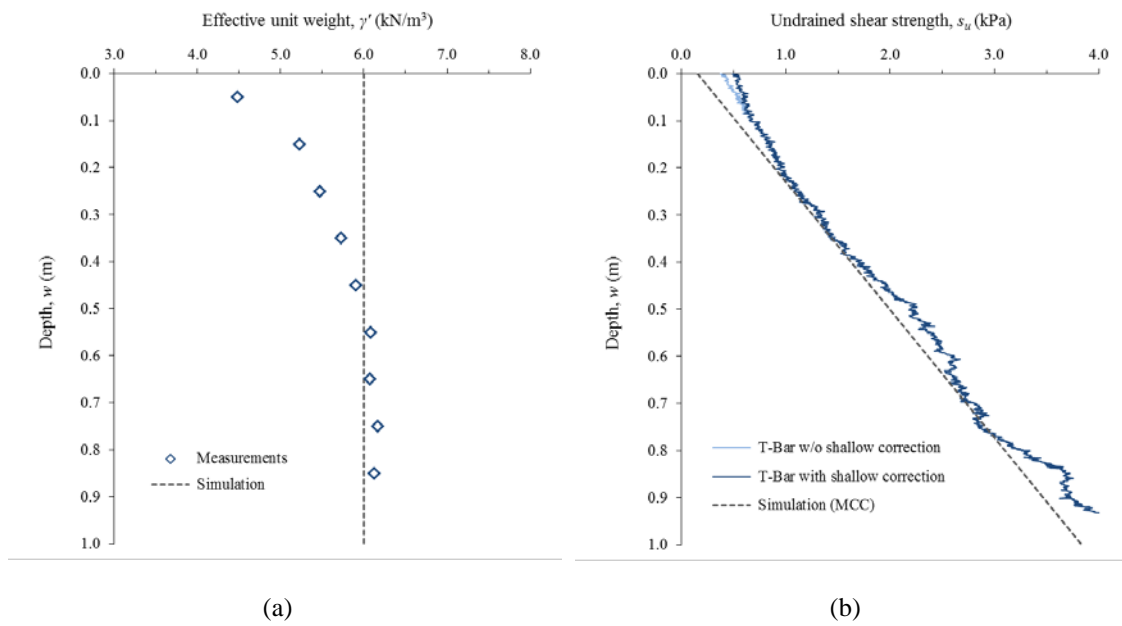
Figure 3: Soil properties measured vs. modelled: (a) effective unit weight; and (b) undrained shear strength.

(a)   (b)
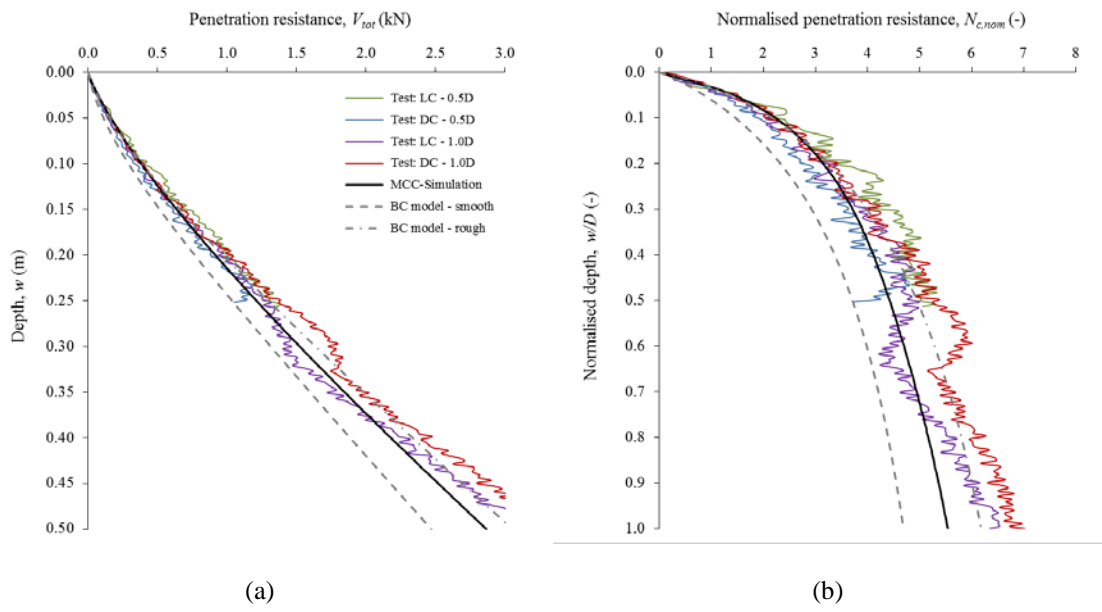
Figure 4: Comparison of experimental measurements and numerical simulation: (a) total penetration resistance vs. depth; and (b) normalised penetration resistance vs. normalised depth.

(a)

(b)

1
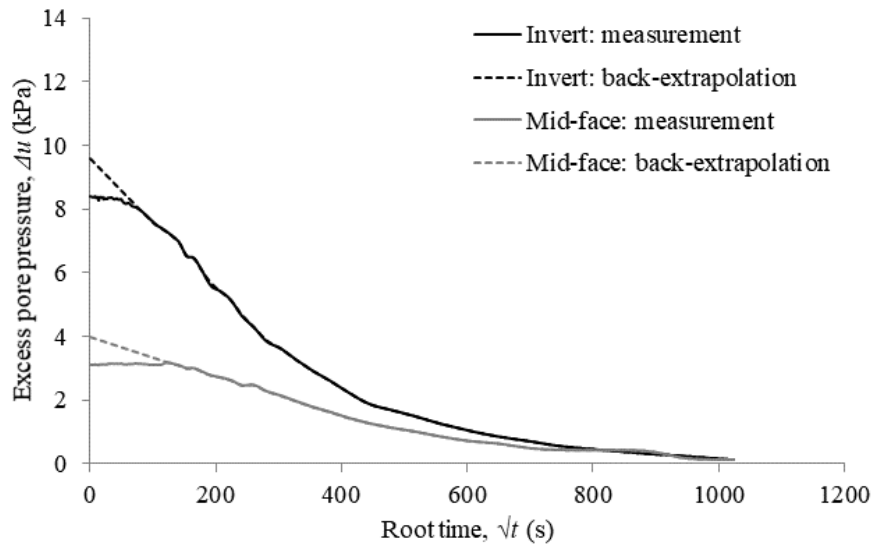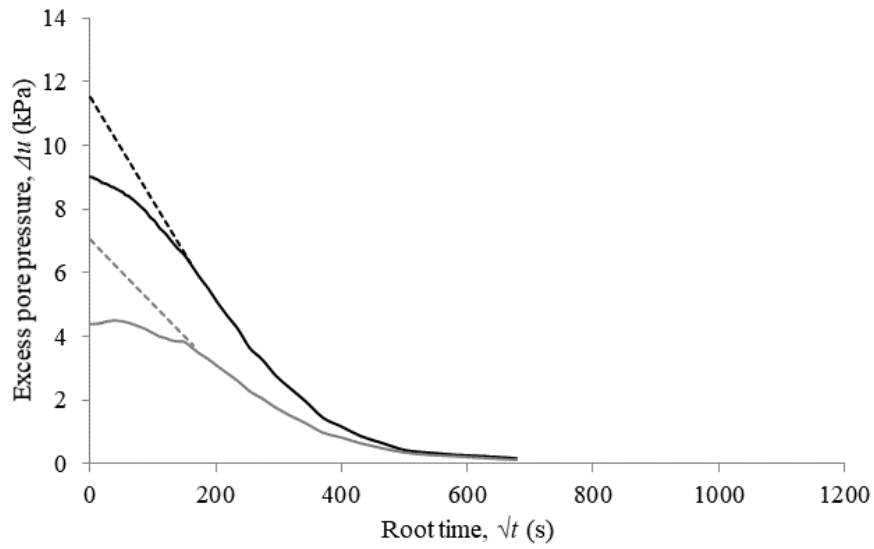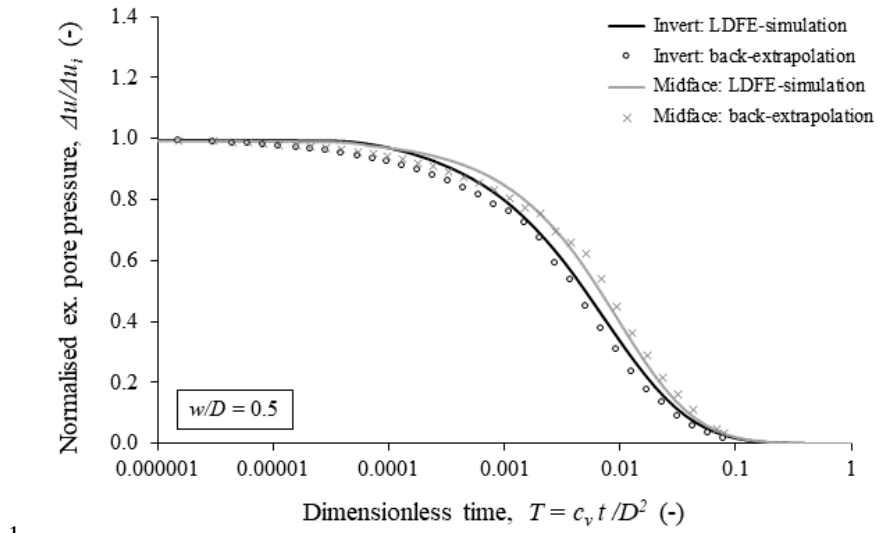
(c)
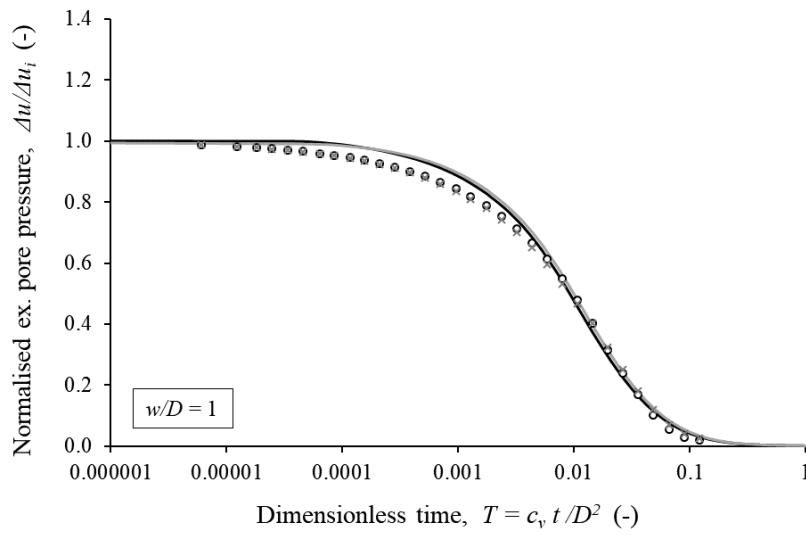
(d)

Figure 5: Experimental measurements with and without the Sully et al. (1999) correction compared to the numerical simulations: (a, b) dimensional response; and (c, d) non-dimensional response for *w/D* of 0.5 and 1, respectively.
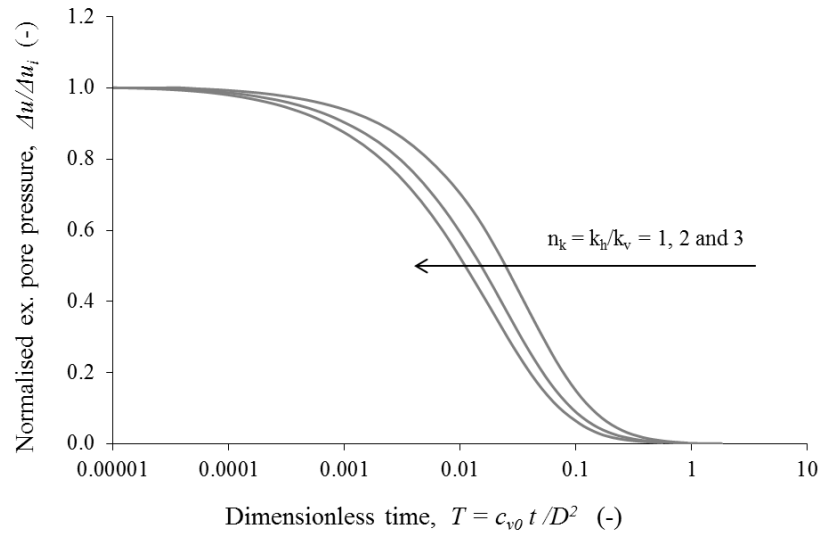
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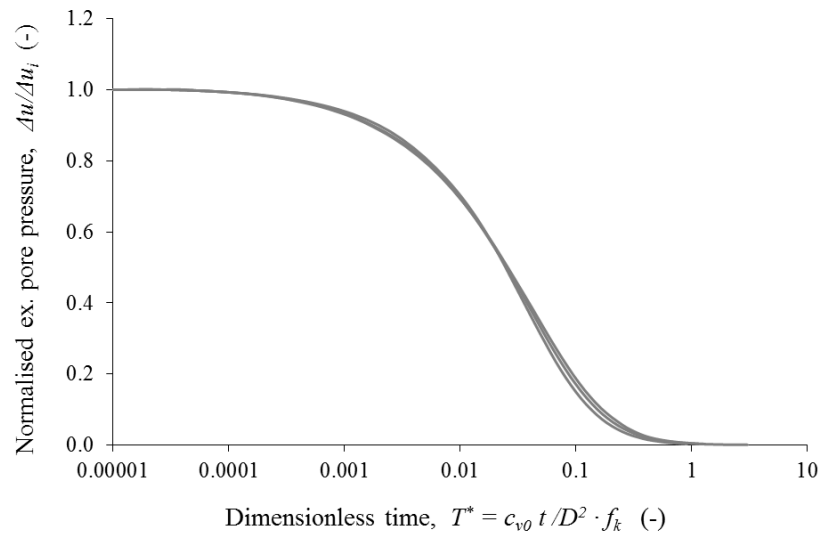
(b)

Figure 6: Effect of n_k on normalised dissipation response at $w/D = 0.5$: (a) conventional normalisation; and (b) proposed normalisation.
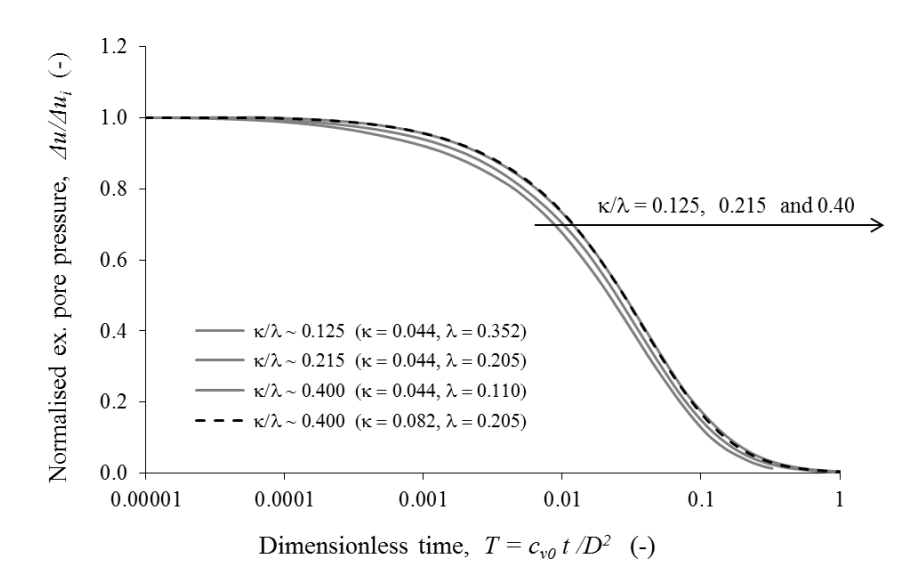
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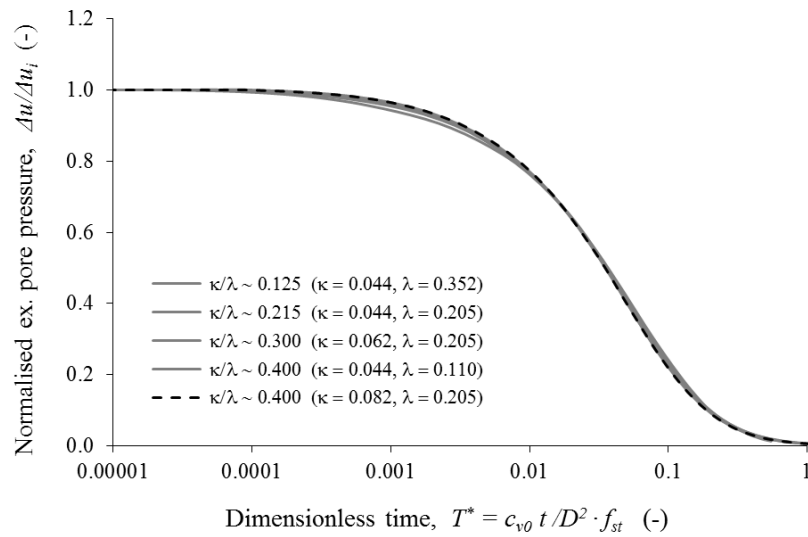
(b)

Figure 7: Effect of ratio κ/λ on normalised dissipation response at $w/D = 0.5$: (a) conventional normalisation; and (b) proposed normalisation.
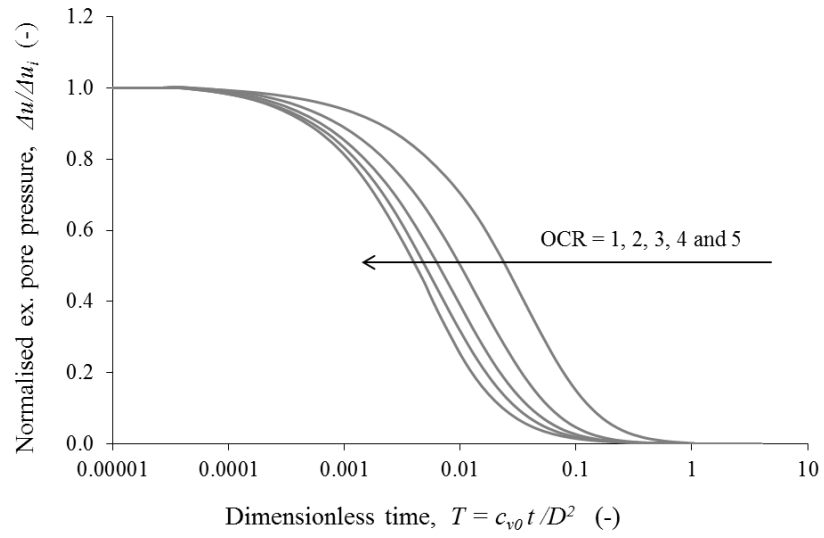
(a)
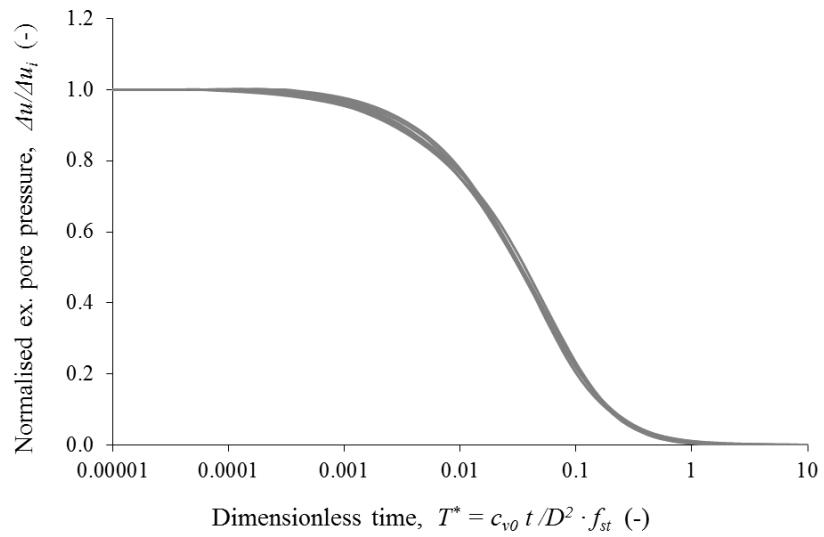
(b)

Figure 8: Effect of *OCR* on normalised dissipation response at *w/D* = 0.5: (a) conventional

normalisation; and (b) proposed normalisation.
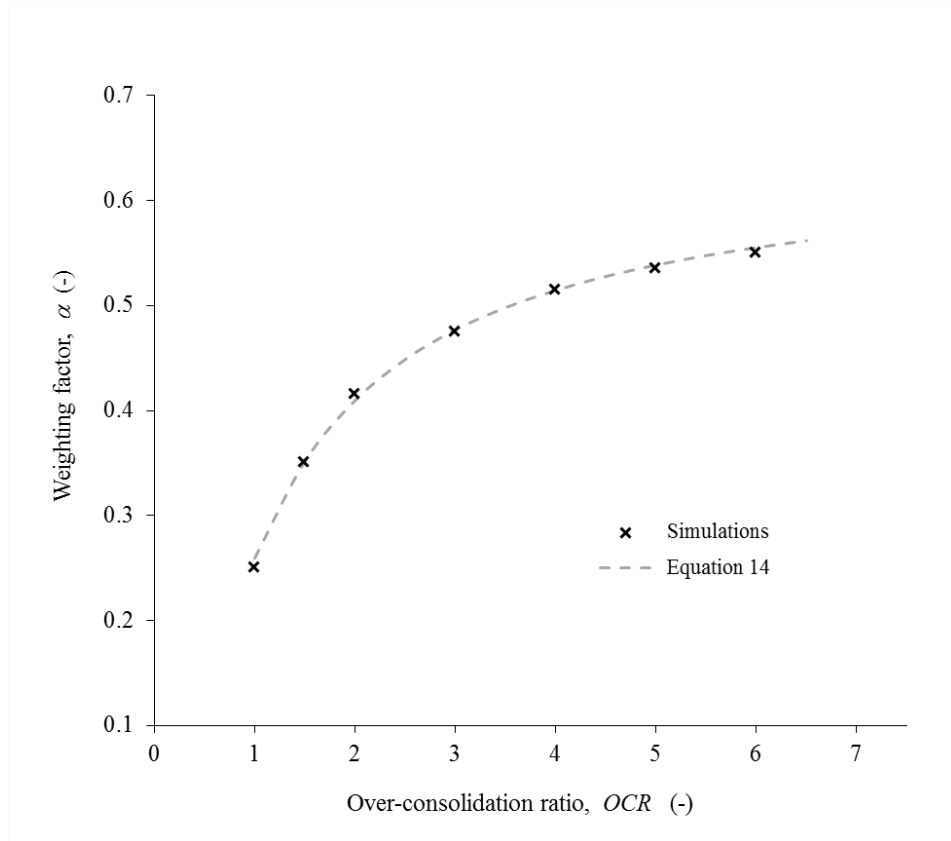
Figure 9: Definition of weighting factor as a function of *OCR*.

(a)   (b)
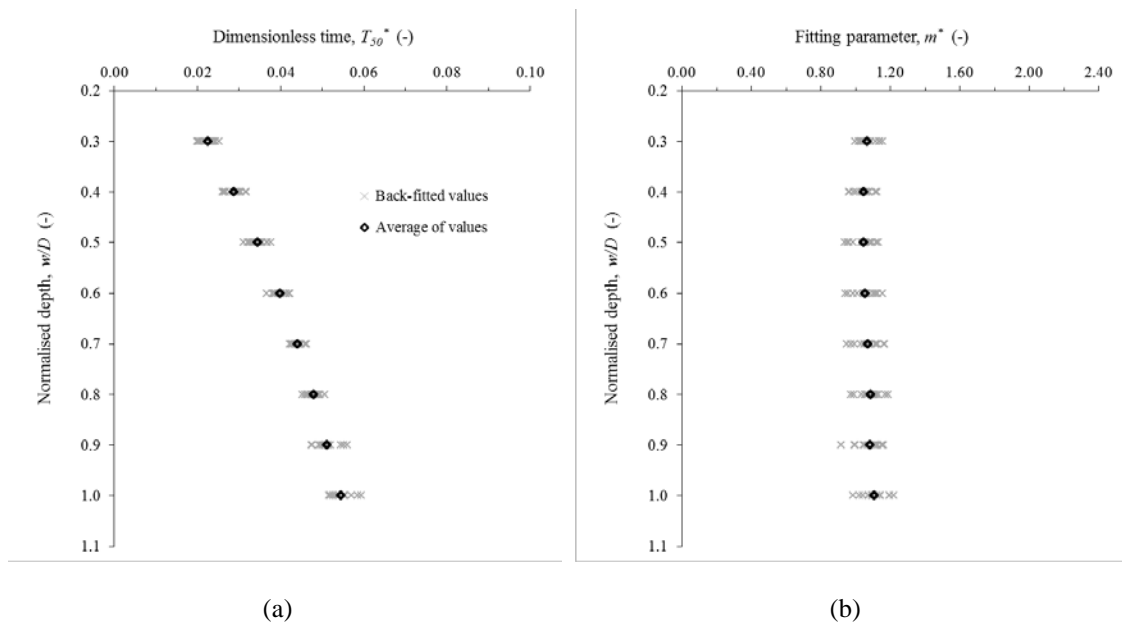
Figure 10: Dependency on embedment depth of back-fitted: (a) $T_{50}*$ and (b) *m** for invert position.
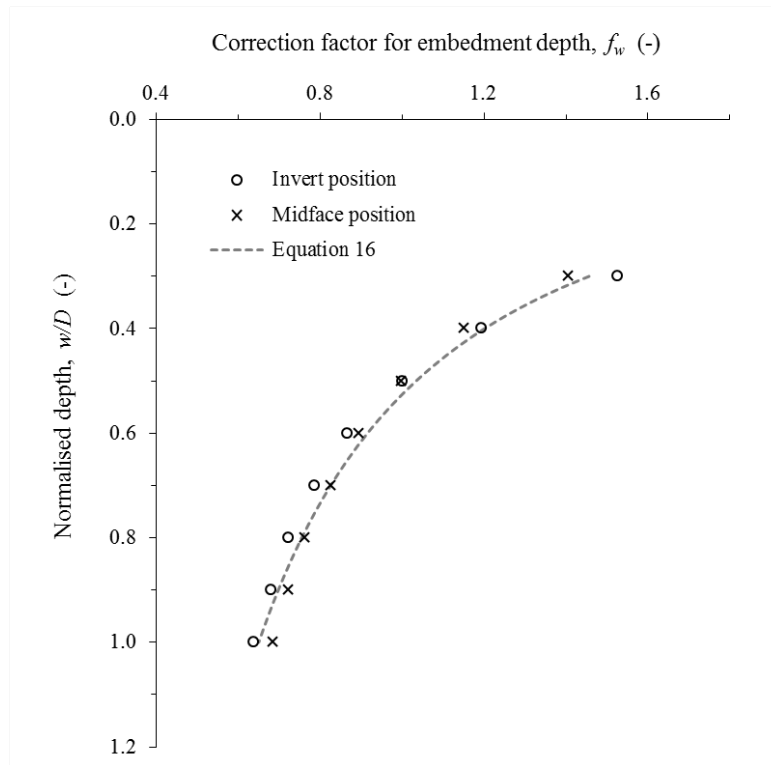
Figure 11: Definition of embedment influence factor for invert and midface location
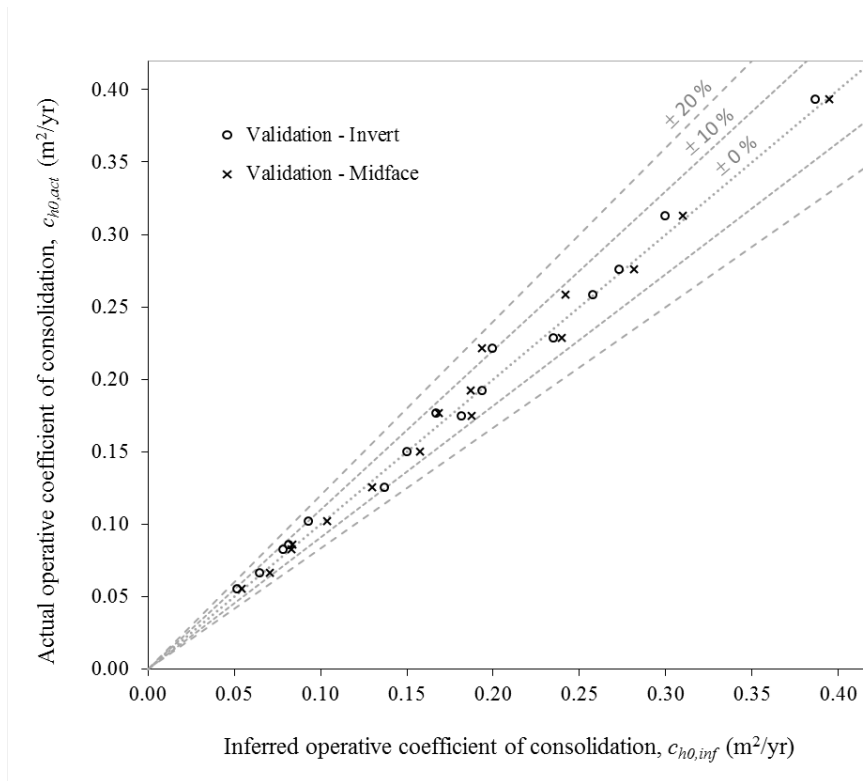
Figure 12: Performance and validation of proposed interpretation-model.
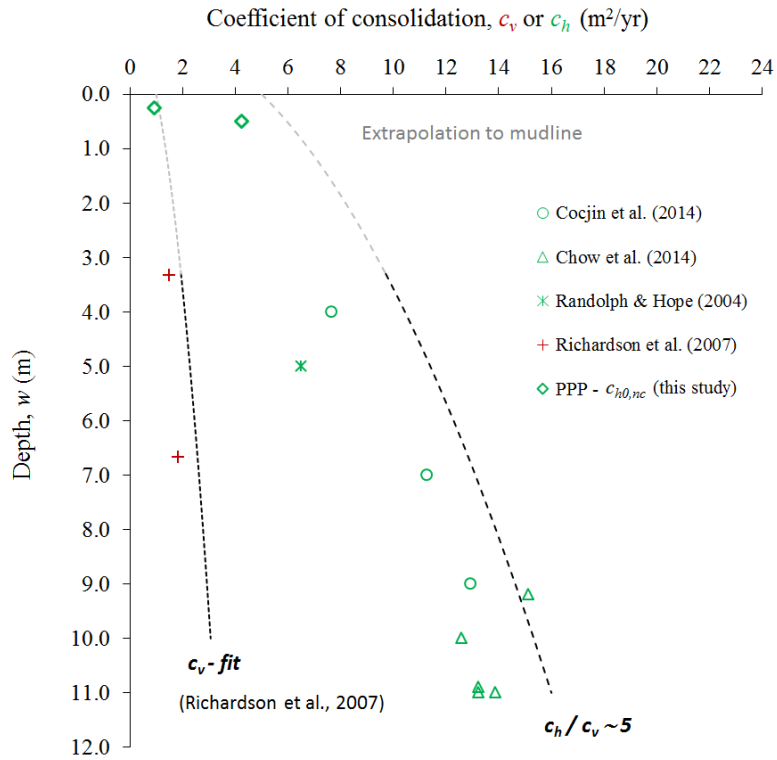
Figure 13: Inferred c_h -values of centrifuge experiments compared to values given in literature.
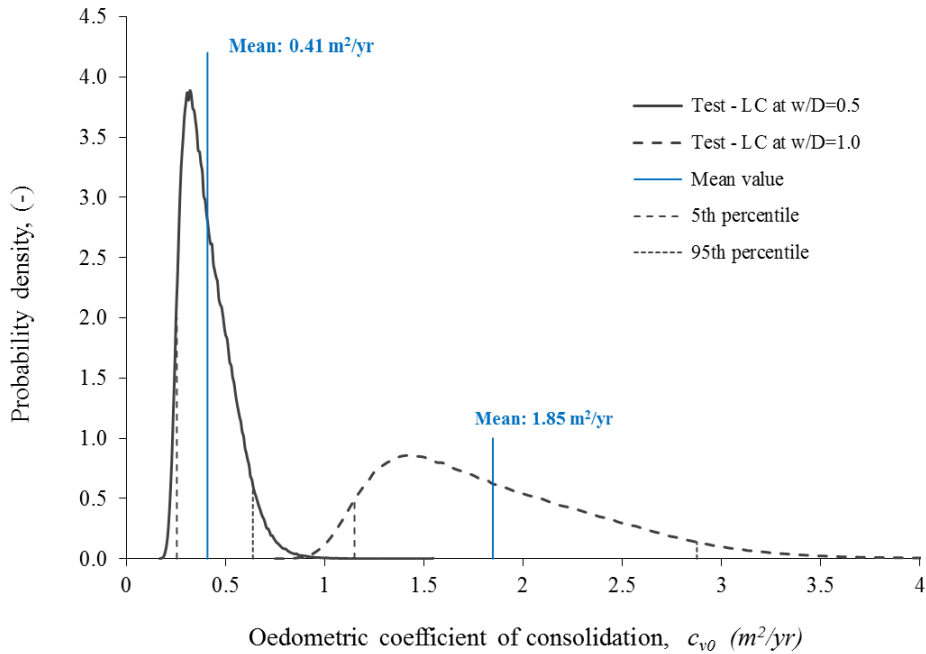
Figure 14: Estimated distributions of oedometric c_{v0} values (Monte Carlo simulation).
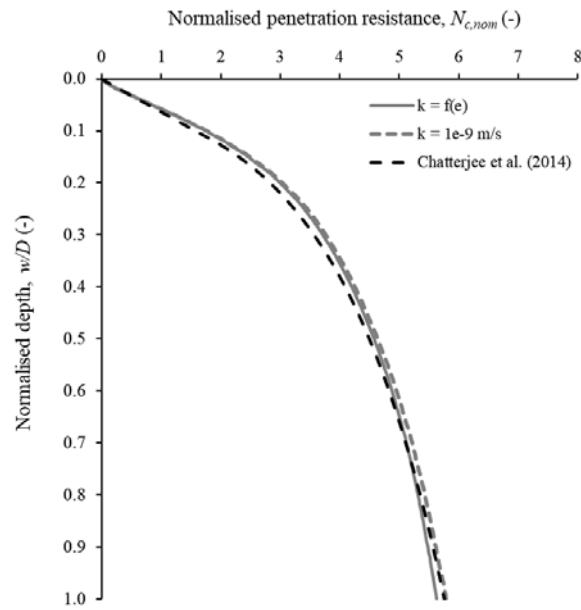
Figure 15: Comparison of results from the current manuscript with a voids ratio dependent permeability function with simulations with a constant permeability assumption and published simulation results after Chatterjee et al. (2014).
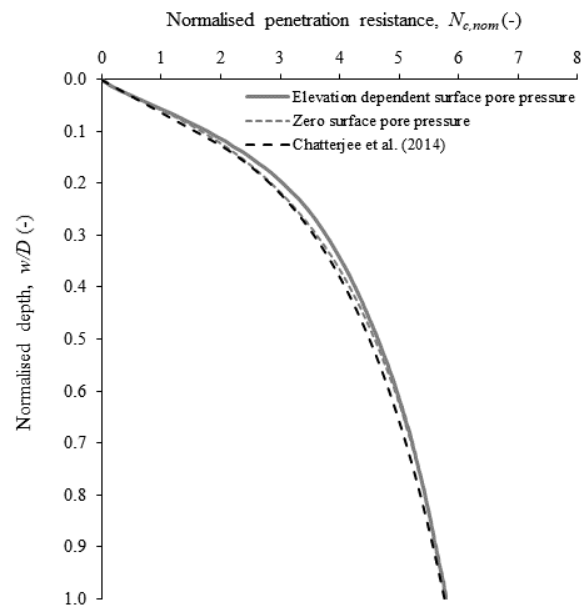

Figure 16: Comparison of results from the current manuscript with an elevation dependent pore pressure assumption with simulations with a zero surface pore pressure assumption and published simulation results after Chatterjee et al. (2014).
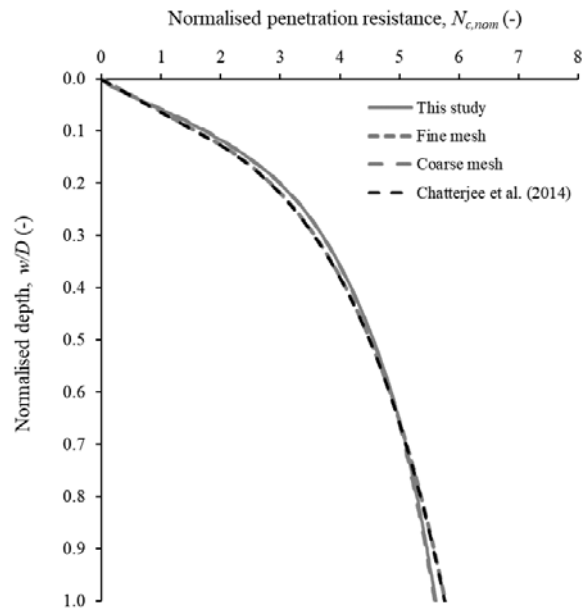
Figure 17: Comparison of results from the current manuscript using a finite element mesh with 18,105 elements with simulations with finer (31,288 elements) and coarser (12,217 elements) meshes and published simulation results after Chatterjee et al. (2014).
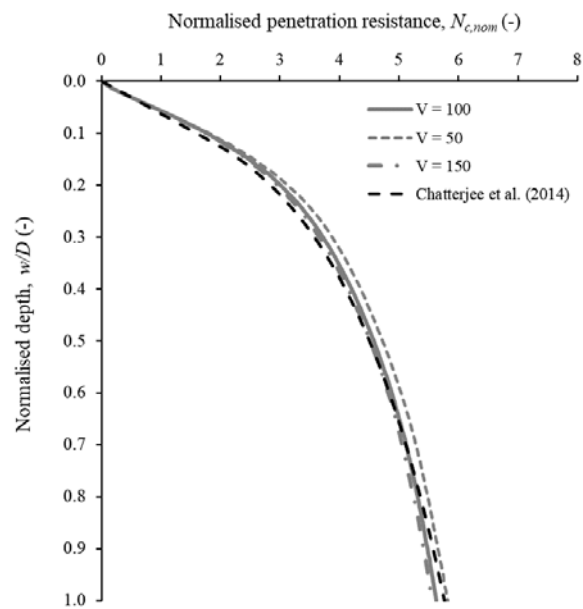

Figure 18: Comparison of results from the current manuscript where non-dimensional penetration velocity V (=vD/c_v) was 100 with simulations with V of 50 and 100 and published simulation results after Chatterjee et al. (2014).