# The planetary nebula population in the halo of M 87 ${ }^{\star}$ 

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Received 5 April 2013 / Accepted 15 August 2013


#### Abstract

Aims. We investigate the diffuse light in the outer regions of the nearby elliptical galaxy M 87 in the Virgo cluster, in the transition region between galaxy halo and intracluster light (ICL). Methods. The diffuse light is traced using planetary nebulas (PNs). The surveyed areas are imaged with a narrow-band filter centred on the redshifted [OIII] $] 5007 \AA$ emission line at the Virgo cluster distance (the on-band image) and with a broad-band $V$-filter (the off-band image). All PNs are identified through the on-off band technique using automatic selection criteria based on the distribution of the detected sources in the colour-magnitude diagram and the properties of their point-spread function. Results. We present the results of an imaging survey for PNs within a total effective area of $0.43 \mathrm{deg}^{2}$, covering the stellar halo of M 87 up to a radial distance of 150 kpc . We extract a catalogue of 688 objects down to $m_{5007}=28.4$, with an estimated residual contamination from foreground stars and background Ly $\alpha$ galaxies, which amounts to $\sim 35 \%$ of the sample. This is one of the largest extragalactic PN samples in number of candidates, magnitude depth, and radial extent, which allows us to carry out an unprecedented photometric study of the PN population in the outer regions of M 87 . We find that the logarithmic density profile of the PN distribution is shallower than the surface brightness profile at large radii. This behaviour is consistent with a model where the luminosity specific PN numbers for the M 87 halo and ICL are different. Because of the depth of this survey we are also able to study the shape of the PN luminosity function (PNLF) in the outer regions of M 87. We find a slope for the PNLF that is steeper at fainter magnitudes than the standard analytical PNLF formula and adopt a generalised model that treats the slope as a free parameter. Conclusions. The logarithmic PN number density profile is consistent with the superposition of two components associated with the halo of M87 and with the ICL, which have different $\alpha$ parameters. We derive $\alpha_{2.5, \text {,halo }}=\left(1.10_{-0.21}^{+0.17}\right) \times 10^{-8} N_{\mathrm{PN}} L_{\odot, \text { bol }}^{-1}$ and $\alpha_{2.5, \text { ICL }}=$ $\left(3.29_{-0.72}^{+0.60}\right) \times 10^{-8} N_{\mathrm{PN}} L_{\odot, b o l}^{-1}$ for the halo and the intracluster stellar components, respectively. The fit of the generalised formula to the empirical PNLF for the M 87 halo returns a value for the slope of 1.17 and a preliminary distance modulus to the M 87 halo of 30.74 . Comparing the PNLF of M 87 and the M31 bulge, both normalised by the sampled luminosity, the M 87 PNLF contains fewer bright PNs and has a steeper slope towards fainter magnitudes.


Key words. galaxies: groups: individual: M 87 - planetary nebulae: general - galaxies: elliptical and lenticular, cD galaxies: clusters: general - galaxies: halos

## 1. Introduction

Stars in the mass range between 1 and $8 M_{\odot}$ go through the planetary nebula (PN) phase before ending their lives as white dwarfs. The optical image of a PN is dominated by the luminous ionized envelope that is powered by the stellar core at its centre. The envelope emits in several strong lines from the UV to the NIR, and Dopita et al. (1992) showed that up to $15 \%$ of the luminosity of the central star is re-emitted in the forbidden [OIII] line at $\lambda 5007 \AA$.

PNs have been used as kinematic tracers of the stellar orbital distribution in the outer regions of galaxies, where the

[^0]continuum from the stellar surface brightness is too low with respect to the night sky, both in nearby galaxies (Hui et al. 1993; Peng et al. 2004; Merrett et al. 2006; Coccato et al. 2009; Cortesi et al. 2013) and out to $50-100 \mathrm{Mpc}$ (Ventimiglia et al. 2011; Gerhard et al. 2005). The outer regions of galaxies are particularly interesting because dynamical times are longer there, so they may preserve information of the mass assembly processes.

The observed properties of the PN population in external galaxies also correlate with the age and metallicity of the parent stellar population. These properties are the luminosity-specific PN number, $\alpha$-parameter for short, that quantifies the stellar luminosity associated with a detected PN, and the shape of the PN luminosity function (PNLF). We discuss these in turn.

Observationally the values of $\alpha$ correlate with the integrated $(B-V)$ colour of the parent stellar population, with
the spread in observed values for the reddest galaxies increasing significantly with respect to the constant value observed in bluer ( $(B-V)<0.8$ ) objects (Hui et al. 1993; Buzzoni et al. 2006). For the reddest galaxies, the value of $\alpha$ correlates with the $(F U V-V)$ colour, with the lowest number of PNs observed in old and metal-rich systems (Buzzoni et al. 2006).

To describe the shape of the PNLF for extragalactic PN populations, the analytical formula proposed by Ciardullo et al. (1989) has generally been used, but see also models by Méndez et al. (1993, 2008). At the brightest magnitudes the PNLF shows a cutoff that is observed to be invariant between different Hubble types and has been used as secondary distance indicator (Ciardullo et al. 2004). From about one magnitude fainter than the PNLF cutoff, the analytical formula predicts an exponential increase, in agreement with the slow PN fading rate described by Henize \& Westerlund (1963). Observationally, the PNLF slope correlates with the star formation history of the parent stellar population, with steeper slopes observed in older stellar populations and flat or slightly decreasing slopes in younger populations (Ciardullo et al. 2004; Ciardullo 2010).

The Virgo cluster, its elliptical galaxies, and intracluster light (ICL) were the targets of several PN surveys (Ciardullo et al. 1998; Feldmeier et al. 1998, 2004; Arnaboldi et al. 2002, 2003, 2004; Castro-Rodríguez et al. 2003, 2009; Aguerri et al. 2005), aimed at measuring distances and the ICL spatial distribution. In this paper we report the results of a deep survey carried out with the Suprime-Cam at the Subaru telescope to study the PN population in the halo around M 87, one of the two brightest galaxies in the Virgo cluster.

NGC 4486 (M 87) is a giant elliptical galaxy situated at the centre of the subcluster A in the Virgo cluster (Binggeli et al. 1987), the nearest large scale structure in the local universe. According to current models of structure formation, M87 acquired its mass over a long period of time through galaxy mergers and mass accretion. The stars in M87 are old (Liu et al. 2005), and its stellar halo contains about $70 \%$ of the galaxy's light down to $\mu_{V} \sim 27.0 \mathrm{mag}_{\mathrm{arcsec}}{ }^{-2}$ (Kormendy et al. 2009). Thus M87 is an ideal target for a survey aimed at detecting PNs in an extended galaxy halo, when investigating the halo kinematics and stellar population.

The paper is organized as follows: in Sect. 2 we describe the Suprime-Cam PN survey and the data reduction procedure. In Sect. 3 we describe the PN catalogue extraction and validation. The relation between the spatial distribution of the PN candidates and the M87 surface brightness profile is investigated in Sect. 4. We present the PNLF measured in the M 87 halo in Sect. 5 and discuss the comparison with the PNLF for the M31 bulge. Finally, we summarize our conclusions in Sect. 6. In the rest of the paper we adopt a distance modulus of 30.8 for M 87 , which means that the physical scale is $73 \mathrm{pc} \operatorname{arcsec}^{-1}$.

## 2. The Suprime-Cam M 87 PN survey

### 2.1. Imaging and observations

In March 2010 we observed two fields with the Suprime-Cam $10 \mathrm{k} \times 8 \mathrm{k}$ mosaic camera, at the prime focus of the 8.2 m Subaru telescope (Miyazaki et al. 2002). The CCDs have a readout noise of $10 \mathrm{e}^{-}$and an average gain of $3.1 \mathrm{e}^{-} \mathrm{ADU}^{-1}$. Each field of view covers an area of $34^{\prime} \times 27^{\prime}$, with a pixel size of $0!^{\prime} 2$; the two pointings cover the halo of M87 out to a radial distance of 150 kpc . Figure 1 shows a deep $V$-band image of the Virgo cluster core region and the two fields studied in this work overlaid.


Fig. 1. The core of the Virgo cluster (Mihos et al. 2005) with the positions of the fields studied in this work (black rectangles) and in previous surveys by Ciardullo et al. (1998) and Feldmeier et al. (2003) (dotted white squares). The region is dominated by the halos of 3 bright galaxies, M 84, M 86 and M 87, with M 87 covered by the Suprime-Cam fields. North is up, East is to the left.

We label these fields as the M 87 SUB1 and M 87 SUB2 fields, respectively.

Both fields were observed through an [OIII] narrow-band filter (on-band filter), centred on $\lambda_{c}=5029 \AA$ with a band width $\Delta \lambda=74 \AA$ and a broad-band $V$-filter (off-band filter). The total exposure time for the on-band images was $\sim 3.7 \mathrm{~h}$ and $\sim 4.3 \mathrm{~h}$, while for the off-band images it was 1 h and 1.4 h , for the M 87 SUB1 and M 87 SUB2 fields, respectively. Deep $V$-band images are needed for the colour selection of the PN candidates (see Sect. 3).

Our strategy for data acquisition was set up to achieve the best image quality. Narrow-band and broad-band images were taken close to each other during the observing nights to secure similar conditions in terms of scattered light and atmospheric seeing, while calibration images, such as dark sky ${ }^{1}$, were taken in between the science images to have a similar signal-to-noise ratio and image quality.

The nights were photometric with an overall seeing on the images less than $1^{\prime \prime}$. Airmasses were 1.01 and 1.06 for the reference M 87 SUB1 [OIII] and $V$-band exposures, and 1.13 and 1.03 for the reference M 87 SUB2 [OIII] and $V$-band exposures ${ }^{2}$. We did not perform any measurements for the extinction coefficients. We adopted the mean value of $X=$ $0.12 \mathrm{mag} /$ airmass, as listed for the [OIII] and $V$ filters at the Mauna Kea summit web site ${ }^{3}$, and in agreement with Buton et al. (2013).

The on-band filter bandpass was designed such that its central wavelength coincides with the redshifted $\lambda 5007 \AA$ emission at the Virgo cluster. The Johnson $V$-band filter can be used as the off-band filter despite the fact that it contains the [OIII] line in its large bandpass ( $\sim 1000 \AA$ ). The depth of the Suprime-Cam survey was chosen to detect all PNs brighter than $m^{*}+2.5$, where $m^{*}$ is the [OIII]5007 $\AA$ apparent magnitude of the bright cutoff of the PNLF for a distance modulus 30.8 . Table 1 gives a summary

[^1]Table 1. Summary of the field positions, filter characteristics, exposure times, and seeing for the narrow-band (on-band) and broad-band (off-band) images.

| Field | $\alpha$ (J2000) | $\delta(\mathrm{J} 2000)$ | [OIII] filter |  |  |  | $V$-band filter |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\lambda_{\text {c }}$ | FWHM | Exposure | $S_{\text {FWHM }}$ | $\lambda_{\text {c }}$ | FWHM | Exposure | $S_{\text {FWHM }}$ |
|  | (hh mm ss) | $\left({ }^{\circ}{ }^{\prime \prime \prime}\right)$ | (A) | (A) | (s) | (') | ( $\AA$ ) | (A) | (s) | ( ${ }^{\prime \prime}$ ) |
| M 87 SUB1 | 123025.230 | +123503.85 | 5029 | 74 | $11 \times 1200$ | 0.96 | 5500 | 956 | $13 \times 360$ | 1.00 |
| M 87 SUB2 | 123115.581 | +120722.33 | 5029 | 74 | $10 \times 1200$ | 0.98 | 5500 | 956 | $14 \times 360$ | 0.8 |

of the field positions, filter characteristics and exposure times for the on-band and off-band exposures for the analysed area around M87.

### 2.2. Data reduction, astrometry and flux calibration

The removal of instrumental signature, geometric distortion correction, background (sky plus galaxy) subtraction, a first astrometric solution and the final image combination were done using standard data reduction packages developed for Suprime-Cam data (sdfred software v2.0 ${ }^{4}$ ). Cosmic rays identification and rejection were carried out with L.A. Cosmic (Laplacian Cosmic Ray Identification) algorithm (van Dokkum 2001). Because of the spectroscopic follow-up our aim was to derive accurate positions of the PN candidates. To do this we improved the astrometry of the images to get a relative positional accuracy with less than $0!3$ in the residuals. The astrometric solution was computed using image astrometry tasks in the IRAF ${ }^{5}$ package imcoords, performing a geometrical transformation by 2nd order polynomial fitting. All images analysed in this paper are on the astrometric reference frame of the 2MASS catalogue ${ }^{6}$.

We flux calibrated the broad-band and narrow-band frames to the $A B$ system by observing standard stars through the same filters used for the survey. We used spectrophotometric standard star Hilt600 and Landolt stars for the [OIII]-band and $V$-band flux calibrations respectively, giving zero points for the [OIII] and $V$-band frames equal to $Z_{[\text {OIII }]}=24.29 \pm 0.04$ and $Z_{[\mathrm{V}]}=27.40 \pm 0.17$, normalised to a 1 second exposure ${ }^{7}$.

However, the integrated flux from the [OIII] line of a PN is usually expressed by the magnitude $m_{5007}$ using the relation introduced by Jacoby (1989):

$$
\begin{equation*}
m_{5007}=-2.5 \log _{10} F_{5007}-13.74, \tag{1}
\end{equation*}
$$

where $F_{5007}$ is in units of ergs $\mathrm{cm}^{-2} \mathrm{~s}^{-1}$. From this we determined the absolute flux calibration for the nebular flux in the [OIII] emission line, following Jacoby et al. (1987). This flux calibration takes the filter transmission efficiency at the wavelength of

[^2]Table 2. On-band and off-band limiting magnitudes.

| Field | $m_{\text {lim,5007 }}$ | $m_{\text {lim,b }}$ | $C$ |
| :--- | :---: | :---: | :---: |
| M 87 SUB1 | 28.39 | 26.4 | 2.49 |
| M 87 SUB2 | 28.39 | 26.6 | 2.49 |

Notes. C is the transformation constant between $A B$ and 5007 magnitudes for the narrow-band [OIII] filter: $m_{5007}=m_{A B}+C$.
the emission line into account, due to the fact that the fast optics of wide-field instruments, such as the Suprime-Cam at the Subaru telescope can affect the transmission properties of the interference filter, especially for narrow-band imaging. This effect was quantified making use of the filter transmission curve described in Arnaboldi et al. (2003), representing the expected transmission of the [OIII] interference filter in the f/1.86 beam of the Suprime-Cam at the Subaru telescope.

The relation between the $m_{5007}$ and $m_{A B}$ magnitudes for the narrow-band filter is given by:
$m_{5007}=m_{A B}+2.49$.
A detailed description of the relation between $A B$ and $m_{5007}$ [OIII] magnitudes is given in Arnaboldi et al. (2002).

In this paper we will use the notation of $m_{\mathrm{n}}$ and $m_{\mathrm{b}}$ to refer to the narrow-band and broad band magnitudes of the objects in the AB system. We will use $m_{5007}$ to refer to the [OIII] magnitudes introduced by Jacoby (1989).

Table 2 gives the constant value for $A B$-to- $m_{5007}$ magnitude conversion, and limiting magnitudes in the on-band and off-band frames analysed in this paper.

The final products for the M 87 SUB1 and M 87 SUB2 pointings consist of the stacked images in the [OIII] and $V$ band, astrometrically and photometrically calibrated. As consequence of the observing strategy the seeing measured as the average FWHM of stellar sources is similar in both pairs of images, and less than $F W H M_{\text {seeing }}<1^{\prime \prime}$ (see Table 1). A fit of the PSF with the IRAF task $p s f$ (in the digiphot/daophot package) shows that a Moffat analytical function with a $\beta$ parameter $\beta=2.5$ (see IRAF/digiphot manual for more details) is the best profile to model the stellar light distribution of point sources in our images. Moreover, the PSF fit was computed in three different regions of the on-band and off-band images for both the M 87 SUB1 and M 87 SUB2 fields, covering the images from the centre to the edges: for all regions examined, the PSF fit gave the same best fit solution, showing that the PSF does not vary across the images.

## 3. Selection of PN candidates and catalogue extraction

As a result of their bright [OIII] (25007) and faint continuum emission, extragalactic PNs can be identified as objects detected in images taken through the on-band [OIII] filter, but not detected in images taken through the off-band continuum filter.

In our work, all PN candidates are extracted through the onoff band technique (Jacoby et al. 1990) using selection criteria based on the distribution of the detected sources in colour magnitude diagrams (Theuns \& Warren 1997). We used an automatic extraction procedure developed and validated in Arnaboldi et al. $(2002,2003)$ for the identification of emission line objects in our images. We give a brief summary of the selection procedure in the next section.

### 3.1. Extraction of point-like emission-line objects

We employed the object detection algorithm SExtractor (Bertin \& Arnouts 1996), that detects and measures flux from pointlike and extended objects. Sources were detected in the on-band image requiring that 20 adjacent pixels or more have flux values $1 \times \sigma$ rms above the background. Magnitudes were then measured in a fixed aperture of radius $R=6$ pixels (1.2", $\sim 3$ times the seeing radius) for sources in the on-band image, and then through the aperture photometry in the $V$-band image at the $(x, y)$ positions of the detected [OIII] sources with SExtractor in dual-image mode. Candidates for which SExtractor could not detect a $m_{\mathrm{b}}$ magnitude at the position of the [OIII] emitter were assigned a $m_{\mathrm{b}}=28.7$, i.e. the flux from an [OIII] emission of $m_{\mathrm{n}}=m_{\text {lim,n }}$ seen through a $V$-band filter (Theuns \& Warren 1997). All objects were plotted in a colour magnitude diagram (CMD), $m_{\mathrm{n}}-m_{\mathrm{b}}$ vs. $m_{\mathrm{n}}$, and classified according to their positions in this diagram. Based on their strong [OIII] line emission, the most likely PN candidates are point-like objects with colour excess corresponding to an observed EW greater than $110 \AA$, after convolution with photometric errors as function of the magnitude. The limit of completeness is defined as the magnitude at which the recovery fraction of an input simulated point-like population with a given luminosity function ${ }^{8}$, drops below a threshold set to $50 \%$. We find $m_{\text {lim,5007 }}=28.39$; this is the limiting magnitude of our sample.

The colour selection of PN candidates requires off-band images deep enough so that the colour can be measured reliably at fainter magnitudes. As for the [OIII] images, we define the $V$-band limiting magnitude as the faintest magnitude at which half of the input simulated sample is retrieved from the image; we then derive $m_{\text {lim,b }}=26.4$ and $m_{\text {lim,b }}=26.6$ for the M 87 SUB1 and M 87 SUB2 fields respectively.

### 3.1.1. Colour selection

PN candidates are defined as objects with [OIII] magnitudes brighter than the [OIII] limiting magnitude and with a colour excess, $m_{\mathrm{n}} \leq m_{\mathrm{lim}, \mathrm{n}}$ and $m_{\mathrm{n}}-m_{\mathrm{b}}<-0.99$, the latter representing the colour excess corresponding to $E W_{\text {obs }}=110 \AA$. The relation between the observed EW and the colour in magnitudes is given by Teplitz et al. (2000): $E W_{\text {obs }} \simeq \Delta \lambda_{\mathrm{nb}}\left(10^{0.4 \Delta m}-1\right)$, where $\Delta \lambda_{\mathrm{nb}}$ is the width of the narrow band filter and $\Delta m=m_{\mathrm{b}}-m_{\mathrm{n}}$ is the colour. A value of $E W_{\text {obs }}=110 \AA$ limits contamination from [OII] $\lambda 3726.9$ emitters at redshift $z \sim 0.34$ (see Sect. 3.2).

Photometric errors may be responsible for continuum emission sources falling below the adopted colour excess, hence contaminating the emission object distribution. This effect is limited by defining regions in which $99 \%$ and $99.9 \%$ of a simulated continuum population would fall in this CMD. Below the $99.9 \%$ line, the probability to detect stars is reduced to the $0.1 \%$ level.

[^3]Theoretically a PN is a point-like source with no detected continuum, i.e. with no broadband magnitude measured by Sextractor. Nevertheless we expect a continuum contribution in an aperture at the position of a [OIII] source in the halo of M87 because of crowding effects or residuals from the subtraction of the continuum light from the M 87 halo. This is confirmed by the distribution of colours measured for a simulated PN population in the outer regions of M 87 , which we discuss in Sect. 3.1.4.

### 3.1.2. Point-like versus extended sources

At a distance of $\sim 15 \mathrm{Mpc}$, PNs are unresolved points of green light. We need to distinguish them from spatially extended background galaxies and, possibily, HII regions. Point-like objects in our catalogue are candidates that satisfy the following criteria:

1. we compare the SExtractor $m_{\mathrm{n}}$ and $m_{\text {core }}$ magnitudes, where $m_{\text {core }}$ represents the measured magnitude in a fixed aperture of radius $R=2$ pixels ( $0.4^{\prime \prime}$ ). For point-like objects $m_{\mathrm{n}}-m_{\text {core }}$ has a constant value as function of magnitude, while it varies for extended sources. We analyzed this difference for simulated point-like objects and determined the range of $m_{\mathrm{n}}-m_{\text {core }}$ as function of $m_{\mathrm{n}}$ where $96 \%$ of the simulated population fall. This range is narrow for bright magnitudes but it becomes wider towards fainter magnitudes due to the photometric errors.
2. We derive the distribution for the SExtractor half-light radius $R_{\mathrm{h}}$, i.e. the radius within which half of the object's total flux is contained. For point-like objects this value should be constant but due to photometric errors it is confined to a range $1 \leq R_{\mathrm{h}} \leq 4$ pixels that we determine as the range in which $95 \%$ of the simulated population lies.

These criteria for the selection of point-like sources are shown in Fig. 2. For the simulated population, $91 \%$ of the input sources are recovered as point-like objects. Therefore, applying these criteria to the observed objects excludes $9 \%$ of the PNs from the sample along with the extended objects.

### 3.1.3. Masking of bad/noisy regions

The last step of our automatic selection is the masking of the areas where the detection and photometric measurements of sources are dominated by non-Poisson noise. These areas include diffraction and bleed spikes from the brightest stars, bad pixel regions and higher background noise regions, the latter mostly at the edges of the images because the dithering strategies lead to different exposure depth near the edges (we will discuss this further in Sect. 3.1.5). After these regions are excluded, the total effective area of our survey is $\sim 0.43 \mathrm{deg}^{2}$.

The selection described above leads to a catalogue, hereafter called automatic sample, containing 792 objects classified as PN candidates. These sources are point-like objects with colour excess, corresponding to an observed equivalent width $E W_{\text {obs }}>110 \AA$ and are located in regions of the colourmagnitude diagram where the contamination by foreground stars is below $0.1 \%$.

Figure 3 shows the colour selection for the M 87 SUB1 and M 87 SUB2 fields, with the PN candidates represented by asterisks.
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Fig. 2. Point-source test, showing $m_{\mathrm{n}}-m_{\text {core }}$ vs. $m_{\mathrm{n}}$ (left) and $m_{\mathrm{n}}$ vs. $R_{\mathrm{h}}$ (right) for observed sources satisfying our colour restrictions in the M87 SUB1 field (top) and for modeled point-like emission objects (bottom). The dark lines in the left panels delimit the region within which $96 \%$ of the modeled point-like emission objects fall. Observed sources in the top panels are considered as point-like objects if they lie in this region and have a half light radius in the range $1 \leq R_{\mathrm{h}} \leq 4$ pixels. This range of $R_{\mathrm{h}}$ was chosen such that $95 \%$ of the modeled population was included. Red dots represent objects that satisfy both criteria and are thus selected as point-like objects. These criteria are also applied to sources in M 87 SUB2 field.

### 3.1.4. Missing PNs in the photometric sample

The selection procedure based on flux thresholds is sensitive to photometric errors. At fainter magnitudes, PN candidates with intrinsic $E W_{\text {obs }}>110 \AA$, or $m_{\mathrm{n}} \leq m_{\text {lim,n }}$, can have smaller measured $E W_{\text {obs }}$, or fainter $m_{\mathrm{n}}$, because of photometric errors and are, therefore, excluded from our selection. We quantified this effect by simulating an [OIII] emission line population, with an exponential LF in the magnitude range $23 \leq m \leq 27.5$, randomly distributed on the on-band scientific image. No continuum emission was assigned to the objects. We then carried out the photometry as for the real sources: their CMD is shown in Fig. 4. We see that many simulated PNs have a measured continuum magnitude due to crowding effects or residuals from the galaxy background. This CMD shows also that for simulated sources brighter than the limiting magnitude, the percentage of PNs that we would miss due to photometric errors is $28.3 \%$ and $29.8 \%$ in the M 87 SUB1 and M 87 SUB2 fields respectively. This implies that our automatic procedure, within the magnitude range $23 \leq m_{\mathrm{n}} \leq m_{\lim , \mathrm{n}}$, recovers 0.71 of the total sample. In Table 5 we show the dependence of this colour completeness on magnitude.

### 3.1.5. Catalogue validation: visual inspection and joint candidates in both fields

Finally, the photometric catalogue obtained from the automatic selection described in the previous sections was visually inspected, in particular for regions near bright stars or with a higher noise level. This visual inspection led to a catalogue of 688 candidates, the removed spurious detections being $\sim 11 \%$ of the automatic extracted sources.


Fig. 3. CMD for all sources in the M87 SUB1 (top panel) and M 87 SUB2 (bottom panel) fields. The horizontal lines indicate the colour excess of emission line objects with an $E W_{\text {obs }}=110 \AA$. The curved lines delimit the regions above which $99 \%$ and $99.9 \%$ of the simulated continuum objects fall in this diagram, given the photometric errors. The set of points on the inclined line represents those objects with no broadband magnitude measured by SExtractor (see Sect. 3.1 for more details). Asterisks represent objects classified as PNs according to the selection criteria discussed in Sect. 3.1.

In the final catalogue 18 candidates appear in both fields and their magnitudes are measured independently in the two pointings. Differences between the independent measurements are consistent with the errors.

### 3.2. Possible sources of contaminants in the $P N$ sample

Following Aguerri et al. (2005), we examined the main contaminants and estimate their contributions to the final catalogue.

Contamination by faint continuum objects - At $m_{\text {lim,n }}$, the faint continuum objects can mimic an [OIII] emission line population, because they are scattered into the region where PN candidates are selected. We constrained this contribution by computing the $99.9 \%$ lines for the distribution of continuum objects. From the total number of the observed foreground stars, we determine the number of objects $(0.1 \%)$ that would be scattered in the region of colour selected PNs. The resulting contribution from faint stars equals $9 \%$ and $11 \%$ of the total extracted sample for the M 87 SUB1 and M 87 SUB2 fields, respectively.


Fig. 4. CMD for a simulated PN population in the M 87 SUB1 field with intrinsic magnitudes $23 \leq m_{\mathrm{n}} \leq m_{\text {lim,n }}$ (crosses). Because of photometric errors, our selection criteria would exclude $28.3 \%$ of the input sample (blue crosses). The remaining $71.7 \%$ would be selected as PNs (red crosses). Dots surrounded by green squares and cyan triangles are emission objects in common between our sample and the PN samples selected by Ciardullo et al. (1998) and Feldmeier et al. (2003), respectively. Solid lines as in Fig. 3.

Contamination by background galaxies: Lyman $\alpha$ galaxies and [OII] emitters - The strong [OIII] $\lambda 5007 \mathrm{PN}$ emission with no associated detected continuum allows us to identify PNs as objects with negative colour (Theuns \& Warren 1997). This colour selection will also identify $\mathrm{Ly} \alpha$ galaxies at redshift $z \sim 3.1$ as well as [OII] $\lambda 3727.26$ emitters at redshift $z \sim 0.34$, whose emission lines fall within the bandpass of our narrow band filter.

The contamination by Ly $\alpha$ is quantified by using the number density of $z=3.1 \mathrm{Ly} \alpha$ galaxies from Gronwall et al. (2007) where their limiting magnitude of $m_{\lim , \mathrm{n}(\mathrm{G} 07)}(5007)=28.31$ for statistical completeness makes their survey as deep as ours. We consider their Ly $\alpha \mathrm{LF}$ given by a Schechter function of the form:
$\phi(L) \mathrm{d}\left(L / L^{*}\right) \propto\left(L / L^{*}\right)^{\alpha} \mathrm{e}^{-L / L^{*}} \mathrm{~d}\left(L / L^{*}\right)$,
with their best-fit values of $\log _{10} L^{*}=42.66 \operatorname{erg~s}^{-1}$ and $\alpha=$ -1.36 , corrected for the effects of photometric errors and their filter's non-square transmission curve. At redshift $z=3.1$, the surveyed area of $0.43 \mathrm{deg}^{2}$, observed through the SuprimeCam narrow-band filter, samples $\sim 3.1 \times 10^{5} \mathrm{Mpc}^{3}$ (Hogg 1999). However, as pointed out by Gronwall et al. (2007), when working with narrow band data taken through a nonsquare filter bandpass, the effective survey volume is $\sim 25 \%$ smaller than that inferred from the interference filter's FWHM. We thus compute the number of expected $\operatorname{Ly} \alpha$ emitters by using a survey volume of $\sim 2.3 \times 10^{5} \mathrm{Mpc}^{3}$. The $\operatorname{Ly} \alpha$ population at $z \sim 3.1$ shows clustering over a correlation length of $r_{0}=3.6 \mathrm{Mpc}$ (Gawiser et al. 2007), corresponding to an angular size in the Virgo cluster of $r_{0}^{\prime} \sim 7.9^{\prime}$. Hence we need to allow for the large-scale cosmic variance in the average Ly $\alpha$ density, which in our case is $\sim 20 \%$ (Somerville et al. 2004; Gawiser et al. 2007). From our effective sampled volume, we predict, then, that the number of expected Ly $\alpha$ contaminants is $25 \% \pm 5 \%$ of our total catalogue.

The contribution from [OII] emitters is considerably reduced by selecting candidates with observed equivalent width, $E W_{\text {obs }}>$ $110 \AA$, corresponding to a colour threshold $m_{\mathrm{n}}-m_{\mathrm{b}}<-0.99$ (Teplitz et al. 2000). This is because no [OII] emitters with $E W_{\text {obs }}>95 \AA$ have been found (Colless et al. 1990; Hammer et al. 1997; Hogg et al. 1998). Note that in the Gronwall et al. (2007) sample of $\operatorname{Ly} \alpha$ galaxies at $z=3.1$, the fraction of [OII]
contaminants is considered to be negligible because of their EW selection $\left(\Delta m_{(G 07)} \sim-1\right)$. This means that if there is a fraction of [OII] emitters with $E W_{\text {obs }}>110 \AA$ in our sample, then their contribution is accounted for by using the Ly $\alpha$ LF from Gronwall et al. (2007).

### 3.3. Comparison with previous $P N$ samples in M87

Our survey area overlaps with those studied by Jacoby et al. (1990), Ciardullo et al. (1998, hereafter C98) and Feldmeier et al. (2003, hereafter F03); the locations of the C98 and F03 fields are over-plotted on Fig. 1.

We have a limited number of objects in common between Jacoby et al. (1990) and our catalogue ( $\sim 14 \%$ of their catalogue), because of the high residual background in our images from the bright central regions of M 87. These fractions are larger for the C98 and F03 catalogues, and we discuss them in turn.

C98 carried out an [OIII] $\lambda 5007$ survey for PNs, covering a $16^{\prime} \times 16^{\prime}$ field around M 87 . They identified 329 PNs in the M 87 halo, 187 of these in a statistically complete sample down to $m_{5007}=27.15$. Of the 329 sources selected by C98, 201 fall within our surveyed area ${ }^{9}$. Of these sources, $91 \%$ are matched with [OIII] detected objects in our survey, but only $\sim 60 \%$ satisfy our selection criteria for PN candidates, see the CMD for the C98 candidates (green squares) in Fig. 4.

F03 carried out a survey of intracluster PNs (ICPNs) over several fields in the Virgo cluster region; the one overlapping with the current Subaru survey is a $16^{\prime} \times 16^{\prime}$ area north of M 87 , labeled "FCJ" field in F03 and Aguerri et al. (2005). 100\% of the candidates in this field match with [OIII] sources in the M 87 SUB1 field, but only $42 \%$ satisfy the selection criteria for PN candidates in our survey, see the CMD for the F03 candidates (cyan triangles) in Fig. 4.

On the basis of the common PN candidates with the largest signal-to-noise ratios, we can compare the photometric calibration for the $m_{5007}$ magnitudes and any variations with magnitude in the different samples. We find a constant offset that does not vary with magnitude between the C98, F03 samples and our survey, with our $m_{5007}$ system being $\sim 0.3$ mag fainter. In Fig. 5 the F03 mags (corrected for $\sim 0.3$ mag shift) are compared with ours.

In Sect. 5 we will compare the empirical PNLF for our PN sample with those for the C98 and F03 data, and based on this comparison will argue that there is a systematic effect in the C98 and F03 photometry, causing brighter $m_{5007}$. In what follows, the calibration offset is therefore applied to the previously published data whenever we compare them with our PN magnitudes.

## 4. The radial profile of the PN population and comparison with the M 87 surface brightness

In what follows we present the number density distribution from our PN sample, one of the largest both in number of tracers and in radial extent. Plotted in Fig. 6 is the position of our PN candidates together with the outline of our survey region.

### 4.1. The PN radial density profile

We now investigate whether the PN number density profile follows the surface brightness profile of the galaxy light. On the

[^4]

Fig. 5. $m_{5007}$ for the F03 PN candidates (corrected for $\sim 0.3$ mag offset) plotted against the $m_{5007}$ magnitudes measured in our survey. The dotted lines represent the $1 \sigma$ uncertainty from the photometric errors of our survey. The two magnitude systems are consistent within the photometric errors with an offset that is constant with magnitude.


Fig. 6. Spatial distribution of PN candidates (black crosses). Red crosses represent objects classified as spurious after visual inspection. The magenta cross indicates the centre of M87. Dotted ellipses trace the M87 isophotes from $R=2.8$ to $R=40.7^{\prime}$ along the photometric major axis, at a position angle $\mathrm{PA}=-25.6^{\circ}$ (Kormendy et al. 2009). The solid squares depict our survey area. North is up, east to the left.
basis of the simple stellar population theory, the luminosityspecific stellar death rate is insensitive to the population's age, initial mass function, and metallicity (Renzini \& Buzzoni 1986). Thus the probability of finding a PN at any location in a galaxy should be proportional to the surface brightness of the galaxy at that location.

In order to compare the surface brightness and PN number density profiles, we bin our PN sample in elliptical annuli, whose major axes are aligned with M 87's photometric major axis and with ellipticities measured from the isophotes (see Fig. 6). We


Fig. 7. Top panel: comparison between surface brightness profile from (Kormendy et al. 2009; crosses) and logarithmic PN number density profile of the emission line candidates, brighter than $m_{5007}=28.3$, and corrected for spatial and colour incompleteness (open circles with error bars, see Table 4 for data), as function of the distance from the M 87 centre. The black dotted line represents the contribution of Ly $\alpha$ emission objects to the logarithmic PN number density profile, assuming a homogeneous distribution over the surveyed area. Under the same hypothesis, filled circles show the logarithmic PN number density profile when the Ly $\alpha$ contribution is statistically subtracted. Red lines mark the inner, intermediate and outermost regions of the M87 halo (see text). Bottom panel: difference between the logarithmic PN number density profiles if we had used the automatically extracted sources without the final inspection: a value of zero would mean that no variation in the number of sources is implied in the annulus at a given radius.
compute PN number densities as ratios between the number of PNs in each annulus and the area of the intersection of the annulus with our field of view. These areas, $A(R)$, are estimated using a Monte Carlo integration technique.

The PN number density profile must be corrected for spatial incompleteness because the bright galaxy background and bright foreground stars may affect the detection of PNs. We compute this completeness function, $\mathrm{C}(R)$, by adding a PN sample modelled according to a Ciardullo et al. (1989) PNLF on the scientific image. $C(R)$ is then the fraction of simulated objects recovered by Sextractor in the different elliptical annuli vs the input modelled population, for PNs brighter than $m_{5007}=28.3$ (values are given in Table 4). The expected PN total number is then:
$N_{\mathrm{c}}(R)=\frac{N_{\mathrm{obs}}(R)}{C(R) 0.71}$,
where the value 0.71 accounts for the average colour incompleteness (see Sect. 3.1.4). In Fig. 7 we show the comparison between the major axis stellar surface brightness profile in the $V$ band, $\mu_{\text {K09 }}$ (Kormendy et al. 2009), and the PN logarithmic number density profile, defined as:
$\mu_{\mathrm{PN}}(R)=-2.5 \log _{10}\left(\Sigma_{\mathrm{PN}}(R)\right)+\mu_{0}$,
where
$\Sigma_{\mathrm{PN}}(R)=\frac{N_{\mathrm{c}}(R)}{A(R)}$
is the PN number density corrected for spatial and colour incompleteness, and $\mu_{0}$ is a constant value added to match the PN number density profile to the $\mu_{\mathrm{K} 09}$ surface brightness profile. In the same plot, we also indicate radii that select three different
regions in the halo of M87; these regions are for $R<\bar{R} / 2$, $\bar{R} / 2 \leq R<\bar{R}$ and $R \geq \bar{R}$, where $\bar{R}=13.5^{\prime}$ represents the mean distance of the PN sample from the centre of M87. The innermost and the outermost number density points are at radii $R=2.8^{\prime}$ and $R=27.6^{\prime}$ respectively, and in Fig. 7 they are indicated with dotted red lines. The surface brightness and the logarithmic PN number density profile agree well in the innermost region, they slightly deviate in the intermediate region while in the outermost region the logarithmic PN number density profile flattens. The difference between the two profiles amounts to 1.2 mag at the outermost radii. This discrepancy would still be observed if we had used instead the candidates from the automatic selection procedure without any final inspection: the difference between the two number densities is too small to affect the slope at large radii (see Fig. 7, bottom panel). We also note that the flattening of the logarithmic number density profile is seen in both Suprime-Cam fields independently.

Empirically, the logarithmic PN number density profile follows light in elliptical (Coccato et al. 2009) and S0 (Cortesi et al. 2013) galaxies. However, these studies cover the halos out to typically only 20 kpc . The presence of Ly $\alpha$ background galaxies at $z \sim 3.1$ could also contribute to the flatter slope of the logarithmic PN number density profile, and so we need to evaluate their contribution to the number density at large radii. In Fig. 7 we show the contribution from Ly $\alpha$ contaminants (black dotted line) to the logarithmic number density ( $25 \% \pm 5 \%$ of the total sample), assuming a homogeneous distribution in the surveyed area. We can make this assumption because the survey area $0.43 \mathrm{deg}^{2}$ extends over many correlation lengths of the Ly $\alpha$ population at $z=3.14$ (see Sect. 3.2).

Hence we can statistically subtract the contribution of the Ly $\alpha$ backgrounds objects from the number of PN candidates in each annulus and obtain the corrected number density profile (filled circles in Fig. 7). Now the error bars also account for the expected fluctuation of Ly $\alpha$ density (see Sect. 3.2 for details) and the flattening of the logarithmic PN number density profile is still observed. Using the derived $\alpha_{2.1}$ value for the halo from Sect. 4.4, the surface brightness profile translates to $\sim 295$ PNs down to $m_{5007}=28.3$. Down to this magnitude our catalogue contains $\sim 420$ estimated PNs. The excess, then, is $\sim 3.6 \times \sigma_{\mathrm{Ly} \alpha}$, where $\sigma_{\text {Ly } \alpha}$ is the standard deviation in the expected number of Ly $\alpha$ emitters from cosmic variance and Poisson statistics. Hence, the flattening can not be explained by fluctuations in the Ly $\alpha$ fraction. In what follows we investigate the physical origin of the flatter logarithmic PN number density profile.

### 4.2. The $\alpha$ parameter

The total number of PNs, $N_{\mathrm{PN}}$, is correlated with the total bolometric luminosity of the parent stellar population, $L_{\mathrm{bol}}$, through the so-called $\alpha$-parameter, that defines the luminosity-specific PN density: $N_{\mathrm{PN}}=\alpha L_{\mathrm{bol}}$.

From stellar evolution theory it is found that the luminosityspecific stellar death rate is insensitive to a stellar population's age, initial mass function, and metallicity (Renzini \& Buzzoni 1986). Therefore, the total number of PNs associated with a parent stellar population can be computed from the bolometric luminosity using the formula:
$N_{\mathrm{PN}}=B L_{\mathrm{TOT}} \tau_{\mathrm{PN}}$,
where $B$ is the specific evolutionary flux (stars $\mathrm{yrs}^{-1} L_{\odot}^{-1}$ ), $L_{\text {TOT }}$ is the total bolometric luminosity of the parent stellar
population, and $\tau_{\text {PN }}$ is the PN visibility lifetime. From Eq. (7), the luminosity-specific PN number, $\alpha$, is
$\alpha=\frac{N_{\mathrm{PN}}}{L_{\mathrm{TOT}}}=B \tau_{\mathrm{PN}}$.
Observed values of the $\alpha$ parameter can then be interpreted as different values of $\tau_{\text {PN }}$ for the PNs associated with different stellar populations, because variations of $B$ with metallicity or Initial Mass Function (IMF) slope are small (Renzini \& Buzzoni 1986).

For any specific observation, the actual value of $N_{\text {PN }}$ depends on the flux limit of the survey in which the PNs are detected. Hence, for our survey depth we are interested in estimating $\alpha_{2.1}$, the number of PNs within $\Delta m=2.1$ magnitudes of the bright cutoff, per given amount of bolometric luminosity emitted by the stellar population of the galaxy's halo or ICL. For any $\Delta m$, $\alpha_{\Delta m}$ is defined such that
$N_{\mathrm{PN}, \Delta \mathrm{m}}=\int_{M^{*}}^{M^{*}+\Delta m} N(m) \mathrm{d} m=\alpha_{\Delta m} L_{\mathrm{bol}}$,
where $N(m)$ is the PNLF and $M^{*}$ is the bright cutoff magnitude.

### 4.3. Halo and intracluster $P N$ population

When studying the PN population in the outer region of M87 out to 150 kpc from the galaxy's centre, we expect contributions from the halo PNs and from ICPNs. The presence of ICL in cluster cores is a by-product of the mass assembly process of galaxy clusters (Murante et al. 2004, 2007).

The existence of intracluster PNs in Virgo has been demonstrated on the basis of extended imaging surveys in the $5007 \AA$ [OIII] line (Feldmeier et al. 1998, 2003; Arnaboldi et al. 2002; Aguerri et al. 2005; Castro-Rodríguez et al. 2009) and spectroscopic follow-up (Arnaboldi et al. 1996, 2003, 2004). From the spectroscopic follow-up of Arnaboldi et al. (2004) we know the M87 halo and the Virgo core ICL to coexist for distances $R>16^{\prime}$ from M 87's centre (the FCJ field). In fact, the projected phase space diagram from Doherty et al. (2009) (PN line-of-sight velocity vs. radial distance from M 87 centre) shows the coexistence of the halo and ICL PN population out to 150 kpc .

To estimate the ICL luminosity in our two fields, we assume a constant surface brightness $\mu_{V}=27.7 \mathrm{mag}_{\operatorname{arcsec}}{ }^{-2}$ (Mihos et al. 2005), and a $V$-band bolometric correction $\mathrm{BC}_{V}=-0.85$ (Buzzoni et al. 2006), which then gives a total bolometric luminosity in the ICL of $L_{\text {ICL }}=1.66 \times 10^{10} L_{\odot, \text { bol }}$. This amounts to about one quoter of the bolometric luminosity of the M 87 halo.

### 4.4. Two component photometric model for M 87 halo and ICL, and determination of their $\alpha_{2.5}$ parameters

Therefore we now investigate whether the observed discrepancy between the logarithmic PN number density profile and $\mu_{V}$ surface brightness profile in Fig. 7 may be explained by considering two PN populations associated with the M87 halo and ICL. The physical parameter that links a PN population to the luminosity of its parent stars is the luminosity-specific PN number, the $\alpha$ parameter, thus a discrepancy between $\mu_{V}$ and the measured logarithmic PN number density profile may come from different $\alpha$ values for the halo and ICL stellar population. This possibility is supported by Doherty et al. (2009) who measured two different values of $\alpha$ for the bound (M87 halo) and unbound (ICL) stellar component, which we are going to label $\alpha_{\text {halo }}$ and $\alpha_{\text {ICL }}$ in
what follows. We can then define a photometric model with two components:

$$
\begin{align*}
\tilde{\Sigma}(R) & =\left[\alpha_{2.1, \text { halo }} I(R)_{\text {halo,bol }}+\alpha_{2.1, \mathrm{ICL}} I_{\mathrm{ICL}, \mathrm{bol}}\right]  \tag{10}\\
& =\alpha_{2.1, \text { halo }}\left[I(R)_{\mathrm{K} 09, \mathrm{bol}}+\left(\frac{\alpha_{2.1, \mathrm{ICL}}}{\alpha_{2.1, \text { halo }}}-1\right) I_{\mathrm{ICL}, \mathrm{bol}}\right] \tag{11}
\end{align*}
$$

where $\tilde{\Sigma}(\mathrm{R})$ represents the predicted PN surface density in units of $N_{\mathrm{PN}} \mathrm{pc}^{-2}, I(R)_{\text {halo }}$ and $I_{\mathrm{ICL}}$ are the surface brightnesses for the halo and the ICL components, and $I_{\mathrm{K} 09}$ from Kormendy et al. (2009) is the observed total surface brightness from M 87 centre out to $40^{\prime}$, accounting for both halo and ICL components. These surface brightnesses are in units of $L_{\odot} \mathrm{pc}^{-2}$ and their bolometric values are computed from the measured profiles in units of mag $\operatorname{arcsec}^{-2}$ via the formula:
$I=10^{-0.4\left(\mathrm{BC}_{\nu}-\mathrm{BC}_{\odot}\right)} 10^{-0.4(\mu-K)}$,
where $\mathrm{BC}_{V}=-0.85$ and $\mathrm{BC}_{\odot}=-0.07$ are the $V$-band and the Sun bolometric corrections, and $K=26.4 \mathrm{mag}_{\mathrm{arcsec}}{ }^{-2}$ is a conversion factor from mag $\operatorname{arcsec}^{-2}$ to physical units $L_{\odot} \mathrm{pc}^{-2}$ in the $V$-band. Assuming a fixed value of $\mathrm{BC}_{\mathrm{V}}=-0.85$ for every galaxy type has a 10 per cent internal accuracy, i.e. $\pm 0.1 \mathrm{mag}$, for a range of simple stellar population (SSP) models ranging from irregular to elliptical galaxies (Buzzoni et al. 2006).

The surface brightness profile can be expressed in terms of PN surface density $\tilde{\Sigma}(R)$ :
$\tilde{\mu}(R)=-2.5 \log _{10} \tilde{\Sigma}(R)+\mu_{0}$,
where $\mu_{0}$ is a function of the $\alpha_{2.1, \text { halo }}$ parameter:
$\mu_{0}=2.5 \log _{10} \alpha_{2.1, \text { halo }}+K+\left(\mathrm{BC}_{\odot}-\mathrm{BC}_{V}\right)$.
The value of $\mu_{0}$ is given by the value of the constant offset used in Eq. (5), and it can be fixed by fitting this offset between the observed logarithmic PN surface density and the surface brightness profile, $\mu_{V}$, at smaller radii ( $R \leq 6.8^{\prime}$ ). From the fitted offset of $\mu_{0}=16.0 \pm 0.1 \mathrm{mag}_{\operatorname{arcsec}}{ }^{-2}$, we compute the value for $\alpha_{2.1, \text { halo }}$ (Eq. (13)) resulting in $\alpha_{2.1, \text { halo }}=(0.63 \pm 0.08) \times 10^{-8} \mathrm{PN} L_{\odot, \text { bol }}^{-1}$. The error on the determined $\alpha_{2.1, \text { halo }}$ is computed from the propagation of the errors on the variables $\mu_{0}$ and $\mathrm{BC}_{V}$, the latter having a $10 \%$ accuracy.

In Fig. 8 we show the fit of the two component PN model to the observed PN logarithmic number density profile for $\alpha_{2.1, \text { ICL }} / \alpha_{2.1, \text { halo }}=3$ and a constant ICL surface brightness of $\mu_{\text {ICL }}=27.7 \mathrm{mag} \operatorname{arcsec}^{-2}$ (Mihos et al. 2005). The proposed model predicts a flatter slope for the PN logarithmic number density profile than the slope of the $V$-band surface brightness profile $\mu_{V}$, as observed. The fitted value for $\alpha_{2.1, \mathrm{ICL}}$ is then $\alpha_{2.1, \mathrm{ICL}}=(1.89 \pm 0.29) \times 10^{-8} \mathrm{PN} L_{\odot, \text { bol }}^{-1}$.

Equation (11) shows explicitly that when $\alpha_{2.1, \text { halo }}=\alpha_{2.1, \mathrm{ICL}}$ then the logarithmic PN number density profile should closely follow light.

The measured values of $\alpha_{2.1, \text { halo }}$ and $\alpha_{2.1, \text { ICL }}$ correspond, down to the survey depth, to an estimated $\sim 390$ halo PNs, and $\sim 310$ ICPNs in the completeness-corrected sample, and to $\sim 230$ halo PNs and $\sim 190$ ICPNs in the observed sample.

To compute $\alpha_{2.5}$ for a PN sample which is not complete to $m^{*}+2.5$, but only to a magnitude $m_{\mathrm{c}}<m^{*}+2.5$, then $\alpha_{2.5}$ is extrapolated by
$\alpha_{2.5}=\Delta_{m_{\mathrm{c}}} \times \alpha_{m_{\mathrm{c}}}$
where
$\Delta_{m_{\mathrm{c}}}=\frac{\int_{M^{*}+2.5}^{M^{*}} N(m) \mathrm{d} m}{\int_{m^{*}}^{m_{\mathrm{c}}} N(m) \mathrm{d} m}$.


Fig. 8. As in the top panel of Fig. 7 but with the modelled surface brightness profile from the two component photometric model superposed (dot-dashed black line). This modelled profile reproduces the flattening observed in the logarithmic number density well.

If we use the derived M 87 PNLF (see Sect. 5) to compute the cumulative number of PNs expected within 2.5 mag from the bright cut off, normalised to the cumulative number in the first 2.1 mag , we obtain $\Delta_{2.1} \simeq 1.7$. As a result, the predicted values of $\alpha_{2.5}$, for the halo and ICL components are $\alpha_{2.5 \text {,halo }}=\left(1.10_{-0.21}^{+0.17}\right) \times 10^{-8}$ $N_{\text {PN }} L_{\odot, \text { bol }}^{-1}$ and $\alpha_{2.5, \mathrm{ICL}}=\left(3.29_{-0.72}^{+0.60}\right) \times 10^{-8} N_{\mathrm{PN}} L_{\odot, \text { bol }}^{-0}$. The errors on the $\alpha_{2.5}$ values also take the uncertainty on the magnitude of the bright cutoff into account.

### 4.5. Comparison with previously determined $\alpha_{2.5}$ values

The $\alpha_{2.5}$ values for the M 87 halo and ICL were measured in previous works by Durrell et al. (2002) and Doherty et al. (2009). There are several assumptions that are made when computing these values, hence is important to address them before the actual numbers are compared. As already pointed out in the previous section, when $\alpha_{2.5}$ is computed for a PN sample which is not complete to $m^{*}+2.5$, then $\alpha_{2.5}$ is extrapolated by following Eq. (14).

In the studies of Durrell et al. (2002) and Doherty et al. (2009), the PN samples were complete one magnitude down the bright cutoff of the PNLF. Then, $\alpha_{2.5}$ was computed using the extrapolation on the basis of the analytic formula for $N(m)$ by Ciardullo et al. (1989).

In Sect. 5 we derive the M 87 PNLF in the brightest 2.5 mag range, which shows a steeper slope at $\sim 1.5$ mag below the cutoff than what is predicted by the analytical formula. If we use the observed PNLF then the cumulative number of PNs expected within 2.5 mag from the bright cut off, normalised to the cumulative number in the first magnitude, is about 2.7 times that predicted by the analytical PNLF. When comparing the actual values for the $\alpha_{2.5}$ measured by Durrell et al. (2002) and Doherty et al. (2009), they need to be rescaled by this fraction.

In the current work and in Doherty et al. (2009), $\alpha_{2.5}$ values were measured for the halo and ICL separately, using only the PNs associated with each component. In Doherty et al. (2009) the line-of-sight velocity of each PN was used to tag the PN candidate as M 87 halo or ICL. In Durrell et al. (2002) this information was not available. Following Doherty et al. (2009), only $58 \%$ of the PN candidates considered by Durrell et al. (2002) are truly ICL. When this correction is applied, then the value measured by Durrell et al. (2002) for the ICPNs is
$\alpha_{2.5, \text { ICL }}=1.3 \times 10^{-8} \mathrm{PN} L_{\odot, b o l}^{-1}$. If in addition we correct this $\alpha_{2.5}$ value for the ICL for the different shape of the PNLF, we get $\alpha_{2.5, \text { ICL,DU02 }}=3.6 \times 10^{-8} \mathrm{PN} L_{\odot, \text { bol }}^{-1}$. This value is $\sim 10 \%$ greater than ours, but consistent within the uncertainties and the contamination from continuum sources in the F03 catalogue (see Sect. 3.3).

When we correct the $\alpha_{2.5}$ values for halo and ICL from Doherty et al. (2009) by a factor 2.7, we obtain $\alpha_{2.5 \text {,halo,D09 }}=$ $8.4 \times 10^{-9} \mathrm{PN} L_{\odot, \text { bol }}^{-1}$ and $\alpha_{2.5, \mathrm{ICL}, \mathrm{D} 09}=1.9 \times 10^{-8} \mathrm{PN} L_{\odot, \text { bol }}^{-1}$. These values are smaller than ours, but consistent within the uncertainties and the colour/detection completeness corrections made here (see Sect. 4.1) but not in Doherty et al. (2009).

### 4.6. Implications of the measured $\alpha_{2.5}$ values

According to the analytical formula of Ciardullo et al. (1989) for the PNLF, $\alpha_{2.5}$ equals $\sim 1 / 10$ of the total luminosity-specific PN number $\alpha$ (see also Buzzoni et al. 2006), assuming that PNs are visible down to 8 mags from the bright cutoff (Ciardullo et al. 1989). If we use this analytical function to extrapolate the total number of PNs from 2.5 to 8 mag below the bright cutoff our measured values for $\alpha_{2.5}$ translate to total luminosityspecific PN numbers for the two components of $\alpha_{\text {halo }}=1.1 \times$ $10^{-7} \mathrm{PN} L_{\odot, b o l}^{-1}$ and $\alpha_{\text {ICL }}=3.3 \times 10^{-7} \mathrm{PN} L_{\odot}^{-1}$.bol . We can recast these numbers in terms of the PN visibility lifetime $\tau_{\text {PN }}$ through Eq. (8), assuming $B=1.8 \times 10^{-11} L_{\odot}^{-1} \mathrm{yr}^{-1}$ (Buzzoni et al. 2006). $\tau_{\text {PN }}$ is then $\simeq 6.1 \times 10^{3} \mathrm{yr}$ and $\simeq 18.3 \times 10^{3} \mathrm{yr}$ for the M 87 halo and ICL PNs. Note, that these would be lower limits, because at this stage we do not know whether the extrapolation from 2.5 mag below the cutoff to fainter magnitudes follows the analytical formula, or whether it is steeper.

Observationally there is some evidence that $\alpha$ is on average larger for bluer systems (Peimbert 1990; Hui et al. 1993). The measurements of the colour profile in M87 show a bluer gradient towards larger radii (Liu et al. 2005; Rudick et al. 2010): a fit of the colour profile along the major axis inside $1000^{\prime \prime}$ has a slope of -0.11 in $\Delta(B-V) / \Delta \log (R)$ (Rudick et al. 2010). The observed PN logarithmic number density profile measured in this work is consistent with the empirical result of a gradient towards bluer colours at large radii. In the proposed model, the gradient is caused by the increased contribution of ICL at large radii, which is bluer than the M87 halo population.

One can ask whether the metallicity of the parent stellar population may influence the number of PNs associated with a given bolometric luminosity. We are interested in population effects in the advanced evolutionary phases of stellar evolution, as the [OIII] $5007 \AA$ emission and its line width are weakly dependent on the chemical composition of the nebula (Dopita et al. 1992; Schönberner et al. 2010). For stellar populations with the same IMF and ages, Weiss \& Ferguson (2009) computed models for the asymptotic giant branch (AGB) for stars between 1.0 and $6.0 M_{\odot}$ with different metallicities. Their results show that the number of AGB stars varies with the chemical composition, because the latter effects the lifetime on the thermally pulsing AGB, with the longest lifetime obtained for metallicity between half and one tenth of $Z_{\odot}$. Given that the evolutionary path followed by a star from the end of the AGB to the beginning of the cooling phase of the central white dwarf corresponds to the planetary nebulae phase, it is suggestive to infer that stellar populations with metallicity -0.5 to -0.1 solar may have a larger number of PNs than stellar populations with solar metallicity or higher, for the same bolometric luminosity. The metallicities of ICL stars in the Virgo cluster core were measured by


Fig. 9. Top panel: luminosity function of the selected PNs in the outer regions of M 87, corrected for colour and detection incompleteness. The error bars show the $1 \sigma$ uncertainty from counting statistics. Data are binned into 0.3 mag intervals (see Table 5 for numerical values). The solid red line represents the analytical PNLF model for a distance modulus of 30.8 , convolved with photometric errors. The black line shows the Ly $\alpha$ LF from Gronwall et al. (2007), scaled to the effective surveyed volume of the M87SUB1 and M 87 SUB2 fields, with the shaded area showing the cosmic variance due to Ly $\alpha$ density fluctuations ( $\sim 20 \%$, see Sect. 3.2). Bottom panel: difference between the PNLF if we had used instead the automatically extracted sources without any final inspection. This plot shows that spurious detections affect mostly the two faintest magnitude bins.

Williams et al. (2007) using colour magnitude diagrams to be between -0.5 to -0.1 solar. If the stars in the M 87 halo have a higher metallicity, we might expect a variation of the luminosity specific PN number in the region of radii where the M 87 stellar halo and the ICL are superposed along the line-of-sight (Doherty et al. 2009), as is quantified for the first time in this work.

## 5. Planetary nebula luminosity function in the outer regions of M 87

### 5.1. PNLF

We can now use our large PN sample in the outer regions of M 87 to investigate the properties of the PNLF. To do this we need to take into account that the fraction of detected PNs on our scientific images can be affected by incompleteness, and that this incompleteness is a function of magnitude. As for the spatial completeness, we quantify this effect by adding a modelled sample of PNs on the scientific images and computing the fraction recovered by Sextractor of this input simulated PN population as function of magnitude (see Table 5 for values). In Fig. 9 we show the PNLF for the extracted candidates corrected for colour and detection incompleteness. We can compare this PNLF with the analytical formula by Ciardullo et al. (1989)
$N(M)=c_{1} \mathrm{e}^{c_{2} M}\left\{1-\mathrm{e}^{3\left(M^{*}-M\right)}\right\}$
where $c_{1}$ is a normalisation constant, $c_{2}=0.307$ and $M^{*}(5007)=-4.51 \mathrm{mag}$ is the absolute magnitude of the PNLF bright cutoff (Ciardullo et al. 1989). In Fig. 9 the red solid line shows the prediction from the analytical formula for a distance modulus of 30.8 , after convolution with photometric errors and normalisation to the brightest observed bins. The comparison of the derived PNLF with the analytical formula
shows two differences. First we detect one object with a $m_{5007}=$ 25.7 that is $\sim 0.6 \mathrm{mag}$ brighter than the expected cutoff for a distance modulus of 30.8 . Second we measure a slope in the PNLF at $\sim 1.5 \mathrm{mag}$ below the cutoff that is steeper than what is predicted by the analytical formula in this magnitude range (Ciardullo et al. 1989; Henize \& Westerlund 1963).

We discuss the significance of these deviations in turn.

Over-luminous source - Figure 9 also shows the comparison of the PNLF from our PN sample with the Ly $\alpha$ LF from Gronwall et al. (2007), scaled to our effective surveyed volume. The hatched range gives the uncertainty in the latter. We see that the bright end of the Ly $\alpha$ LF is consistent with the luminosity of the over-luminous object, within the photometric errors. Earlier suggestions that such overluminous objects could be due to a depth effect from Virgo ICL (Jacoby et al. 1990, C98) are not consistent with more recent studies of the ICL in Virgo; see Sect. 5.4. To definitively resolve the question of the nature of this object, whether it is a $\operatorname{Ly} \alpha$ emitter or an object in the M 87 halo, requires spectroscopic follow-up.

Steeper PNLF 1.5 mag below the bright cutoff - First, we carried out a Kolmogorov-Smirnov test to check whether our empirical PNLF can be drawn from the Ciardullo et al. (1989) analytical function, and this possibility is rejected. Next, because our sample covers $0.5^{\circ}$ in the M 87 halo, we can investigate the radial variation of the PNLF out to radii of $30^{\prime}$. We compute the PNLF for each of the three PN subsamples associated with the radial bins described in Sect. 4.1, correcting for colour and detection incompleteness, and subtracting the respective contribution from Ly $\alpha$ background objects. These are shown in the upper panel of Fig. 10, where the error bars also account for $\sim 20 \%$ cosmic variance in the Ly $\alpha$ density (see Sect. 3.2). We then compare the three PNLFs after normalisation to the total number of objects in each radial bin and carry out a Kolmogorov-Smirnov test to check whether they can result from the same underlying distribution. The probability that these three PNLFs are extracted from the same distribution is high, $P_{\mathrm{KS}}>99 \%$.

These results are significant because the steepening of the PNLF is thus shown to be present in all three radial bins, while we know that the ICPN population contributes mostly to the outermost bin, see discussion in Sect. 4.3, and that any residual contamination of Ly $\alpha$ background emitters is also largest in the outermost radial region. We also checked that the PNLFs in the two Suprime-Cam fields are similar; both show the steepening at faint magnitudes. Hence we must conclude that the observed steepening of the PNLF is an intrinsic property of the PN population (halo and ICL) in the outer regions of M 87.

### 5.2. Generalised analytical model for the PNLF and distance modulus of M87 halo

We determine the PNLF for the M 87 halo as follows. From the colour and detection corrected PNLF, shown in the top panel of Fig. 9, we subtract the expected contribution from Ly $\alpha$ emitters. Using the measured values of $\alpha_{2.5}$ for the M 87 halo and ICL PN population, we derive the fraction of PN in the M87 halo, using
$\frac{N_{\text {halo }}(m)}{N_{\text {tot }}(m)}=\frac{\alpha_{2.5, \text { halo }} L_{\text {halo }}}{\alpha_{2.5, \text { halo }} L_{\text {halo }}+\alpha_{2.5, \text { ICL }} L_{\text {ICL }}}=\frac{1}{1+3 \frac{L_{\text {CCL }}}{L_{\text {halo }}}}$


Fig. 10. Top panel: empirical PNLFs in three radial ranges corrected for colour and detection incompleteness: PN candidates within $6.5^{\prime}$ from M 87 centre - triangles, PN candidates between $6.5^{\prime}$ and $13.5^{\prime}$ from M 87 centre - diamonds, PN candidates in the outermost region (distances greater than $13.5^{\prime}$ ) - squares. The respective Ly $\alpha$ contribution expected in each radial bin was subtracted. Magnitudes are binned in 0.3 mag bins and the error bars represent the $1 \sigma$ uncertainty from counting statistics combined with the uncertainty from cosmic variance in the $\operatorname{Ly} \alpha$ density (see text for details). As before, the red solid line is the convolved analytical formula of Ciardullo et al. (1989) for distance modulus 30.8. Lower panel: same as for the upper plot, but now the three PNLFs are normalised at the total number of objects in each radial bin. The three data sets are consistent with being drawn from the same underlying distribution.
where $L_{\mathrm{ICL}}, L_{L_{\text {nalo }}}$ are given in Table 3 and $\alpha_{2.5, \mathrm{ICL}} / \alpha_{2.5 \text {,halo }}=3$. We show the PNLF of the halo of M87 in Fig. 11; error bars include Poisson statistics and a $20 \%$ cosmic variance of the Ly $\alpha$ density.

We now attempt to fit this PNLF with a generalised version of the analytical formula reported in Eq. (16). We continue to assume that the bright cutoff near $M^{*}$ is invariant for different PN populations, but we now allow for a free faint-end slope parameter $c_{2}$, in addition to varying the parameter $c_{1}$ equivalent to sample size. For the fit to the data we use robust non-linear least squares curve fitting, i.e., the IDL routine mpfit (Markwardt 2009), and account for the photometric errors. We derive the following values for the free parameters: $c_{1}=2017.2, c_{2}=1.17$ and $m^{*}=26.23$, for a reduced $\chi^{2}=1.01$. Figure 11 shows that


Fig. 11. Completeness-corrected PNLF for the M 87 halo (full dots) with magnitudes binned in 0.2 mag bins; error bars include Poisson statistics and $20 \%$ variance in the number of subtracted Ly $\alpha$ contaminants. The continuous line indicates the resulting fit of the generalised analytical formula Eq. (16), for the values of the free parameters given by $c_{1}=2017.2, c_{2}=1.17$ and a distance modulus of $m-M=30.74$. The generalised PNLF is convolved with the photometric errors.
this model is an excellent fit to the empirical PNLF for the halo of M87.

The fitted value of $m^{*}=26.23$ corresponds to a nominal distance modulus for M87 of $m-M=30.74 \mathrm{mag}$, or $D=14.1 \mathrm{Mpc}$. Since the generalised PNLF formula has not been calibrated and our candidates are not spectroscopically confirmed, we regard this as preliminary and do not give an error on $m-M$. This value for the distance modulus is $\sim 0.4$ mag brighter than that measured with the surface brightness fluctuation method, $31.18 \pm 0.07 \mathrm{mag}$ (Mei et al. 2007), and with the tip of the red giant branch, $31.12 \pm 0.14 \mathrm{mag}$ (Bird et al. 2010), which correspond to distances of $17.2 \pm 0.5 \mathrm{Mpc}$ and $16.7 \pm 0.9 \mathrm{Mpc}$.

### 5.3. Comparison of the PNLF in the M87 halo and in the M31 bulge

Here we compare the observed properties of the PNLF in M87 with the PNLF in the M31 bulge which was used to calibrate the analytical formula by C98. The PN population of the M31 bulge was studied in detail by Ciardullo et al. (1989); it has similar depth to our PNLF, i.e. it is complete 2.5 mag down the bright cutoff of the PNLF. Also, the stellar population in the M31 has similar metallicity, colour and stellar population age as the population in the inner $\sim 6^{\prime}$ of M 87; see Table 3 for a complete list of the parameters.

We take the PN samples for M31 and the halo of M 87 and normalise them by the sampled luminosity, then correct for the distance modulus. The results are shown in Fig. 12, where the PNLF for the halo of M 87 is shown before and after the subtraction of $\operatorname{Ly} \alpha$ contaminants. For the points where the $\mathrm{Ly} \alpha$ contribution is subtracted the error bars take a $\sim 20 \%$ cosmic variance of the Ly $\alpha$ density (see Sect. 3.2) into account. Within 1 mag of the bright cutoff, the M 87 PN population has fewer PNs than the PNLF of M31, i.e., the slope of the PNLF for the halo of M87 is steeper towards fainter magnitudes.

In old stellar populations, one expects the PN central stars to be dominated by low mass cores $M_{\text {core }} \leq 0.55 M_{\odot}$. Thus it
is plausible that the slope of the PNLF should be steeper than predicted by modelling the fading of a uniformly expanding homogeneous gas sphere ionised by a non-evolving star in a single PN (Henize \& Westerlund 1963). The comparison between the PNLFs of M 87 and M 31 may indicate that the M 87 halo hosts a stellar population with a larger fraction of low mass cores with respect to the M 31 bulge.

From observations, there is further evidence that the faint end slope of the luminosity function may depend on the parent stellar population. Ciardullo et al. (2004) reported that star-forming systems, like the disk of M33 and the Small Magellanic Cloud (SMC), have shallower slopes $\sim 1.5$ mags below the bright cutoff when compared to older stellar populations such as NGC 5128 or M31. These shallower slopes correspond to lower values of $c_{2}$ in Eq. (16).

### 5.4. Comparison with previous PNLF distance measurements for M87

We already referred in Sect. 3.3 to the work of C98 who carried out a PN survey in an area of $16^{\prime} \times 16^{\prime}$ centred on M87, and investigated the properties of the PNLF. F03 studied the properties of ICPNs in the Virgo ICL, including an area of $16^{\prime} \times 16^{\prime}$ centred 14.8' north of M87. Both surveys overlap with our current survey, but have a constant zero point offset $\Delta=0.3 \mathrm{mag}$ relative to our measured magnitudes (see discussion in Sect. 3.3).

Figure 13 compares the PNLFs of the matched subsamples common to our catalogue and those of C98 and F03, respectively. A residual zero point offset $\Delta=0.3$ mag has been applied to the C98 and F03 subsamples. With this zero point shift, the empirical PNLFs agree very well within one magnitude of the bright cutoff, and are consistent with a distance modulus of 30.8 . Without the zero point shift, the distance modulus obtained from the PNLFs of C98 and F03 would be 30.5. Thus the value obtained for our new M 87 halo PN sample (30.75), which is closer to other determinations (Sect. 5.2), indicates a systematic effect in the C98, F03 photometry, in the sense of brighter $m_{5007}$ in these samples. This systematic effect can explain and resolve some of the tension between the assumptions and results of C98, F03, and more recent findings on the spatial distribution of ICPNs in the Virgo cluster and the radial extension of the M87 halo, as discussed now.

C98 find that their empirical PNLF deviates from the analytical formula and link the deviations with the presence of an ICPN population uniformly distributed in the Virgo cluster volume. C98 assume that all PNs at distances larger than $R_{\text {iso }}>4.8^{\prime}$ from the centre of M 87 are ICPNs. Fitting a PNLF to this component, they derive that the ICPN population must extend 4 Mpc in front of M87; see Fig. 8 and its figure caption in C98 for further details. The depth effect, which is equivalent to a brightening of the PNLF by foreground ICPNs, places the near edge of the ICL population at a distance modulus of 30.3 , corresponding to a distance of 11 Mpc .

The assumptions of C98 on the membership of PNe at $R_{\text {iso }}>$ $4.8^{\prime}$ from M 87 to the ICL and on the spatial distribution of the ICL are not supported by the results of the spectroscopic followup of Arnaboldi et al. (2004) and the wide area ICPN survey by Castro-Rodríguez et al. (2009). The spectroscopic follow-up by Arnaboldi et al. (2004) showed that in the FCJ field of F03 at $14.8^{\prime}$ from the M 87 centre $87 \%$ of the PNs are bound to the M 87 halo, and only $13 \%$ are ICPNs. Thus the fraction of ICPNs in regions that are even closer to the centre, as in the $\mathrm{C} 98 R_{\text {iso }}>$ $4.8^{\prime}$, sample, will be down to a few $\%$. The wide area survey for ICPNs carried out by Castro-Rodríguez et al. (2009) shows

Table 3. Properties of the stellar populations in the bulge of M 31 and in the halo of M 87 .

| Name | Distance | $L_{\odot, \text { bol }}$ | $(B-V)_{0}$ | $[\mathrm{Fe} / \mathrm{H}]^{a}$ | $\alpha_{2.5}$ | Age $^{a}$ | Ref. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $(\mathrm{Mpc})$ | $L_{\odot, \text { bol }}$ |  |  |  | Gyr |  |
| M31 (bulge) | 0.76 | $6.5 \times 10^{9}$ | 0.95 | $\sim 0$ | $16.3 \times 10^{-9}$ | $>10$ | $(1)$ |
| M87 (halo) | 14.5 | $6.2 \times 10^{10}$ | 0.93 | $\sim 0$ | $8.2 \times 10^{-9}$ | $>10$ | $(2)$ |

Notes. ${ }^{(a)}$ Ratio $[\mathrm{Fe} / \mathrm{H}]$ and age from Saglia et al. (2010; M31) and Liu et al. (2005; M 87 ). M 87 [ $\left.\mathrm{Fe} / \mathrm{H}\right]$ and age analysis covers the first $400^{\prime \prime}$. References. (1) Buzzoni et al. (2006); (2) This work.


Fig. 12. Luminosity-normalised PNLFs for the bulge of M31 (triangles) and the halo of M 87 (circles). Open circles and filled circles represent, respectively, the PNLF of the halo of M 87 before and after subtraction of the expected number of $\mathrm{Ly} \alpha$ contaminants in each bin. Data are binned into 0.25 mag intervals. M 87 has a higher number of faint PNs per unit bolometric luminosity and its PNLF has a steeper slope towards faint magnitudes than M31.
that the ICL is associated with only the densest regions of the Virgo cluster, $\sim 0.4 \mathrm{Mpc}$ around M 87 . Hence the brightening of the PNLF expected due to foreground ICPNs is $<0.1$ mag. These results indicate that the C98 PNs at $R_{\text {iso }}>4.8^{\prime}$ are bound to the M 87 halo, with very limited contamination by ICL: thus they are at the distance of M87 and the brightening of the C98 sample is not caused by volume effects or a contamination by ICPNs. Similar arguments apply to the F03 PN sample.

We therefore conclude that the magnitudes for the C98, F03 PNs sample must be systematically too bright by 0.3 mag , and that our new photometry is reliable.

## 6. Summary and conclusions

We carried out a deep survey for planetary nebulas (PNs) in two wide fields of $34^{\prime} \times 27^{\prime}$, covering the halo of the cD galaxy NGC 4486 (M 87) in the Virgo cluster with Suprime-Cam at the Subaru telescope. Both fields were imaged through a narrowband filter centred at the redshifted [OIII] $\lambda 5007 \AA$ emission and a broad-band $V$ filter. The surveyed area covers the halo of M 87 out to a radial distance of 150 kpc . This is the largest survey so far for PNs in the M 87 halo in terms of number of detected PN candidates, depth and area coverage.

PN candidates were identified via the on-off band technique on the basis of automatic selection criteria using their narrowband colours and their two-dimensional light distributions. The


Fig. 13. Luminosity functions of the matched PN samples from this survey (filled circles), from C98 (top panel, green squares), and from F03 (bottom panel, cyan triangles). The error bars show the $1 \sigma$ uncertainty from counting statistics. Data are binned into 0.2 mag intervals. The solid red line represents the analytical PNLF model using a distance modulus of 30.8 , convolved with photometric errors. The magnitude range is driven by the magnitude limit of the C98 sample (top panel) and F03 sample (bottom panel). A zero point shift $\Delta=0.3$ mag relative to our sample was applied to both survey.
final photometric catalogue contains 688 objects, with a magnitude range extending from the apparent magnitude of the bright cutoff at Virgo distance down to 2.2 mag deeper.

We studied the radial number density profile of the PN candidates and compared it with the $V$-band surface brightness profile of the stellar light in the M 87 halo. The logarithmic PN number density profile shows good agreement with the $\mu_{\mathrm{V}}$ surface brightness profile within 13 ' from M 87's centre, but flattens at large radii. At the most distant point the difference to the prediction from the light profile is 1.2 mags. We investigated whether contributions from background Ly $\alpha$ emitters at redshift $z=3.1$ can be responsible for the flatter distribution. By using the Ly $\alpha$ LF from Gronwall et al. (2007) scaled to our effective surveyed volume, we constrained the $\operatorname{Ly} \alpha$ contribution to be $25 \% \pm 5 \%$ of the total sample over the whole surveyed area, and we concluded that it cannot explain the factor 3 more sources in the outer regions that are responsible for the flatter profile.

Stimulated by the early finding of Doherty et al. (2009) who determined different luminosity specific PN numbers for the M 87 halo light and the ICL, we propose a two component model for the PN population, with the ICL contributing a larger number of PNs per unit light. This composite model is consistent with the observed flattening of the logarithmic PN density profile when the luminosity specific PN numbers are $\alpha_{2.5 \text {,halo }}=\left(1.10_{-0.21}^{+0.17}\right) \times$ $10^{-8} N_{\mathrm{PN}} L_{\odot, \text { bol }}^{-1}$ and $\alpha_{2.5, \mathrm{ICL}}=\left(3.29_{-0.72}^{+0.60}\right) \times 10^{-8} N_{\mathrm{PN}} L_{\odot, \text { bol }}^{-1}$, for the M 87 halo and ICL population respectively.

Because of the large magnitude range of this PN survey, we were able to study the shape of the PNLF in detail and measured a steeper slope at faint magnitudes than what is expected from the analytical formula of Ciardullo et al. (1989). The fit of the generalised PNLF formula (Eq. (16)) to the empirical PNLF of the M 87 halo population gives faint-end slope of $c_{2}=1.17$ and a nominal distance modulus of 30.74 .

The depth of the current survey allowed us to carry out a comparison with the benchmark for PNLF studies, the M31 bulge. The comparison of the M 87 halo PNLF with the M31 bulge PNLF, when both are normalised by the sampled bolometric luminosity, shows that the former has fewer PNs at bright magnitudes, and a steeper slope towards the faint end. The steepening of the PNLF at fainter magnitudes is consistent with a larger fraction of PNs with low mass cores. PN evolution models and stellar population measurements at large radii will be needed to understand the stellar population effects that shape the PNLF of the M 87 halo.

Acknowledgements. We thank the on-site Subaru staff for their support and A. Aguerri and N. Castro-Rodriguez for helping with the routines that were used for the PNs catalogue extraction. We are also thankful to G. Bono and A. Weiss for helpful discussions on stellar evolution in the AGB phase, and to the referee for her/his comments which improved the paper. A.L. thanks J. Elliott, B. Agarwal and G. Avvisati for the support and helpful comments on the paper. M.A.R. would like to thank F. Makata for support in using the SuprimeCam Data Reduction (sdfred) pipeline. L.C. acknowledges funding from the European Community's Seventh Framework Programme (FP7/2007-2013/) under grant agreement No. 229517. This research has made use of the 2MASS catalogue data.

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Table 4. Number density and logarithm number density profile for the colour and spatial corrected sample of emission line objects.

| $R$ | $\frac{N_{\mathrm{c}}}{A}$ | $-2.5 \log _{10}\left(\frac{N_{\mathrm{c}}}{A}\right)+\mu_{0}$ | $C(R)$ |
| :--- | :---: | :---: | :---: |
| $\left(\operatorname{arcsec}^{1 / 4}\right)$ | $\left(N / \operatorname{arcsec}^{2}\right)$ | $\mathrm{mag} / \operatorname{arcsec}^{2}$ |  |
| 3.6 | $1.7 \times 10^{-3}$ | 22.9 | 0.55 |
| 3.9 | $1.5 \times 10^{-3}$ | 23.1 | 0.84 |
| 4.1 | $8.4 \times 10^{-4}$ | 23.7 | 0.91 |
| 4.2 | $6.0 \times 10^{-4}$ | 24.0 | 0.87 |
| 4.4 | $5.0 \times 10^{-4}$ | 24.2 | 0.87 |
| 4.6 | $5.2 \times 10^{-4}$ | 24.2 | 0.85 |
| 4.9 | $2.8 \times 10^{-4}$ | 24.9 | 0.86 |
| 5.1 | $1.8 \times 10^{-4}$ | 25.3 | 0.83 |
| 5.3 | $1.6 \times 10^{-4}$ | 25.5 | 0.86 |
| 5.6 | $1.2 \times 10^{-4}$ | 25.8 | 0.88 |
| 5.8 | $1.2 \times 10^{-4}$ | 25.8 | 0.88 |
| 6.0 | $7.4 \times 10^{-5}$ | 26.3 | 0.88 |
| 6.4 | $5.1 \times 10^{-5}$ | 26.7 | 0.91 |

Notes. The term $C_{R}$ is the spatial completeness factor as function of the distance from M 87's centre.
Table 5. PNLF for the colour and detection corrected sample of emission line objects.

| $m_{5007}$ | $\log _{10}($ N/bin $)$ | Colour completeness | Detection completeness |
| :---: | :---: | :---: | :---: |
| 25.7 | 0.6 | $100 \%$ | $85 \%$ |
| 26.0 | - | $75 \%$ | $85 \%$ |
| 26.3 | 1.6 | $70 \%$ | $90 \%$ |
| 26.6 | 2.1 | $88 \%$ | $90 \%$ |
| 26.9 | 2.3 | $85 \%$ | $90 \%$ |
| 27.2 | 2.6 | $85 \%$ | $90 \%$ |
| 27.5 | 2.7 | $98 \%$ | $90 \%$ |
| 27.8 | 2.9 | $81 \%$ | $80 \%$ |
| 28.1 | 3.0 | $66 \%$ | $80 \%$ |
| 28.4 | 2.9 | $43 \%$ | $40 \%$ |

Notes. The term Colour completeness represents the percentage of simulated PNs that we retrive with our colour selection, as function of the magnitude. The term Detection completeness represents the recovery fraction of an input simulated PN population as function of magnitude.


[^0]:    * Tables 4 and 5 are available in electronic form at http://www.aanda.org

[^1]:    1 Dark sky is an image of an empty field (off target) on the sky.
    2 The reference [OIII] and $V$-band exposures are the one used as reference images for the final image combination.
    ${ }^{3}$ http://www.jach.hawaii.edu/UKIRT/astronomy/exts.html

[^2]:    4 http://www.naoj.org/Observing/Instruments/SCam/ sdfred
    5 IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under cooperative agreement with the National Science Foundation.
    6 The astrometry accuracy of the [OIII] frames was improved by using the corresponding $V$-band image plate solution after being registered to the $V$-band image coordinate system. On/off images need to be registered on the same system due to the selection of PNs via colour excess (see Sect. 3.1).
    7 These values of $Z_{[0 I I I]}$ and $Z_{[V]}$ are consistent with those obtained by Castro-Rodríguez et al. (2009) where they analyze data collected with the Suprime-Cam at the Subaru telescope through the same filters: [OIII] narrow-band filter $\left(\lambda_{c}=5029 \AA \Delta \lambda=74 \AA\right)$, and broad-band $V$-filter $\left(\lambda_{\mathrm{c}}=5500 \AA \Delta \lambda=956 \AA\right)$.

[^3]:    ${ }^{8}$ In these simulations we adopted a Moffat $\beta=2.5$ profile to define the PSF of unresolved sources (see Sect. 2.2 for details) and an exponential LF similar to the one describing the PNLF in Ciardullo et al. (1998).

[^4]:    ${ }^{9}$ This area does not include the regions affected by high background noise and bad pixels (see Sect. 3.1.3).

