

# The role of sodium bicarbonate in the nucleation of noctilucent clouds

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**Abstract.** It is proposed that a component of meteoric smoke, sodium bicarbonate ( $\text{NaHCO}_3$ ), provides particularly effective condensation nuclei for noctilucent clouds. This assertion is based on three conditions being met. The first is that  $\text{NaHCO}_3$  is present at sufficient concentration ( $\approx 10^4 \text{ cm}^{-3}$ ) in the upper mesosphere between 80 and 90 km. It is demonstrated that there is strong evidence for this based on recent laboratory measurements coupled with atmospheric modelling. The second condition is that the thermodynamics of  $\text{NaHCO}_3(\text{H}_2\text{O})_n$  cluster formation allow spontaneous nucleation to occur under mesospheric conditions at temperatures below 140 K. The Gibbs free energy changes for forming clusters with  $n = 1$  and 2 were computed from quantum calculations using hybrid density functional/Hartree-Fock (B3LYP) theory and a large basis set with added polarization and diffuse functions. The results were then extrapolated to higher  $n$  using an established dependence of the free energy on cluster size and the free energy for the sublimation of  $\text{H}_2\text{O}$  to bulk ice. A 1-dimensional model of sodium chemistry was then employed to show that spontaneous nucleation to form ice particles ( $n > 100$ ) should occur between 84 and 89 km in the high-latitude summer mesosphere. The third condition is that other metallic components of meteoric smoke are less effective condensation nuclei, so that the total number of potential nuclei is small relative to the amount of available  $\text{H}_2\text{O}$ . Quantum calculations indicate that this is probably the case for major constituents such as  $\text{Fe}(\text{OH})_2$ ,  $\text{FeO}_3$  and  $\text{MgCO}_3$ .

**Key words:** Atmospheric composition and structure (aerosols and particles; cloud physics and chemistry; middle atmosphere – composition and chemistry)

## Introduction

Noctilucent clouds (NLC) occur at high latitudes in the summer mesosphere, when the temperature falls below 150 K (e.g. Seele and Hartogh, 1999; Lübken, 1999). Water vapour, which is present at mixing ratios of only a few parts per million above 80 km, is then able to condense on available nuclei to form particles that can grow to more than 20 nm in radius, when they can be observed by lidar (e.g. von Cossart *et al.*, 1999) and also become optically visible (Thomas, 1991). Meteor ablation has been proposed as a major source of condensation nuclei, and two distinct types of nuclei have been considered. First are clusters of  $\text{H}_2\text{O}$  around metallic ions such as  $\text{Fe}^+$ ,  $\text{Mg}^+$  and  $\text{Na}^+$ , which then undergo successive hydration with falling temperature (Witt, 1969). A difficulty with this nucleation source has recently emerged from kinetic studies of the mechanisms which neutralize metallic ions in the upper mesosphere (Cox and Plane, 1998; Rollason and Plane, 1998; Plane *et al.*, 1999b). These studies have shown that metallic ions should be rapidly neutralized below 95 km by forming molecular ions which undergo dissociative recombination with electrons. Indeed, the predicted depletion of metallic ions below 95 km has been confirmed by rocket-borne mass spectrometry (e.g., Kopp, 1997). Hence, it is unlikely that metallic ions are a major source of condensation nuclei. On the other hand, proton hydrates of the form  $\text{H}^+(\text{H}_2\text{O})_n$  sometimes occur at sufficiently high concentrations below 90 km to play a role in NLC formation (Balsiger *et al.*, 1996). However, Reid (1990) has shown that the observed electron “bite-outs” in NLC layers are not consistent with an ion nucleation mechanism.

The second type of condensation nucleus that has been proposed is meteoric “smoke” particles (Hunten *et al.*, 1980). Although this term conjures up the image of particles being produced directly in the trail of an ablating meteoroid, this is rarely the case because the median mass of incoming meteoroids is only about 10  $\mu\text{g}$

(Hunten *et al.*, 1980). When such small particles ablate, the resulting concentration of metal atoms, ions and oxides is too low for coagulation to compete with the outward diffusion of the meteor trail (Rosinski and Snow, 1961). Hence, a typical trail loses its identity completely, diffusing into the background atmosphere before any significant coagulation occurs. Recognizing this fact, Hunten *et al.* (1980) assumed that the lower limit to the smoke particle size is a molecular radius of 2 Å. These workers constructed a meteoric dust model which included a fairly detailed treatment of ablation, particle coagulation and sedimentation. This model showed that most ablation occurred between 80 and 90 km, and that coagulation did not significantly reduce the concentration of the smallest particles until below 80 km. Although more recent work (e.g. Taylor, 1995) indicates that the average meteoroid velocity of 14.5 km s<sup>-1</sup> assumed by Hunten *et al.* (1980) was too low by about a factor of 2 (and hence the peak ablation altitude is actually around 95 km), this should not greatly affect the conclusions of the earlier study. The implication is that if smoke particles do provide condensation nuclei for NLC at the summer mesopause around 88 km, then these particles are either individual molecules or small macromolecules less than 10 Å in radius.

The purpose of the present work is to begin to explore the nature of these smoke particles. Here the case will be made for sodium bicarbonate (NaHCO<sub>3</sub>) being an important nucleating agent. To establish this, the following questions need to be addressed. First, is NaHCO<sub>3</sub> present in the upper mesosphere in sufficient concentrations? Second, do the thermodynamics for NaHCO<sub>3</sub> clustering with H<sub>2</sub>O allow spontaneous nucleation to occur within the ranges of humidity and temperature that characterize the high-latitude summer mesopause? Third, what about other metallic species formed from meteoric ablation, are there in fact too many nucleating agents available, thus preventing particles growing to the optically visible range that give rise to NLC? These questions will now be considered in turn.

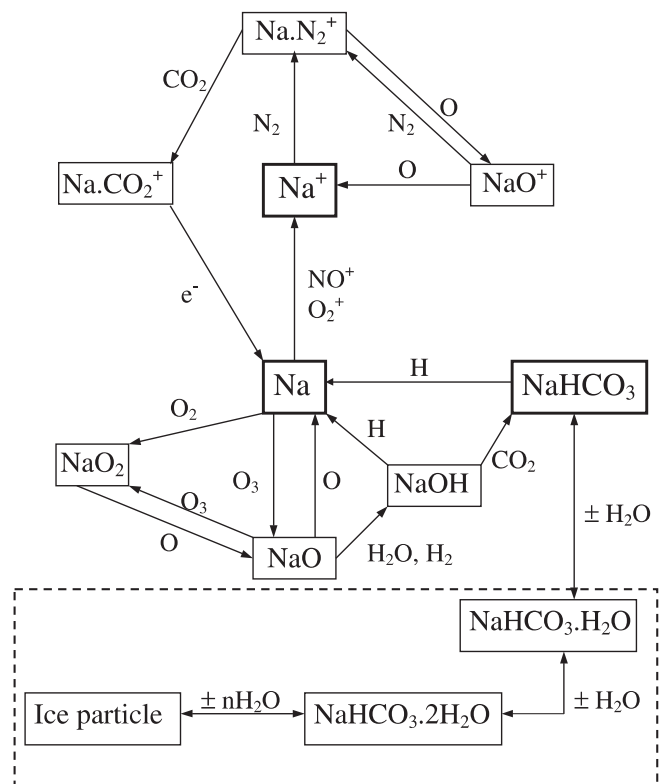
Before doing so, the author would like to acknowledge the significant contribution that Professor Lance Thomas has made in three areas relevant to this paper. First, Professor Thomas played an important role in the early development of the sodium resonance fluorescence lidar (Gibson *et al.*, 1979) while working at the Rutherford Appleton Laboratory. Later at the University of Wales at Aberystwyth, his group developed a model of the mesospheric Na layer that showed for the first time that the characteristic features of the layer could be explained by the gas-phase chemistry of sodium alone (Thomas *et al.*, 1983). Most recently, his group have been active in studying the phenomenon of mesospheric summer echoes, which are closely related to NLC (Thomas *et al.*, 1996).

### NaHCO<sub>3</sub> in the mesosphere

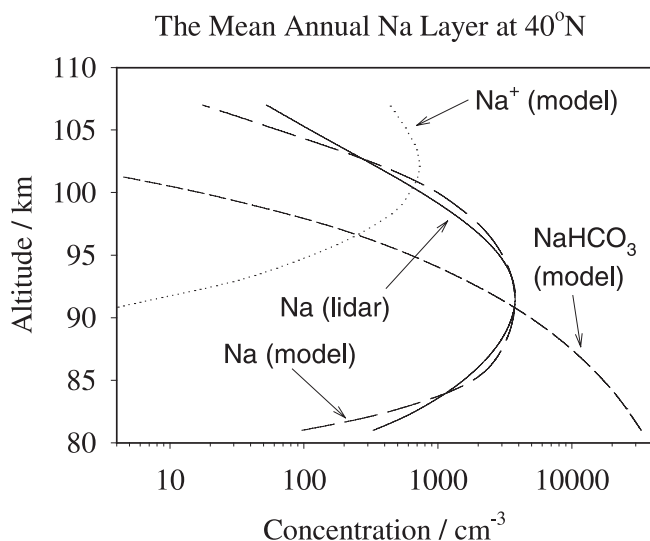
The only sodium species that can be observed directly in the upper atmosphere are atomic Na, measured by lidar

since the advent of the tunable dye laser (e.g. Gibson *et al.*, 1979; Plane *et al.*, 1998, 1999a), and Na<sup>+</sup> ions, detected by rocket-borne mass spectrometry (e.g. Kopp, 1997). Thus the molecular forms of sodium have to be inferred from chemical/transport models (e.g. Thomas *et al.*, 1983; Plane, 1991; McNeil *et al.*, 1995; Plane *et al.*, 1998, 1999a, b). Figure 1 is a schematic drawing of the important chemistry that sodium is known to undergo in the upper mesosphere. Apart from the reactions enclosed by the dashed line (which are the subject of the present study), all of these reactions have been studied as isolated processes in the laboratory, and most of their rate coefficients have been measured at temperatures around 200 K (e.g. Ager and Howard, 1987; Plane and Helmer, 1994; Plane *et al.*, 1999a, b). This applies in particular to the sequence of reactions that convert atomic Na to NaHCO<sub>3</sub> via NaO and NaOH.

Rajasekhar and Plane (1993) demonstrated using ab initio quantum theory that NaHCO<sub>3</sub> should be a relatively stable molecule in the mesosphere, since its only exothermic reaction is with atomic H. Plane *et al.* (1999b) have recently confirmed experimentally that this reaction does occur very slowly at low temperatures, as required by sodium models: if there were not a path for breaking down NaHCO<sub>3</sub> to Na, the atomic Na layer could not be sustained below 95 km.



**Fig. 1.** Schematic drawing of the important chemistry of sodium in the upper mesosphere (NaO<sub>3</sub> and NaCO<sub>3</sub> are not included for the sake of clarity). The major sodium species are in the *thick-edged boxes*. The cluster reactions between NaHCO<sub>3</sub> and H<sub>2</sub>O, that are proposed to occur at the cold summer mesopause, are surrounded by the *dashed line*



**Fig. 2.** Annual mean profiles of Na, Na<sup>+</sup> and NaHCO<sub>3</sub> predicted by the UEA 1D sodium model at 40°N. The modelled Na layer is compared with the average from a 3-year set of lidar observations (Plane *et al.*, 1999a)

Figure 2 illustrates the annual average profiles of the major sodium species between 80 and 110 km, predicted by the UEA sodium model (Plane *et al.*, 1999a) for mid-latitude conditions at 40°N (this will be contrasted later with the cold summer mesopause at high latitudes). The Na layer peaks at about 90 km, in good agreement with a very large data base of lidar observations (Plane *et al.*, 1999a). Na<sup>+</sup> is the dominant species in the lower thermosphere, and NaHCO<sub>3</sub> in the upper mesosphere. Note that the predicted NaHCO<sub>3</sub> concentration at 85 km is about 10<sup>4</sup> cm<sup>-3</sup>, an order of magnitude larger than the concentration of meteoric smoke particles that appears to be required to nucleate a visible NLC with an ice particle concentration of about 100 cm<sup>-3</sup> (Jensen and Thomas, 1991). This sodium model has now been shown to reproduce in detail the observed seasonal and latitudinal variations of the Na layer (Plane *et al.*, 1998, 1999a). It therefore seems reasonable to conclude that NaHCO<sub>3</sub> is the major sodium reservoir immediately below the Na layer peak at 90 km, and that its concentration should be sufficient to provide a significant source of condensation nuclei.

### Thermodynamics of NaHCO<sub>3</sub>-water clusters

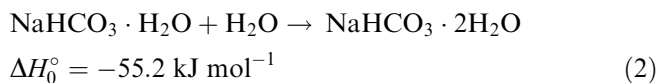
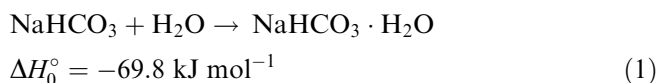
Although solid NaHCO<sub>3</sub> is quite hygroscopic and is highly soluble in bulk water, there appears to be no information concerning the thermodynamics of clusters formed between isolated NaHCO<sub>3</sub> and H<sub>2</sub>O molecules in the gas phase. This deficiency was addressed here by carrying out high-level quantum theory calculations using hybrid density functional/Hartree-Fock (B3LYP) theory, within the GAUSSIAN 98 set of programmes (Frisch *et al.*, 1998). The large, flexible 6-311+G(2d,p) basis set was employed, which has both polarization and diffuse functions added to the atoms. This combination

of theory and basis set was chosen because theoretical estimates of the thermochemistries for a wide variety of reactions compare well with experimental measurements (see later) (Foresman and Frisch, 1996). The geometries of NaHCO<sub>3</sub>, NaHCO<sub>3</sub> · H<sub>2</sub>O and NaHCO<sub>3</sub> · 2H<sub>2</sub>O were first optimized at the B3LYP/6-311+G(2d,p) level. The vibrational frequencies of each species were then calculated, since these are required both to make zero-point-energy corrections to the cluster binding energies, and to compute the binding entropies.

Calculations on clusters containing more than two H<sub>2</sub>O were not attempted because at this level of theory these become very expensive in computer resources. In order to benchmark the theory, calculations were also carried out on NaOH, H<sub>2</sub>O and CO<sub>2</sub>, for which there is experimental data on their respective geometries, dipole moments and vibrational frequencies. As shown in Table 1, there is in general excellent agreement. The greatest discrepancies are in the vibrational frequencies of NaOH; however, the experimental frequencies were determined in a matrix isolation study, and the frequencies of the isolated molecule could be significantly shifted compared to the matrix environment.

The optimised geometries of NaHCO<sub>3</sub> and the first and second H<sub>2</sub>O clusters are illustrated in Fig. 3, and their molecular parameters are listed in Table 2. There are several points to note. First, NaHCO<sub>3</sub> is highly ionized with a large dipole moment of nearly 7 Debye, so that the clustering reaction with H<sub>2</sub>O will be enhanced by a strong dipole-dipole interaction. Second, the two H<sub>2</sub>O molecules are bound directly to the Na atom, which has a Mulliken charge of +0.65, and the binding is further stabilized by hydrogen bonds with the bicarbonate anion (shown as broken lines in Fig. 3). Third, even after the addition of two H<sub>2</sub>O molecules, the cluster still has a large dipole moment which should facilitate its further growth. A final point is that the assumption of Hunten *et al.* (1980) that the initial smoke particles above 80 km would have a radius of 2 Å is not a bad approximation to the spherically-averaged dimensions of NaHCO<sub>3</sub>.

The computed binding energies of the clusters are then:

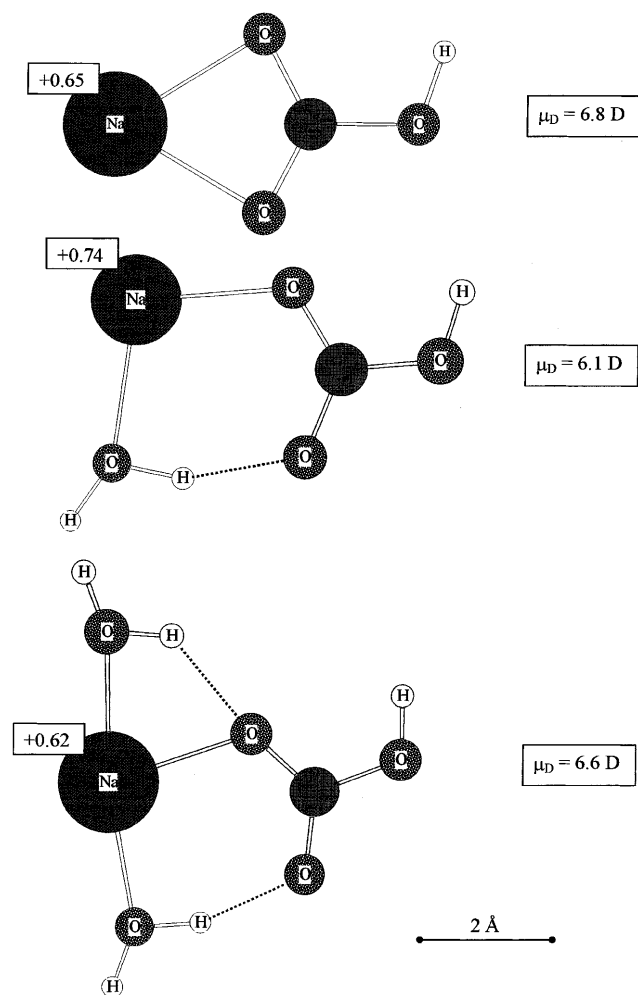


The uncertainty in these energies is probably around ±12 kJ mol<sup>-1</sup> (95% confidence level) at this level of theory, based on a comparison of experimental and theoretical thermochemistries for a wide range of molecules (Foresman and Frisch, 1996). These binding energies are quite large, and are a significant fraction of the first and second binding energies of H<sub>2</sub>O to bare Na<sup>+</sup> ions ( $\Delta H_{298}^\circ = -100.3$  and  $-82.8$  kJ mol<sup>-1</sup>, respectively (Džidić and Kebarle, 1970)).

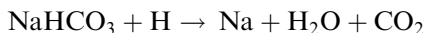
These theoretical results can also be used to estimate the enthalpy changes for the reaction of atomic H with

**Table 1.** Calculated molecular parameters at the B3LYP/6-311+G(2d,p) level of theory for NaOH, H<sub>2</sub>O and CO<sub>2</sub>. For comparison, experimental values are shown in parenthesis

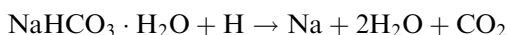
Species	Geometry <sup>a</sup>	Dipole moment <sup>b</sup>	Rotational constants <sup>c</sup>	Vibrational frequencies <sup>d</sup>
NaOH	$r_{\text{Na-O}} = 1.95$ (1.95 <sup>e</sup> ) $r_{\text{O-H}} = 0.95$ , linear	6.58 (6.83 <sup>f</sup> )	12.61 (12.57 <sup>f</sup> )	214 (337 <sup>g</sup> ) (x2), 565 (431 <sup>g</sup> , 437 <sup>h</sup> ), 3966 ( $\approx$ 3600 <sup>g</sup> )
H <sub>2</sub> O	$r_{\text{O-H}} = 0.96$ (0.96 <sup>i</sup> ) $\angle_{\text{H-O-H}} = 105.2$ (104.5 <sup>i</sup> )	2.08 (1.85 <sup>j</sup> )	826 (842 <sup>j</sup> ), 428 (438 <sup>j</sup> ), 282 (280 <sup>j</sup> )	1618 (1594 <sup>i</sup> ), 3812 (3651 <sup>i</sup> ), 3917 (3756 <sup>i</sup> )
CO <sub>2</sub>	$r_{\text{C-O}} = 1.16$ (1.16 <sup>i</sup> ), linear	0.0	11.73 (11.75 <sup>j</sup> )	677 (667 <sup>i</sup> ) (x2), 1363 (1385 <sup>i</sup> ), 2400 (2349 <sup>i</sup> )

<sup>a</sup> Bond length in Å, bond angle in degrees<sup>b</sup> In Debye (=  $3.336 \times 10^{-30}$  cm)<sup>c</sup> In GHz<sup>d</sup> In  $\text{cm}^{-1}$ <sup>e</sup> Kuijpers *et al.* (1976)<sup>f</sup> Kawashima *et al.* (1996)<sup>g</sup> Acquista and Abramowitz (1969)<sup>h</sup> Spinar and Margrave (1958)<sup>i</sup> Chase *et al.* (1985)<sup>j</sup> Lide (1998)**Fig. 3.** Geometries and dipole moments ( $\mu_D$ ) of NaHCO<sub>3</sub> and the first and second H<sub>2</sub>O clusters, calculated at the B3LYP/6-311+G(2d,p) level of theory. All structures are planar. The dark shaded atomic centre is carbon

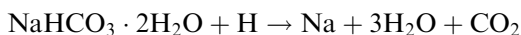
NaHCO<sub>3</sub> and the H<sub>2</sub>O clusters (note that the reactions of NaHCO<sub>3</sub> with other radical species such as OH and O are quite endothermic and will not occur in the mesosphere (Rajasekhar and Plane, 1993)):



$$\Delta H_0^\circ = -59.2 \text{ kJ mol}^{-1} \quad (3)$$



$$\Delta H_0^\circ = +10.6 \text{ kJ mol}^{-1} \quad (4)$$



$$\Delta H_0^\circ = +65.8 \text{ kJ mol}^{-1} \quad (5)$$

These results demonstrate that NaHCO<sub>3</sub> · 2H<sub>2</sub>O (and the higher clusters) should not undergo chemical reaction in the mesosphere (other than the addition or loss of H<sub>2</sub>O), and this may also apply to the first H<sub>2</sub>O cluster. That is, once these clusters start to form, their stability will only be governed by the temperature and to a lesser extent the mixing ratio of H<sub>2</sub>O.

The equilibrium constants  $K_1$  and  $K_2$  can now be calculated by statistical mechanics using the data in Table 2. Inspection of this table shows that both the first and second H<sub>2</sub>O clusters have several vibrational modes with frequencies below 100  $\text{cm}^{-1}$ . These modes really correspond to hindered internal rotations of the H<sub>2</sub>O molecules against the NaHCO<sub>3</sub>. However, treating them in the limit as free rotors (Benson, 1968) rather than harmonic oscillators produced very little difference in the calculated values of  $K_1$  and  $K_2$  over the temperature range of 130–220 K. Hence, the rotational and vibrational partition functions were calculated assuming that the clusters are rigid rotors and that all vibrations are harmonic. This yields:

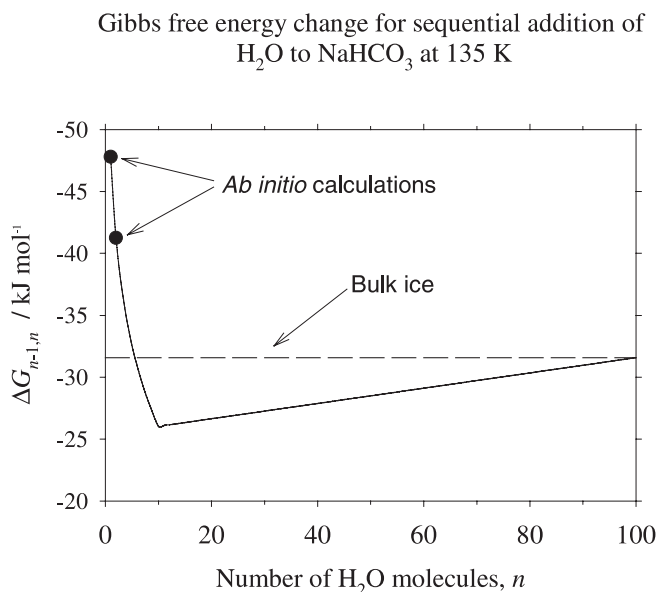
$$K_1(T) = 2.22 \times 10^{-26} \exp(7590/T) \text{ cm}^3 \text{ molecule}^{-1}$$

$$K_2(T) = 3.81 \times 10^{-26} \exp(5890/T) \text{ cm}^3 \text{ molecule}^{-1}$$

The equilibrium constants  $K_n$  for  $n \geq 3$  can now be estimated by analogy with the hydration thermodynamics of metallic ions, where the Gibbs free energy for addition of the  $n$ th H<sub>2</sub>O,  $\Delta G_{n-1,n}$ , is proportional to  $\log n$  up to about  $n = 10$  (Džidić and Kebarle, 1970). This is illustrated for the present case in Fig. 4, which is a plot of  $\Delta G_{n-1,n}$  versus  $n$  at a temperature of 135 K. At higher  $n$ ,  $\Delta G_{n-1,n}$  becomes more negative again and tends in the limit to the free energy of sublimation for H<sub>2</sub>O on bulk

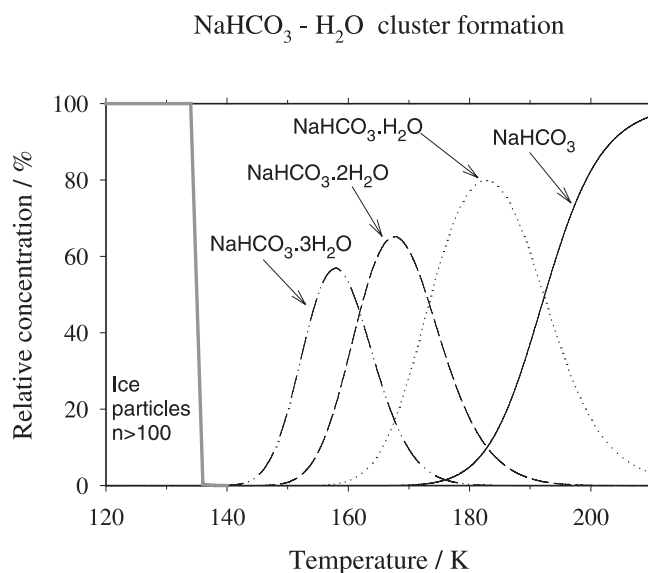
**Table 2.** Calculated molecular parameters at the B3LYP/6-311+G(2d,p) level of theory for  $\text{NaHCO}_3$ ,  $\text{NaHCO}_3 \cdot \text{H}_2\text{O}$  and  $\text{NaHCO}_3 \cdot 2\text{H}_2\text{O}$ . The geometries and dipole moments are contained in Fig. 3

Species	Rotational constants <sup>a</sup>	Vibrational frequencies <sup>b</sup>
$\text{NaHCO}_3$	12.29, 3.34, 2.63	112, 247, 333, 570, 581, 700, 833, 1008, 1237, 1389, 1659, 3802
$\text{NaHCO}_3 \cdot \text{H}_2\text{O}$	5.53, 1.95, 1.44	67, 85, 86, 132, 263, 320, 332, 571, 610, 636, 702, 829, 976, 1010, 1246, 1381, 1659, 1707, 2802, 3804, 3917
$\text{NaHCO}_3 \cdot 2\text{H}_2\text{O}$	2.33, 1.57, 0.94	30, 69, 79, 83, 98, 130, 153, 207, 250, 288, 351, 487, 533, 582, 603, 620, 696, 825, 947, 1015, 1237, 1377, 1617, 1673, 1717, 2915, 3618, 3815, 3913, 3915

<sup>a</sup> In GHz<sup>b</sup> In  $\text{cm}^{-1}$ **Fig. 4.** Hypothetical dependence of  $\Delta G_{n-1,n}$ , the Gibbs free energy for the addition of the  $n$ th  $\text{H}_2\text{O}$  to a  $\text{NaHCO}_3(\text{H}_2\text{O})_{n-1}$  cluster, as a function of  $n$  at 135 K.  $\Delta G_{0,1}$  and  $\Delta G_{1,2}$  are derived from the present ab initio quantum calculations. The value for bulk ice is extrapolated from the measurements of Marti and Mauersberger (1993)

ice (Marti and Mauersberger, 1993). In Fig. 4 this is assumed arbitrarily to occur at  $n = 100$ .

A free energy dependence of this form has the following important property. The addition of  $\text{H}_2\text{O}$  becomes increasingly less favourable up to  $n = 10$  (in this case). However, if the temperature is low enough (or  $[\text{H}_2\text{O}]$  high enough) to reach this point, then the subsequent addition of  $\text{H}_2\text{O}$  becomes more and more favourable, causing spontaneous growth and the formation of ice particles. This is illustrated in Fig. 5, which shows the relative equilibrium concentrations of  $\text{NaHCO}_3$ , the first three  $\text{H}_2\text{O}$  clusters, and “ice particles” (defined as  $n > 100$ ), plotted as a function of temperature from 120 to 220 K. The  $\text{H}_2\text{O}$  mixing ratio is fixed at 3 ppm, typical of the high-latitude summer mesopause (Seele and Hartogh, 1999).  $\text{NaHCO}_3$  is the dominant form above 190 K; at lower temperatures, successively higher  $\text{H}_2\text{O}$  clusters dominate the equilibrium population, until spontaneous growth occurs at about 137 K. Note that the temperature at which this runaway nucleation occurs is sensitive to the turning point in

**Fig. 5.** Equilibrium populations of  $\text{NaHCO}_3$  and a selection of  $\text{NaHCO}_3(\text{H}_2\text{O})_n$  clusters ( $n = 1, 2, 3$  and  $> 100$ ), as a function of temperature. The  $\text{H}_2\text{O}$  mixing ratio is constant at 3 ppm

the plot of  $\Delta G_{n-1,n}$  versus  $n$  (Fig. 4). The value of  $n = 10$  was chosen here for illustrative purposes because there is a large body of evidence that the temperature in the 85–90 km height range must fall below 140 K for NLC to form [e.g., Seele and Hartogh, 1999].

To explore the likely cluster populations in the high latitude summer mesosphere, the thermodynamics of these cluster reactions were incorporated into the UEA 1-dimensional sodium model by making the following approximations. First, it was assumed that only the first cluster,  $\text{NaHCO}_3 \cdot \text{H}_2\text{O}$ , is able to react with H, with a rate coefficient arbitrarily set to that of  $\text{NaHCO}_3 + \text{H}$  [Plane *et al.*, 1999a]. Second, because the rate of addition and loss of  $\text{H}_2\text{O}$  from the clusters is likely to be much faster than the rate of formation of  $\text{NaHCO}_3$  from Na or the reverse, the clusters were assumed to be in a quasi-equilibrium with  $\text{NaHCO}_3$ .

The model was then run for conditions of 70°N in July [Plane *et al.*, 1998]. A new temperature profile obtained from falling sphere measurements at Andoya (69°N) [Lübken, 1999] was used, where the mesopause was found to occur at 88 km with a temperature of 129 K. Note that the use of a climatological temperature profile is appropriate here, since the aim of this study is



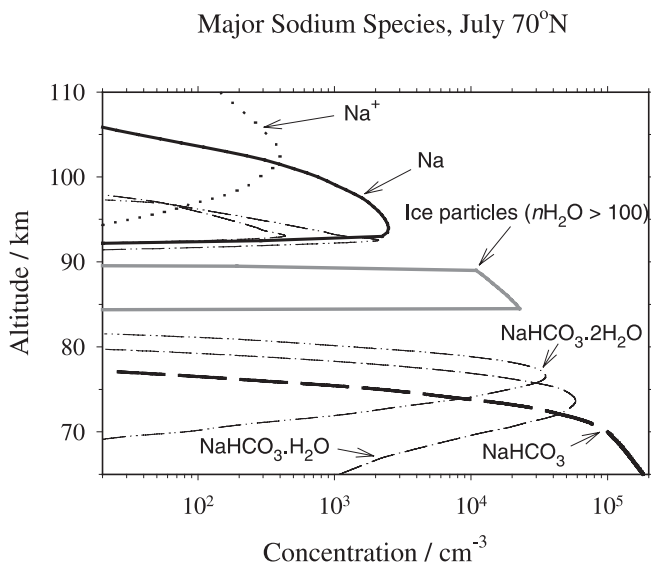


Fig. 6. Profiles of Na,  $\text{Na}^+$ ,  $\text{NaHCO}_3$ , and  $\text{NaHCO}_3(\text{H}_2\text{O})_n$  clusters ( $n = 1, 2$  and  $>100$ ), predicted by the 1D sodium model for early July at  $70^\circ\text{N}$

to establish whether the free energy of  $\text{NaHCO}_3$ -water cluster formation is of the right order to allow particle growth under summer mesopause conditions. Future studies could address the role of short-term cooling induced by gravity waves in triggering nucleation.

The modelled profiles of Na,  $\text{Na}^+$ ,  $\text{NaHCO}_3$  and the clusters are illustrated in Figure 6. The peak of the Na layer is now at 92.5 km, in accord with lidar observations at several high latitude stations [Gardner *et al.*, 1988; Kurzawa and von Zahn, 1990; Plane *et al.*, 1998]. Note that this is significantly higher than at mid-latitudes (cf. Figure 2). Another contrast with the mid-latitude case is that  $\text{NaHCO}_3$  only occurs as a free molecule below 80 km (although it will eventually polymerise with itself and other metallic compounds, a process that is not included in the present model). Above 80 km  $\text{NaHCO}_3$  is clustered with  $\text{H}_2\text{O}$ , and runaway nucleation is predicted to occur in a layer between 84 and 89 km. Models of NLC (e.g. Jensen and Thomas, 1991) require nucleation at this height, followed by sedimentation of the growing ice particles to around 83 km, where visible NLC are observed. Finally, the very steep underside of the Na layer, and the gap of 2–3 km between the Na and NLC layers (Fig. 6), are in excellent agreement with the lidar observations of Hansen *et al.* (1989).

### Presence of other metallic species

The most abundant metals in meteoroids are Fe and Mg (Plane, 1991). Fe appears to ablate quite efficiently, giving rise to an observable atomic Fe layer peaking at about 85 km (Helmer *et al.*, 1998). Recent laboratory studies (Plane *et al.*, 1999b) have shown that the two likely stable reservoirs of iron above 80 km are  $\text{FeO}_3$ , which forms most rapidly, and  $\text{Fe}(\text{OH})_2$ , which is the most stable thermodynamically. Figure 7 illustrates the

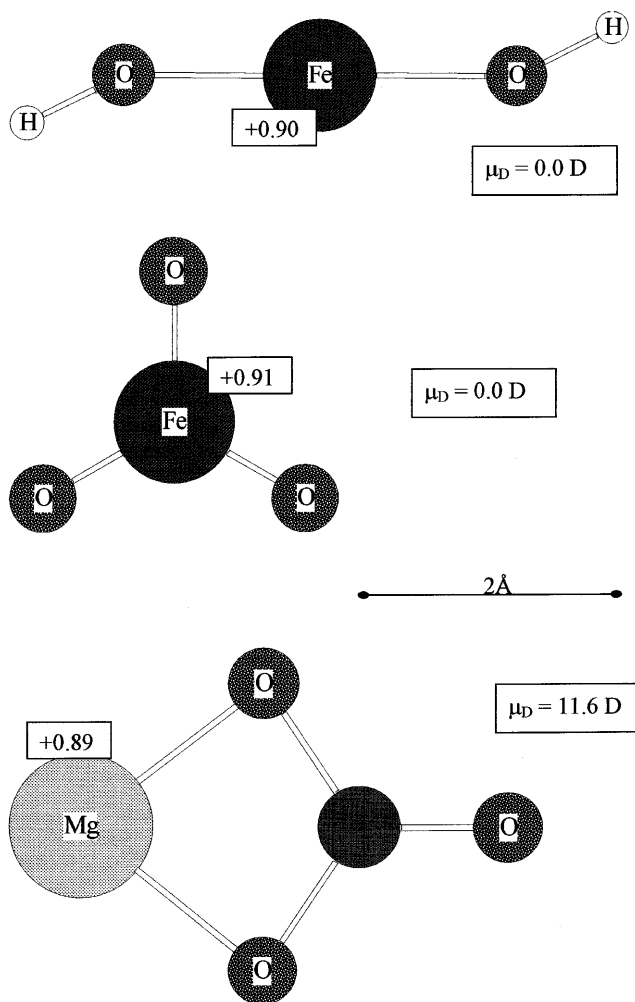


Fig. 7. Geometries and dipole moments ( $\mu_D$ ) of  $\text{Fe}(\text{OH})_2$ ,  $\text{FeO}_3$  and  $\text{MgCO}_3$ , calculated at the B3LYP/6-311 + G(2d,p) level of theory. All structures are planar. The dark shaded atomic centre is carbon

calculated geometries of these species at the B3LYP/6-311 + G(2d,p) level of theory. These molecules have zero dipole moments, so that they are unlikely to bind strongly to  $\text{H}_2\text{O}$  and act as effective condensation nuclei.

In the case of Mg, recent laboratory studies by R. J. Rollason and the author have shown that  $\text{MgCO}_3$  will form readily above 80 km from the recombination of  $\text{MgO}$  and  $\text{CO}_2$ . The calculated geometry of this species is also illustrated in Fig. 7. Note that the molecule has a huge dipole moment of 11.6 Debye, which should make it an excellent condensation nucleus. However, when a water molecule actually approaches  $\text{MgCO}_3$ , further quantum calculations (at the B3LYP/6-311 + G(2d,p) level) reveal that the electrostatic forces are large enough to effect a chemical reaction, producing  $\text{Mg}(\text{OH})_2$  and  $\text{CO}_2$ . The dihydroxide has the same linear structure as  $\text{Fe}(\text{OH})_2$  (Fig. 7), with a zero dipole moment, and is therefore a less effective nucleus. In any case, the absence of an observed layer of atomic Mg in the mesosphere implies that this metal does not ablate efficiently from meteoroids (Plane and Helmer, 1995), as is also the case for Ca (McNeil *et al.*, 1998).

## Conclusions

This study has attempted to show that there is a *prima facie* case for  $\text{NaHCO}_3$ , a component of meteoric smoke, being a particularly effective condensation nucleus for NLC. This assertion is based on the following points: that there is strong evidence for the presence of  $\text{NaHCO}_3$  at sufficient concentrations in the upper mesosphere; that the thermodynamics for  $\text{NaHCO}_3(\text{H}_2\text{O})_n$  cluster formation allow spontaneous nucleation to occur under mesospheric conditions at temperatures below 140 K; and that other metallic compounds are probably less effective condensation nuclei, so that the total number of potential nuclei is small relative to the amount of available  $\text{H}_2\text{O}$ .

The most speculative aspect of the present study is the extrapolation of the Gibbs free energy change to clusters with more than two  $\text{H}_2\text{O}$  molecules (Fig. 4). Unfortunately, laboratory studies of the neutral  $\text{H}_2\text{O}$  clusters of metallic compounds such as  $\text{NaHCO}_3$  will be extremely challenging because of the difficulty of detecting the clusters without working at such high concentrations that *in situ* polymerization starts to dominate. Conversely, *ab initio* calculations on closed-shell species such as  $\text{NaHCO}_3$  and  $\text{H}_2\text{O}$  appear to be a very promising approach for future studies.

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